

Introduction to Neutrino BSM

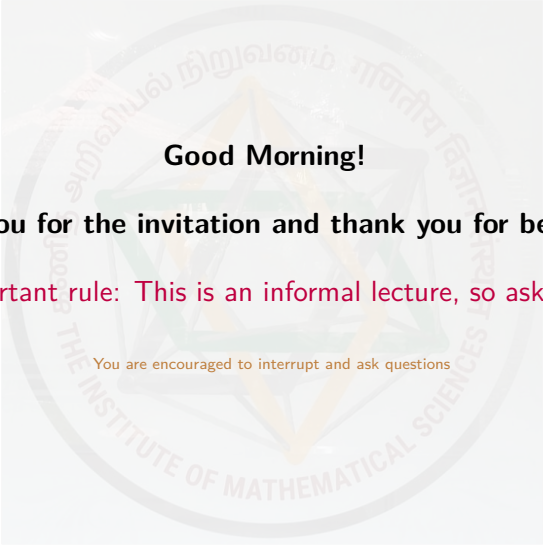
MadGraph School 2019
Institute of Mathematical Sciences, Chennai

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Universite Catholique de Louvain

21 November 2019





Good Morning!

Thank you for the invitation and thank you for being here

Most important rule: This is an informal lecture, so ask questions!

You are encouraged to interrupt and ask questions

Apologies, Disclaimers, Words of Warning

Lectures are "Summer School" style: fast and intense

- There is more material here than time permits (aiming for 3/4 of slides)
- Not everything will be covered (slides kept for completeness)
- **Not** an historical talk

Lectures include modern topics and research

- While known by the community, much material is not yet in textbooks

Central goal is to fill in gaps between coursework and research

- I never saw some of the following ever in any lecture
(informal survey of lecturers shows the same)
- Again, questions are welcomed! :)

(and sorry for the typos!)

Lecture Plan

Lecture I (Thursday): Intro to Neutrino BSM

- Neutrino Oscillations
- Neutrino Masses and Possible Origins

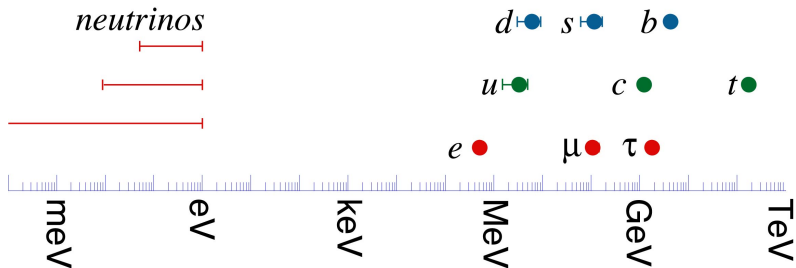
Lecture II (Friday): Neutrino Physics at the LHC

- Building a Collider Analysis: Left-Right Symmetric Model Case Study
- Monte Carlo Tool Chain

Lunch break at 1:00ish

Big Picture (1 slide)

Big Picture



Unambiguous expt evidence that neutrino have nonzero masses

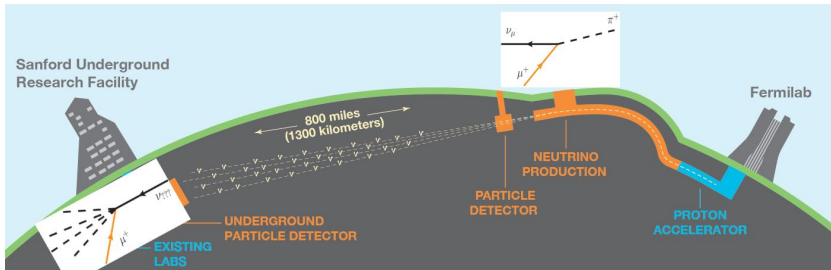
- This is contrary to the Standard Model (SM) of particle physics
- Under general arguments, implies new particles exist (more later)

Investigating $m_\nu \neq 0$ is a very active research topic

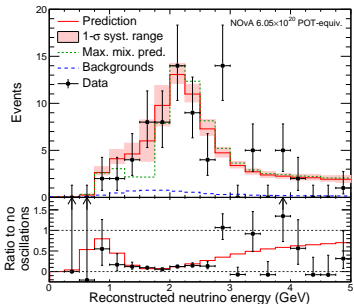
- InSpires: `find hep-ph (hep-ex) and ti neutrino and date > 2014` \sim 2.6k (1.1k) hits

Collider and oscillation facilities provide complementary probes of ν physics

ν Oscillations



In neutrino fixed-target expts, ν_μ beams from collimated π^\pm are studied at near and far detectors (think SLAC DIS expts)



Deficit/disappearance of expected ν_μ
 (+appearance of ν_e/ν_τ) now interpreted as
 $\nu_{\ell_1} \rightarrow \nu_{\text{mass}} \rightarrow \nu_{\ell_2}$ neutrino flavor
transitions/oscillations

[E.g. NO ν A ν_μ disapp., 1701.05891]

Question: How does one describe the data?

The Massive ν Hypothesis

Consider left-handed (LH), $SU(2)_L$ lepton doublets (**gauge eigenbasis**):

$$L_{aL} = \begin{pmatrix} \nu_a \\ l_a \end{pmatrix}_L, \quad a = 1, 2, 3.$$

The SM W^\pm boson coupling to **leptons** in the **flavor eigenbasis** is

$$\mathcal{L}_{CC} = -\frac{g}{\sqrt{s}} W_\mu^+ \sum_{l=1}^3 [\overline{\nu}_{lL} \gamma^\mu P_L l^-] + \text{H.c.}$$

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Supposing $m_\nu \neq 0$, we can rotate ν_l and l into the **mass eigenbasis**:

$$\nu_l = \sum_{m=1}^3 \Omega_{lm} \nu_m \quad \text{and} \quad l = \sum_{\ell=3}^{\tau} \Omega_{l\ell} \ell$$

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This allows us to describe SM W^\pm boson coupling to *massive neutrinos*:

$$\mathcal{L}_{CC} = -\frac{g}{\sqrt{s}} W_\mu^+ \sum_{\ell=e}^{\tau} \sum_{m=1}^3 \overline{\nu}_m \underbrace{U_{m\ell}^*}_{U_{m\ell}^* \equiv \sum_l \Omega_{ml}^* \Omega_{l\ell}} \gamma^\mu P_L \ell^- + \text{H.c.}$$

Like the CKM, SM Feynman rules are modified by **PMNS** mixing factor:

$$\Gamma^\mu = \frac{-ig}{\sqrt{2}} \gamma^\mu P_L \rightarrow \tilde{\Gamma}^\mu = \frac{-ig}{\sqrt{2}} U_{m\ell}^* \gamma^\mu P_L$$

2-State Neutrino Mixing

Generically, mixing between **flavor eigenstates** and **mass eigenstates** is given by **unitary transformation/rotation**

$$\underbrace{\begin{pmatrix} \nu_e \\ \nu_e \end{pmatrix}}_{\text{flavor basis}} = \underbrace{\begin{pmatrix} U_{e1} & U_{e2} \\ U_{\mu1} & U_{\mu2} \end{pmatrix}}_{\text{mixing}} \underbrace{\begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}}_{\text{mass basis}} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

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For a **two-state system**, the state vector for ν_ℓ ($\ell = e, \mu$) is simply

$$\underbrace{|\nu_\ell\rangle}_{\text{flavor basis}} = U_{e1} \underbrace{|\nu_1\rangle}_{\text{light}} + U_{e2} \underbrace{|\nu_2\rangle}_{\text{heavy}} = \cos \theta |\nu_1\rangle + \sin \theta |\nu_2\rangle$$

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If we treat the spacetime propagation of ν_m ($m = 1, 2$) as a plane wave, then the **evolution** from $x^\mu = x_a^\mu$ to $x^\mu = x_b^\mu$ is

$$|\nu_\ell(x_b, x_a)\rangle = U_\ell(x_b, x_a) |\nu_\ell\rangle = U_{\ell 1} U_1(x_b, x_a) |\nu_1\rangle + U_{\ell 2} U_2(x_b, x_a) |\nu_2\rangle$$

Evolution through space and time

Assuming $\hat{p}_\nu = \Delta\hat{x}$, the plane wave evolution over $L = |\vec{x}_b - \vec{x}_a|$ is

$$U_m(x_b, x_a) = e^{-ip_m \cdot (x_b - x_a)} = e^{-i(E_m \Delta t_m - \vec{p}_m \cdot (\vec{x}_b - \vec{x}_a))} \approx e^{-i(E_m \Delta t_m - |\vec{p}_m| L_m)}$$

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Now, working in the ultra relativistic limit, where $E_m + |\vec{p}_m| \approx 2E_m$,

$$(E_m \Delta t_m - |\vec{p}_m| L) \approx (E_m - |\vec{p}_m|) L = \left(\frac{E_m^2 - |\vec{p}_m|^2}{E_m + |\vec{p}_m|} \right) L \approx \left(\frac{m_m^2}{2E_m} \right) L$$

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Since $m_2, m_1 \ll E_1, E_2$, the E_m can be approximated as the same:

$$|\nu_e(E, L)\rangle = U_{e1} e^{-im_1^2 L/2E} |\nu_1\rangle + U_{e2} e^{-im_2^2 L/2E} |\nu_2\rangle$$

$$|\nu_\mu(E, L)\rangle = U_{\mu 1} e^{-im_1^2 L/2E} |\nu_1\rangle + U_{\mu 2} e^{-im_2^2 L/2E} |\nu_2\rangle$$

We are now ready to compute **oscillation transtions!**

Neutrino Oscillation Transitions

To reproduce the ν_μ deficit, consider the $\nu_\mu \rightarrow \nu_\mu$ *transition amplitude*:

$$\begin{aligned}\mathcal{M}(\nu_\mu \rightarrow \nu_\mu) &\equiv \langle \nu_\mu | \nu_\mu(E, L) \rangle \\ &= \underbrace{[\langle \nu_1 | U_{\mu 1}^* + \langle \nu_2 | U_{\mu 2}^*]}_{= \langle \nu_\mu |} \times \underbrace{[U_{\mu 1} e^{-im_1^2 L/2E} |\nu_1\rangle + U_{\mu 2} e^{-im_2^2 L/2E} |\nu_2\rangle]}_{= |\nu_\mu(E, L)\rangle}\end{aligned}$$

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Since $|\nu_m\rangle$ are mass **eigenstates**, $\langle \nu_{m'} | \nu_m \rangle = \delta_{m'm}$. This implies

$$\mathcal{M}(\nu_\mu \rightarrow \nu_\mu) = e^{-im_1^2 L/2E} |U_{\mu 1}|^2 \langle \nu_1 | \nu_1 \rangle + e^{-im_2^2 L/2E} |U_{\mu 2}|^2 \langle \nu_2 | \nu_2 \rangle$$

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The $\nu_\mu \rightarrow \nu_\mu$ *transition probability* is

$$\begin{aligned}\text{Pr}(\nu_\mu \rightarrow \nu_\mu) &= |\mathcal{M}(\nu_\mu \rightarrow \nu_\mu)|^2 = |U_{\mu 1}|^4 + |U_{\mu 2}|^4 \\ &+ e^{-i\Delta m_{21}^2 L/2E} |U_{\mu 1}|^2 |U_{\mu 2}|^2 + e^{+i\Delta m_{21}^2 L/2E} |U_{\mu 1}|^2 |U_{\mu 2}|^2\end{aligned}$$

where we defined $\Delta m_{21}^2 \equiv (m_2^2 - m_1^2)$

Some Quick Algebra

Recalling that $U_{e1} = U_{\mu 2} = \cos \theta$ and $U_{e2} = -U_{\mu 1} = \sin \theta$,

$$\begin{aligned}\Pr(\nu_{\mu} \rightarrow \nu_{\mu}) &= \sin^4 \theta + \cos^4 \theta + 2 \sin^2 \theta \cos^2 \theta \cos \left[\frac{\Delta m_{21}^2 L}{2E} \right] \\ &= 1 - \sin^2(2\theta) \sin^2 \left[\frac{\Delta m_{21}^2 L}{4E} \right] \stackrel{\theta \ll 1}{\approx} = 1 - 4\theta^2 \left[\frac{\Delta m_{21}^2 L}{4E} \right]^2\end{aligned}$$

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Lots to unpack:

$$\Pr(\nu_\mu \rightarrow \nu_\mu) = \underbrace{1}_{\text{unitarity}} - \underbrace{\sin^2(2\theta)}_{\text{minimum of dip}} \underbrace{\sin^2 \left[\frac{\Delta m_{21}^2 L}{4E} \right]}_{\text{spacing between beats}}$$

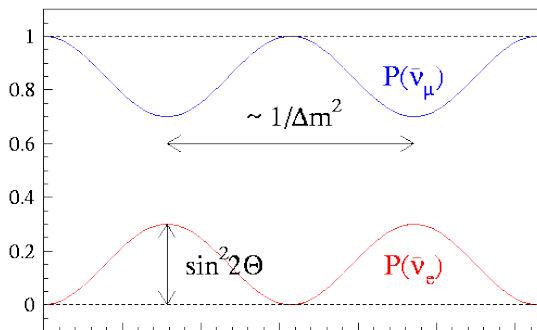
By conservation of probability $1 = \Pr(\nu_\mu \rightarrow \nu_\mu) + \Pr(\nu_\mu \rightarrow \nu_e)$, so the $\nu_\mu \rightarrow \nu_e$ *appearance probability* is

$$\Pr(\nu_\mu \rightarrow \nu_e) = 1 - \Pr(\nu_\mu \rightarrow \nu_\mu) = \sin^2(2\theta) \sin^2 \left[\frac{\Delta m_{21}^2 L}{4E} \right]$$

Understanding Neutrino Oscillation Plots

$$\Pr(\nu_\mu \rightarrow \nu_\mu) = \underbrace{1}_{\text{unitarity}} - \underbrace{\sin^2(2\theta)}_{\text{minimum of dip}} \underbrace{\sin^2 \left[\frac{\Delta m_{21}^2 L}{4E} \right]}_{\text{spacing between beats}}$$

$$\Pr(\nu_\mu \rightarrow \nu_e) = \underbrace{\sin^2(2\theta)}_{\text{maximum of peak}}$$

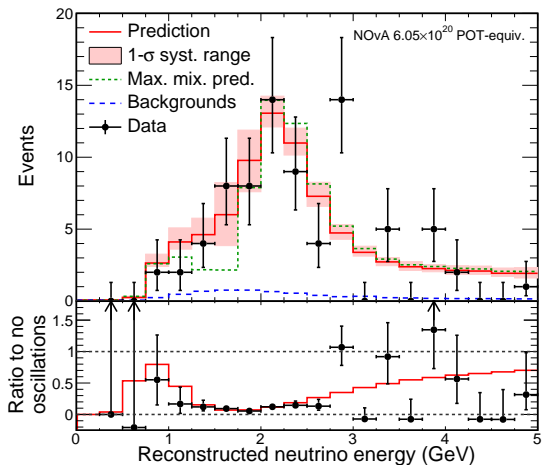


The success and the maturity of the ν oscillation paradigm provides us with
a new probe of new physics:

- Are there additional neutrinos N ? Would manifest as non-unitarity of $3 \times 3 U_{\ell m}$
- How much CP violation is in the lepton sector?
- What drives the CKM matrix "diagonal" but the PMNS matrix "non-diagonal"?
- Are neutrinos Majorana?

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- What is the origin of m_ν ?

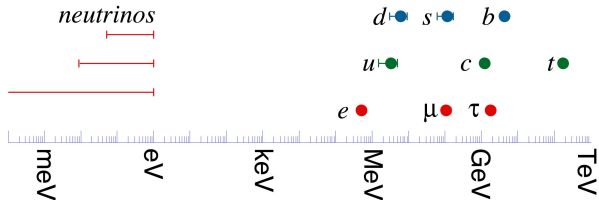


The Massive ν Problem

Okay, so neutrinos have masses $\lesssim \mathcal{O}(0.1)$ eV

Is this a problem?

Yes.



Neutrinos Masses and New Physics

To generate Dirac masses for ν like other SM fermions, we need N_R

$$\begin{aligned}\mathcal{L}_{\nu \text{ Yuk.}} &= -y_\nu \bar{L} \tilde{\Phi} N_R + H.c. = -y_\nu (\bar{\nu}_L \quad \bar{\ell}_L) \begin{pmatrix} \langle \Phi \rangle + h \\ 0 \end{pmatrix} N_R + H.c. \\ &= \underbrace{-y_\nu \langle \Phi \rangle}_{=m_D} \bar{\nu}_L N_R + H.c. + \dots\end{aligned}$$

However, N_R^i do not exist in the SM, implying $m_D = 0$

Significance of Neutrino Oscillations:

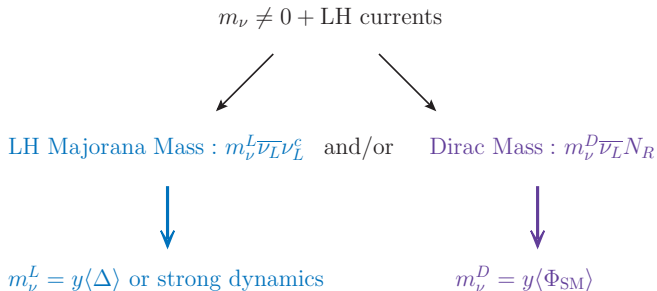
- Neutrino masses $\implies \mathcal{L}_{\text{Universe}} \neq \mathcal{L}_{\text{SM}} (+\mathcal{L}_{\text{gravity}})$
- Instead, $\mathcal{L}_{\text{Universe}} \approx \mathcal{L}_{\text{SM}} + \underbrace{\mathcal{L}_{\nu \text{ masses}}}_{\text{BSM physics!}} + \dots$

BSM physics! 

Neutrino masses \implies existence of physics beyond the SM!

Neutrinos Masses and New Particles?

Nonzero neutrino masses implies new degrees of freedom exist [Ma'98]:



$m_\nu \neq 0 + \text{renormalizability} + \text{gauge inv.} \implies \text{new particles!}$

- New particles might be charged under new or old gauge symm., E.g., N_R may have $U(1)_{B-L}$ charge and Δ_L is an $SU(2)_L$ triplet
- Particles must couple to h or L , often inducing $LN\nu/c\text{LFV!}$

Pathways to Nautrally Small m_ν

Seesaw Mechanisms: Pathways to Naturally Small m_ν

Spinor/gauge algebra + renormalizability restrict ways to build m_ν [Ma'98]

"Type 0": Add SM-singlet N_R with $y_\nu \sim 10^{-12}$ and forbid Majorana mass

- Possible, but tiny y_ν is theoretically unsatisfying

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Type I: Add N_R and keep the Majorana mass term

- $\mathcal{L} \ni -y_\nu \bar{L} \tilde{\Phi} N_R - \frac{m_R}{2} \overline{N_R^c} N_R \implies m_\nu \propto m_D^2 / m_R, \quad m_D = y_\nu \langle \Phi \rangle$

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Type II: Add scalar $SU(2)_L$ triplet ($\Delta^{0,\pm,\pm\pm}$) - **No N_R required**

- $\mathcal{L} \ni y_\Delta \bar{L} (i\sigma_2) \Delta L^c \implies m_\nu \propto y_\Delta \langle \Delta \rangle \overline{\nu^c} \nu, \quad \langle \Delta \rangle < \text{few GeV}$

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Type III: Add fermion $SU(2)_L$ triplet ($T^{0,\pm}$)

- $\mathcal{L} \ni y_T \bar{L} T^a \sigma^a (i\sigma^2) \Phi + \frac{m_T}{2} \overline{T^{0c}} T^0 \implies m_\nu \propto m_D^2 / m_T$

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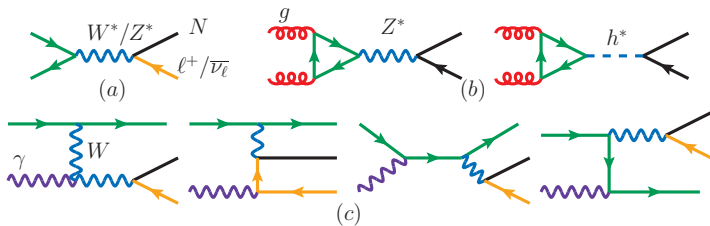
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Less Minimal Models: Hybrid, Inverse, Radiative, ..., all with rich pheno

Type I Seesaw



Canonical Type I Seesaw Mechanism

... extends the Standard Model (**SM**) field content with N_R , and supposes the existence of Dirac and RH Majorana masses:

$$\mathcal{L}_{\text{Type I}} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{N \text{ Kin.}} - \underbrace{y_\nu \bar{L} \tilde{\Phi} N_R + \text{H.c.}}_{\text{Dirac mass}} - \underbrace{\mu_R \overline{N_R^c} N_R}_{\text{Majorana mass}}$$

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Combining the mass terms makes manifest neutrino mass-mixing

$$\mathcal{L}_{D+M} = -\frac{1}{2} \overline{\tilde{N}} \tilde{M} \tilde{N} = \left(\overline{\nu_L} \quad \overline{N_R^c} \right) \begin{pmatrix} 0 & m_D \\ m_D & \mu_R \end{pmatrix} \begin{pmatrix} \nu_L^c \\ N_R \end{pmatrix}$$

Canonical Type I Seesaw Mechanism

... extends the Standard Model (**SM**) field content with N_R , and supposes the existence of Dirac and RH Majorana masses:

$$\mathcal{L}_{\text{Type I}} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{N \text{ Kin.}} - \underbrace{y_\nu \bar{L} \tilde{\Phi} N_R + H.c.}_{\text{Dirac mass}} - \underbrace{\mu_R \bar{N}_R^c N_R}_{\text{Majorana mass}}$$

Combining the mass terms makes manifest neutrino mass-mixing

$$\mathcal{L}_{D+M} = -\frac{1}{2} \bar{\tilde{N}} \tilde{M} \tilde{N} = \left(\bar{\nu}_L \quad \bar{N}_R^c \right) \begin{pmatrix} 0 & m_D \\ m_D & \mu_R \end{pmatrix} \begin{pmatrix} \nu_L^c \\ N_R \end{pmatrix}$$

This gives the following mass eigenvalues when $\mu_R \gg m_D$:

$$m_1 \approx -m_D \left| \frac{V}{\mu_R} \right|^2 = -m_D \frac{m_D}{\mu_R}, \quad m_2 \approx \mu_R$$

Realistic **models** have large and messy mass matrix \tilde{M} , where

$$\tilde{m}_\nu = -\tilde{M}_D \tilde{M}_R^{-1} \tilde{M}_D^T \text{ with active-sterile mixing } \tilde{V} = \tilde{M}_D \tilde{M}_R^{-1}$$

Seesaw Mechanisms at Work

By introducing new particles and writing the most general, gauge-invariant Lagrangian allowed, we have simultaneously:

- **Established neutrino masses** through Yukawa couplings and
- **Suppressed the effective neutrino masses** through **mixing**

However, **Seesaws are more frameworks than models**. Their strength and weakness are their ability to be readily embedded in specific models.

- Going beyond fermionic $SU(3)_C \otimes U(1)_{EM}$ singlets makes physics and life more entertaining due to additional mixing

E.g., **Type II, III Seesaws**, **(N)MSSM**, **Randall-Sundrum**, **GUTs**

Agnostic Approach to Heavy N Mixing

In pure Type I scenarios, tiny m_ν obtained in two ways:

① **High-scale seesaw:** $\mu_M \gg \langle \Phi_{SM} \rangle \implies m_\nu \sim m_D \left(\frac{m_D}{\mu_M} \right), m_N \sim \mu_M$

Leads to generic decoupling of N and LNV from colliders

② **Low-scale seesaw:** $\mu_M \ll \langle \Phi_{SM} \rangle \implies m_\nu \sim \mu_M \left(\frac{m_D}{m_R} \right)^2, m_N \sim m_R$

Known also in literature as Inverse Seesaw, Linear Seesaw, Protective Symmetries, etc.

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Apriori, no preference for either without additional theory prejudice:

- **LNC Option:** Low-scale Type I + if ν approx. massless on expt scale, i.e., $\tilde{m}_\nu^2/Q^2 \approx 0 \implies$ **approximate L conservation** w/ Pascoli, et al, [1812.08750]

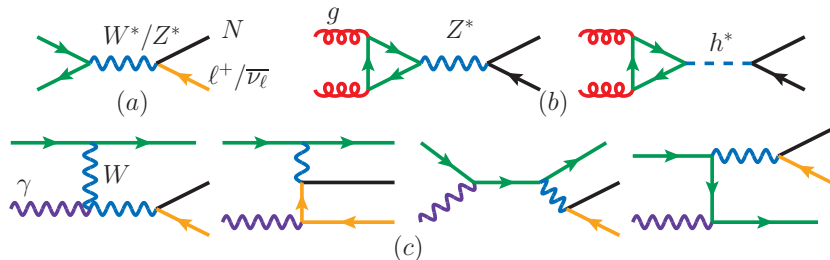
See also, Pilaftsis [hep-ph/9901206], Kersten and Smirnov [0705.3221], Pascoli, et al, [1712.07611]

- **LNV Options:** Collider LNV via $N_i \implies$ *more new particles!*

RR [1703.04669]

Heavy Neutrino Production At Hadron Colliders

Heavy N can be produced through a variety of mechanisms in pp collisions



In fact, a resurgence of calculations in recent years¹

- Clarity needed on understanding m_N, \sqrt{s} dependence

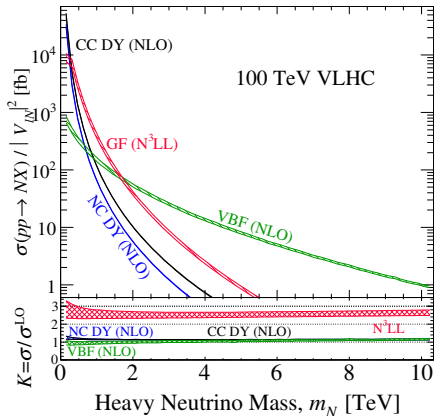
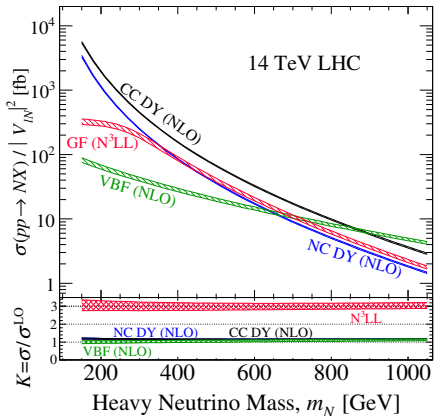
⇒ more physical collider definitions + public tools

HeavyN UFOs [1602.06957]

¹DY@NLO [*1509.06375]; GF [1408.0983; *1602.06957] @NNNLL [*1706.02298]; VBF [1308.2209, *1411.7305,

*1602.06957]; DY,VBF Automation@NLO [*1602.06957]. For extensive details, see review: [*1711.02180].

Across different colliders, wild interplay of PDF and matrix elements



w/ Pascoli, RR, et al, [1812.08750]

Plotted: Flavor-independent heavy N production rate ($\sigma/|V|^2$) vs mass

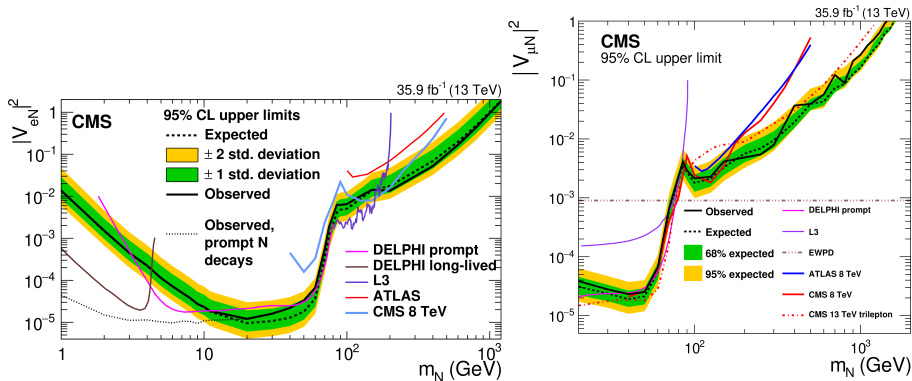
- **GF** and **VBF** dominate at larger \sqrt{s} , m_N
- At $\sqrt{s} = 100$ TeV and $|V_{eN}|^2 \sim 10^{-3}$, about one $N(10 \text{ TeV})/\text{ab}^{-1}$

If roughly $BR \times \varepsilon \times \mathcal{A} \times \mathcal{L} \sim \frac{1}{3} \times 30 \text{ ab}^{-1}$, then $\sqrt{N_{Obs}} > 3\sigma$

Experimental Tests on Intermediate- and High-Mass N

Joint push by hep-ex and hep-ph/th have broken new ground!

Plotted: LHC 14 sensitivity to $(\text{coupling})^2$ vs heavy neutrino mass



Plotted: Exclusion on mixing $|V_{eN}|^2$ vs heavy N mass (m_N)

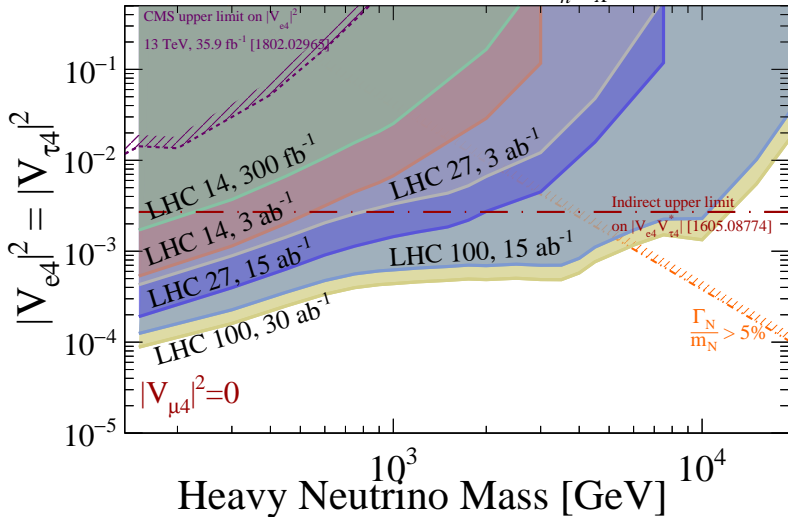
• (L) Search for $pp \rightarrow Nl \rightarrow 3l + X$

[1802.02965]

• (R) Search for $pp \rightarrow Nl \rightarrow l^\pm l^\pm + nj + X$

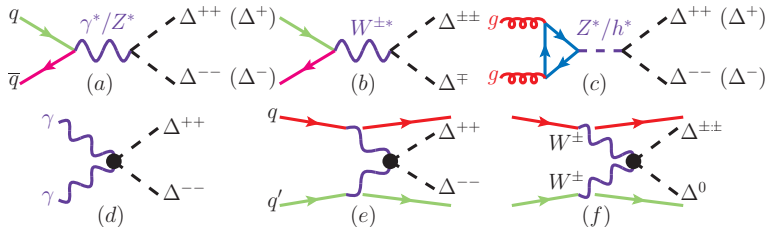
[1806.10905]

95% Sensitivity - $pp \rightarrow \tau_h e l_X / 3e / 2e\mu$



With $\mathcal{L} = 300 - 3000 \text{ fb}^{-1}$ of data, LHC can compete with dedicated experiments testing **charged lepton flavor violation**.

Type II Seesaw



Type II Seesaw Mechanism

Hypothesize an $SU(2)_L$ **scalar** triplet with **lepton number** $L = -2$

$$\hat{\Delta} = \frac{1}{\sqrt{2}} \begin{pmatrix} \Delta^+ & \sqrt{2}\Delta^{++} \\ \sqrt{2}\Delta^0 & -\Delta^+ \end{pmatrix}, \quad \text{with} \quad \mathcal{L}_{\Delta\Phi} \ni \mu_{h\Delta} \left(\Phi^\dagger \hat{\Delta} \cdot \Phi^\dagger + \text{H.c.} \right)$$

The mass scale $\mu_{h\Delta}$ explicitly breaks **lepton number**, and induces $\langle \hat{\Delta} \rangle$:

$$\sqrt{s} \langle \hat{\Delta} \rangle = v_\Delta \approx \frac{\mu_{h\Delta} v_{EW}}{\sqrt{2} m_\Delta^2}$$

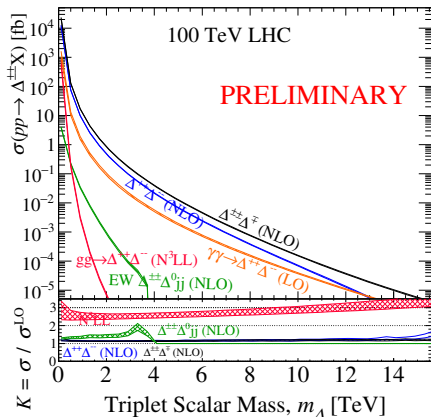
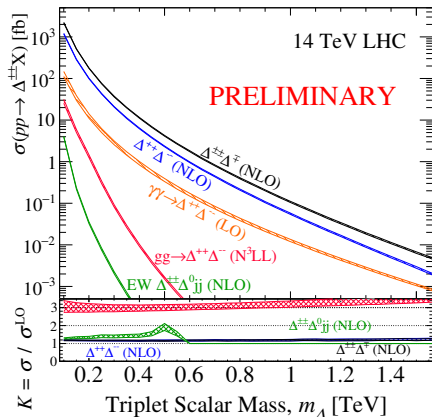
This includes a left-handed Majorana mass of neutrinos!

$$\begin{aligned} \mathcal{L} &= \frac{y_\Delta^{ij}}{\sqrt{2}} \overline{L^c} \hat{\Delta} L = \frac{y_\Delta^{ij}}{\sqrt{2}} \begin{pmatrix} \overline{\nu^{jc}} & \overline{\ell^{jc}} \end{pmatrix} \begin{pmatrix} 0 & 0 \\ v_\Delta & 0 \end{pmatrix} \begin{pmatrix} \nu^i \\ \ell^i \end{pmatrix} \\ &\ni \frac{1}{2} \underbrace{\left(\sqrt{2} y_\Delta^{ij} v_\Delta \right)}_{=m_\nu^{ij}} \overline{\nu^{jc}} \nu^i \end{aligned}$$

Generates light ν_m masses via vev **WITHOUT** invoking a sterile N !

Type II Seesaw is characterized by existence of **scalars** that are triplets under $SU(2)_L$: Δ^0 , Δ^\pm , $\Delta^{\pm\pm}$

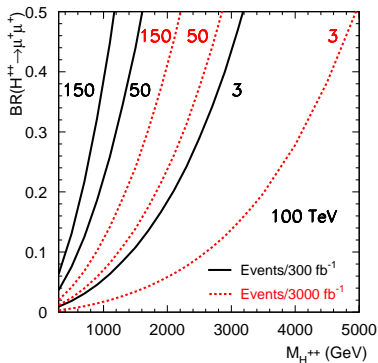
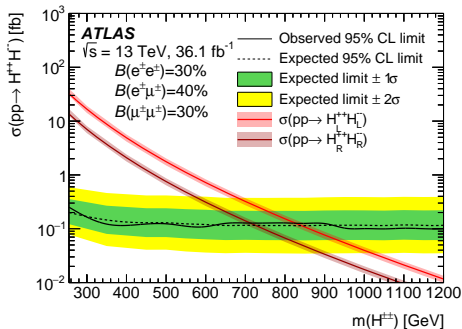
- Couples to W, Z, γ through gauge couplings



Production at 100 TeV **HUGE** compared to LHC!

- Clear that $\sigma_{DY}(\Delta^{\pm\pm} \Delta^{\mp\mp}) \gg \sigma_{\gamma\gamma}(\Delta^{\pm\pm} \Delta^{\mp\mp})$

Discovery Potential of Triplet Scalars

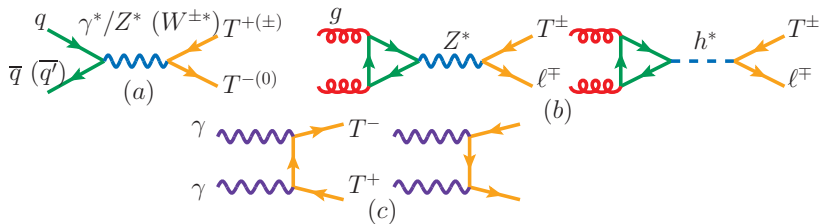


LHC: $m_{\Delta^{\pm\pm}} \lesssim 700 - 900 \text{ GeV}$ excluded with $\mathcal{L} \approx 36 \text{ fb}^{-1}$

- LHC Run III-V: Anticipate $\sim 10 - 150\times$ more data

100 TeV: $m_{\Delta^{\pm\pm}} \lesssim 3 - 5 \text{ TeV}$ can be discovered within first 300-3000 fb^{-1}

Type III Seesaw



Type III Seesaw Mechanism

Introduce $SU(2)_L$ **fermion** triplet (zero hypercharge) with mass m_T

$$\Sigma = \begin{pmatrix} \Sigma_L^3 & \sqrt{2}\Sigma_L^+ \\ \sqrt{2}\Sigma_L^- & -\Sigma_L^3 \end{pmatrix},$$

$$\mathcal{L}_T = \frac{1}{2} \text{Tr} [\overline{\Sigma}_L i \not{D} \Sigma_L] - \left(\frac{m_T}{2} \overline{\Sigma}_L^3 \Sigma_R^{3c} + m_T \overline{\Sigma}_L^- \Sigma_R^{+c} + \text{H.c.} \right)$$

and couple to SM leptons via Higgs Yukawa couplings

$$\mathcal{L}_Y = y_T \overline{L}^c \Sigma_L (i\sigma^2) \Phi \rightarrow \frac{y_T}{\sqrt{2}} (v + h) \overline{\nu}_R^c \Sigma_L^3 + y_T (v + h) \overline{e}_R \Sigma_L^-$$

The resulting mass matrix for neutral fermions is

$$\mathcal{L} \ni \frac{1}{2} \overline{\mathcal{N}}^c \mathcal{M} \mathcal{N} = \frac{1}{2} \begin{pmatrix} \overline{\nu}_L^c & \overline{\Sigma}_L^{3c} \end{pmatrix} \begin{pmatrix} 0 & y_{\Sigma} v / \sqrt{2} \\ y_{\Sigma} v / \sqrt{2} & m_T \end{pmatrix} \begin{pmatrix} \nu_L \\ \Sigma_L^3 \end{pmatrix}$$

Type III Interaction Theory

Assuming that m_T (**Majorana** mass) $\gg y_T \langle \Phi \rangle$ (**Dirac** mass)

$$m_{\text{light}} \approx \frac{y_T^2 v^2}{2m_T}, \quad m_{\text{heavy}} \approx -m_T$$

For $m_{\text{light}} = 0.1$ eV, if $y_T \sim \mathcal{O}(y_e) \sim 1 \cdot 10^{-6}$, $m_{\text{heavy}} \approx 300$ GeV!

For today, denote mixing between gauge and mass states by Y and ϵ :

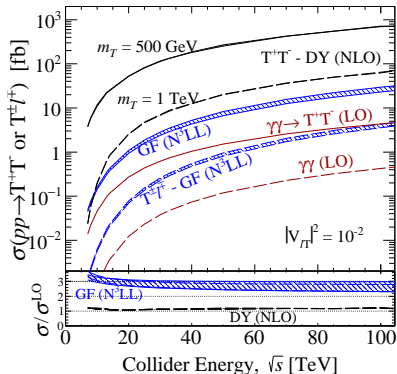
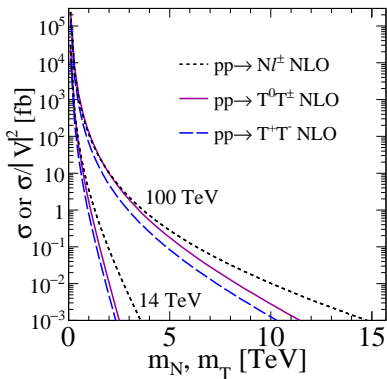
$$\tilde{T}^\pm = Y T^\pm + \epsilon \ell^\pm, \quad \tilde{T}^0 = Y T^0 + \epsilon \nu_m, \quad |Y| \sim \mathcal{O}(1), \quad |\epsilon| \ll 1.$$

In the mass basis (after mixing)

$$\mathcal{L}_T^{\text{Mass Basis}} \ni -\overline{T^-} (eY\gamma^\mu A_\mu + g \cos\theta_W Y\gamma^\mu Z_\mu) T^- \\ - gY\overline{T^-}\gamma^\mu W_\mu^- T^0 - gY\overline{T^0}\gamma^\mu W_\mu^+ T^-$$

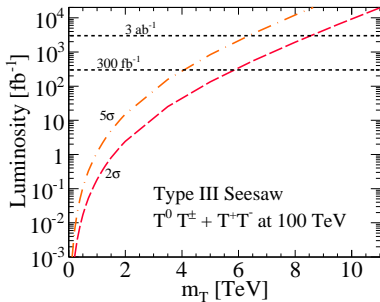
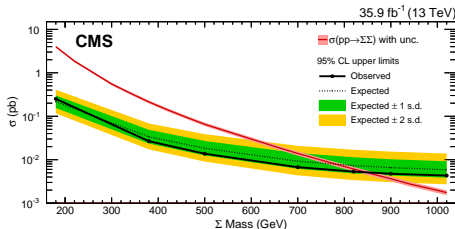
Type III Seesaw is characterized by existence of **leptons** that are triplets under $SU(2)_L$: T^0, T^\pm

- Couples to W, Z, γ through gauge couplings
- Generates light ν_m masses similar to Type I



- Production at 100 TeV **HUGE** compared to LHC!
- Clear that $\sigma_{DY}(T^+ T^-) \gg \sigma_{\gamma\gamma}(T^+ T^-)$
 - ▶ $\sigma_{GF}(T^\pm \ell^\mp)$ competitive if mixing sizable!

Discovery Potential of Triplet Leptons



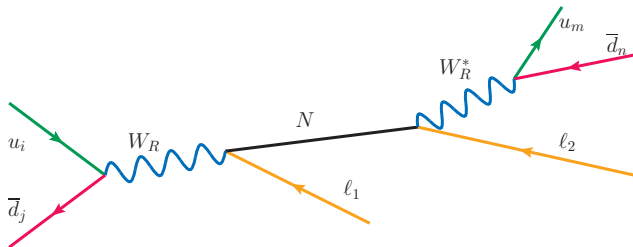
LHC: $m_T \lesssim 800$ GeV excluded with $\mathcal{L} \approx 36 \text{ fb}^{-1}$

- LHC Run III-V: Anticipate $\sim 10 - 150\times$ more data

100 TeV: $m_T \lesssim 4 - 6$ TeV can be discovered within first 300-3000 fb^{-1}

- Sensitivity can be improved with refined analysis and combining channels (See [[RR, 1509.05416](#)] for details)

Lecture II: Left-Right Symmetric Model





Thank you for your time.