



# Binding energy studies of shell closures in exotic nuclei with ISOLTRAP

**Maxime Mougeot**  
**for the ISOLTRAP collaboration**

# Outline:

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- Introduction
- Neutron-rich Argon isotopes
- Evolution of  $N=28$  shell gap
- Conclusion and perspectives

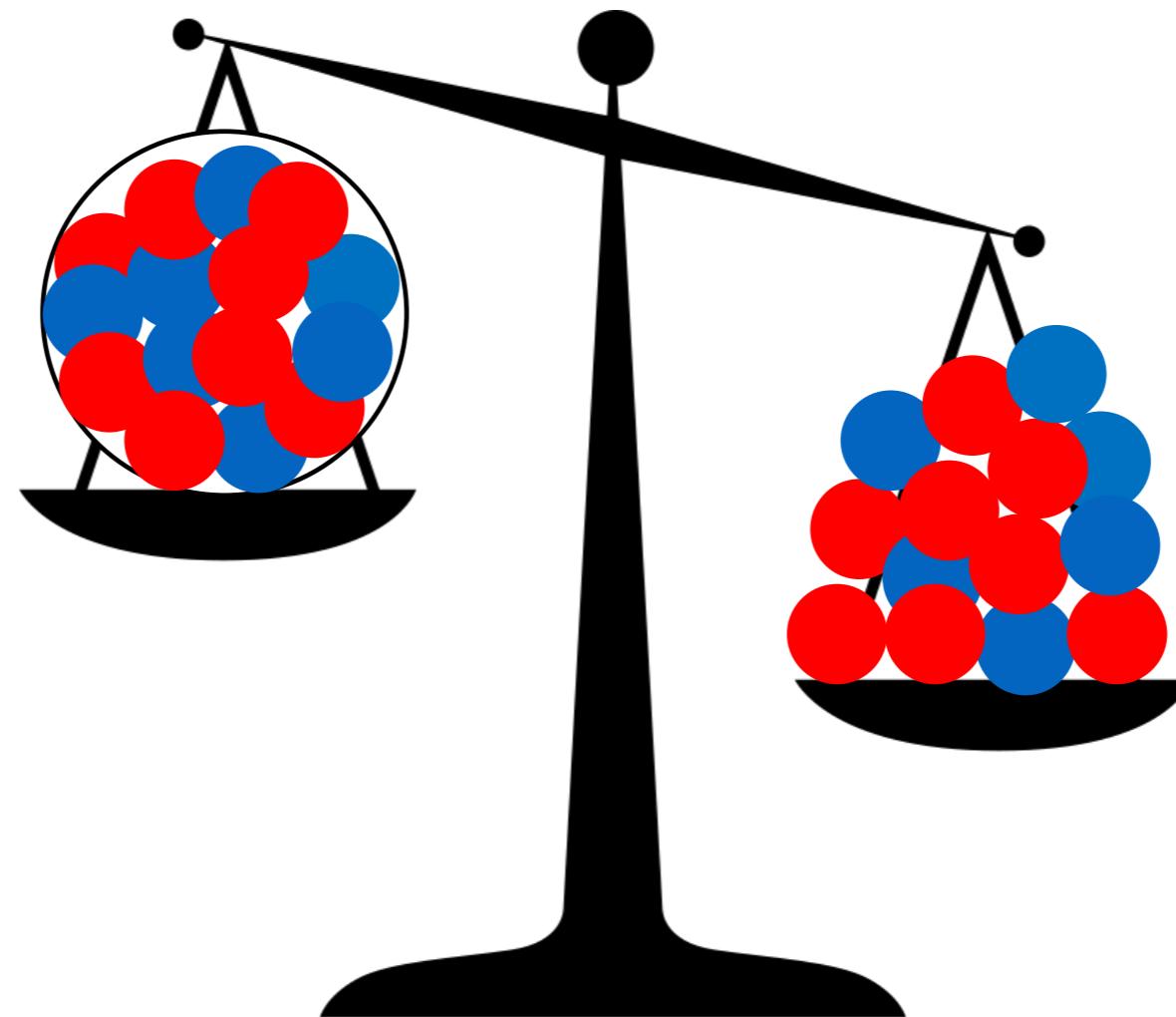
# INTRODUCTION

# The nuclear binding energy

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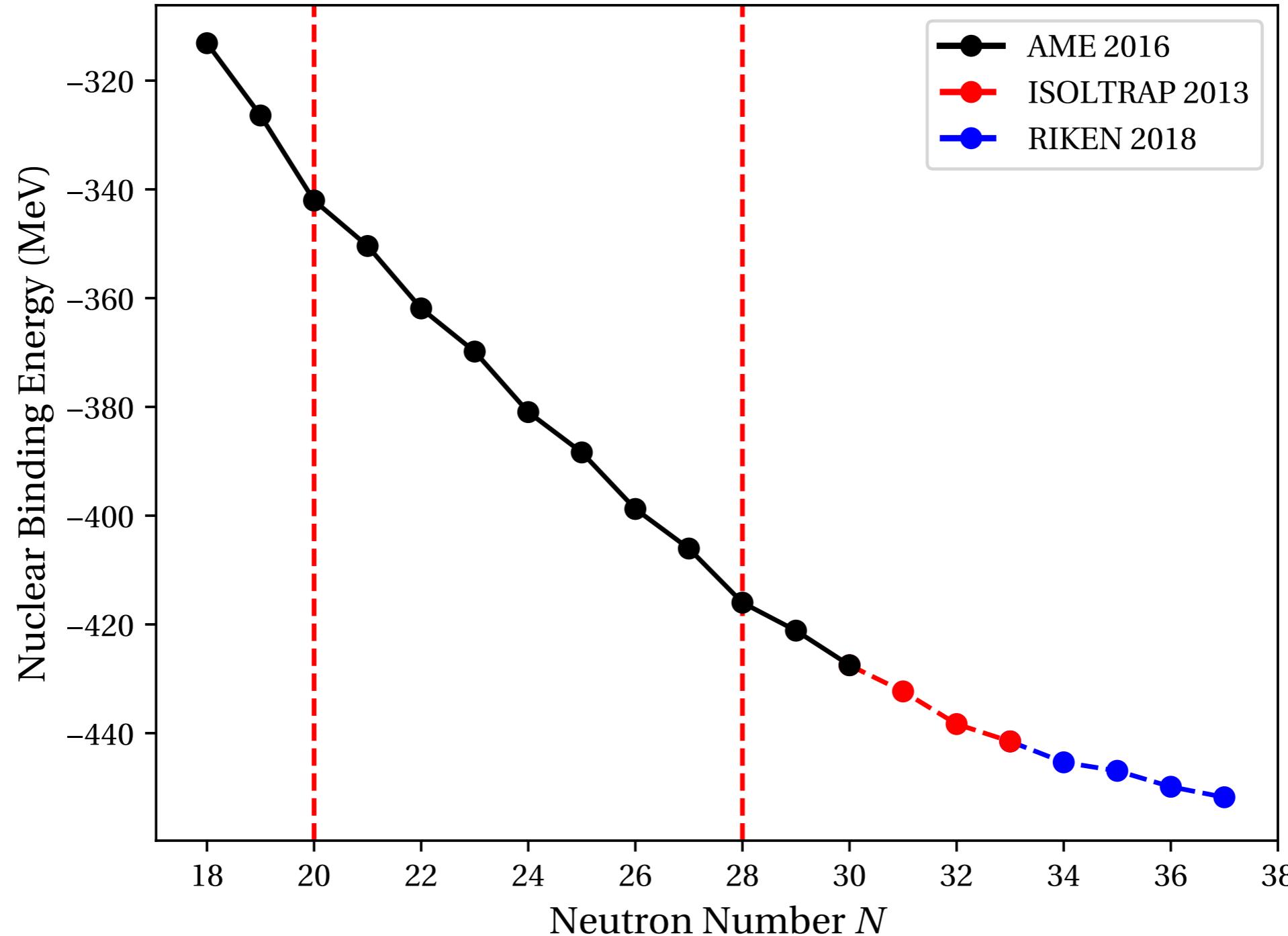
- Reflects the interaction of ALL the nuclear constituents

$$M_{nuc}(Z, N) = \textcolor{red}{Zm_p} + \textcolor{blue}{Nm_n} + E(Z, N)/c^2$$



# Example : Calcium chain

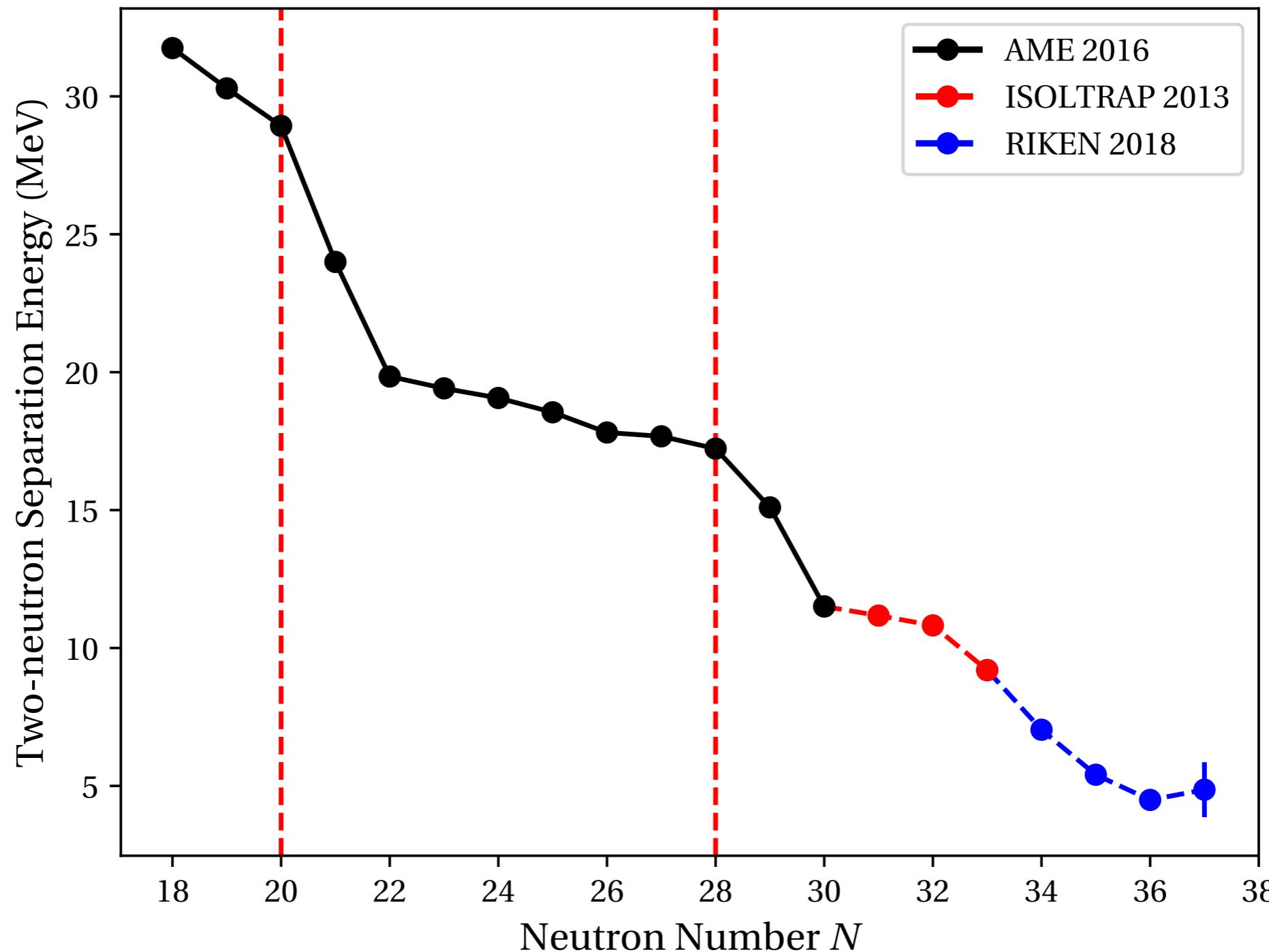
$$M_{nuc}(Z, N) = Zm_p + Nm_n + E(Z, N)/c^2$$



G. Audi *et al.*, Chinese Phys. C **41**, 3 (2017) F. Wienholtz *et al.*, Nature **498**, 346 (2013) S. Michimasa *et al.*, Phys. Rev. Lett. **121**, 022506 (2018)

# New features far from stability

$$S_{2n}(Z, N) = E(Z - 2, N) - E(Z, N)$$



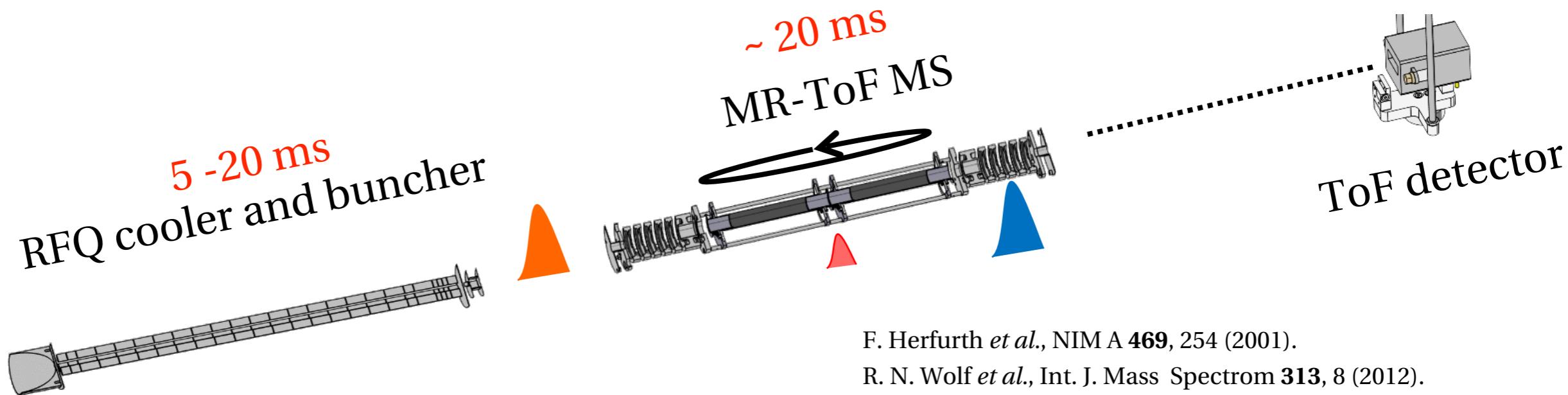
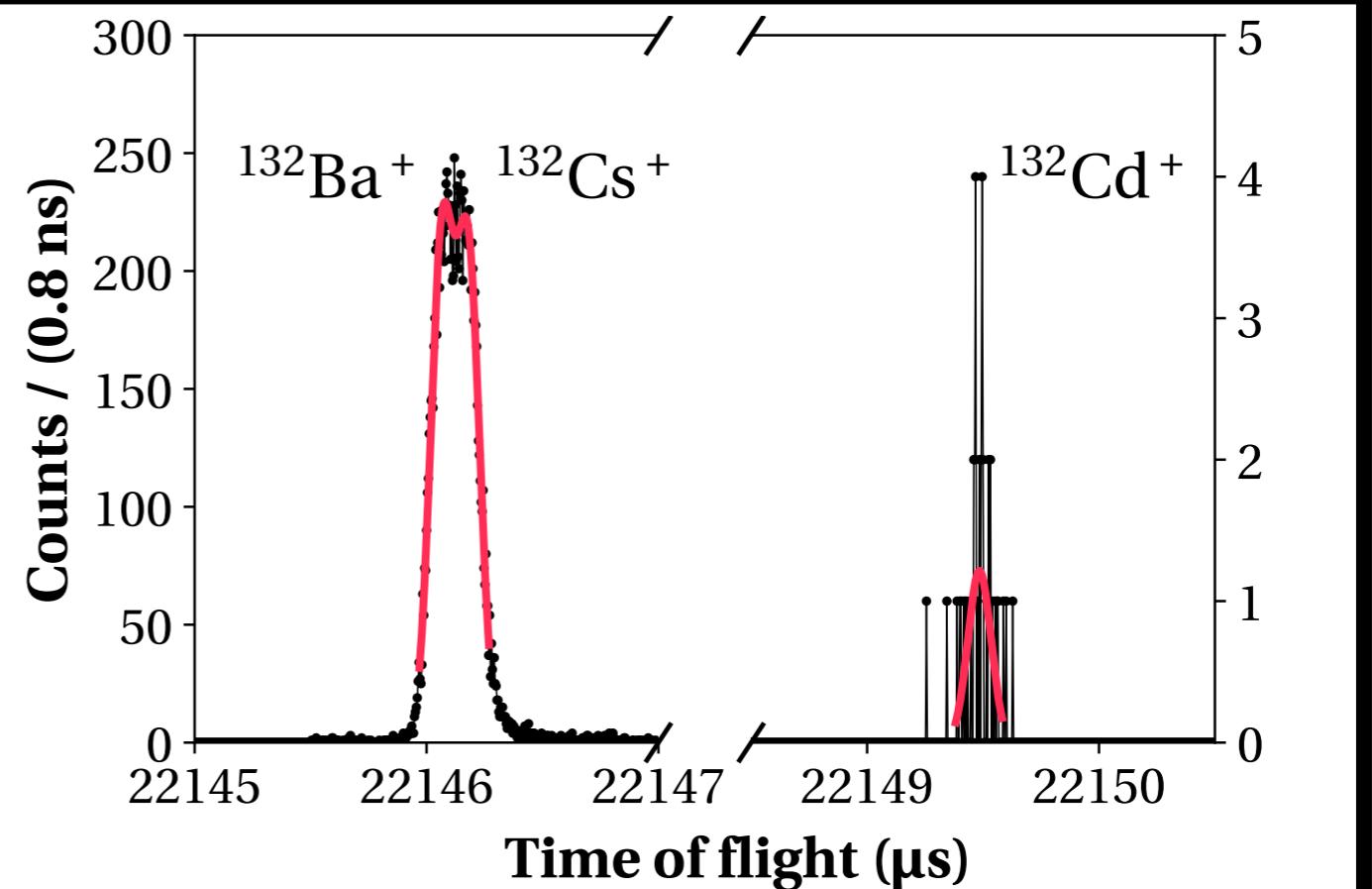
G. Audi *et al.*, Chinese Phys. C **41**, 3 (2017) F. Wienholtz *et al.*, Nature **498**, 346 (2013) S. Michimasa *et al.*, Phys. Rev. Lett. **121**, 022506 (2018)

# MR-ToF mass spectrometry

## MR-ToF MS:

- $m/\Delta m \approx 10^5$  in  $\sim 20$  ms
- $\delta m/m \approx 10^{-6}$

$$t_i = a \cdot \sqrt{\frac{m_i}{q_i}} + b$$



F. Herfurth *et al.*, NIM A **469**, 254 (2001).

R. N. Wolf *et al.*, Int. J. Mass Spectrom **313**, 8 (2012).

V. Manea, J. Karthein *et al.*, Submitted to Phys. Rev. Lett. (2019).

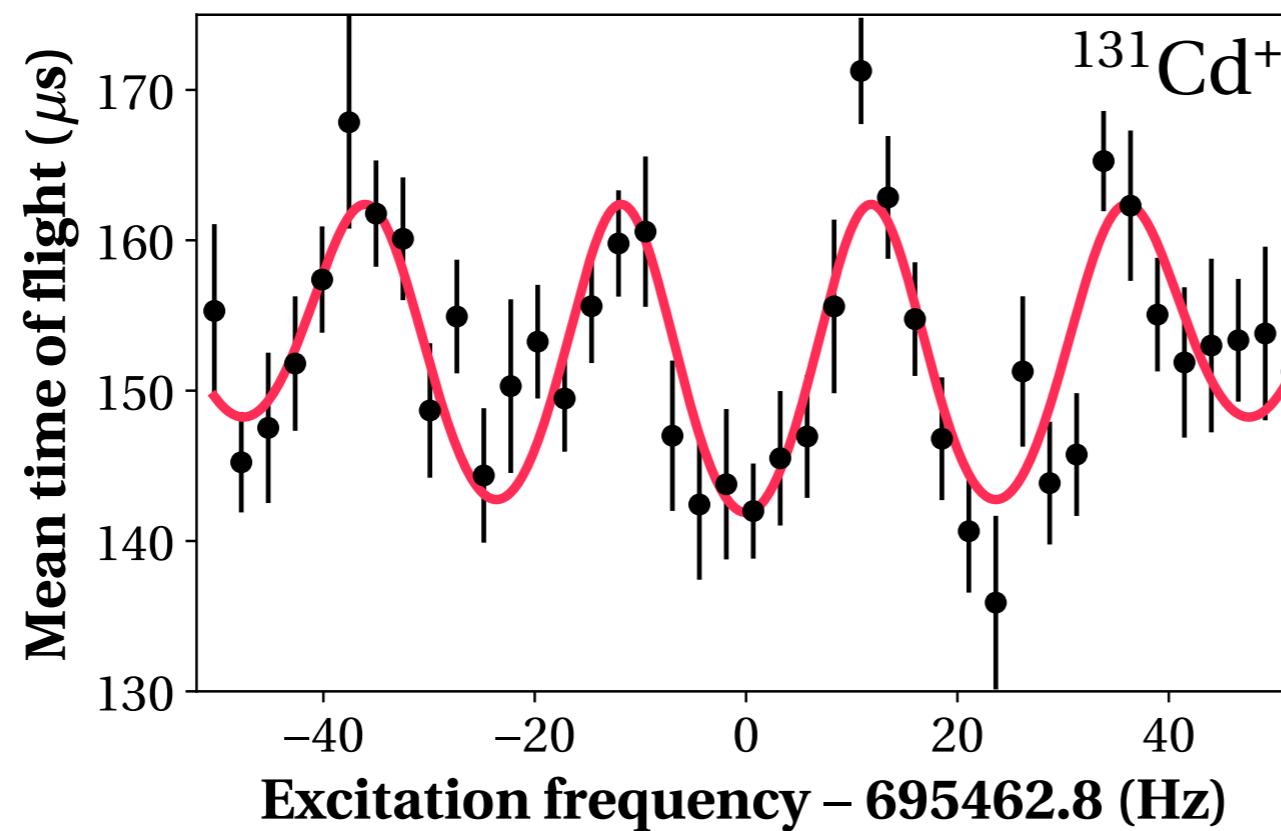
# Penning-trap mass spectrometry

## ToF-ICR:

- Scanning
- $t_{\text{meas}} \sim 50 - 2000 \text{ ms}$

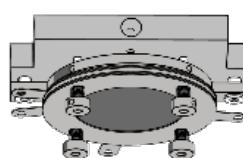
- $\delta m/m \sim 10^{-7} - 10^{-9}$
- $m/\Delta m \sim 10^4 - 10^6$

$$\nu_c = \frac{qB}{2\pi m_{\text{ion}}}$$

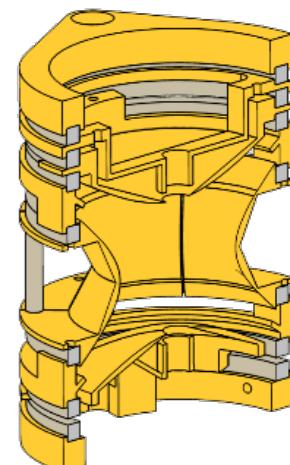


V. Manea, J. Karthein *et al.*, Submitted to Phys. Rev. Lett. (2019).

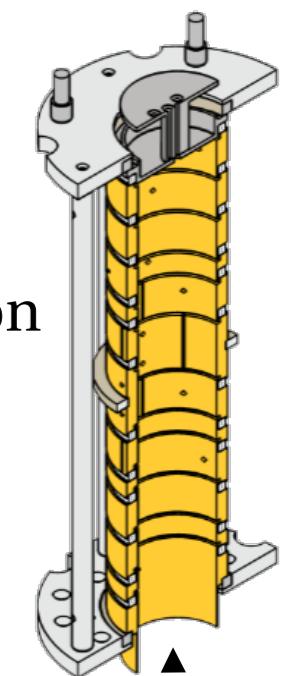
MCP



Precision trap



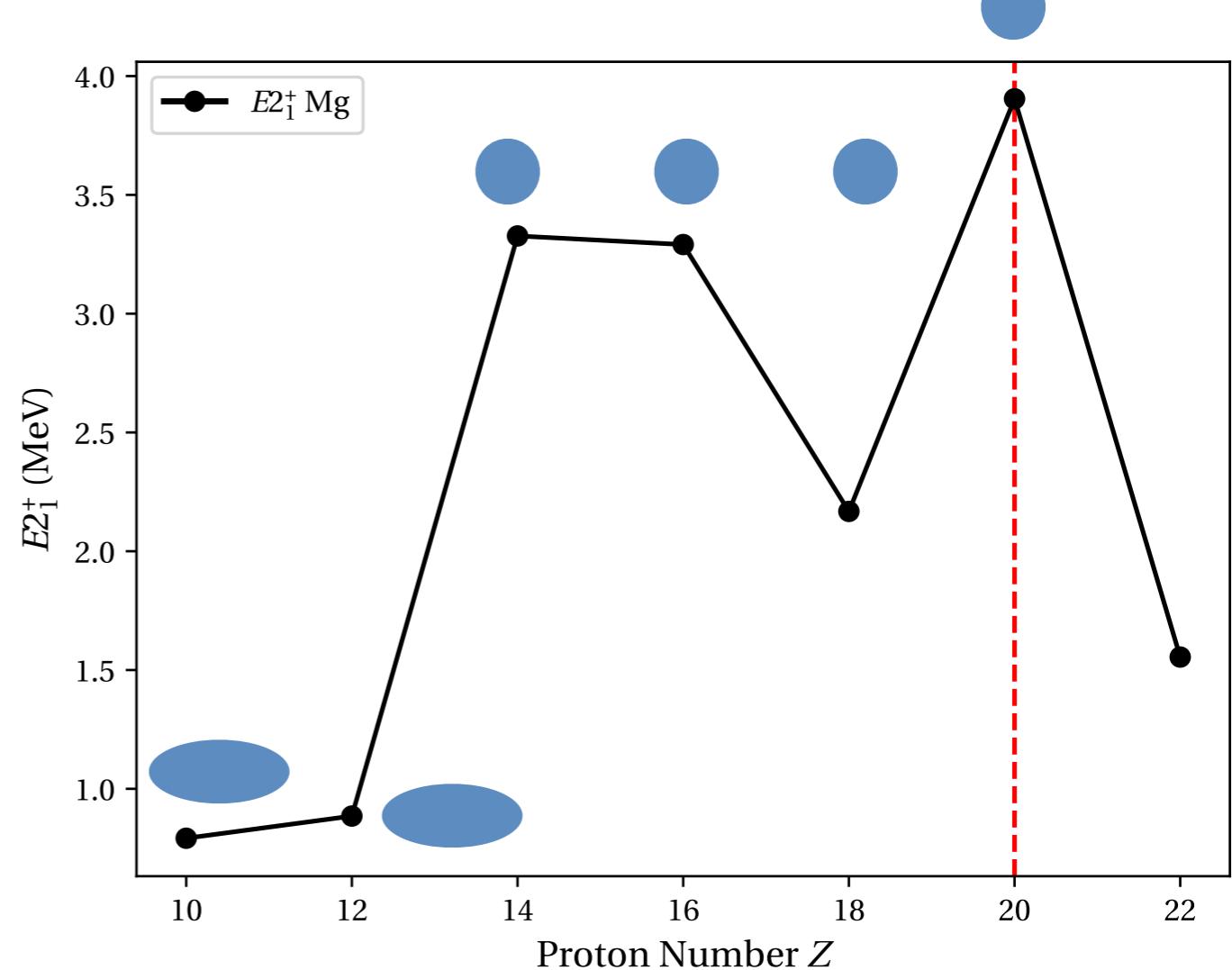
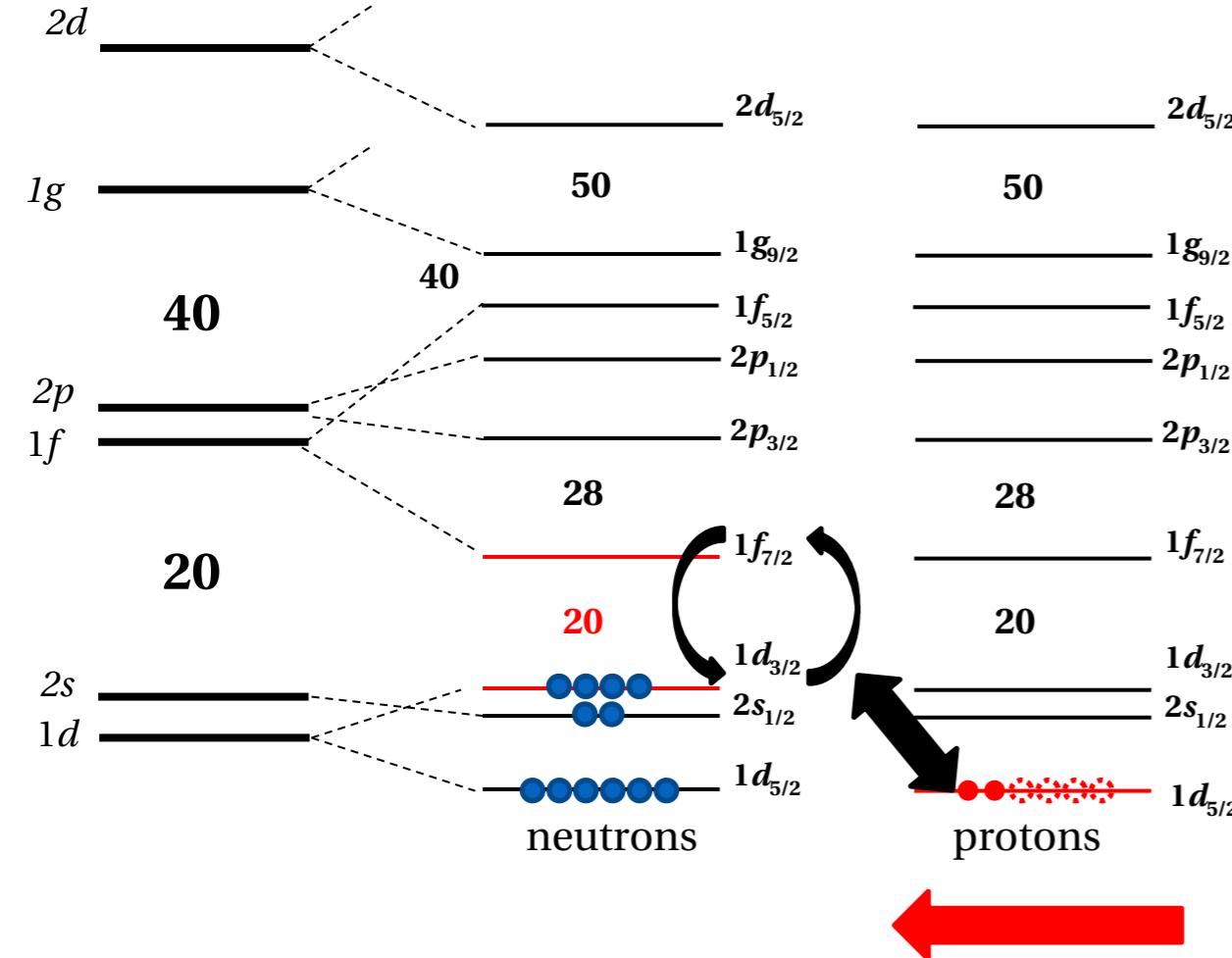
Preparation trap



# Neutron-rich Argon isotopes

# The vanishing of nuclear shells

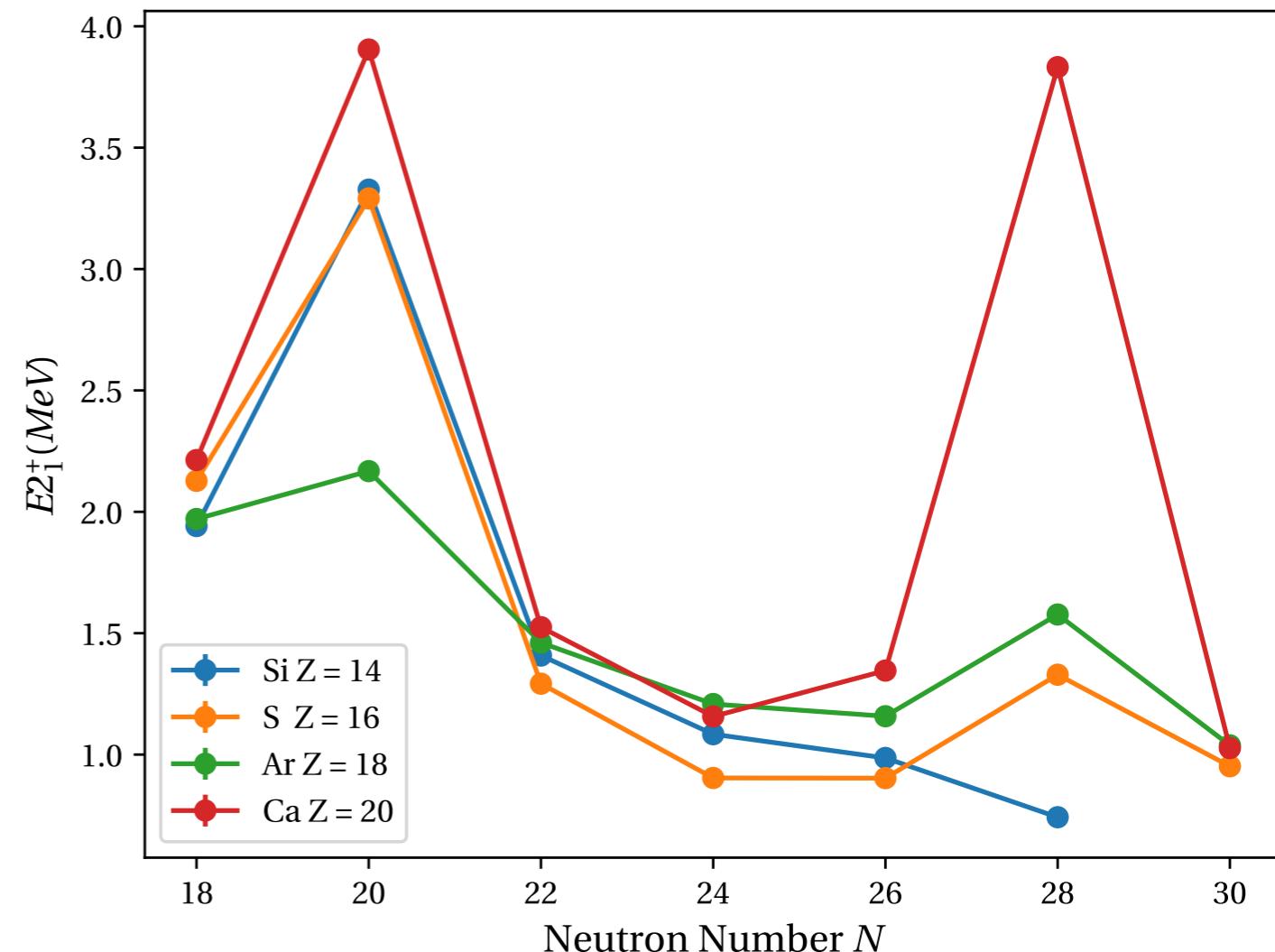
- Example:  $N = 20$  “Island of Inversion”



# What happens for $N=28$ ?

- Fast reduction of  $E2_{1^+}$  below  $^{48}Ca$
- Collapse of the N=28 shell-closure

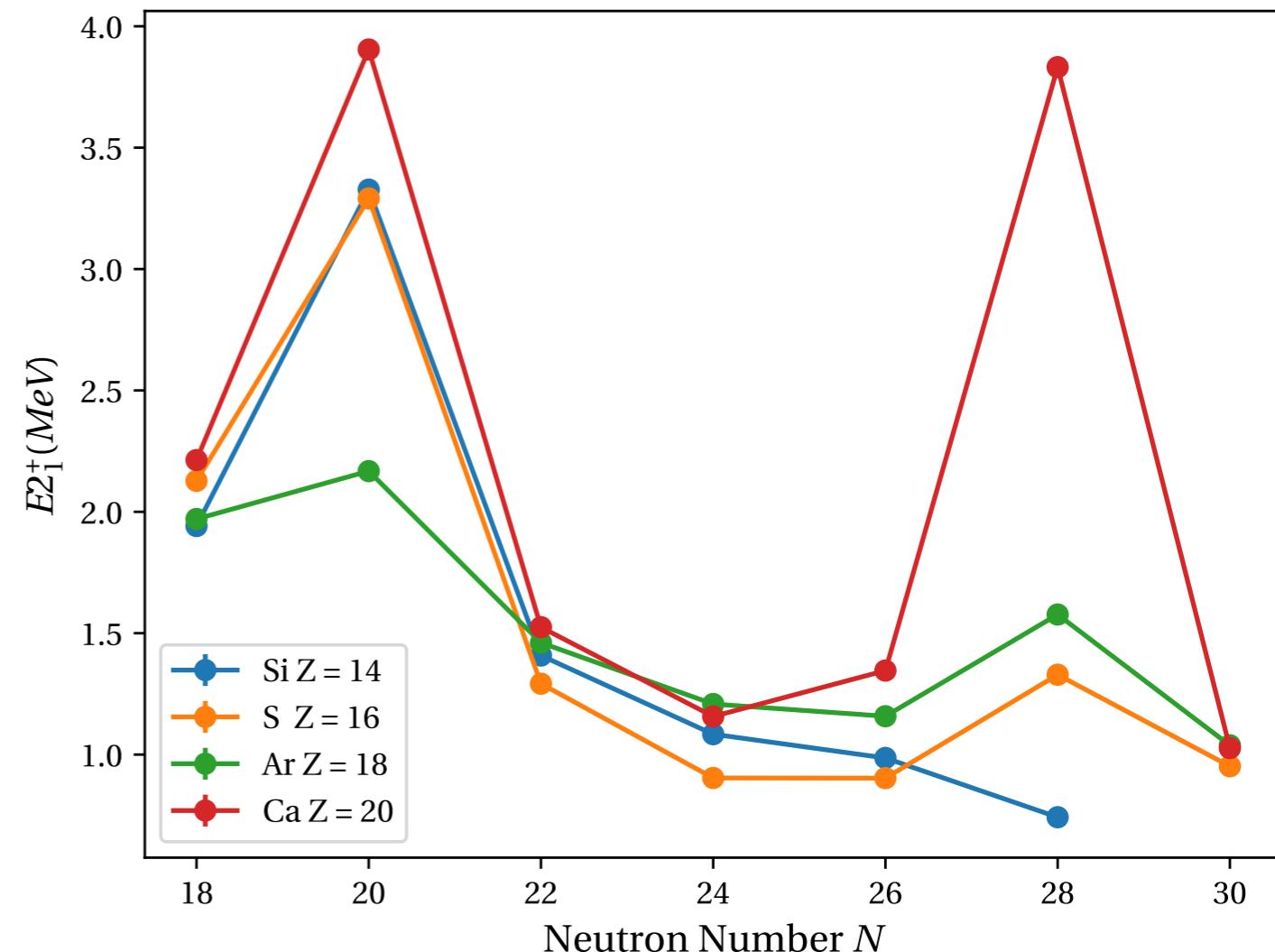
Ca 47 4.538 d	Ca 48 0.187 5.3E+19 y	Ca 49 8.72 m	Ca 50 13.9 s	Ca 51 10.0 s	Ca 52 4.6 s	Ca 53 90 ms
K 46 1.75 m	K 47 17.5 s	K 48 6.8 s	K 49 1.26 s	K 50 472 ms	K 51 365 ms	K 52 105 ms
Ar 45 21.48 s	Ar 46 8.4 s	Ar 47 580 ms	Ar 48 500 ms	Ar 49 170 ms	Ar 50 85 ms	Ar 51 60 ms
Cl 44 560 ms	Cl 45 400 ms	Cl 46 220 ms	Cl 47 200 ms	Cl 48 100 ms	Cl 49 50 ms	Cl 50 20 ms
S 43 260 ms	S 44 123 ms	S 45 82 ms	S 46 30 ms	S 47 20 ms	S 48 10 ms	S 49 200 ns



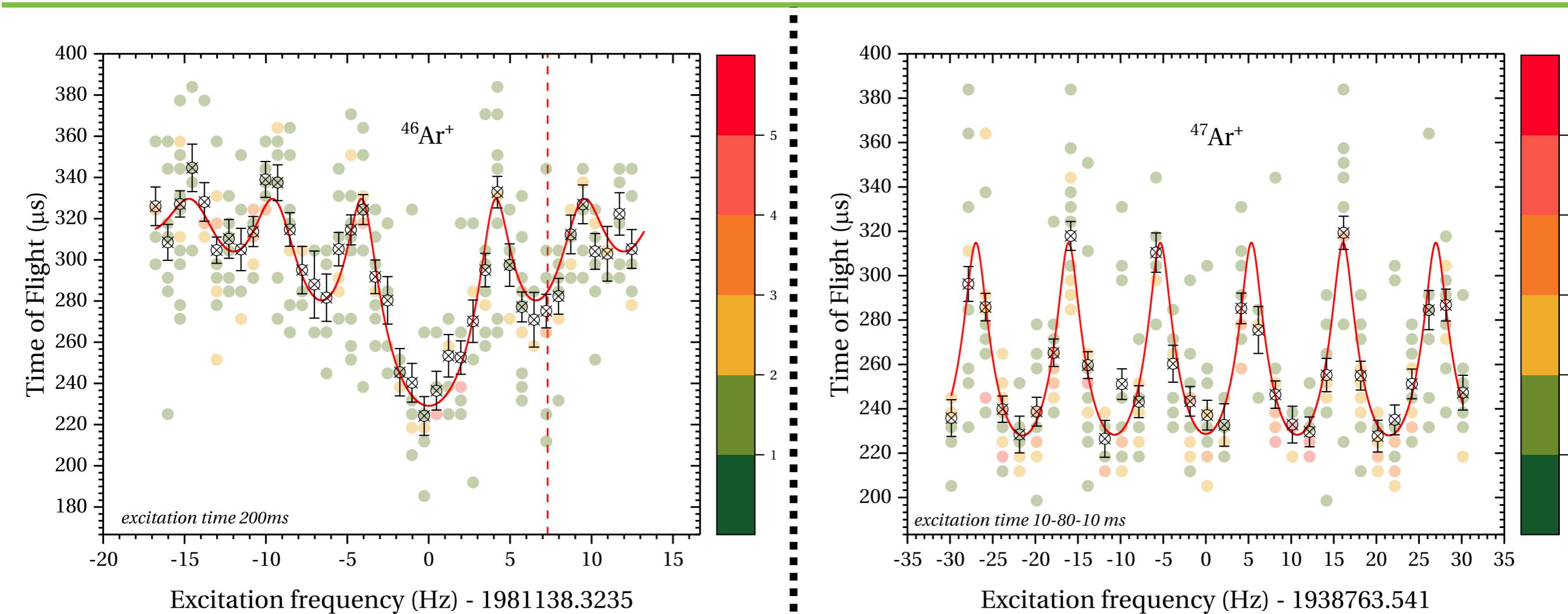
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# Mass measurements of $^{46-47}\text{Ar}$



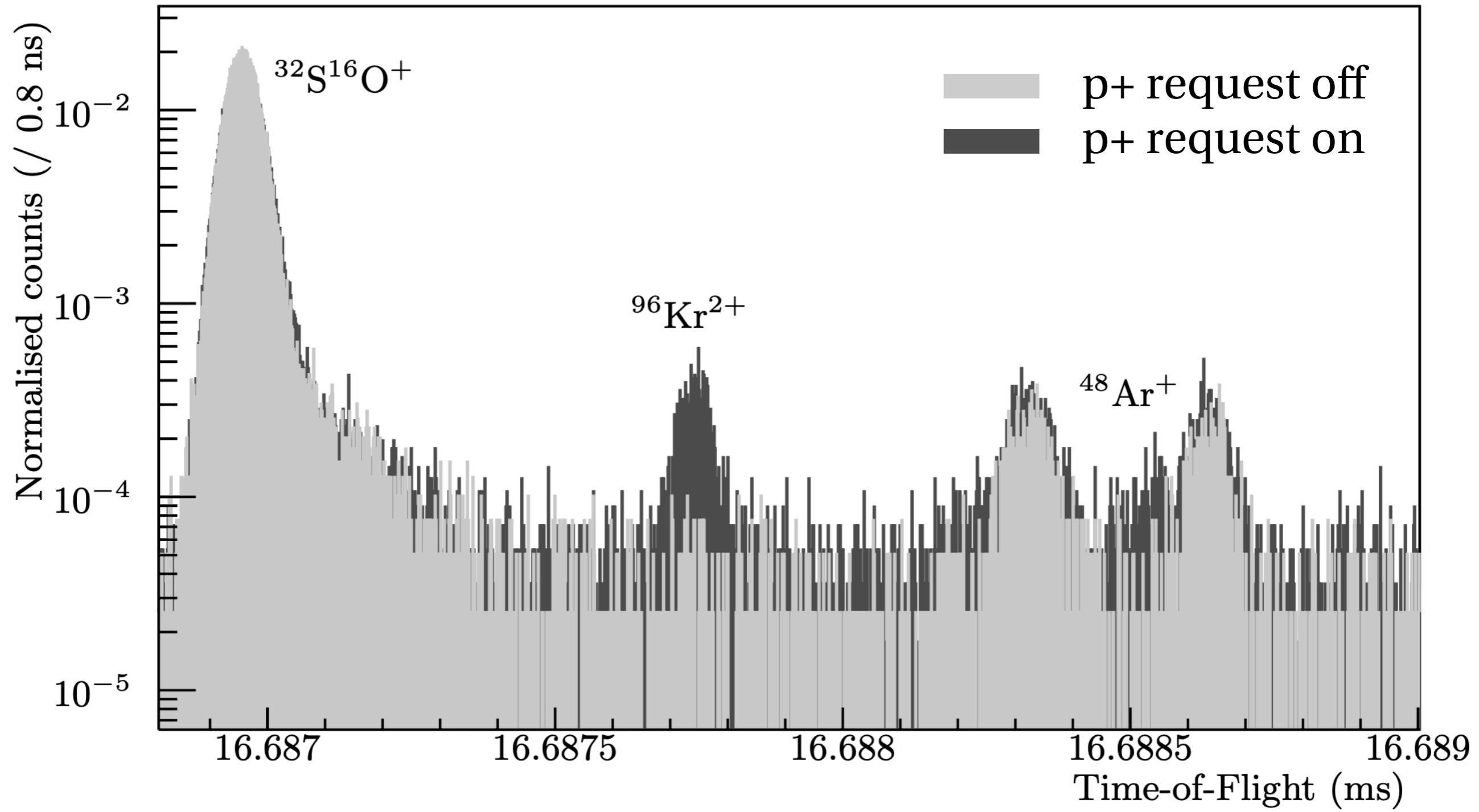
- ~ 40 keV more bound
- ~ 40 times more precise
- ~ 160 keV more bound
- ~ 90 times more precise

M. Wang *et al.*, Chinese Physics C **36**, 1603 (2012).

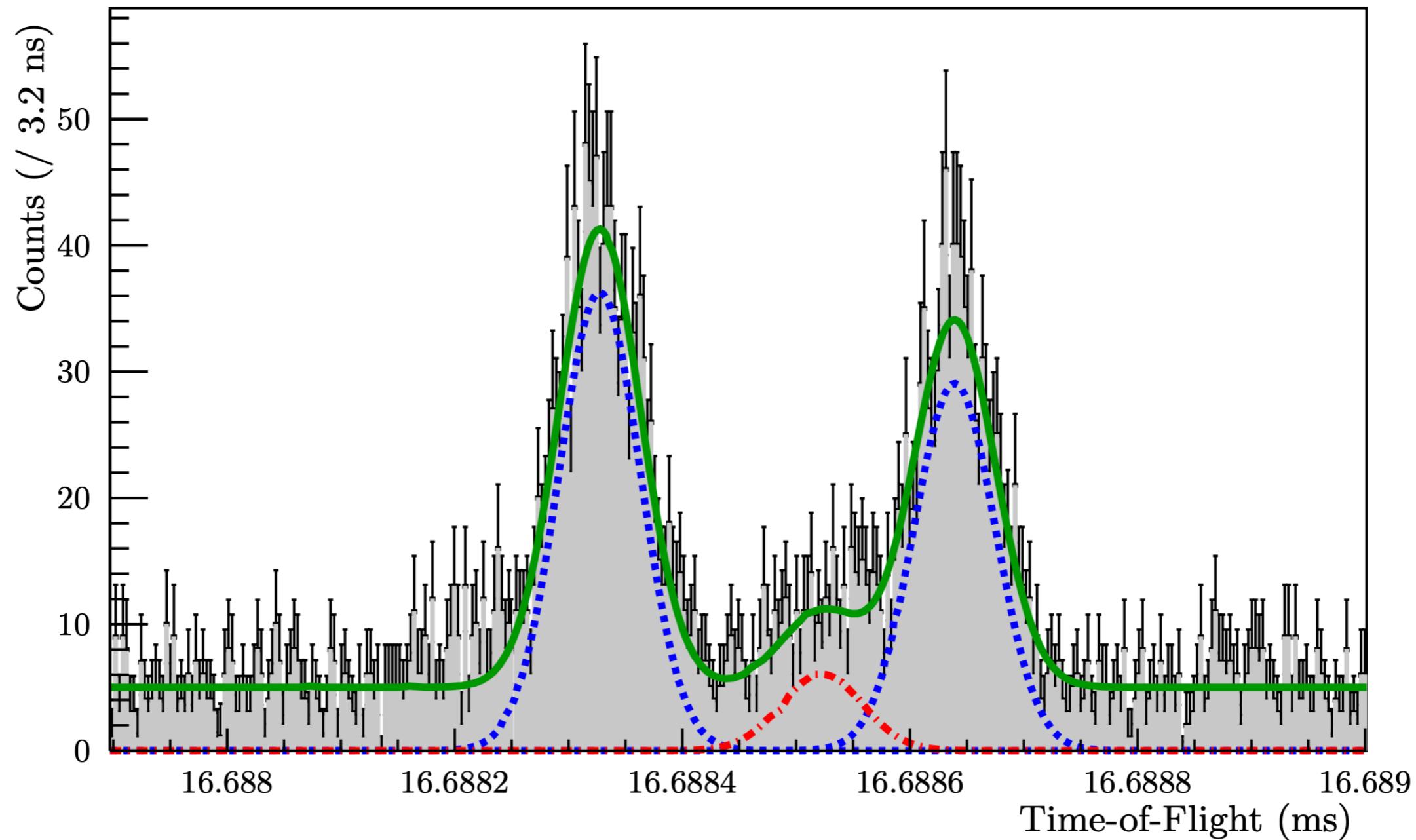
Z. Meisel *et al.*, Phys. Rev. Lett. **94**, 022501 (2015).

# Mass measurements of $^{48}\text{Ar}$

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# Mass measurements of $^{48}\text{Ar}$



- ~ 75 keV more bound
- ~ 19 times more precise

- Background comp.
- Signal comp.
- Sum + Uniform comp.

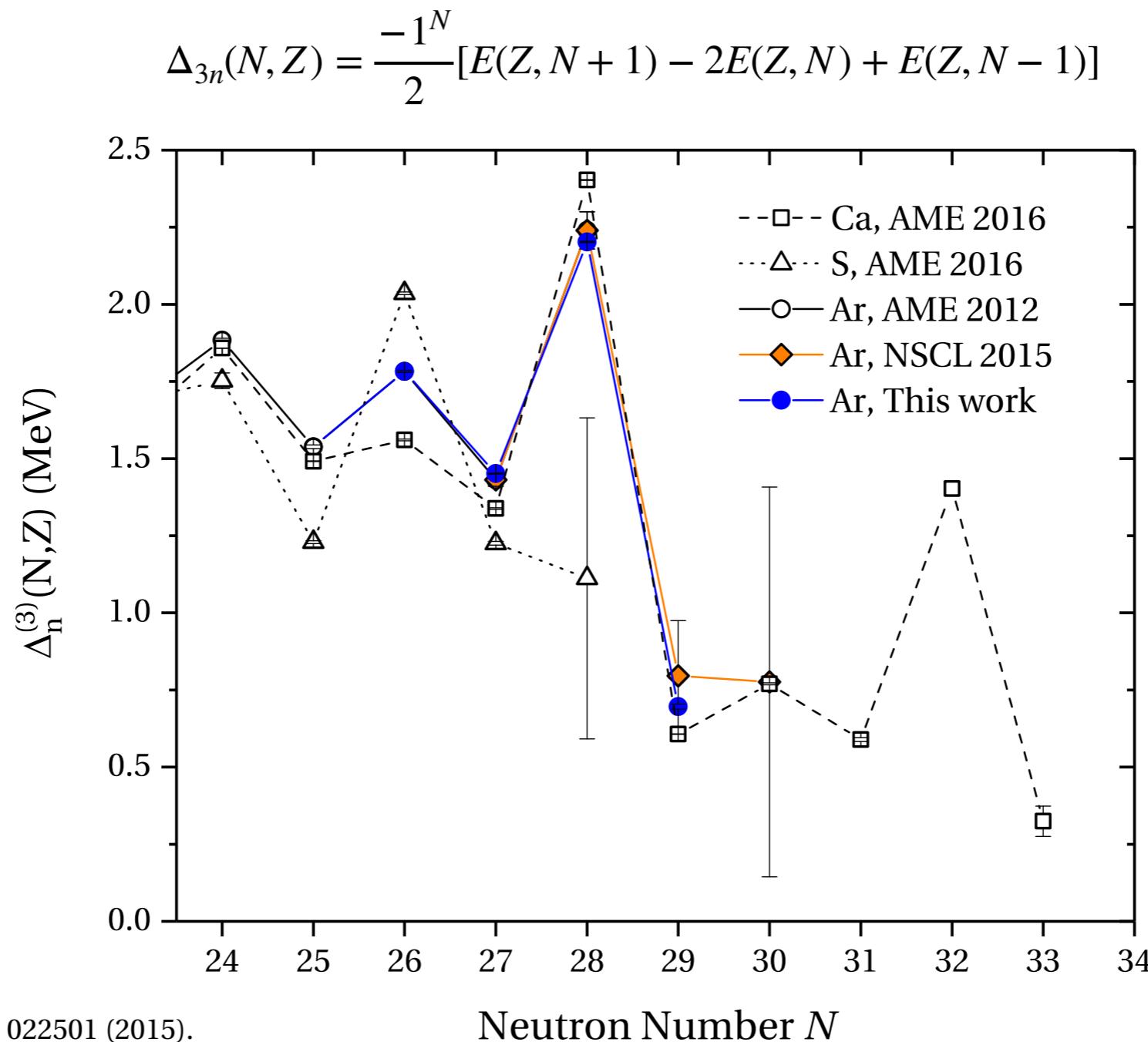
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# **Evolution of the $N=28$ empirical shell gap**

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# Strength of the $N=28$ shell gap

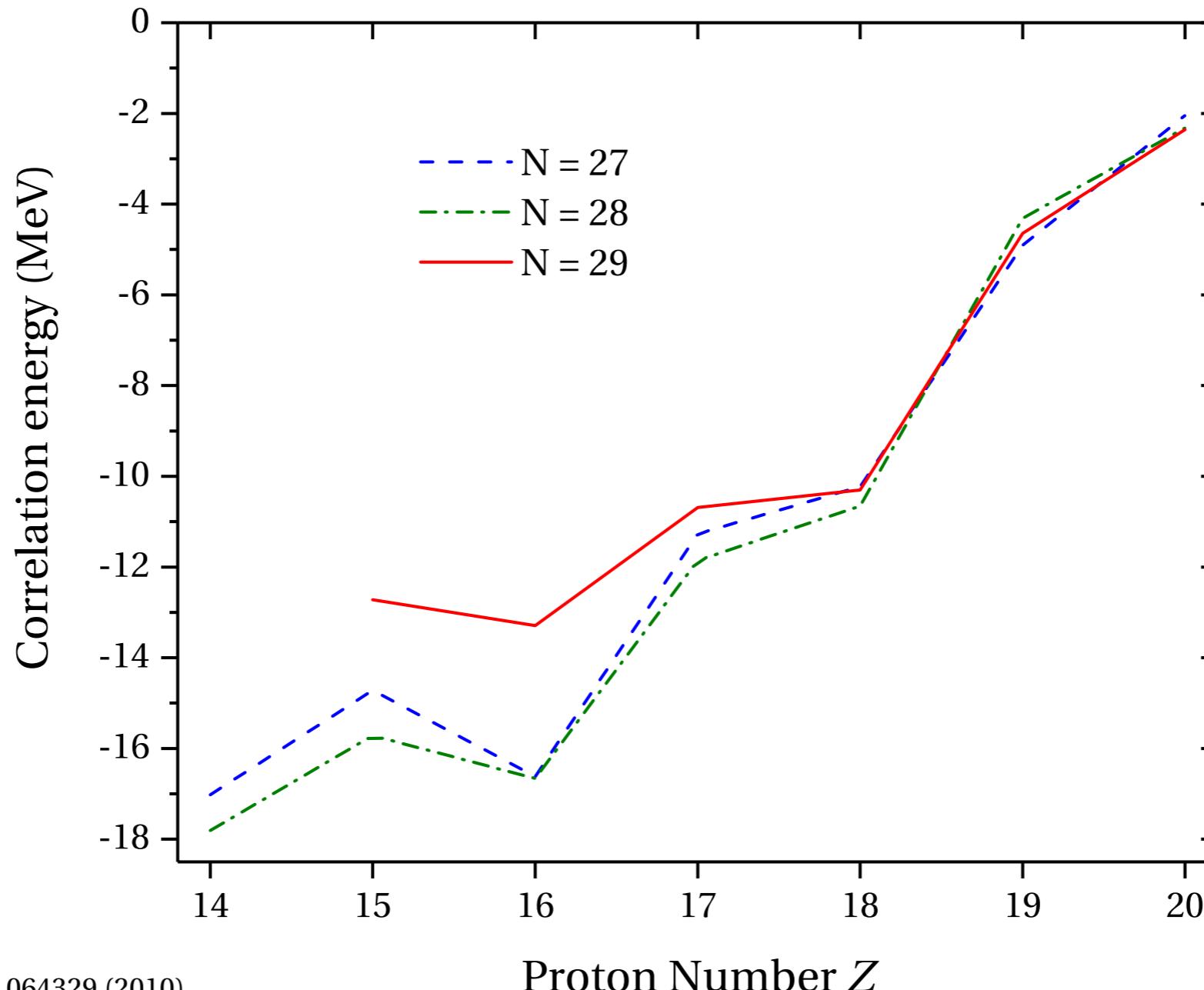
- Rapid collapse of the  $N=28$  one-neutron empirical shell gap for  $Z < 18$
- From Ca to Ar,  $\sim 400$  keV reduction



# Correlations south of $^{48}\text{Ca}$

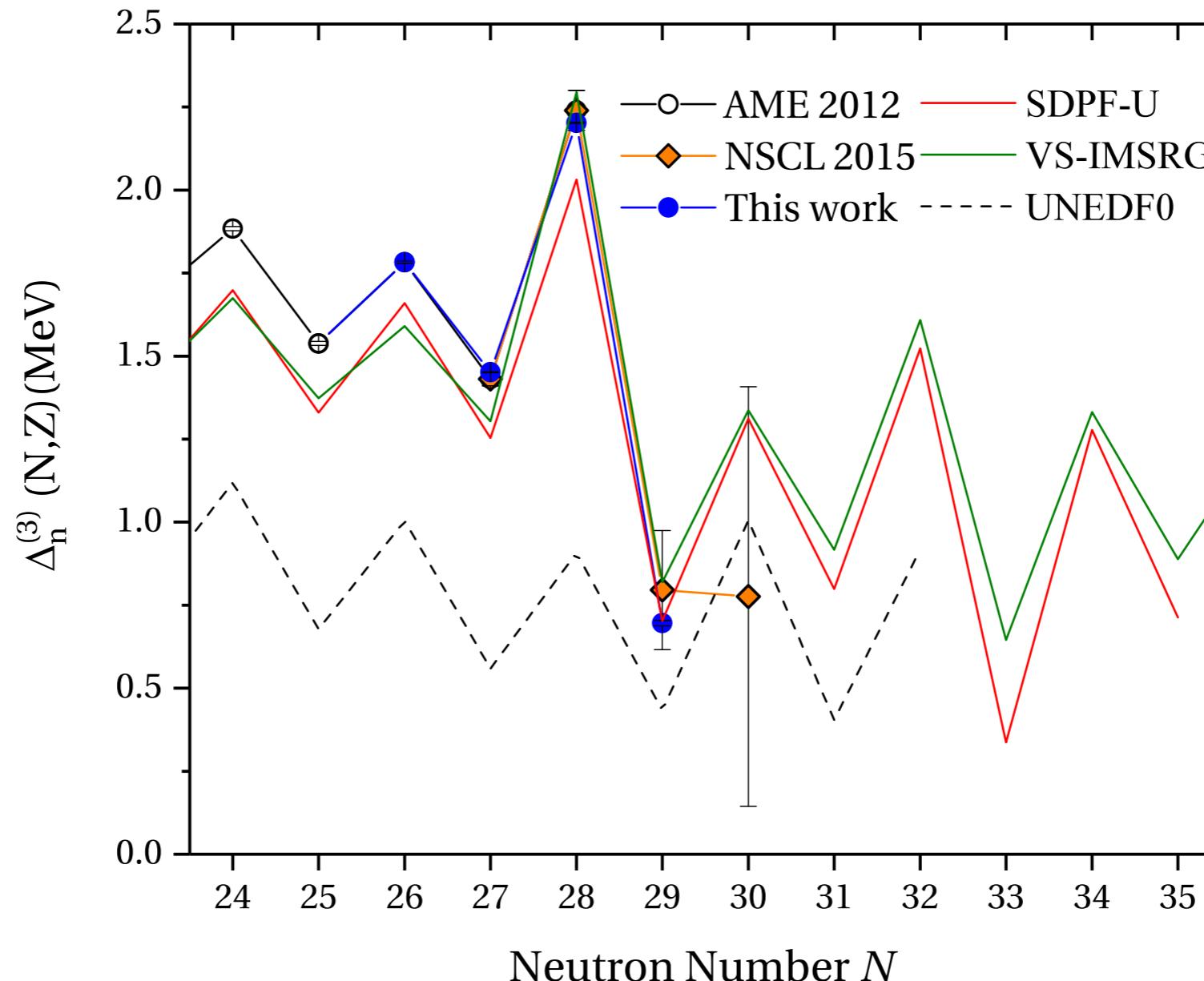
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- Multipole energy extracted from calculated g.s
- ANTOINE code using *SDPF-U* interaction



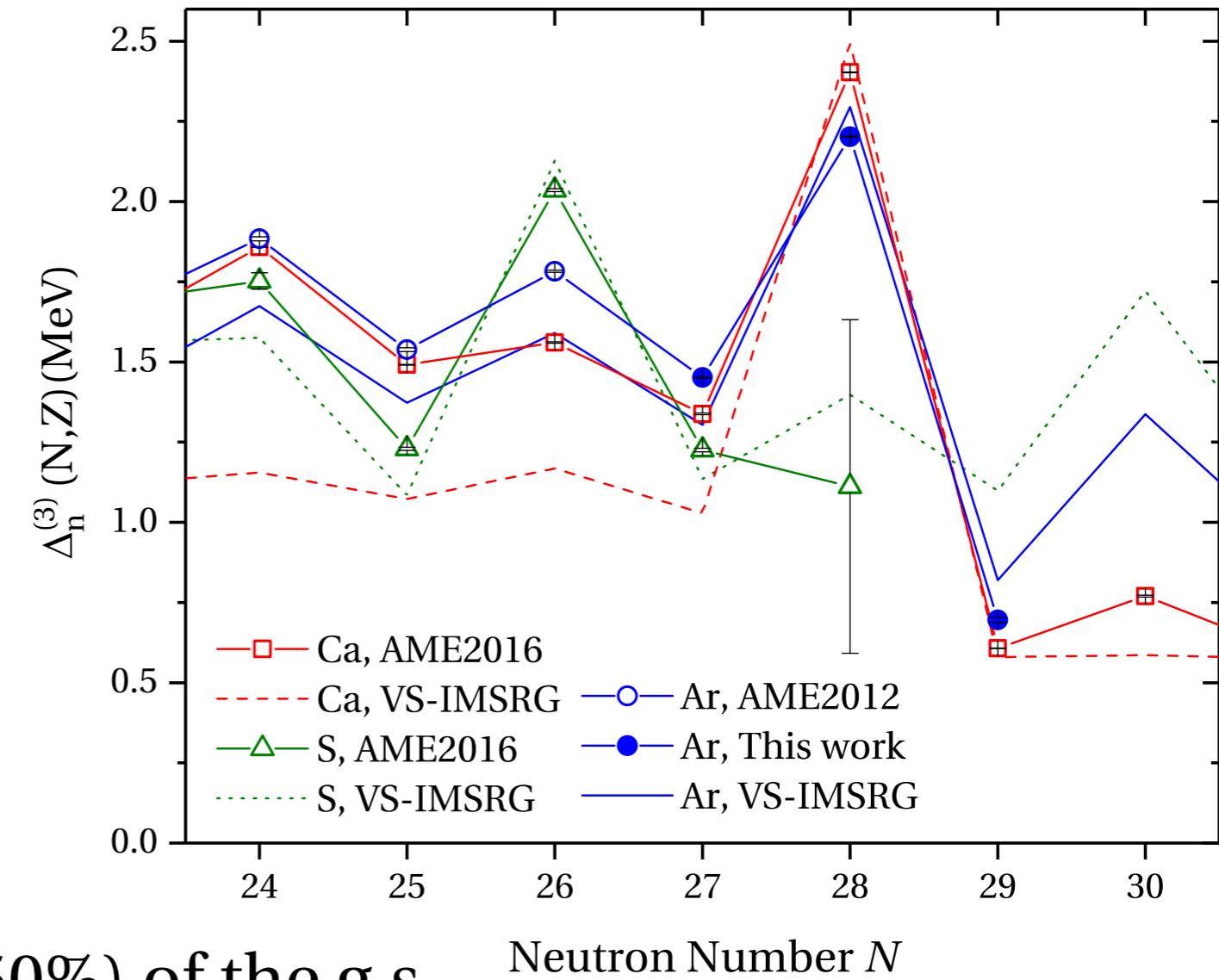
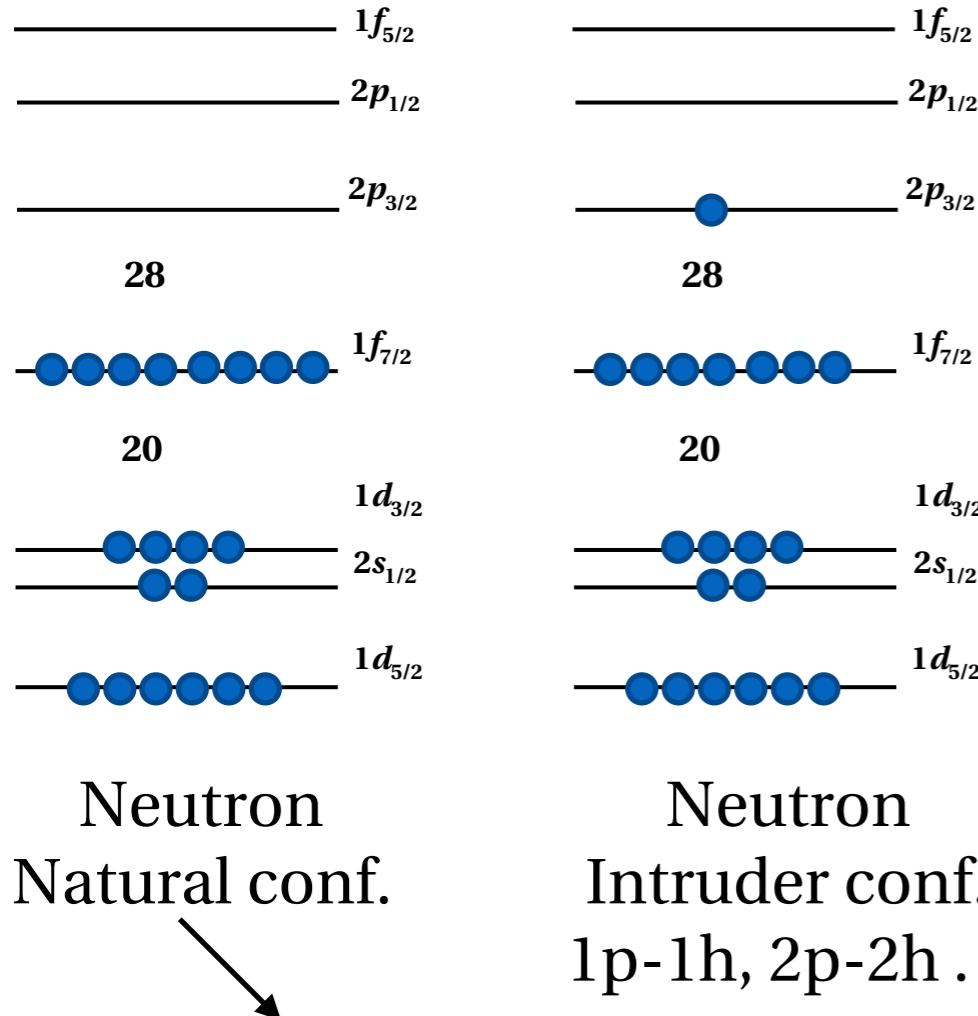
# Theoretical trends

- *SDPF-U* phenomenological interaction → good agreement
- *VS-IMSRG* *ab-initio* approach → also good agreement
- *UNEDF0* → strength of pairing too low



# VS-IMSRG in the region

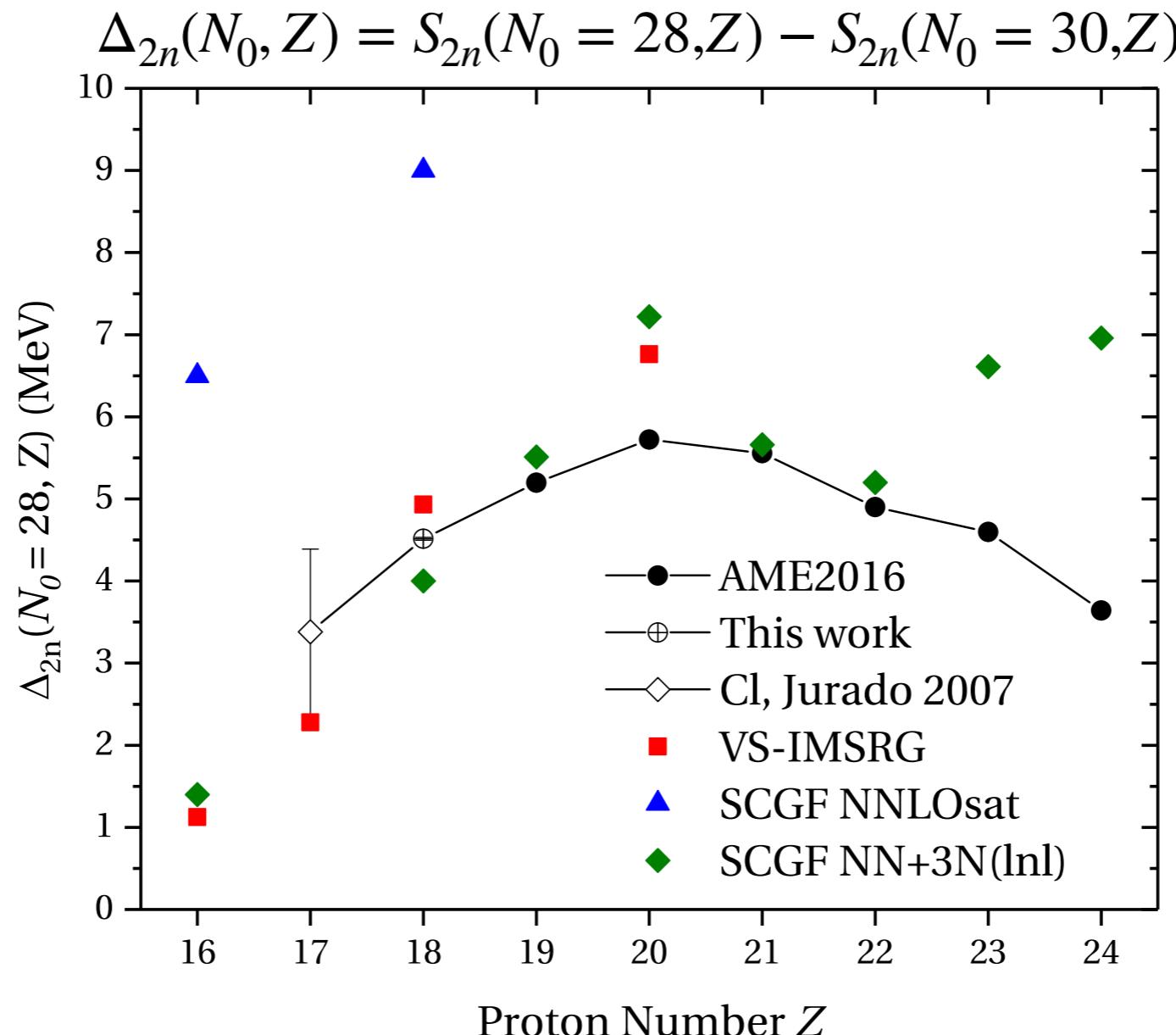
- VS-IMSRG *ab-initio* approach extended down to S
- Predicts erosion of  $N=18$  shell gap
- Need for more precise mass data below  $Z < 18$



- SDPF-U →  $^{48}\text{Ca}$  (90%),  $^{46}\text{Ar}$  (50%) of the g.s
- VS-IMSRG →  $^{48}\text{Ca}$  (90%),  $^{46}\text{Ar}$  (40%) of the g.s

# SCGF predictions :

- *ab-initio* calculations using Self Consistant Green's Function
- Two nuclear interactions
- Good agreement with experiment
- Also predicts a reduction of the  $N=28$  shell gap  $Z < 18$



# Conclusion

# In summary:

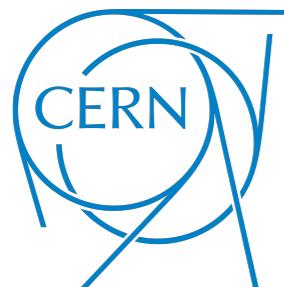
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- Improved precision for  $^{46-48}\text{Ar}$
- ~ 400 keV reduction of the one-neutron empirical shell-gap
- Apparently strong shell gap
- Argon rather a transitional chain
- Ab-initio (VS-IMSRG,SCGF) results in good agreement
- Need for high-precision measurements of isotopes with  $Z < 18$

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