

# CAN MEASUREMENT OF 2HDM PARAMETERS PROVIDE A HINT FOR HIGH SCALE SUSY?

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Sept. 6, 2019*



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# SUSY - HIGH AND LOW

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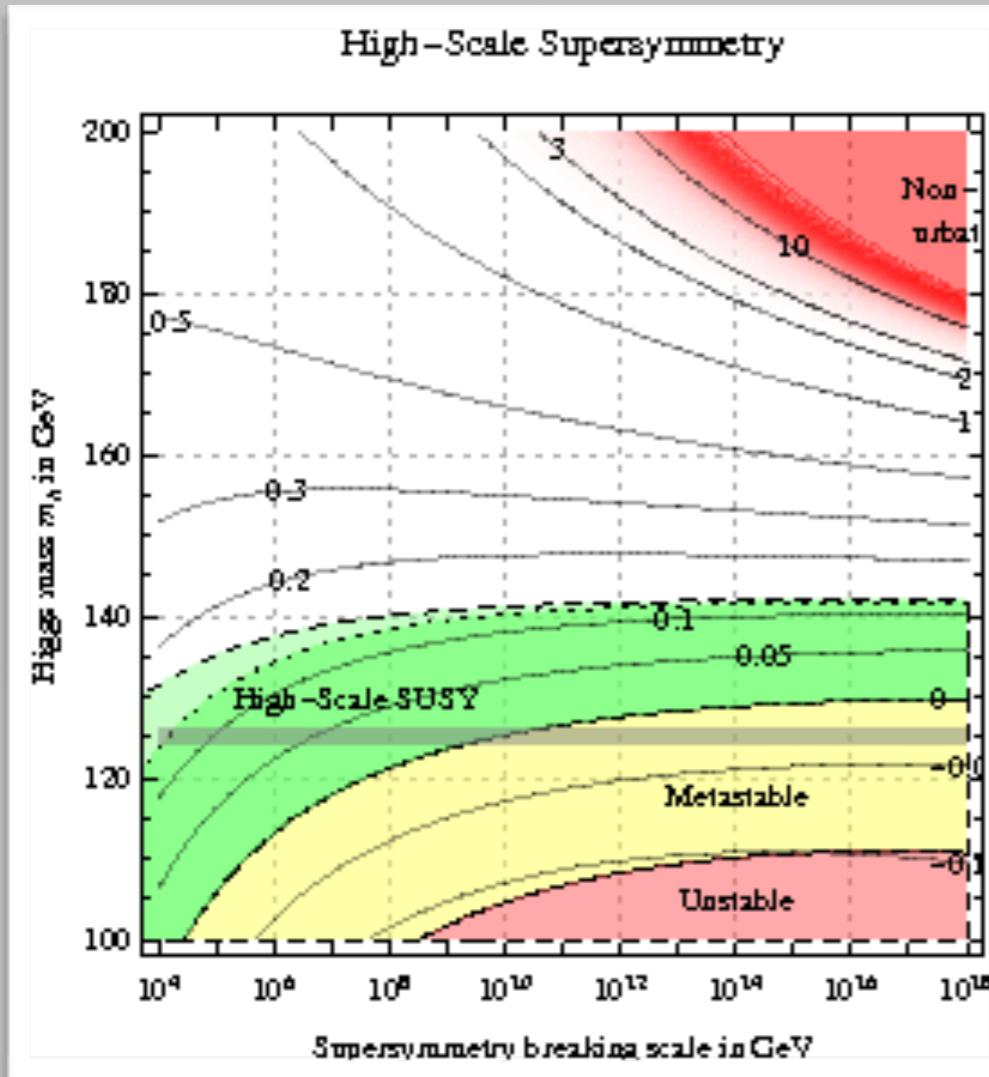
## High Scale SUSY

- Naturalness Solution
- Gauge Coupling Unification
- Viable Thermal Dark Matter candidate

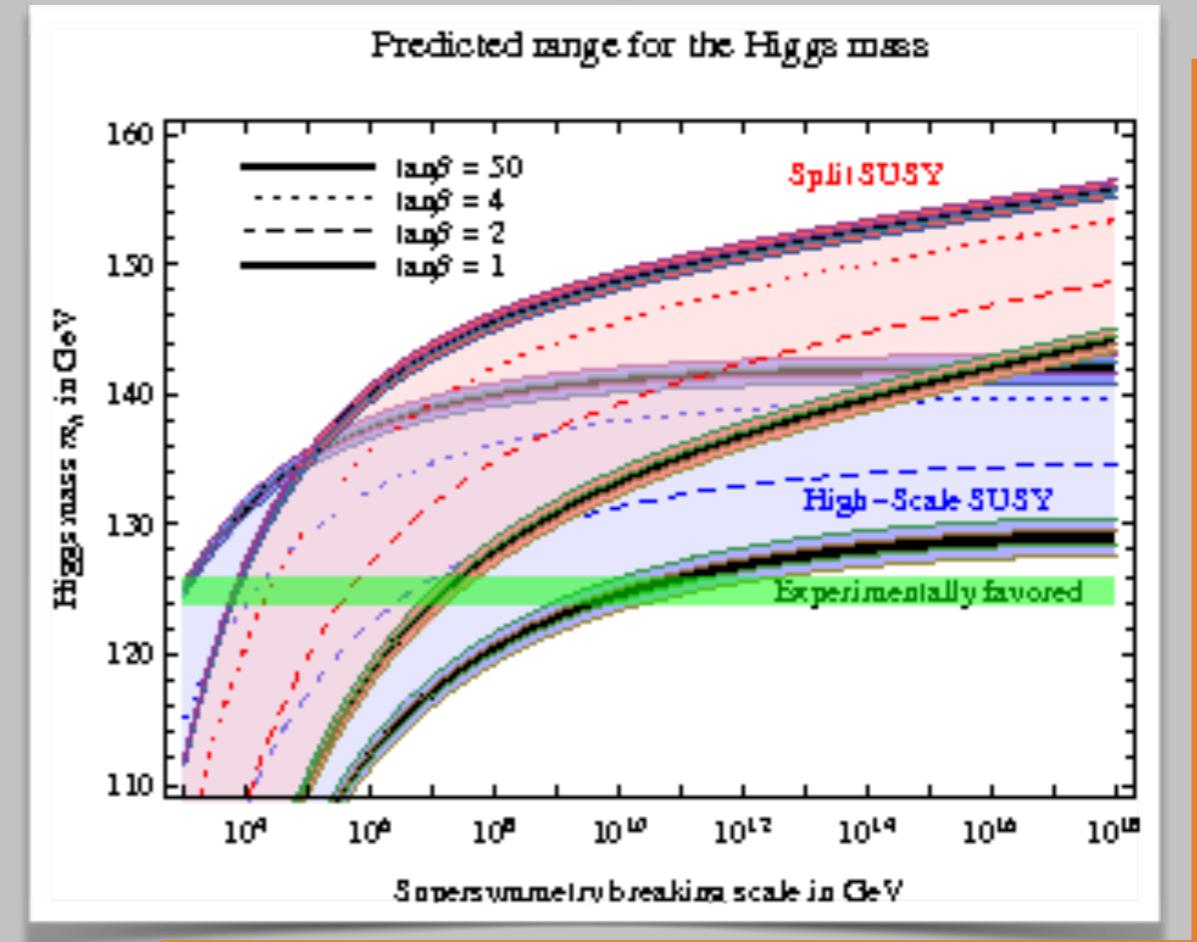


# HIGH-SCALE SUSY AS AN UV COMPLETE THEORY

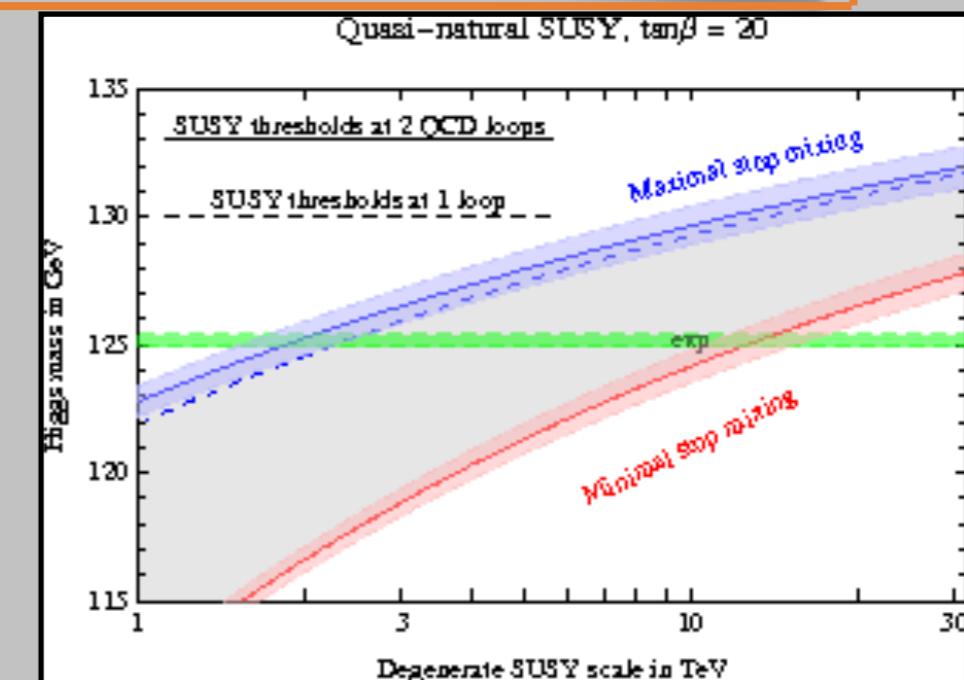
► *SM as the low energy effective theory* : Vega & Villadoro 1504.05200; Isidori & Paltieri 1710.11060;



Nucl.Phys. B858 (2012) 63-83  
Giudice, Strumia



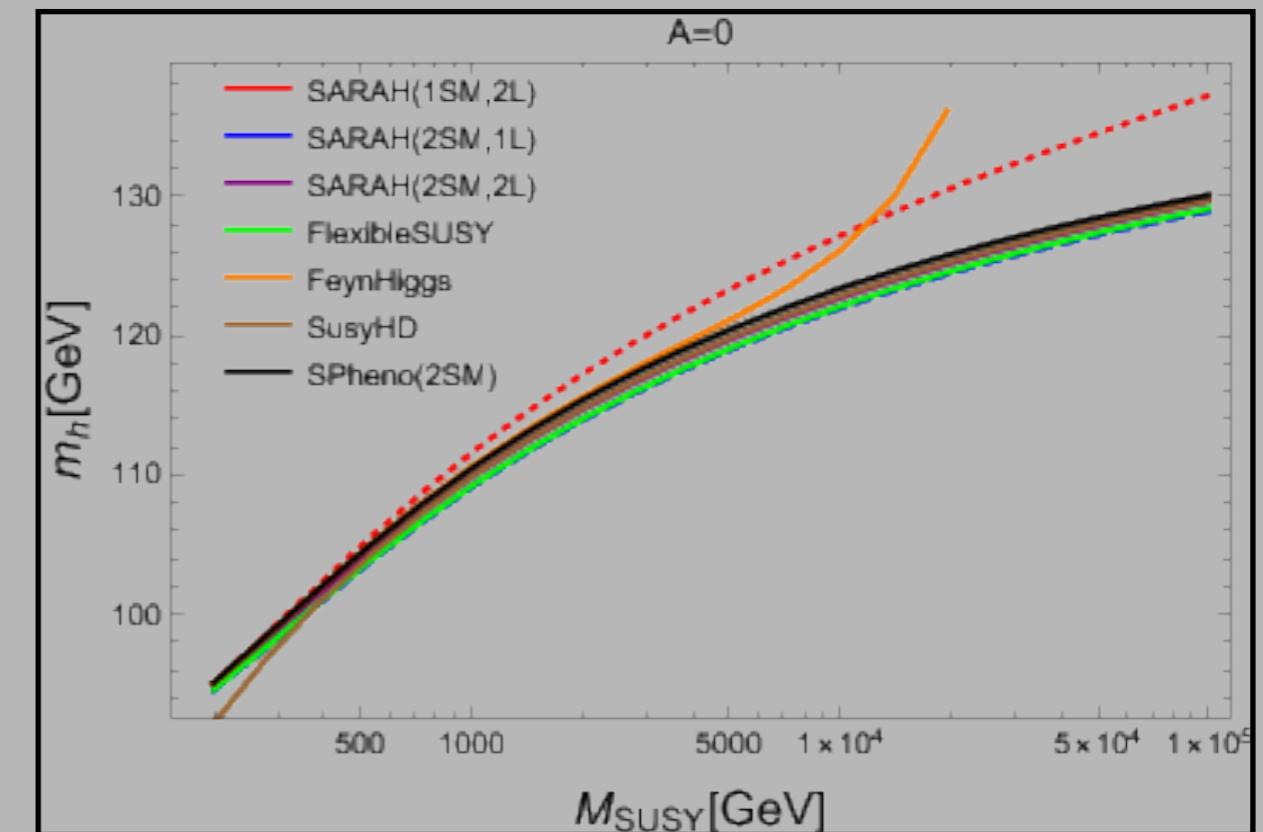
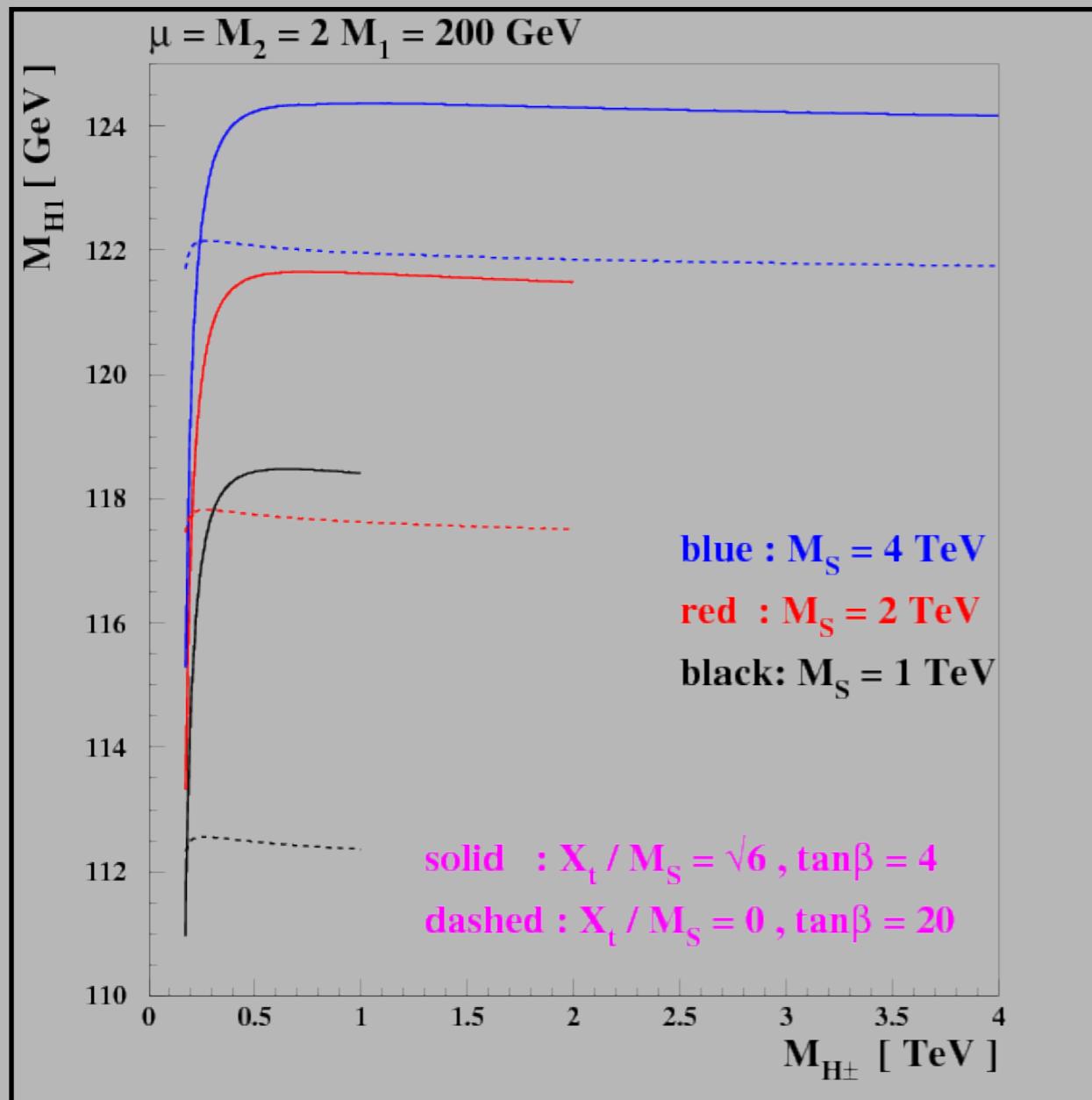
JHEP 1409 (2014) 092  
Bagnaschi, Giudice, Slavich, Strumia



# HIGH-SCALE SUSY AS AN UV COMPLETE THEORY

- 2HDM as an low energy effective theory : *Moderately high SUSY scale*

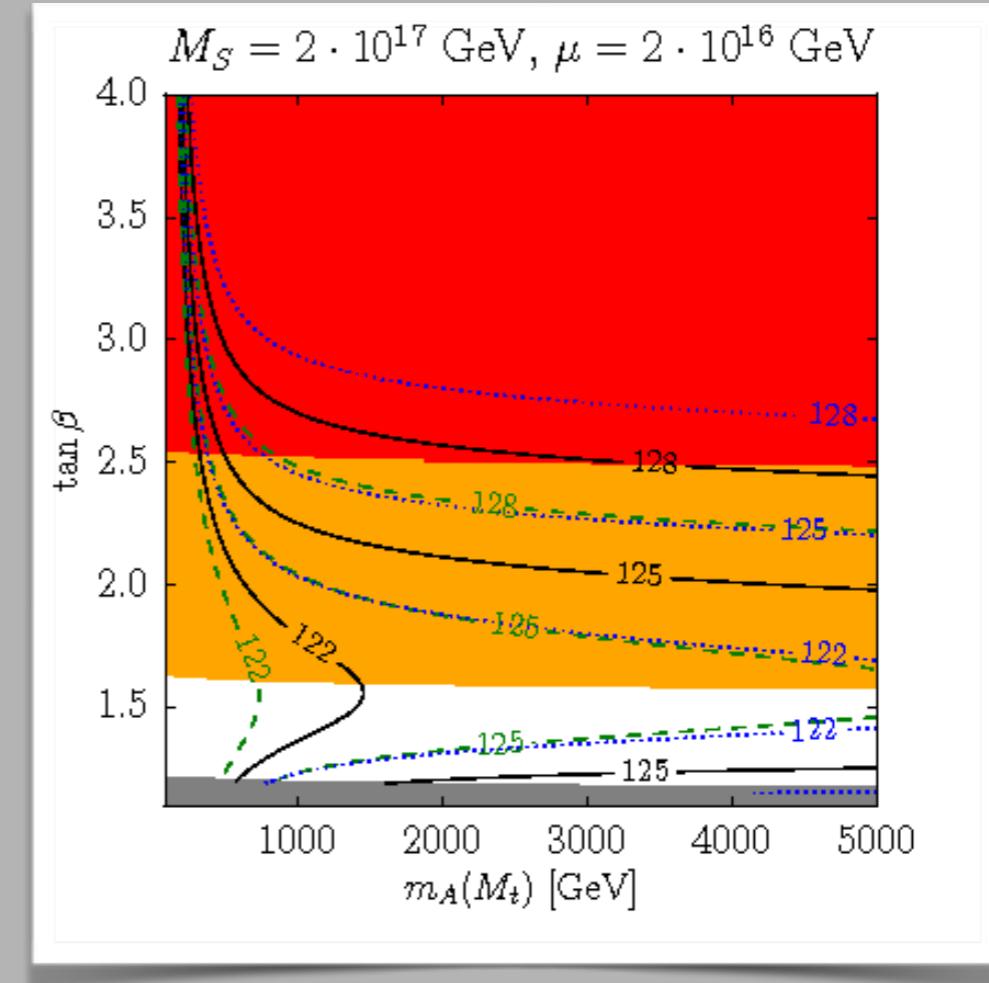
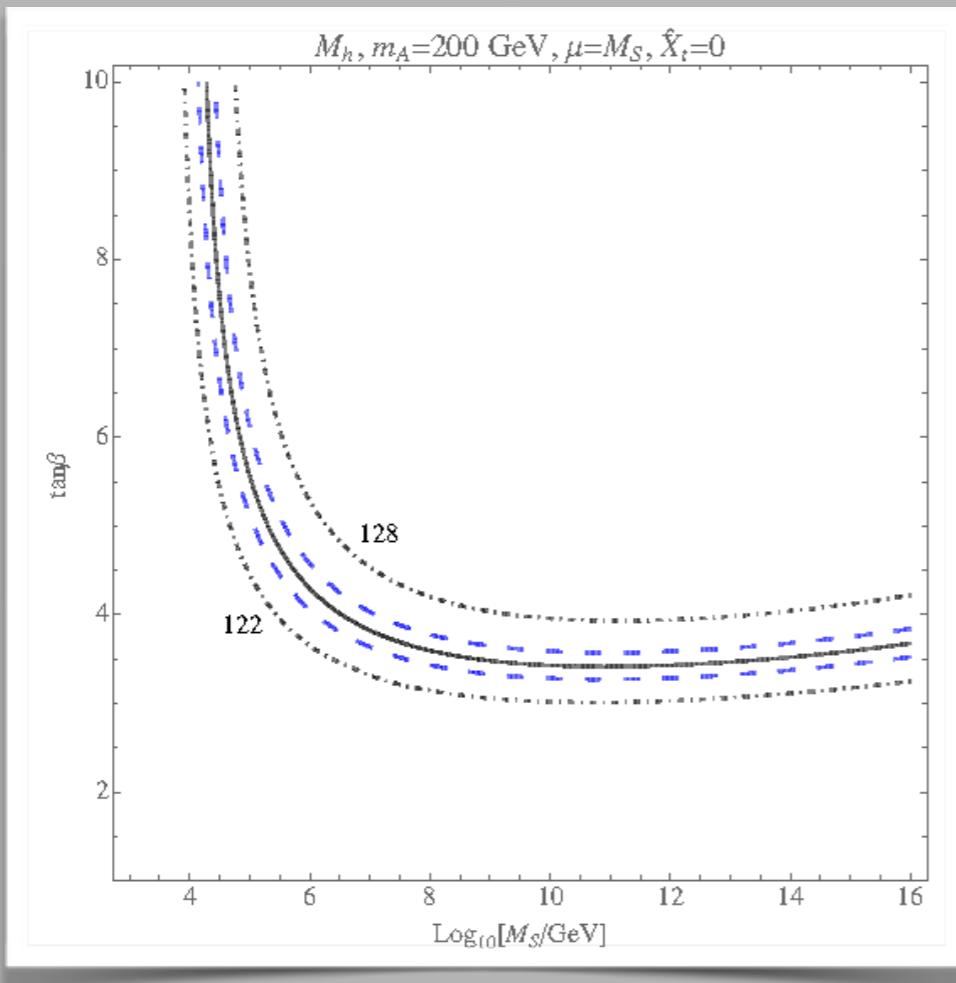
Similar references: Athron et. al (1609.00371); Haber et. al (1708.04461); Chalons et. Al (1709.02332)



Eur.Phys.J. C77 (2017) no.5, 338  
 Staub & Porede

# HIGH-SCALE SUSY AS AN UV COMPLETE THEORY

- 2HDM as an low energy effective theory : *High SUSY scale*



Phys.Rev. D92 (2015) no.7, 075032  
Li & Wagner

JHEP 1603 (2016) 158  
Bagnaschi, Brummer, Buchmuller, Voigt, Weiblein

- State of the art calculations. Matching at high scale.
- More information for low energy observables will be useful.

# BOTTOM-UP APPROACH

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- *Spectrum of scalar masses and mixing measured at the EW scale.*
- *Run from low to high scale using 2HDM RGE.*
- *Check the SUSY boundary conditions at the high scale.*
- *Independent of the detail of the underlying theory of the matching conditions.*

PHYSICAL REVIEW D 97, 095018 (2018)

G.Bhattacharyya, D. Das, M. Jay Pérez, IS, A. Santamaria, and O. Vives

# 2HDM PARAMETER COUNTING

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$$V_{II} = m_{11}^2 \phi_1^\dagger \phi_1 + m_{22}^2 \phi_2^\dagger \phi_2 - \left( m_{12}^2 \phi_1^\dagger \phi_2 + \text{h.c.} \right) + \frac{\lambda_1}{2} \left( \phi_1^\dagger \phi_1 \right)^2 + \frac{\lambda_2}{2} \left( \phi_2^\dagger \phi_2 \right)^2 + \lambda_3 \left( \phi_1^\dagger \phi_1 \right) \left( \phi_2^\dagger \phi_2 \right) \\ + \lambda_4 \left( \phi_1^\dagger \phi_2 \right) \left( \phi_2^\dagger \phi_1 \right) + \left[ \frac{\lambda_5}{2} \left( \phi_1^\dagger \phi_2 \right)^2 + \left( \lambda_6 \left( \phi_1^\dagger \phi_1 \right) + \lambda_7 \left( \phi_2^\dagger \phi_2 \right) \right) \left( \phi_1^\dagger \phi_2 \right) + \text{h.c.} \right]$$

- Softly broken  $Z_2$  symmetric potential   $\lambda_6 = \lambda_7 = 0$
- Type-II Structure :  $\phi_1$  couples only to down type fermions and  $\phi_2$  to up-type fermions
- Eight independent parameters  Five  $\lambda$ 's and three bilinear, or,

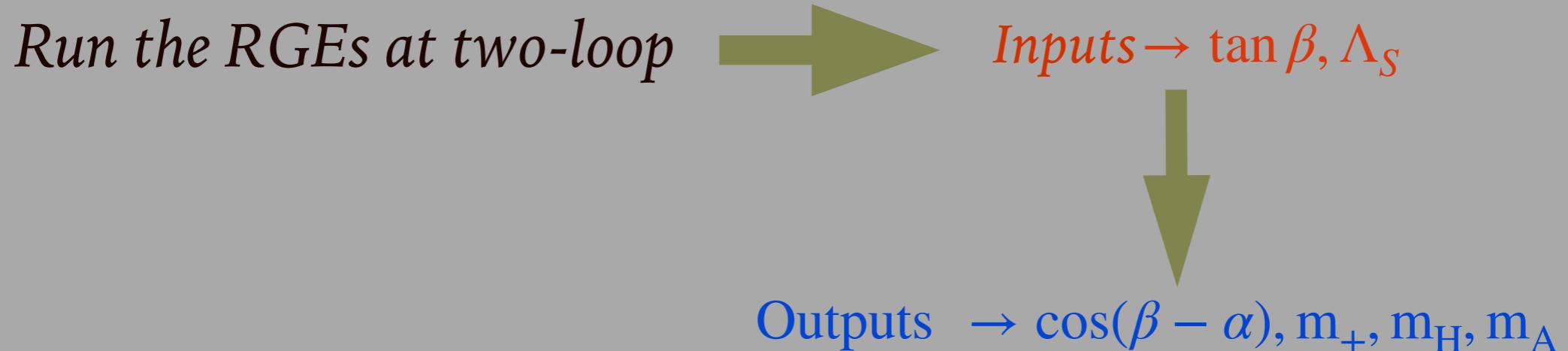
$$m_h, m_H, m_A, m_+, \tan \beta, v, \cos(\beta - \alpha), m_{12}^2$$

# ANALYSIS

- Higgs quartic couplings, at tree level, are simple functions of gauge couplings.
- Matching condition at High scale  $\Lambda_S$

$$\lambda_1 = \lambda_2 = \frac{1}{4} (g^2 + g_Y^2), \quad \lambda_3 = \frac{1}{4} (g^2 - g_Y^2), \quad \lambda_4 = -\frac{g^2}{2}, \quad \lambda_5 = \lambda_6 = \lambda_7 = 0$$

- Only four quartic couplings to be determined.
- RG running below follows 2HDM RGEs.



- Look for data driven region near  $\cos(\beta - \alpha) \simeq 0$

# RESULTS: QUALITATIVE UNDERSTANDING

- *Evolution of gauge coupling combination,*

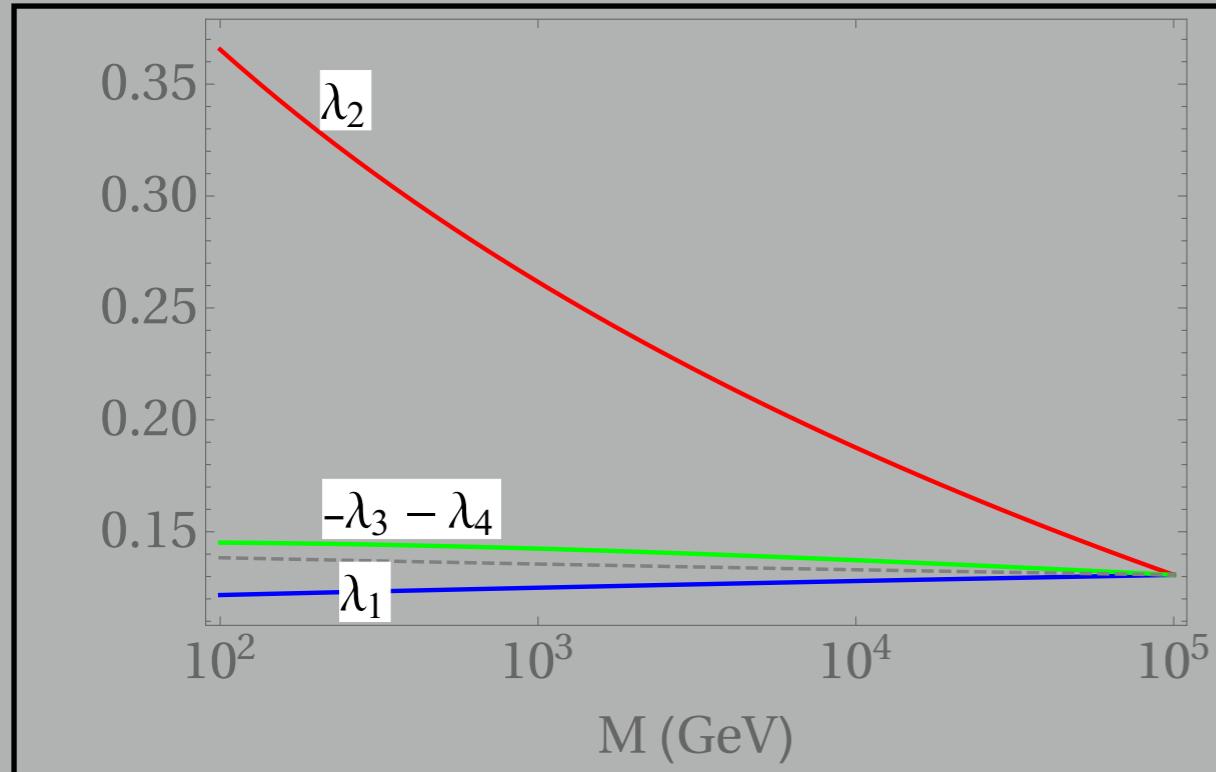
$$\mathcal{D}(g^2 + g_Y^2) = \frac{-3g^4 + 7g_Y^4}{8\pi^2}, \quad (-3g^4 + 7g_Y^4)/(8\pi^2) \Big|_{M_z} \simeq 0.003$$

- *One-loop RGE of scalar quartics,*

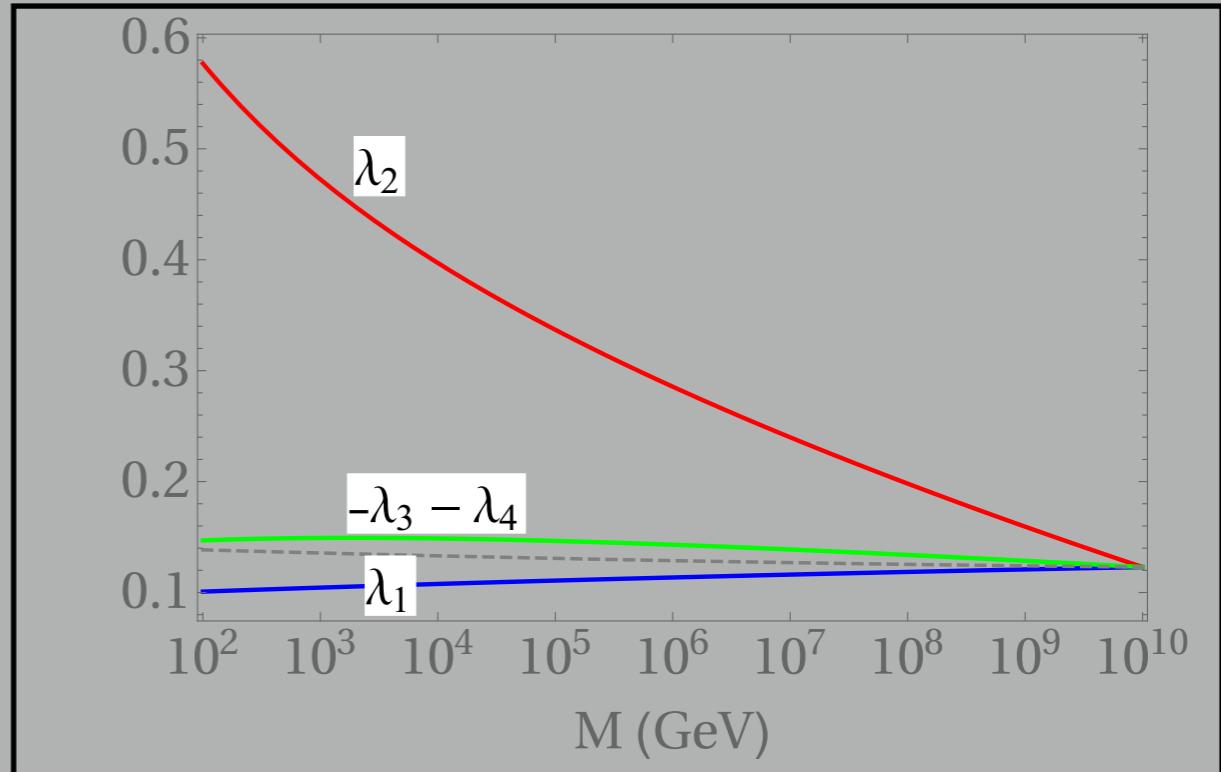
$$\begin{aligned} \mathcal{D}\lambda_1 &= \frac{1}{16\pi^2} \left[ \frac{3}{4} (3g^4 + g_Y^4 + 2g^2g_Y^2) - 3\lambda_1 (3g^2 + g_Y^2) \right. \\ &\quad \left. + 12\lambda_1^2 + 4\lambda_3^2 + 4\lambda_3\lambda_4 + 2\lambda_4^2 + 4\lambda_1 (3y_b^2 + y_\tau^2) - 12y_b^4 - 4y_\tau^4 \right] \\ \mathcal{D}\lambda_2 &= \frac{1}{16\pi^2} \left[ \frac{3}{4} (3g^4 + g_Y^4 + 2g^2g_Y^2) - 3\lambda_2 (3g^2 + g_Y^2) \right. \\ &\quad \left. + 12\lambda_2^2 + 4\lambda_3^2 + 4\lambda_3\lambda_4 + 2\lambda_4^2 + 12\lambda_2 y_t^2 - 12y_t^4 \right] \\ \mathcal{D}\lambda_3 &= \frac{1}{16\pi^2} \left[ \frac{3}{4} (3g^4 + g_Y^4 - 2g^2g_Y^2) - 3\lambda_3 (3g^2 + g_Y^2) \right. \\ &\quad \left. + 2(\lambda_1 + \lambda_2)(3\lambda_3 + \lambda_4) + 4\lambda_3^2 + 2\lambda_4^2 + 2\lambda_3 (3y_t^2 + 3y_b^2 + y_\tau^2) - 12y_t^2 y_b^2 \right] \\ \mathcal{D}\lambda_4 &= \frac{1}{16\pi^2} \left[ 3g^2g_Y^2 - 3\lambda_4 (3g^2 + g_Y^2) \right. \\ &\quad \left. + 2(\lambda_1 + \lambda_2 + 4\lambda_3)\lambda_4 + 4\lambda_4^2 + 2\lambda_4 (3y_t^2 + 3y_b^2 + y_\tau^2) + 12y_t^2 y_b^2 \right] \end{aligned}$$

- Only  $\lambda_2$  should have significant evolution due to the large top Yukawa coupling  $y_t \sim \mathcal{O}(m_t/(v \sin \beta))$
- 2-loop running is essential in the close proximity of unit  $\tan \beta$

# RESULTS: RUNNING QUARTICS



$\tan \beta \sim 3, \Lambda_S = 10^5 \text{ GeV}$

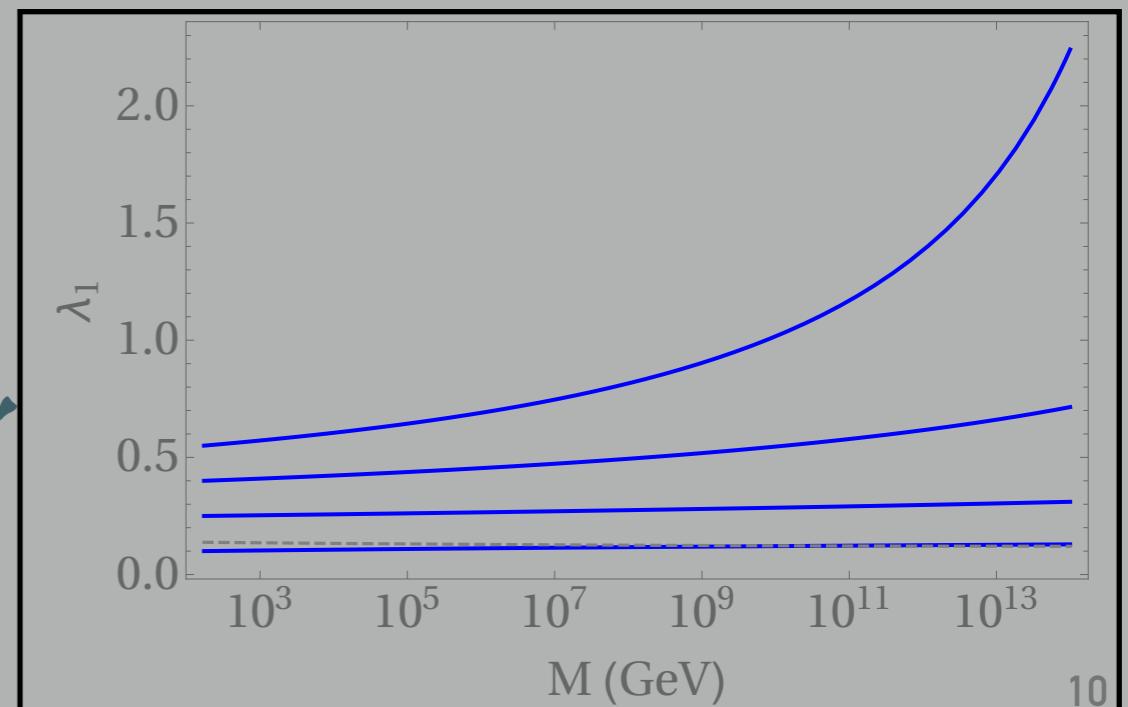


$\tan \beta \sim 2, \Lambda_S = 10^{10} \text{ GeV}$

- Comparison with  $\frac{(g^2 + g_Y^2)}{4}$  2-loop matching.
- At the SUSY scale,  

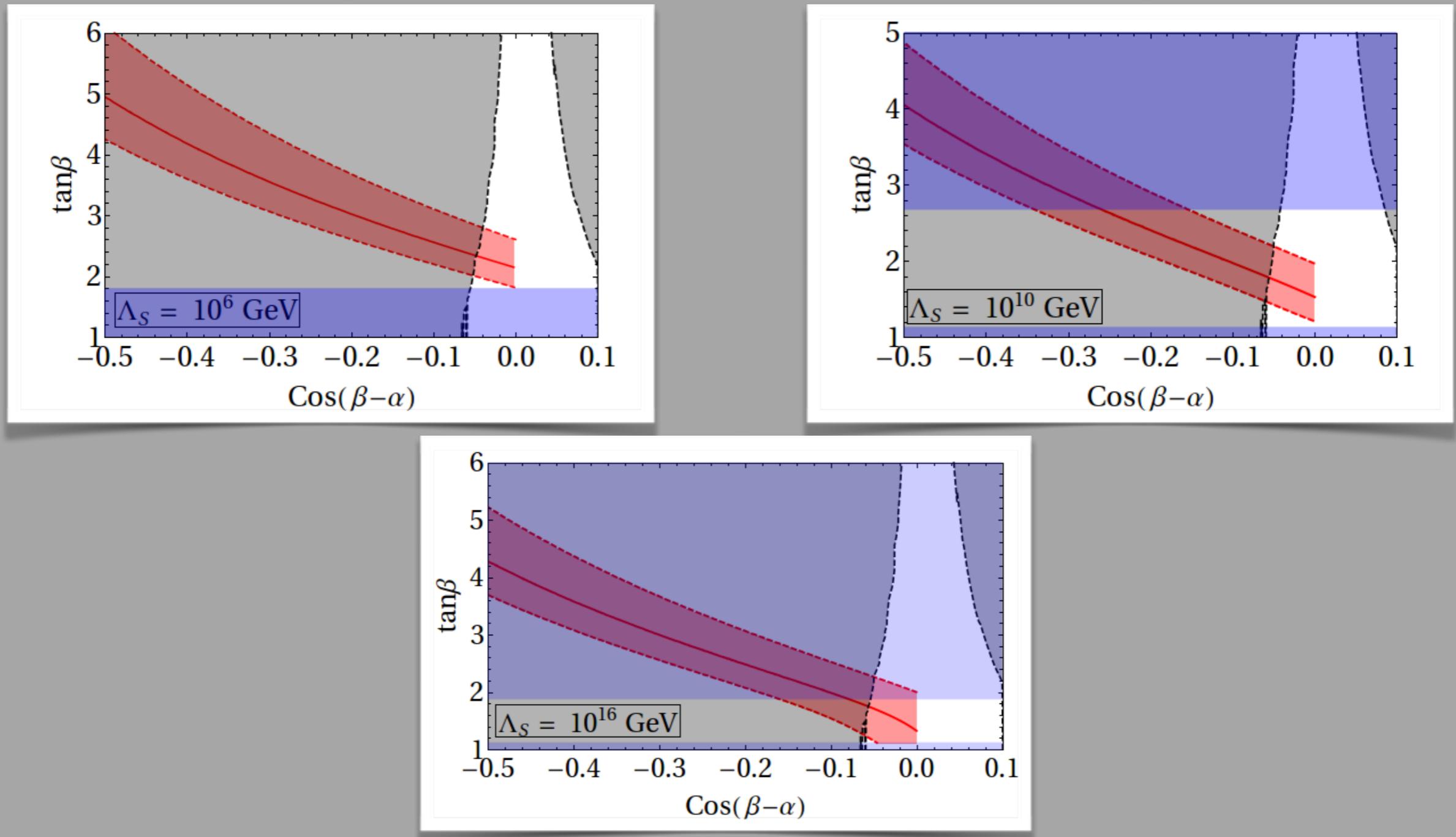
$$\lambda_1 = \lambda_2 = -(\lambda_3 + \lambda_4) = (g^2 + g_Y^2)/4$$
- Result is independent of  $\tan \beta$

$\lambda_1$  running for  $\lambda_1|_{(EW)} = 0.1, 0.25, 0.4, 0.55$  with  
 $\lambda_2 = 0.56, \lambda_3 = 0.015$  and  $\lambda_4 = -0.16$  for  $\tan \beta = 2$ .

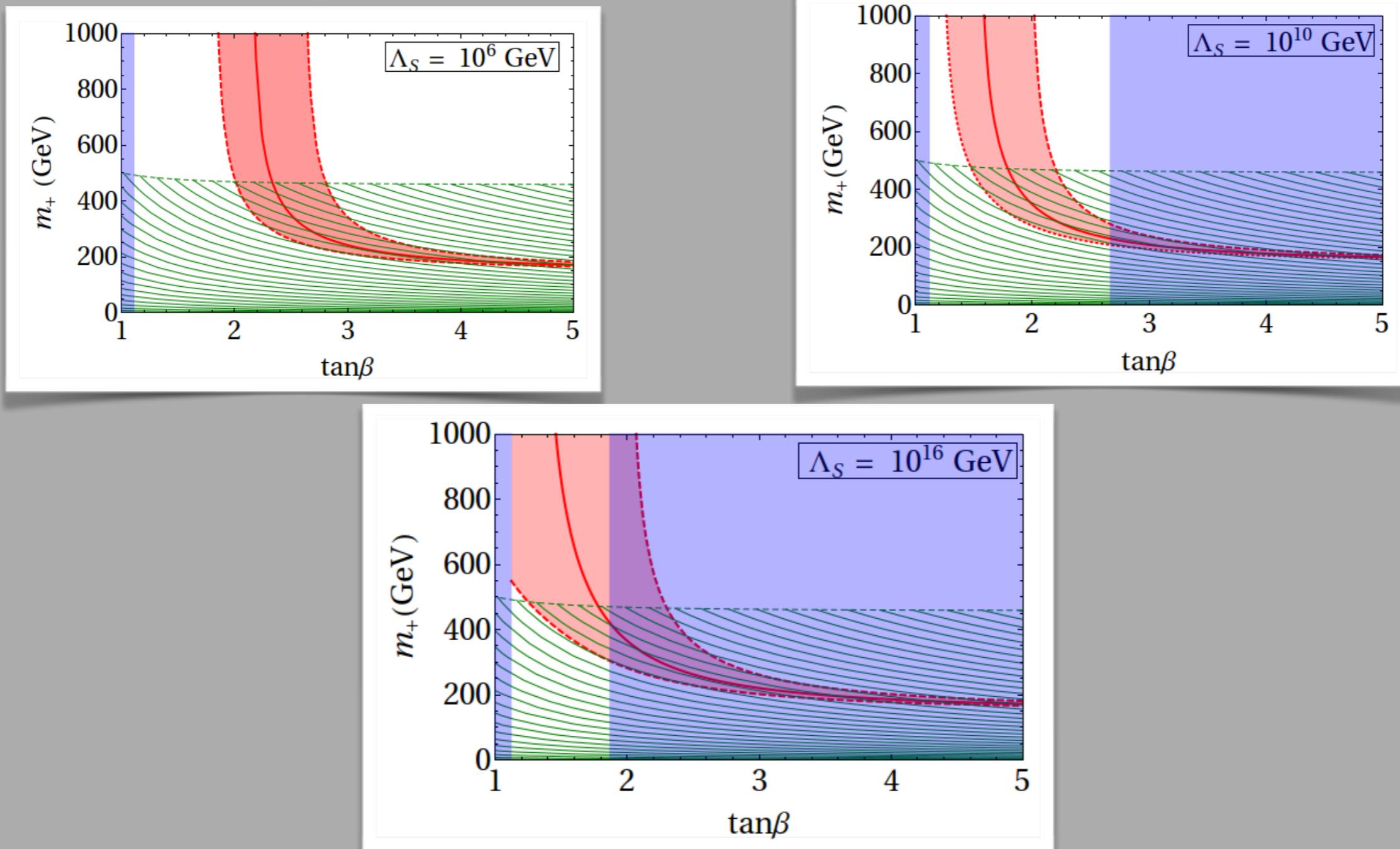


# SUSY SCALE DETERMINATION

- The shaded blue region corresponds to absolute vacuum of the potential.
- The current or projected value of  $\cos(\beta - \alpha)$  will narrow down the region of all the scalar masses and  $\tan \beta$

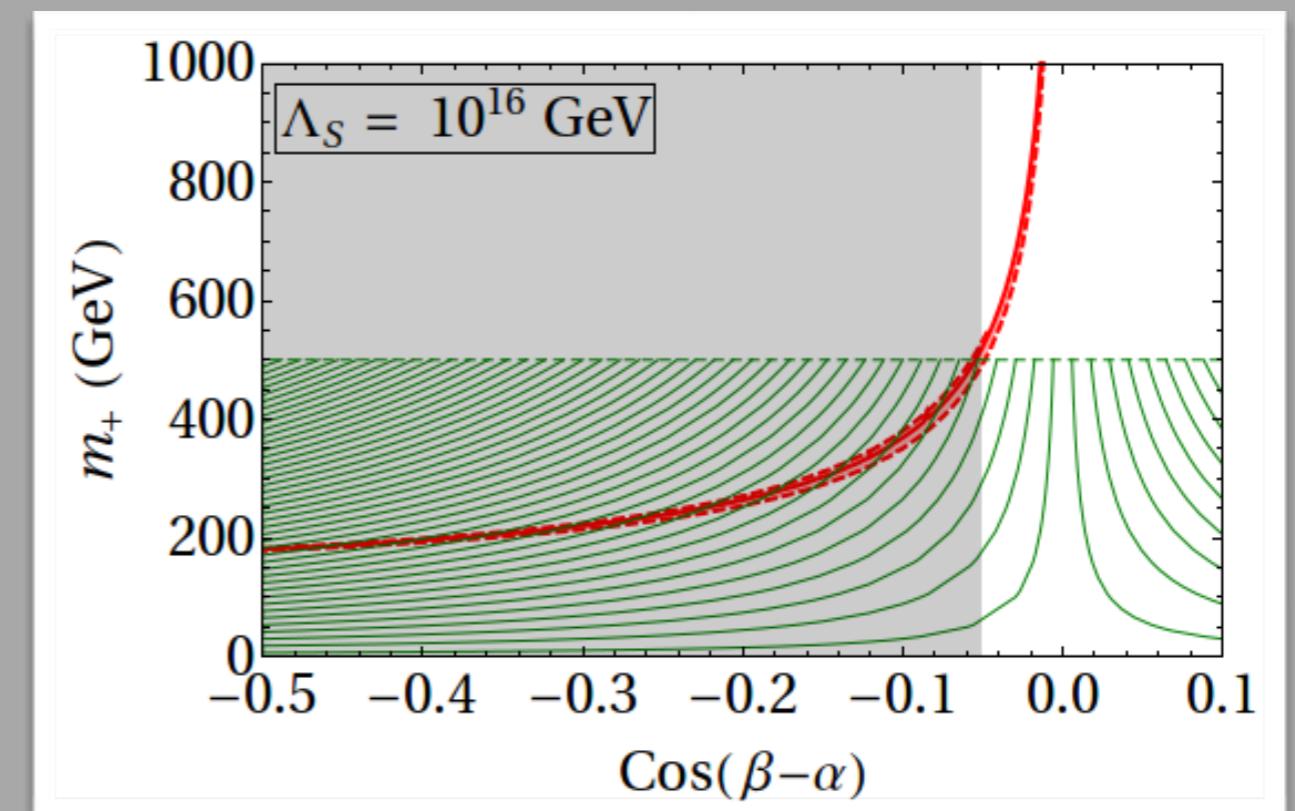
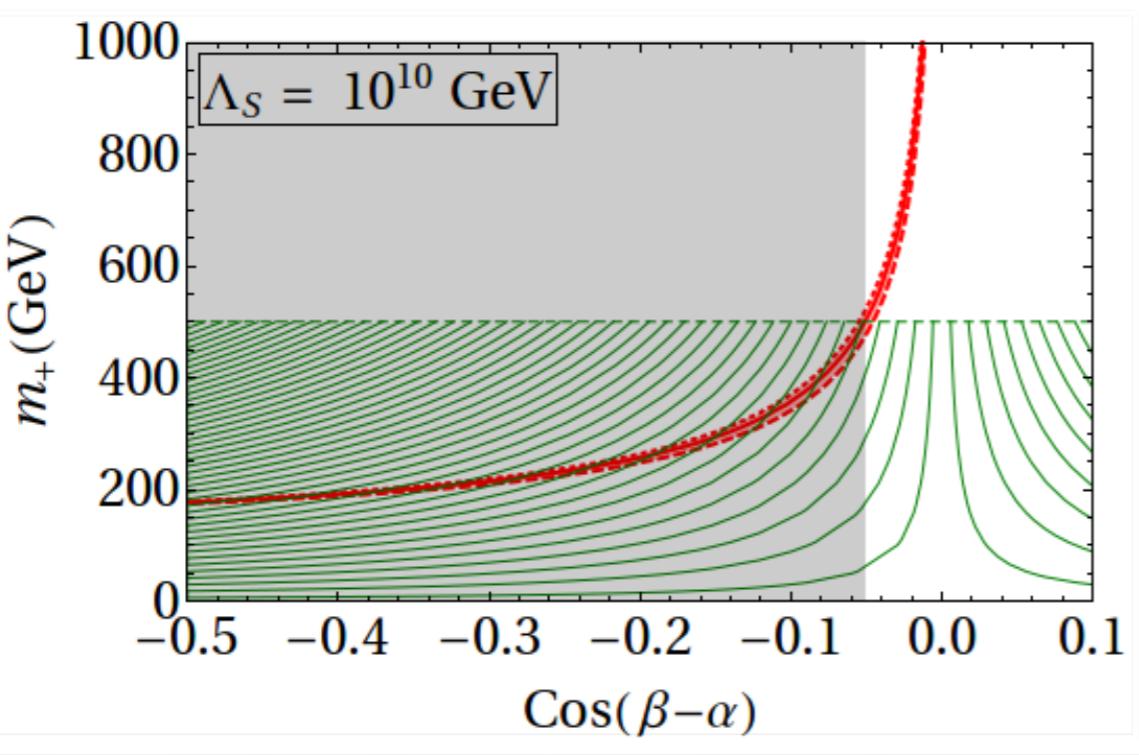


# SUSY SCALE DETERMINATION



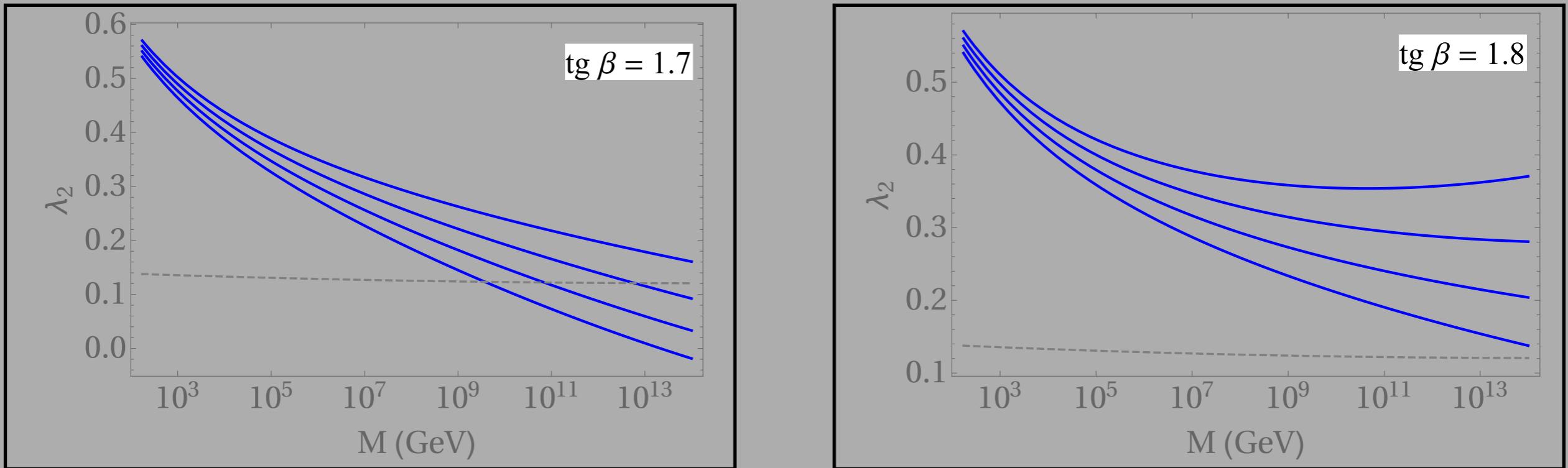
- Dashed region denotes the constraints on charged Higgs mass from flavor observable  $b \rightarrow s\gamma$

# SUSY SCALE DETERMINATION



- The  $m_+$  and  $\cos(\beta - \alpha)$  is strongly correlated despite input uncertainties.
- The bounds on one can be translated to the other.

# AN A POSTERIORI EXPLANATION



- The Solution is sensitive to  $m_t$  and  $\tan \beta$ . Uncertainties can be translated as

$$\Delta \tan \beta = \tan \beta (1 + \tan^2 \beta) (\Delta m_t / m_t)$$

- To a good approximation,

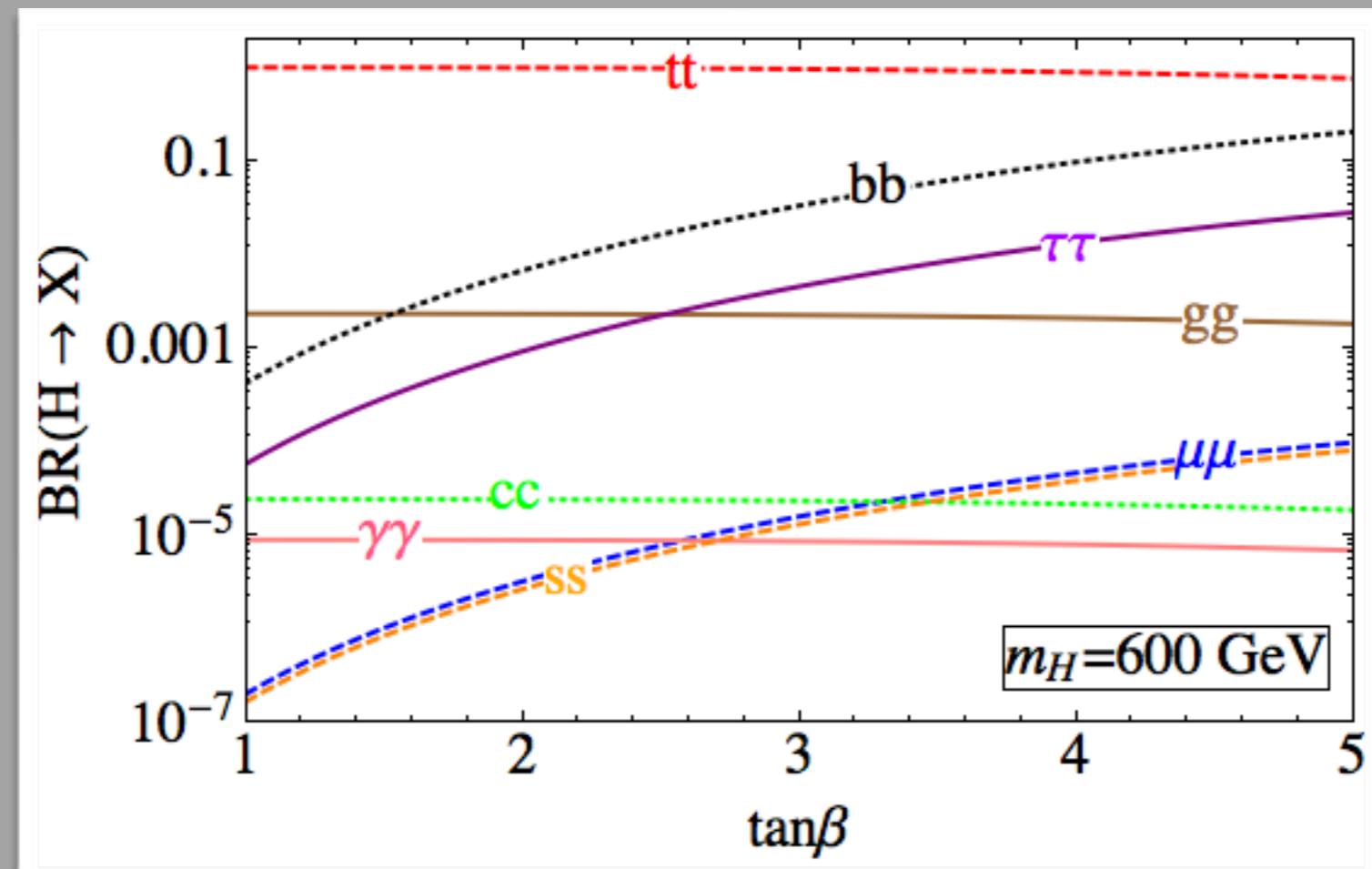
$$\lambda_1(M_Z) \simeq \lambda_1(\Lambda_S) = \lambda_2(\Lambda_S) = \frac{(g^2 + g_Y^2)}{4} = -\{\lambda_3(\Lambda_S) + \lambda_4(\Lambda_S)\} \simeq -\{\lambda_3(M_Z) + \lambda_4(M_Z)\}$$

- The Higgs mass,

$$m_h^2 = M_Z^2 \cos^2(2\beta) + \Delta \lambda_2 v^2 \frac{\tan^4 \beta}{(1 + \tan^2 \beta)^2}, \quad \Delta \lambda_2 = \lambda_2(M_Z) - \lambda_2(\Lambda_S)$$

# PHENOMENOLOGICAL IMPLICATIONS

- Branching ratios of different decay channels mainly depend on  $\tan \beta$
- Observation of extra scalars can be tested.
- An example plot for  $m_H = 600$  GeV



# CONCLUSIONS

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- We have considered a general framework for fixing the 2HDM parameter space.
- We assume that the low energy effective 2HDM is embedded in a large theoretical framework at UV.
- The quartic couplings are unambiguously determined at High scale.
- MSSM is a well motivated scenario. Even if super-partners are super-heavy, the ancestral symmetry leaves its imprints on low scale observables and observation of nonstandard scalar provide a hint towards the high SUSY scale.
- This strategy, however, crucially depends on whether  $\tan \beta$  can be determined with a percent level precision in order to make a reasonable prediction for the MSSM scale.
- Our methodology is quite general, can be applied to a wide category of UV scenarios.

THANK YOU

# BACK UPS

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# A RECENT STUDY

*Heavy Higgs bosons at low  $\tan \beta$  : from the LHC to 100 TeV*

*Craig, Hajer, Li, Liu and Zhang : JHEP 01(2017) 018*

