

Hints for decaying dark matter from S_8 measurements

Guillermo Franco Abellán



Based on [arXiv:2008.09615](https://arxiv.org/abs/2008.09615) with
Riccardo Murgia, Vivian Poulin and Julien Laval

10/12/20

The S_8 tension

$$S_8 = \sigma_8 \sqrt{\frac{\Omega_m}{0.3}}$$

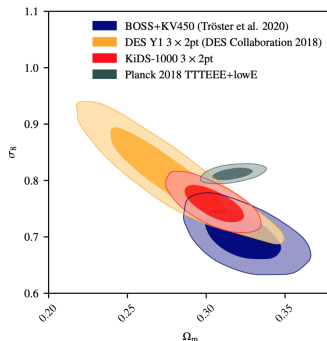
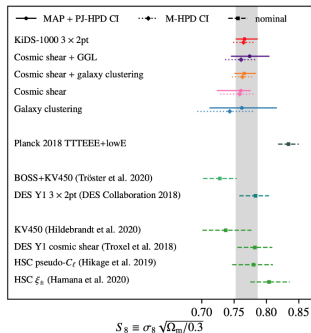
$$\text{where } \sigma_8 = \int \frac{k^3}{2\pi} P(k) W_R^2(k) d\ln k \quad \text{at } R = 8 \text{ Mpc}/h$$

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2–3 σ tension between Weak Lensing and CMB (assuming Λ CDM)



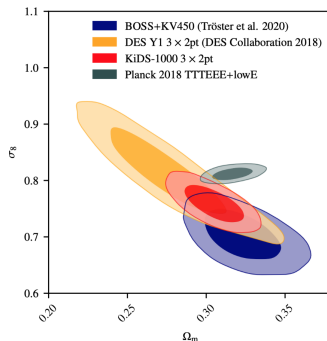
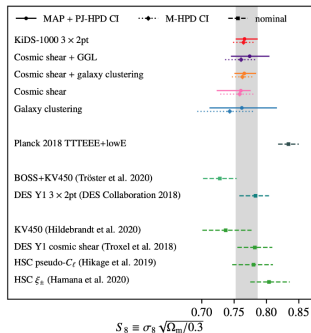
From [2008.11285](#)

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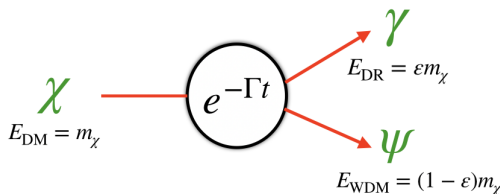
BOSS+KIDS+2dfLenS analysis revealed tension is mainly **driven by σ_8**

- Could the S_8 tension be related to **new physics**?

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Framework of the 2-body decay

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- Could it be related to the **stability of Dark Matter** (DM) on cosmological times scales?
- We explore DM decays to massless (**Dark Radiation**) and massive (**Warm Dark Matter**) particles, $\chi(\text{DM}) \rightarrow \gamma(\text{DR}) + \psi(\text{WDM})$



Two extra parameters:
 Γ and ϵ

Current status of the 2-body decay?

**Evolution of perturbations and
cosmological constraints in decaying
dark matter models with arbitrary
decay mass products**

Shohei Aoyama,¹ Toyokazu Sekiguchi,^{1,2} Kiyotomo
Ichiki³ and Naoshi Sugiyama^{1,3,4}

Full treatment of perts.,
no parameter scan

1402.2972

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Late universe decaying dark matter can relieve the H_0 tension

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*Department of Physics, Brown University, 182 Hope St., Providence, RI 02912 and
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Abraham Loeb
Department of Astronomy, Harvard University, 60 Garden St., Cambridge, MA 02138

1903.06220

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Late-time decaying dark matter: constraints and implications for the H_0 -tension

Balakrishna S. Haridasu,^{1,2*} Matteo Viel^{3,4,5,6†}

2004.07709

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CMB constraints on late-universe decaying dark matter as a solution to the H_0 tension

Steven J. Clark,^{*} Kyriakos Vattis[†] and Savvas M. Koushiappas[†]
*Department of Physics, Brown University, Providence, RI 02912-1843, USA and
Brown Theoretical Physics Center, Brown University, Providence, RI 02912-1843, USA*

2006.03678

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- Effects on $P(k)$ and C_ℓ ? \rightarrow Track **linear perturbations** for the daughter particles: δ_D , θ_D and σ_D

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- Boltzmann hierarchy of eqs. dictate the evolution of the **p.s.d. multipoles** $\Delta f_\ell(q, k, \tau)$
 - ◇ **DR treatment is easy**, momentum d.o.f. are integrated out
 - ◇ **For WDM**, one needs to follow the evolution of the full p.s.d. Computationally expensive $\rightarrow \mathcal{O}(10^8)$ **ODEs to solve !**

Evolution of perturbations: fluid approximation for the WDM

Based on a **fluid** description for massive neutrinos ([1104.2935](#))

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The eqs. (valid at $k\tau \gg 1$) read

$$\dot{\delta}_{\text{D}} = -3\mathcal{H}(c_{\text{syn}}^2 - w)\delta_{\text{D}} - (1 + w) \left(\theta_{\text{D}} + \frac{\dot{h}}{2} \right) + a\Gamma(1 - \varepsilon) \frac{\bar{\rho}_{\text{DM}}}{\bar{\rho}_{\text{D}}} (\delta_{\text{DM}} - \delta_{\text{D}})$$

$$\dot{\theta}_{\text{D}} = -\mathcal{H}(1 - 3c_a^2)\theta_{\text{D}} + \frac{c_{\text{syn}}^2}{1 + w} k^2 \delta_{\text{D}} - k^2 \sigma_{\text{D}} - a\Gamma(1 - \varepsilon) \frac{\bar{\rho}_{\text{DM}}}{\bar{\rho}_{\text{D}}} \frac{1 + c_a^2}{1 + w} \theta_{\text{D}}$$

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where

$$c_a^2(\tau) = w \left(5 - \frac{p_D}{\bar{P}_D} - \frac{\bar{\rho}_{\text{DM}}}{\bar{\rho}_D} \frac{a\Gamma}{3w\mathcal{H}} \frac{\varepsilon^2}{1 - \varepsilon} \right) \left[3(1 + w) - \frac{\bar{\rho}_{\text{DM}}}{\bar{\rho}_D} \frac{a\Gamma}{\mathcal{H}} (1 - \varepsilon) \right]^{-1}$$

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$$c_{\text{syn}}^2(k, \tau) = c_a^2(\tau) [1 + (1 - 2\varepsilon) T(k/k_{\text{fs}})]$$

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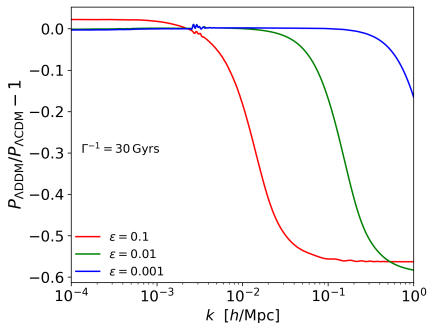
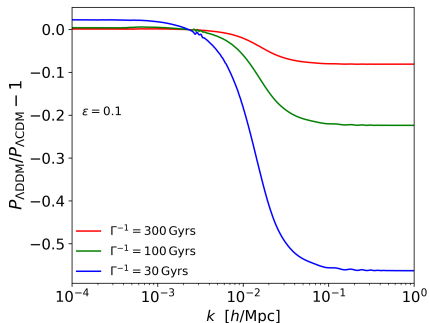
Accurate at the $\mathcal{O}(0.1\%)$ level in C_ℓ , and at $\mathcal{O}(1\%)$ level in $P(k)$

CPU time reduced from ~ 1 day to ~ 1 minute!

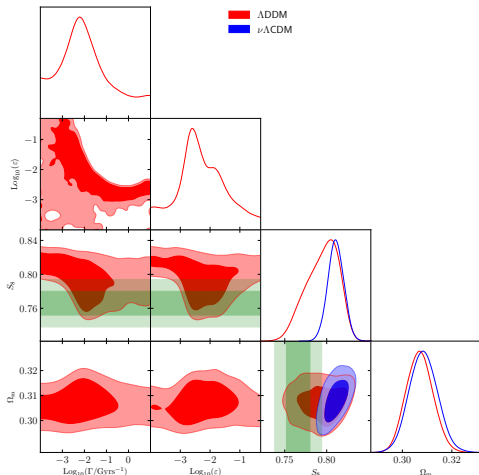
The WDM daughter leads to a **power suppression** in $P(k)$
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- Γ controls the **depth** of the power suppression
- ϵ controls the **cut-off** scale (k_{fs})



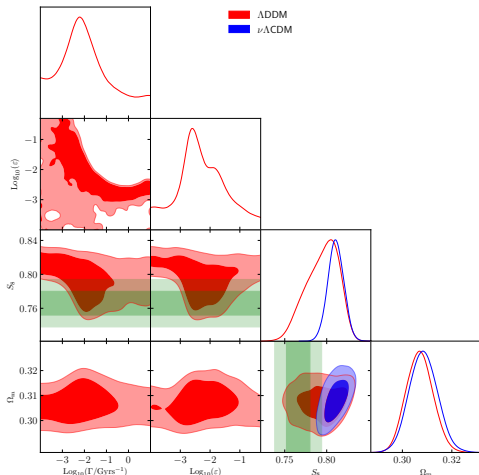
Resolving the S_8 tension with the 2-body decay



- Modified version of CLASS
Run MCMC against **Planck**, **BAO**
SN Ia, $f\sigma_8$ & S_8 ¹

¹ $S_8 = 0.766^{+0.020}_{-0.014}$ from KIDS+BOSS+2dfLenS

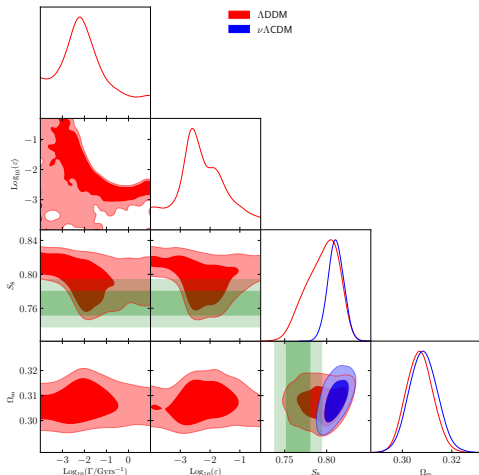
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	$\nu\Lambda\text{CDM}$	ADDM
χ^2_{CMB}	1015.9	1015.2
$\chi^2_{S_8}$	5.64	0.002

$$\rightarrow \Delta\chi^2_{\text{min}} \simeq -5.5$$

$$\epsilon \simeq 0.7 \% \text{ and } \Gamma^{-1} \simeq 55 \text{ Gyrs}$$

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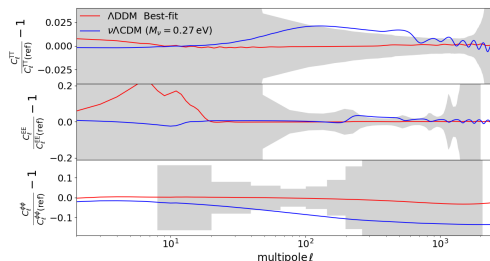
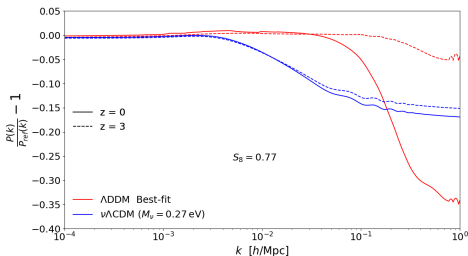
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Best-fit cosmology and comparison with massive neutrinos

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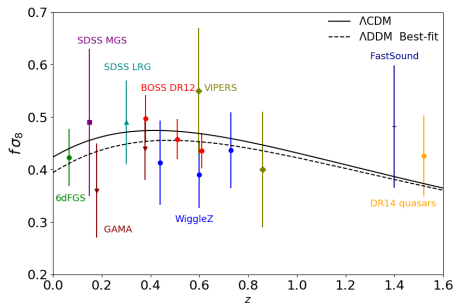
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Some promising implications

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Accurate measurements of $f\sigma_8$ at $0 \lesssim z \lesssim 1$ will further test the 2-body decay

- First thorough cosmological analysis of the 2-body decay scenario
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- Many interesting implications (DM model building, small-scale crisis, Xenon-1T excess)
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THANKS FOR YOUR ATTENTION

Bonus I: The full Boltzmann hierarchy

$$f(q, k, \mu, \tau) = \bar{f}(q, \tau) + \Delta f(q, k, \mu, \tau)$$

Expand Δf in multipoles. The Boltzmann eq. leads to the following **hierarchy** (in *synchronous* gauge comoving with the mother)

$$\begin{aligned}\frac{\partial}{\partial \tau} (\Delta f_0) &= -\frac{\mathbf{q}k}{\mathcal{E}} \Delta f_1 + q \frac{\partial \bar{f}}{\partial q} \frac{\dot{h}}{6} + a \frac{\Gamma \bar{N}_M(\tau)}{4\pi q^3 \mathcal{H}} \delta(\tau - \tau_q) \delta_M, \\ \frac{\partial}{\partial \tau} (\Delta f_1) &= \frac{\mathbf{q}k}{3\mathcal{E}} [\Delta f_0 - 2\Delta f_2], \\ \frac{\partial}{\partial \tau} (\Delta f_2) &= \frac{\mathbf{q}k}{5\mathcal{E}} [2\Delta f_1 - 3\Delta f_3] - q \frac{\partial \bar{f}}{\partial q} \frac{(\dot{h} + 6\dot{\eta})}{15}, \\ \frac{\partial}{\partial \tau} (\Delta f_l) &= \frac{\mathbf{q}k}{(2l+1)\mathcal{E}} [l\Delta f_{l-1} - (l+1)\Delta f_{l+1}] \quad (\text{for } l \geq 3).\end{aligned}$$

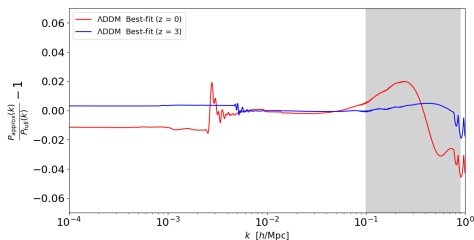
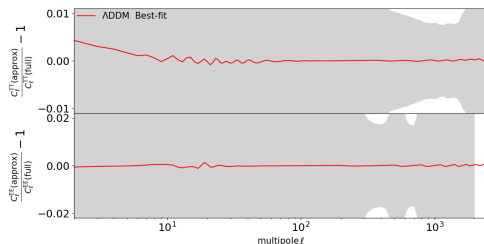
where $q = a(\tau_q) p_{\text{max}}$. In the relat. limit $\mathbf{q}/\mathcal{E} = 1$, so we can take

$F_l \equiv \frac{4\pi}{\rho_c} \int dq q^3 \Delta f_l$ and **integrate out the dependency on q**

Bonus II: Checking the accuracy of the fluid approximation

We compare two configurations (at the **best-fit** values)

- **Full**: Solve Boltzmann hierarchy with $N_q = 10^4$
- **Approx**: Solve Boltzmann hierarchy with $N_q = 300$ and switch-on fluid eqs. at $k\tau > 25$



The residual error on S_8 is $\sim 0.65\%$, smaller than the $\sim 1.8\%$ error of the measurement from BOSS+KIDS+2dfLenS