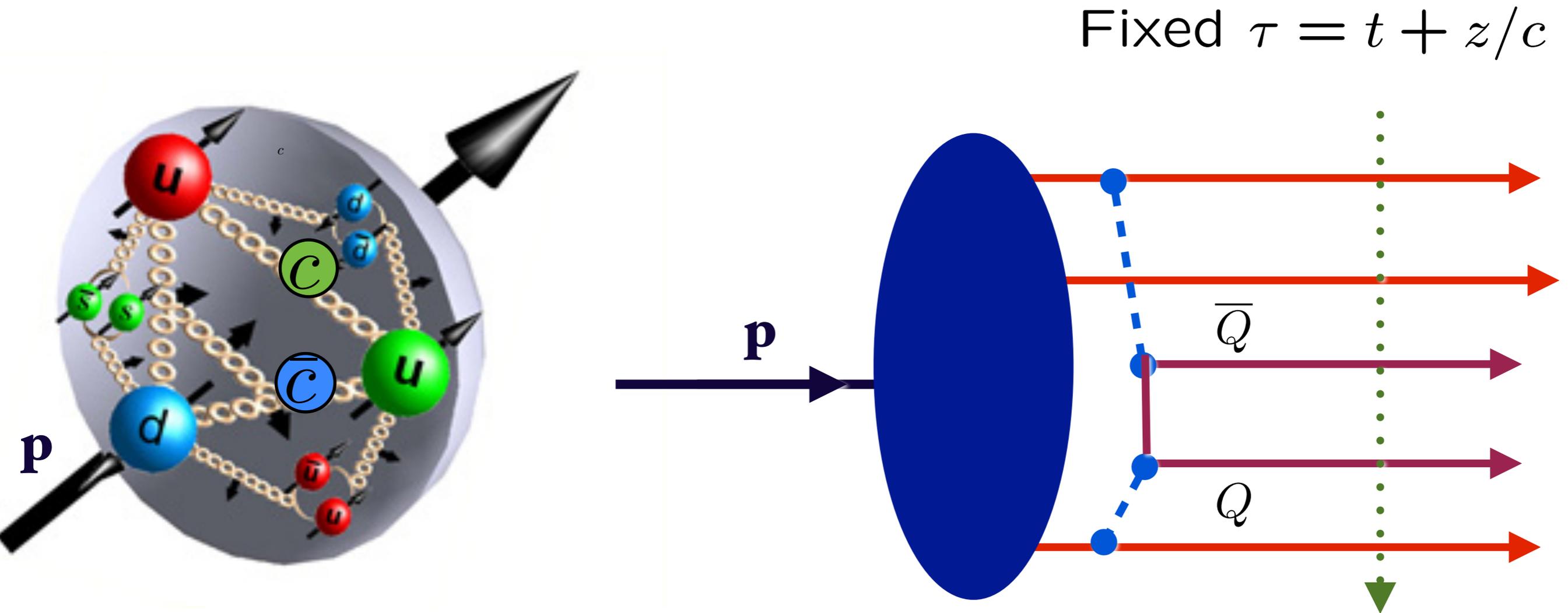


QCD, Heavy Flavors, and Higgs Production in the Very Forward Region



*Workshop on Forward Physics and QCD at the LHC,
the Future Electron Collider, and Cosmic Ray Physics*

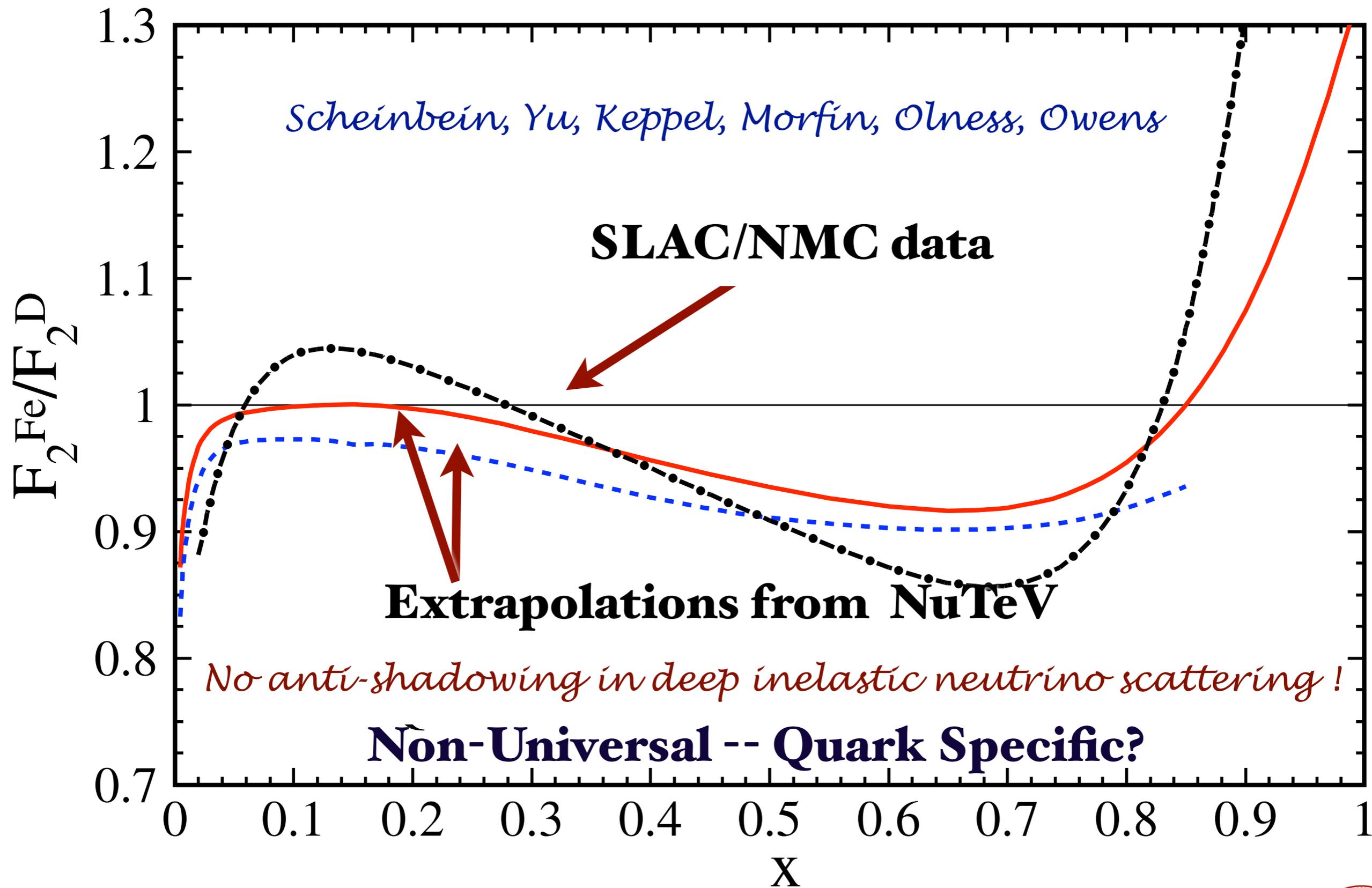
*Hotel Guanajuato,
Ciudad de Guanajuato,
Mexico*

November 18, 2019

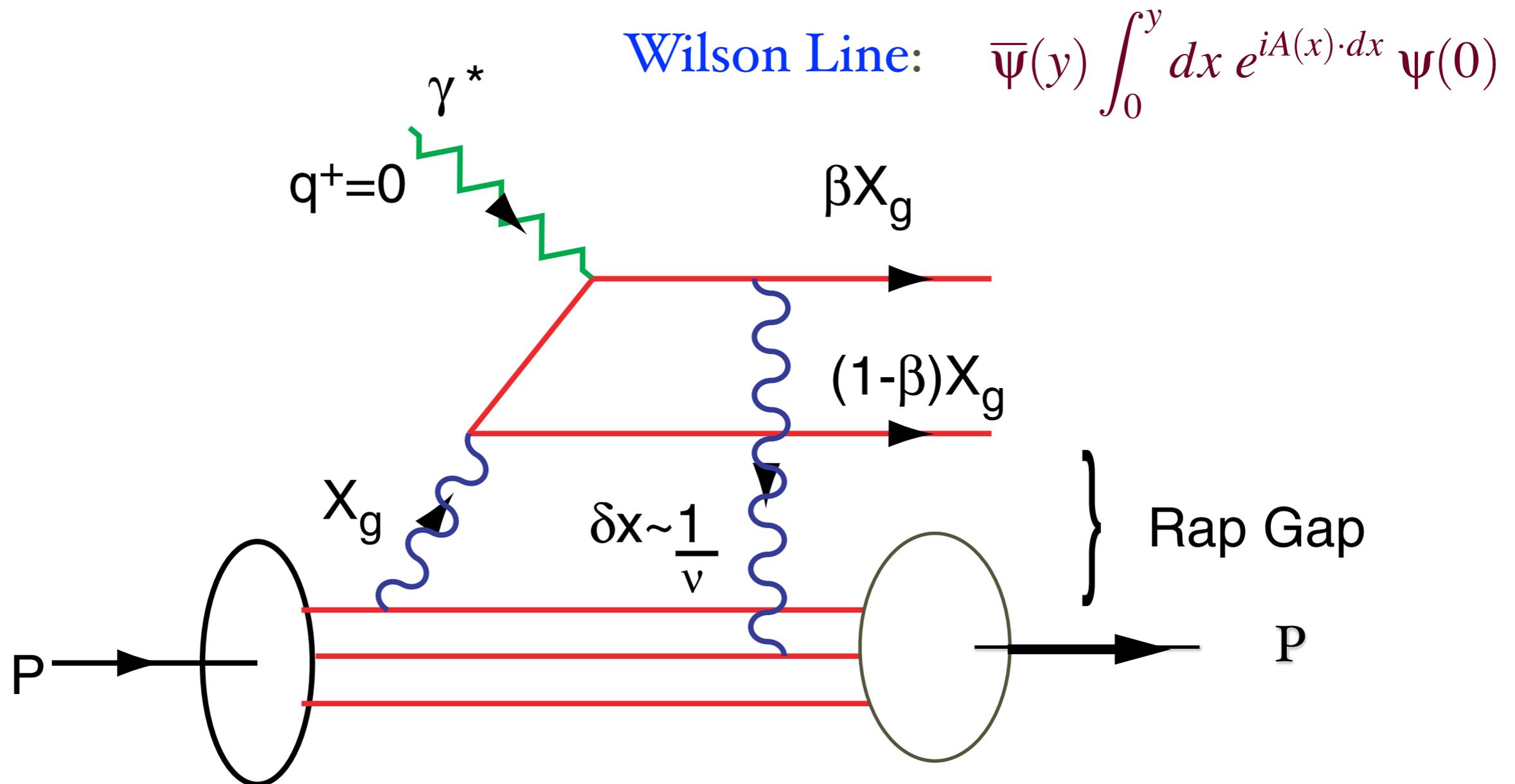
Stan Brodsky



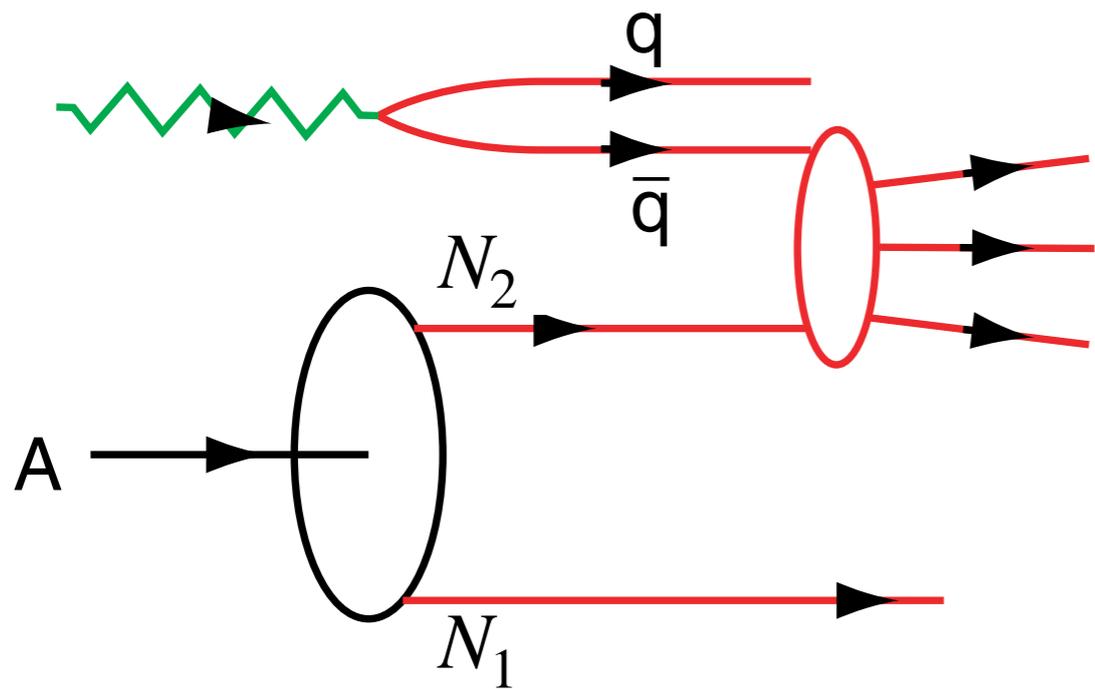
$$Q^2 = 5 \text{ GeV}^2$$



QCD Mechanism for Rapidity Gaps

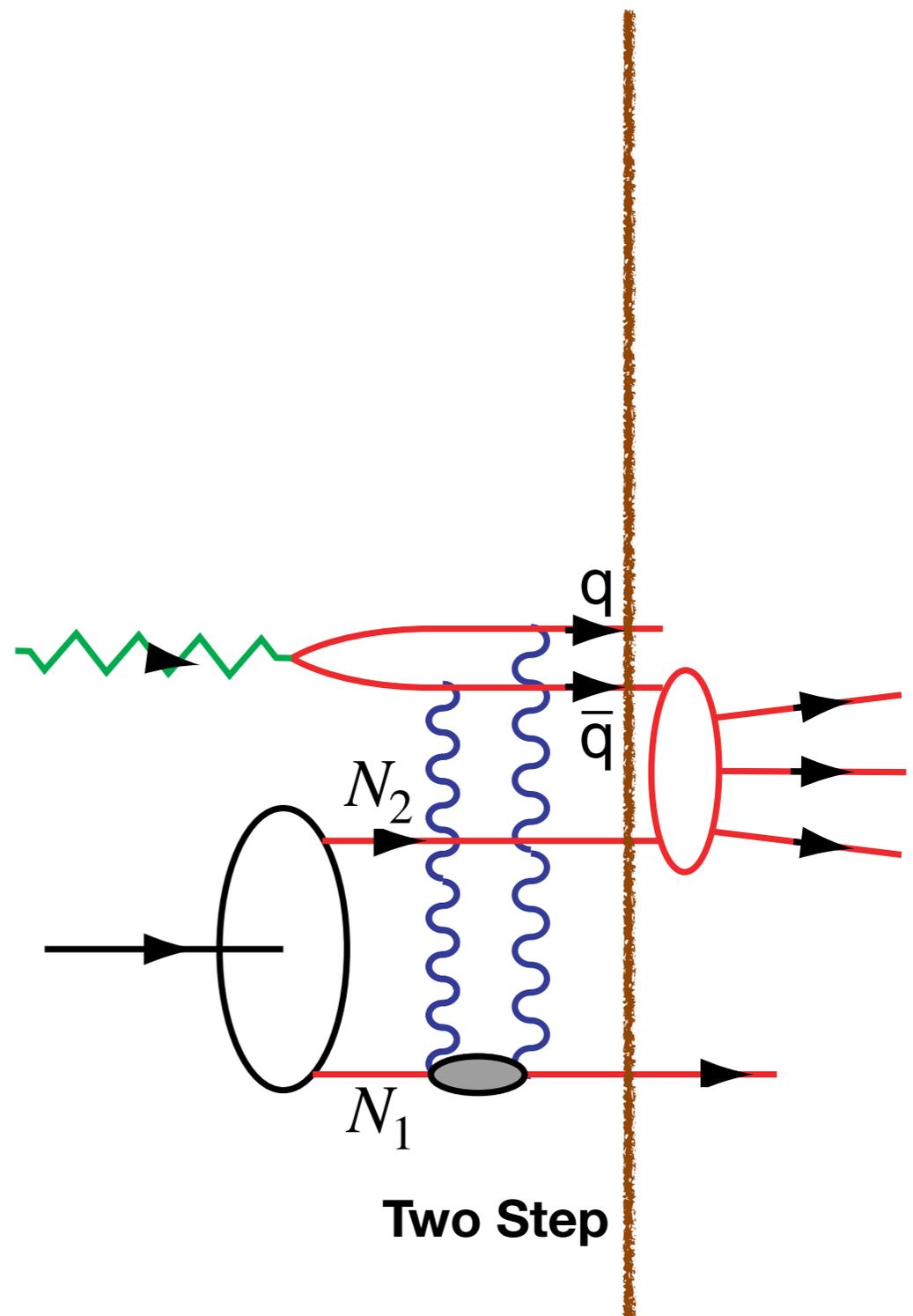


Reproduces lab-frame color dipole approach
DDIS: Input for leading twist nuclear shadowing



One Step

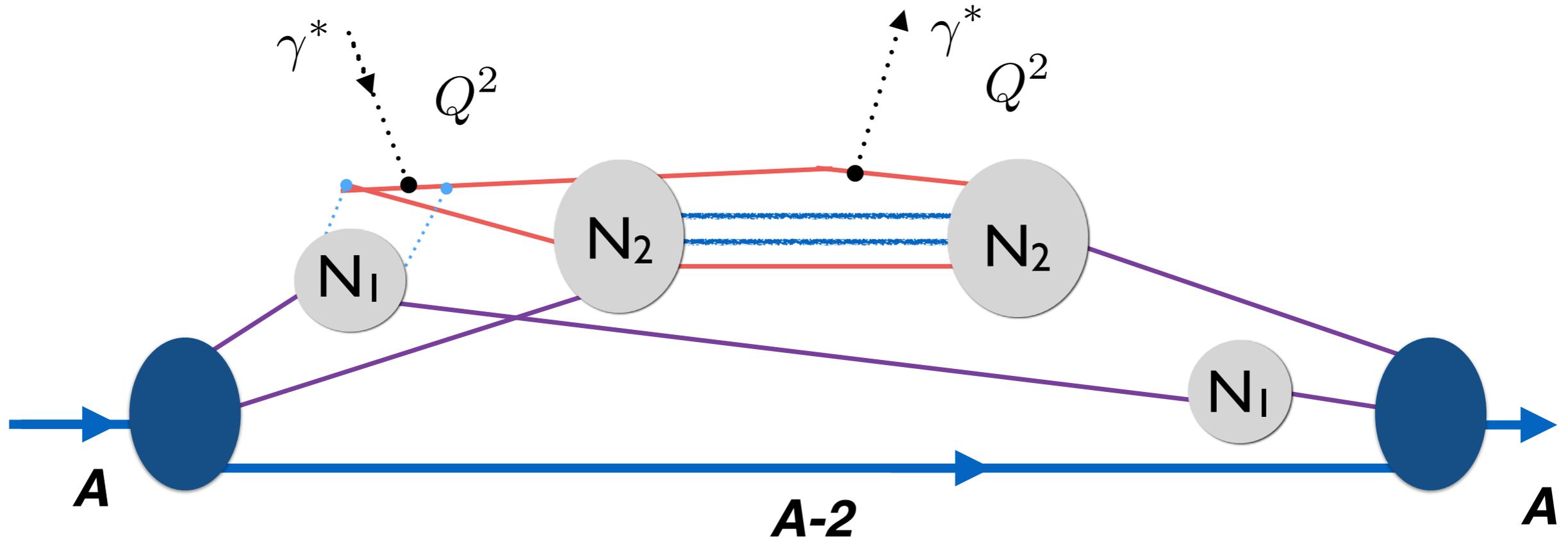
+



Two Step

*Glauber Cut:
On-Shell Propagation*

Doubly Virtual Nuclear Compton Scattering $\gamma^*(q)A \rightarrow \gamma^*(q)A$



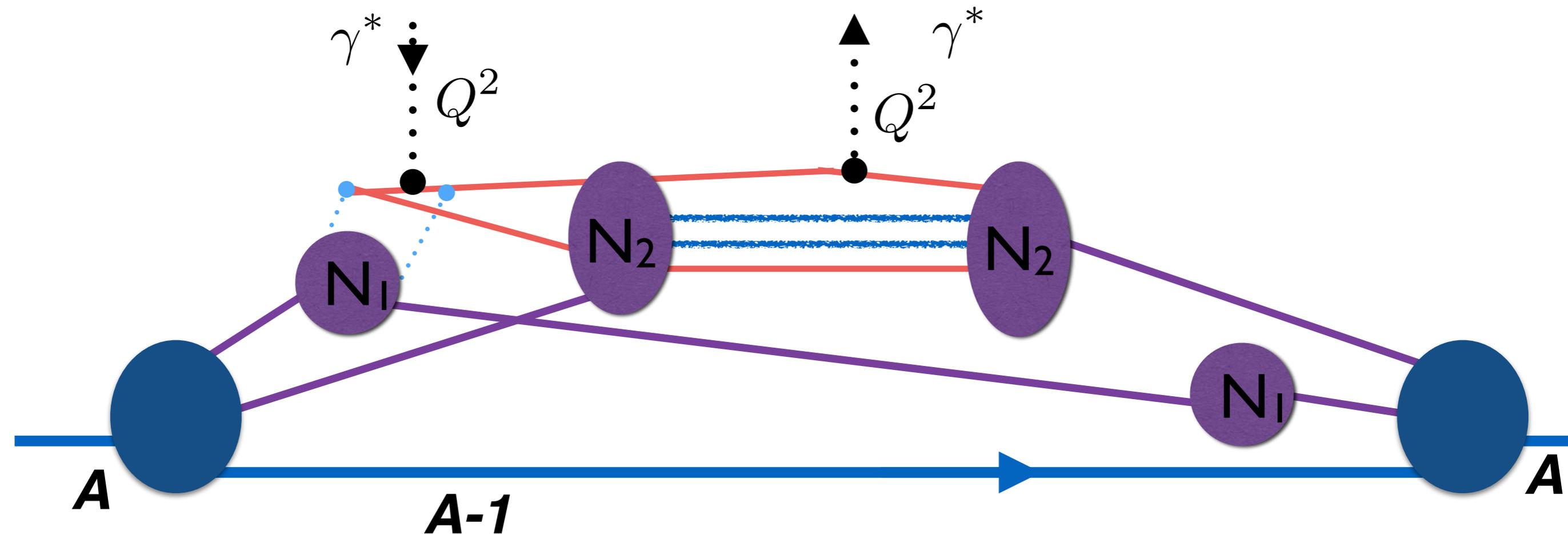
Front-Face Nucleon N_1 struck

Front-Face Nucleon N_1 not struck

Contribution from One-Step / Two-Step Interference

**Illustrates the
LF time sequence**

$$q^+ = 0 \quad q_{\perp}^2 = Q^2 = -q^2$$



Front-Face Nucleon N_1 struck

Front-Face Nucleon N_1 not struck

One-Step / Two-Step Interference

Study Double Virtual Compton Scattering $\gamma^* A \rightarrow \gamma^* A$

**Cannot reduce to matrix element
of local operator! No Sum Rules!** Liuti, Schmidt sjb

- Unlike shadowing, anti-shadowing from Reggeon exchange is flavor specific;
- Each quark and anti-quark will have distinctly different constructive interference patterns
- The flavor dependence of antishadowing explains why anti-shadowing is different for electron (neutral electro-magnetic current) vs. neutrino (charged weak current) DIS reactions.
- Test of the explanation of antishadowing: Bjorken-scaling leading-twist charge exchange DDIS reaction $\gamma^*p \rightarrow nX^+$ with a rapidity gap due to $I=1$ Reggeon exchange
- The finite path length due to the on-shell propagation of V^0 between N_1 and N_2 contributes a finite distance $(\Delta z)^2$ between the two virtual photons in the DVCS amplitude.

The usual “handbag” diagram where the two $J^\mu(x)$ and $J^\nu(0)$ currents acting on an uninterrupted quark propagator are replaced by a local operator $T^{\mu\nu}(0)$ as $Q^2 \rightarrow \infty$, is inapplicable in deeply virtual Compton scattering from a nucleus since the currents act on different nucleons.

Δz^2 does not vanish as $\frac{1}{Q^2}$.

OPE and Sum Rules invalid for nuclear pdfs

Origin of Regge Behavior of Deep Inelastic Structure Functions

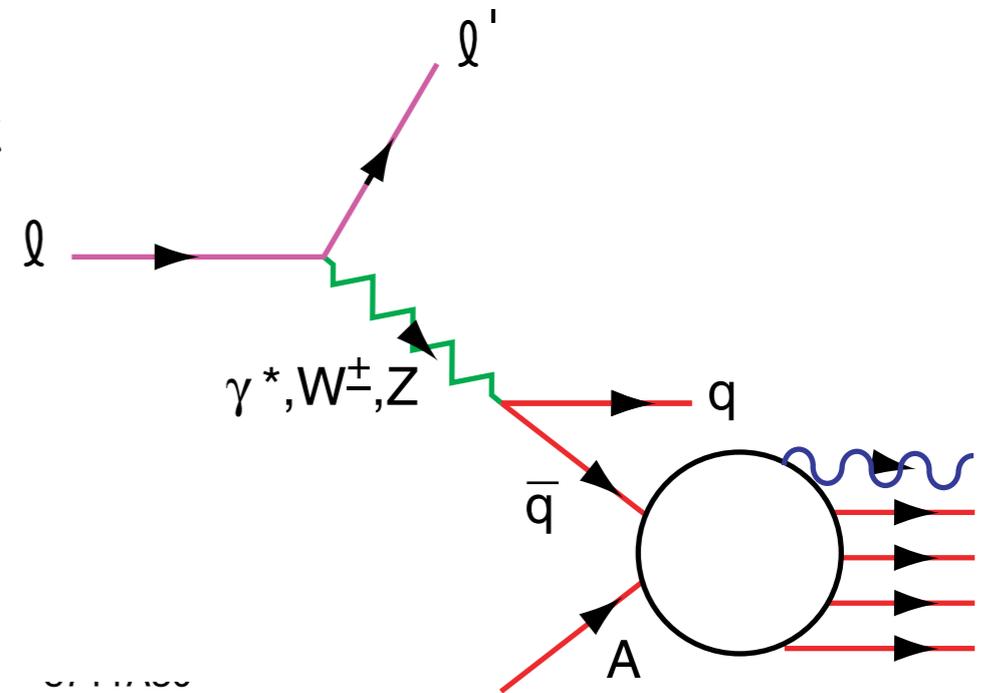
$$F_{2p}(x) - F_{2n}(x) \propto x^{1/2}$$

Antiquark interacts with target nucleus at energy $\hat{s} \propto \frac{1}{x_{bj}}$

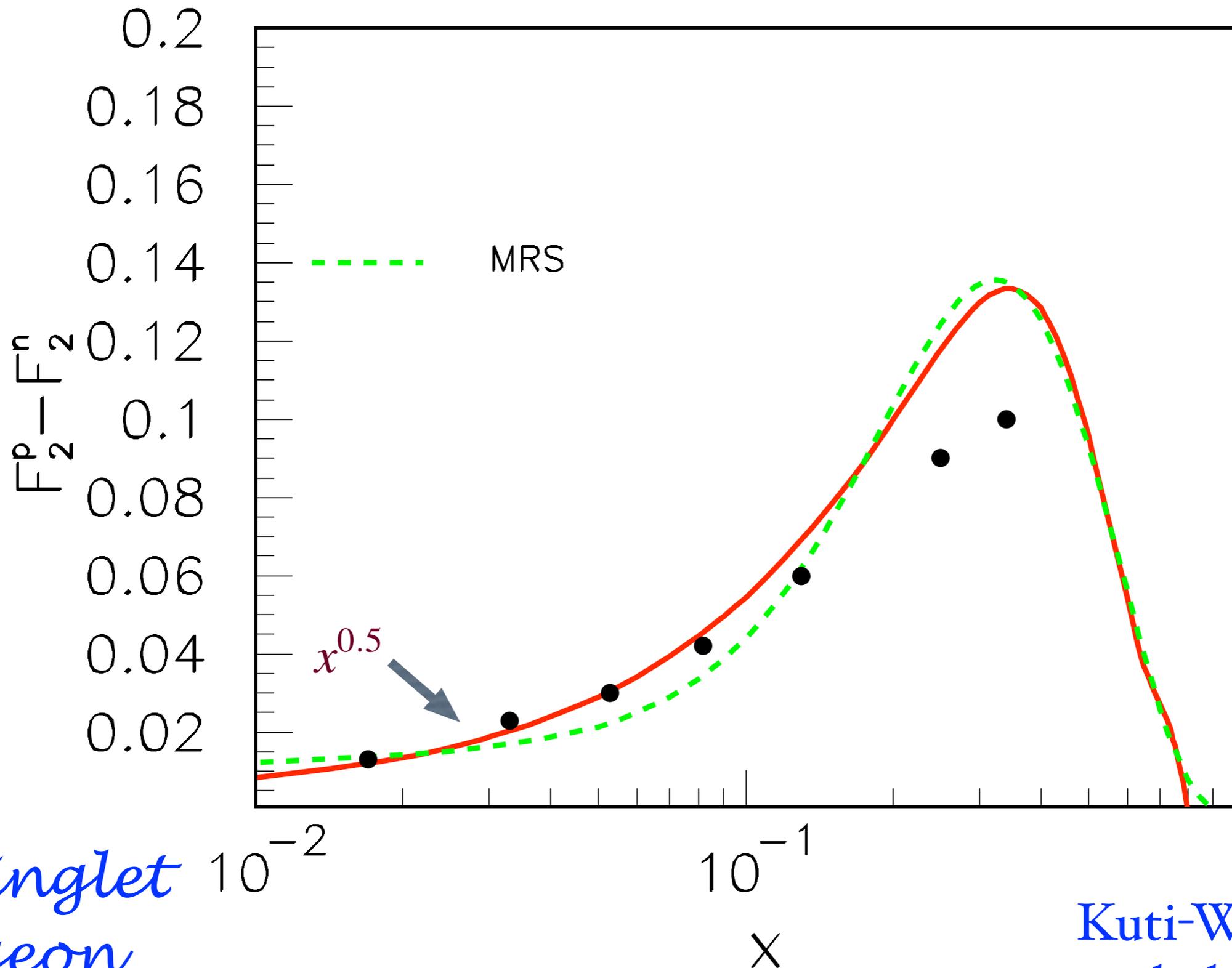
Regge contribution: $\sigma_{\bar{q}N} \sim \hat{s}^{\alpha_R - 1}$

Nonsinglet Kuti-Weisskoff $F_{2p} - F_{2n} \propto \sqrt{x_{bj}}$ at small x_{bj} .

Shadowing of $\sigma_{\bar{q}M}$ produces shadowing of nuclear structure function.



Landshoff,
Polkinghorne, Short
Close, Gunion, sjb
Schmidt, Yang, Lu,
sjb



*Non-singlet
Reggeon
Exchange*

*Kuti-Weisskopf
behavior*

**Forward Physics
Workshop,
Guanajuato, Mexico
19 November 2019**

**Novel Features of Heavy Quark
Phenomenology**

Stan Brodsky
SLAC
NATIONAL ACCELERATOR LABORATORY



Reggeon Exchange

Phase of two-step amplitude relative to one step:

$$\frac{1}{\sqrt{2}}(1 - i) \times i = \frac{1}{\sqrt{2}}(i + 1)$$

Constructive Interference

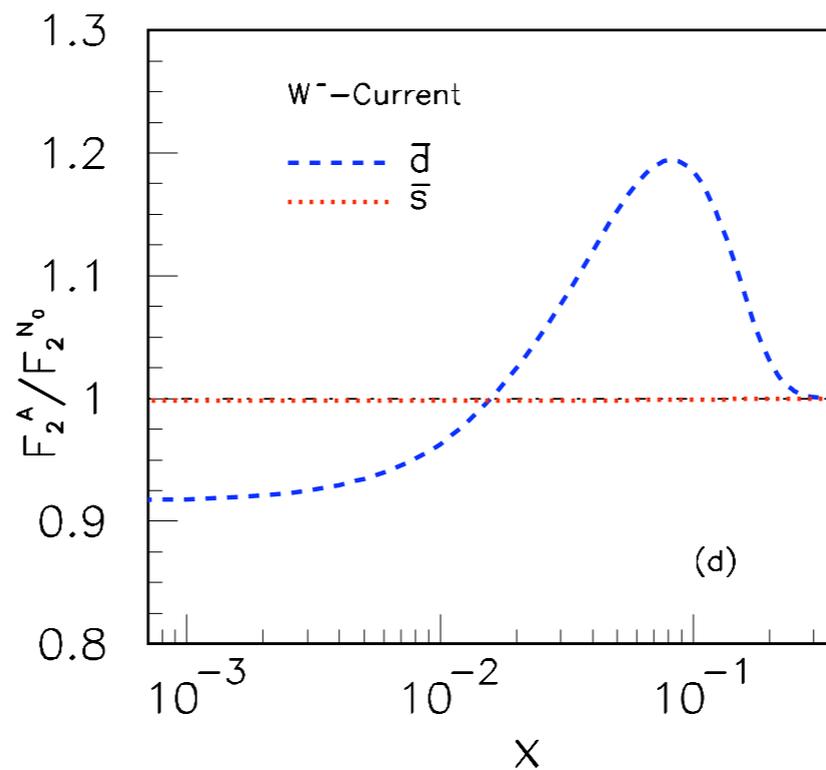
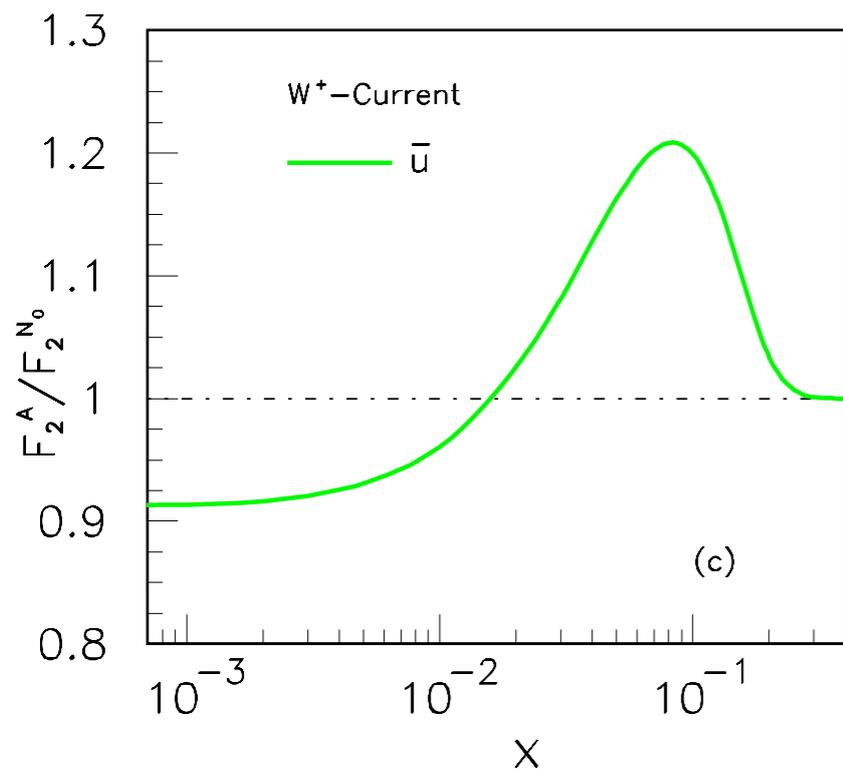
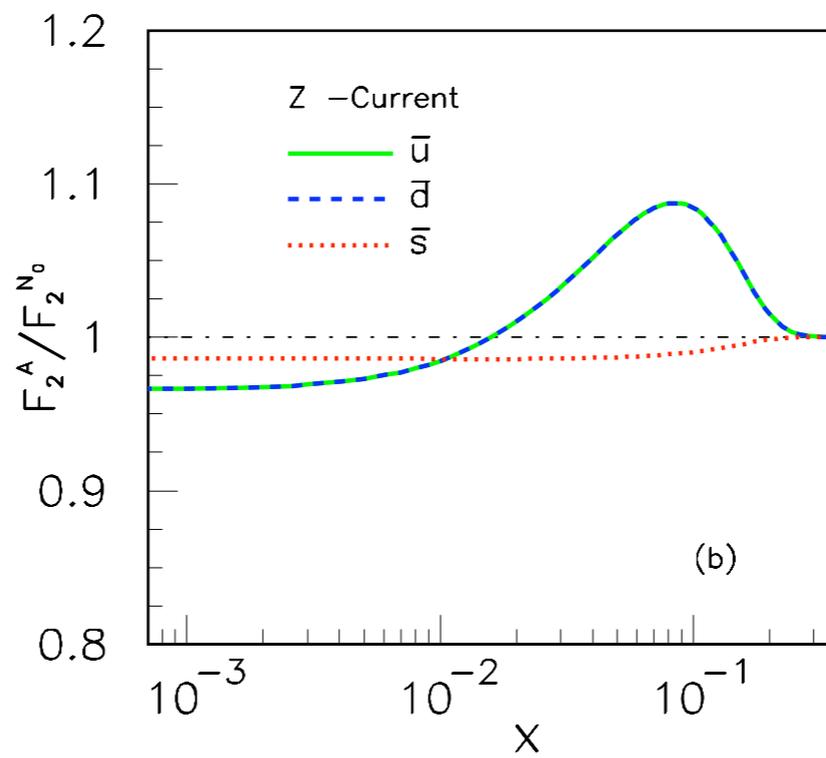
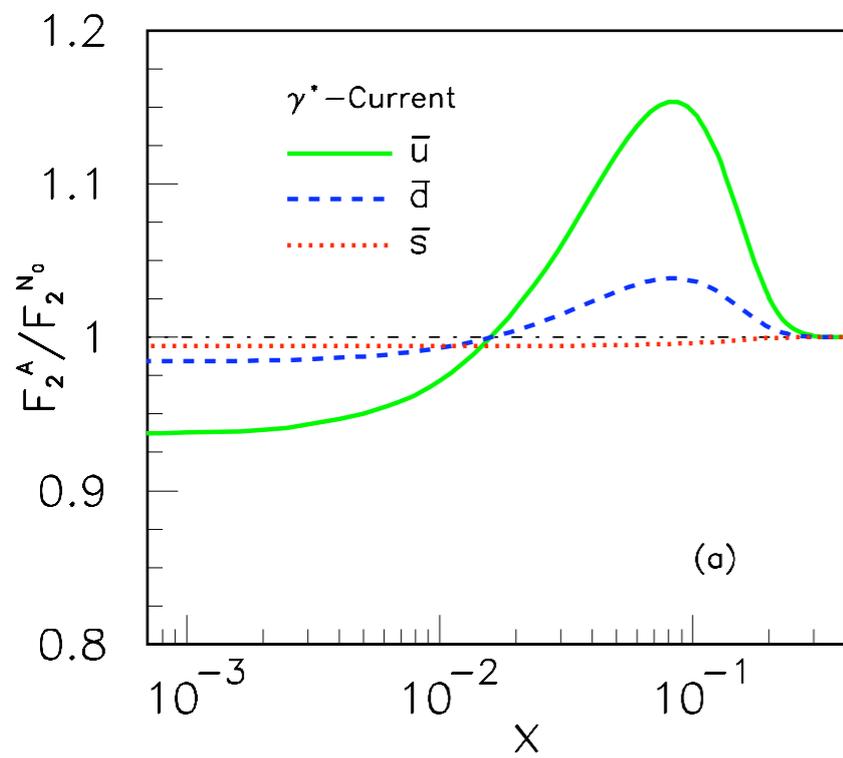
Depends on quark flavor!

Thus antishadowing is not universal

Different for couplings of γ^* , Z^0 , W^\pm

Critical tests: Tagged SIDIS, Drell-Yan

Schmidt, Yang; sjb

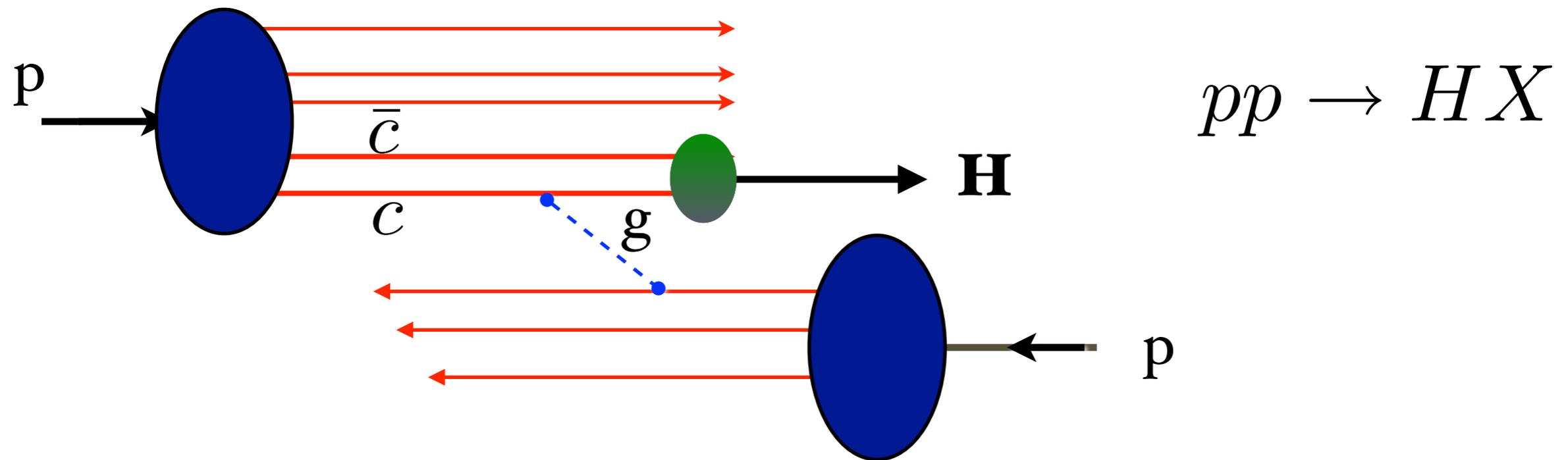


Modifies
NuTeV extraction of
 $\sin^2 \theta_W$

Test in flavor-tagged
DIS at the EIC

Nuclear Antishadowing not universal !

*Intrinsic Charm Mechanism for Inclusive
High- x_F Higgs Production*

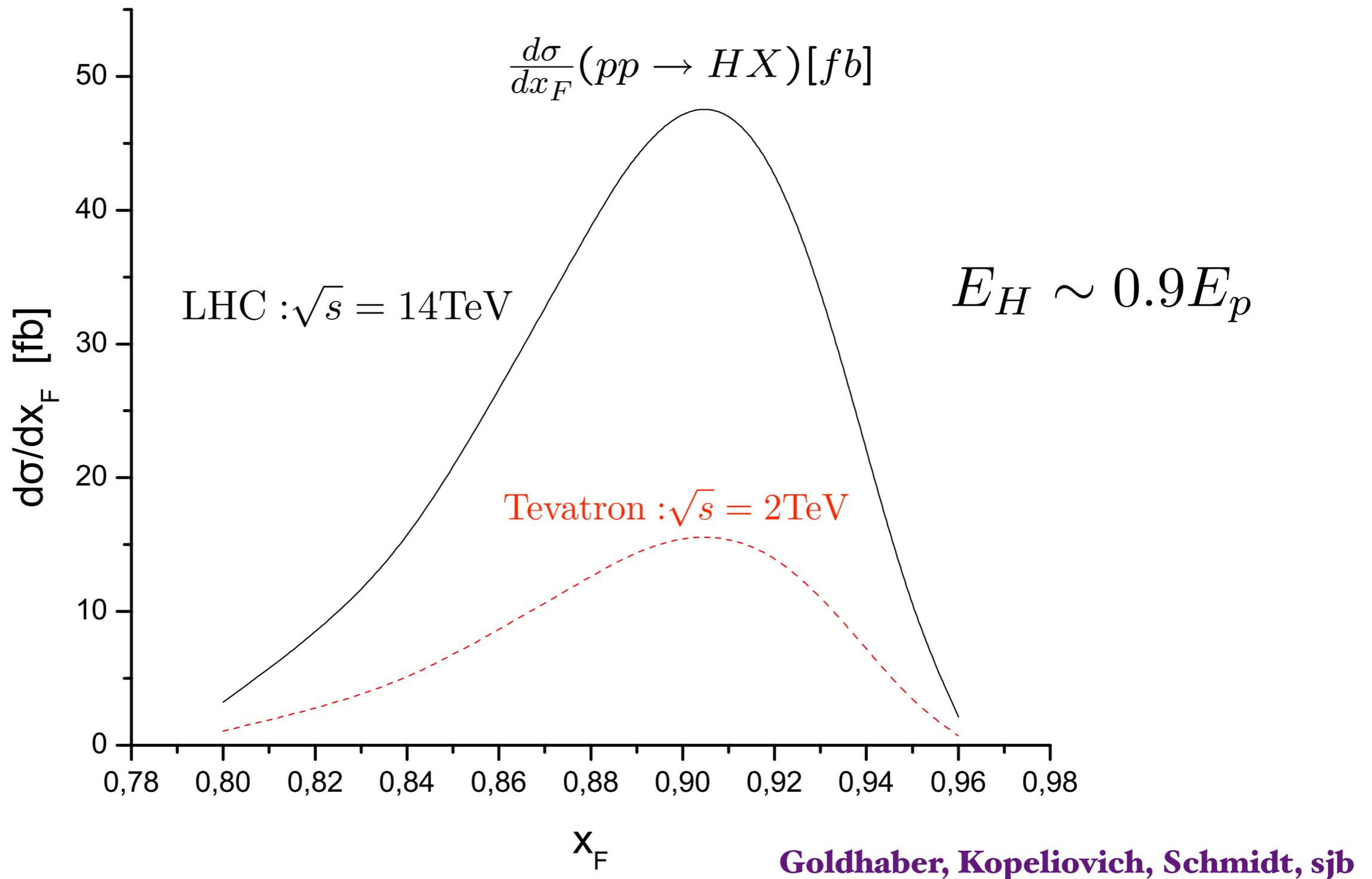


Also: intrinsic strangeness, bottom, top

Higgs can have > 80% of Proton Momentum!

New production mechanism for Higgs

Intrinsic Heavy Quark Contribution to Inclusive Higgs Production



Measure $H \rightarrow ZZ^* \rightarrow \mu^+ \mu^- \mu^+ \mu^-$.

$$H_{LF}^{QCD} |\psi\rangle = M^2 |\psi\rangle$$

$$x = \frac{k^+}{P^+} = \frac{k^0 + k^3}{P^0 + P^3}$$

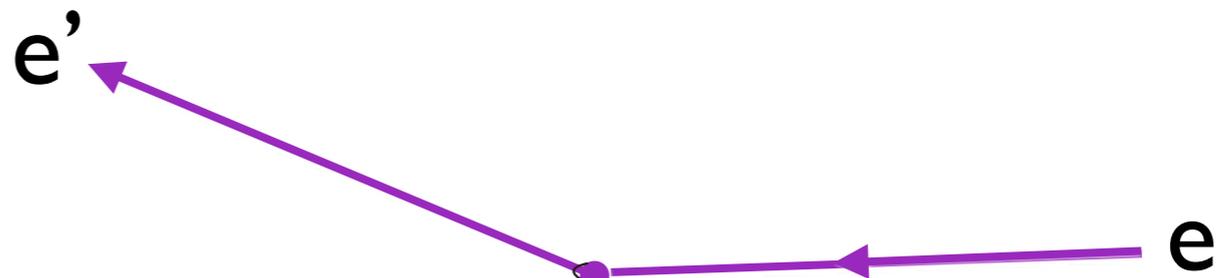
$$P^+, \vec{P}_\perp$$

$$\psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

*Eigenstate of LF Hamiltonian:
Off-shell in Invariant Mass*

***Measurements of hadron LF
wavefunction are at fixed LF time***

Like a flash photograph



$$x_i P^+, x_i \vec{P}_\perp + \vec{k}_{\perp i}$$

Light Front Wave Functions: Boost Invariant

Fixed $\tau = t + z/c$

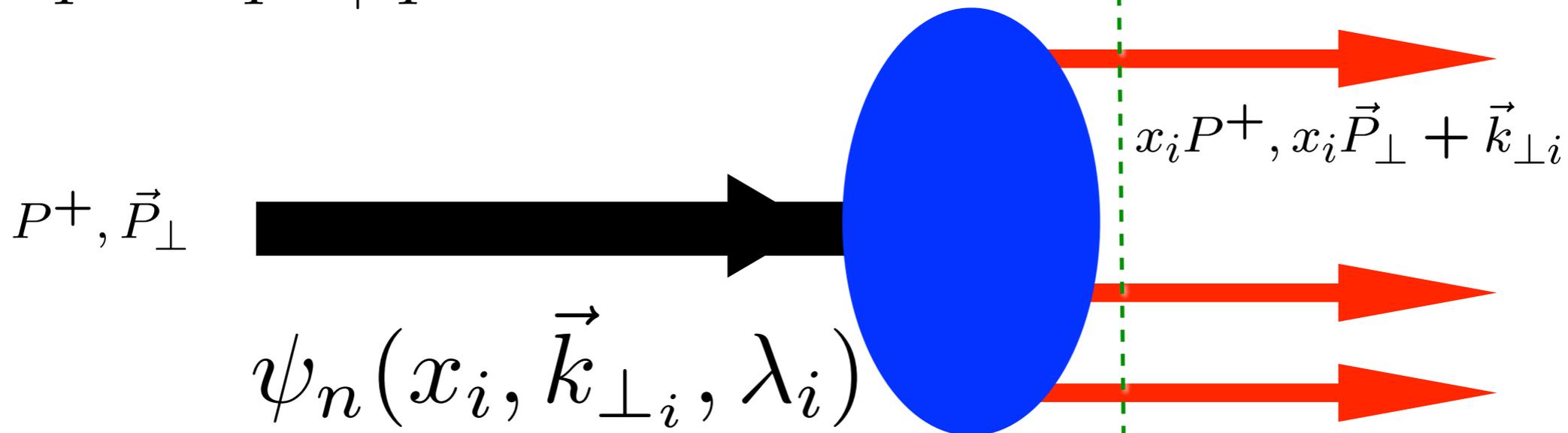
$$x_{bj} = x = \frac{k^+}{P^+}$$

Light-Front Wavefunctions: **rigorous** representation of composite systems in quantum field theory

Eigenstate of LF Hamiltonian

$$x = \frac{k^+}{P^+} = \frac{k^0 + k^3}{P^0 + P^3}$$

Fixed $\tau = t + z/c$



$$H_{LF}^{QCD} |\psi\rangle = M^2 |\psi\rangle$$

$$|p, J_z\rangle = \sum_{n=3} \psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; x_i, \vec{k}_{\perp i}, \lambda_i\rangle$$

$$\sum_i^n x_i = 1$$

$$\sum_i^n \vec{k}_{\perp i} = \vec{0}_\perp$$

Invariant under boosts! Independent of P^μ

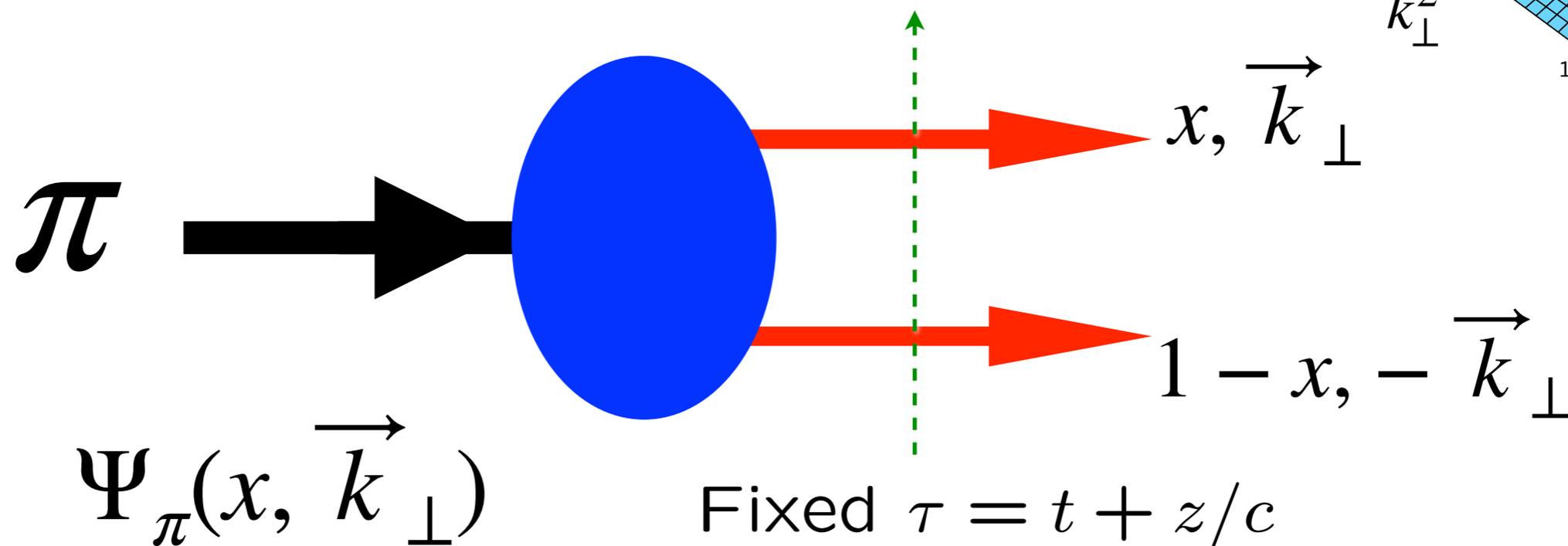
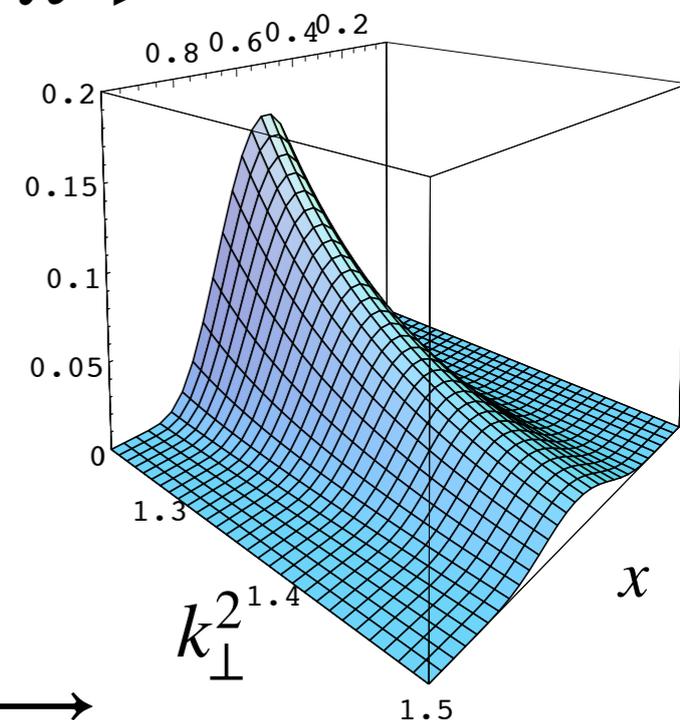
Causal, Frame-independent. Creation Operators on Simple Vacuum, Current Matrix Elements are Overlaps of LFWFS

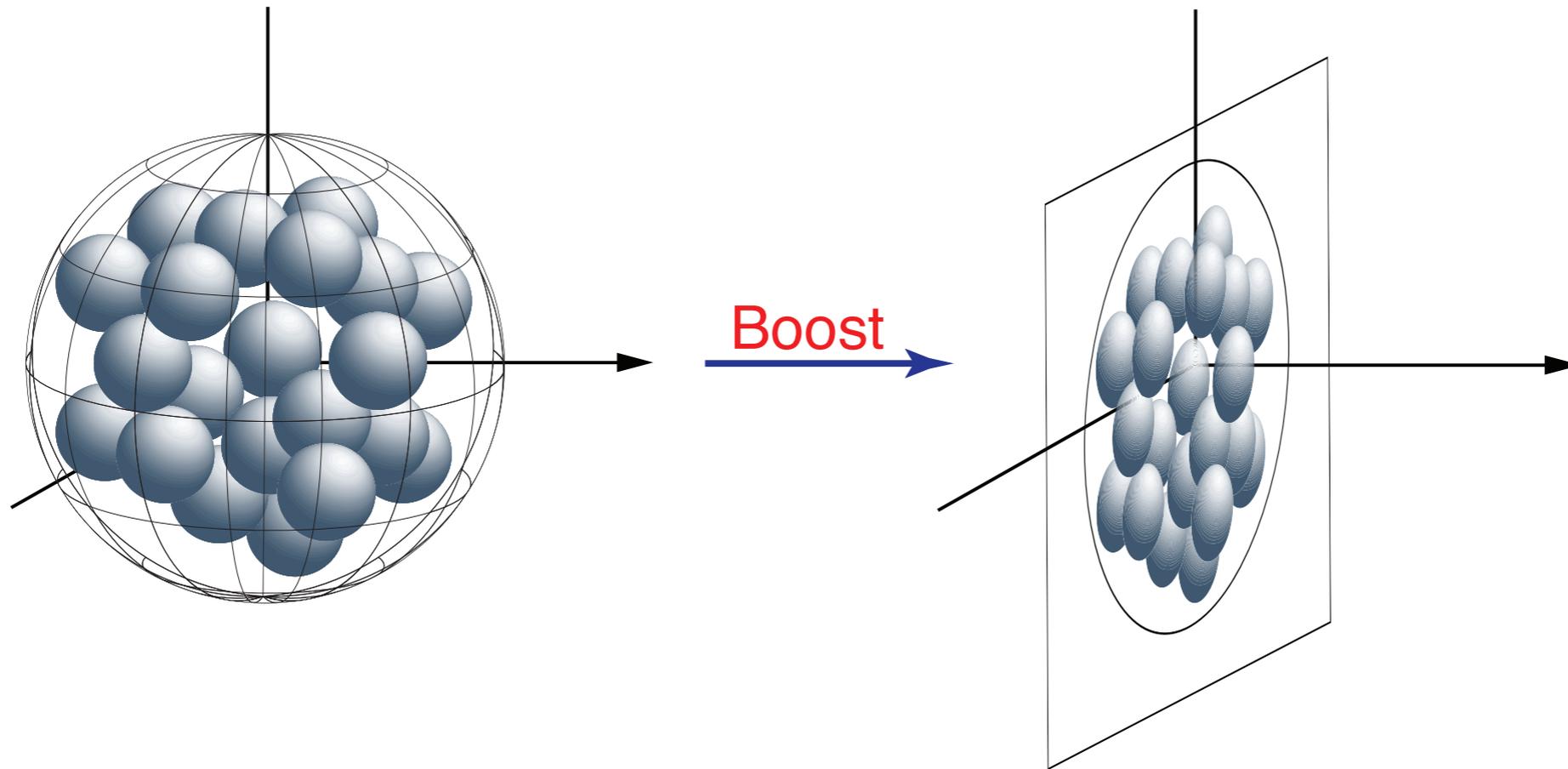
The Pion's Valence Light-Front Wavefunction

- Relativistic Quantum-Mechanical Wavefunction of the pion eigenstate $H_{LF}^{QCD} |\pi\rangle = m_\pi^2 |\pi\rangle$

$$\Psi_\pi(x, \vec{k}_\perp) = \langle q(x, \vec{k}_\perp) \bar{q}(1-x, -\vec{k}_\perp) | \pi \rangle$$

- Independent of the observer's or pion's motion
- No Lorentz contraction; causal
- **Confined** quark-antiquark bound state





large nucleus before and after an ultra-relativistic boost.

Is this really true? Will an electron-proton collider see different results than a fixed target experiment such as SLAC because the nucleus is squashed to a pancake?

Light-Front: No length contraction — no pancakes!

**Penrose
Terrell
Weiskopf**

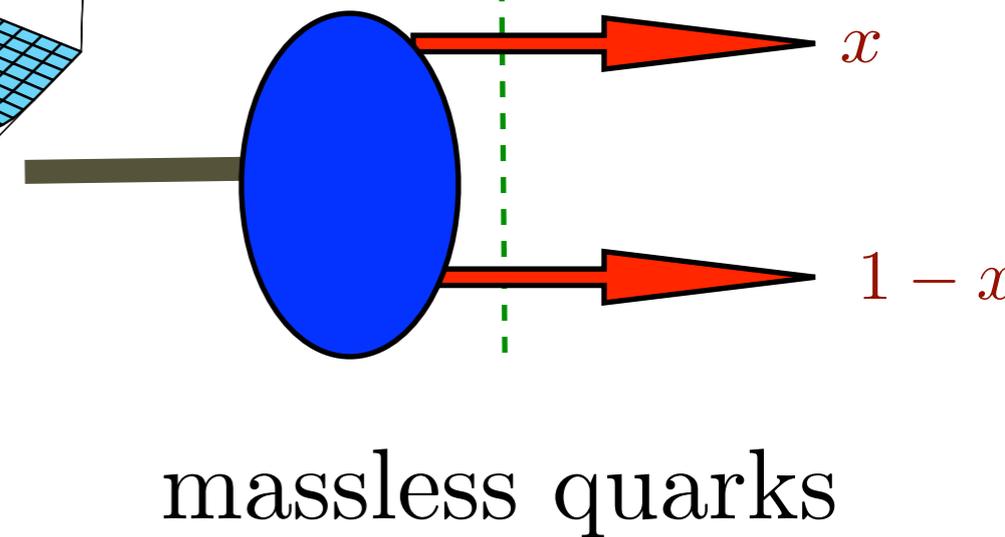
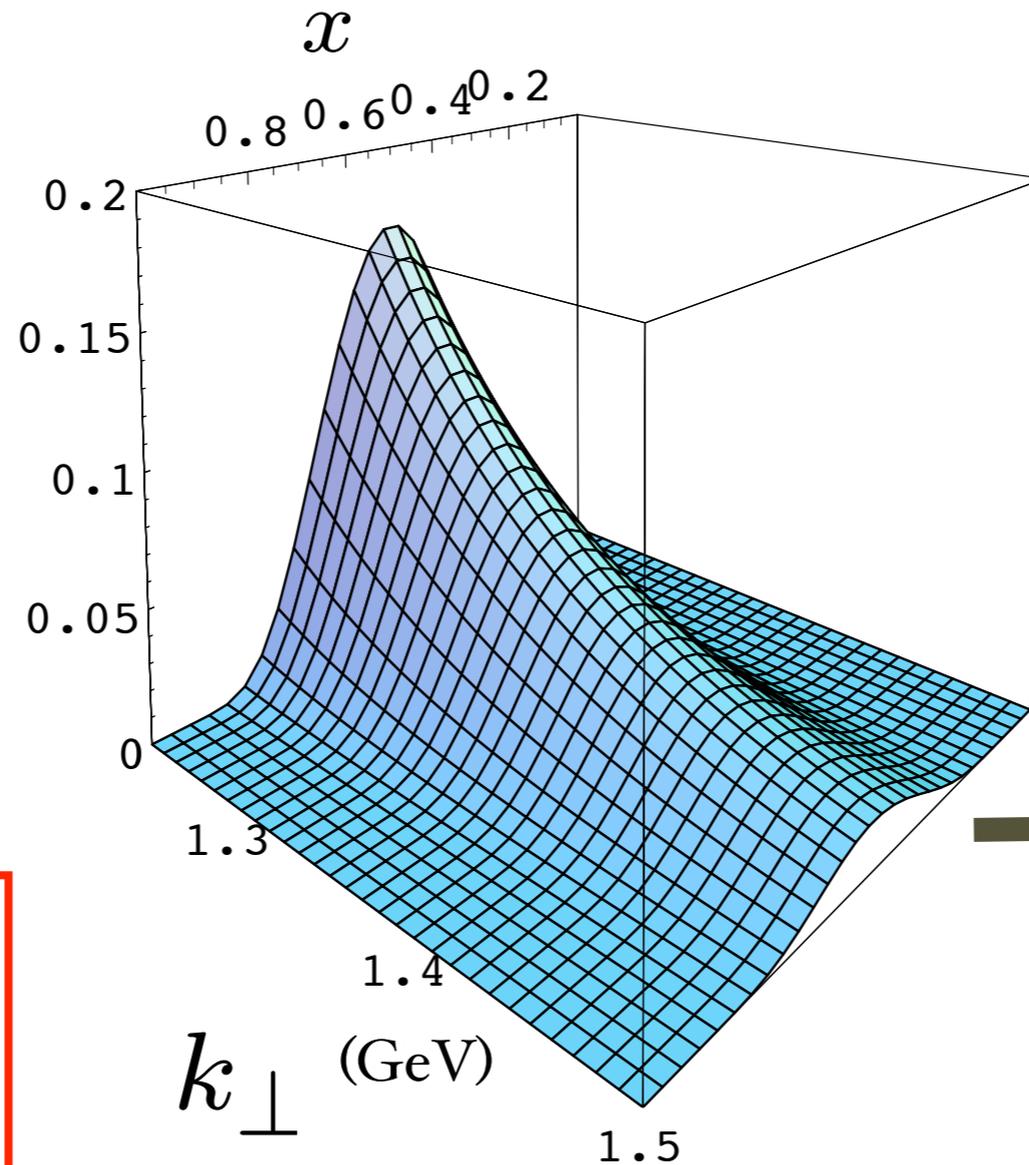
We do not make observations at one time t !

Prediction from AdS/QCD: Meson LFWF

de Teramond,
Cao, sjb

“Soft Wall”
model

$$\psi_M(x, k_{\perp}^2)$$



Note coupling

$$k_{\perp}^2, x$$

$$\psi_M(x, k_{\perp}) = \frac{4\pi}{\kappa \sqrt{x(1-x)}} e^{-\frac{k_{\perp}^2}{2\kappa^2 x(1-x)}}$$

$$\phi_{\pi}(x) = \frac{4}{\sqrt{3}\pi} f_{\pi} \sqrt{x(1-x)}$$

$$f_{\pi} = \sqrt{P_{q\bar{q}}} \frac{\sqrt{3}}{8} \kappa = 92.4 \text{ MeV}$$

Provides Connection of Confinement to Hadron Structure

$$\psi_n(\vec{k}_{\perp i}, x_i) \propto \frac{1}{\kappa^{n-1}} e^{-\mathcal{M}_n^2/2\kappa^2} \prod_{j=1}^n \frac{1}{\sqrt{x_j}}$$

Properties of Color-Confining LFWF

- minimal $\mathcal{M}_n^2 = \sum_{i=1}^n \left(\frac{k_{\perp}^2 + m^2}{x} \right)_i$
- Maximum when $x_i \propto m_{\perp i} = \sqrt{m_i^2 + k_{\perp i}^2}$
- Maximum overlap at matching rapidity

$$y = \frac{1}{2} \log \frac{k^+}{k^-} = \log \frac{x P^+}{m_{\perp}}$$

Frame independent $\Delta y = y_a - y_b = \log \frac{x_a}{m_{\perp a}} - \log \frac{x_b}{m_{\perp b}}$

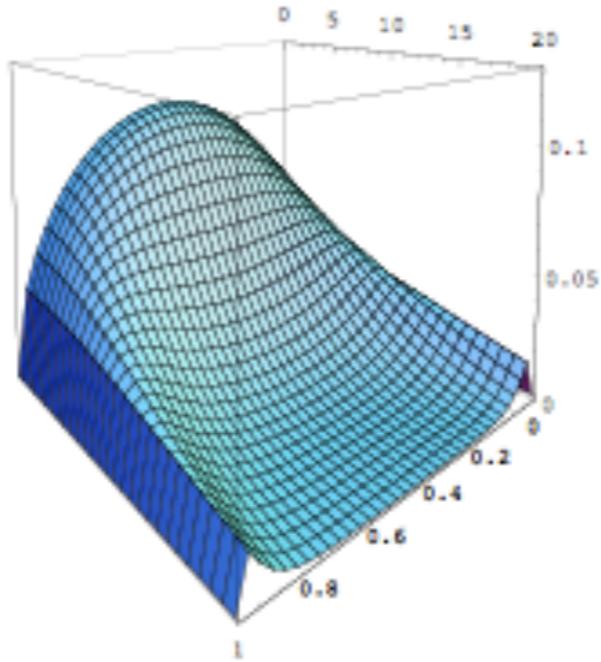
Relative to proton $\Delta y = y_H - y_p = \log \frac{x_H}{m_{\perp H}/m_p}$

Feynman: Correlations with proton $\Delta y < 2$

$$|\pi^+\rangle = |u\bar{d}\rangle$$

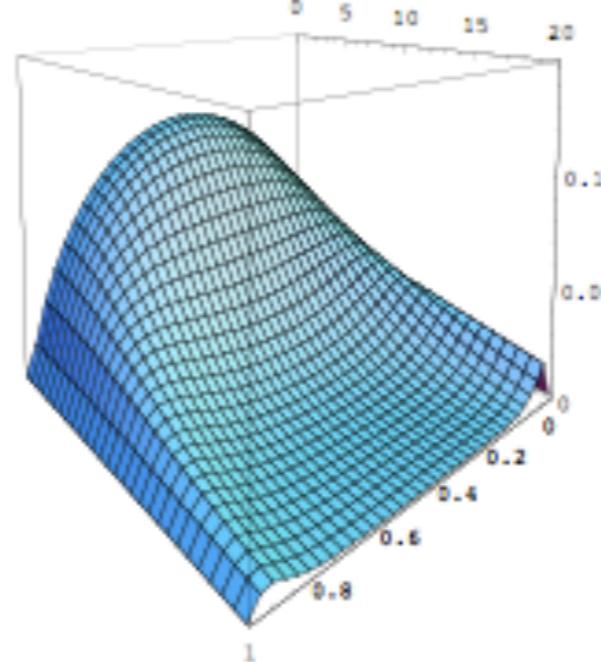
$$m_u = 2 \text{ MeV}$$

$$m_d = 5 \text{ MeV}$$



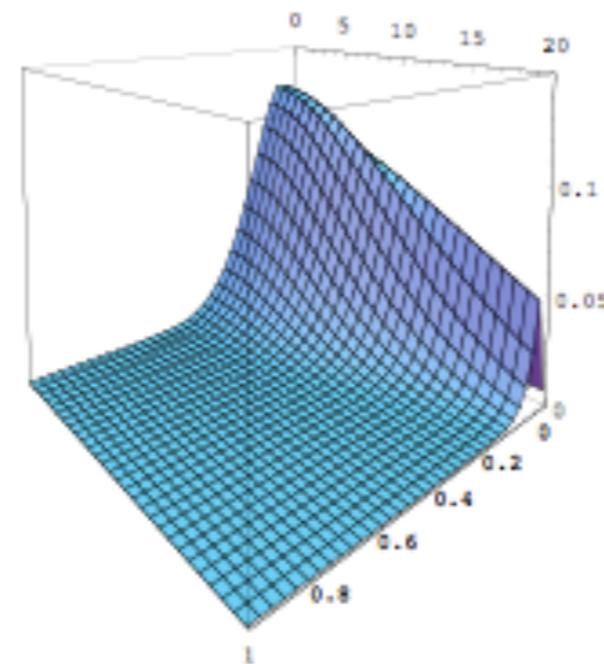
$$|K^+\rangle = |u\bar{s}\rangle$$

$$m_s = 95 \text{ MeV}$$

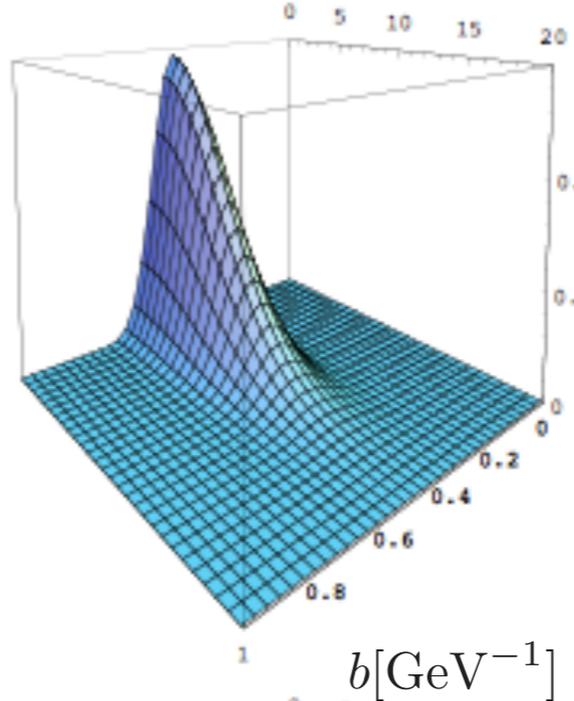


$$|D^+\rangle = |c\bar{d}\rangle$$

$$m_c = 1.25 \text{ GeV}$$

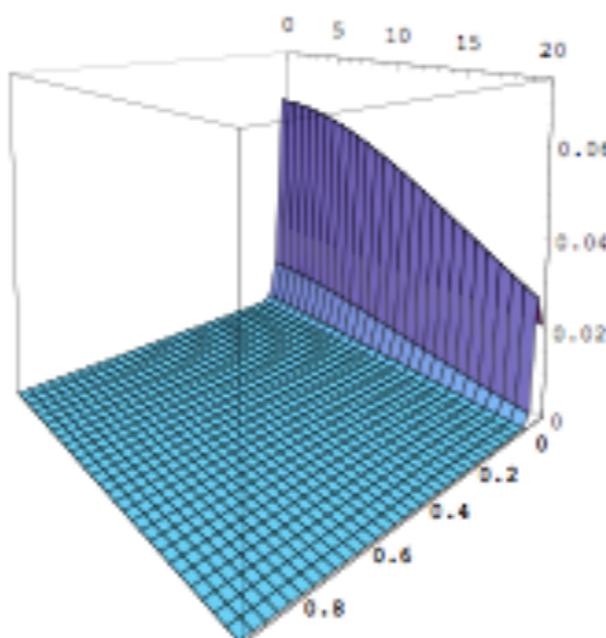


$$|\eta_c\rangle = |c\bar{c}\rangle$$



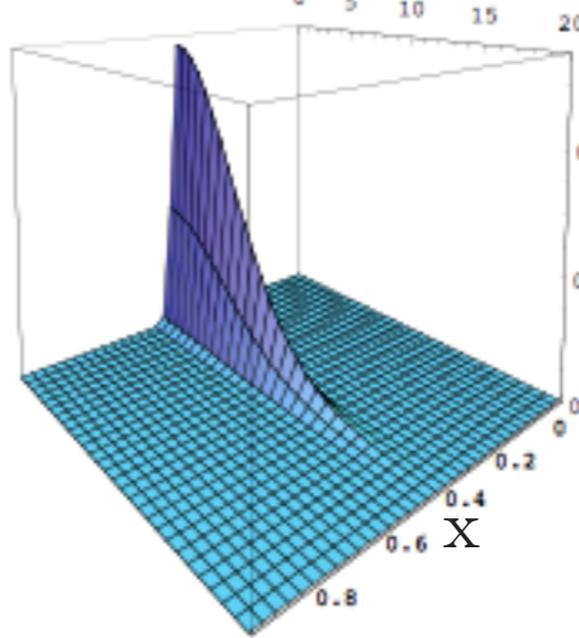
$$|B^+\rangle = |u\bar{b}\rangle$$

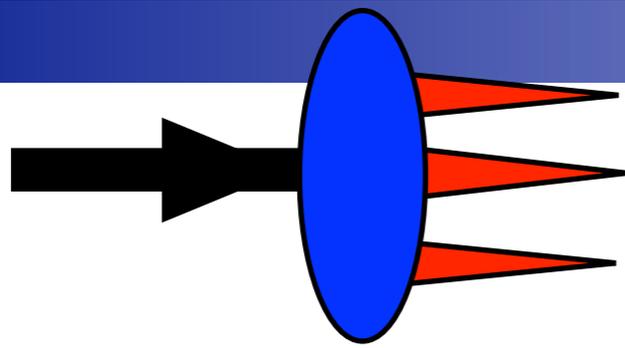
$$m_b = 4.2 \text{ GeV}$$



$$|\eta_b\rangle = |b\bar{b}\rangle$$

$$\kappa = 375 \text{ MeV}$$





• *Light Front Wavefunctions:*

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

Transverse density in momentum space

GTMDs

$$x, \vec{k}_{\perp}, \vec{b}_{\perp}$$

Momentum space $\vec{k}_{\perp} \leftrightarrow \vec{z}_{\perp}$ Position space
 $\vec{\Delta}_{\perp} \leftrightarrow \vec{b}_{\perp}$

Transverse density in position space

TMDs

$$x, \vec{k}_{\perp}$$

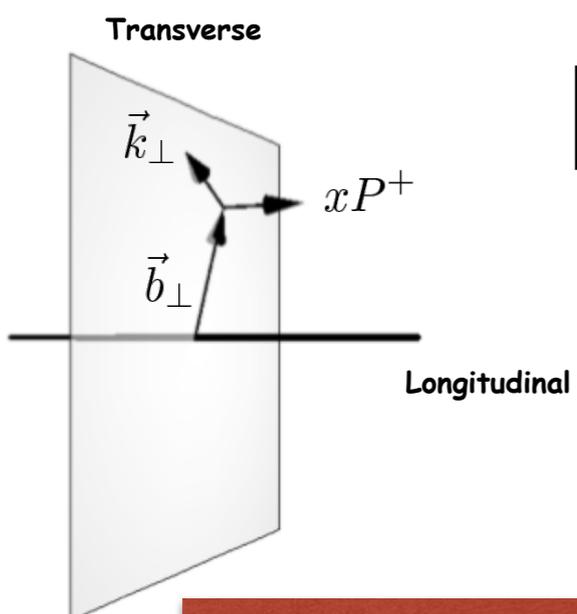
TMFFs

$$\vec{k}_{\perp}, \vec{b}_{\perp}$$

GPDs

$$x, \vec{b}_{\perp}$$

Lorce, Pasquini



TMSDs

$$\vec{k}_{\perp}$$

PDFs

$$x,$$

FFs

$$\vec{b}_{\perp}$$

Charges

- $\int d^2 b_{\perp}$
- $\int dx$
- $\int d^2 k_{\perp}$

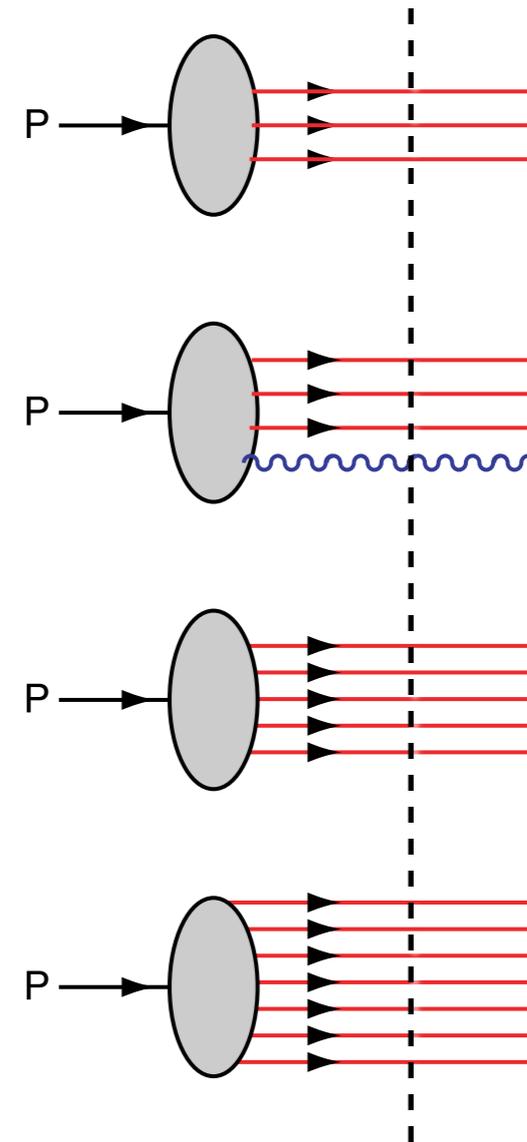
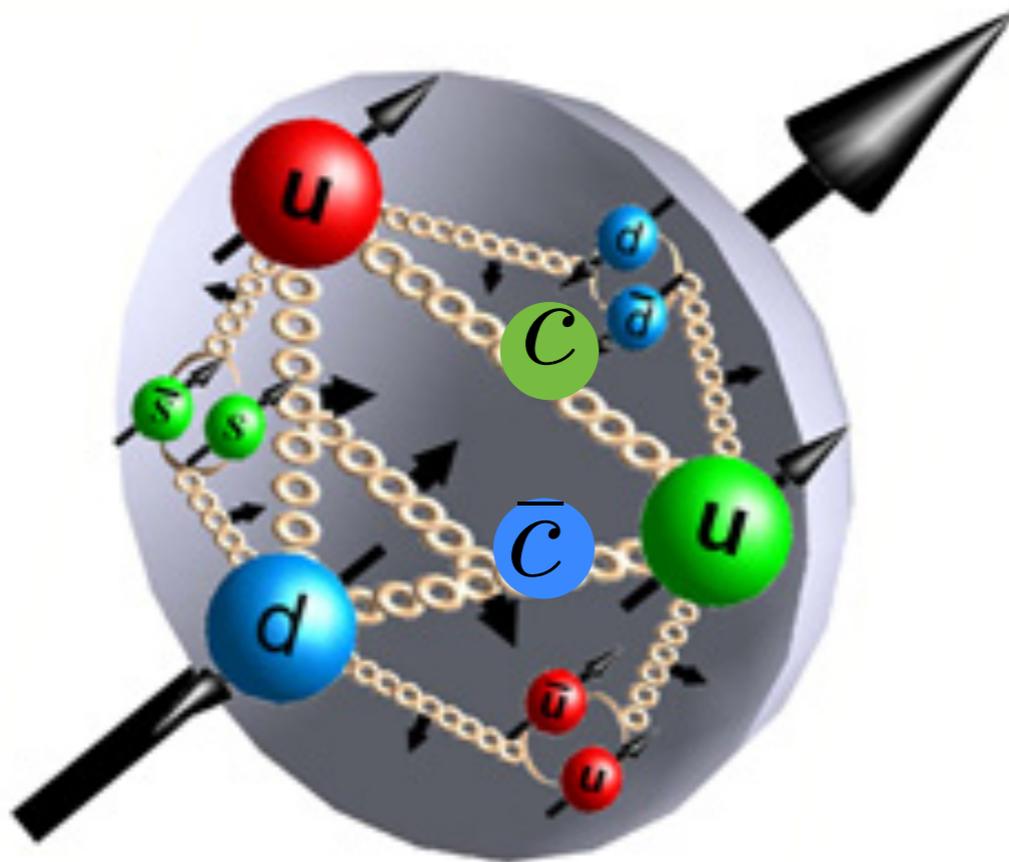
+ Factorization-Breaking Lensing Corrections: Sivers, T-odd

Wavefunction at fixed LF time: Arbitrarily Off-Shell in Invariant Mass

$$H_{LF}^{QCD} |\psi\rangle = M^2 |\psi\rangle$$

Higher Fock States of the Proton:

$$|p, J_z\rangle = \sum_{n=3} \psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; x_i, \vec{k}_{\perp i}, \lambda_i\rangle$$



Fixed LF time

Eigenstate of LF Hamiltonian: all Fock states contribute

$$|p, S_z\rangle = \sum_{n=3} \Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; \vec{k}_{\perp i}, \lambda_i\rangle$$

sum over states with $n=3, 4, \dots$ constituents

The Light Front Fock State Wavefunctions

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

are boost invariant; they are independent of the hadron's energy and momentum P^μ .

The light-cone momentum fraction

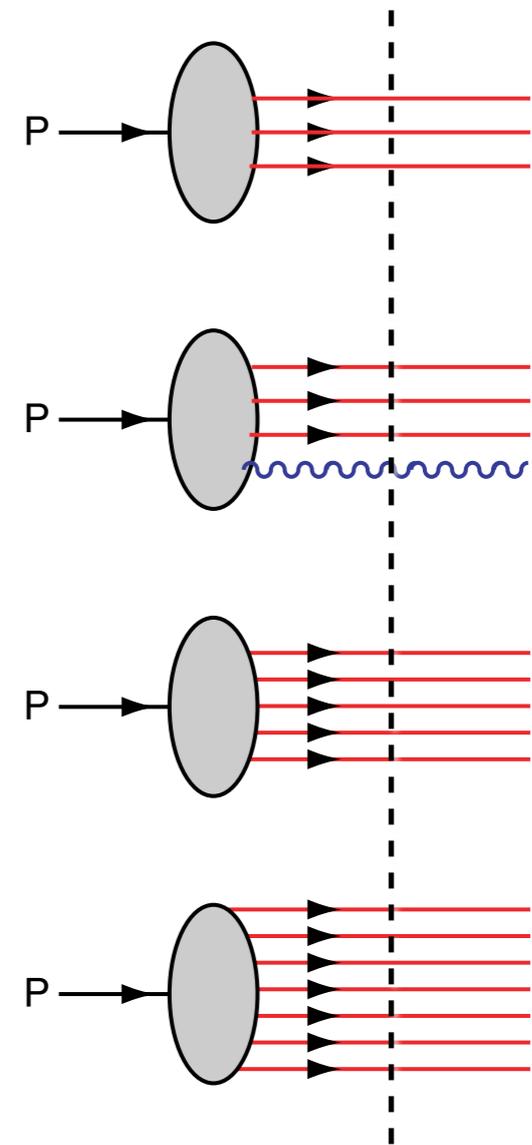
$$x_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^z}{P^0 + P^z}$$

are boost invariant.

$$\sum_i^n k_i^+ = P^+, \quad \sum_i^n x_i = 1, \quad \sum_i^n \vec{k}_i^\perp = \vec{0}^\perp.$$

Intrinsic heavy quarks
 $s(x), c(x), b(x)$ at high x !

$\bar{s}(x) \neq s(x)$
 $\bar{u}(x) \neq \bar{d}(x)$



Fixed LF time
 $\tau = t + z/c$

Deuteron: Hidden Color

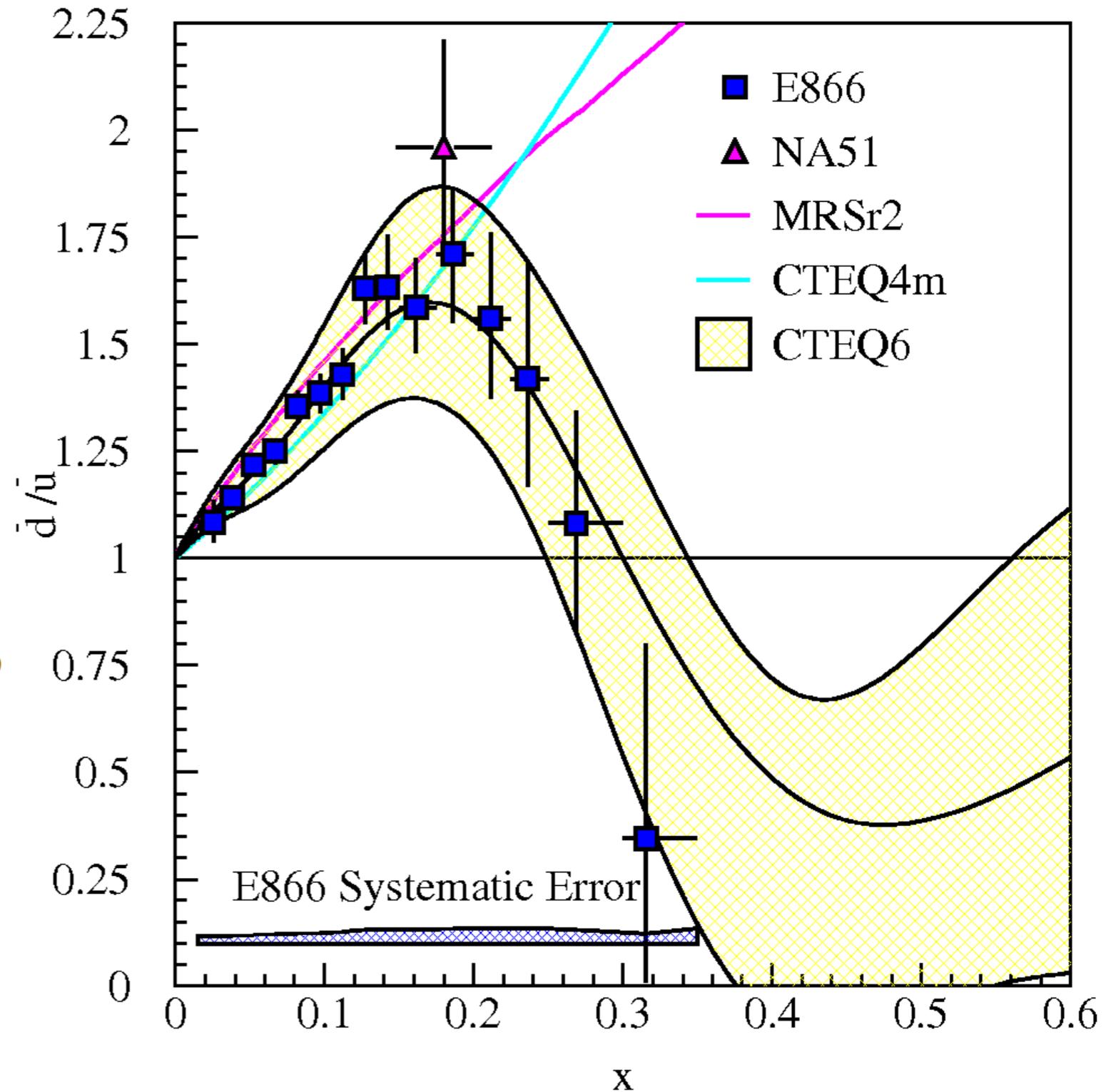
$\bar{d}(x)/\bar{u}(x)$ for $0.015 \leq x \leq 0.35$

■ E866/NuSea (Drell-Yan)

$$\bar{d}(x) \neq \bar{u}(x)$$

Interactions of quarks at same rapidity in 5-quark Fock state

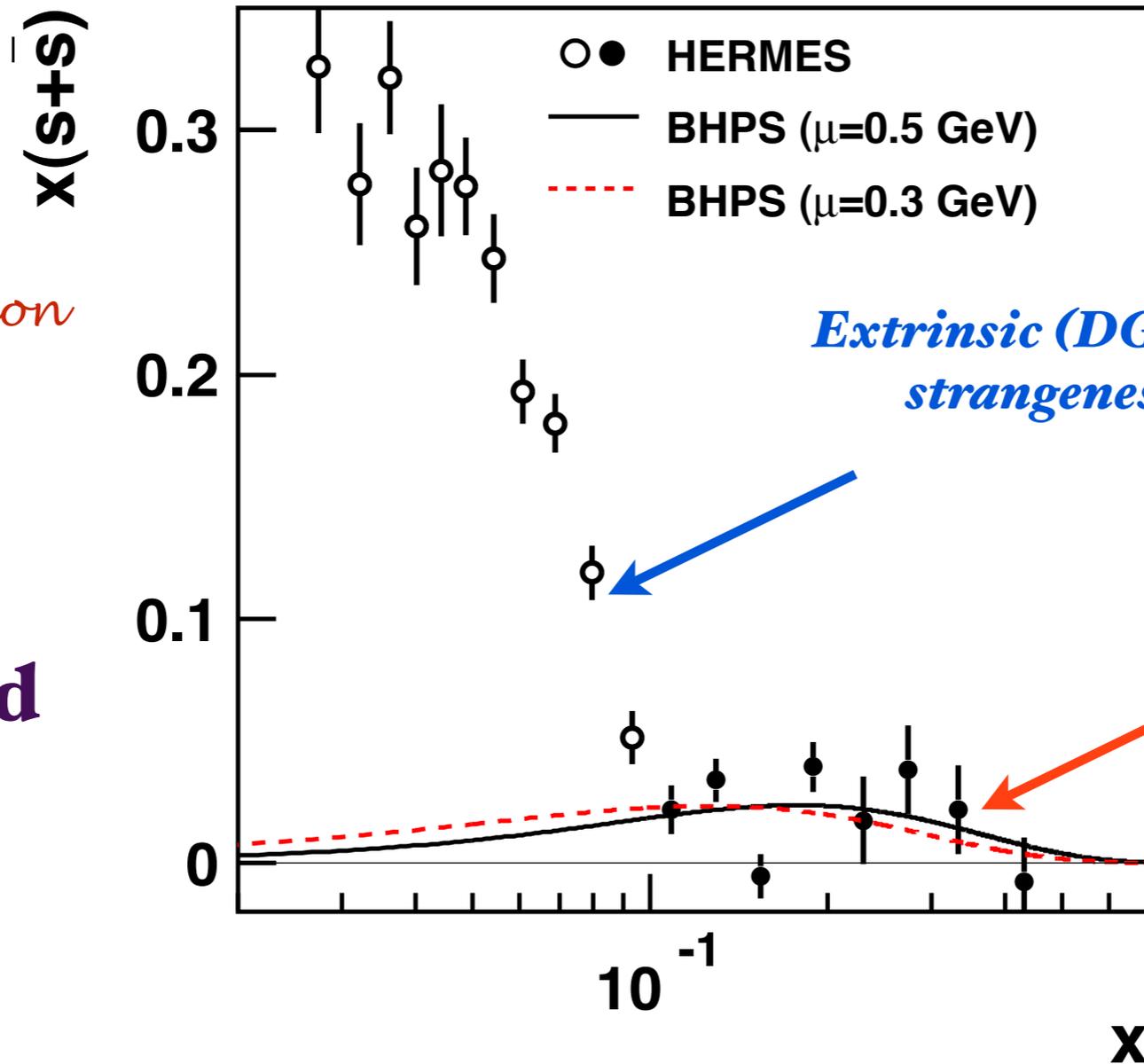
Intrinsic sea quarks



HERMES: Two components to $s(x, Q^2)$!

BHPS: Hoyer, Sakai, Peterson, sjb

Sensitive to Fragmentation Function



Intrinsic strangeness!

Consistent with intrinsic charm data

QCD: $\frac{1}{M_Q^2}$ scaling

W. C. Chang and J.-C. Peng
arXiv:1105.2381

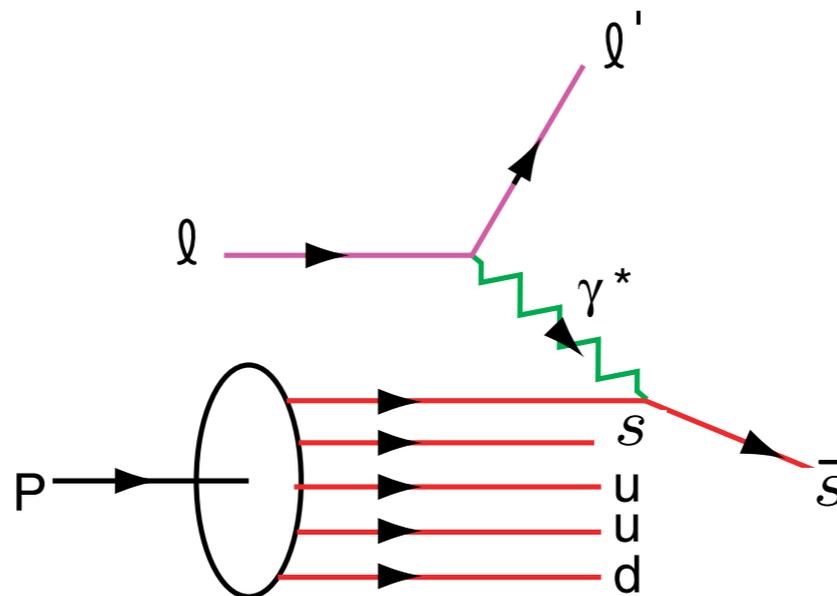
Comparison of the HERMES $x(s(x) + \bar{s}(x))$ data with the calculations based on the BHPS model. The solid and dashed curves are obtained by evolving the BHPS result to $Q^2 = 2.5 \text{ GeV}^2$ using $\mu = 0.5 \text{ GeV}$ and $\mu = 0.3 \text{ GeV}$, respectively. The normalizations of the calculations are adjusted to fit the data at $x > 0.1$ with statistical errors only, denoted by solid circles.

$$s(x, Q^2) = s(x, Q^2)_{\text{extrinsic}} + s(x, Q^2)_{\text{intrinsic}}$$

Measure strangeness distribution in Semi-Inclusive DIS at JLab

$$\text{Is } s(x) = \bar{s}(x)?$$

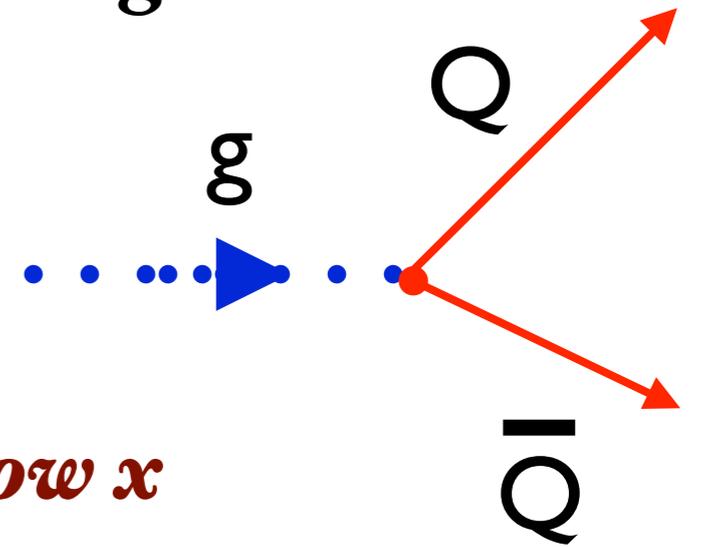
- **Non-symmetric strange and antistrange sea?**
- **Non-perturbative physics; e.g** $|uuds\bar{s}\rangle \simeq |\Lambda(uds)K^+(\bar{s}u)\rangle$
- **Important for interpreting NuTeV anomaly** **B. Q. Ma, sjb**



Tag struck quark flavor in semi-inclusive DIS $ep \rightarrow e' K^+ X$

Do heavy quarks exist in the proton at high x ?

*Conventional wisdom:
gluon splitting*



*Heavy quarks generated only at low x
via DGLAP evolution
from gluon splitting*

Maximally off-shell - requires low x , high W^2

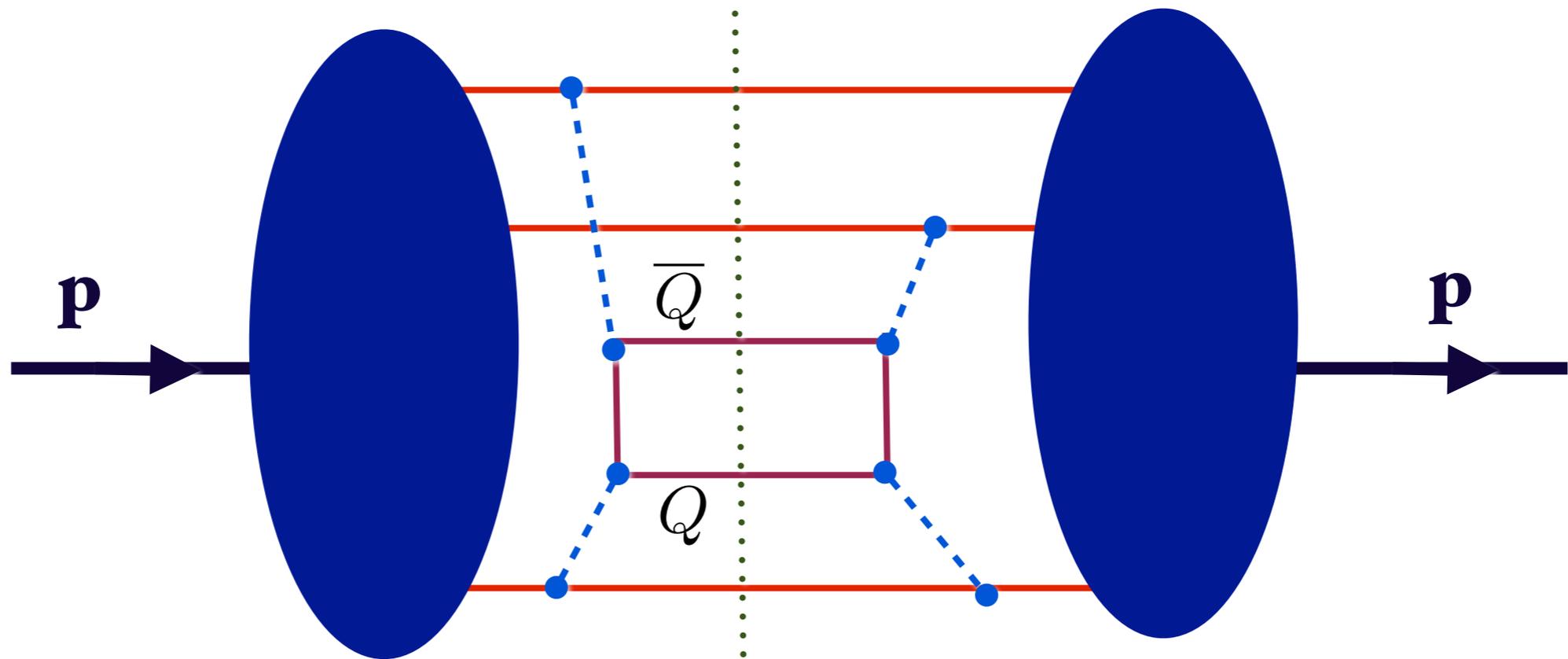
$$s(x, \mu_F^2) = c(x, \mu_F^2) = b(x, \mu_F^2) \equiv 0$$

at starting scale $Q_0^2 = \mu_F^2$

Conventional wisdom is wrong even in QED!

Fixed LF time

*Proton Self Energy
Intrinsic Heavy Quarks*



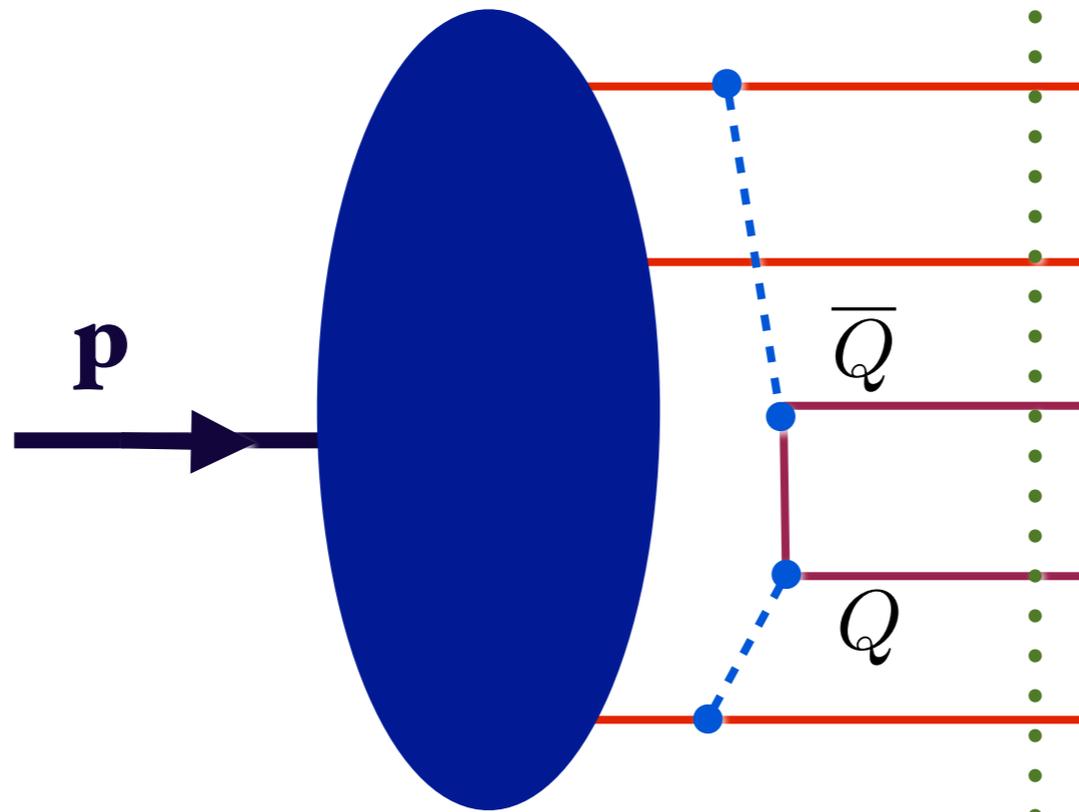
Probability (QED) $\propto \frac{1}{M_\ell^4}$

Probability (QCD) $\propto \frac{1}{M_Q^2}$

Rigorous OPE Analysis

**Collins, Ellis, Gunion, Mueller, sjb
M. Polyakov, et al.**

*Proton 5-quark Fock State:
Intrinsic Heavy Quarks*



*QCD predicts
Intrinsic Heavy
Quarks at high x !*

Minimal off-shellness

$$x_Q \propto (m_Q^2 + k_{\perp}^2)^{1/2}$$

Maximum at Equal rapidity!

Probability (QED) $\propto \frac{1}{M_{\ell}^4}$

Probability (QCD) $\propto \frac{1}{M_Q^2}$

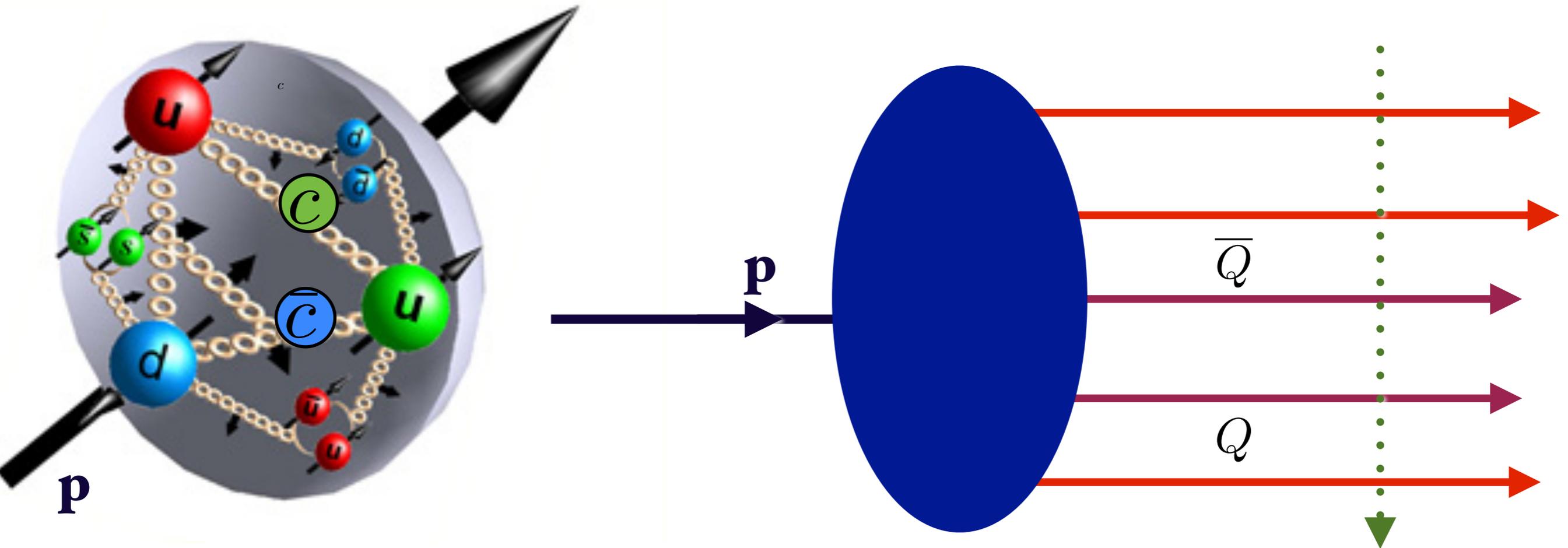
**Rigorous OPE
Analysis**

**Collins, Ellis, Gunion, Mueller, sjb
Polyakov, et al.**

Color confinement potential from AdS/QCD

$$U(\zeta^2) = \kappa^4 \zeta^2 = b_{\perp}^2 x(1-x)$$

Fixed $\tau = t + z/c$



$$\psi_n(\vec{k}_{\perp i}, x_i) \propto \frac{1}{\kappa^{n-1}} e^{-\mathcal{M}_n^2/2\kappa^2} \prod_{j=1}^n \frac{1}{\sqrt{x_j}}$$

$$\mathcal{M}_n^2 = \sum_{i=1}^n \left(\frac{k_{\perp}^2 + m^2}{x} \right)_i$$

$$\psi_n(\vec{k}_{\perp i}, x_i) \propto \frac{1}{\kappa^{n-1}} e^{-\mathcal{M}_n^2/2\kappa^2} \prod_{j=1}^n \frac{1}{\sqrt{x_j}}$$

Properties of Color-Confining LFWF

- minimal $\mathcal{M}_n^2 = \sum_{i=1}^n \left(\frac{k_{\perp}^2 + m^2}{x} \right)_i$
- Maximum when $x_i \propto m_{\perp i} = \sqrt{m_i^2 + k_{\perp i}^2}$
- Maximum overlap at matching rapidity

$$y = \frac{1}{2} \log \frac{k^+}{k^-} = \log \frac{x P^+}{m_{\perp}}$$

Frame independent $\Delta y = y_a - y_b = \log \frac{x_a}{m_{\perp a}} - \log \frac{x_b}{m_{\perp b}}$

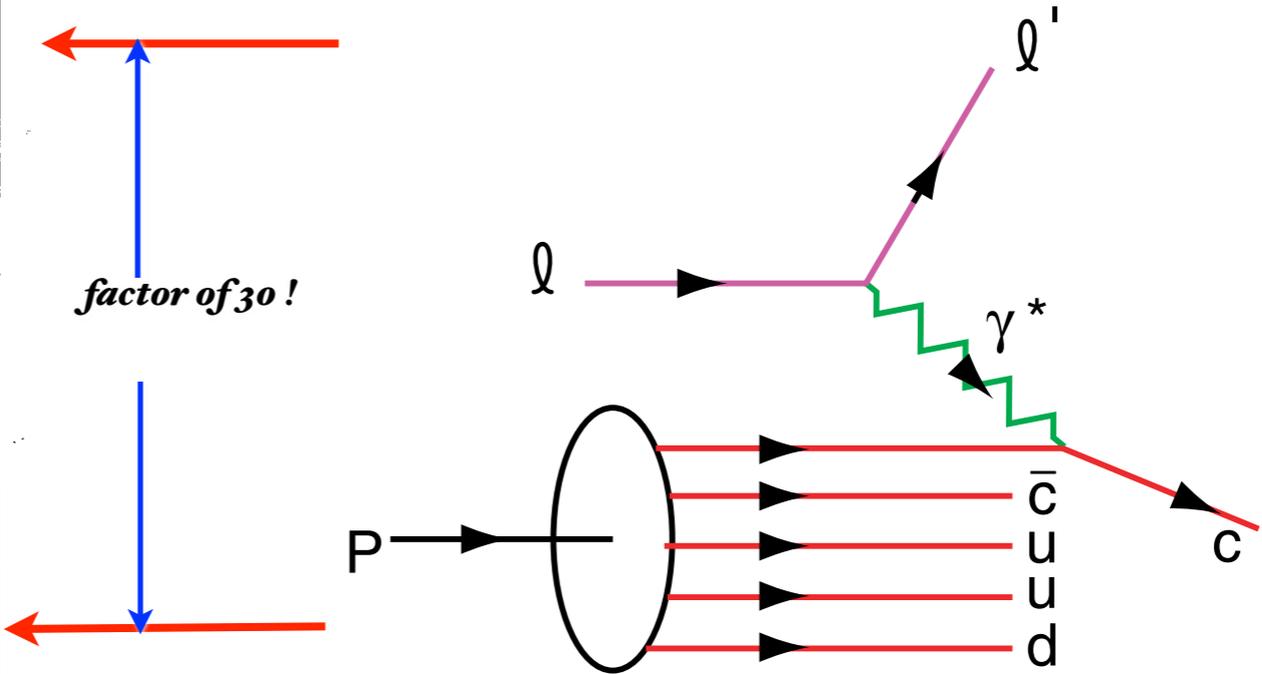
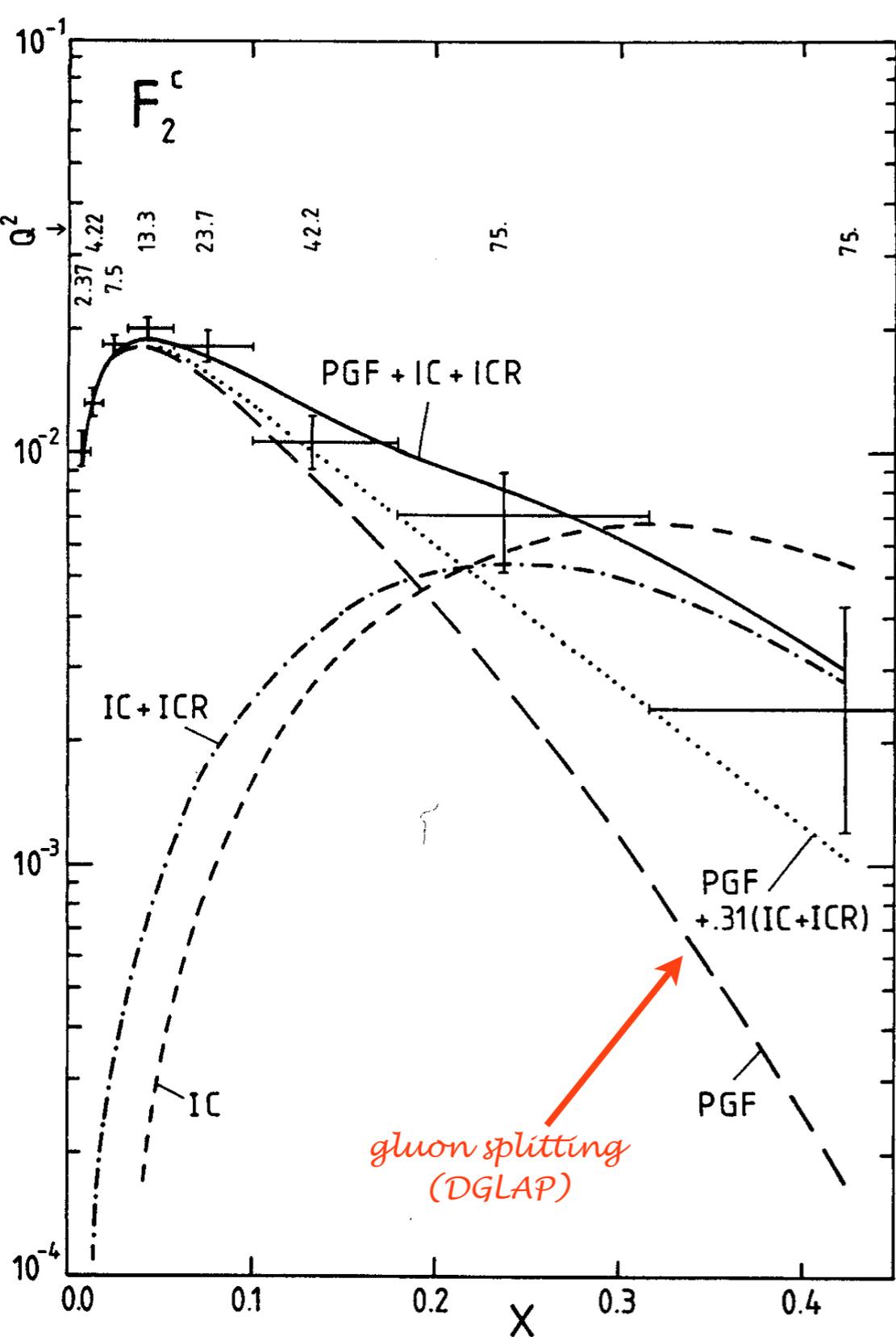
Relative to proton $\Delta y = y_H - y_p = \log \frac{x_H}{m_{\perp H}/m_p}$

Feynman: Correlations with parent proton $\Delta y < 2$

Measurement of Charm Structure Function

J. J. Aubert et al. [European Muon Collaboration], "Production Of Charmed Particles In 250-GeV Mu+ - Iron Interactions," Nucl. Phys. B 213, 31 (1983).

First Evidence for Intrinsic Charm Hoyer, Peterson, Sakai, sjb



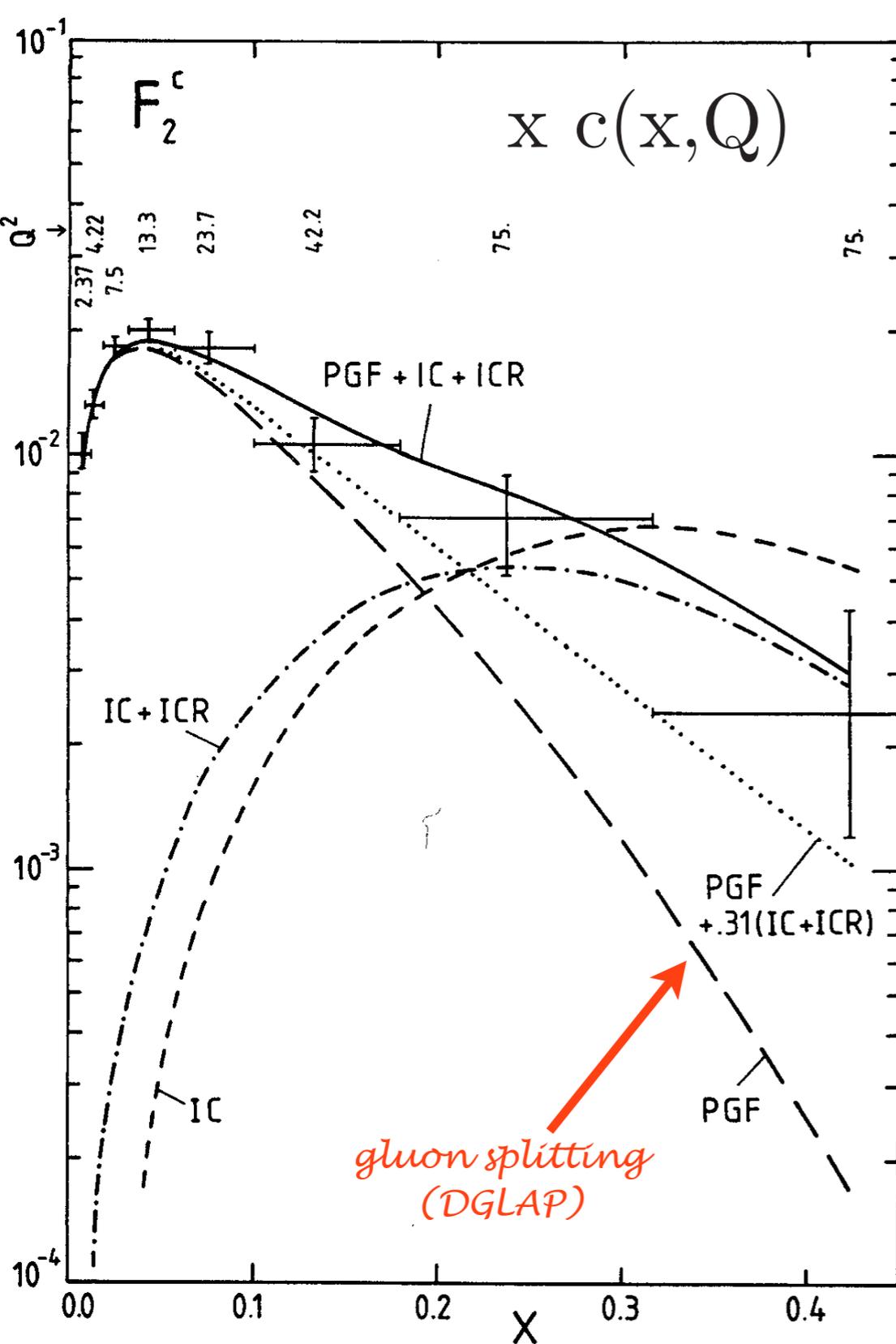
DGLAP / Photon-Gluon Fusion: factor of 30 too small

Two Components (separate evolution):

$$c(x, Q^2) = c(x, Q^2)_{\text{extrinsic}} + c(x, Q^2)_{\text{intrinsic}}$$

Measurement of Charm Structure Function!

J. J. Aubert et al. [European Muon Collaboration], "Production Of Charmed Particles In 250-GeV Mu+ - Iron Interactions," Nucl. Phys. B 213, 31 (1983).

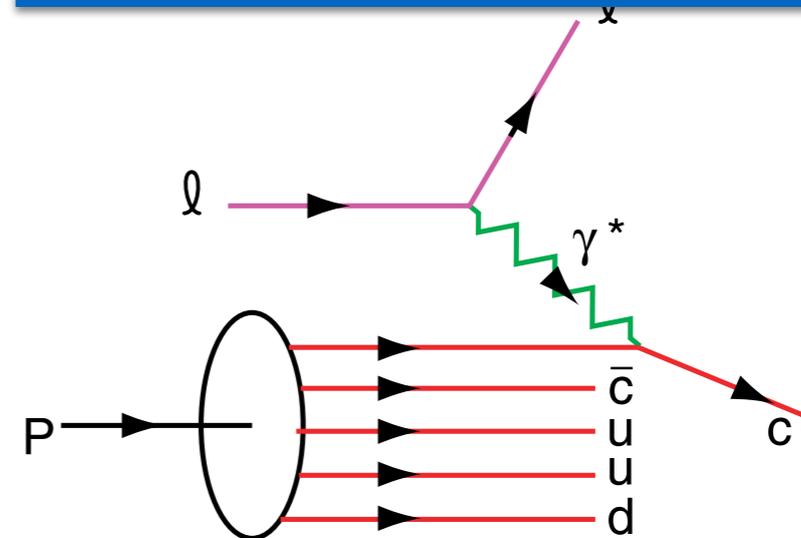


Evidence for Intrinsic Charm

$$\langle x_{c\bar{c}} \rangle_p \simeq 1\%$$

New Analysis:
 R.D. Ball, et al. [NNPDF Collaboration],
 "A Determination of the Charm Content
 of the Proton,"
 arXiv:1605.06515 [hep-ph].

factor of 30!



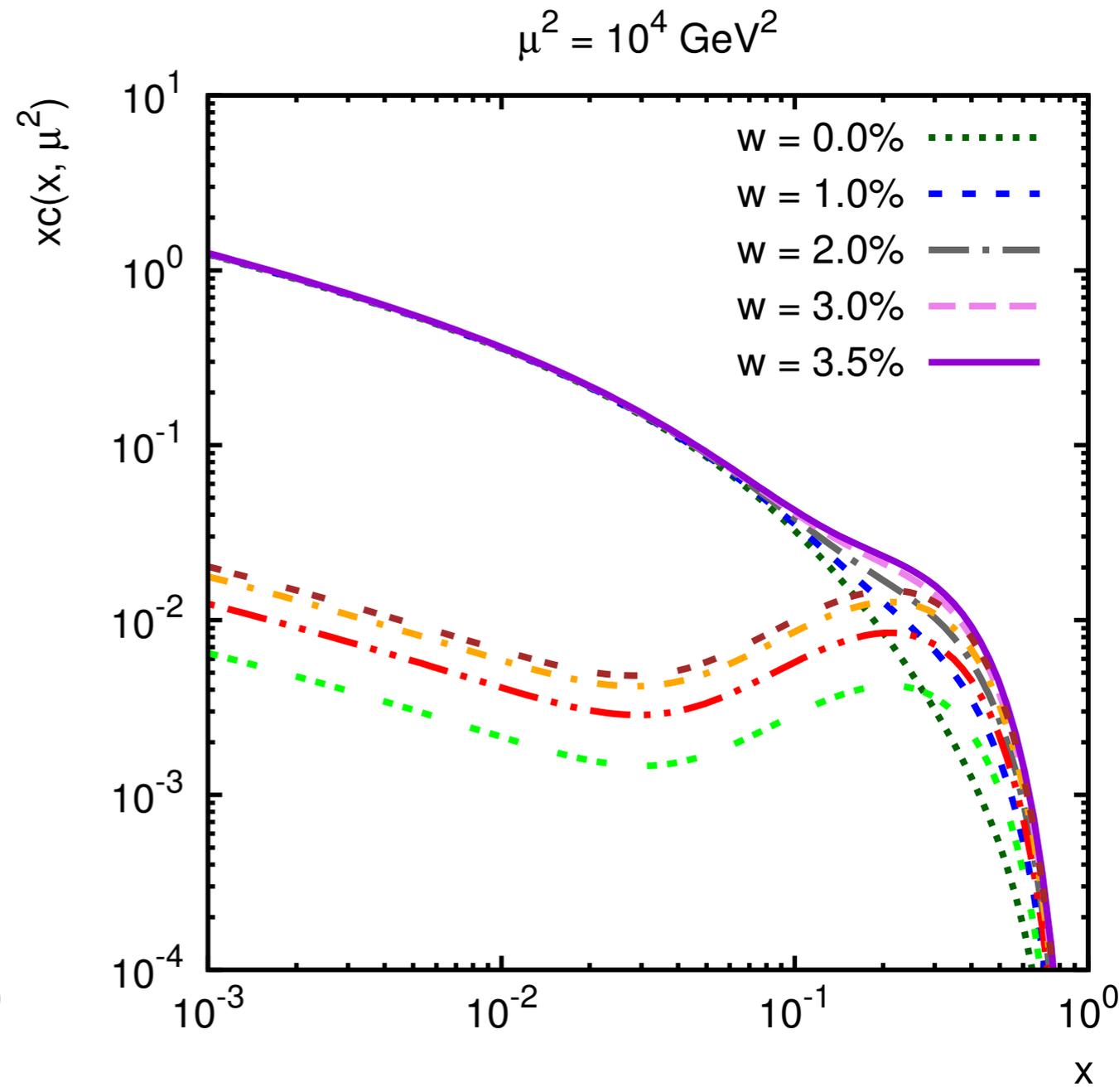
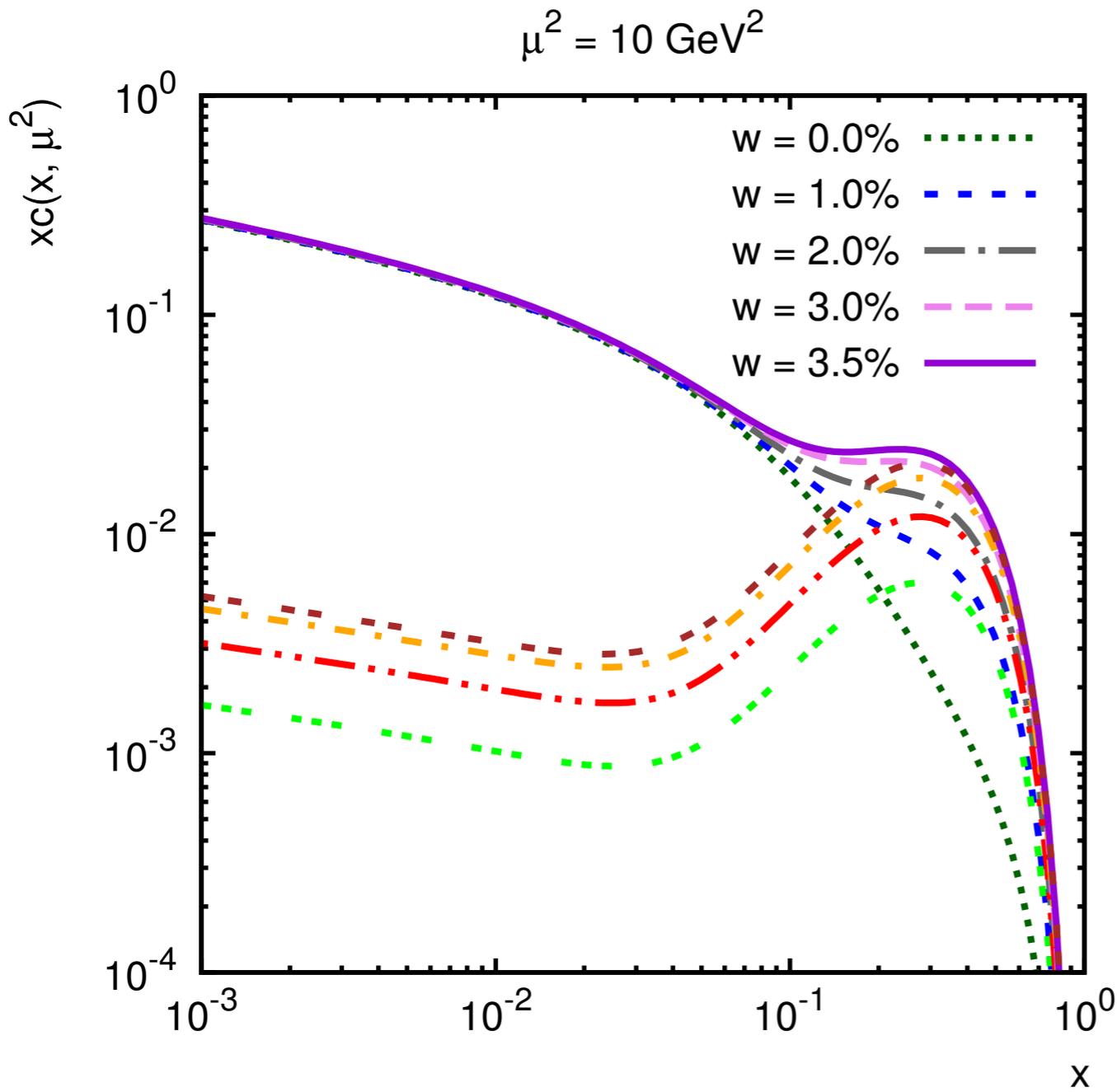
DGLAP / Photon-Gluon Fusion: factor of 30 too small

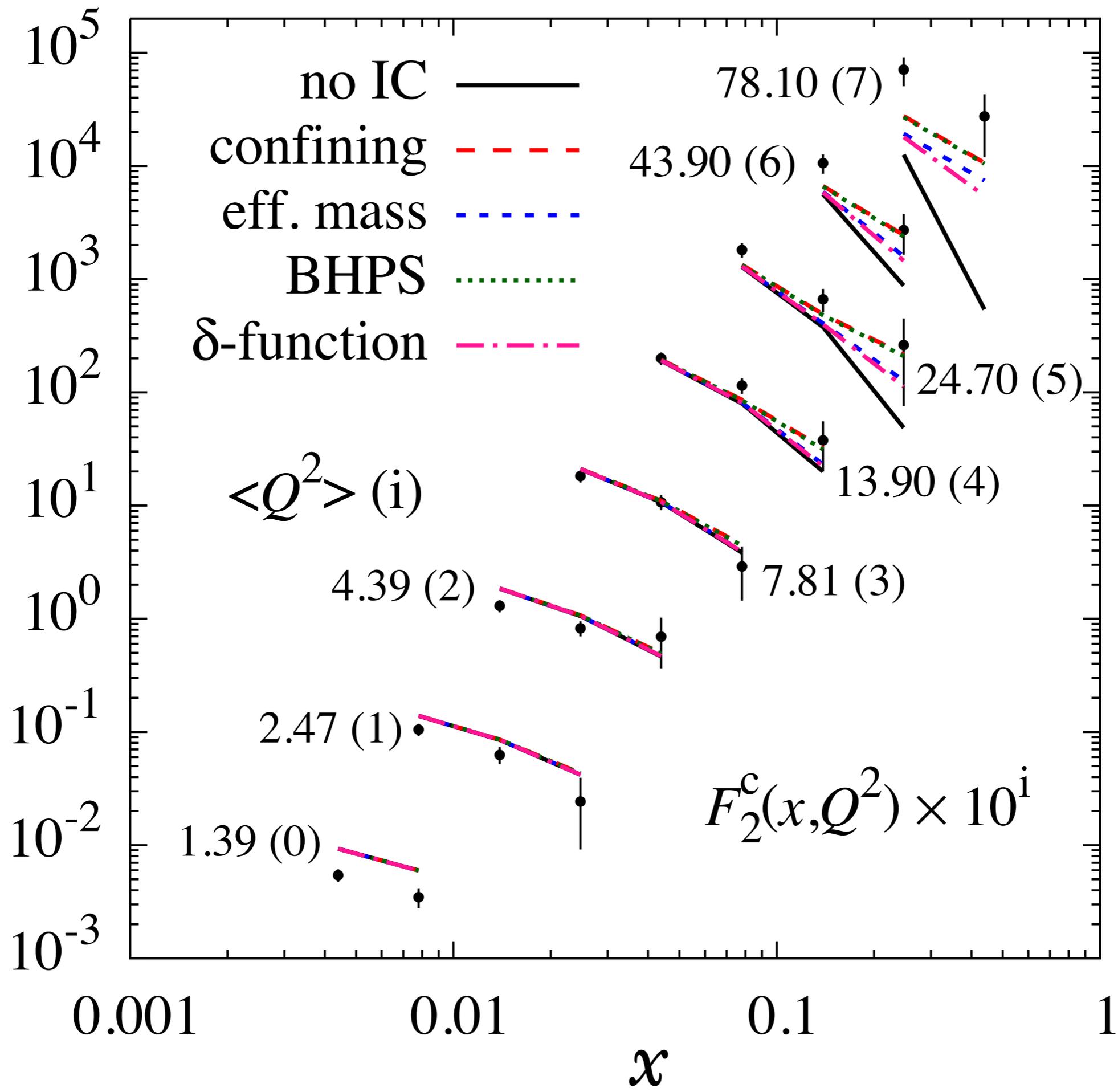
Two Components (separate evolution):

$$c(x, Q^2) = c(x, Q^2)_{\text{extrinsic}} + c(x, Q^2)_{\text{intrinsic}}$$

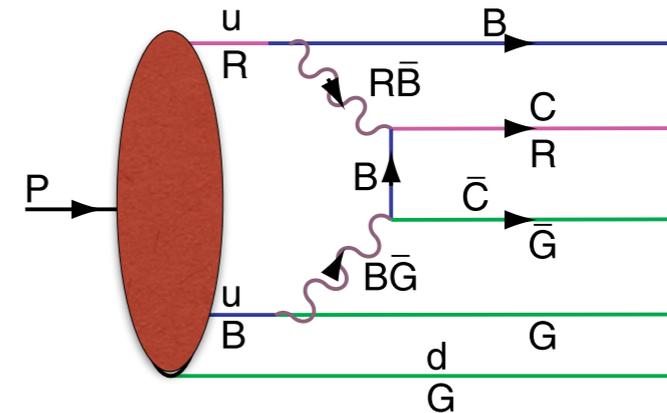
$$x c(x, Q)$$

x





Intrinsic Heavy-Quark Fock



- **Rigorous prediction of QCD, OPE**

- **Color-Octet Color-Octet Fock State**

- **Probability**

$$P_{Q\bar{Q}} \propto \frac{1}{M_Q^2} \quad P_{Q\bar{Q}Q\bar{Q}} \sim \alpha_s^2 P_{Q\bar{Q}} \quad P_{c\bar{c}/p} \simeq 1\%$$

- **Large Effect at high x**

- **Greatly increases kinematics of colliders such as Higgs production (Kopeliovich, Schmidt, Soffer, sjb)**

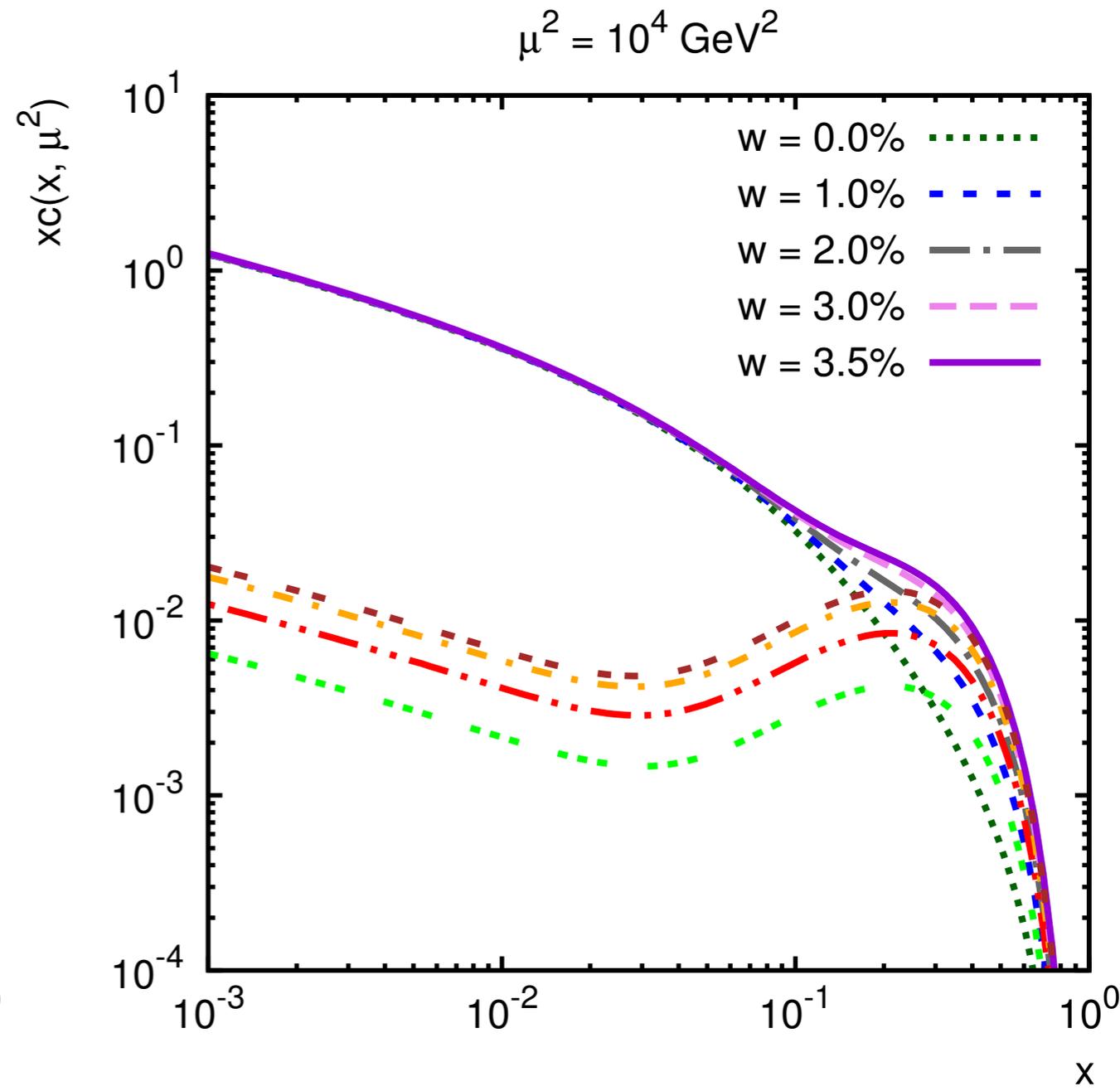
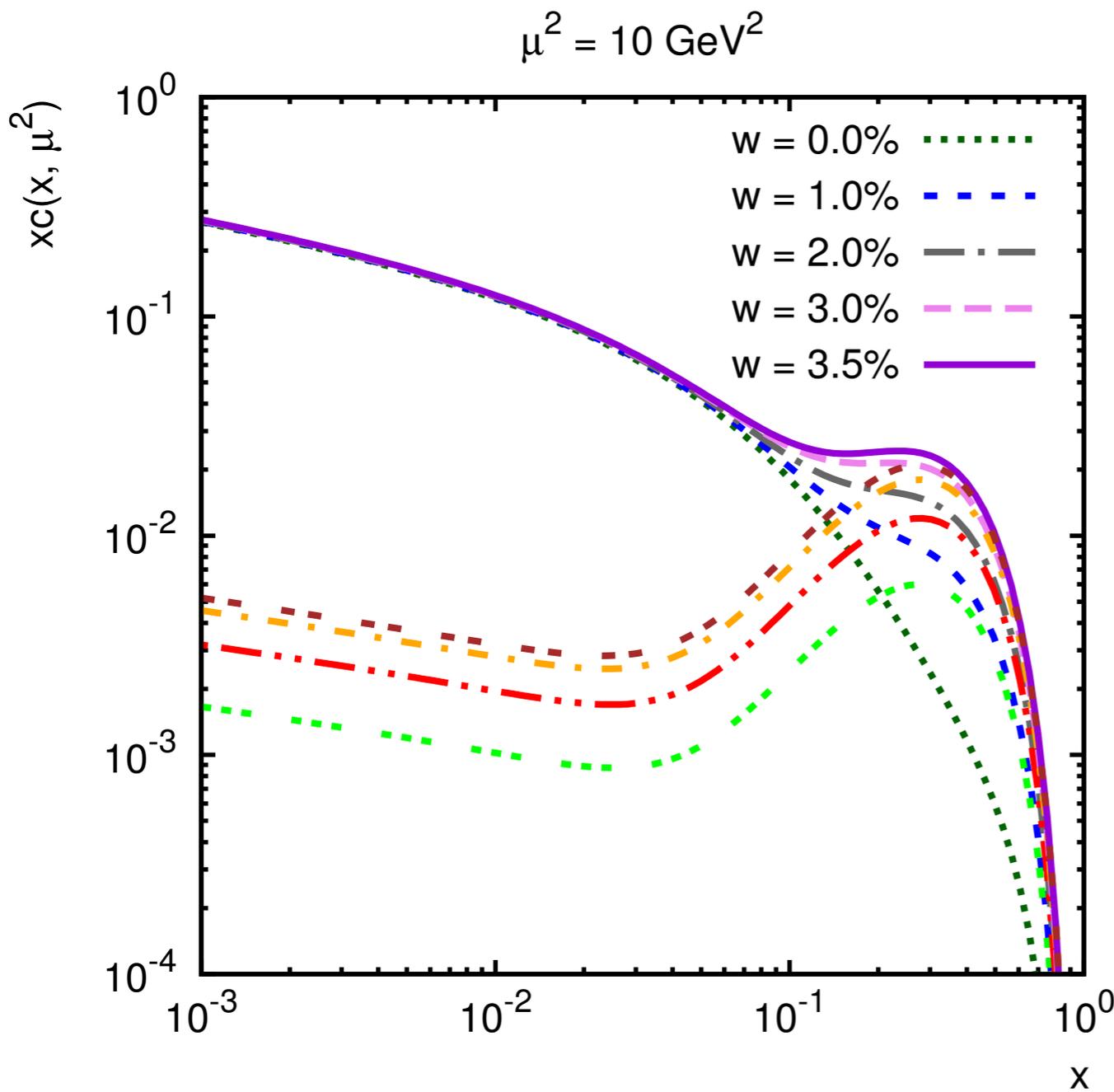
- **Underestimated in conventional parameterizations of heavy quark distributions (Pumplin, Tung)**

- **Many EIC tests**

OPE: Collins, S. Ellis, Gunion, Mueller, sjb
 Franz, Goecke, M. Polyakov,

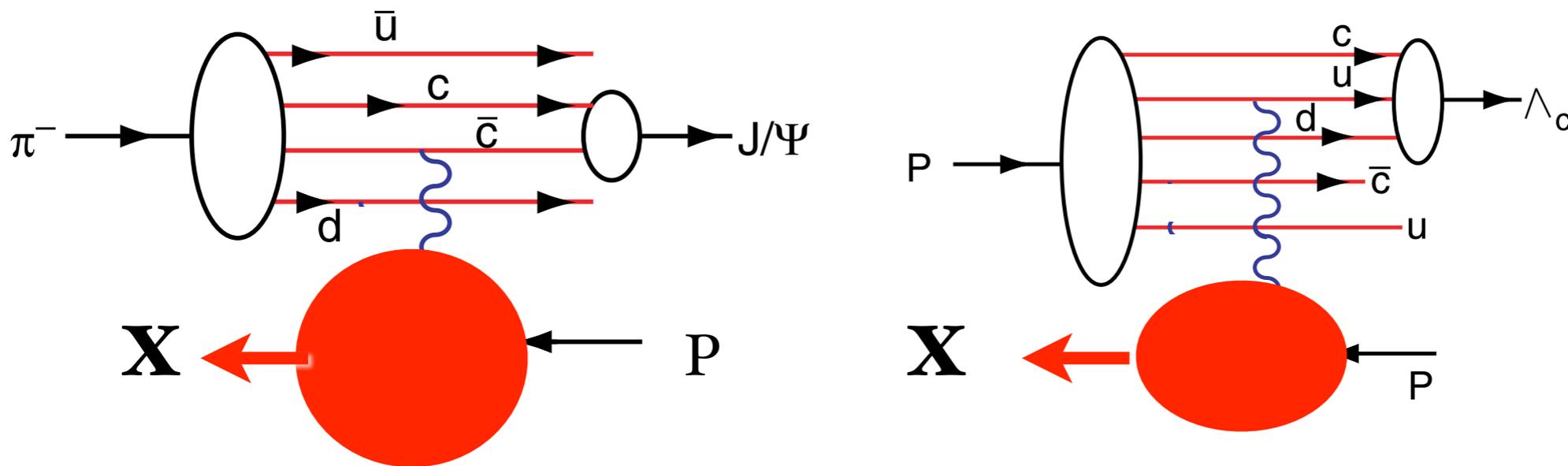
$xc(x, \mu^2)$

x



$$w = P_{c\bar{c}}^{\text{intrinsic}}$$

Coalescence of comovers produces high x_F heavy hadrons

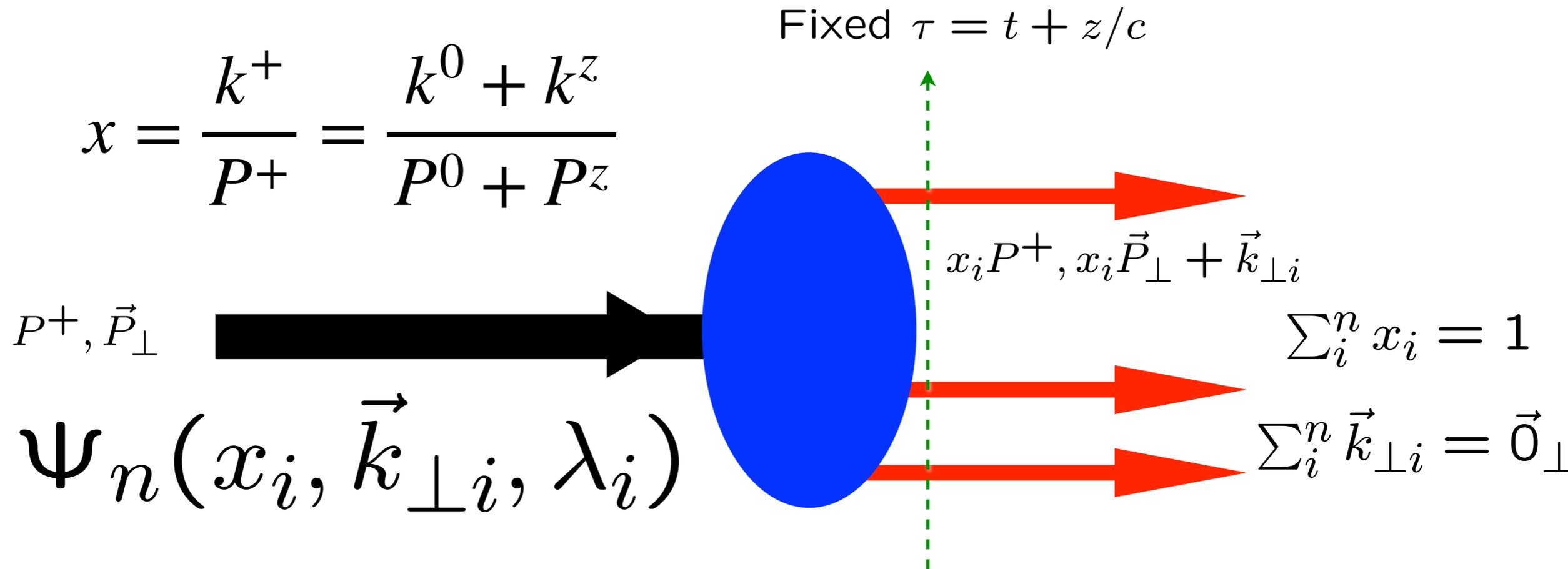


Spectator counting rules

$$\frac{dN}{dx_F} \propto (1 - x_F)^{2n_{spect} - 1}$$

Coalescence of Comoving Charm and Valence Quarks
Produce J/ψ , Λ_c and other Charm Hadrons at High x_F

Light-Front Wavefunctions: rigorous representation of composite systems in quantum field theory



Invariant under boosts! Independent of P^μ

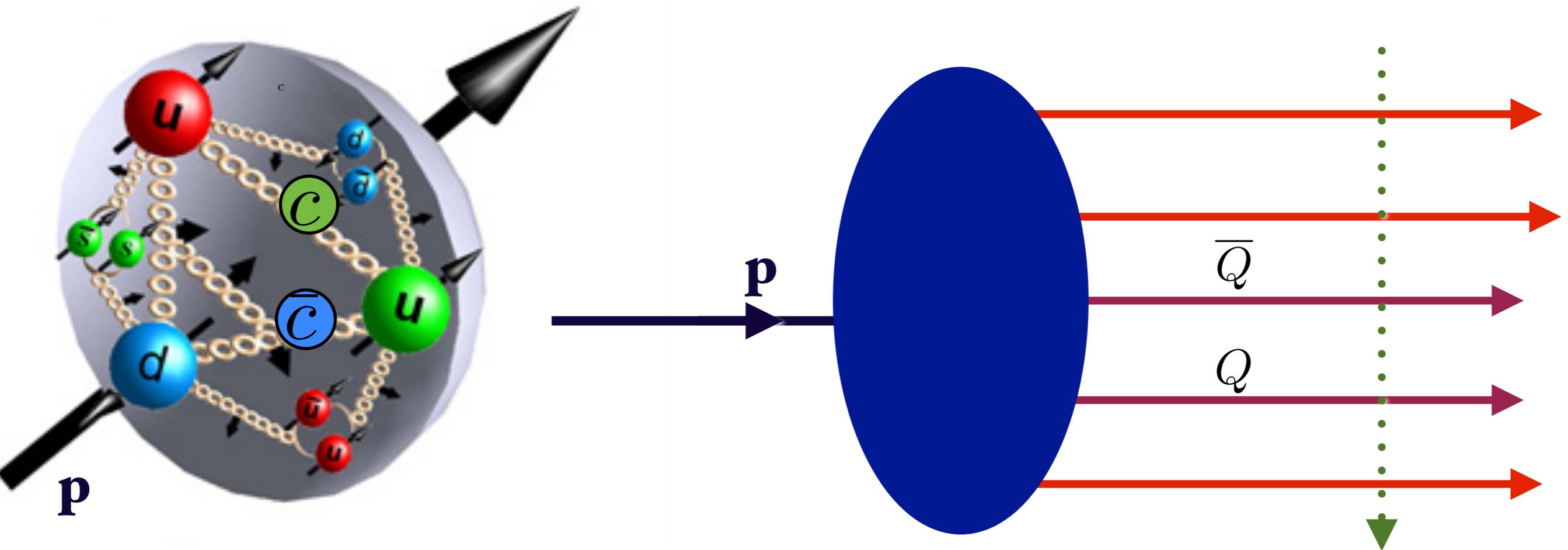
Light-Front Wavefunctions: Off-Shell in Invariant Mass

$$\mathcal{M}_n^2 = \left(\sum_{i=1}^n k^\mu \right)^2 = \sum_{i=1}^n \frac{k_{\perp i}^2 + m_i^2}{x_i} \quad M^2 - \mathcal{M}_n^2 < 0$$

Color confinement potential from AdS/QCD

$$U(\zeta^2) = \kappa^4 \zeta^2 = \kappa^4 b_{\perp}^2 x(1-x)$$

Fixed $\tau = t + z/c$



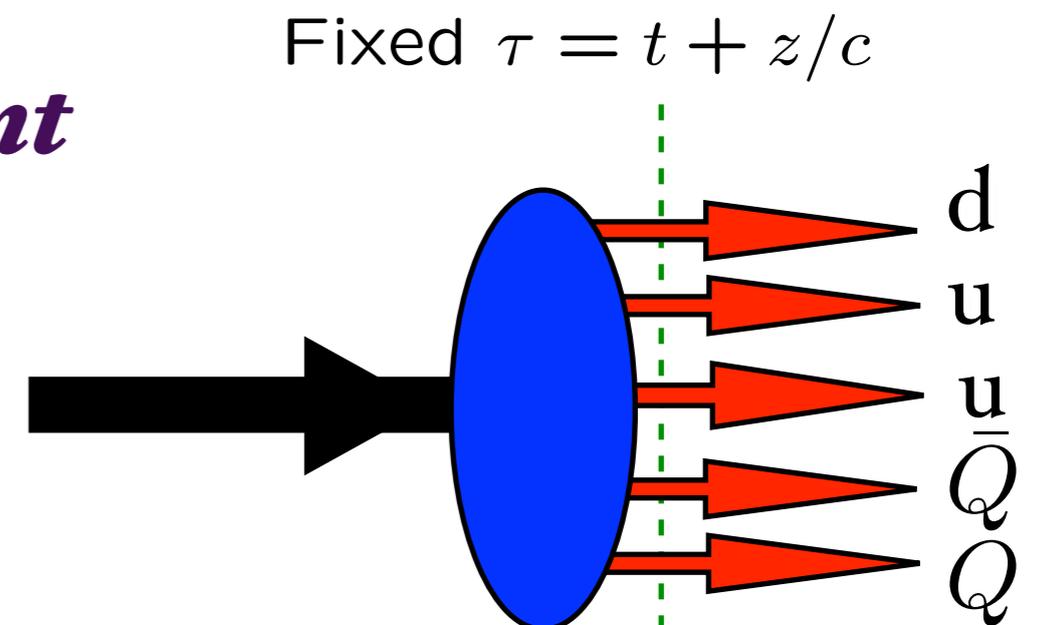
$$\psi_n(\vec{k}_{\perp i}, x_i) \propto \frac{1}{\kappa^{n-1}} e^{-\mathcal{M}_n^2/2\kappa^2} \prod_{j=1}^n \frac{1}{\sqrt{x_j}}$$

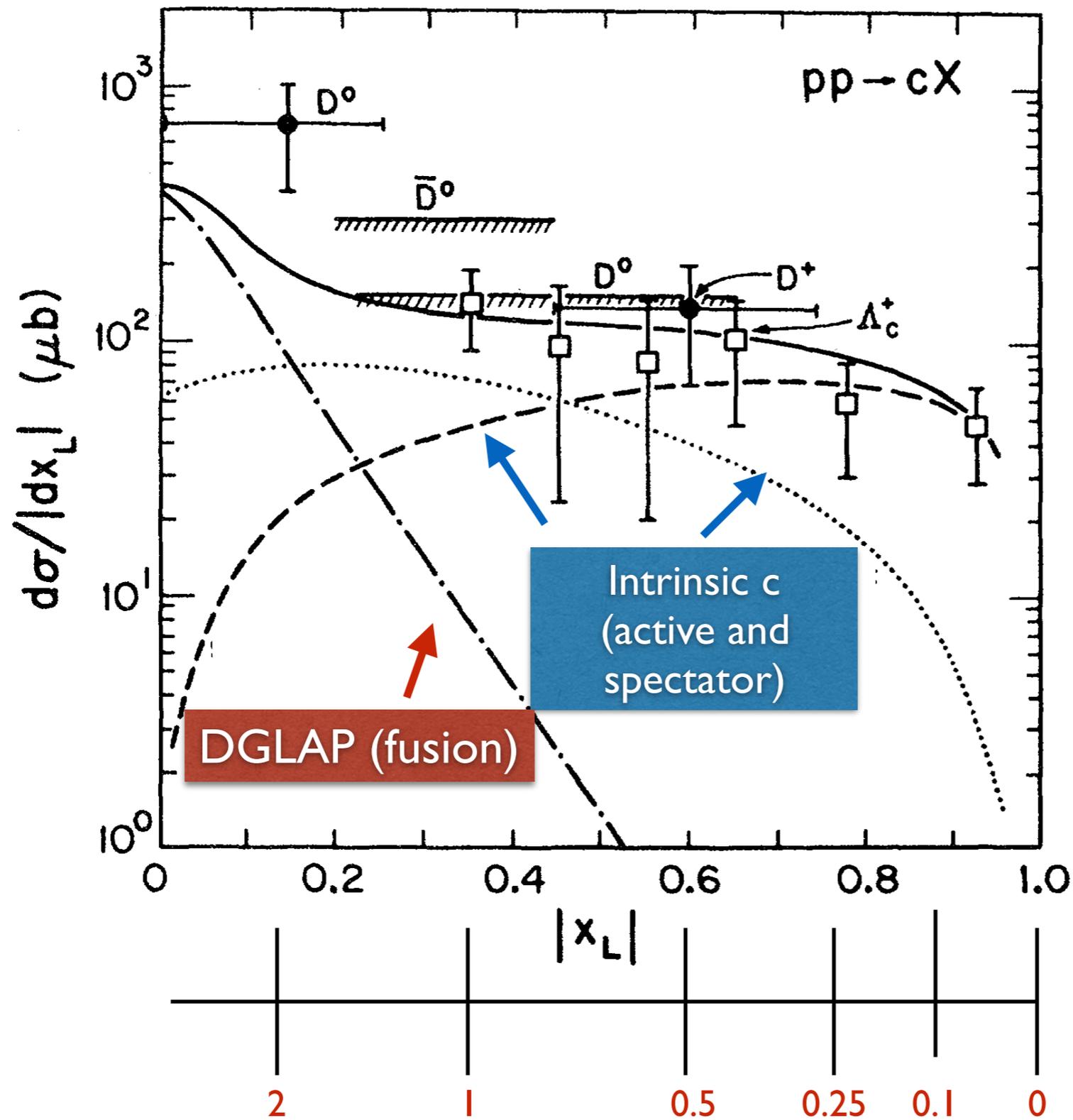
$$\mathcal{M}_n^2 = \sum_{i=1}^n \left(\frac{k_{\perp}^2 + m^2}{x} \right)_i$$

Minimally Off-Shell

Properties of Non-Perturbative Five-Quark Fock-State

- *Dominant configuration: same rapidity*
- *Heavy quarks have most momentum*
- *Correlated with proton quantum numbers*
- *Duality with meson-baryon channels*
- *strangeness asymmetry at $x > 0.1$*
- *Maximally energy efficient*

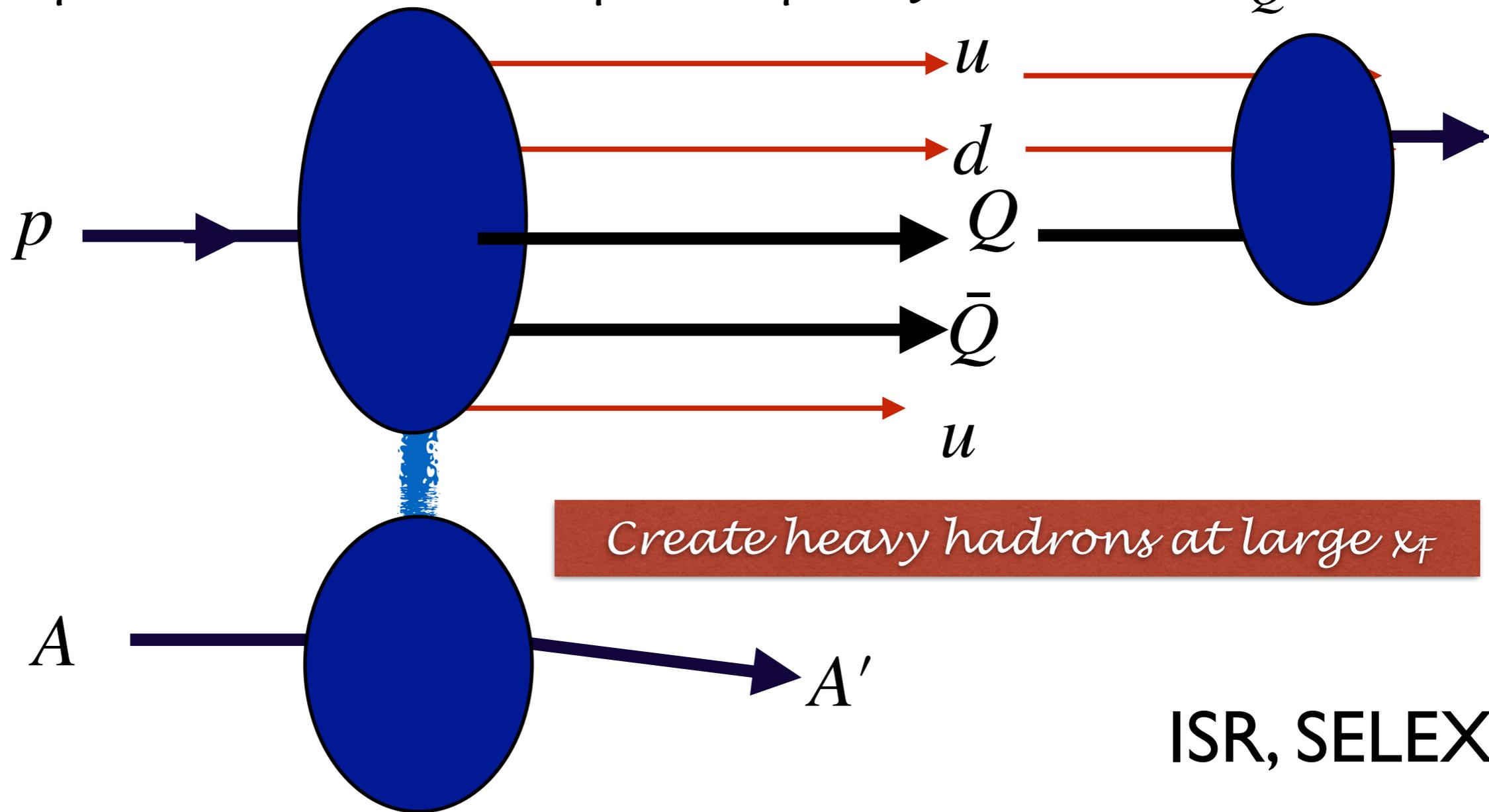




$$\Delta y = \log x$$

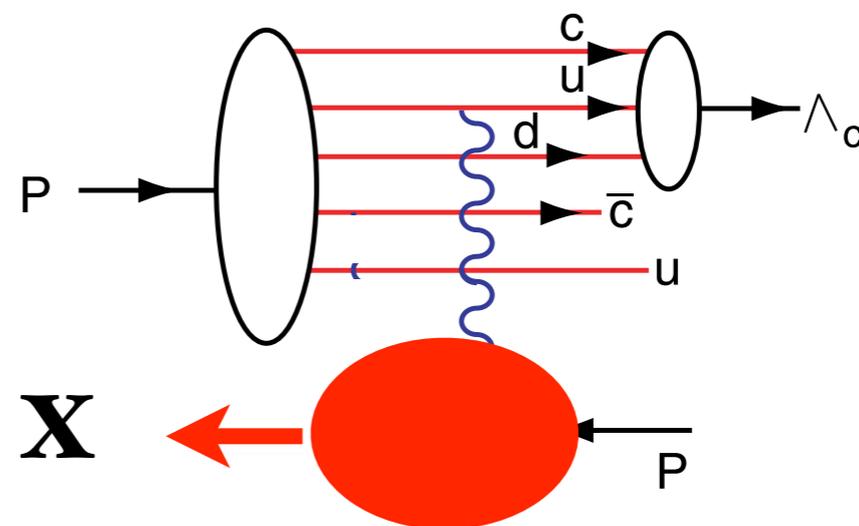
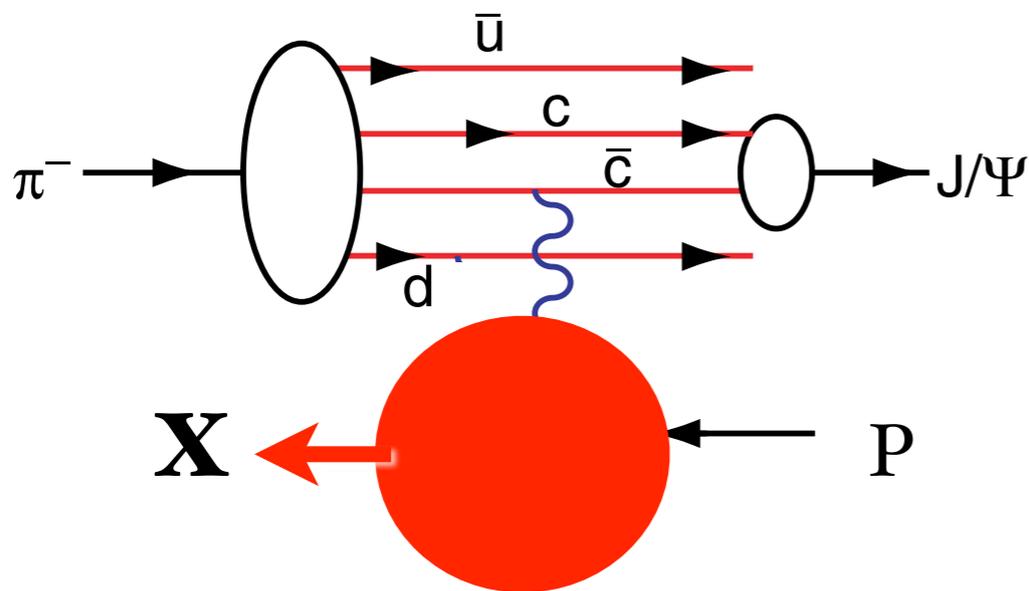
Novel Effects Derived from Light-Front Wavefunctions

Intrinsic quarks coalesce at equal rapidity to make $\Lambda_Q(udQ)$



ISR, SELEX

Coalescence of comovers produces high- x_F heavy hadrons



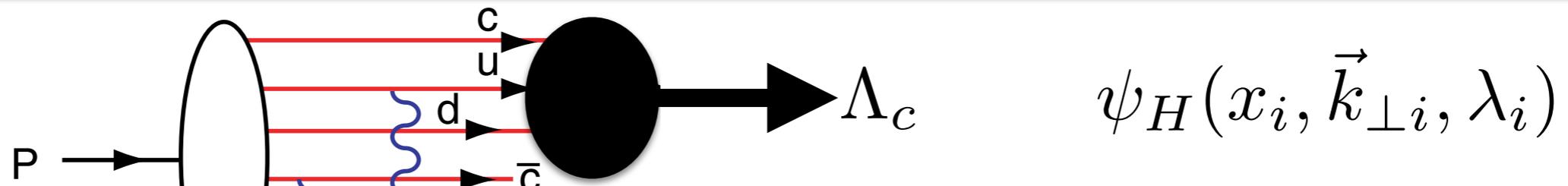
Spectator counting rules

$$\frac{dN}{dx_F} \propto (1 - x_F)^{2n_{spect} - 1}$$

Coalescence of Comoving Charm and Valence Quarks
Produce J/ψ , Λ_c and other Charm Hadrons at High x_F

Coalescence of comovers produces high x_F heavy hadrons

High x_F hadrons combine most of the comovers, fewest spectators



LFWF maximum at equal rapidity

maximum at minimal invariant mass

X \rightarrow *Asymmetries of leading hadrons*

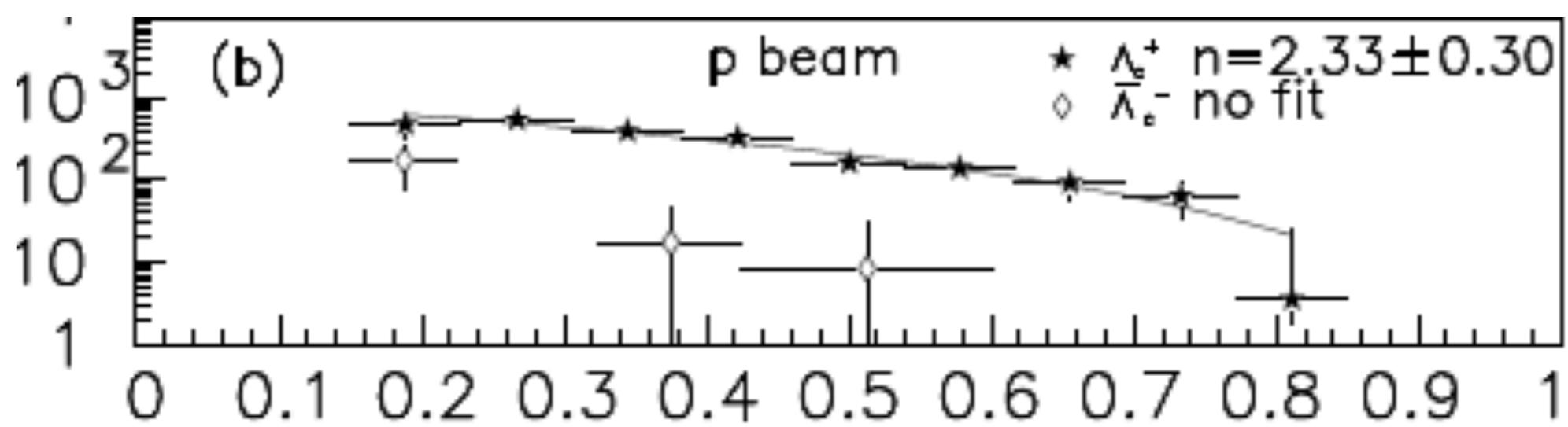
Spectator counting rules

$$\frac{dN}{dx_F} \propto (1 - x_F)^{2n_{spect} - 1}$$

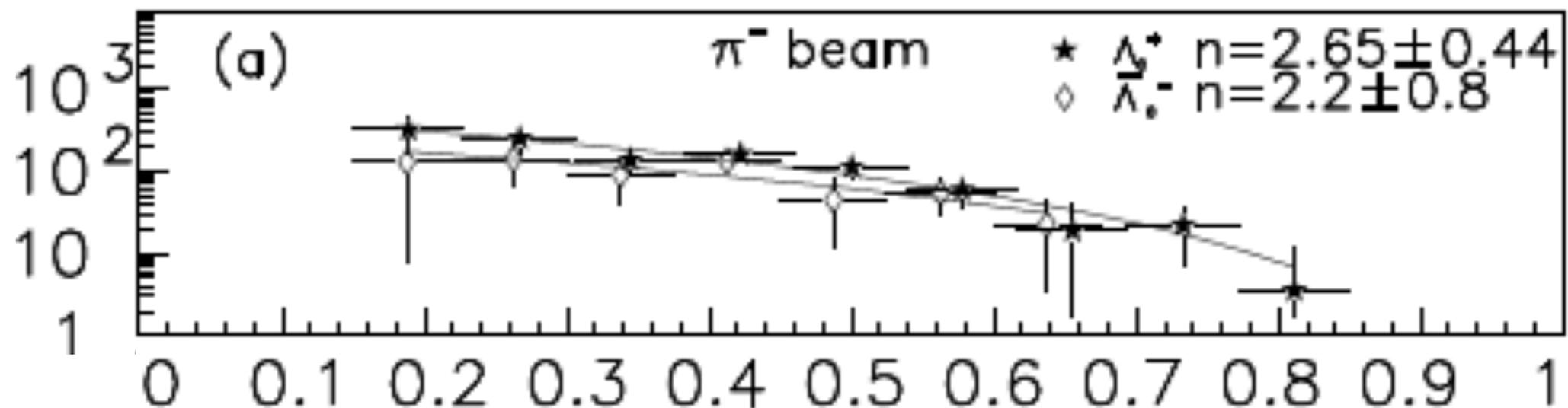
Coalescence of Comoving Charm and Valence Quarks
Produce J/ψ , Λ_c and other Charm Hadrons at High x_F

Vogt, sjb

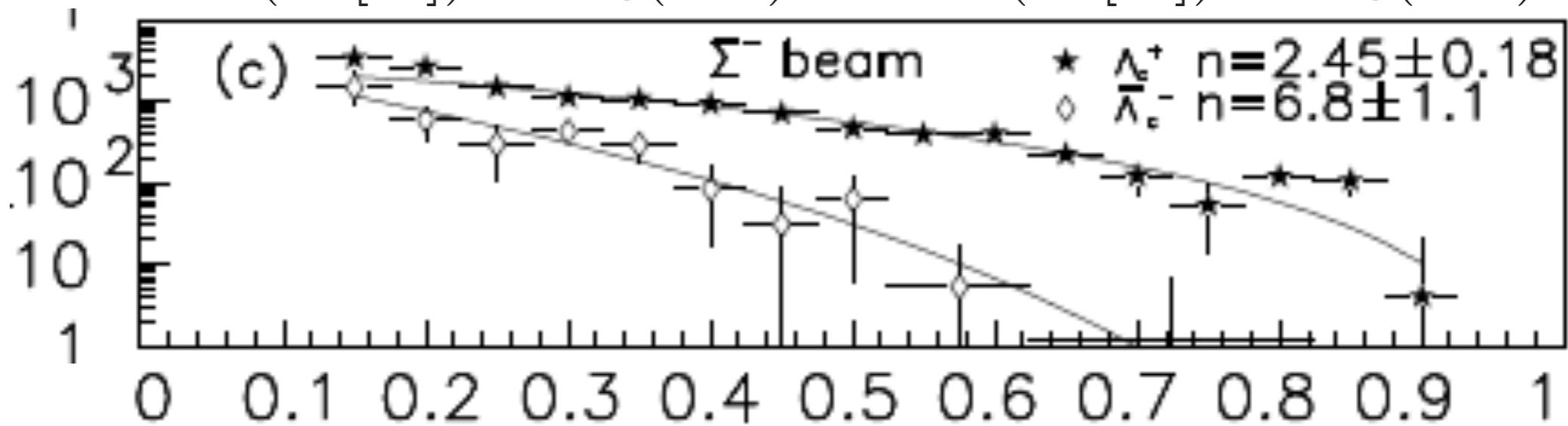
SELEX



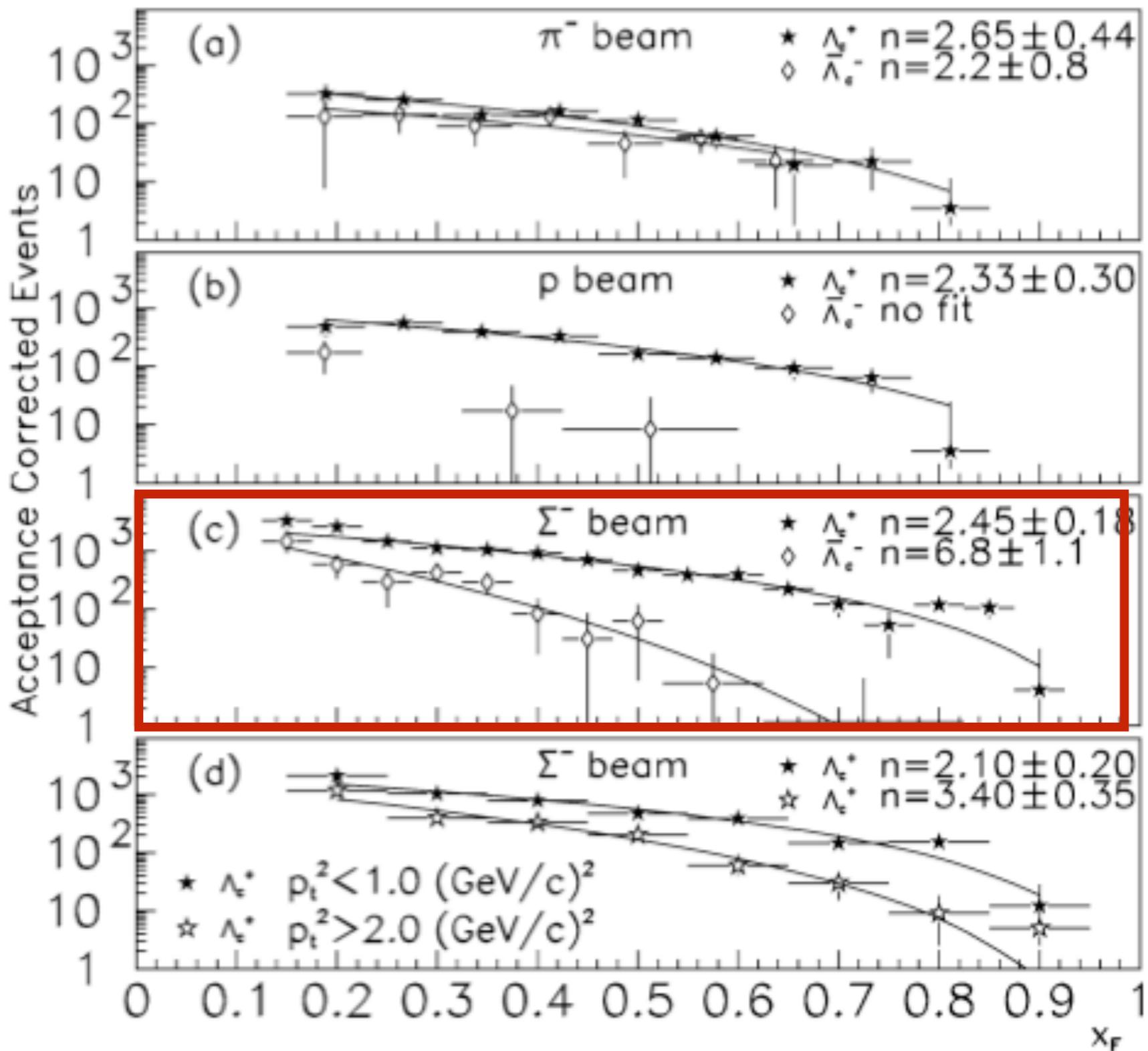
$p(uud[c\bar{c}]) \rightarrow \Lambda_c(udc)$ vs. $p(uud[c\bar{c}]) \rightarrow \bar{\Lambda}_c(\bar{u}\bar{d}\bar{c})$



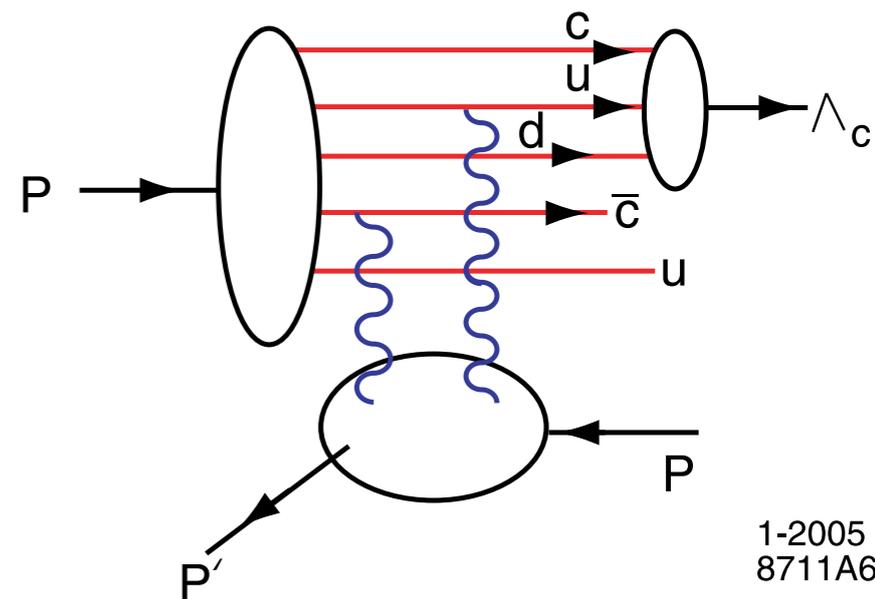
$\pi^-(\bar{u}d[c\bar{c}]) \rightarrow \Lambda_c(udc)$ vs. $\pi^-(\bar{u}d[c\bar{c}]) \rightarrow \bar{\Lambda}_c(\bar{u}\bar{d}\bar{c})$



$\Sigma^-(uds[c\bar{c}]) \rightarrow \Lambda_c(udc)$ vs. $\Sigma^-(uds[c\bar{c}]) \rightarrow \bar{\Lambda}_c(\bar{u}\bar{d}\bar{c})$



SELEX



$$p(udc\bar{c})$$

$$\rightarrow \Lambda_c(cud)$$

$$n_s = 2$$

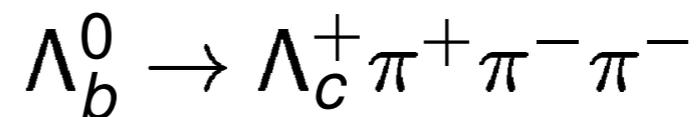
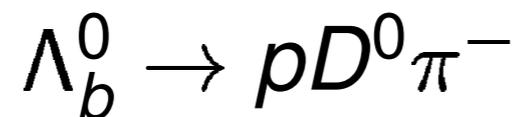
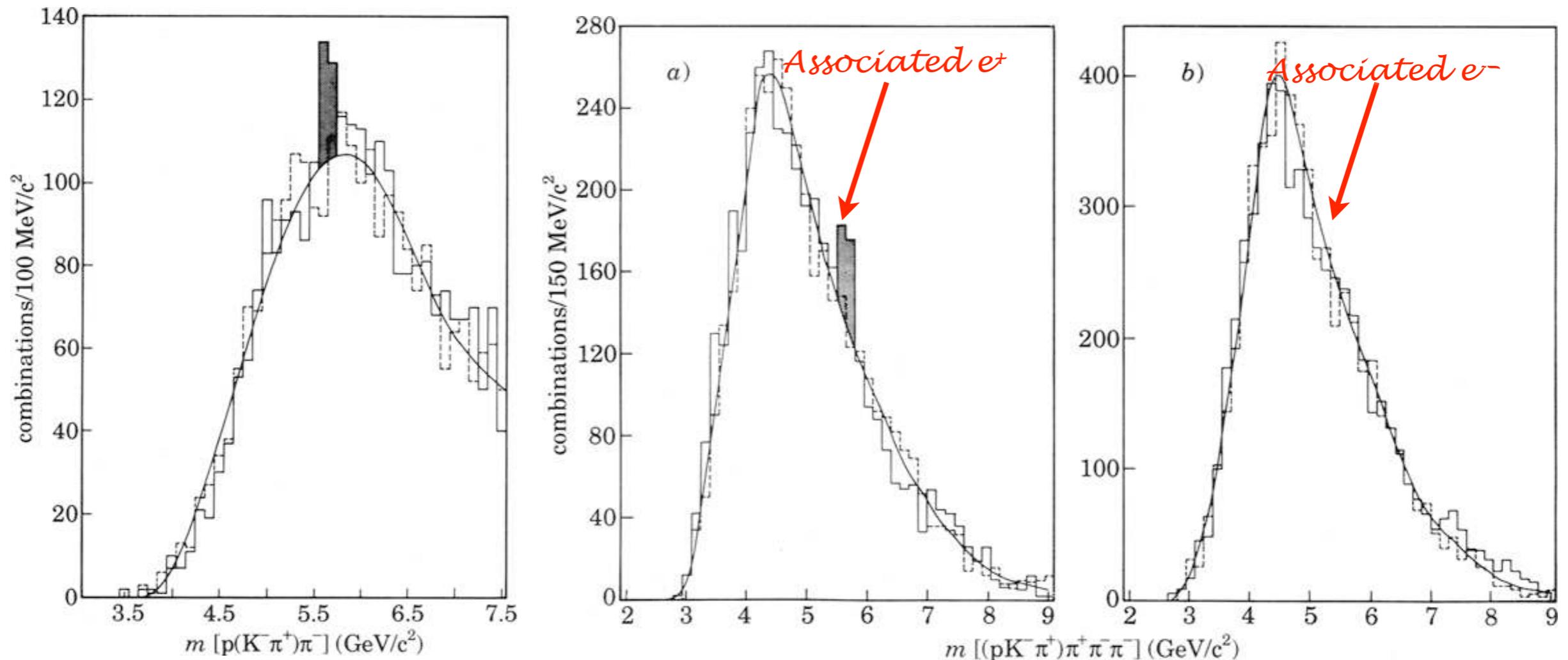
**Phase space gives
minimum power p**

$$(1 - x_F)^p, p = n_s - 1$$

$$\Sigma^- (sddc\bar{c})A \rightarrow \Lambda_c(cdu)X \text{ vs. } \Sigma^- (sddc\bar{c})A \rightarrow \bar{\Lambda}_c(\bar{c}d\bar{u})X$$

$$pp \rightarrow \Lambda_b(bud)B(\bar{b}q)X \text{ at large } x_F \quad \sqrt{s} = 63 \text{ GeV}$$

CERN-ISR R422 (Split Field Magnet), 1988/1991



Il Nuovo Cimento 104, 1787

Discovery of Λ_b ; Associated Production; Evidence for Intrinsic $b\bar{b}$

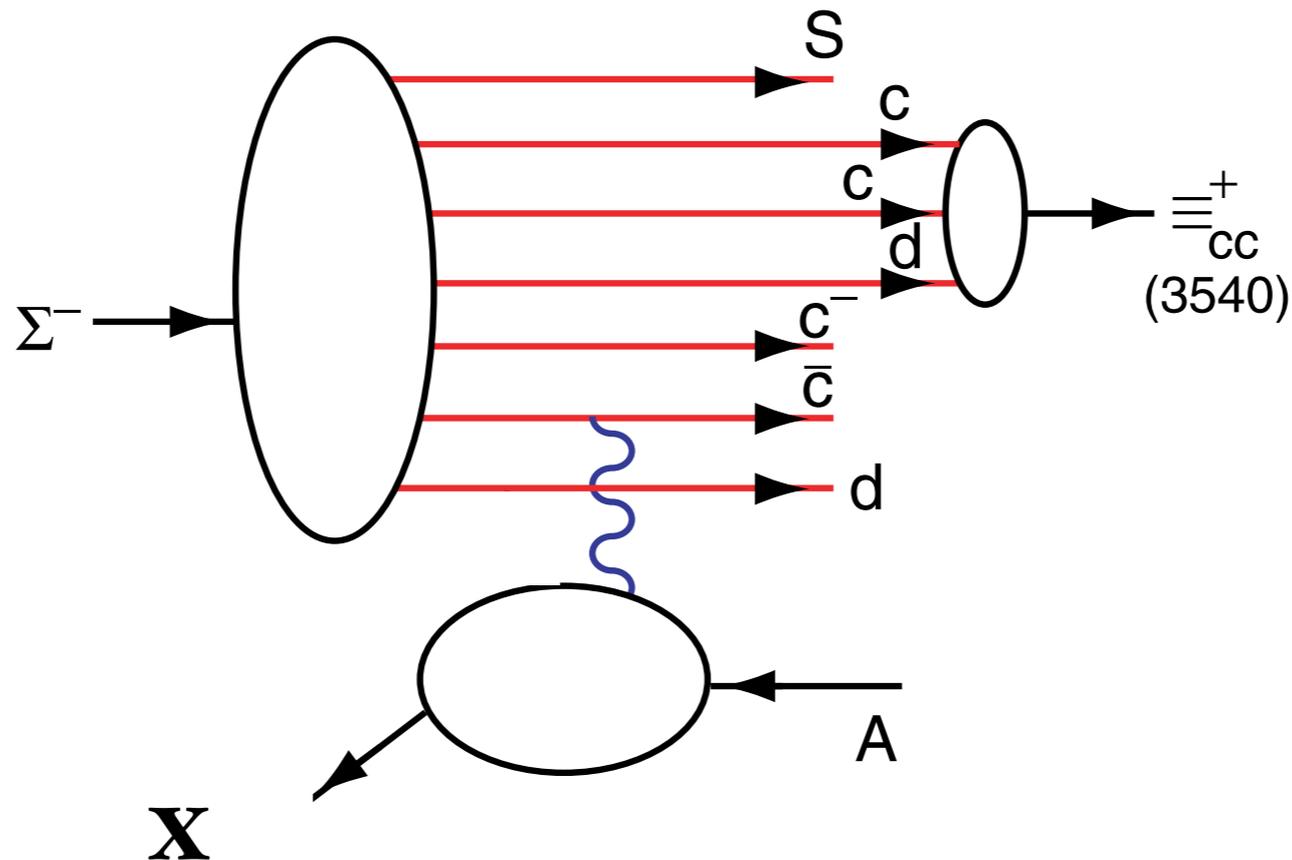
Create Λ_b at rest at LHCb at $\sqrt{s} = \sqrt{13000} = 115 \text{ GeV}$

Λ_b^0 MASS

$m_{\Lambda_b^0}$



VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
5619.51 ± 0.23	OUR AVERAGE			
5619.30 ±0.34	1	AAIJ	2014AA	LHCB $p p$ at 7 TeV
5620.15 ±0.31 ±0.47	2	AALTONEN	2014B	CDF $p \bar{p}$ at 1.96 TeV
5619.7 ±0.7 ±1.1	2	AAD	2013U	ATLS $p p$ at 7 TeV
5619.44 ±0.13 ±0.38	2	AAIJ	2013AV	LHCB $p p$ at 7 TeV
5621 ±4 ±3	3	ABE	1997B	CDF $p \bar{p}$ at 1.8 TeV
5668 ±16 ±8	4	ABREU	1996N	DLPH $e^+ e^- \rightarrow Z$
5614 ±21 ±4	4	BUSKULIC	1996L	ALEP $e^+ e^- \rightarrow Z$
*** We do not use the following data for averages, fits, limits, etc ***				
5619.19 ±0.70 ±0.30	2	AAIJ	2012E	LHCB Repl. by AAIJ 2013AV
5619.7 ±1.2 ±1.2	5	ACOSTA	2006	CDF Repl. by AALTONEN 2014B
not seen	6	ABE	1993B	CDF Repl. by ABE 1997B
5640 ±50 ±30	16	ALBAJAR	1991E	UA1 $p \bar{p}$ 630 GeV
5640 $^{+100}_{-210}$	52	BARI	1991	SFM $\Lambda_b^0 \rightarrow p D^0 \pi^-$
5650 $^{+150}_{-200}$	90	BARI	1991	SFM $\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^+ \pi^- \pi^-$



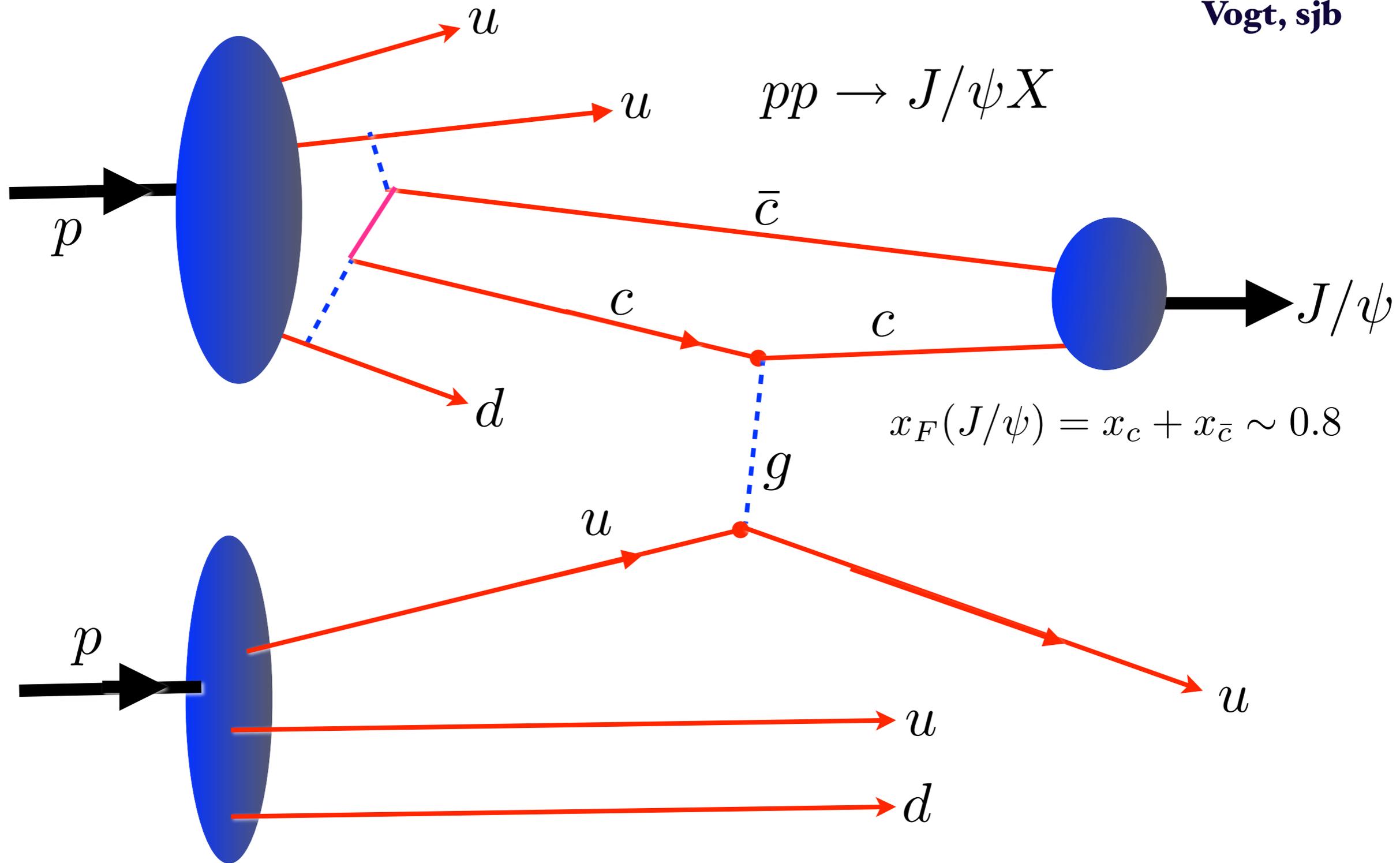
Production of a Double-Charm Baryon

SELEX high x_F $\langle x_F \rangle = 0.33$

Intrinsic Heavy Quark Contribution to Quarkonium Hadroproduction at High x_F

Lansberg, sjb

Vogt, sjb



Maximal Wavefunction Strength at Minimal Invariant Mass : Equal Rapidity

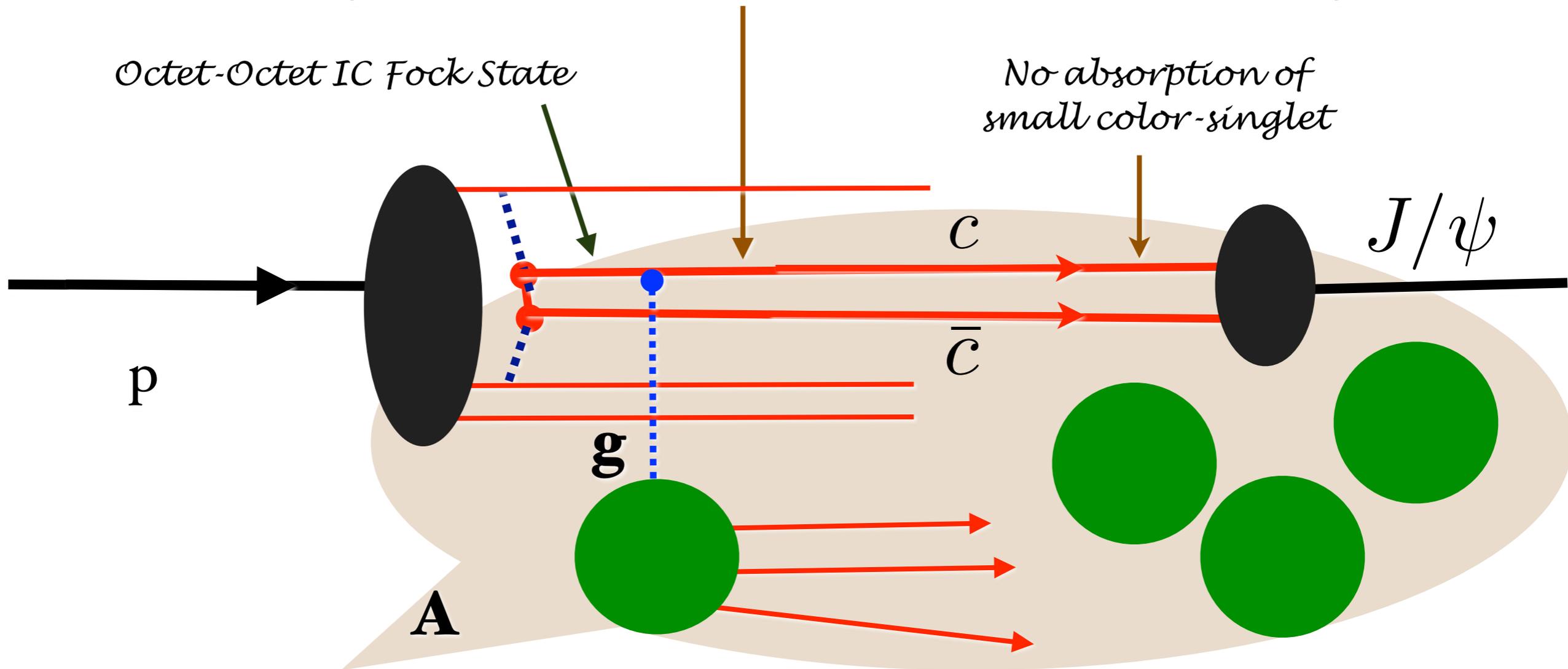
$$x_i \propto \frac{m_{\perp i}}{\sum_j m_{\perp j}}$$

High x_F

*Color-Opaque IC Fock state
interacts on nuclear front surface*

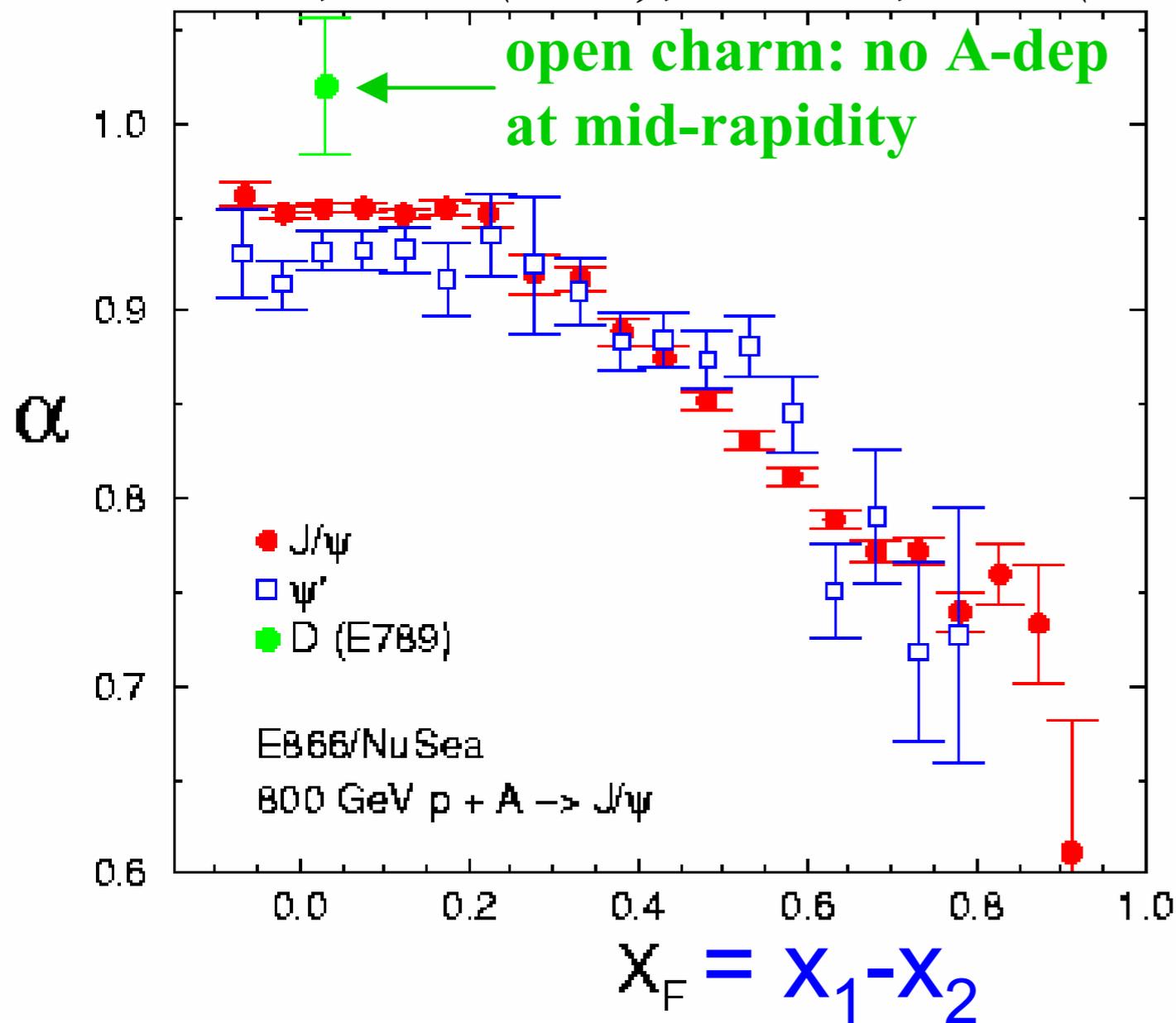
**Kopeliovich,
Schmidt, Soffer, sjb**

Scattering on front-face nucleon produces color-singlet $c\bar{c}$ pair



$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X) = A^{2/3} \times \frac{d\sigma}{dx_F}(pN \rightarrow J/\psi X)$$

800 GeV p-A (FNAL) $\sigma_A = \sigma_p * A^\alpha$
PRL 84, 3256 (2000); PRL 72, 2542 (1994)



$$\frac{d\sigma}{dx_F} (pA \rightarrow J/\psi X)$$

Remarkably Strong Nuclear Dependence for Fast Charmonium

Violation of PQCD Factorization

Violation of factorization in charm hadroproduction.

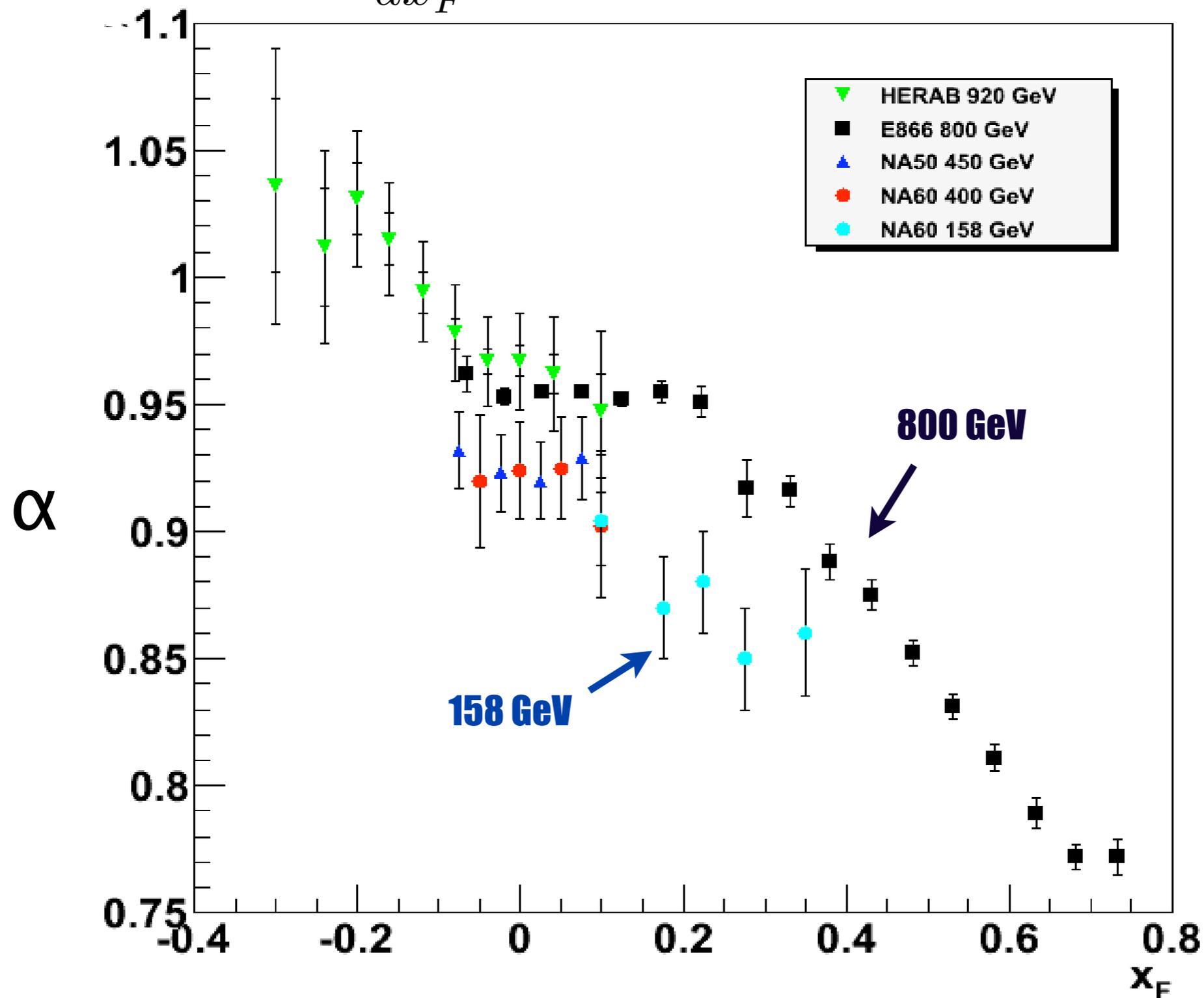
[P. Hoyer](#), [M. Vanttinen](#) (Helsinki U.), [U. Sukhatme](#) (Illinois U., Chicago) . HU-TFT-90-14, May 1990. 7pp.

Published in Phys.Lett.B246:217-220,1990

IC Explains large excess of quarkonia at large x_F , A-dependence

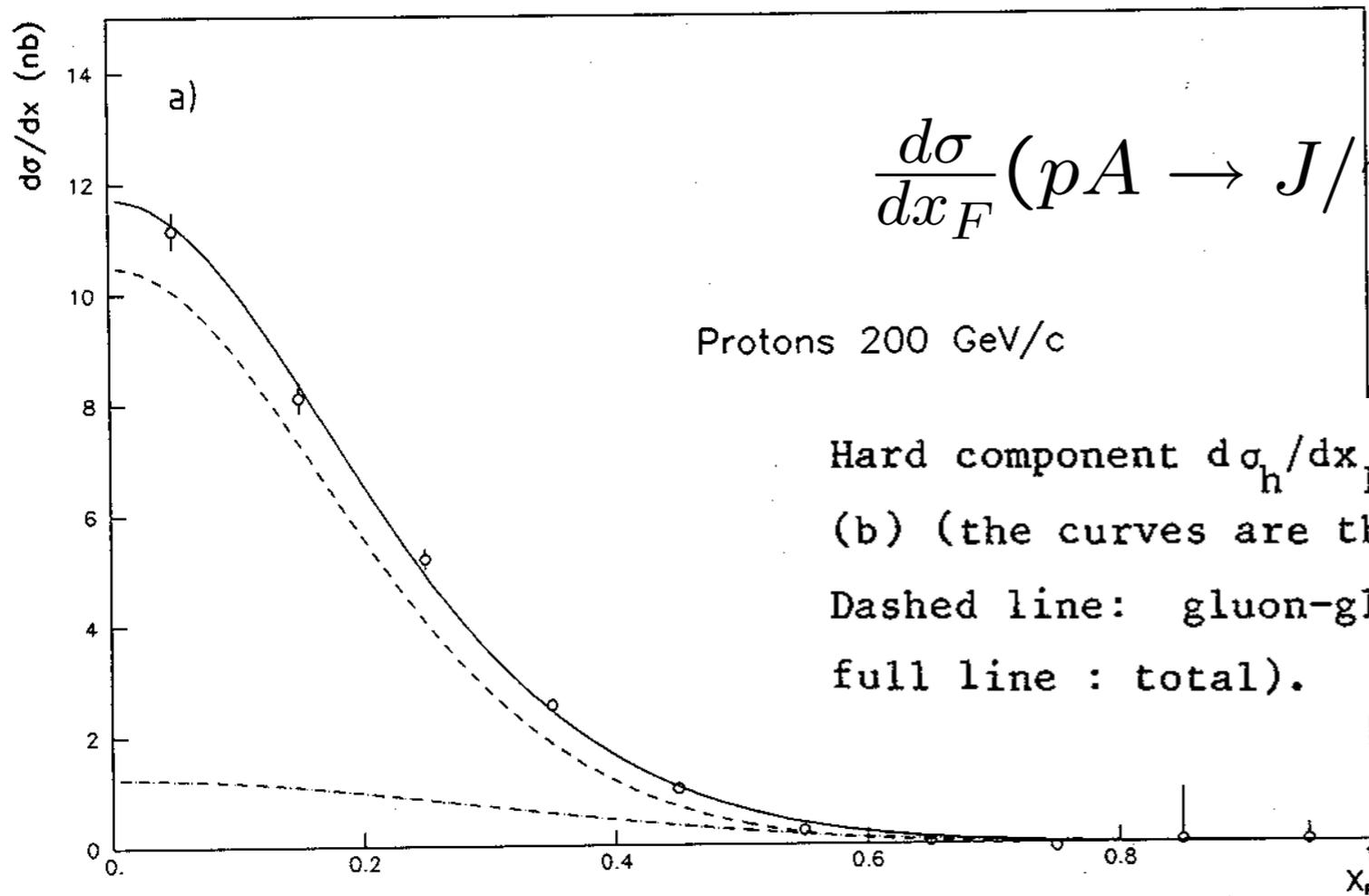
NA60 pA data @ 158GeV

$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X) \propto A^\alpha$$

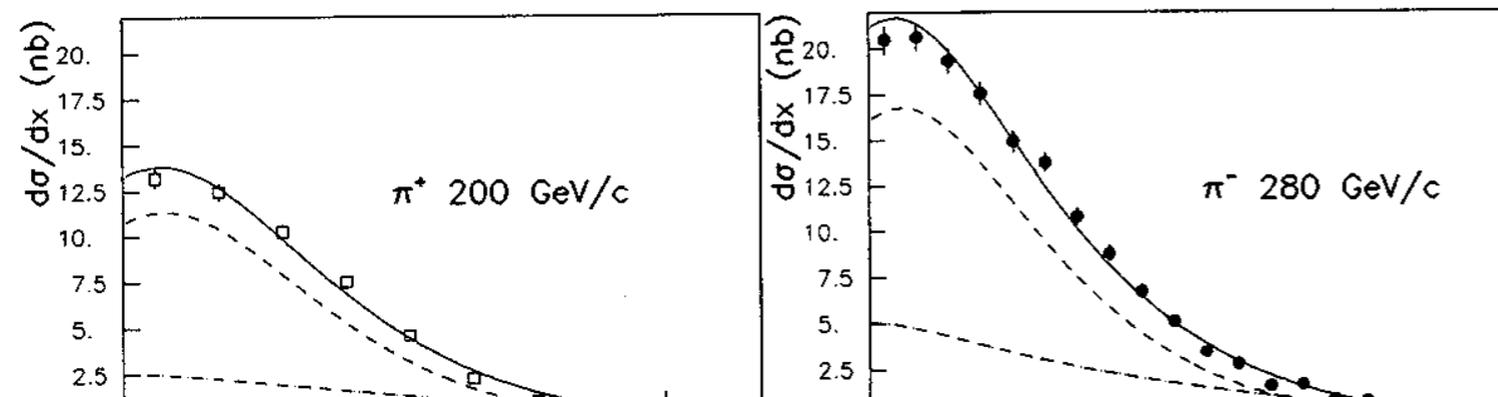
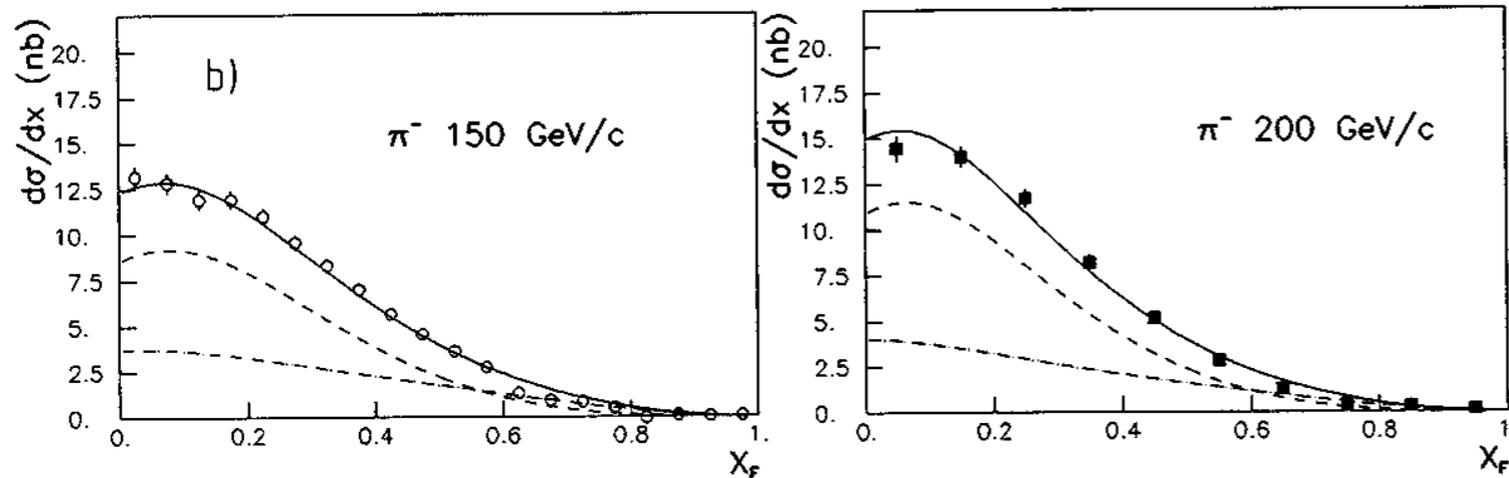


*Clear dependence
on x_F and
beam energy*

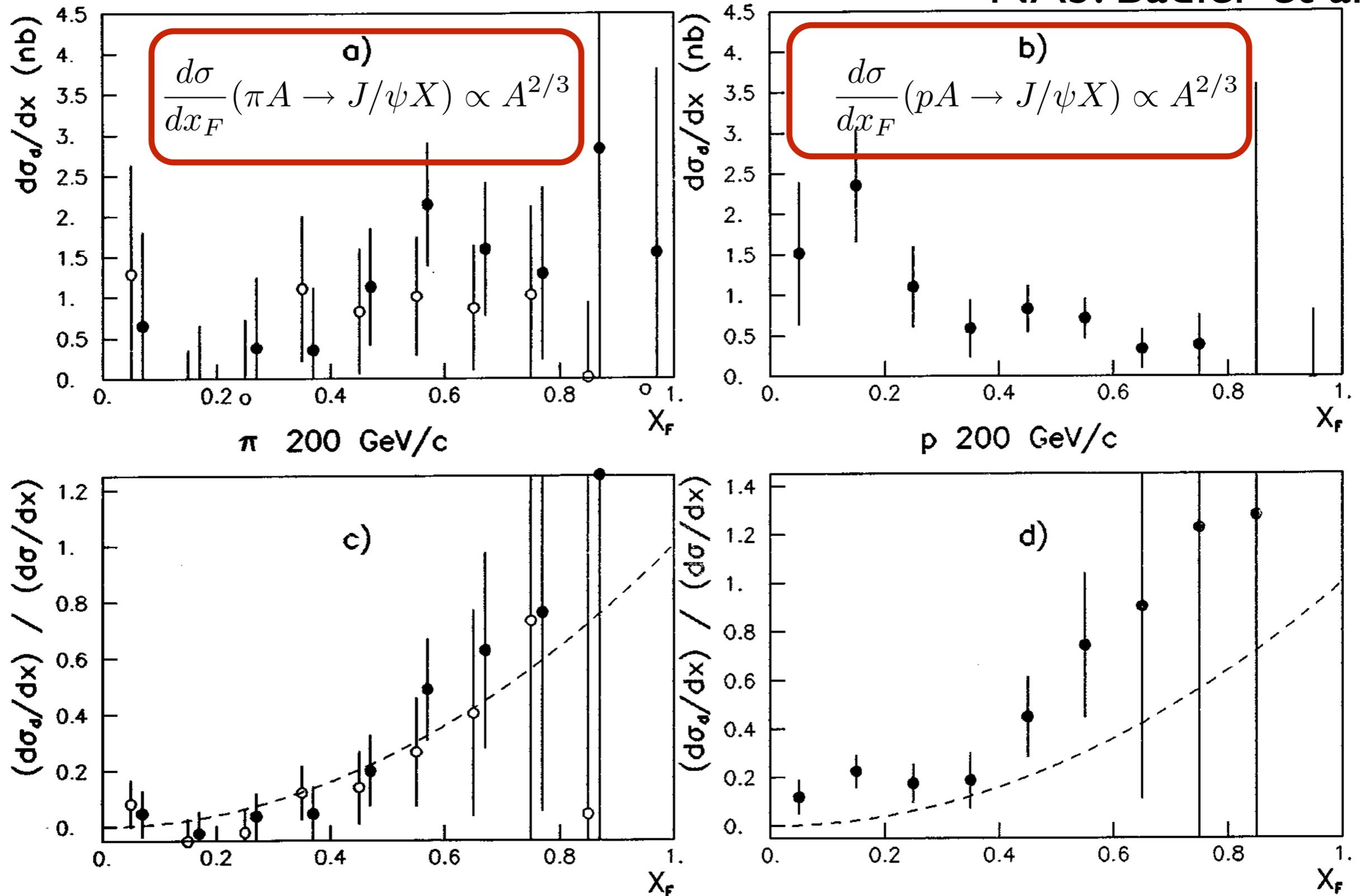
Dramatic change in nuclear dependence



Hard component $d\sigma_h/dx_F$ for incident protons (a) and pions (b) (the curves are the result of the fit described in the text. Dashed line: gluon-gluon fusion; dash-dotted line : $q\bar{q}$ fusion; full line : total).



A^1 component consistent with sum of gg and $q\bar{q}$ fusion

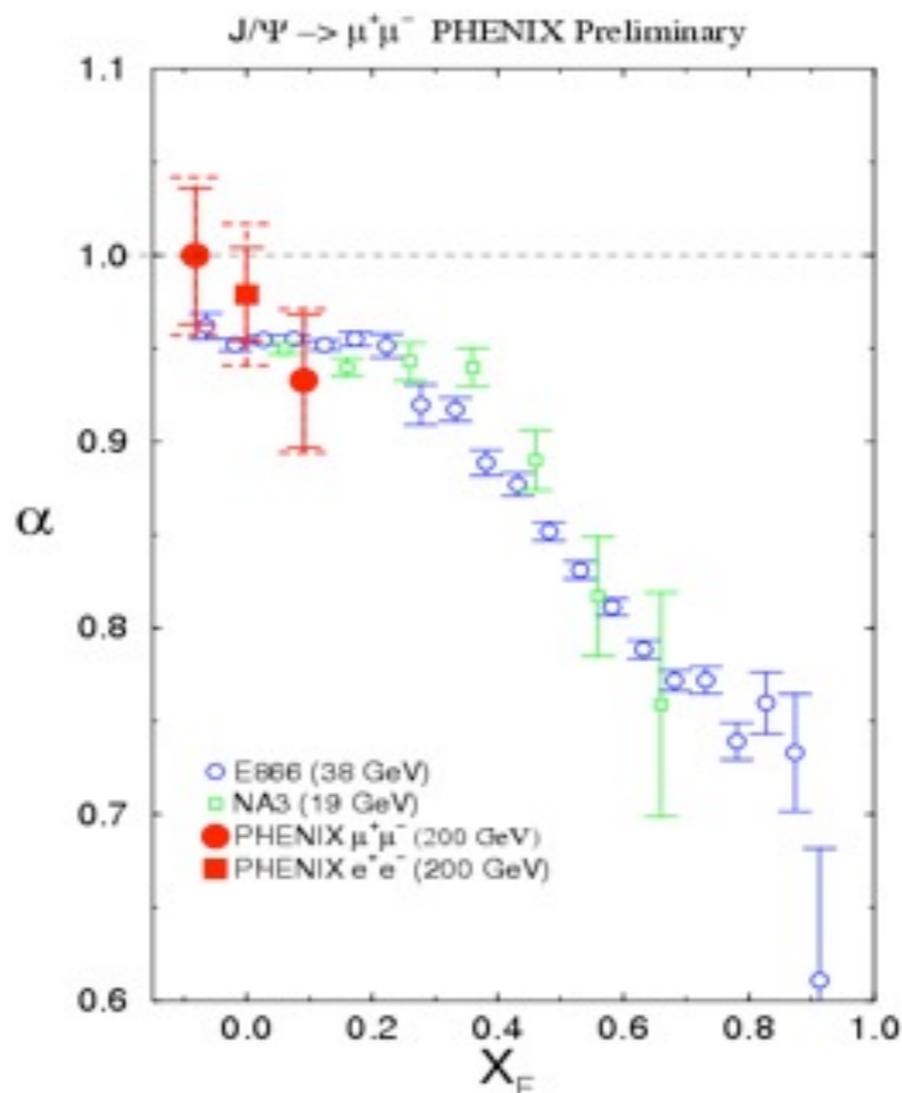
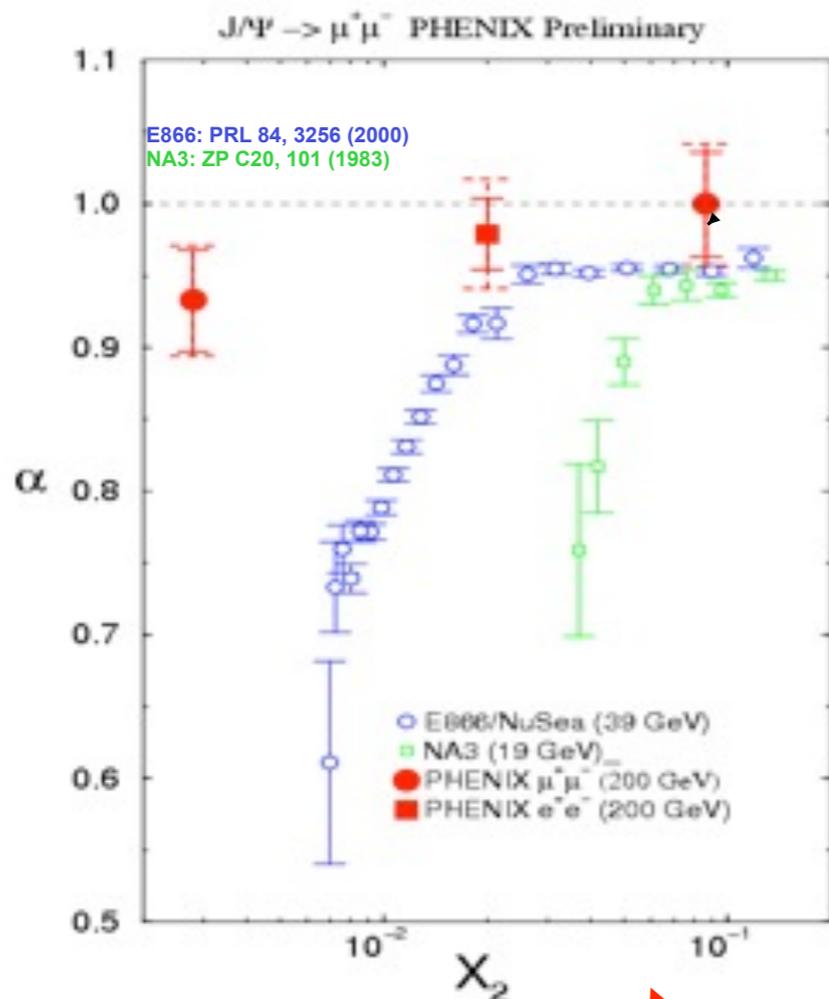


Flat x_F distribution explained by IC

J/ψ nuclear dependence versus rapidity, x_{Au} , x_F

M.Leitch

PHENIX compared to lower energy measurements



*Huge
"absorption"
effect*



Klein, Vogt, PRL 91:142301, 2003
Kopeliovich, NP A696:669, 2001

*Violates PQCD
factorization!*

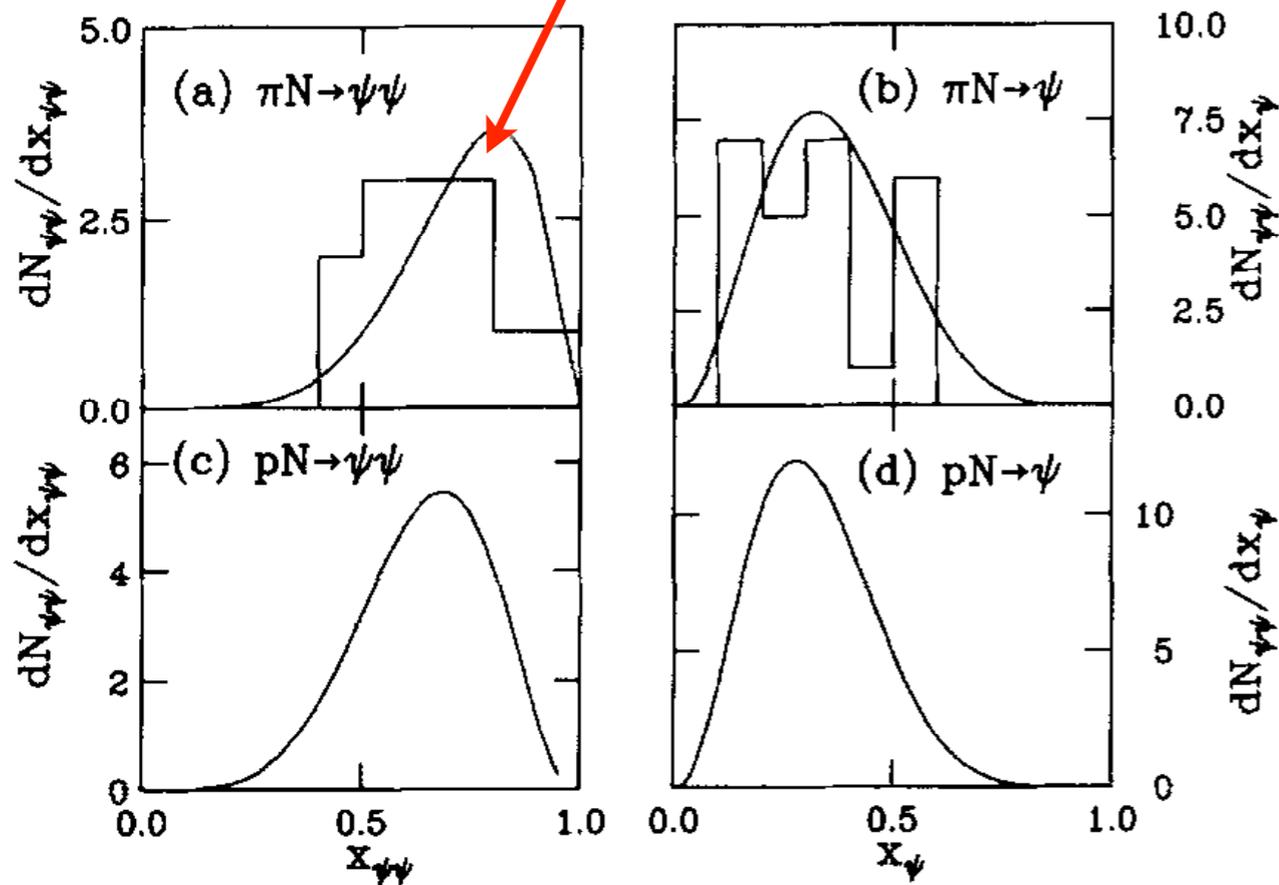
$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X)$$

Hoyer, Sukhatme, Vanttinen

Violates PQCD Factorization: $A^\alpha(x_F)$ not $A^\alpha(x_2)$

Excludes 'color drag' model

All events have $x_{\psi\psi}^F > 0.4$!



$$\pi A \rightarrow J/\psi J/\psi X$$

R. Vogt, sjb

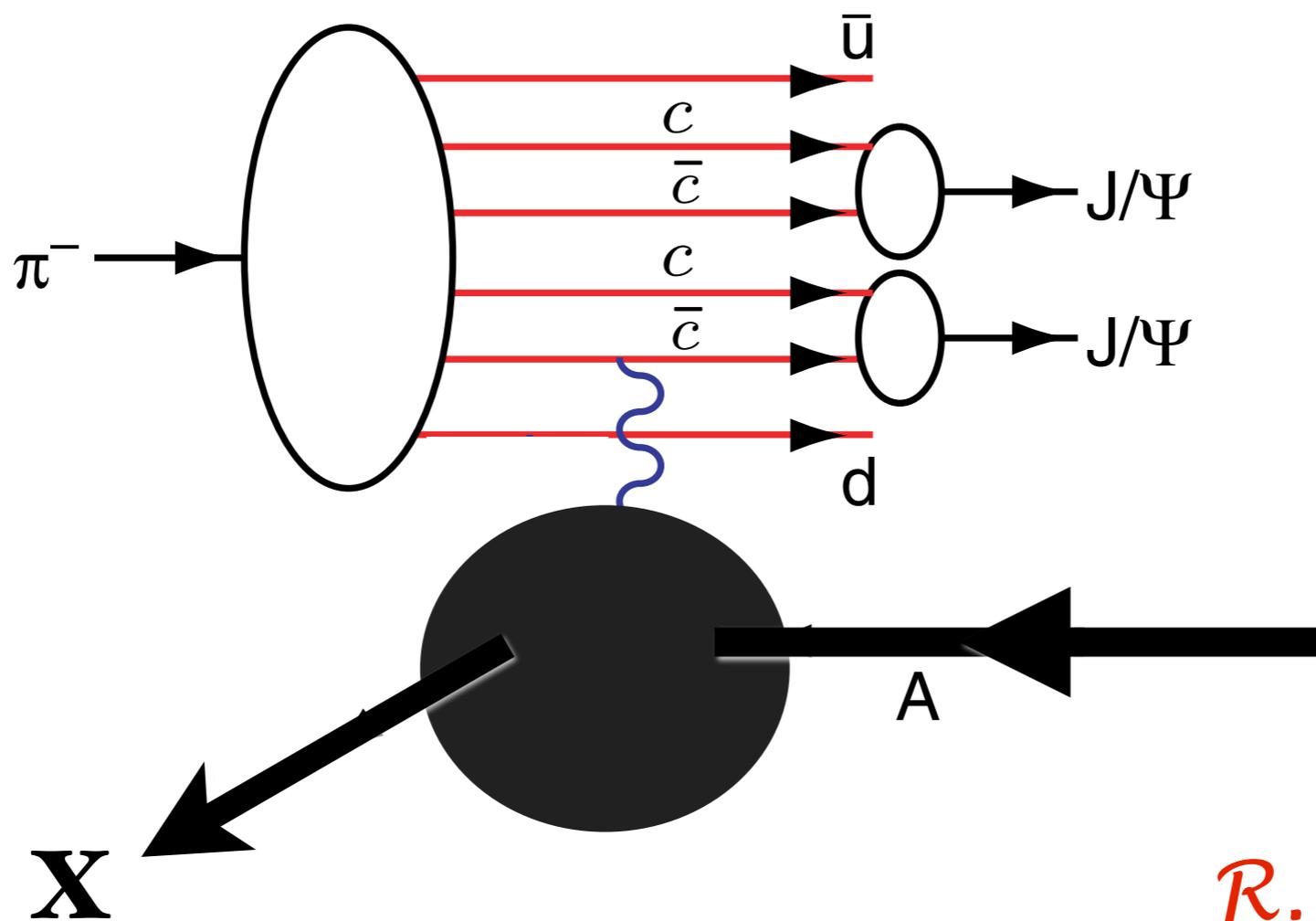
The probability distribution for a general n -particle intrinsic $c\bar{c}$ Fock state as a function of x and k_T is written as

$$\frac{dP_{ic}}{\prod_{i=1}^n dx_i d^2 k_{T,i}} = N_n \alpha_s^4 (M_{c\bar{c}}) \frac{\delta(\sum_{i=1}^n k_{T,i}) \delta(1 - \sum_{i=1}^n x_i)}{(m_h^2 - \sum_{i=1}^n (m_{T,i}^2/x_i))^2},$$

Fig. 3. The $\psi\psi$ pair distributions are shown in (a) and (c) for the pion and proton projectiles. Similarly, the distributions of J/ψ 's from the pairs are shown in (b) and (d). Our calculations are compared with the $\pi^- N$ data at 150 and 280 GeV/c [1]. The $x_{\psi\psi}$ distributions are normalized to the number of pairs from both pion beams (a) and the number of pairs from the 400 GeV proton measurement (c). The number of single J/ψ 's is twice the number of pairs.

NA3 Data

*Cannot be explained
by Color Drag Model*



R. Vogt, s1b

- EMC data: $c(x, Q^2) > 30 \times \text{DGLAP}$
 $Q^2 = 75 \text{ GeV}^2, x = 0.42$
- High x_F $pp \rightarrow J/\psi X$
- High x_F $pp \rightarrow J/\psi J/\psi X$
- High x_F $pp \rightarrow \Lambda_c X$
- High x_F $pp \rightarrow \Lambda_b X$
- High x_F $pp \rightarrow \Xi(ccd)X$ (SELEX)

Rules out color drag (Pythia)

Explain Tevatron anomalies: $p\bar{p} \rightarrow \gamma cX, ZcX$

Interesting spin, charge asymmetry, threshold, spectator effects

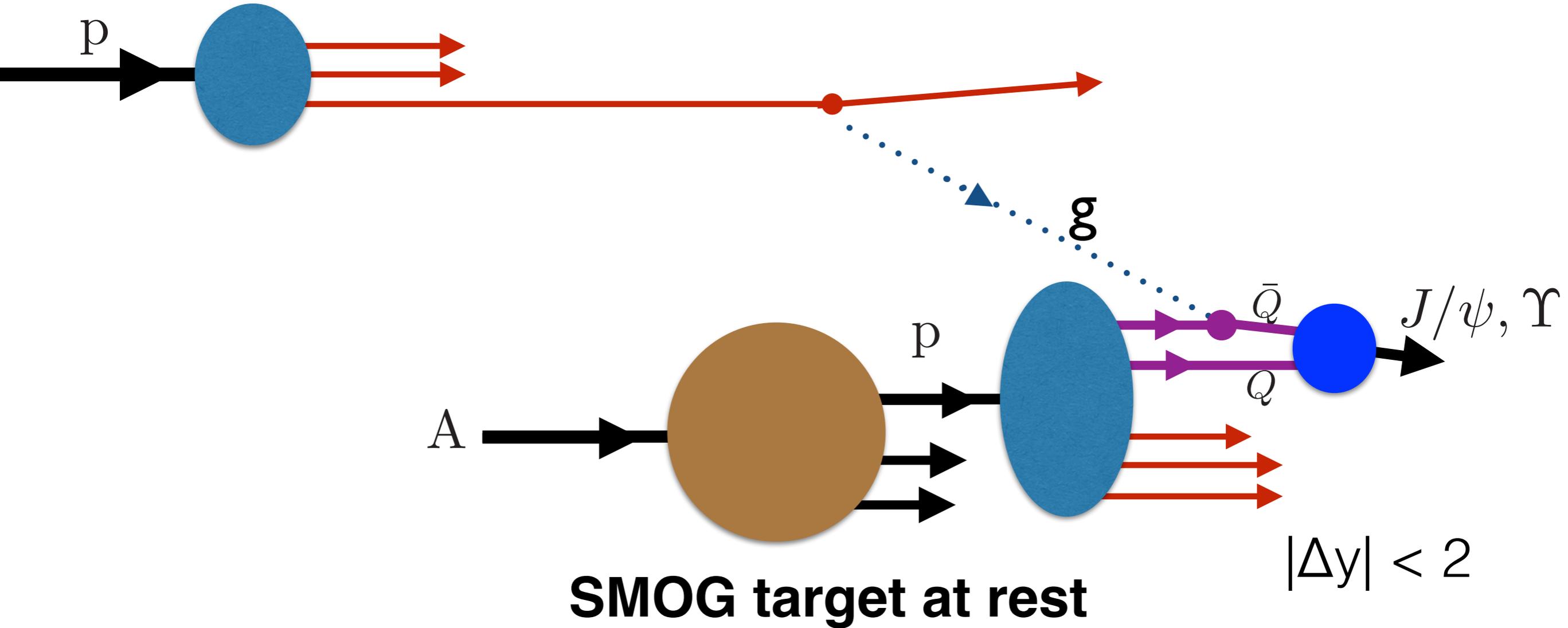
Important corrections to B decays; Quarkonium decays

Gardner, Karliner, sjb

$$pA \rightarrow J/\psi X$$

$$E_p = 6.5 \text{ TeV}$$

p

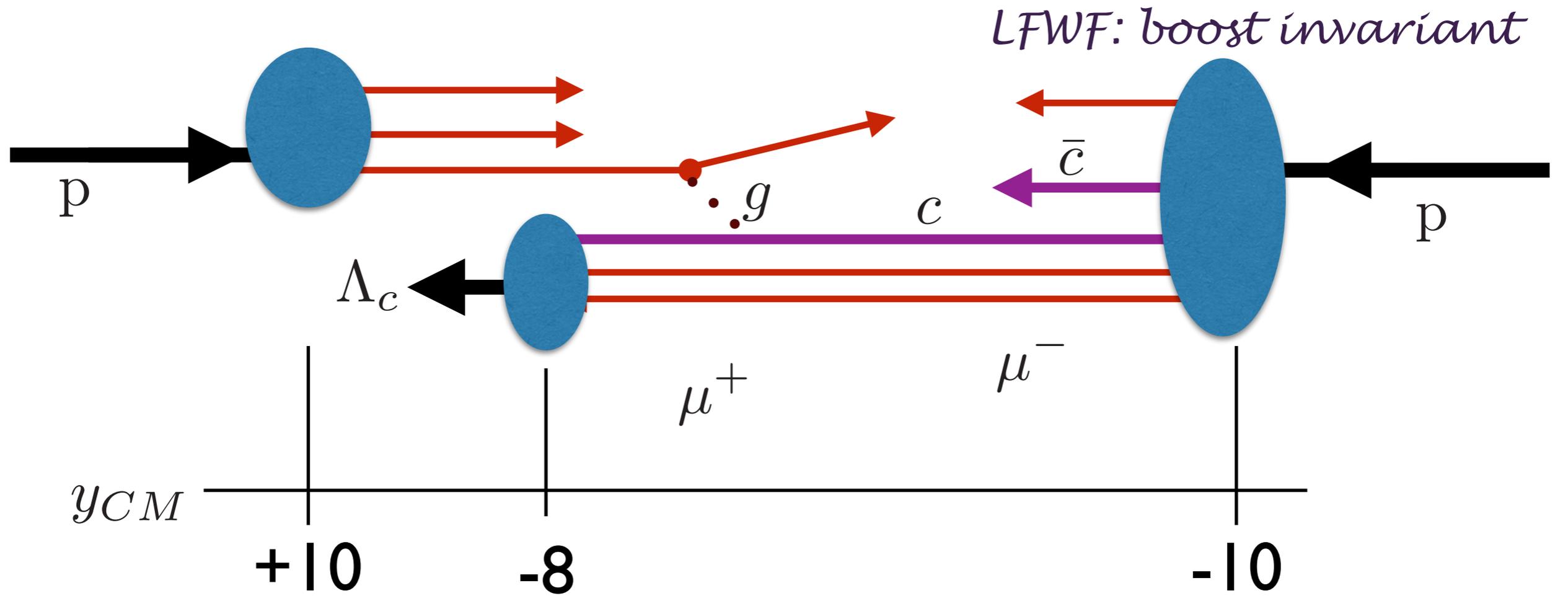


SMOG target at rest

$$|\Delta y| < 2$$

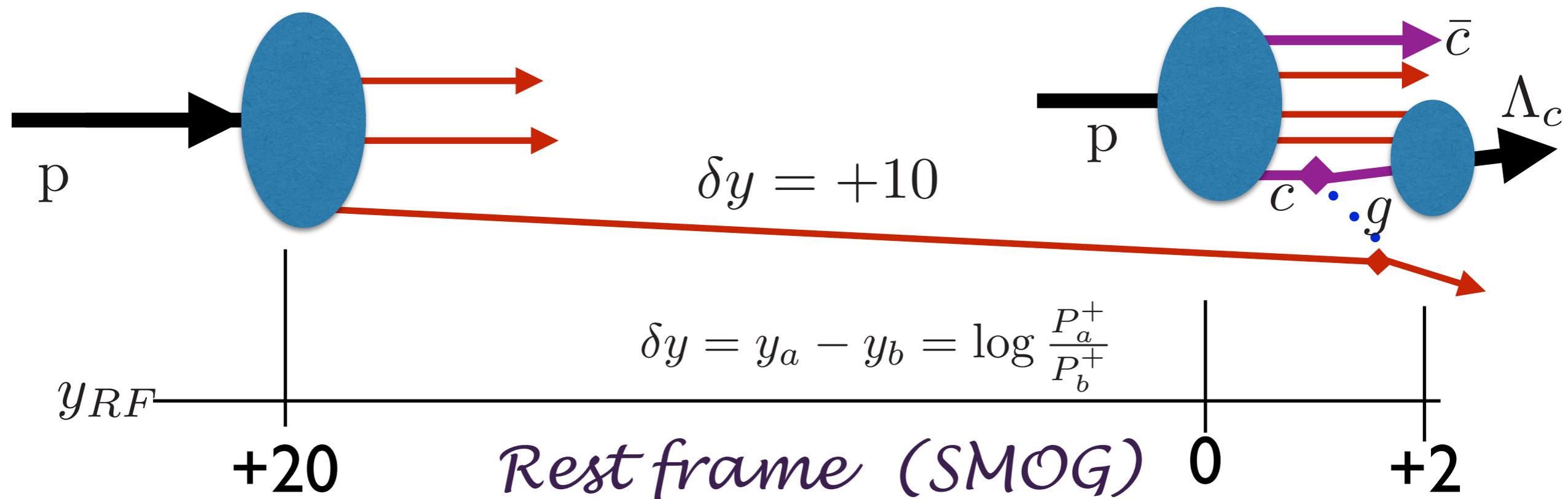
Intrinsic heavy quark probability in the nucleon maximal at minimum off-shellness

Quarkonium produced nearly at rest — has small rapidity in target rest frame



$ISR \ x_F(\Lambda_c) = 0.8$

CM frame

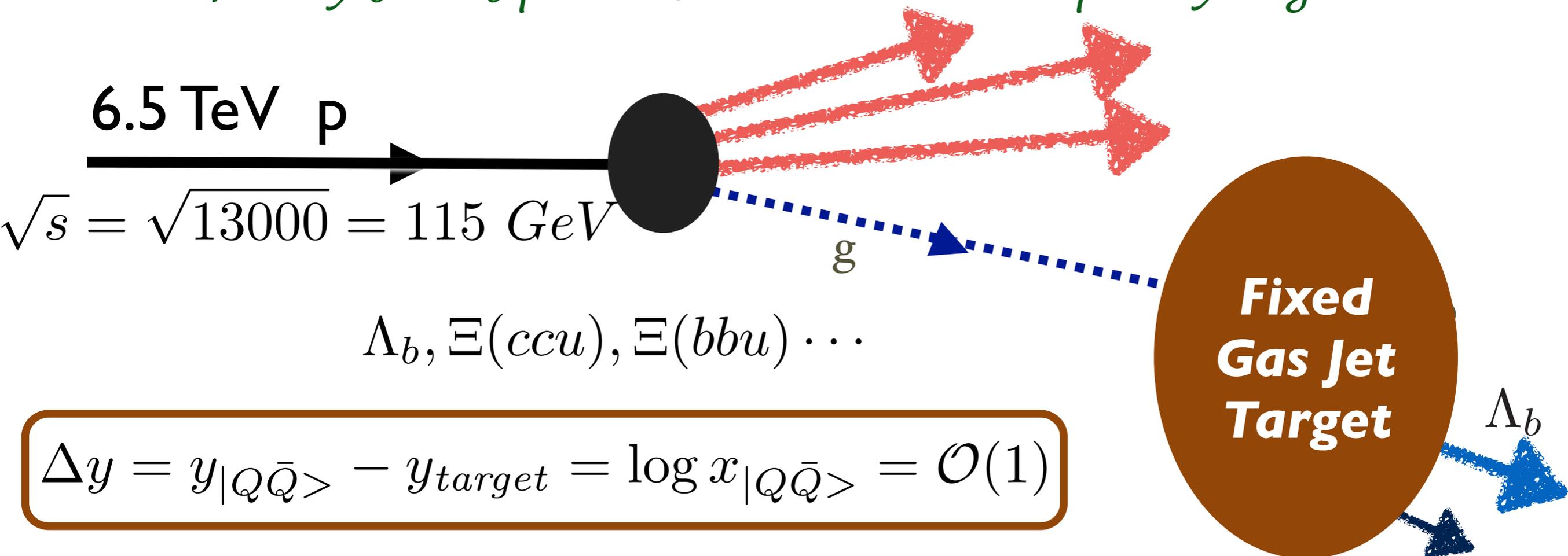


Excitation of Intrinsic Heavy Quarks in a Fixed Target

*Amplitude maximal at minimal invariant mass,
in target rapidity domain!*

$$x_i \sim \frac{m_{\perp i}}{\sum_j^n m_{\perp j}} \quad \frac{d\sigma}{dy_{J/\psi}} (pA \rightarrow J/\psi X)$$

Heavy states produced in TARGET rapidity region



Produce $J/\psi, \Upsilon, \Lambda_c, \Lambda_b, |ccu\rangle, |cud\bar{c}\rangle, |cuudddu\bar{c}\rangle, \dots$

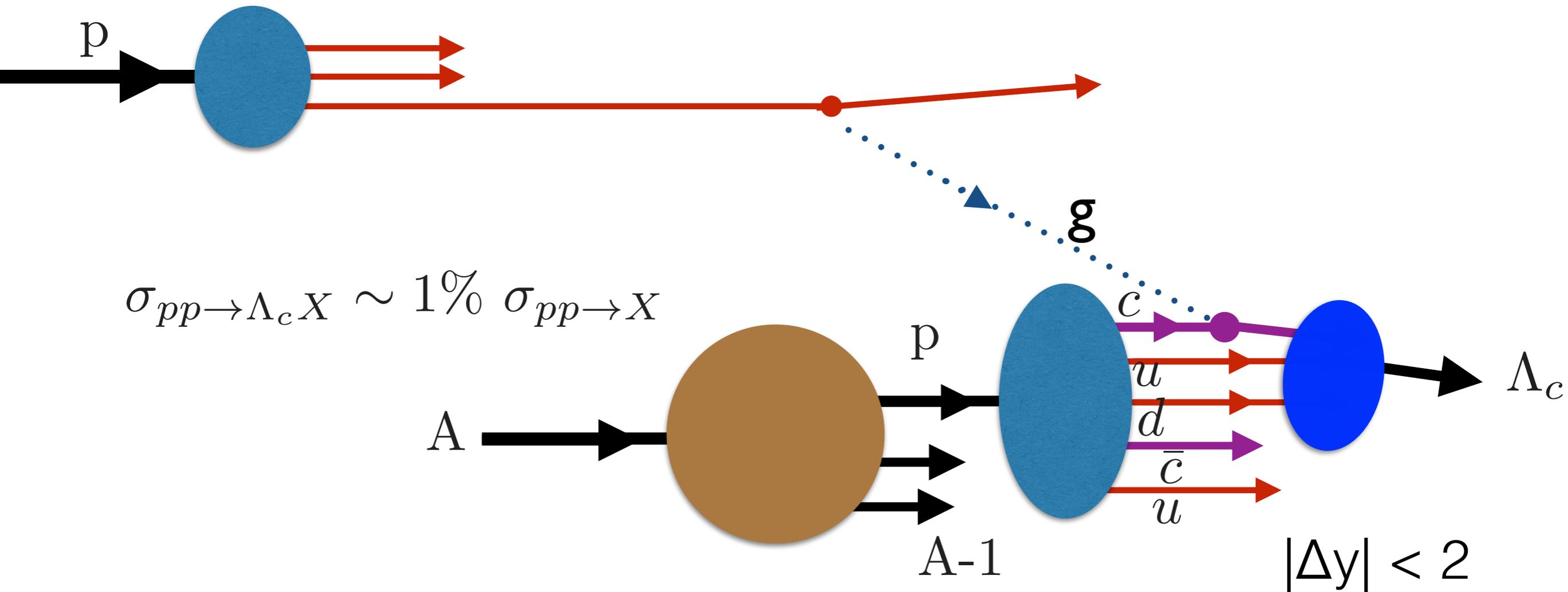
Test at Smog@LHCb

discussions with M. Williams

$$pA \rightarrow \Lambda_c X$$

$$E_p = 6.5 \text{ TeV}$$

p



SMOG target at rest

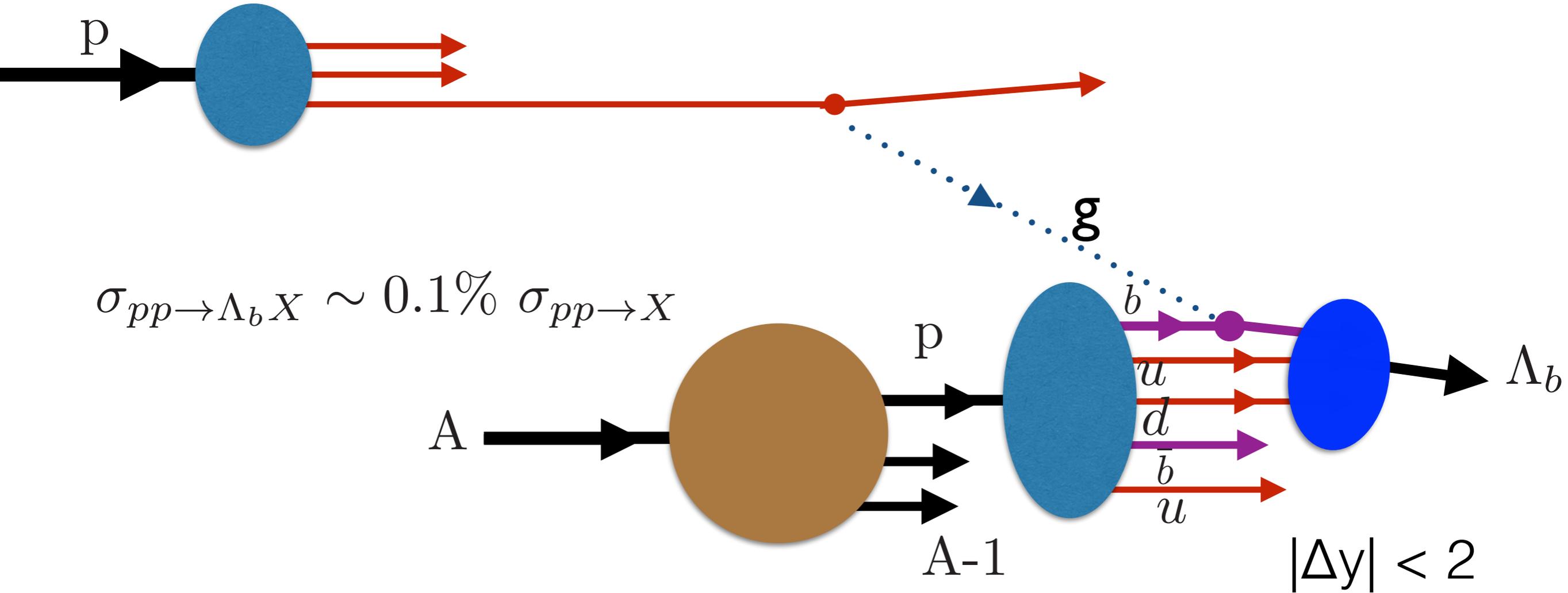
Intrinsic heavy quark probability in the nucleon maximal at minimum off-shellness

Heavy hadrons produced nearly at rest — has small rapidity in target rest frame

$$pA \rightarrow \Lambda_b X$$

$$E_p = 6.5 \text{ TeV}$$

p

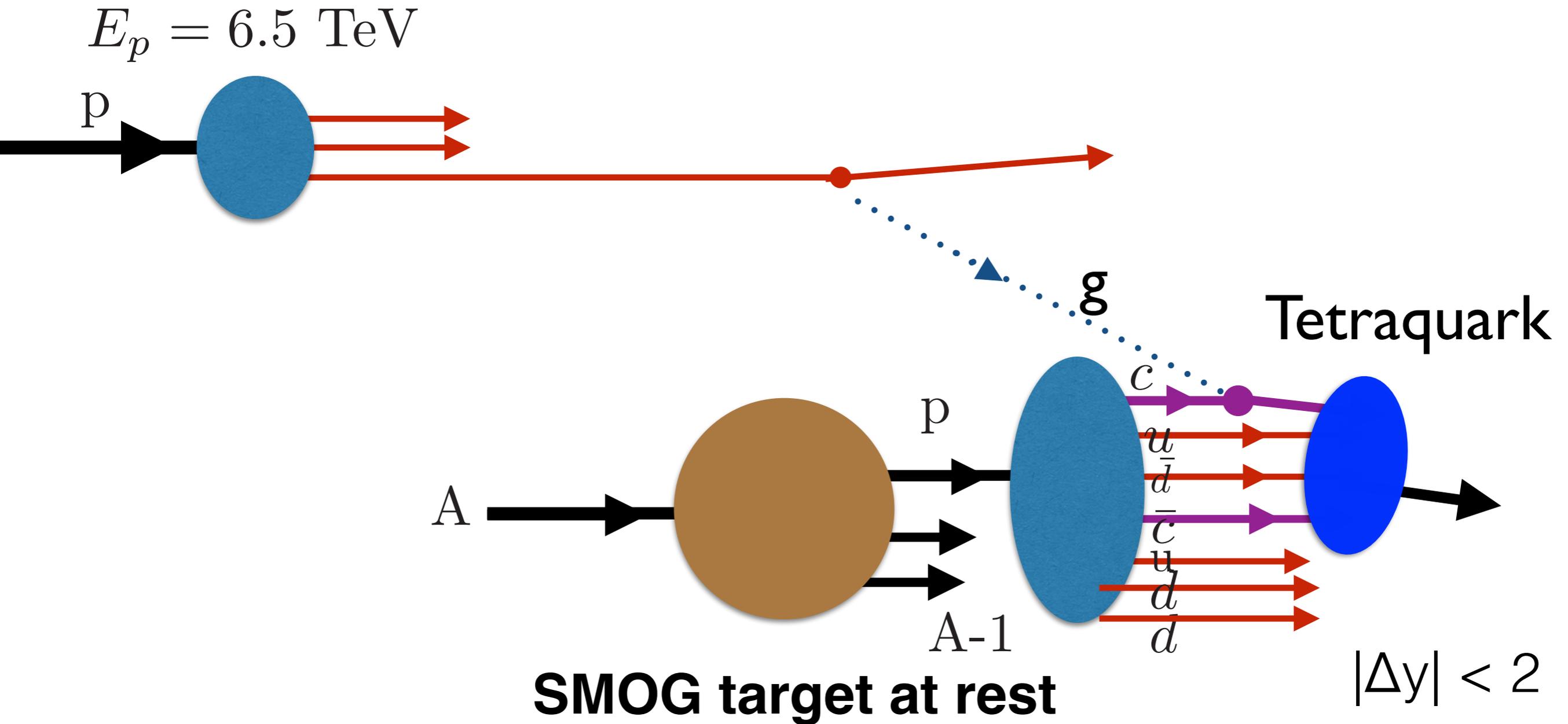


SMOG target at rest

Intrinsic heavy quark probability in the nucleon maximal at minimum off-shellness

Quarkonium produced nearly at rest — has small rapidity in target rest frame

$$pA \rightarrow \text{Tetraquark}(|cu\bar{c}\bar{d}\rangle)X$$



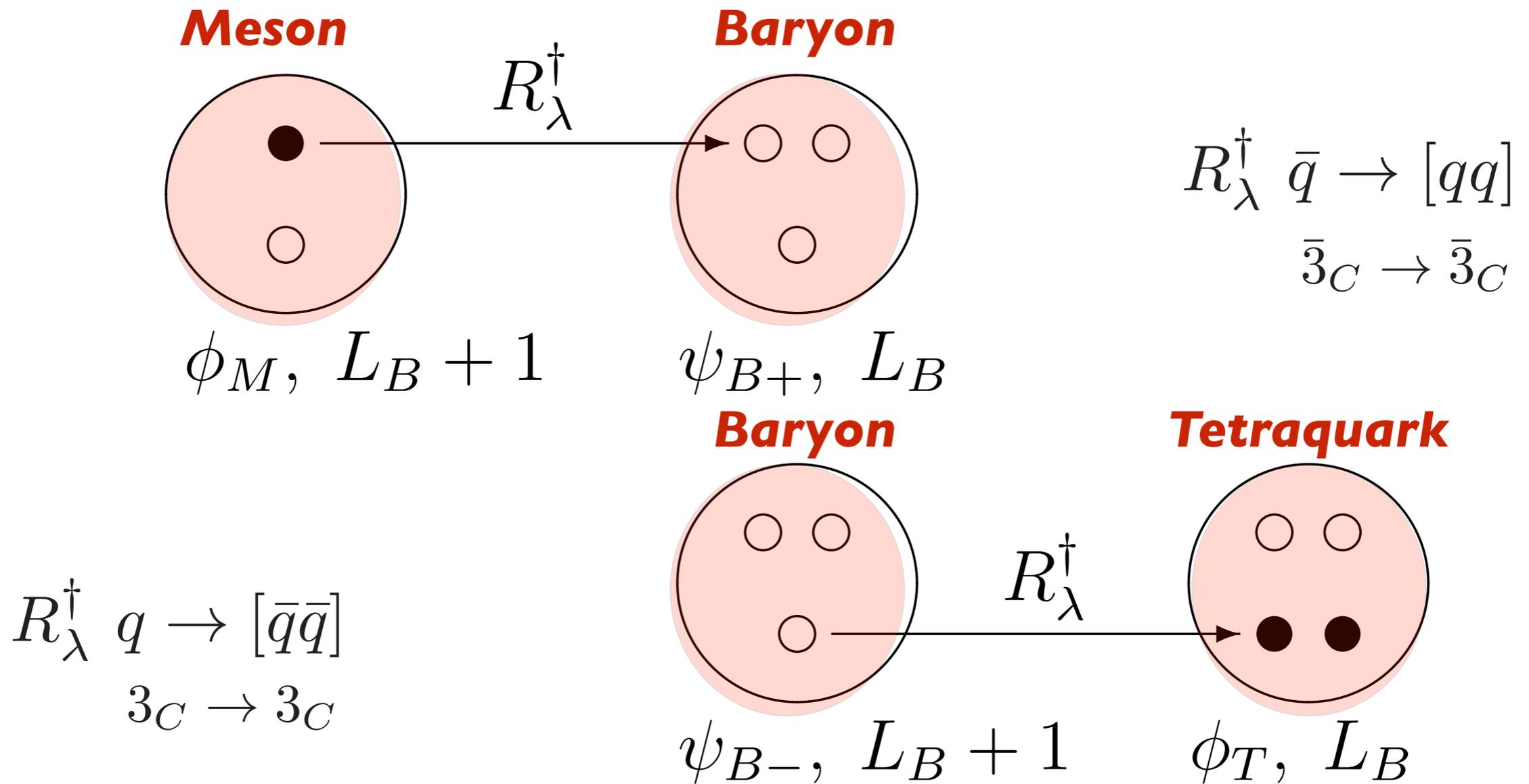
Intrinsic heavy quark probability in the nucleon maximal at minimum off-shellness

Tetraquark produced nearly at rest — has small rapidity in target rest frame

Superconformal Algebra

2X2 Hadronic Multiplets: 4-Plet

Bosons, Fermions with Equal Mass!



Proton: $|u[ud]\rangle$ Quark + Scalar Diquark
 Equal Weight: $L=0, L=1$

New World of Tetraquarks

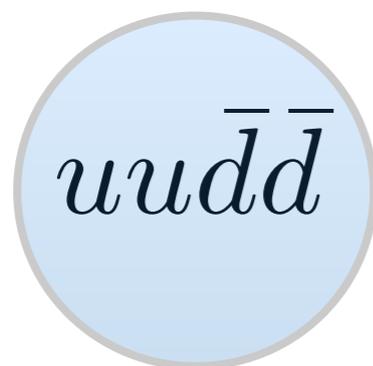
$$3_C \times 3_C = \bar{3}_C + 6_C$$

Bound!

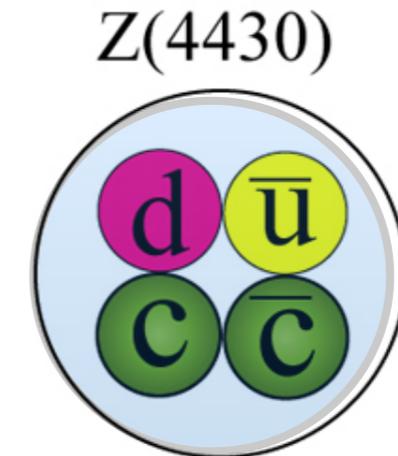
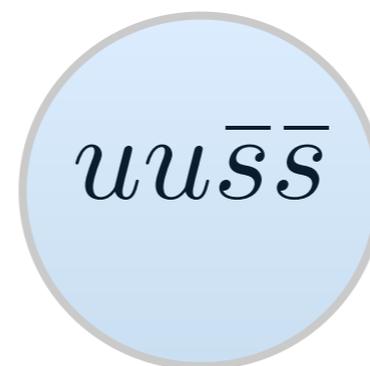
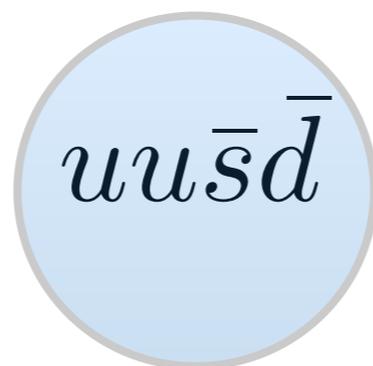
- Diquark Color-Confined Constituents: Color $\bar{3}_C$
- Diquark-Antidiquark bound states
- Confinement Force Similar to quark-antiquark mesons $\bar{3}_C \times 3_C = 1_C$

Complete Regge spectrum in n, L

- Isospin $I = 0, \pm 1, \pm 2$ Charge $Q = 0, \pm 1, \pm 2$

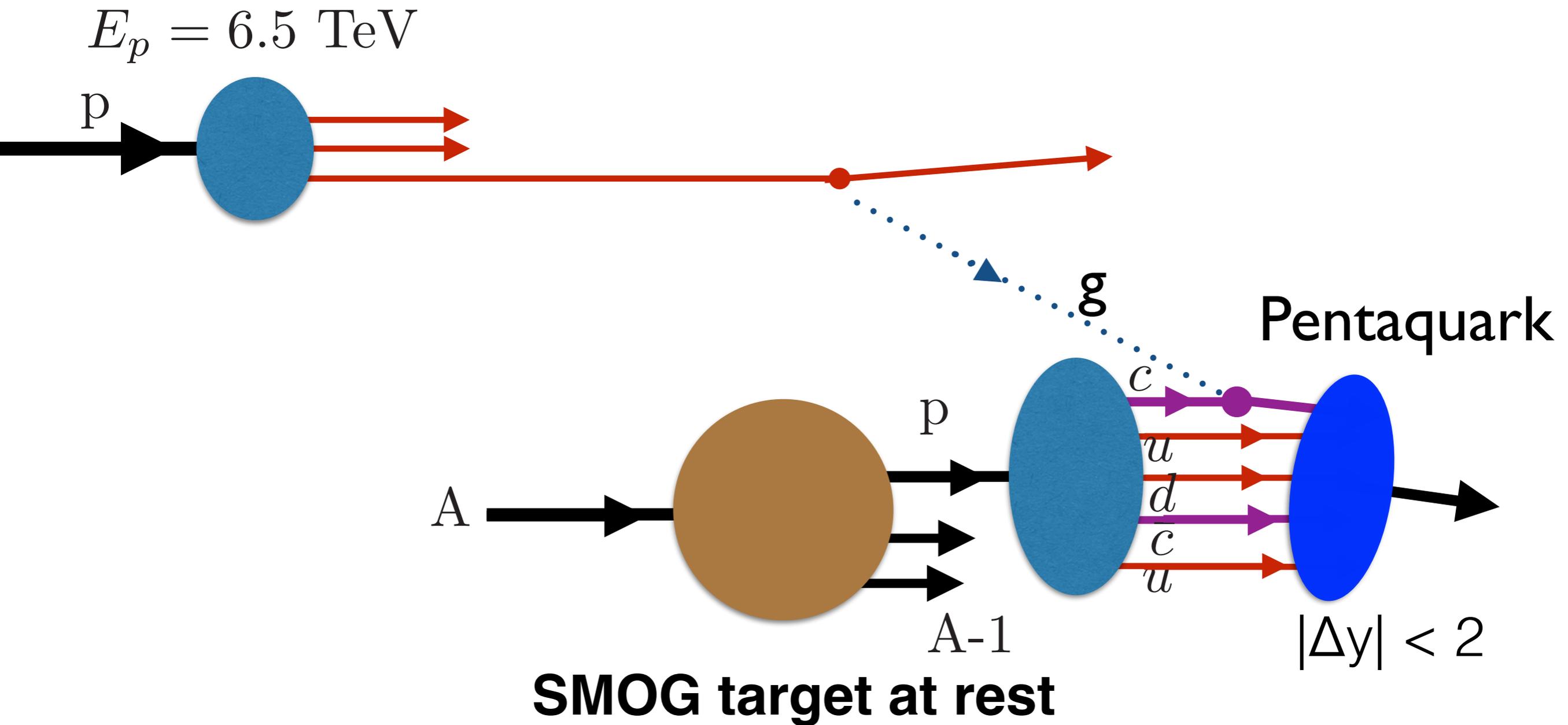


$$Q = +2$$



$$Q = -1$$

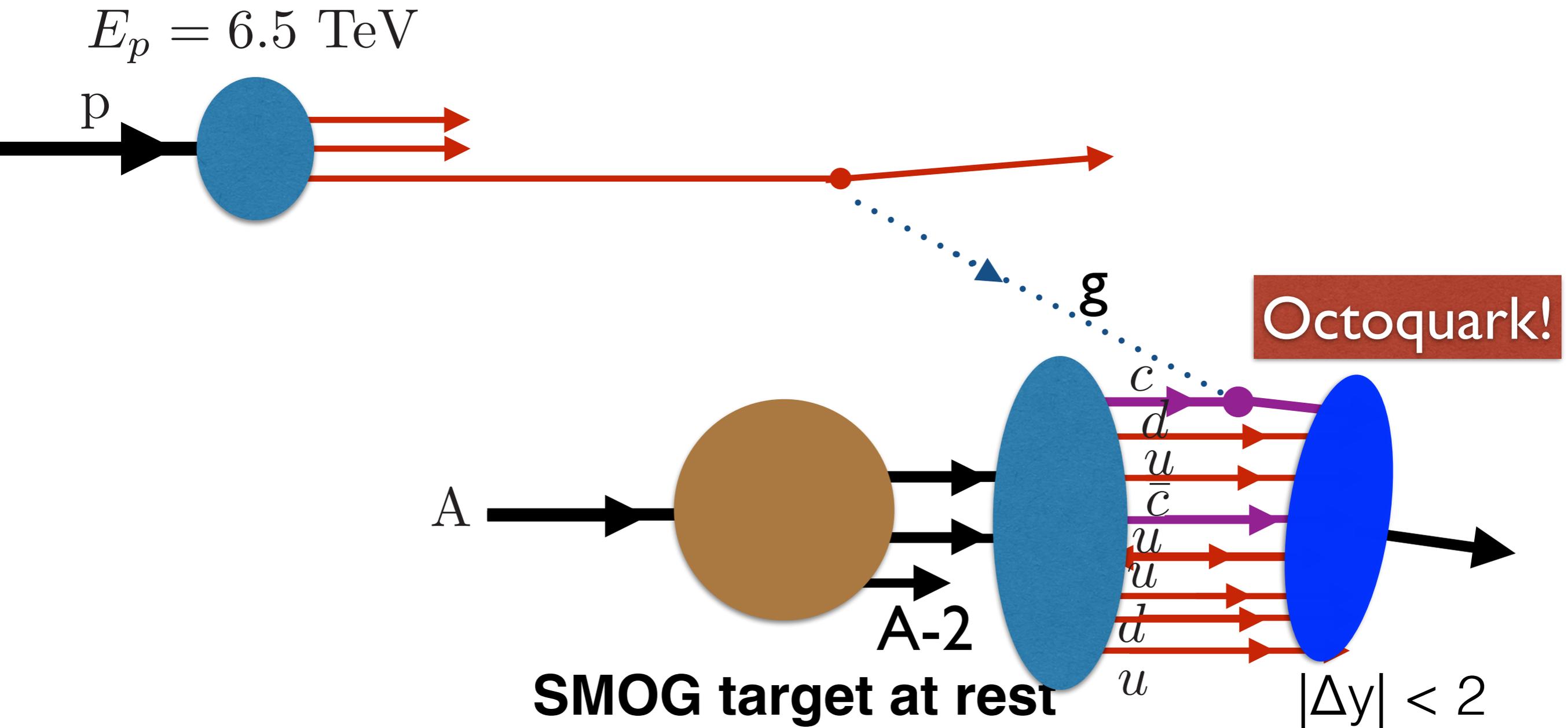
$$pA \rightarrow \text{Pentaquark}(|uudc\bar{c}\rangle)X$$



Intrinsic heavy quark probability in the nucleon maximal at minimum off-shellness

Produced nearly at rest — has small rapidity in target rest frame

$$pA \rightarrow \text{Octoquark}(|uuduudc\bar{c}\rangle)X$$

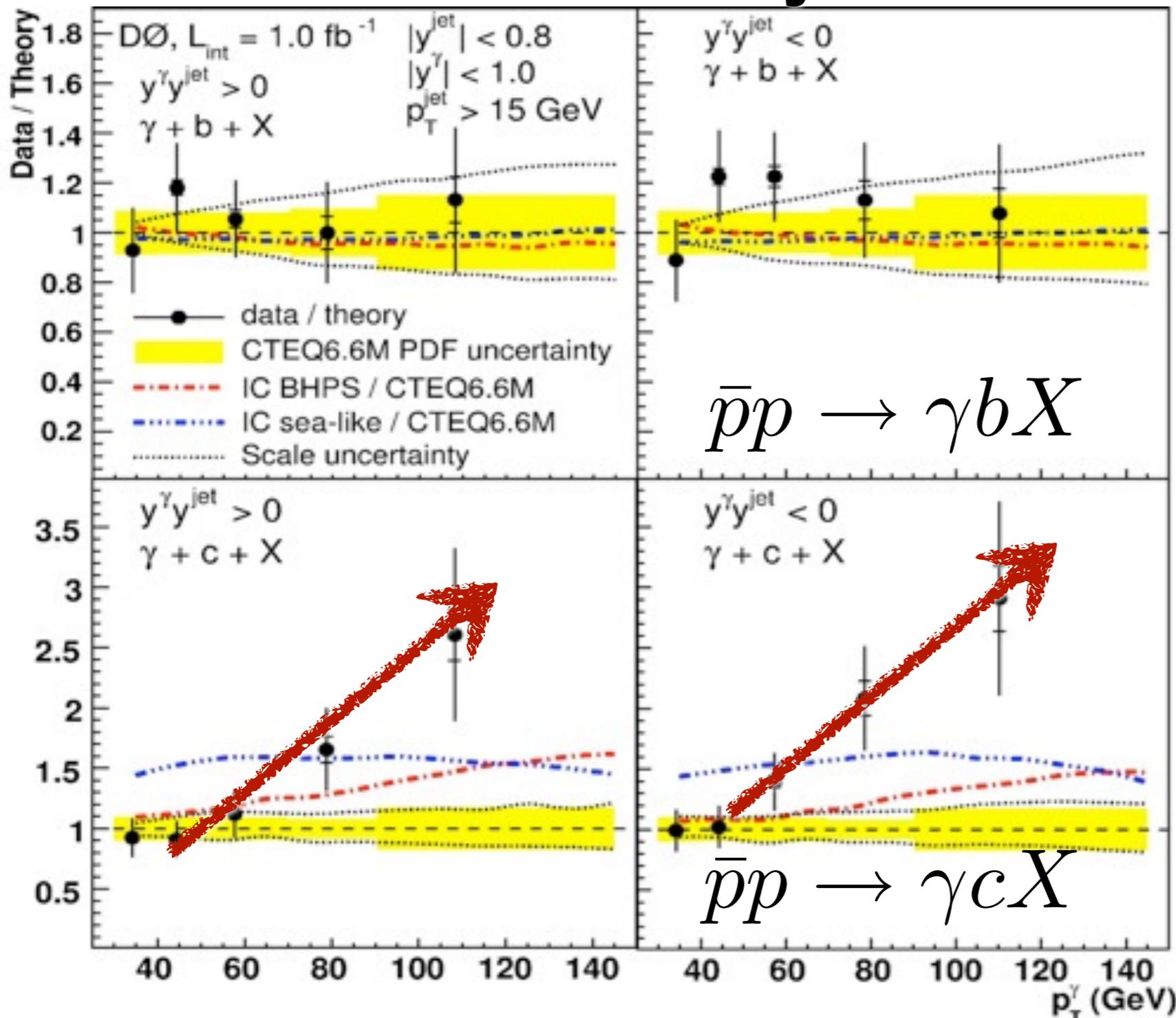


Intrinsic heavy quark probability in the nucleon maximal at minimum off-shellness

Produced nearly at rest — has small rapidity in target rest frame

Measurement of $\gamma + b + X$ and $\gamma + c + X$ Production Cross Sections
in $p\bar{p}$ Collisions at $\sqrt{s} = 1.96$ TeV

Data/Theory



$$\frac{\Delta\sigma(\bar{p}p \rightarrow \gamma c X)}{\Delta\sigma(\bar{p}p \rightarrow \gamma b X)}$$

**Ratio insensitive
to gluon PDF,
scales**

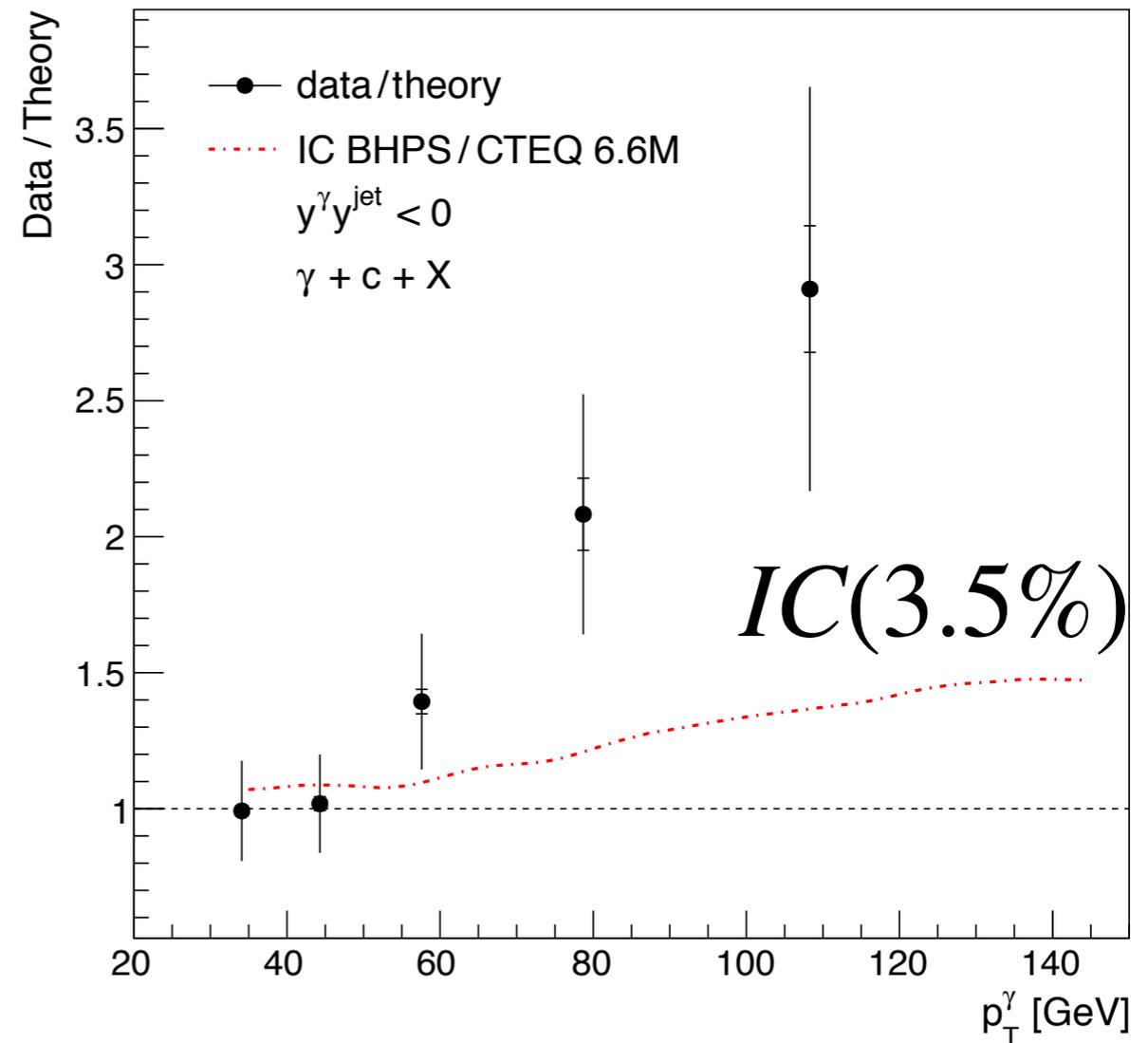
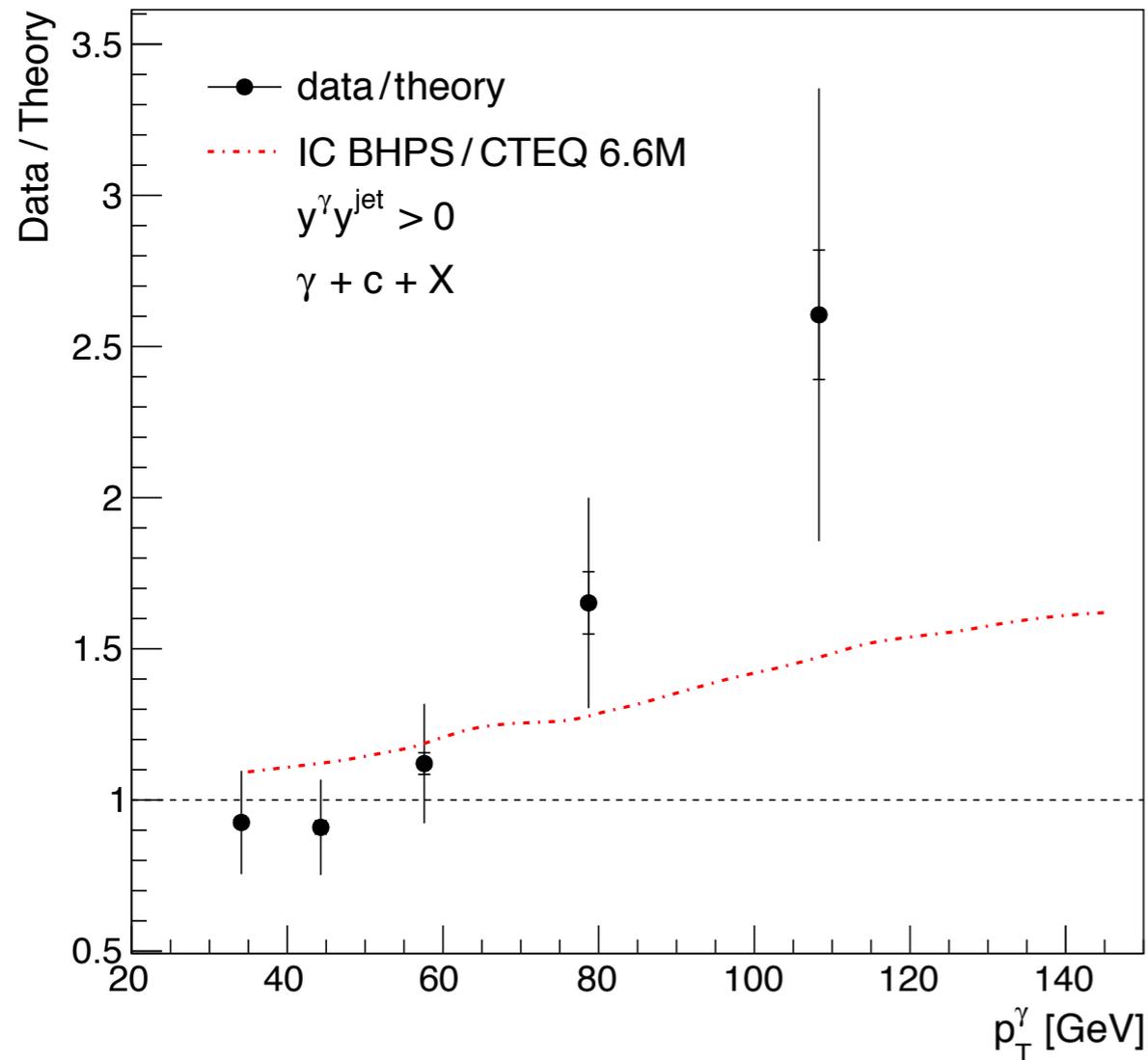
**Signal for significant
IC
at $x > 0.1$**

*Consistent with EMC measurement of charm
structure function at high x*

Production of Prompt Photon and c or b -jet in Hard pp Collisions

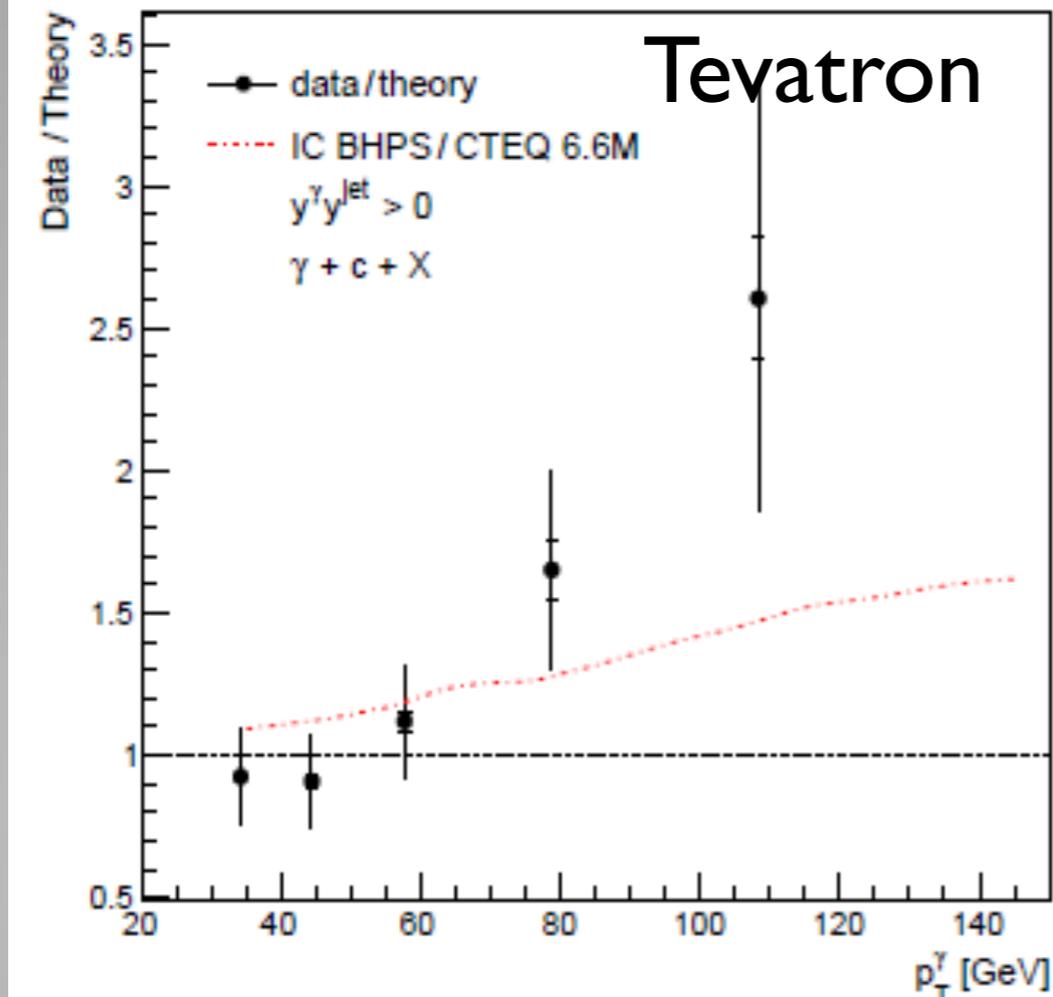
$$p\bar{p} \rightarrow \gamma cX$$

Juraj Smieško



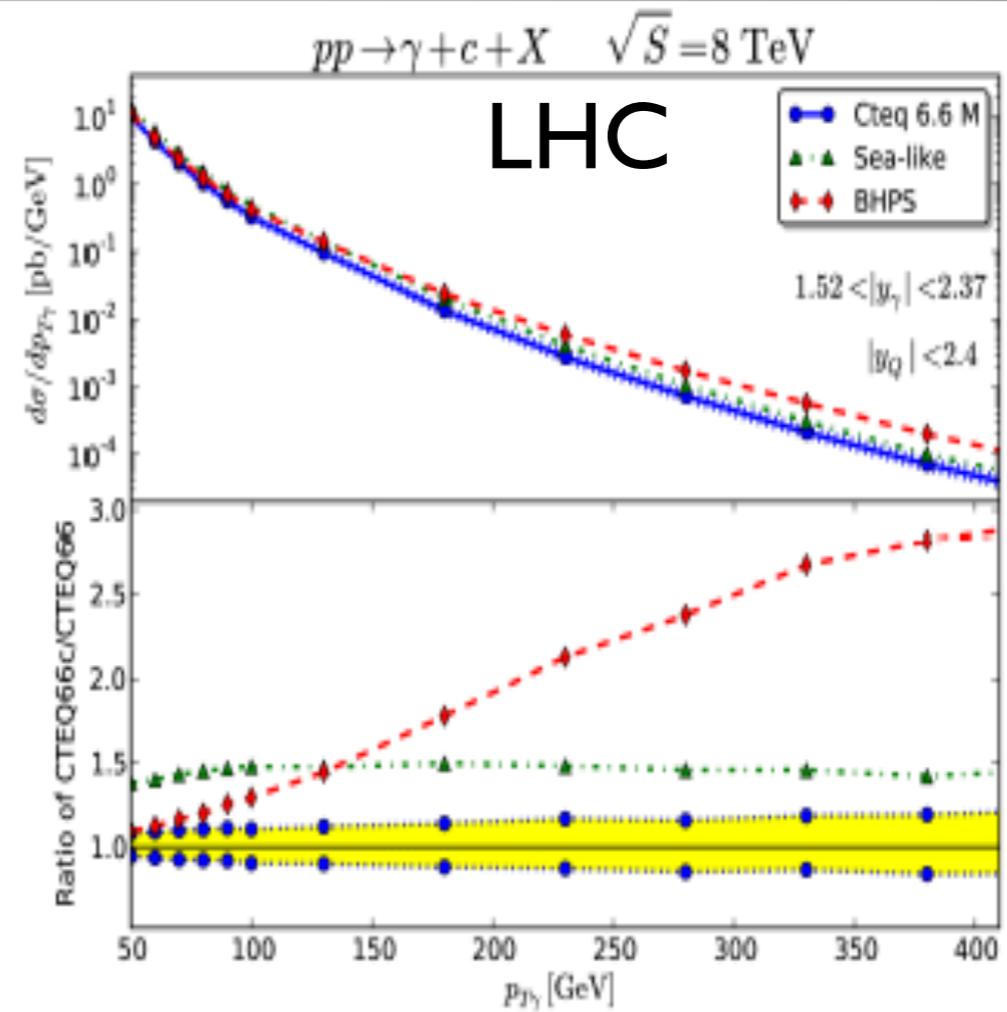
The data-to-theory ratio [8] for the processes $p\bar{p} \rightarrow \gamma + c + X$, when $y^\gamma y^{\text{jet}} > 0$ (left) and the same ratio, when $y^\gamma y^{\text{jet}} < 0$ (right) at $\sqrt{s} = 1.96$ TeV. The dash-dotted line is the calculation of this ratio using the **BHPS IC** model with the **IC** probability about 3.5 %.

Ratio Data/Theory for $p \bar{p} \rightarrow \gamma + c + X$
 (D0 experiment) at $s^{1/2} = 1.96$ TeV (left)



*V.M. Abazov, et al. (D0) Phys.Rev.Lett.
 102 (2009) 192002.*

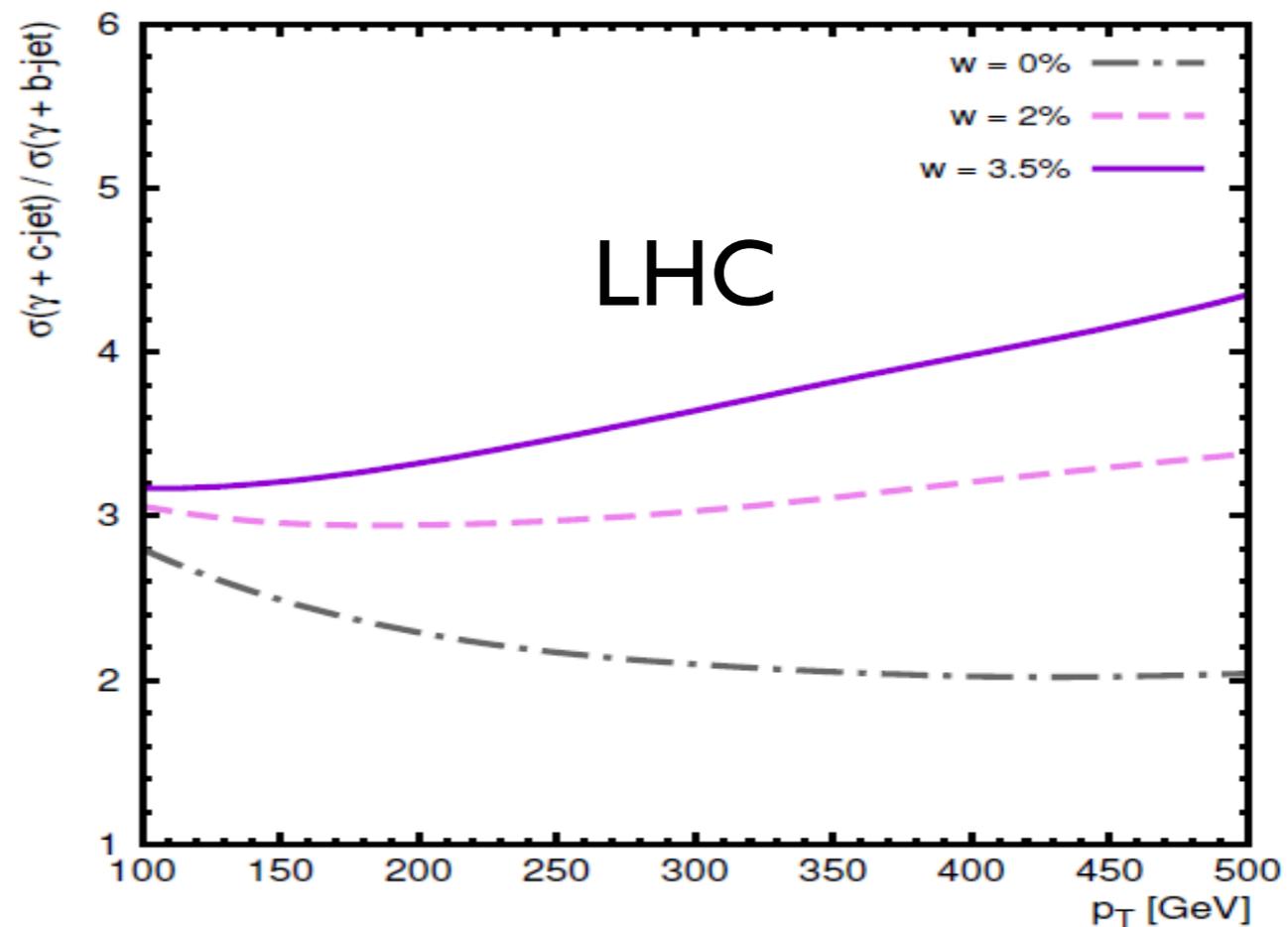
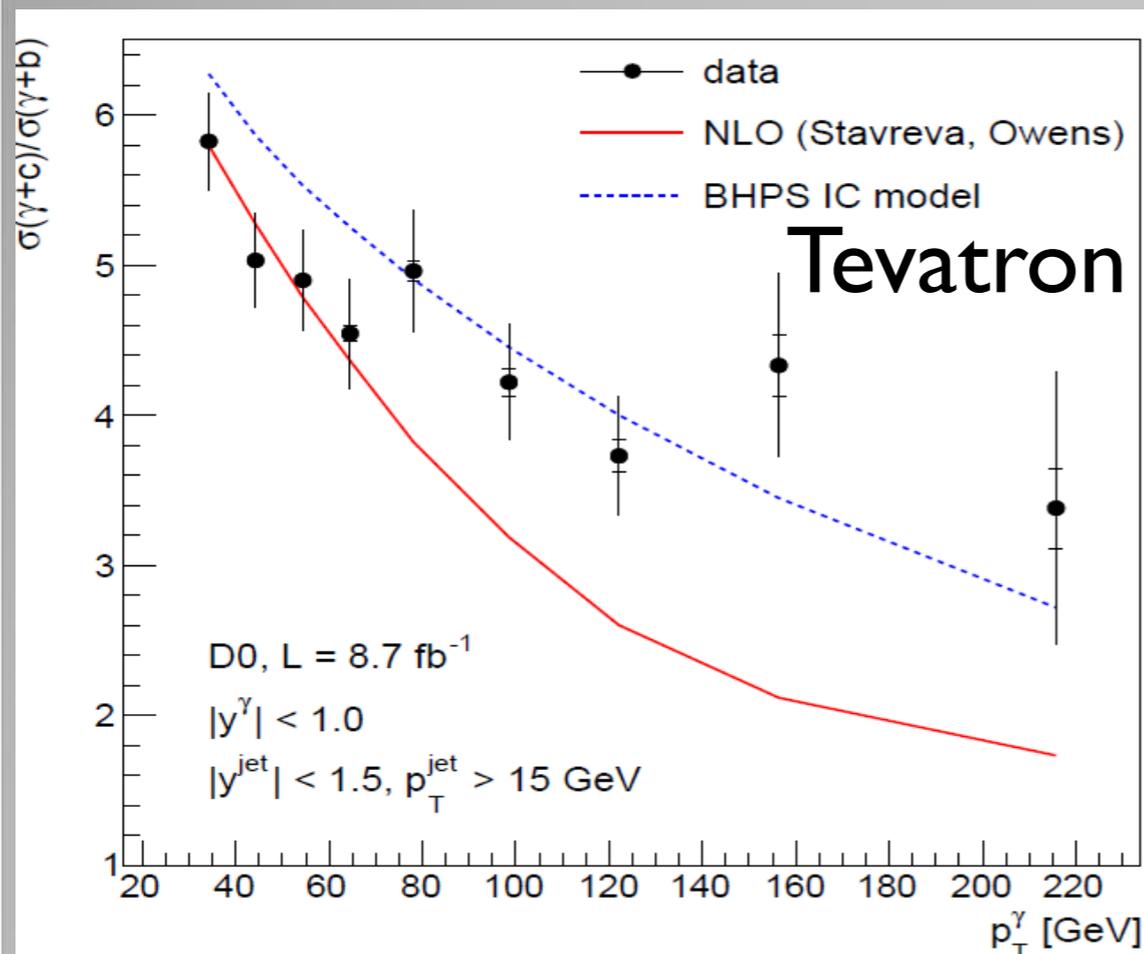
p_T –spectrum in
 $pp \rightarrow \gamma + c(\text{jet}) + X$



*V.A. Bednyakov, M.A. Demichev, G.I. Lykasov,
 T. Stavreva, M. Stockton, Phys.Lett. B728
 (2014) 602 (right).*

$R = \sigma(\gamma + c) / \sigma(\gamma + b)$ for $p \bar{p} \rightarrow \gamma + Q$ at $s^{1/2} = 1.98 \text{ TeV}$ (left)

$R = \sigma(\gamma + c) / \sigma(\gamma + b)$ for $pp \rightarrow \gamma + Q$ at $s^{1/2} = 8 \text{ TeV}$ (right)



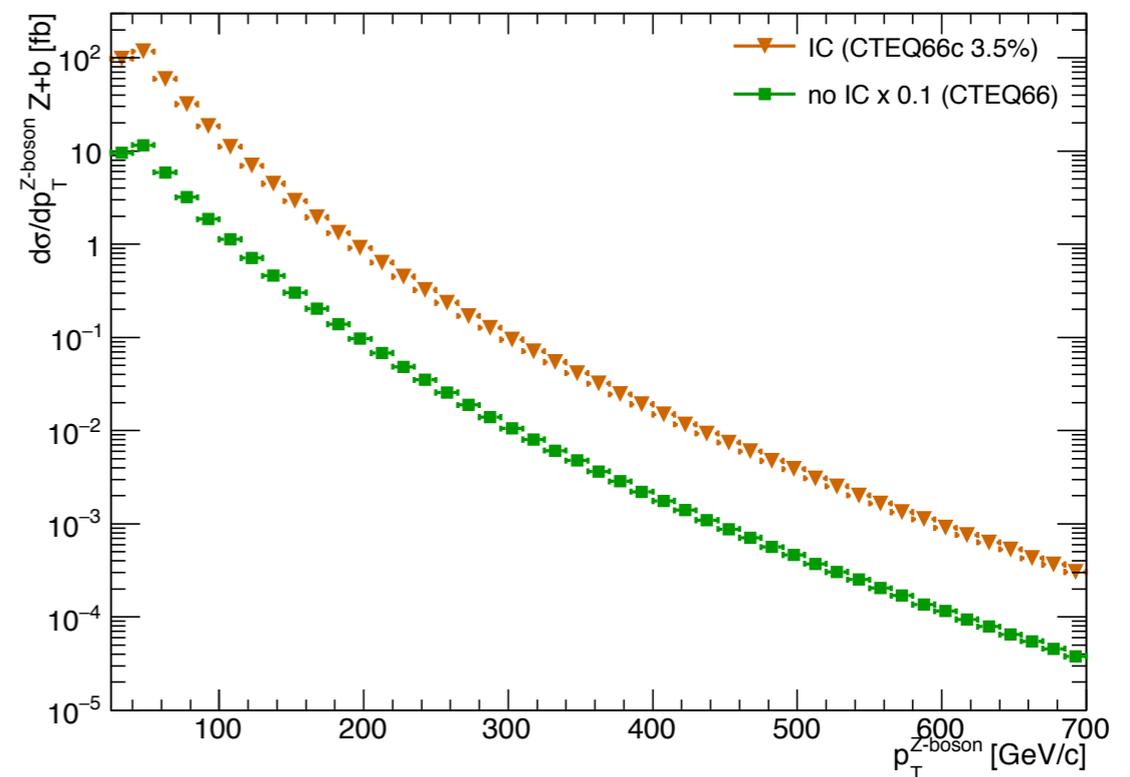
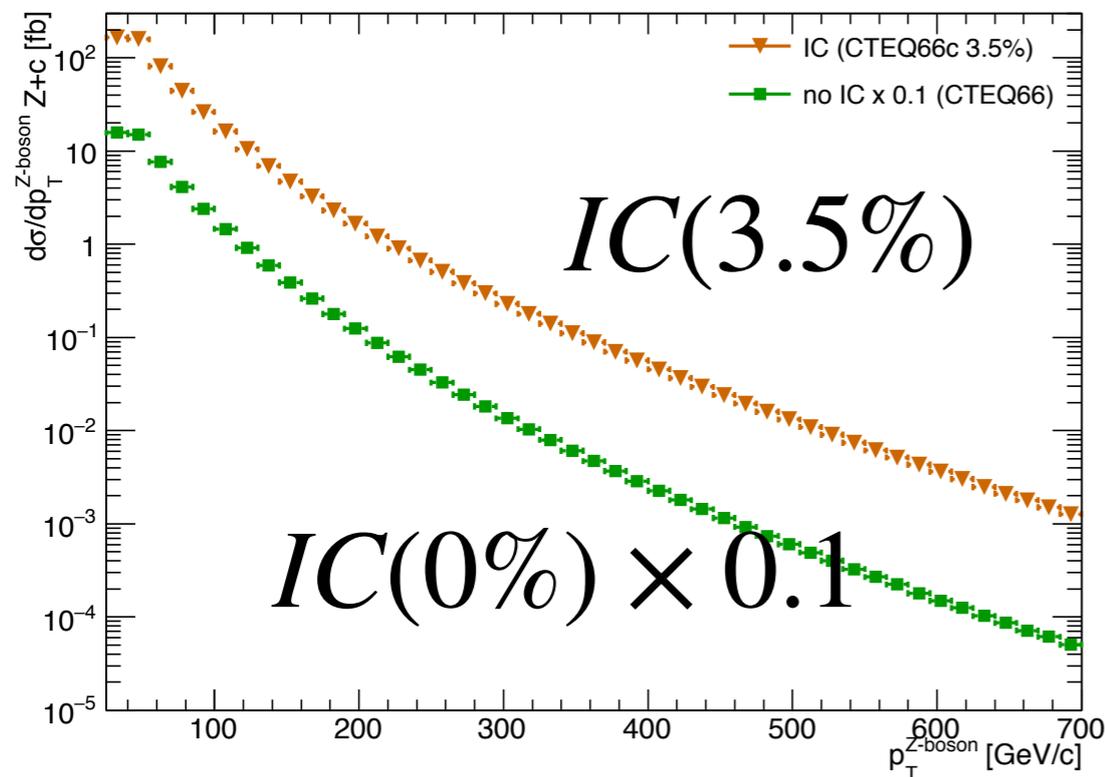
V.M. Abazov, et al. (D0) Phys.Lett. B719 (2013) 354 .

$$\frac{\sigma(pp \rightarrow \gamma c X)}{\sigma(pp \rightarrow \gamma b X)}$$

A.V. Lipatov, G.I. Lykasov, Yu.Yu. Stepanenko, V.A. Bednyakov, Phys.Rev. D94, 053011 (2016); S.J. Brodsky, V.A. Bednyakov, G.I. Lykasov, J. Smiesko, S. Tokar, arXiv:1612.01351, Prog. Part. Nucl. Phys. in press

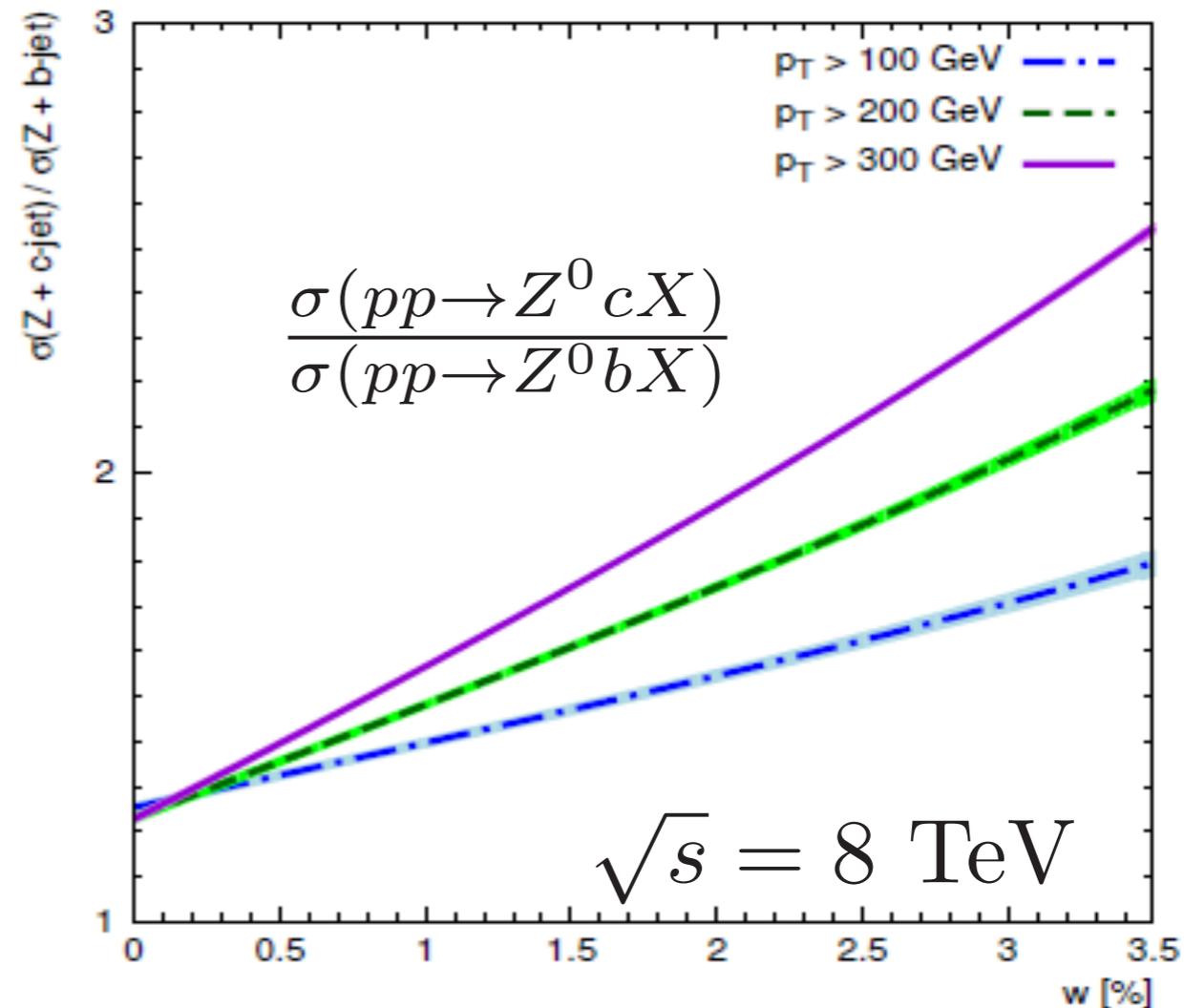
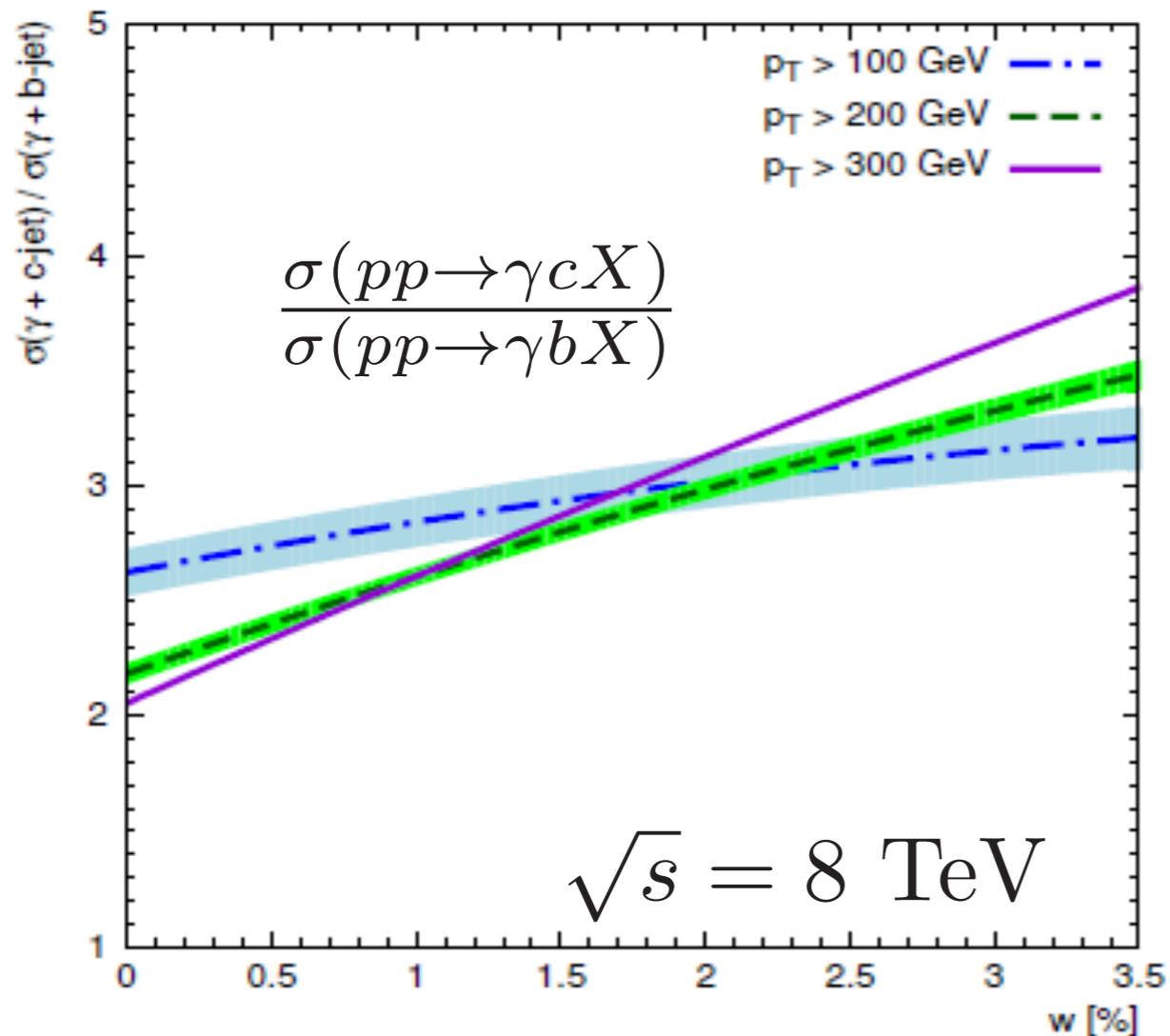
$$\frac{d\sigma}{dp_T}(pp \rightarrow Z + c + X)(fb)$$

$$\frac{d\sigma}{dp_T}(pp \rightarrow Z + b + X)(fb)$$



The cross-sections of the associated $Z+c$ (left) and $Z+b$ (right) production in pp collision calculated as a function of the Z boson transverse momentum p_T at $\sqrt{s} = 13$ TeV within the MCFM routine.

$$\sqrt{s} = 13 \text{ TeV}$$



Ratio between the x-sections of $\gamma + c$ and $\gamma + b$ production in p-p collision at $s^{1/2} = 8$ TeV integrated over p_T . (left) and the similar ratio between $Z+c$ and $Z+b$ production cross sections (right). Bands mean the QCD scale uncertainty .

A.V.Lipatov, G.I.Lykasov, Yu.Yu.Stepanenko, V.A.Bednyakov,
Phys.Rev. D94 , 053011 (2016) ;

S.J.Brodsky, V.A.Bednyakov, G.I.Lykasov, J.Smiesko, S.Tokar,
arXiv:1612.01351 , Prog. Part.Nucl.Phys. in press

Why is Intrinsic Heavy Quark Phenomena Important?

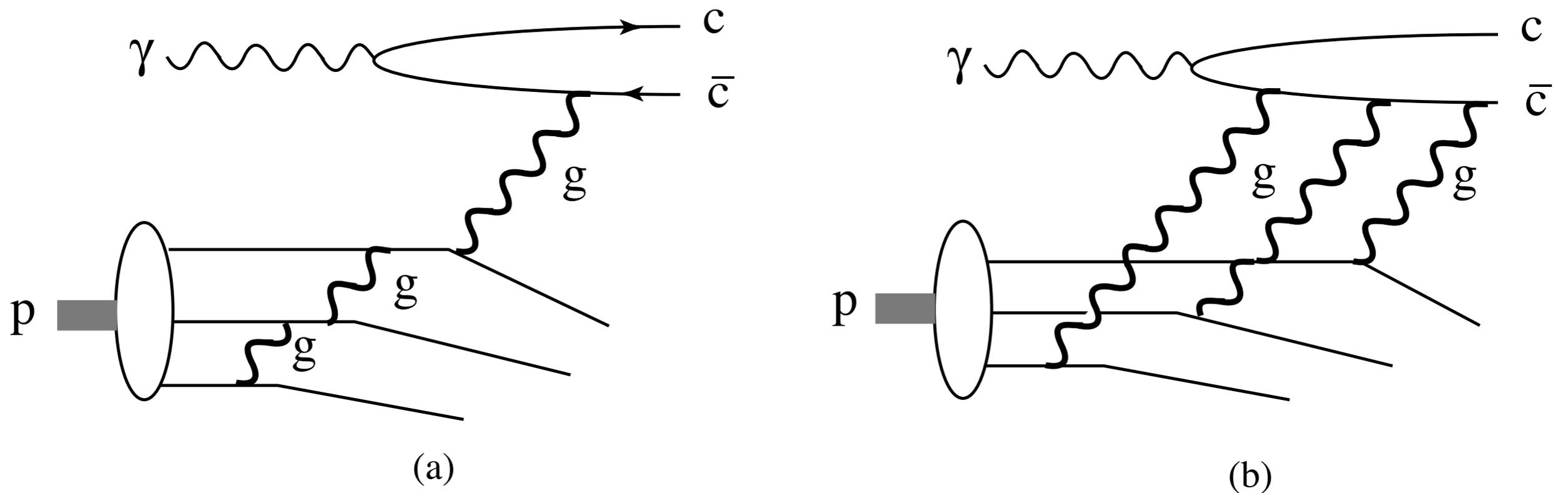
- **Test Fundamental QCD predictions OPE, Non-Abelian QCD**

$$\text{Non-Abelian: } P_{Q\bar{Q}} \propto \frac{1}{M_{Q\bar{Q}}^2} \quad \text{Abelian: } P_{Q\bar{Q}} \propto \frac{1}{M_{Q\bar{Q}}^4}$$

- **Test non-perturbative effects**
- **Important for correctly identifying the gluon distribution**
- **High- x_F open and hidden charm and bottom; discover exotic states**
- **Explain anomalous high p_T charm jet + γ data at Tevatron**
- **Important source of high energy ν at IceCube**

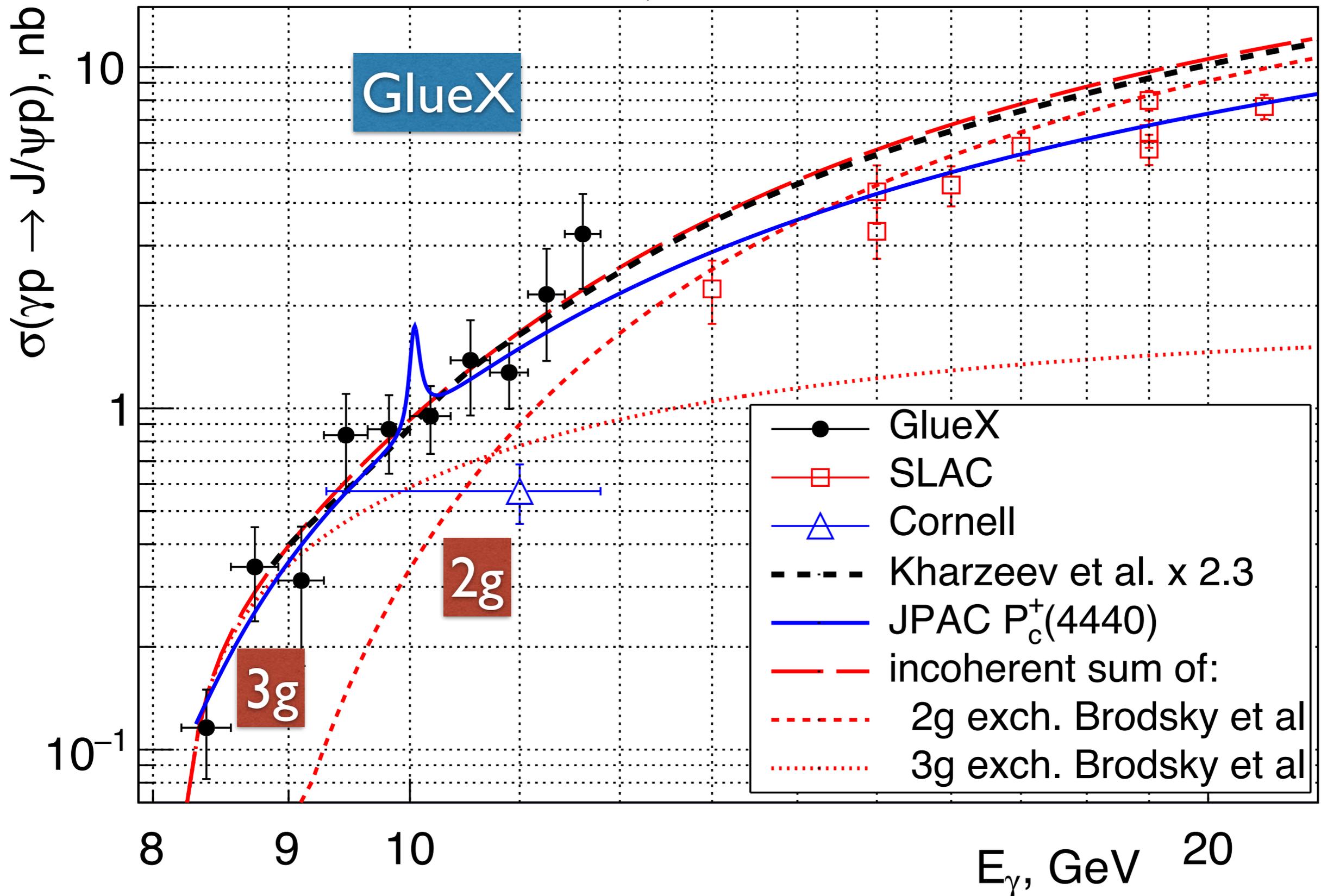
Photoproduction of charm near threshold

S. J. Brodsky,¹ E. Chudakov,² P. Hoyer,³ J.M. Laget,⁴



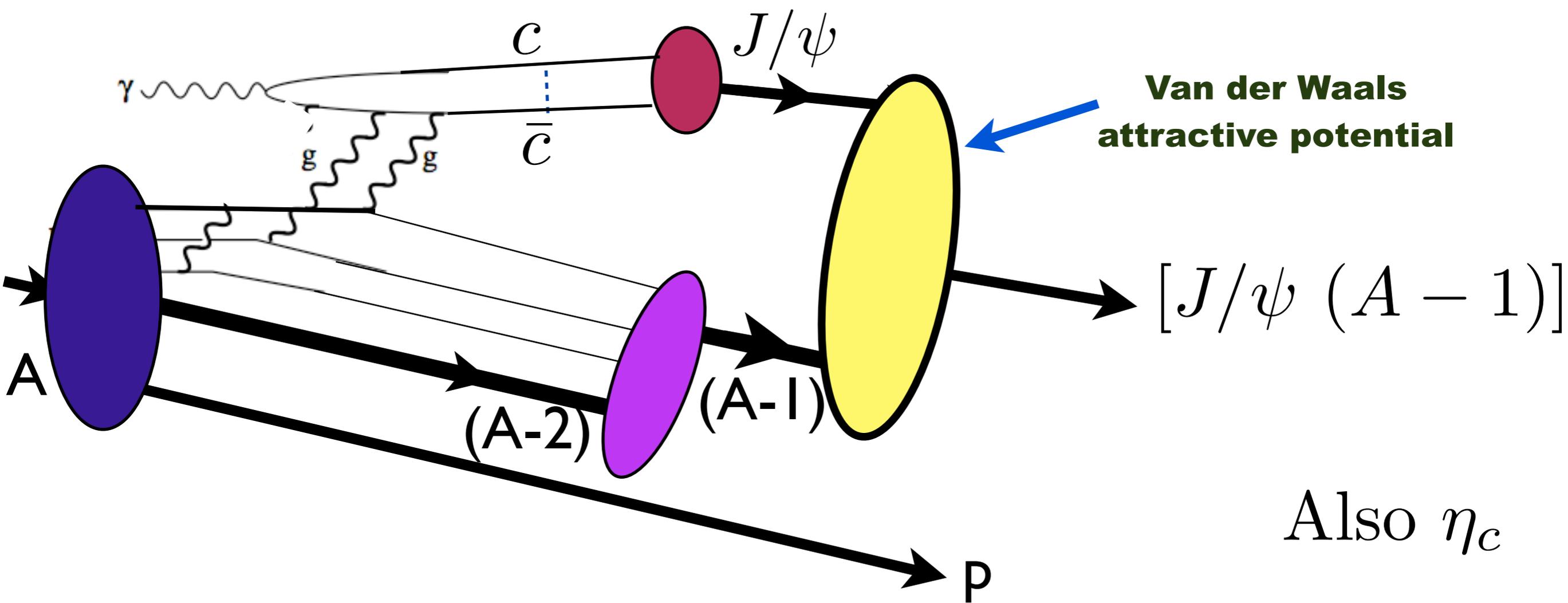
Another aspect of IC

First measurement of near-threshold J/ψ exclusive photoproduction off the proton



GlueX results for the J/ψ total cross section vs beam energy, compared to the Cornell [15] and SLAC [16] data, the theoretical predictions [11, 13], and the JPAC model [6] corresponding to $\mathcal{B}(P_c^+(4440) \rightarrow J/\psi p) = 1.6\%$ for the $J^P = 3/2^-$ case as discussed in the text. All curves are fitted/scaled to the GlueX data only. For our data the quadratic sums of statistical and systematic errors are shown; the overall normalization uncertainty is 27%.

Charmonium Production at Threshold



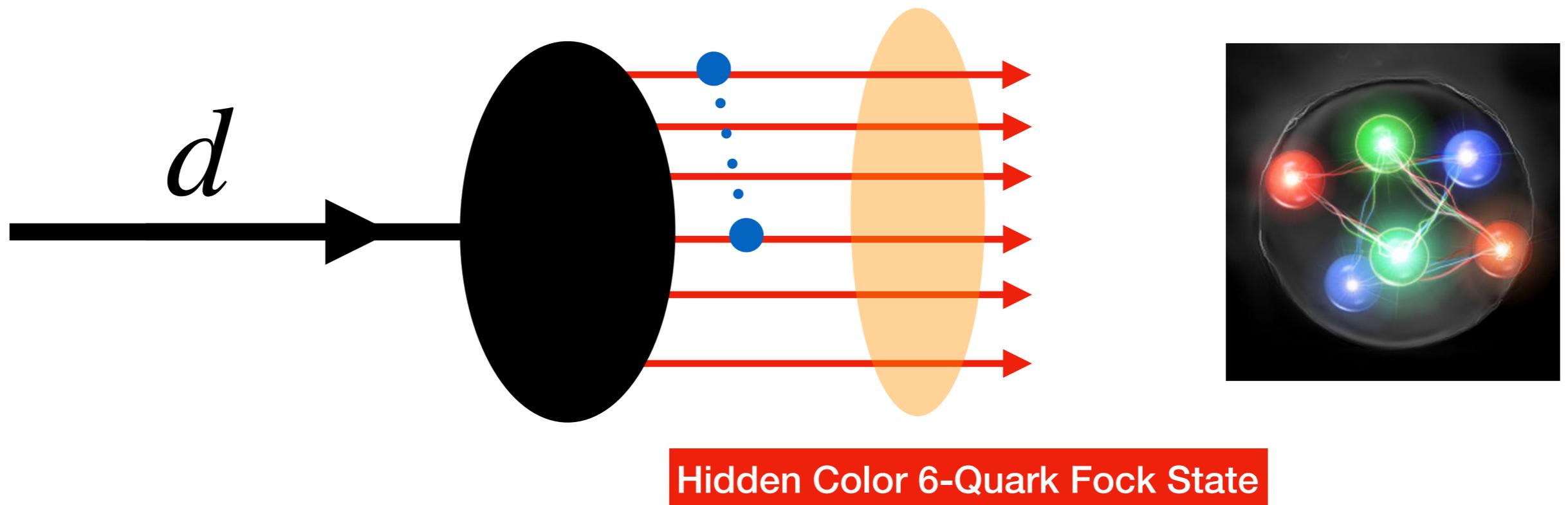
Also η_c



Form nuclear bound-charmonium bound state!

Hidden Color in QCD

- Deuteron: Five color-singlet combinations of 6 color-triplets
- One Fock state is n-p nucleon cluster, one state is Δ - Δ

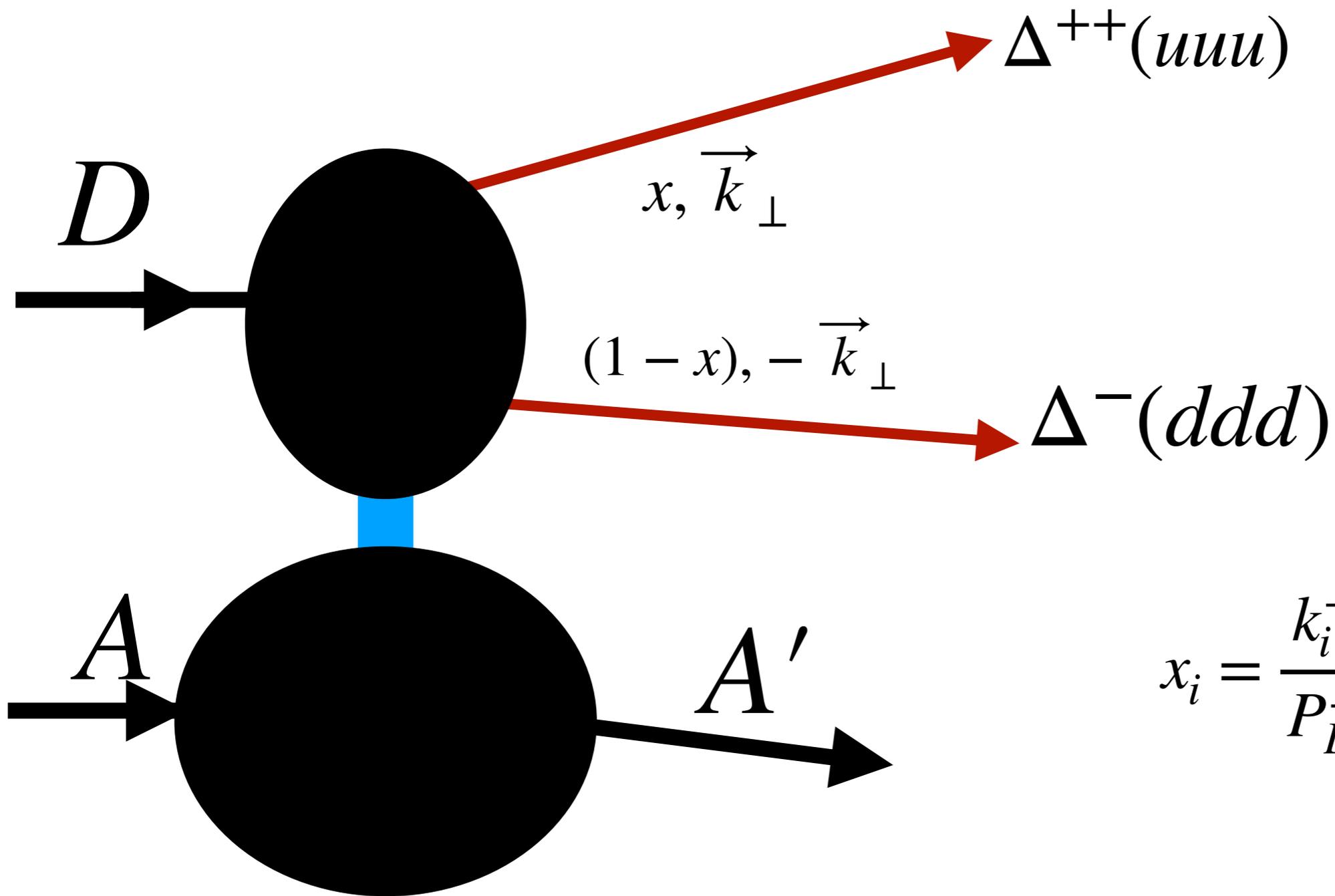


Rigorous Feature of QCD!

Lepage, Ji, sjb

Measure Hidden-Color Fock state of the Deuteron LFWF

$$\psi_D^{\Delta\Delta}(x, \vec{k}_\perp) = \langle \Delta^{++}(x, \vec{k}_\perp) \Delta^-(1-x, -\vec{k}_\perp | \Psi_D \rangle$$



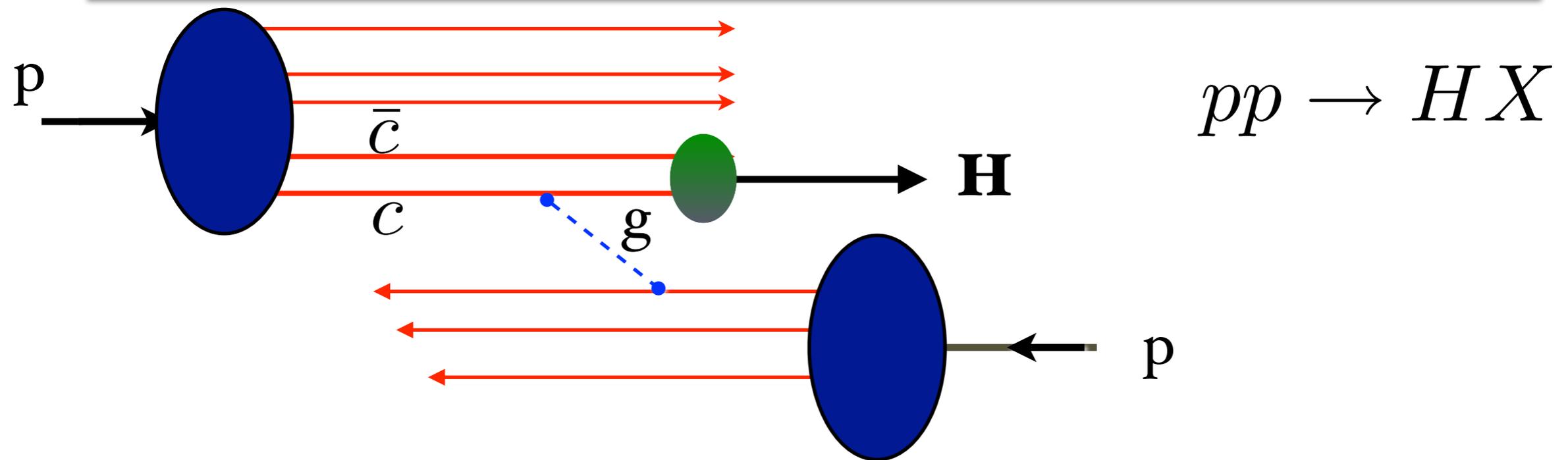
$$x_i = \frac{k_i^+}{P_D^+} = \frac{k_i^0 + k_i^z}{P_D^0 + P_D^z}$$

$$D + A \rightarrow \Delta^{++} \Delta^- + A' \quad \text{Measure } \mathcal{M}_{pn}^2 = (p_{\Delta^{++}} + p_{\Delta^-})^2 = \frac{k_\perp^2 + M_\Delta^2}{x(1-x)}$$

- IC Explains Anomalous $\alpha(x_F)$ not $\alpha(x_2)$ dependence of $pA \rightarrow J/\psi X$
(Mueller, Gunion, Tang, SJB)
- Color Octet IC Explains $A^{2/3}$ behavior at high x_F (NA3, Fermilab) *Color Opacity*
(Kopeliovitch, Schmidt, Soffer, SJB)
- IC Explains $J/\psi \rightarrow \rho\pi$ puzzle
(Karliner, SJB)
- IC leads to new effects in B decay
(Gardner, SJB)

Higgs production at $x_F = 0.8$

Intrinsic Heavy Quark Contribution to Inclusive Higgs Production



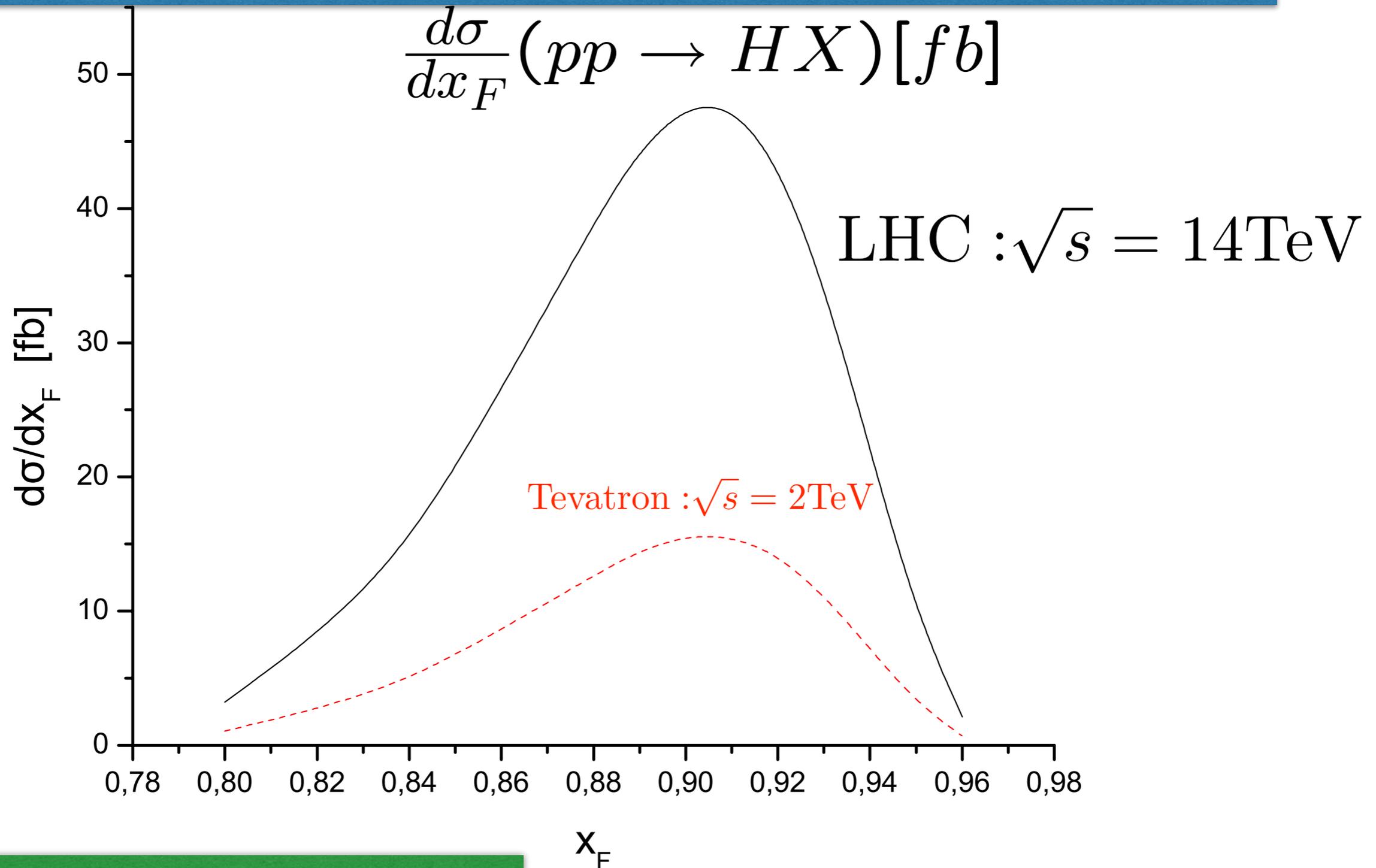
Also: intrinsic strangeness, bottom, top

Higgs can have > 80% of Proton Momentum!

New production mechanism for Higgs at the LHC

AFTER: Higgs production at threshold!

Intrinsic Heavy Quark Contribution to High x_F Inclusive Higgs Production



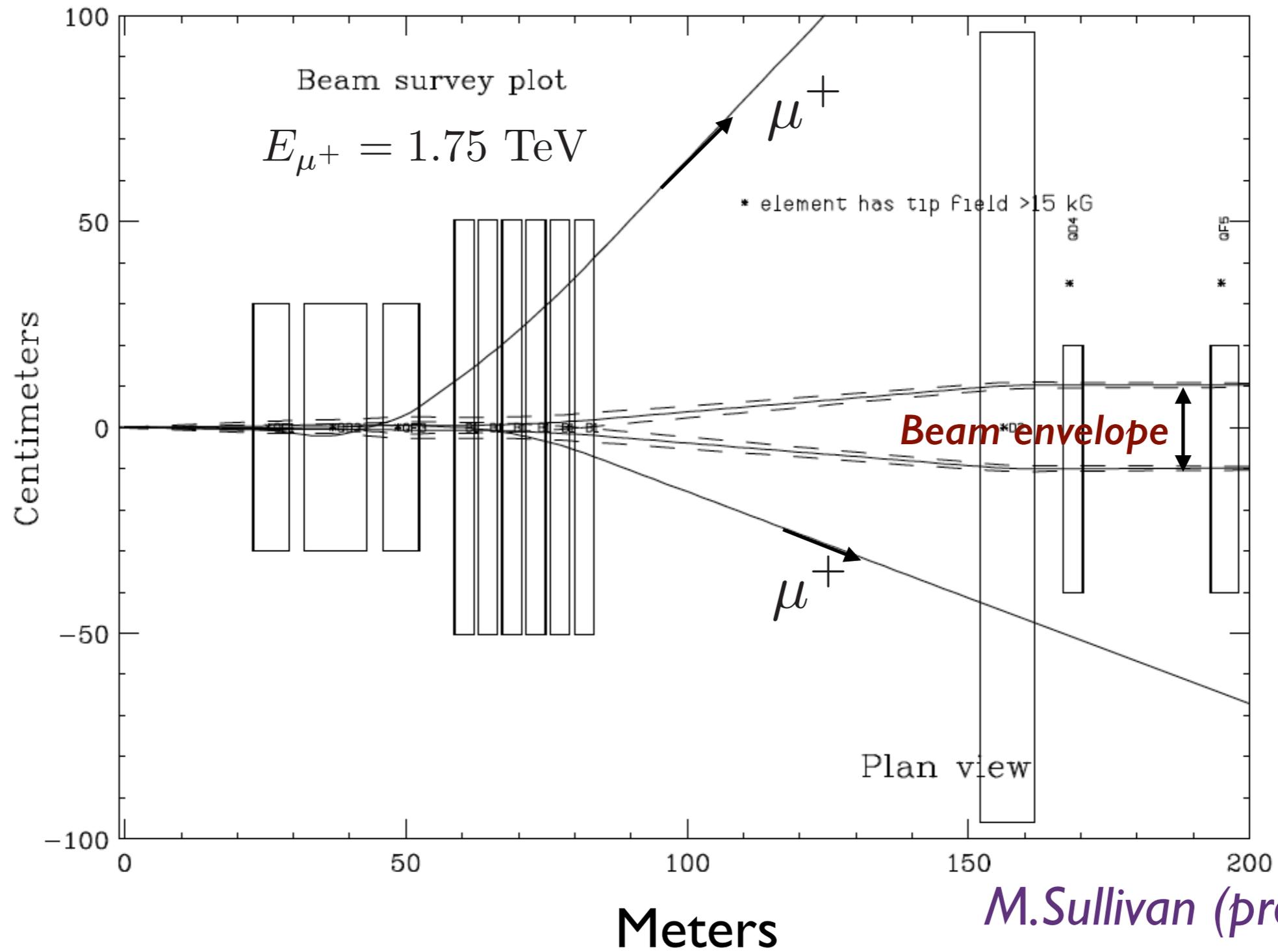
Need High x_F Acceptance

Most practical: Higgs to 4 muons

Goldhaber, Kopeliovich,
Schmidt, Soffer, sjb

Use LHC Magnetic Field as Downstream Muon Spectrometer

$$pp \rightarrow H X \rightarrow \mu^+ \mu^- \mu^+ \mu^- X$$



M.Sullivan (preliminary)

Measure exotic events at SMOG@LHCb such as

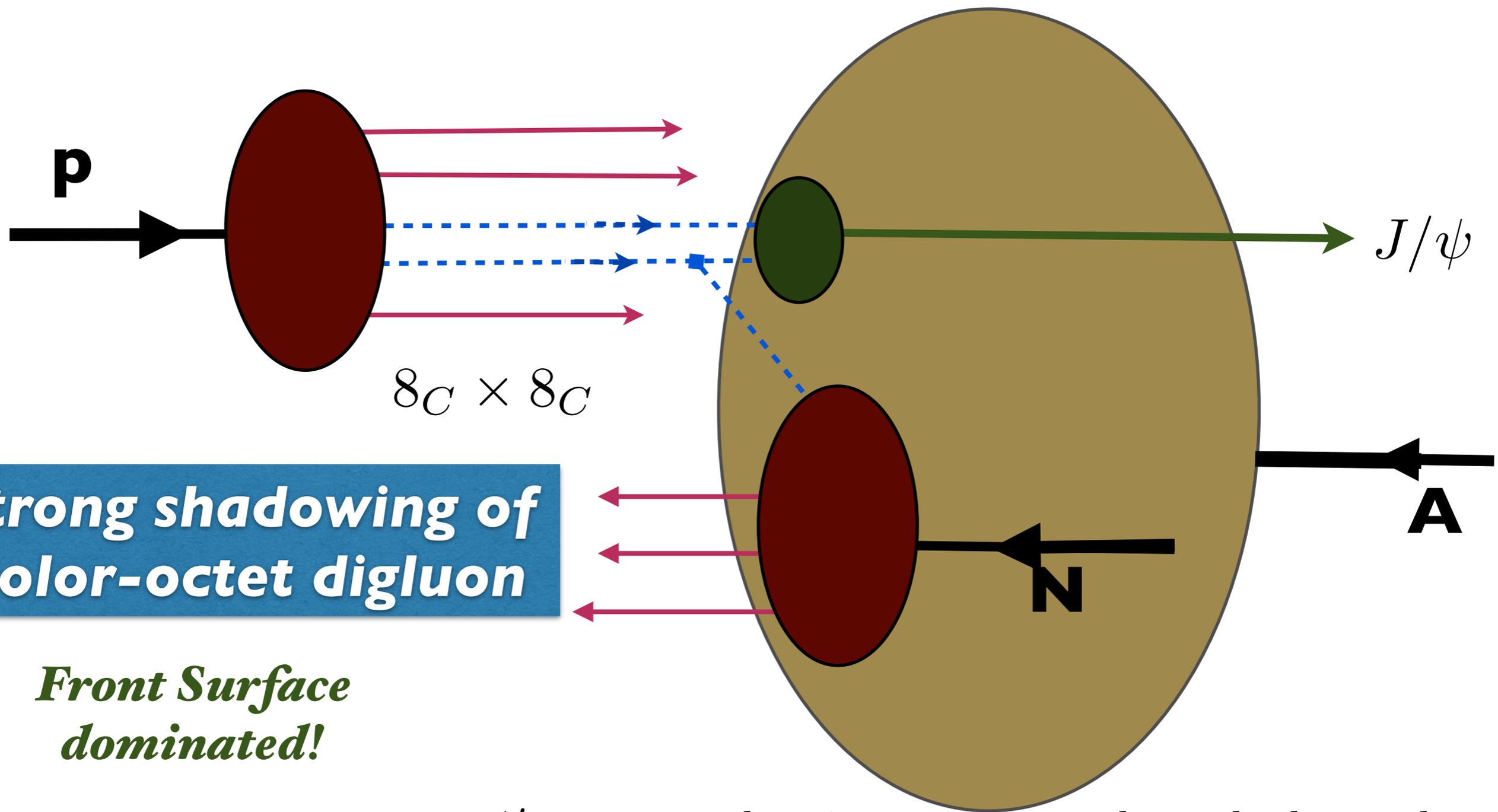
$$pA \rightarrow \Upsilon + J/\psi X \rightarrow \mu^+ \mu^- \mu^+ \mu^- X$$

Digluon-initiated subprocess!

**Forward
rapidity $y \sim 4$**

Another mechanism

$$pA \rightarrow J/\psi X$$
$$(gg)_{8_C} + g_{8_C} \rightarrow J/\psi$$



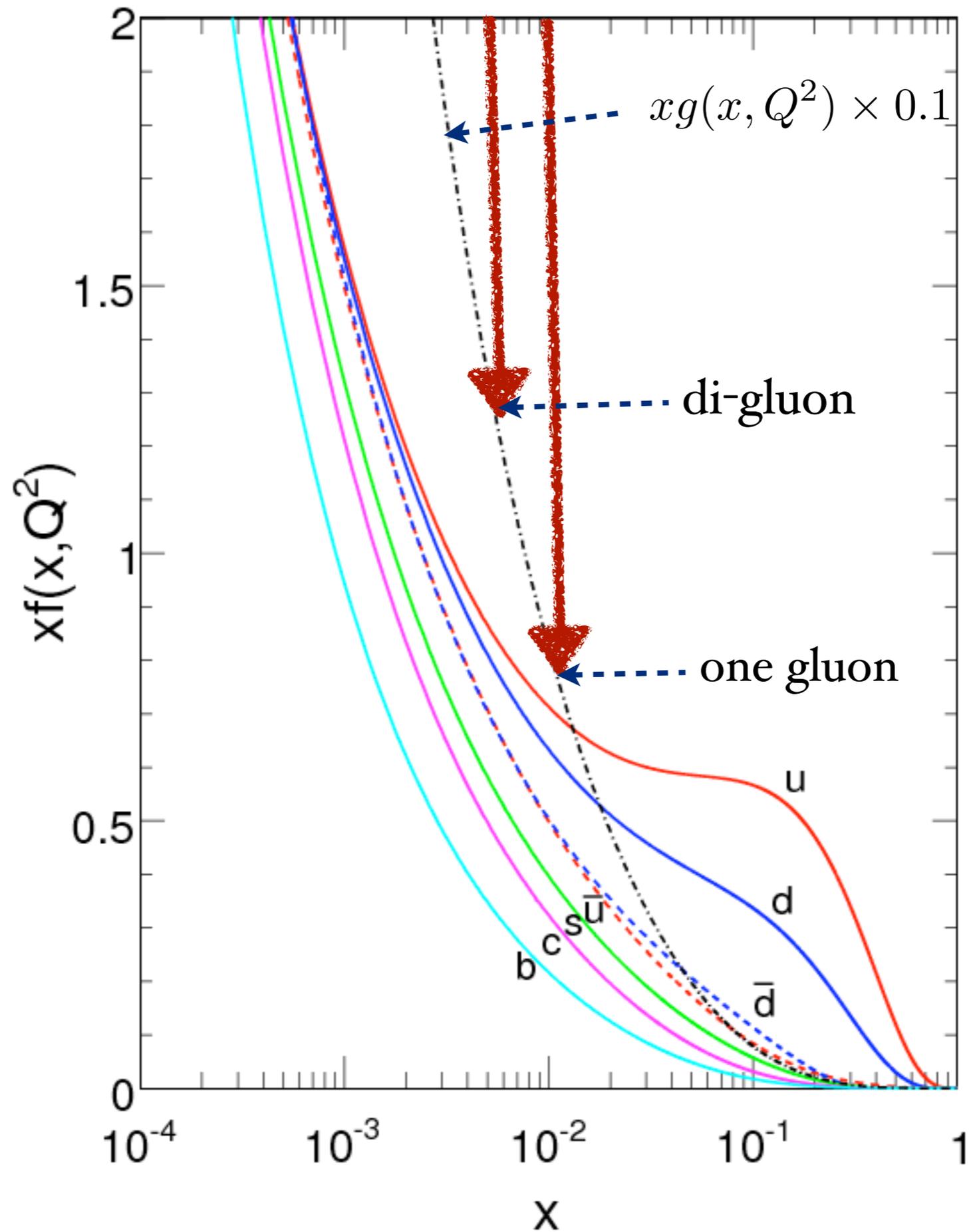
**Strong shadowing of
color-octet digluon**

**Front Surface
dominated!**

**Crossing: Diffractive
& pomeron exchange**

ψ' suppressed as it propagates through the nucleus

Two gluons at $g(0.005) \sim \frac{13}{0.005} = 2600$ vs. one gluon at $g(0.01) \sim \frac{8}{0.01} = 800$

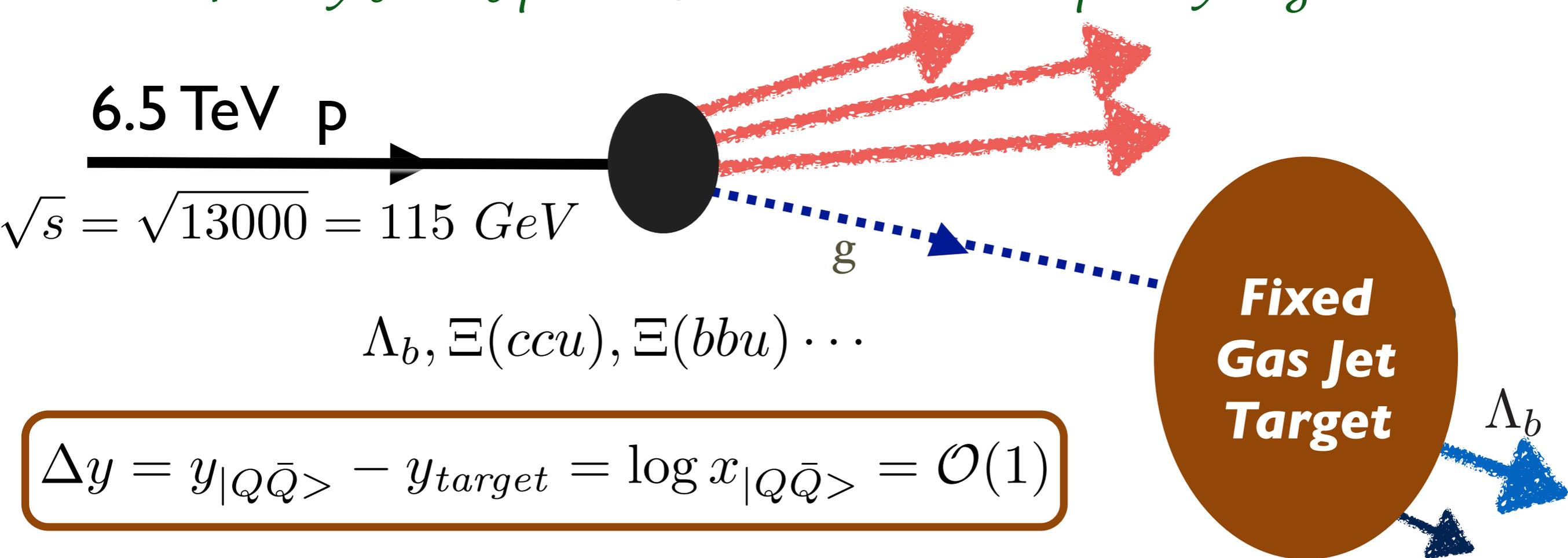


Excitation of Intrinsic Heavy Quarks in a Fixed Target

*Amplitude maximal at minimal invariant mass,
in target rapidity domain!*

$$x_i \sim \frac{m_{\perp i}}{\sum_j^n m_{\perp j}} \quad \frac{d\sigma}{dy_{J/\psi}} (pA \rightarrow J/\psi X)$$

Heavy states produced in TARGET rapidity region



Produce $J/\psi, \Upsilon, \Lambda_c, \Lambda_b, |ccu\rangle, |cud\bar{c}\rangle, |cuudddu\bar{c}\rangle, \dots$

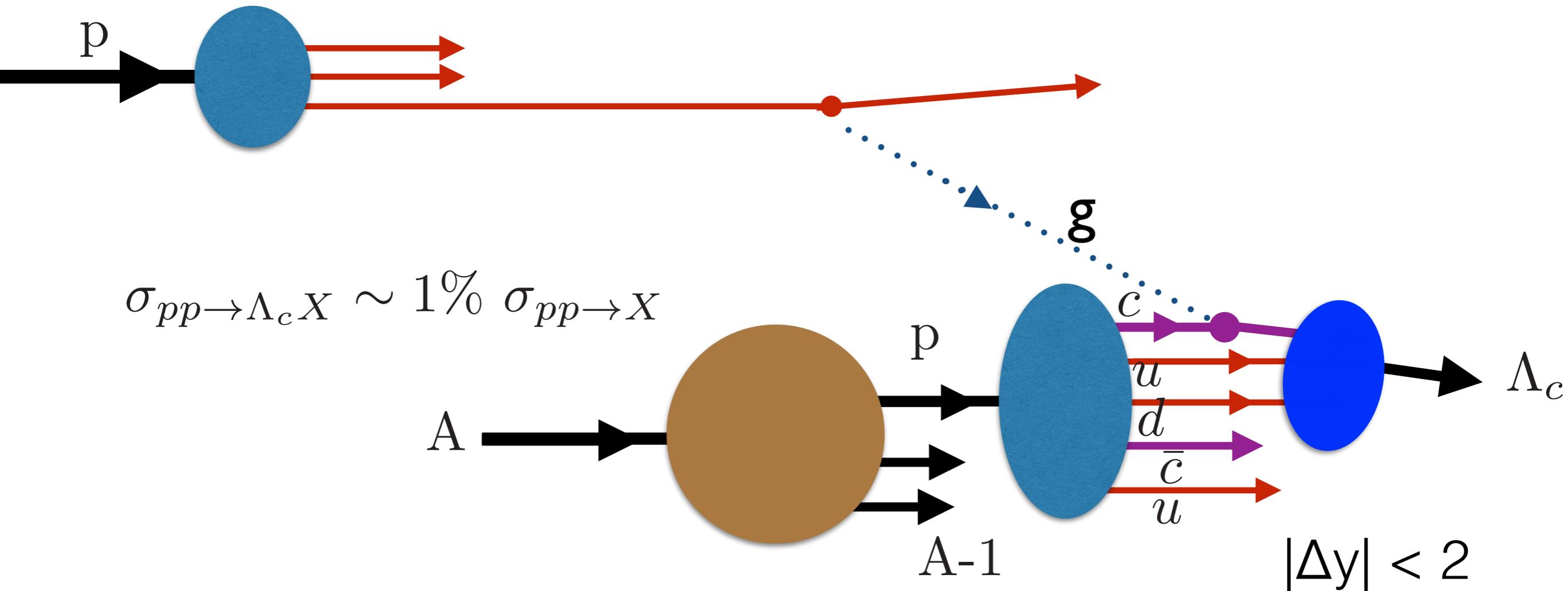
Test at Smog@LHCb

discussions with M. Williams

$$pA \rightarrow \Lambda_c X$$

$$E_p = 6.5 \text{ TeV}$$

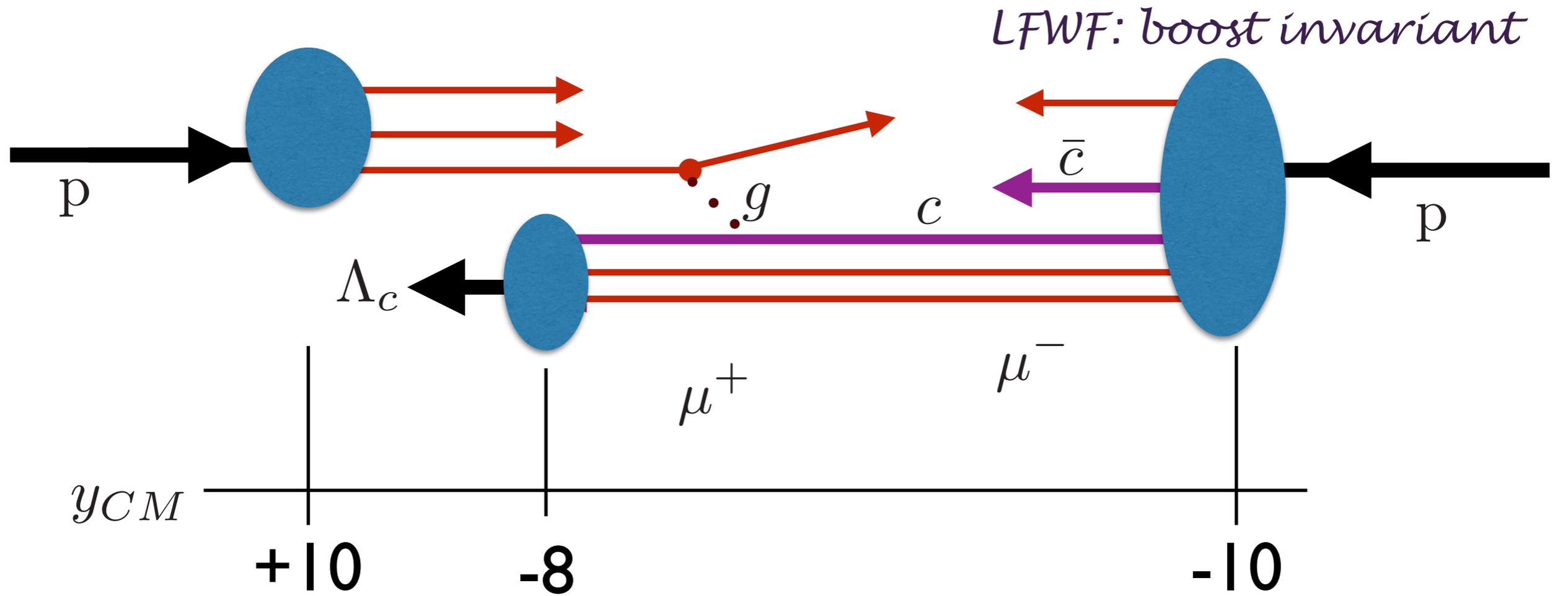
p



SMOG target at rest

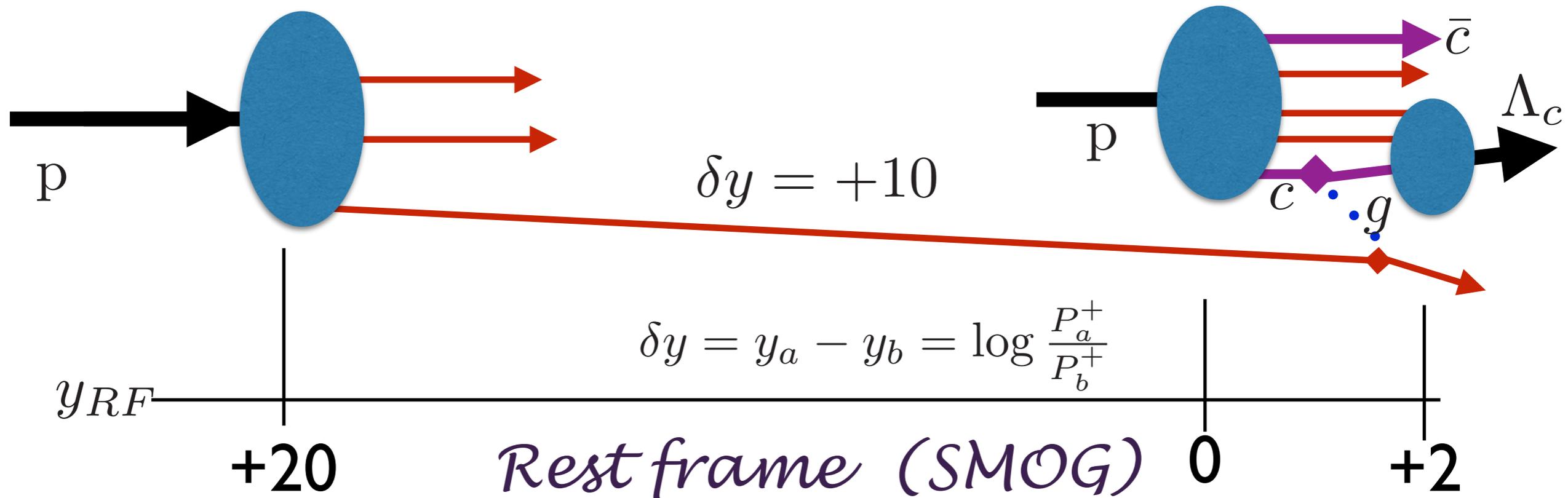
Intrinsic heavy quark probability in the nucleon maximal at minimum off-shellness

Quarkonium produced nearly at rest — has small rapidity in target rest frame



$ISR \ x_F(\Lambda_c) = 0.8$

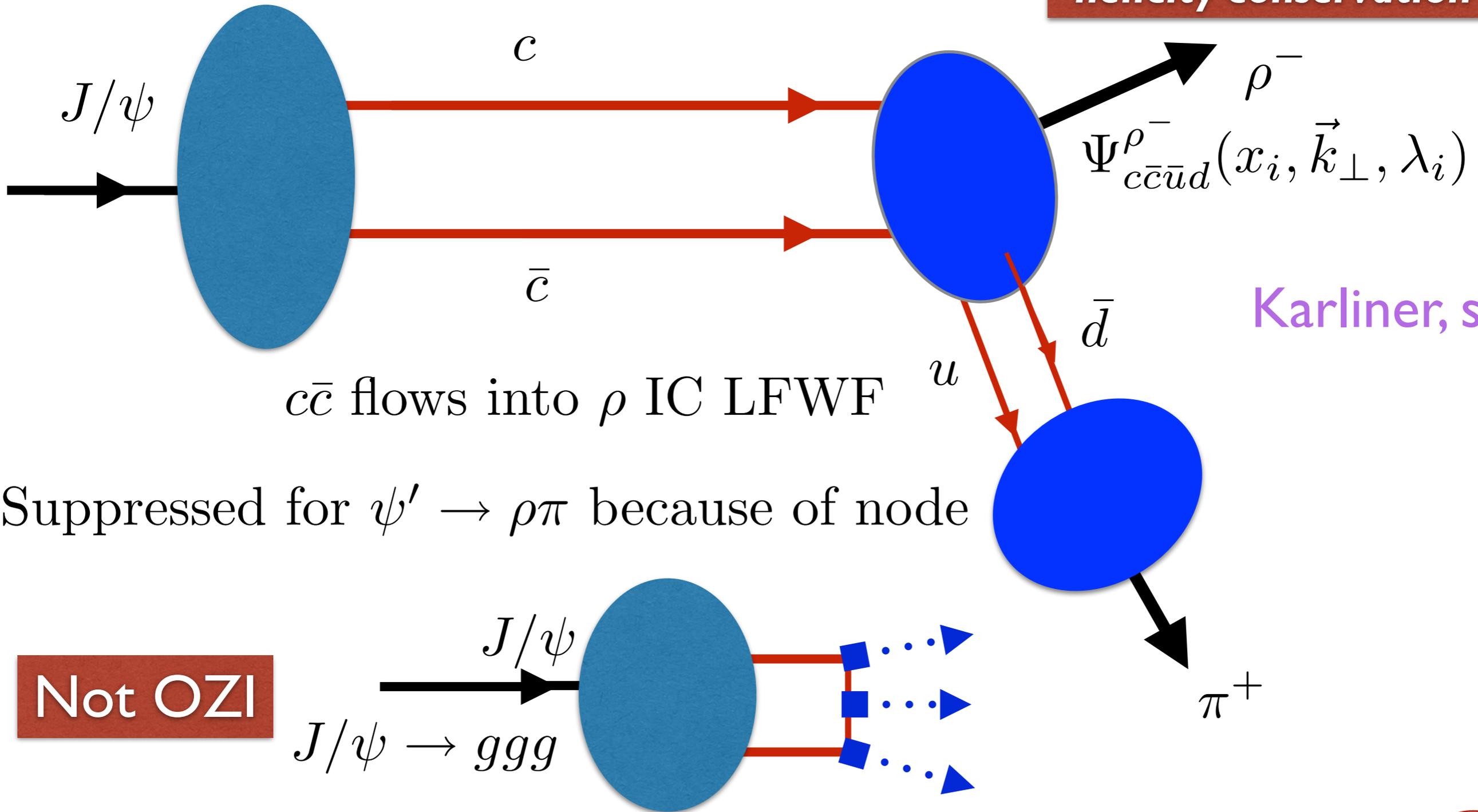
CM frame



J/ψ to $\rho\pi$ Puzzle

$$\frac{\Gamma(\psi(2S) \rightarrow \rho\pi)/\Gamma_{\text{tot}}}{\Gamma(J/\psi \rightarrow \rho\pi)/\Gamma_{\text{tot}}} = \frac{3.2 \pm 1.2 \times 10^{-5}}{1.69 \pm 0.15 \times 10^{-2}} \simeq 0.2\%$$

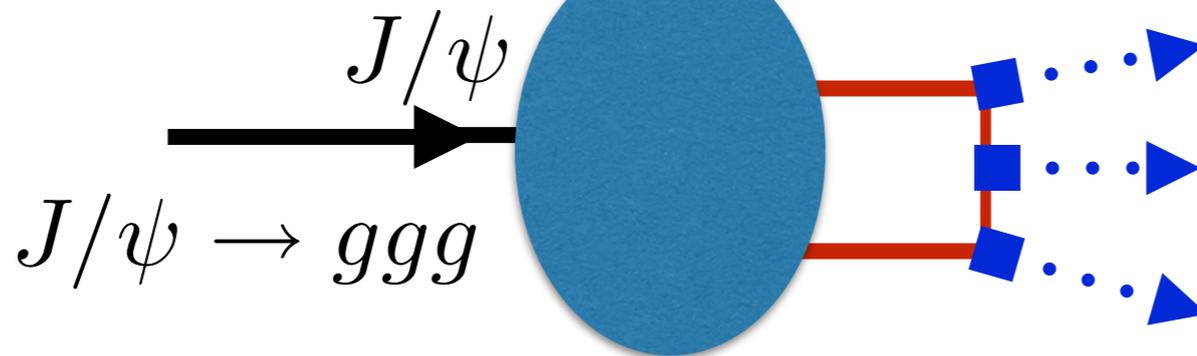
Not 13%
VP decay violates
hadron
helicity conservation



Karliner, sjb

Suppressed for $\psi' \rightarrow \rho\pi$ because of node

Not OZI



Novel Features of Heavy Quark Phenomenology

Vast array of novel physics studies at LHCb and SMOG@LHCb

- Heavy Quark Phenomena: Intrinsic + Extrinsic
- High-x Gluon Distributions
- Exotic Heavy Quark Spectroscopy
- Higher Fock States of Proton and Nuclei
- Strangeness Asymmetry
- Novel Drell-Yan Studies
- Nuclear and Heavy Ion Effects: Ridge, baryon to meson
- Ultra-Peripheral Collisions
- Single-Spin Asymmetries
- Many Advantages of Fixed Target at LHC (AFTER and SMOG@LHCb)

Novel Drell-Yan Physics Topics at LHCb

- Sivers effect: sign change in single-spin asymmetry
- Double Boer-Mulders Effect: Double initial-state interactions at leading twist
- Breakdown of Lam Tung and factorization theorems
- Flavor-Dependent Antishadowing (Explains NuTeV?) $pA \rightarrow l\bar{l}X$
- Analogous effects in gluon subprocesses $gg \rightarrow Q\bar{Q}$

QCD Myths

- **Anti-Shadowing is Universal**
- **ISI and FSI are higher twist effects and universal**
- **High transverse momentum hadrons arise only from jet fragmentation -- baryon anomaly!**
- **Heavy quarks only from gluon splitting**
- **Renormalization scale cannot be fixed**
- **QCD condensates are vacuum effects**
- **QCD gives 10^{42} to the cosmological constant**
- **Colliding Pancakes**

Features of the Principle of Maximum Conformality

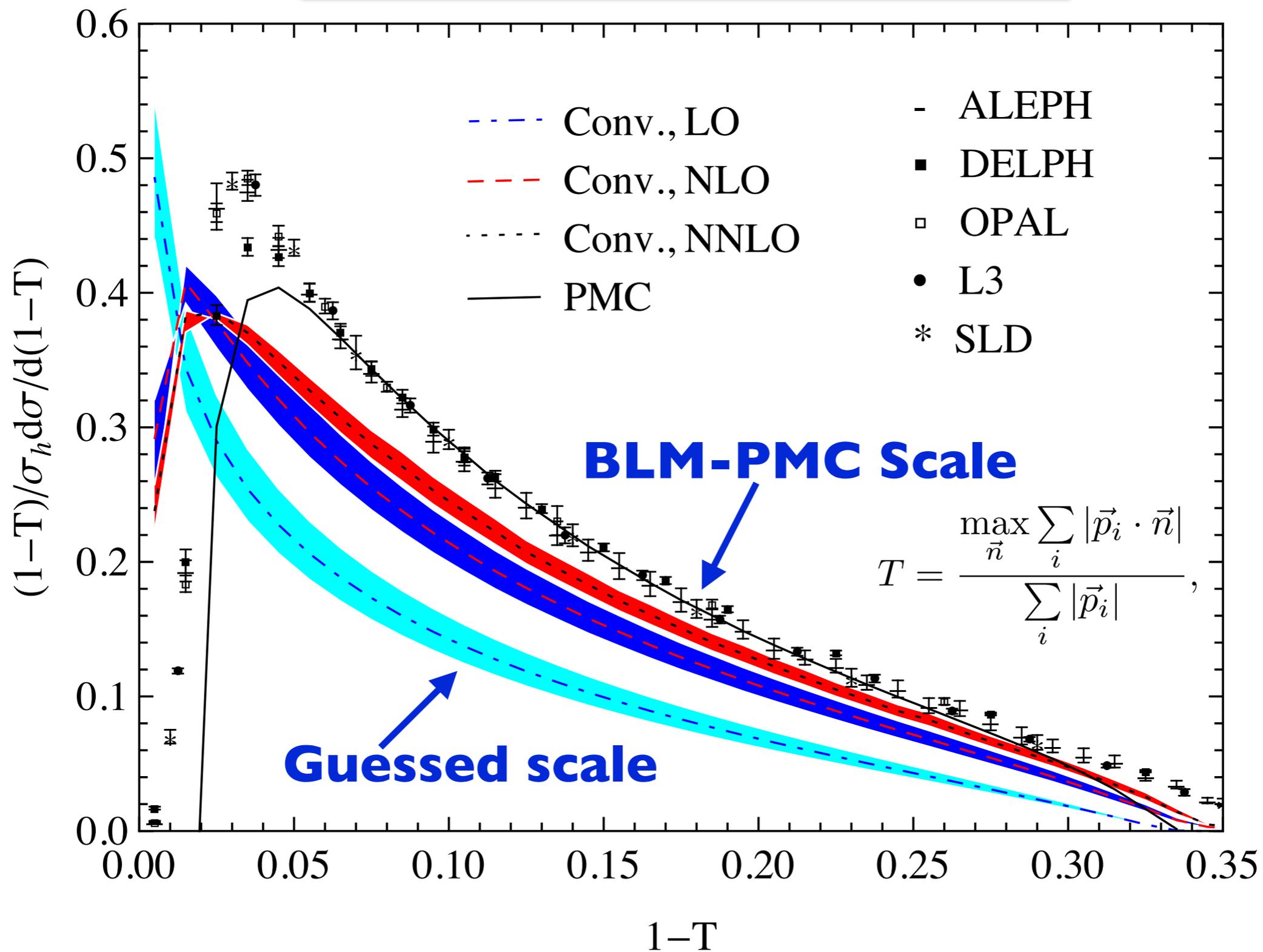
**Lepage, Mackenzie, sjb
Ellis, Gardi, Karliner, Samuel, sjb**

Wu, Mojaza, di Giustino, sjb

- **Predictions are scheme-independent**
- **Matches conformal series**
- **Commensurate Scale Relations between observables: Generalized Crewther Relation**
- **No $n!$ Renormalon growth**
- **New scale at each order; n_F determined at each order**
- **Multiple Physical Scales Incorporated**
- **Rigorous: Satisfies all Renormalization Group Principles**
- **Reduces to standard Gell-Mann — Low Scale Setting for $N_c=0$**
- **Realistic Estimate of Higher-Order Terms**
- **Eliminates unnecessary theory error**
- **Increases sensitivity to new physics**

T. Gehrmann, N. H'afliker, P. F. Monni

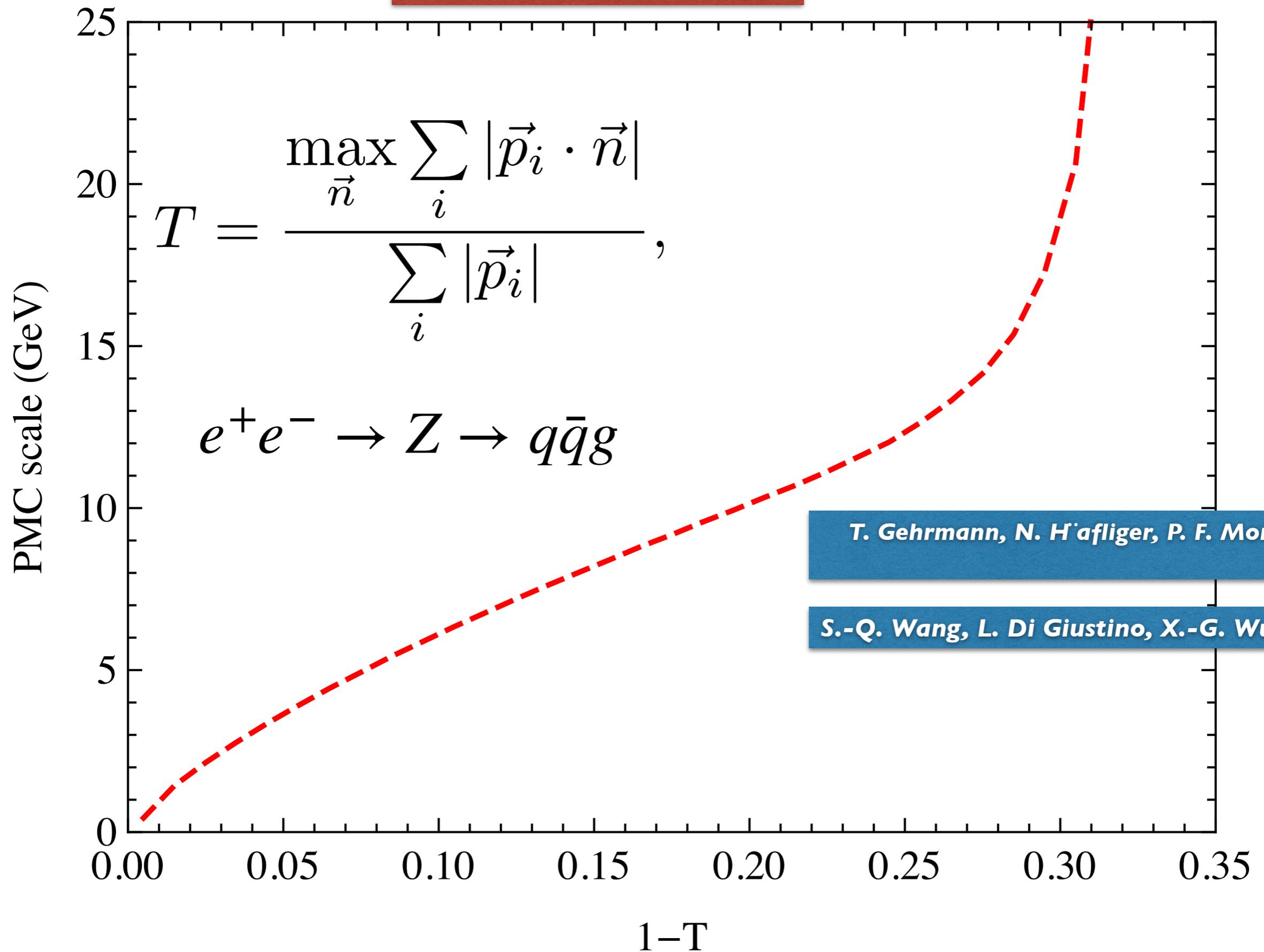
S.-Q. Wang, L. Di Giustino, X.-G. Wu, sjb

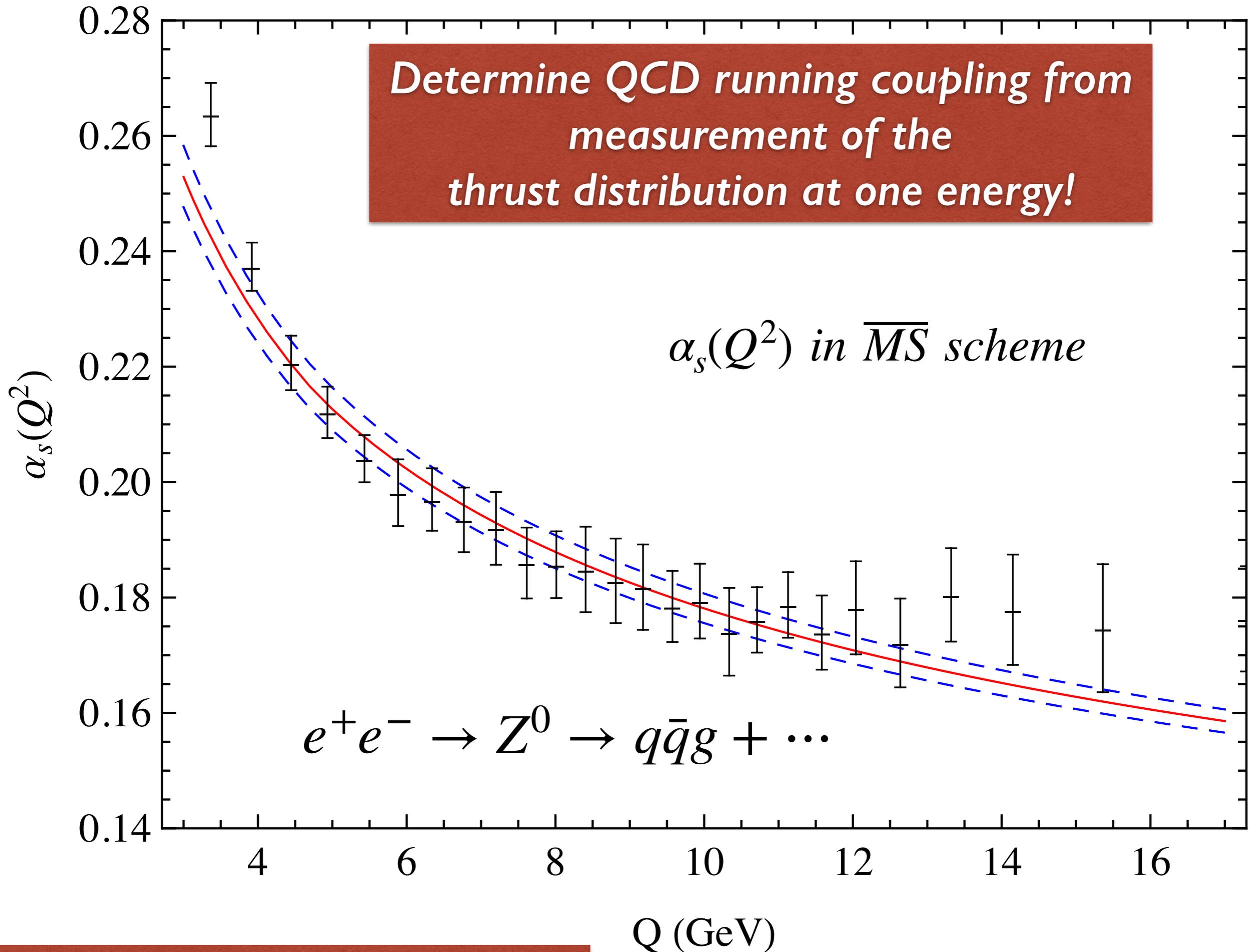


Principle of Maximum Conformality (PMC)

Renormalization scale depends on the thrust

Not constant

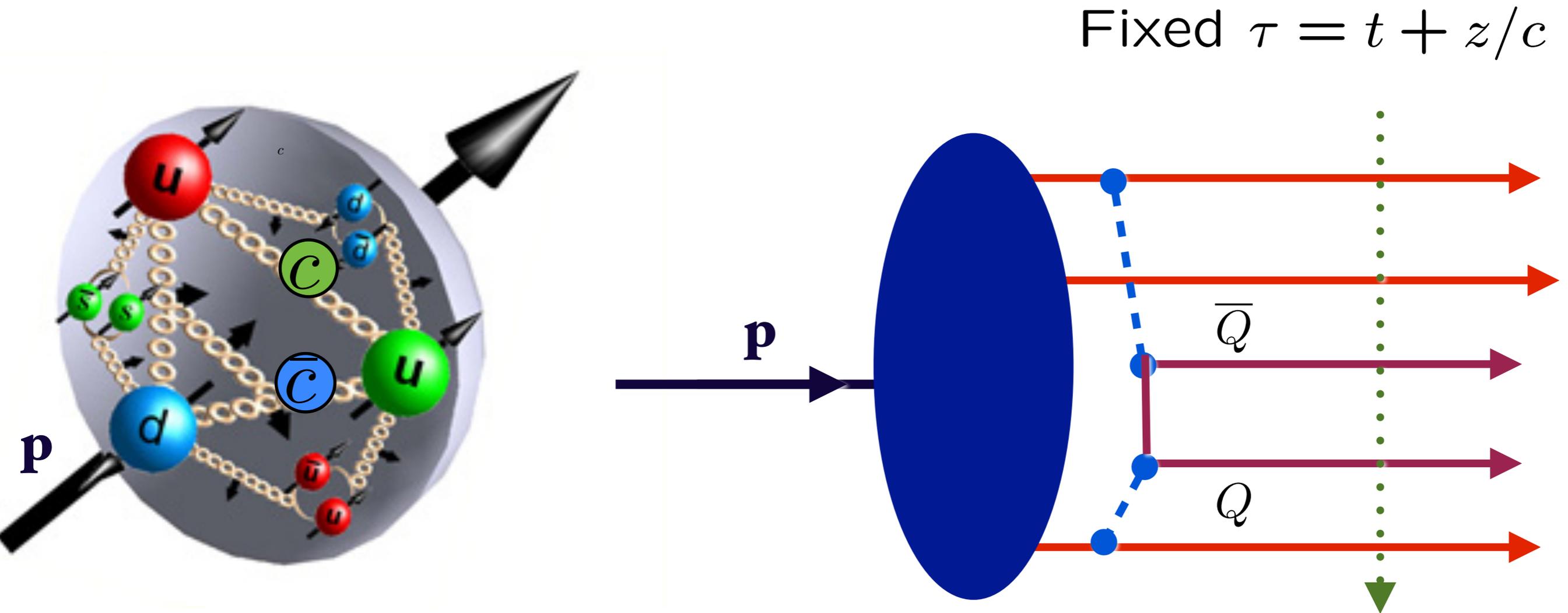




Invariance Principles of Quantum Field Theory

- **Polncarè Invariance:** *Physical predictions must be independent of the observer's Lorentz frame: Front Form*
- **Causality:** *Information within causal horizon: Front Form*
- **Gauge Invariance:** *Physical predictions of gauge theories must be independent of the choice of gauge*
- **Scheme-Independence:** *Physical predictions of a renormalizable theory must be independent of the choice of the renormalization scheme —Principle of Maximum Conformality (PMC)*
- **Mass-Scale Invariance:** *Conformal Invariance of the Action (DAFF)*

QCD, Heavy Flavors, and Higgs Production in the Very Forward Region



*Workshop on Forward Physics and QCD at the LHC,
the Future Electron Collider, and Cosmic Ray Physics*

Stan Brodsky

**Hotel Guanajuato,
Ciudad de Guanajuato,
Mexico**

November 18, 2019

