

Impact of PDFs on global interpretations
Celine Degrande

Plan

- Introduction
- PDF
- EFT
- PDF and EFT
- Outlook

PRL 123 (2019) no.13, 132001 with S. Carrazza, S. Iranipour, J. Rojo and M. Ubiali

Introduction

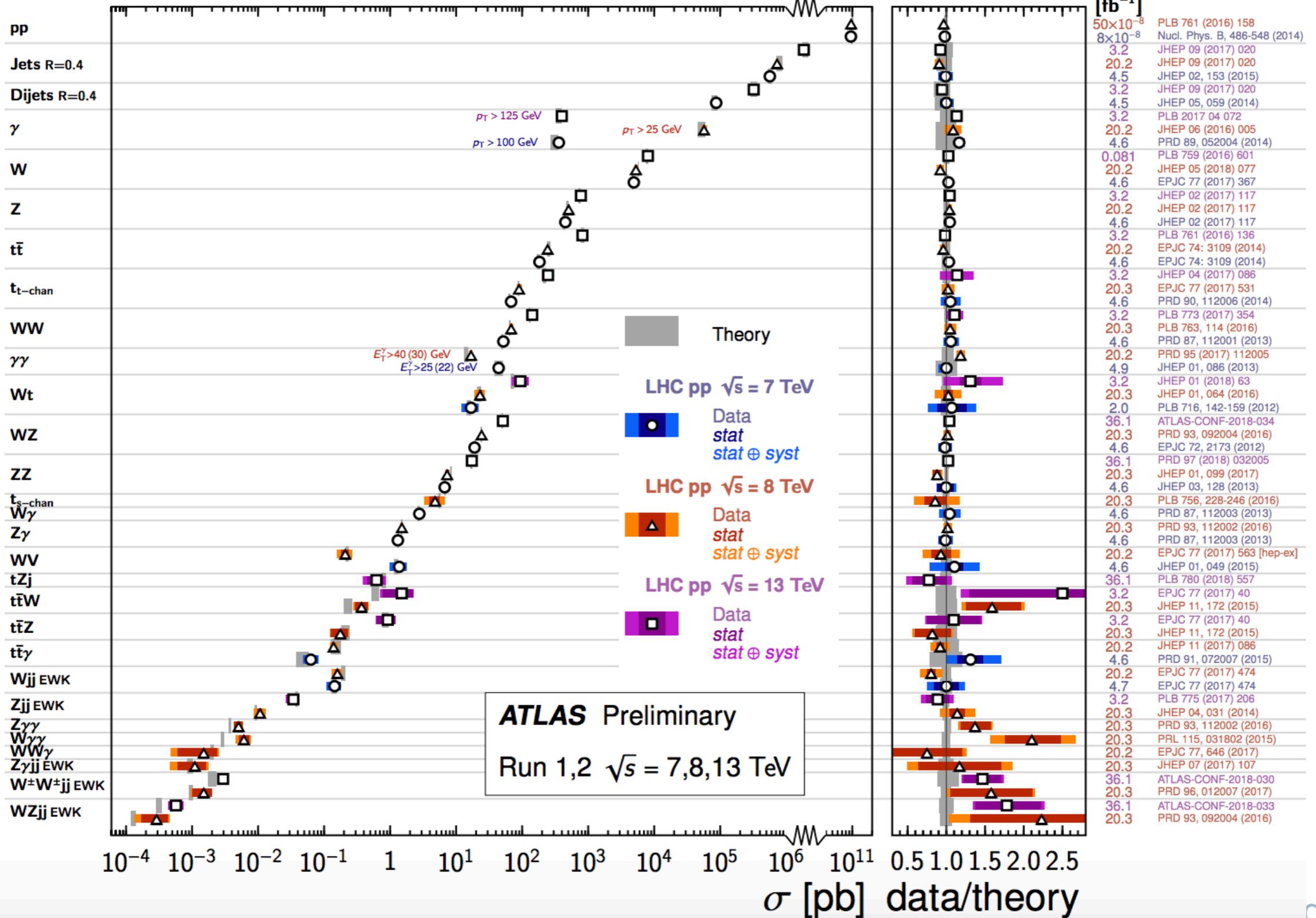
Precision era at the LHC

Standard Model Production Cross Section Measurements

Status: July 2018

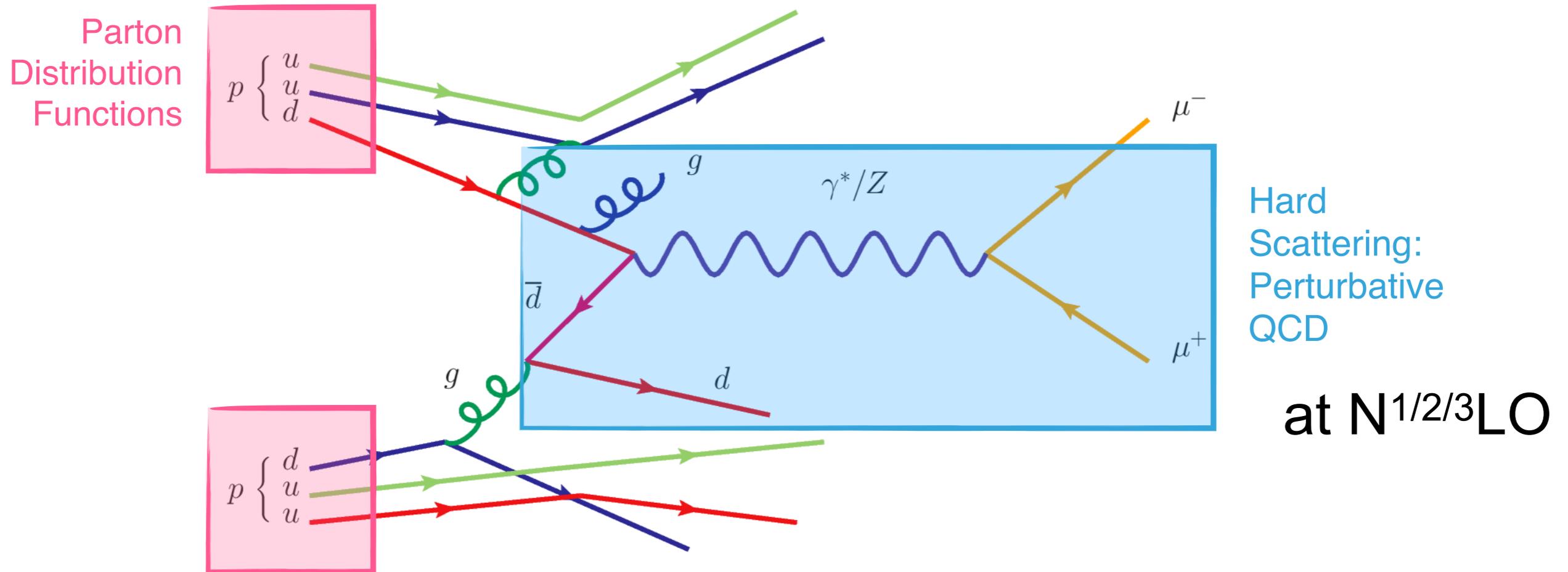
$\int \mathcal{L} dt$
[fb⁻¹]
50 × 10⁻⁸
8 × 10⁻⁸

Reference



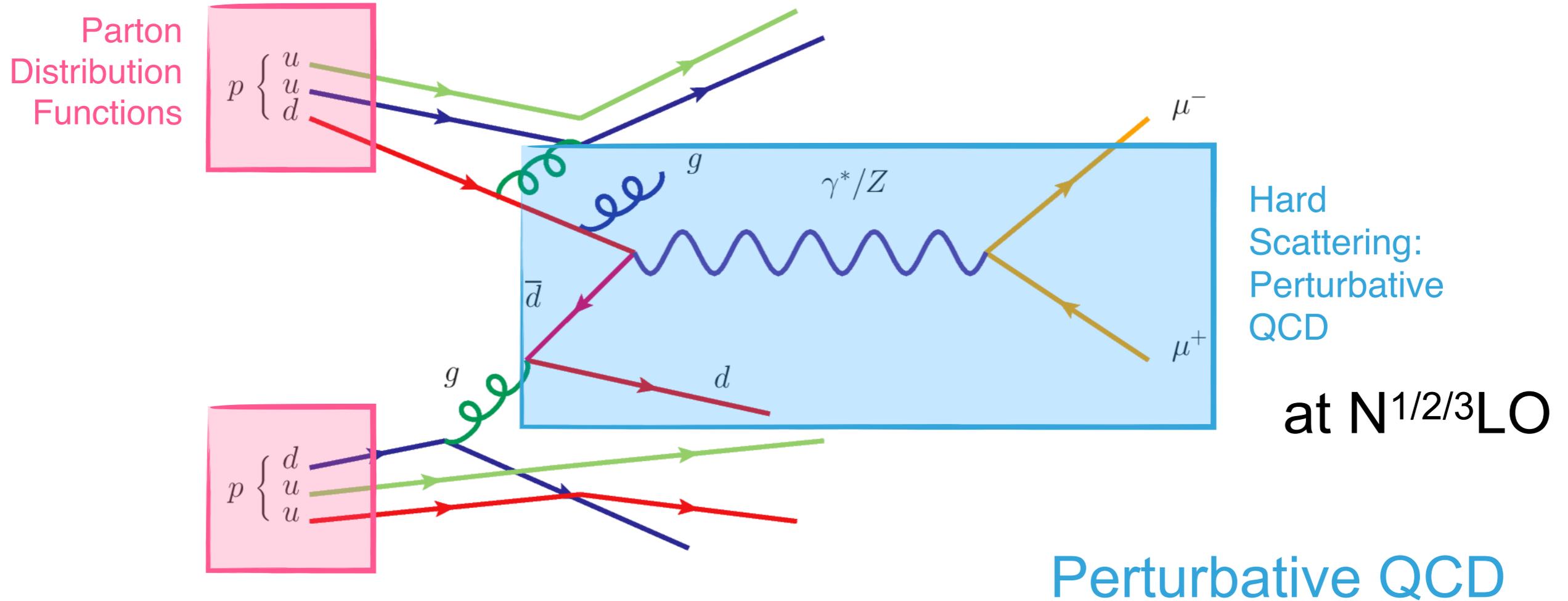
PDF

Precise predictions



$$d\sigma^{pp \rightarrow ab} = \sum_{i,j} f_i \otimes f_j \otimes d\hat{\sigma}^{ij \rightarrow ab} + \dots$$

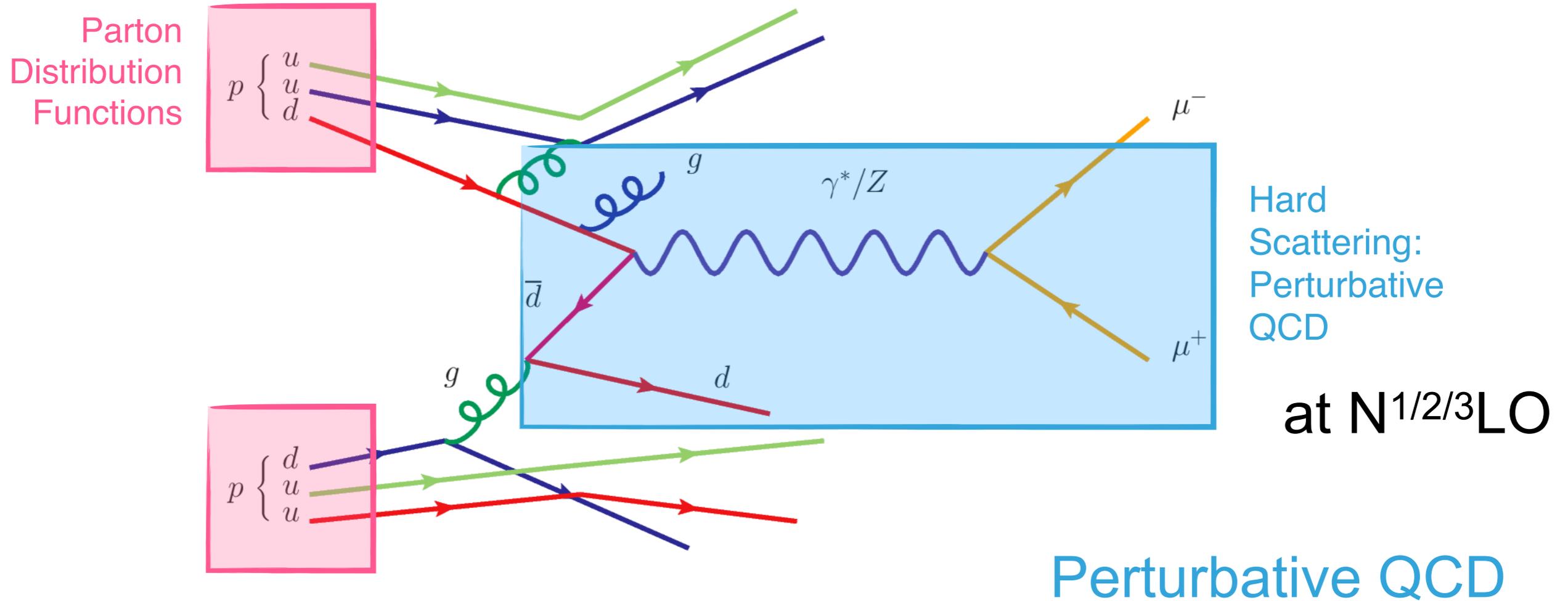
Precise predictions



$$d\sigma^{pp \rightarrow ab} = \sum_{i,j} f_i \otimes f_j \otimes d\hat{\sigma}^{ij \rightarrow ab} + \dots$$

$f_i(x, \mu)$
↑ data
↓ Perturbative QCD

Precise predictions

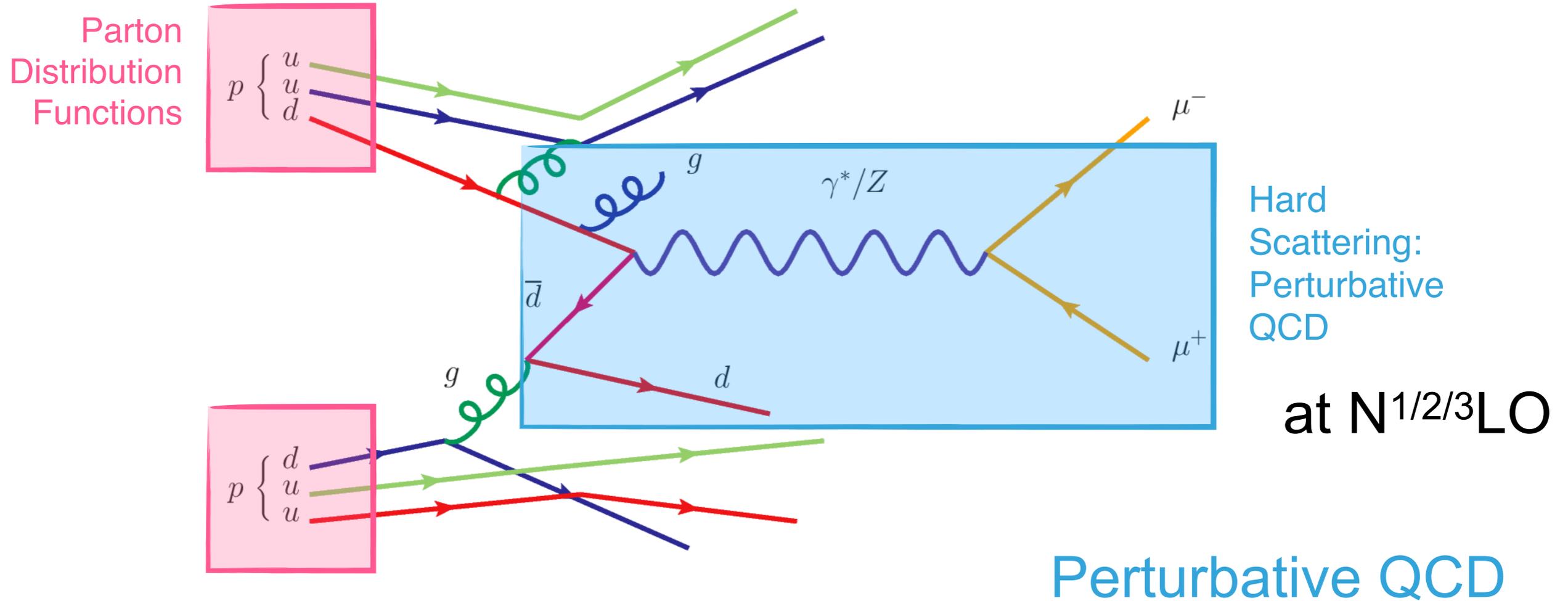


$$d\sigma^{pp \rightarrow ab} = \sum_{i,j} f_i \otimes f_j \otimes d\hat{\sigma}^{ij \rightarrow ab} + \dots$$

$f_i(x, \mu)$
↑ data
↓ Perturbative QCD

PDF are process universal

Precise predictions



$$d\sigma^{pp \rightarrow ab} = \sum_{i,j} f_i^{\text{SM}} \otimes f_j^{\text{SM}} \otimes d\hat{\sigma}^{ij \rightarrow ab} + \dots$$

\ni LHC

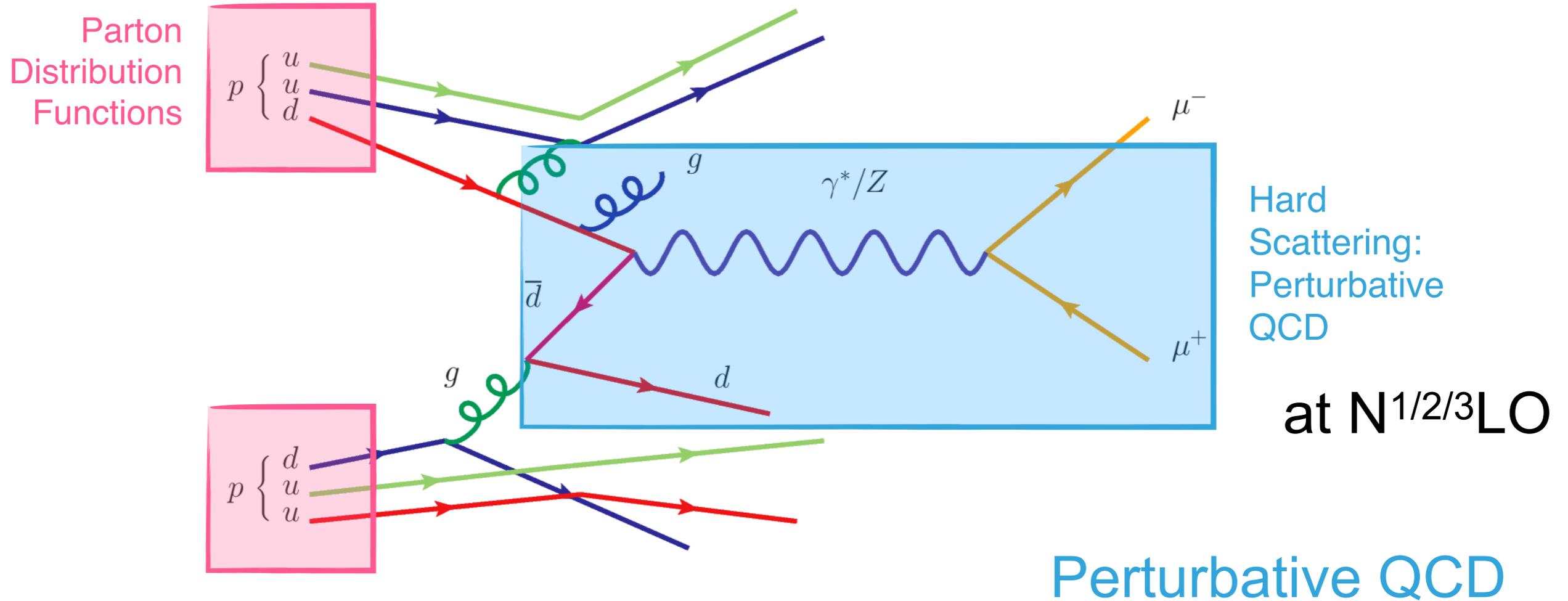
SM

data

$f_i(x, \mu)$

PDF are process universal

Precise predictions



$$d\sigma^{pp \rightarrow ab} = \sum_{i,j} f_i^{\text{SM}} \otimes f_j^{\text{SM}} \otimes d\hat{\sigma}^{ij \rightarrow ab} + \dots$$

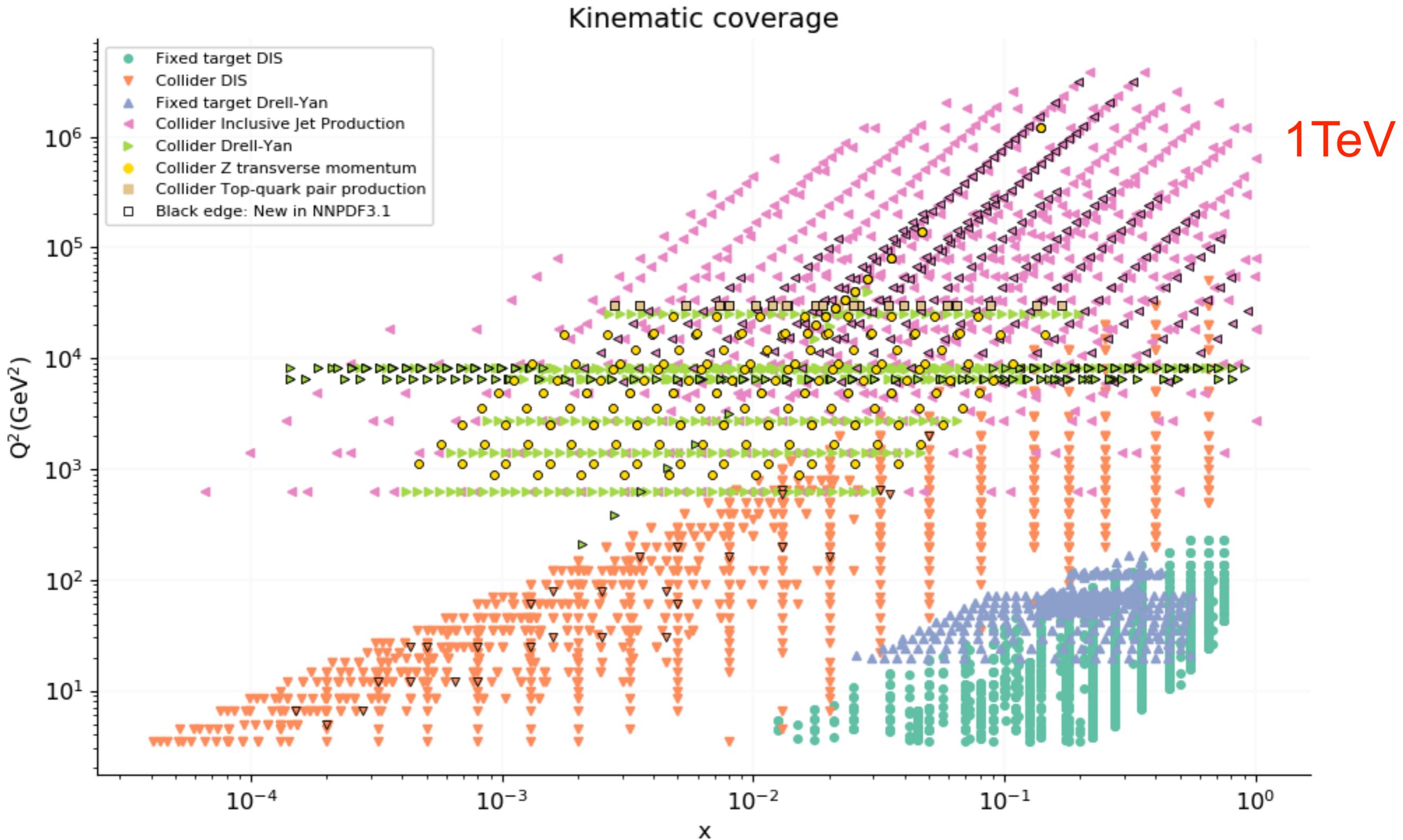
\ni LHC SM data

$f_i(x, \mu)$

Perturbative QCD

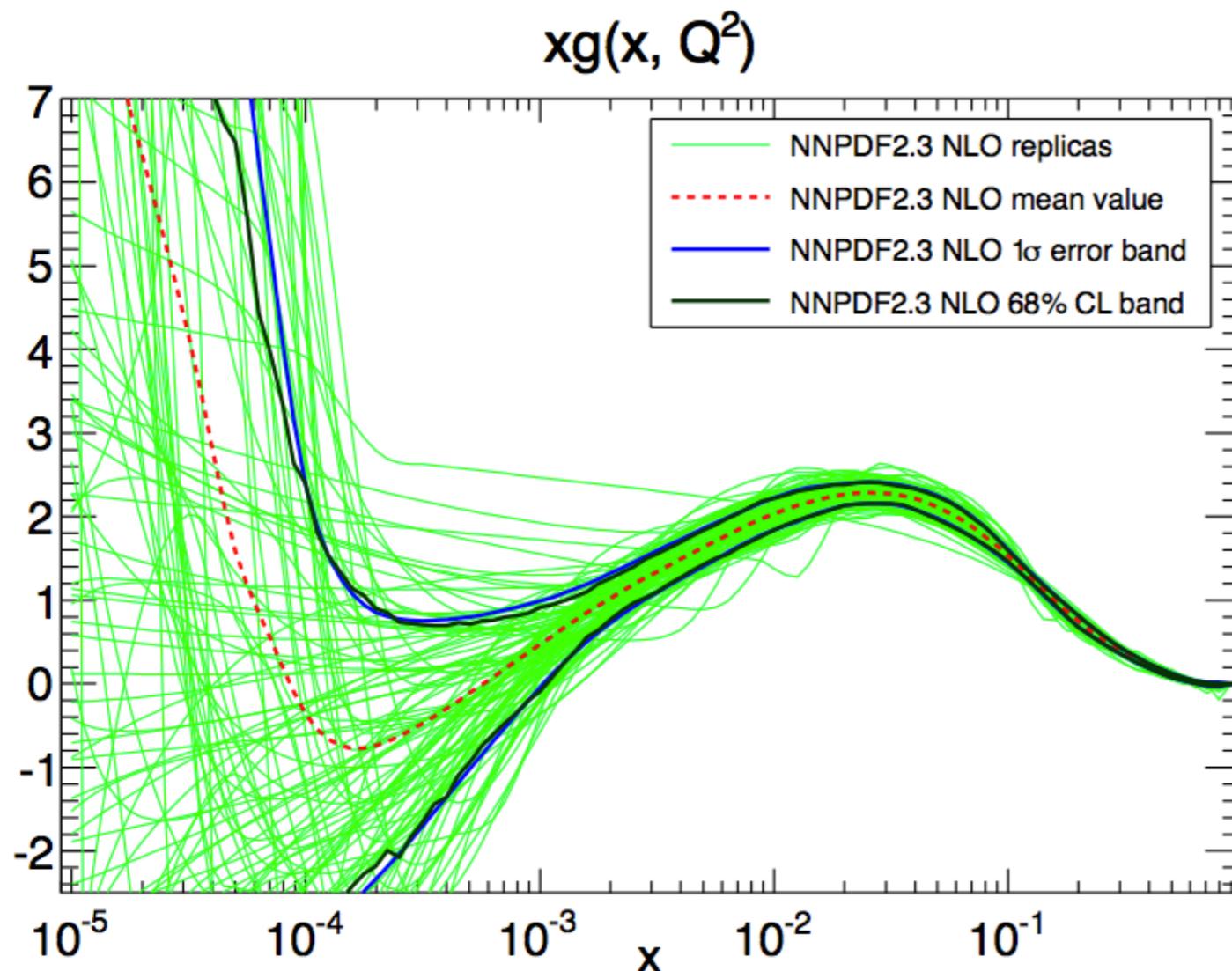
PDF are process universal **but model dependent**

PDF data



NNPDF

$$F_p^{(\text{art})}(k) = S_{p,N}^{(k)} F_p^{(\text{exp})} \left(1 + \sum_{l=1}^{N_c} r_{p,l}^{(k)} \sigma_{p,l} + r_p^{(k)} \sigma_{p,s} \right)$$

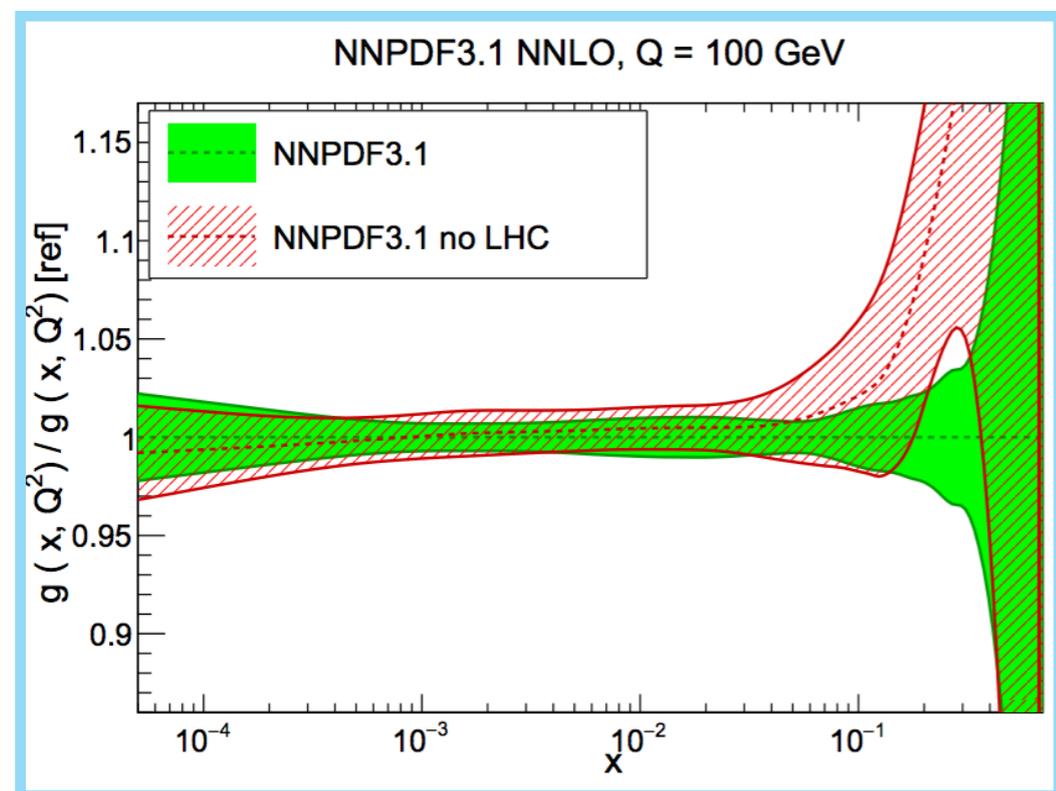
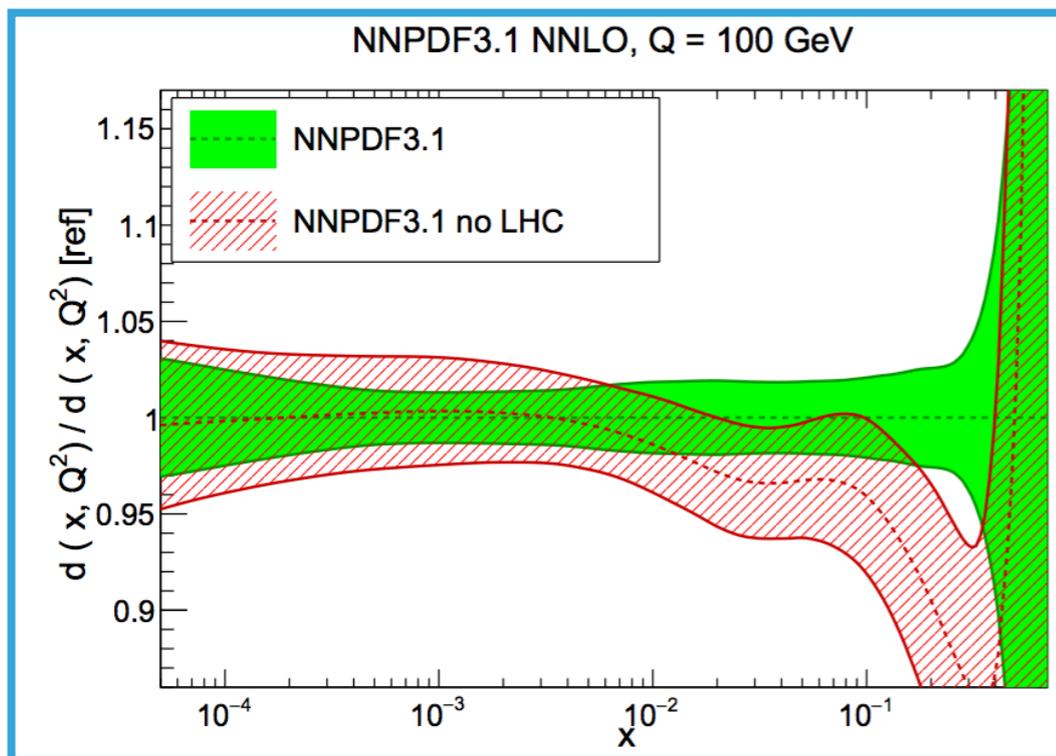


The N(eural)N(etwork)PDFs:

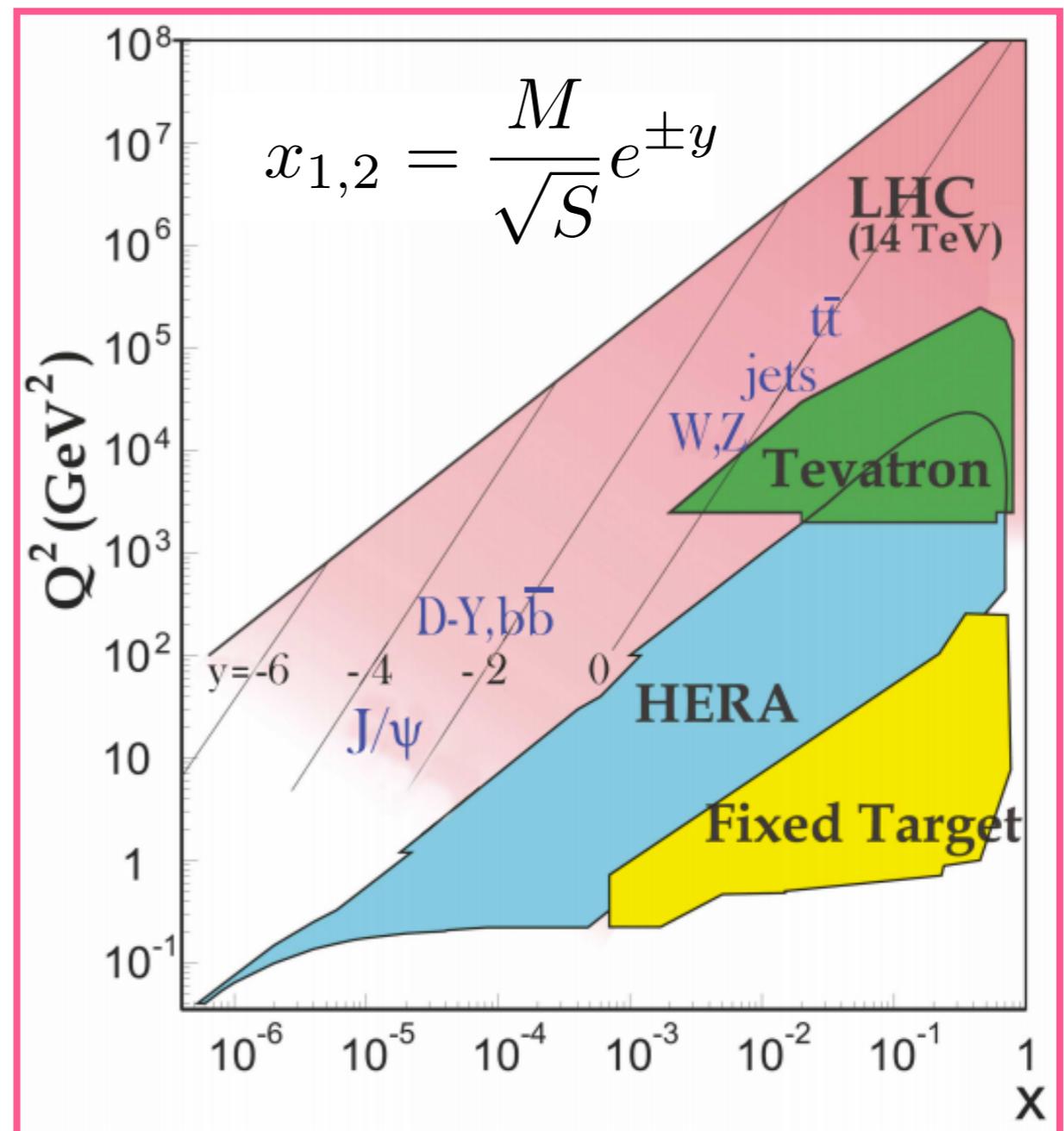
- Monte Carlo techniques: sampling the probability measure in PDF functional space
- Neural Networks: all independent PDFs are associated to an unbiased and flexible parametrization: $O(300)$ parameters versus $O(30)$ in polynomial parametrization
- Genetic algorithm and cross-validation methods

$$\chi^2 = \sum_{i,j=1}^{N_{\text{dat}}} (D_i - T_i) (\text{cov})_{ij}^{-1} (D_j - T_j)$$

Impact of LHC data



Ball et al, EPJC 77 (2017)



- LHC data provide powerful constrain especially at large x, in the large invariant mass region

EFT

Indirect detection of NP

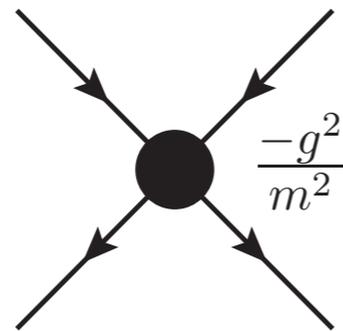
- Assumption : NP scale \gg energy probed in experiments E



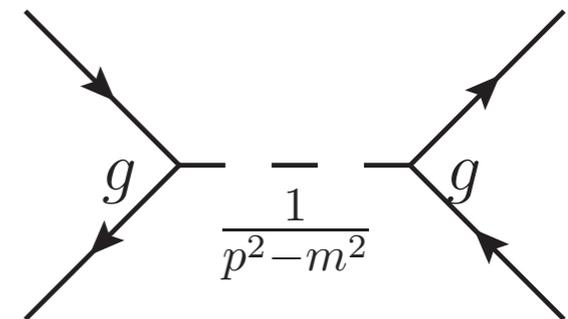
Exp. range



NP scale



$$p^2 \ll m^2$$



One assumption : $p^2 \ll m^2$

Ex : Fermi theory $-\frac{G_F}{\text{Sqrt}[2]} J^\mu J_\mu, \quad J_\mu = J_\mu^l + J_\mu^h, \quad J_\mu^l = \nu_l \gamma_\mu (1 - \gamma_5) l$

Expansion of the Lagrangian

$$L^{NP} = -\frac{1}{4}V^{\mu\nu}V_{\mu\nu} + M^2V^\mu V_\mu + \sum_i g_i V_\mu J_i^\mu + h.c.$$

- if V is very heavy $-\frac{1}{4}V^{\mu\nu}V_{\mu\nu} \sim 0$
- and the EOM is $V^\mu = -\frac{1}{M^2} \sum_i g_i J_i^\mu + h.c.$

$$L_{EFT}^{NP} = -\frac{\left(\sum_i g_i J_i^\mu\right) \left(\sum_i g_i J_{\mu_i}\right)^\dagger}{M^2}$$

EFT

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{d>4} \sum_i \frac{C_i}{\Lambda^{d-4}} \mathcal{O}_i^d \leftarrow \text{SM fields \& sym.}$$

EFT

Parametrize any NP but an ∞ number of coefficients

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{d>4} \sum_i \frac{C_i}{\Lambda^{d-4}} \mathcal{O}_i^d \leftarrow \text{SM fields \& sym.}$$

- Assumption : $E_{\text{exp}} \ll \Lambda$

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{C_i}{\Lambda^2} \mathcal{O}_i^6$$

a finite number of
coefficients
=> Predictive!

- Model independent (i.e. parametrize a large class of models) : any **HEAVY** NP
- SM is the leading term : EFT for precision physics

EFT

Parametrize any NP but an ∞ number of coefficients

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{d>4} \sum_i \frac{C_i}{\Lambda^{d-4}} \mathcal{O}_i^d \leftarrow \text{SM fields \& sym.}$$

- Assumption : $E_{\text{exp}} \ll \Lambda$

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{C_i}{\Lambda^2} \mathcal{O}_i^6$$

measure only C_i/Λ^2

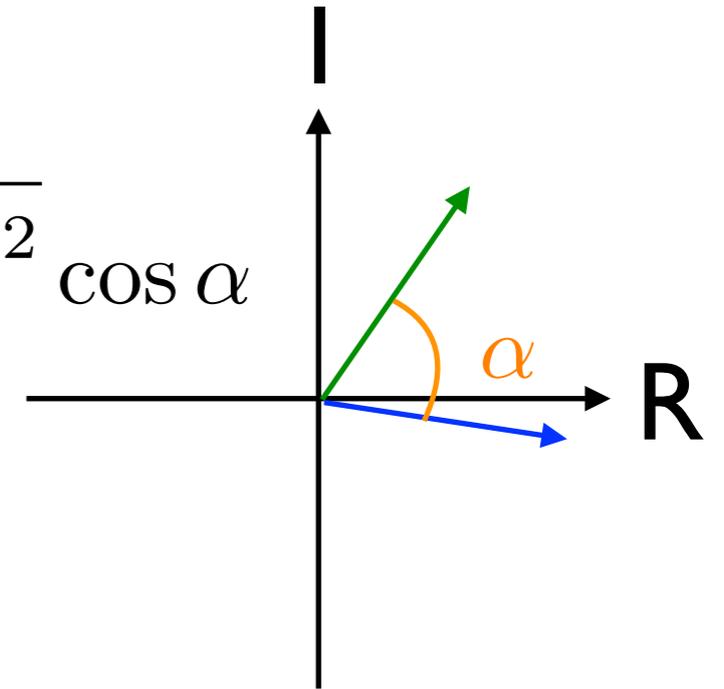
a finite number of
coefficients
 \Rightarrow Predictive!

- Model independent (i.e. parametrize a large class of models) : any **HEAVY** NP
- SM is the leading term : EFT for precision physics

Interference

$$|M(x)|^2 = \underbrace{|M_{SM}(x)|^2}_{\Lambda^0} + \underbrace{2\Re(M_{SM}(x)M_{d6}^*(x))}_{\Lambda^{-2}} + \underbrace{|M_{d6}(x)|^2 + \dots}_{\mathcal{O}(\Lambda^{-4})}$$

$$\Re(M_{SM}(x)M_{d6}^*(x)) = \sqrt{|M_{SM}(x)|^2 |M_{d6}(x)|^2} \cos \alpha$$



Not always positive

Can be suppressed

$$\sigma \propto \sum_x |M(x)|^2 \quad \text{if} \quad \begin{array}{l} M_{SM}(x_1) = 1, M_{SM}(x_2) = 0 \\ M_{d6}(x_1) = 0, M_{d6}(x_2) = 1 \end{array} \quad \sigma_{int} = 0$$

Observable dependent

A top example

Top operators

Assume (**To be checked**) that all the **operators without top** are better **constrained** by other processes (i.e. not involving the top)

$U(2)_q \times U(2)_u \times U(2)_d$ flavour symmetry

=MFV with all F massless but t,b

four heavy quarks	11 + 2 CPV
two light and two heavy quarks	14
two heavy quarks and bosons	9 + 6 CPV
two heavy quarks and two leptons	(8 + 3 CPV) × 3 lepton flavours

top pair production

From the Warsaw basis

Two-light-two-heavy (14 d.o.f.)

$$\begin{aligned}
 c_{Qq}^{3,1} &\equiv C_{qq}^{3(ii33)} + \frac{1}{6}(C_{qq}^{1(i33i)} - C_{qq}^{3(i33i)}) \\
 c_{Qq}^{3,8} &\equiv C_{qq}^{1(i33i)} - C_{qq}^{3(i33i)} \\
 c_{Qq}^{1,1} &\equiv C_{qq}^{1(ii33)} + \frac{1}{6}C_{qq}^{1(i33i)} + \frac{1}{2}C_{qq}^{3(i33i)} \\
 c_{Qq}^{1,8} &\equiv C_{qq}^{1(i33i)} + 3C_{qq}^{3(i33i)} \\
 c_{Qu}^1 &\equiv C_{qu}^{1(33ii)} \\
 c_{Qu}^8 &\equiv C_{qu}^{8(33ii)} \\
 c_{Qd}^1 &\equiv C_{qd}^{1(33ii)} \\
 c_{Qd}^8 &\equiv C_{qd}^{8(33ii)} \\
 c_{tq}^1 &\equiv C_{qu}^{1(ii33)} \\
 c_{tq}^8 &\equiv C_{qu}^{8(ii33)} \\
 c_{tu}^1 &\equiv C_{uu}^{(ii33)} + \frac{1}{3}C_{uu}^{(i33i)} \\
 c_{tu}^8 &\equiv 2C_{uu}^{(i33i)} \\
 c_{td}^1 &\equiv C_{ud}^{1(33ii)} \\
 c_{td}^8 &\equiv C_{ud}^{8(33ii)}
 \end{aligned}$$

Two-heavy

$$c_{tG}^{[I]} \equiv \frac{[\text{Im}]}{[\text{Re}]} \{ C_{uG}^{(33)} \}$$

$$\begin{aligned}
 O_{qq}^{1(ijkl)} &= (\bar{q}_i \gamma^\mu q_j)(\bar{q}_k \gamma_\mu q_l), \\
 O_{qq}^{3(ijkl)} &= (\bar{q}_i \gamma^\mu \tau^I q_j)(\bar{q}_k \gamma_\mu \tau^I q_l), \\
 O_{qu}^{1(ijkl)} &= (\bar{q}_i \gamma^\mu q_j)(\bar{u}_k \gamma_\mu u_l), \\
 O_{qu}^{8(ijkl)} &= (\bar{q}_i \gamma^\mu T^A q_j)(\bar{u}_k \gamma_\mu T^A u_l), \\
 O_{qd}^{1(ijkl)} &= (\bar{q}_i \gamma^\mu q_j)(\bar{d}_k \gamma_\mu d_l), \\
 O_{qd}^{8(ijkl)} &= (\bar{q}_i \gamma^\mu T^A q_j)(\bar{d}_k \gamma_\mu T^A d_l), \\
 O_{uu}^{(ijkl)} &= (\bar{u}_i \gamma^\mu u_j)(\bar{u}_k \gamma_\mu u_l), \\
 O_{ud}^{1(ijkl)} &= (\bar{u}_i \gamma^\mu u_j)(\bar{d}_k \gamma_\mu d_l), \\
 O_{ud}^{8(ijkl)} &= (\bar{u}_i \gamma^\mu T^A u_j)(\bar{d}_k \gamma_\mu T^A d_l),
 \end{aligned}$$

$$\ddagger O_{uG}^{(ij)} = (\bar{q}_i \sigma^{\mu\nu} T^A u_j) \tilde{\varphi} G_{\mu\nu}^A,$$

Top operators

Two-heavy (9 + 6 CPV d.o.f.)

$$\begin{aligned}
 c_{t\varphi}^{[I]} &\equiv \frac{[\text{Im}]\{C_{u\varphi}^{(33)}\}}{\text{Re}} \\
 c_{\varphi q}^- &\equiv C_{\varphi q}^{1(33)} - C_{\varphi q}^{3(33)} \\
 c_{\varphi Q}^3 &\equiv C_{\varphi q}^{3(33)} \\
 c_{\varphi t} &\equiv C_{\varphi u}^{(33)} \\
 c_{\varphi tb}^{[I]} &\equiv \frac{[\text{Im}]\{C_{\varphi ud}^{(33)}\}}{\text{Re}} \\
 c_{tW}^{[I]} &\equiv \frac{[\text{Im}]\{C_{uW}^{(33)}\}}{\text{Re}} \\
 c_{tZ}^{[I]} &\equiv \frac{[\text{Im}]\{-s_W C_{uB}^{(33)} + c_W C_{uW}^{(33)}\}}{\text{Re}} \\
 c_{bW}^{[I]} &\equiv \frac{[\text{Im}]\{C_{dW}^{(33)}\}}{\text{Re}} \\
 c_{tG}^{[I]} &\equiv \frac{[\text{Im}]\{C_{uG}^{(33)}\}}{\text{Re}}
 \end{aligned}$$

Two-heavy-two-lepton (8 + 3 CPV)

$$\begin{aligned}
 c_{Ql}^{3(\ell)} &\equiv C_{lq}^{3(\ell\ell 33)} \\
 c_{Ql}^{-\ell} &\equiv C_{lq}^{1(\ell\ell 33)} - C_{lq}^{3(\ell\ell 33)} \\
 c_{Qe}^{(\ell)} &\equiv C_{eq}^{(\ell\ell 33)} \\
 c_{tl}^{(\ell)} &\equiv C_{lu}^{(\ell\ell 33)} \\
 c_{te}^{(\ell)} &\equiv C_{eu}^{(\ell\ell 33)} \\
 c_t^{S[I](\ell)} &\equiv \frac{[\text{Im}]\{C_{lequ}^{1(\ell\ell 33)}\}}{\text{Re}} \\
 c_t^{T[I](\ell)} &\equiv \frac{[\text{Im}]\{C_{lequ}^{3(\ell\ell 33)}\}}{\text{Re}} \\
 c_b^{S[I](\ell)} &\equiv \frac{[\text{Im}]\{C_{ledq}^{(\ell\ell 33)}\}}{\text{Re}}
 \end{aligned}$$

From the Warsaw basis

$$\begin{aligned}
 \ddagger O_{u\varphi}^{(ij)} &= \bar{q}_i u_j \tilde{\varphi} (\varphi^\dagger \varphi), \\
 O_{\varphi q}^{1(ij)} &= (\varphi^\dagger \overleftrightarrow{iD}_\mu \varphi) (\bar{q}_i \gamma^\mu q_j), \\
 O_{\varphi q}^{3(ij)} &= (\varphi^\dagger \overleftrightarrow{iD}_\mu^I \varphi) (\bar{q}_i \gamma^\mu \tau^I q_j), \\
 O_{\varphi u}^{(ij)} &= (\varphi^\dagger \overleftrightarrow{iD}_\mu \varphi) (\bar{u}_i \gamma^\mu u_j), \\
 \ddagger O_{\varphi ud}^{(ij)} &= (\tilde{\varphi}^\dagger iD_\mu \varphi) (\bar{u}_i \gamma^\mu d_j), \\
 \ddagger O_{uW}^{(ij)} &= (\bar{q}_i \sigma^{\mu\nu} \tau^I u_j) \tilde{\varphi} W_{\mu\nu}^I, \\
 \ddagger O_{dW}^{(ij)} &= (\bar{q}_i \sigma^{\mu\nu} \tau^I d_j) \varphi W_{\mu\nu}^I, \\
 \ddagger O_{uB}^{(ij)} &= (\bar{q}_i \sigma^{\mu\nu} u_j) \tilde{\varphi} B_{\mu\nu}, \\
 \ddagger O_{uG}^{(ij)} &= (\bar{q}_i \sigma^{\mu\nu} T^A u_j) \tilde{\varphi} G_{\mu\nu}^A,
 \end{aligned}$$

$$\begin{aligned}
 O_{lq}^{1(ijkl)} &= (\bar{l}_i \gamma^\mu l_j) (\bar{q}_k \gamma^\mu q_l), \\
 O_{lq}^{3(ijkl)} &= (\bar{l}_i \gamma^\mu \tau^I l_j) (\bar{q}_k \gamma^\mu \tau^I q_l), \\
 O_{lu}^{(ijkl)} &= (\bar{l}_i \gamma^\mu l_j) (\bar{u}_k \gamma^\mu u_l), \\
 O_{eq}^{(ijkl)} &= (\bar{e}_i \gamma^\mu e_j) (\bar{q}_k \gamma^\mu q_l), \\
 O_{eu}^{(ijkl)} &= (\bar{e}_i \gamma^\mu e_j) (\bar{u}_k \gamma^\mu u_l), \\
 \ddagger O_{lequ}^{1(ijkl)} &= (\bar{l}_i e_j) \varepsilon (\bar{q}_k u_l), \\
 \ddagger O_{lequ}^{3(ijkl)} &= (\bar{l}_i \sigma^{\mu\nu} e_j) \varepsilon (\bar{q}_k \sigma_{\mu\nu} u_l), \\
 \ddagger O_{ledq}^{(ijkl)} &= (\bar{l}_i e_j) (\bar{d}_k q_l),
 \end{aligned}$$

Data

Process	Dataset	\sqrt{s}	Info	Observables	N_{dat}	Ref
$t\bar{t}$	ATLAS_tt_8TeV_1jets	8 TeV	lepton+jets	$d\sigma/d y_t $, $d\sigma/dp_t^T$, $d\sigma/dm_{t\bar{t}}$, $d\sigma/d y_{t\bar{t}} $	5, 8, 7, 5	[92]
$t\bar{t}$	CMS_tt_8TeV_1jets	8 TeV	lepton+jets	$d\sigma/dy_t$, $d\sigma/dp_t^T$, $d\sigma/dm_{t\bar{t}}$, $d\sigma/dy_{t\bar{t}}$	10, 8, 7, 10	[93]
$t\bar{t}$	CMS_tt2D_8TeV_dilep	8 TeV	dileptons	$d^2\sigma/dy_t dp_t^T$, $d^2\sigma/dy_t dm_{t\bar{t}}$, $d^2\sigma/dp_{t\bar{t}}^T dm_{t\bar{t}}$, $d^2\sigma/dy_{t\bar{t}} dm_{t\bar{t}}$	16, 16, 16, 16	[94]
$t\bar{t}$	CMS_tt_13TeV_1jets	13 TeV	lepton+jets	$d\sigma/d y_t $, $d\sigma/dp_t^T$, $d\sigma/dm_{t\bar{t}}$, $d\sigma/d y_{t\bar{t}} $	7, 9, 8, 6	[97]
$t\bar{t}$	CMS_tt_13TeV_1jets2	13 TeV	lepton+jets	$d\sigma/d y_t $, $d\sigma/dp_t^T$, $d\sigma/dm_{t\bar{t}}$, $d\sigma/d y_{t\bar{t}} $	11, 12, 10, 10	[99]
$t\bar{t}$	CMS_tt_13TeV_dilep	13 TeV	dileptons	$d\sigma/dy_t$, $d\sigma/dp_t^T$, $d\sigma/dm_{t\bar{t}}$, $d\sigma/dy_{t\bar{t}}$	8, 6, 6, 8	[100]
$t\bar{t}$	ATLAS_WhelF_8TeV	8 TeV	W helicity fract	F_0, F_L, F_R	3	[95]
$t\bar{t}$	CMS_WhelF_8TeV	8 TeV	W helicity fract	F_0, F_L, F_R	3	[96]

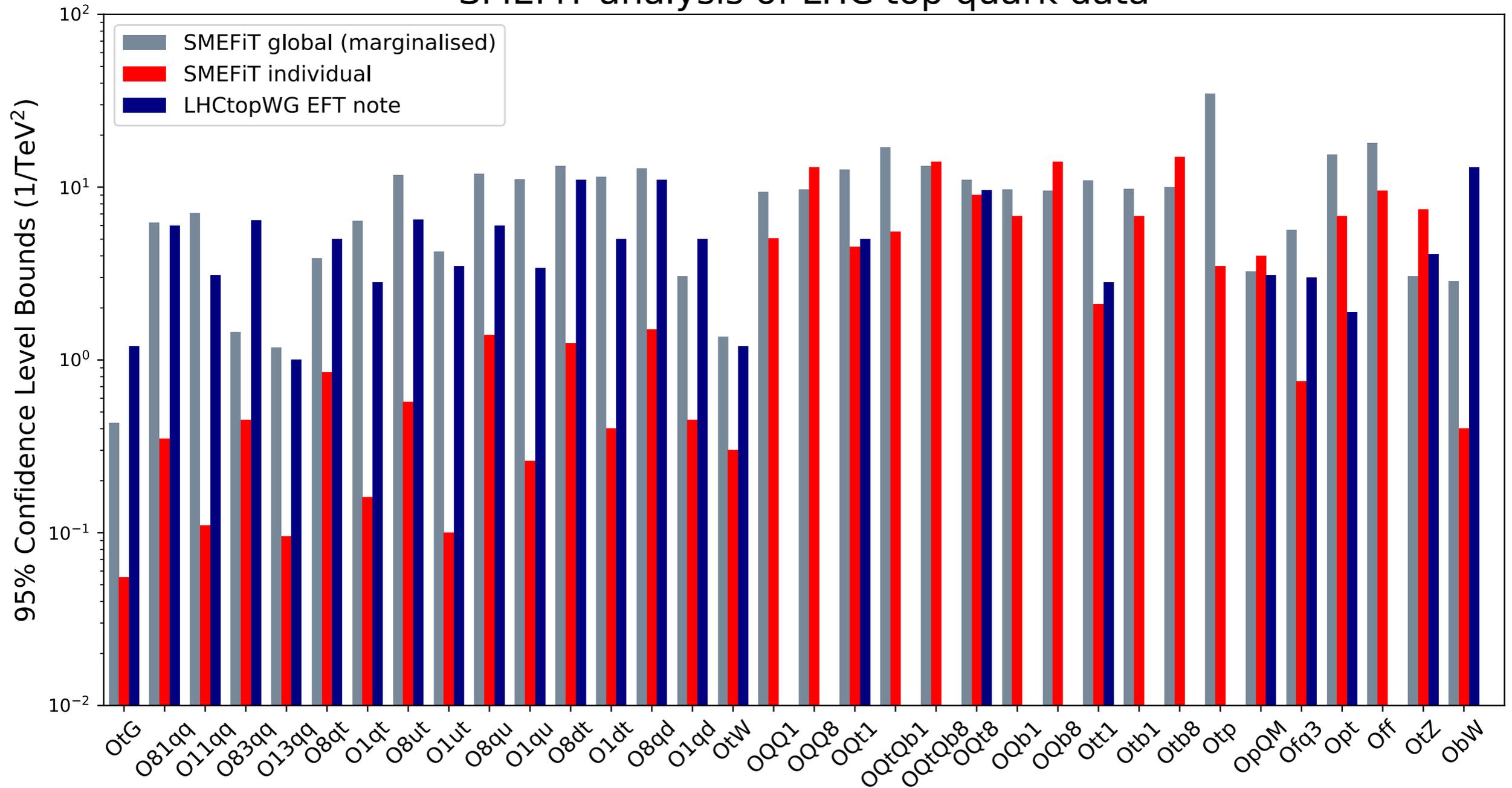
Only one distribution per measurement (correlation)

Data

Process	Dataset	\sqrt{s}	Info	Observables	N_{dat}	Ref
$t\bar{t}b\bar{b}$	CMS_ttbb_13TeV	13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}b\bar{b})$	1	[101]
$t\bar{t}t\bar{t}$	CMS_tttt_13TeV	13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}t\bar{t})$	1	[102]
$t\bar{t}Z$	CMS_ttZ_8_13TeV	8+13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}Z)$	2	[103, 104]
$t\bar{t}Z$	ATLAS_ttZ_8_13TeV	8+13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}Z)$	2	[105, 106]
$t\bar{t}W$	CMS_ttW_8_13TeV	8+13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}W)$	2	[103, 104]
$t\bar{t}W$	ATLAS_ttW_8_13TeV	8+13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}W)$	2	[105, 106]
$t\bar{t}H$	CMS_tth_13TeV	13 TeV	signal strength	$\mu_{t\bar{t}H}$	1	[107]
$t\bar{t}H$	ATLAS_tth_13TeV	13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}H)$	1	[108]

Global top fit

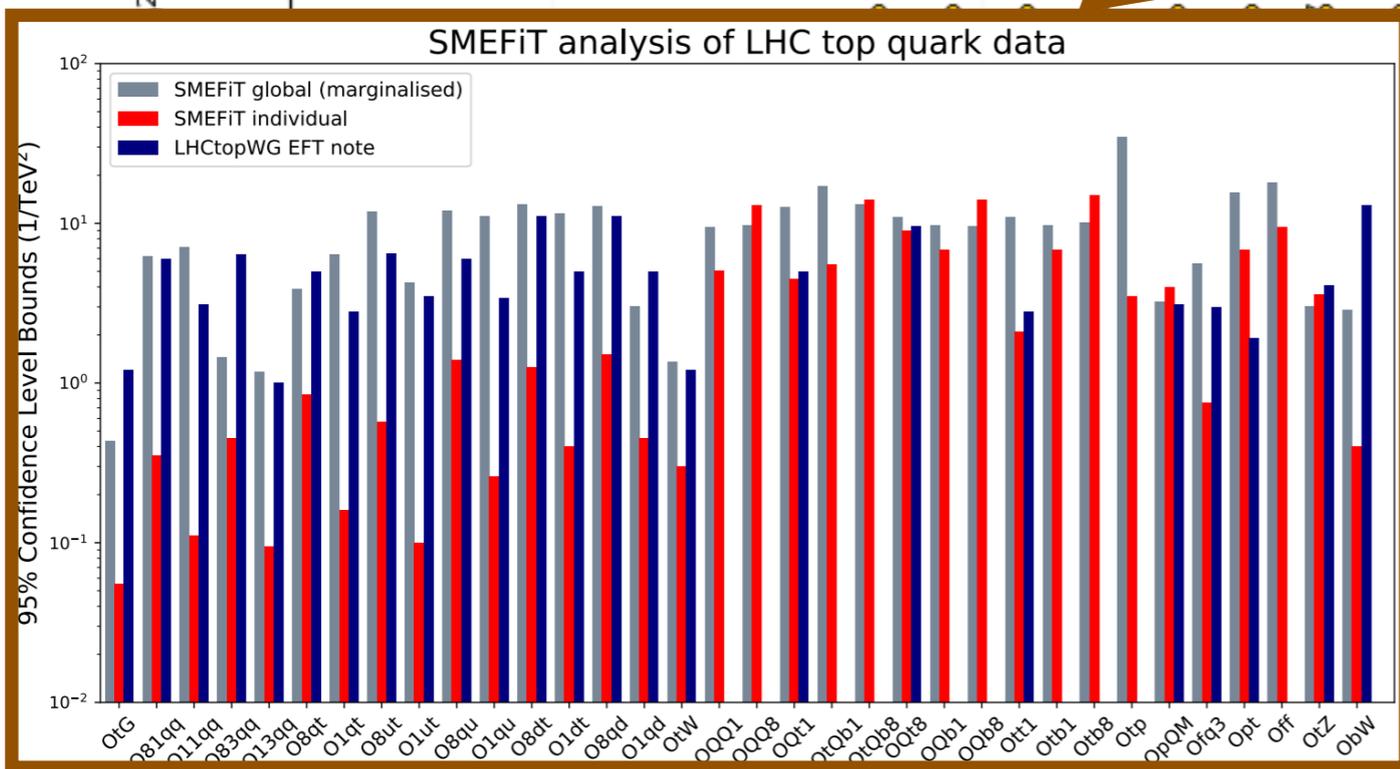
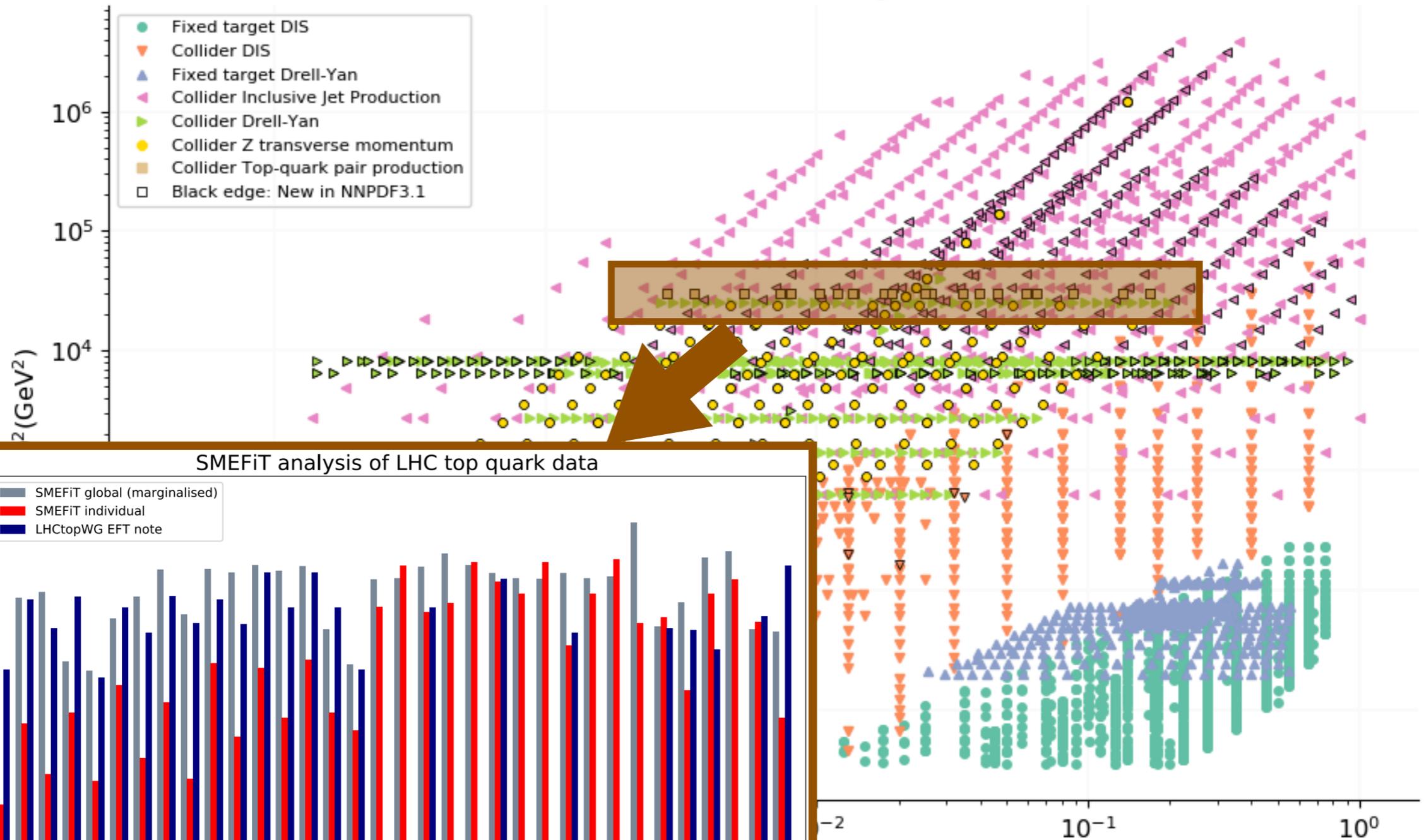
SMEFiT analysis of LHC top quark data



Marg. less constrained than ind.

SMEFT constraints data

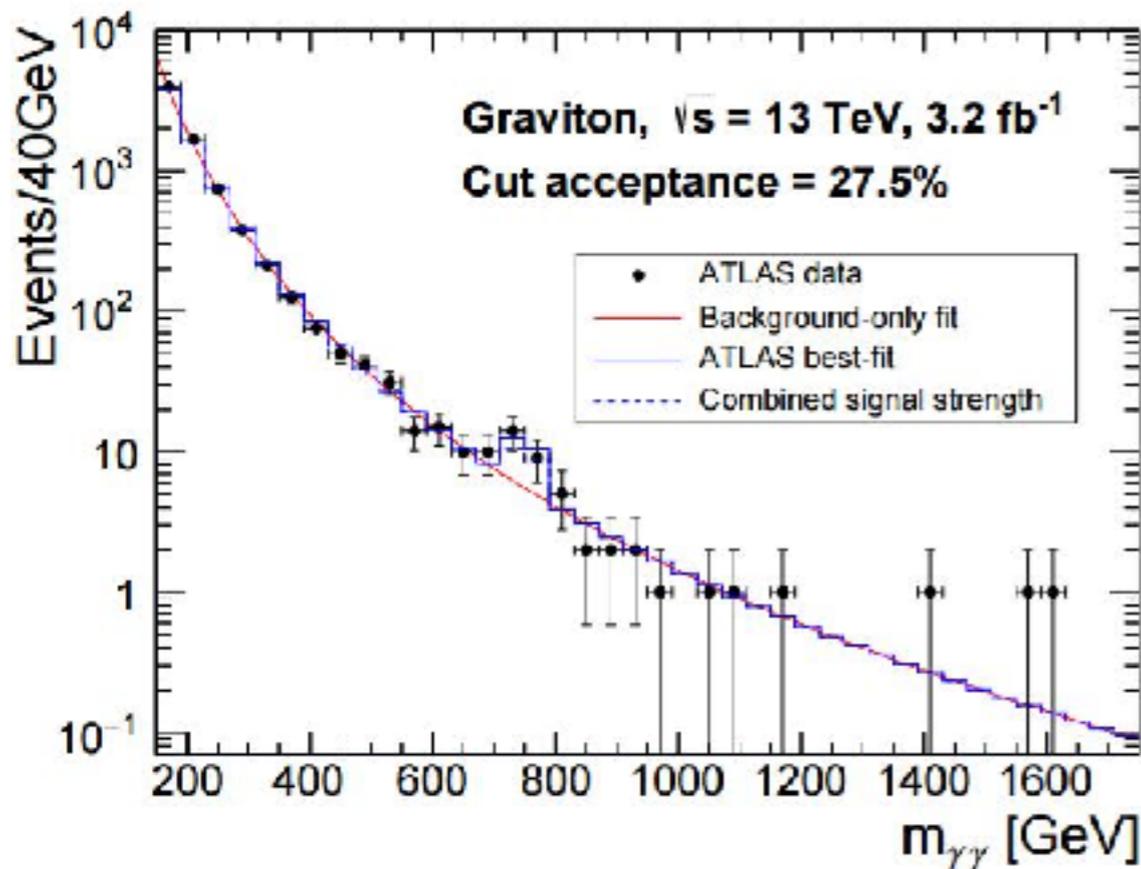
Kinematic coverage



Remove the top data from pdf fit for the top EFT fit

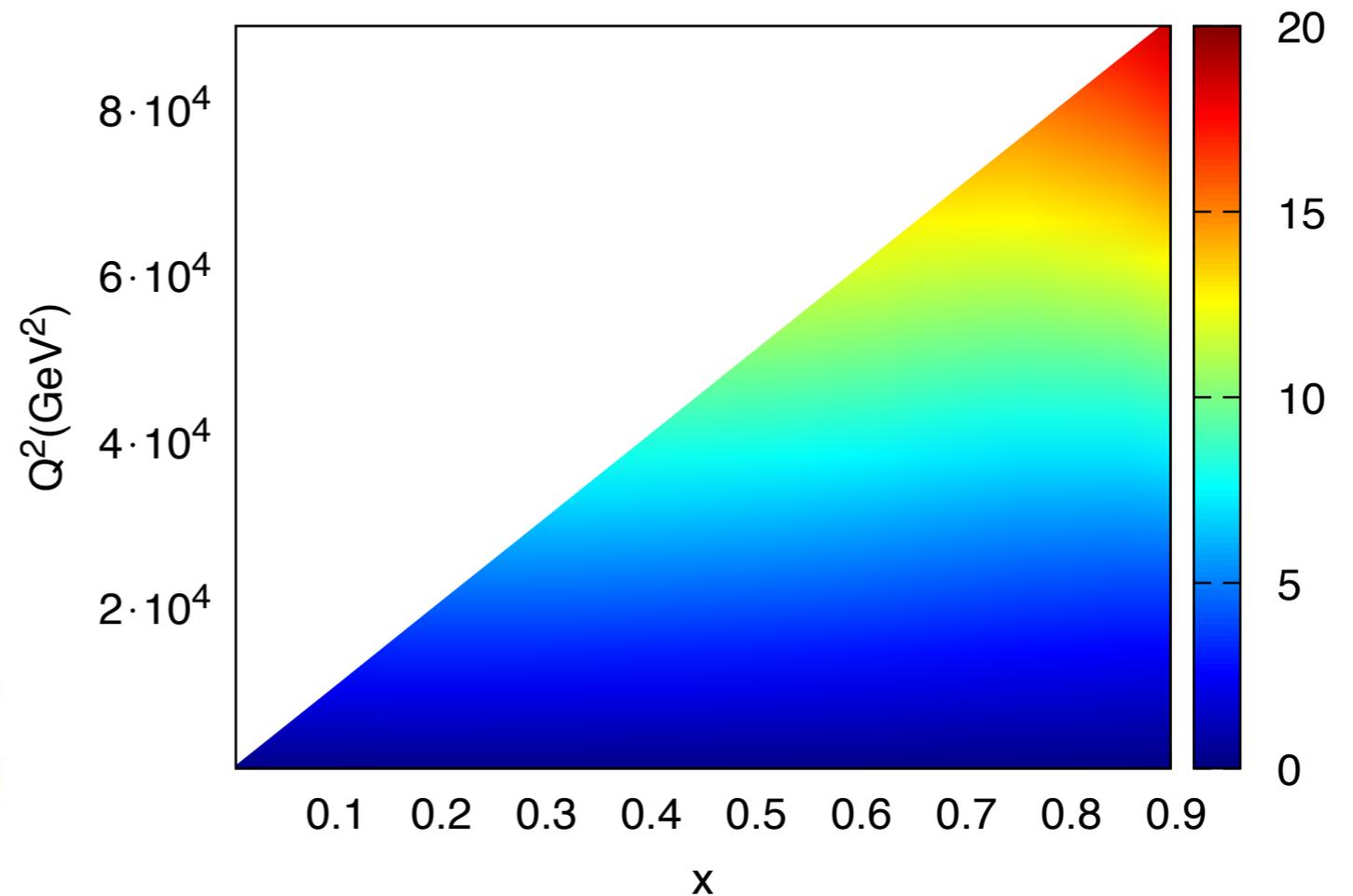
EFT and PDF

$$\mathcal{O}_{lq} = (\bar{l}_R \gamma^\mu l_R) (\bar{q}_R \gamma_\mu q_R), \quad q = u, d, s, c,$$



Not single process
Not localised

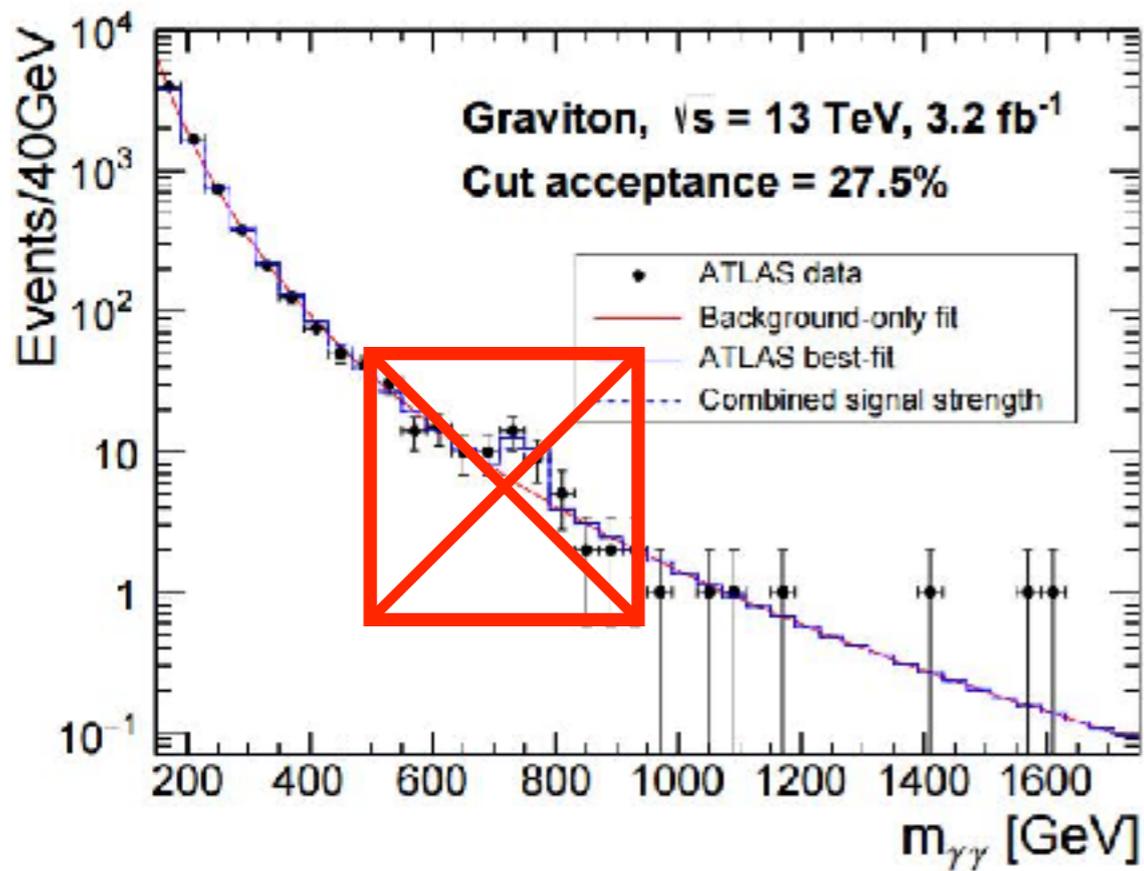
BP1: $a_u = a_c = +0.28$, $a_d = a_s = -0.10$



$$\Delta F_2^{\text{smeft}} \supset \frac{x}{12e^4} \left(4a_u e^2 \frac{Q^2}{\Lambda^2} (1 + 4K_Z s_W^4) + 3a_u^2 \frac{Q^4}{\Lambda^4} \right) \times (u(x, Q^2) + \bar{u}(x, Q^2))$$

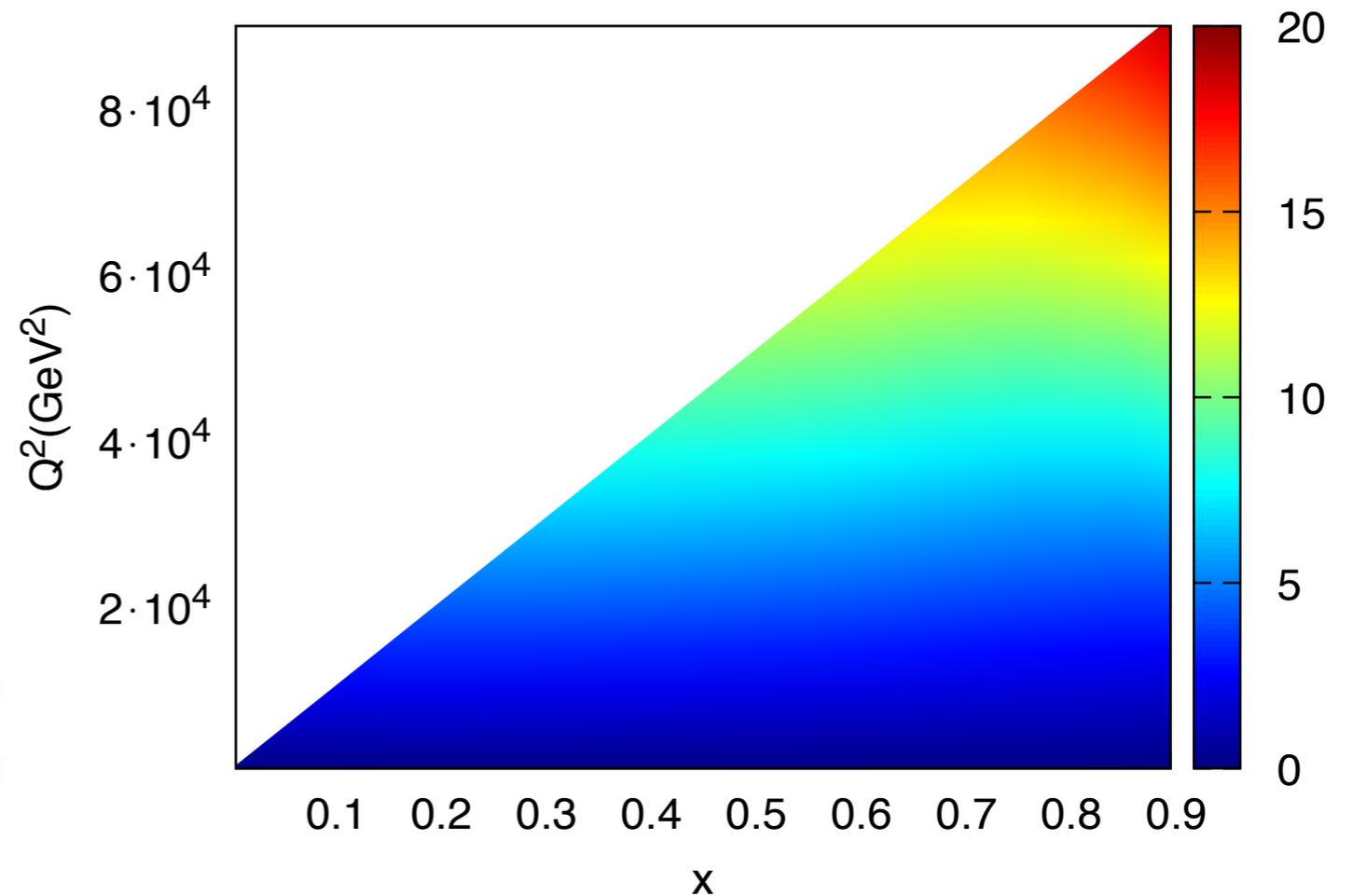
EFT and PDF

$$\mathcal{O}_{lq} = (\bar{l}_R \gamma^\mu l_R) (\bar{q}_R \gamma_\mu q_R), \quad q = u, d, s, c,$$



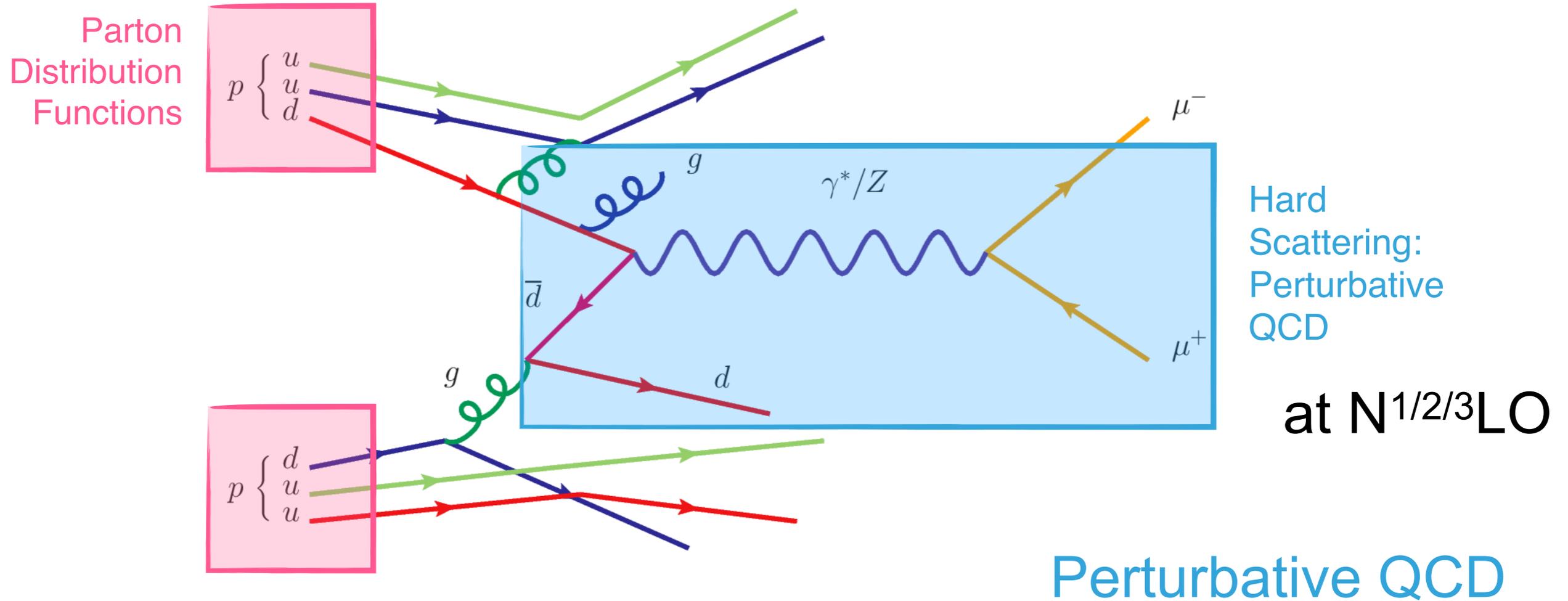
Not single process
Not localised

BP1: $a_u = a_c = +0.28$, $a_d = a_s = -0.10$



$$\Delta F_2^{\text{smeft}} \supset \frac{x}{12e^4} \left(4a_u e^2 \frac{Q^2}{\Lambda^2} (1 + 4K_Z s_W^4) + 3a_u^2 \frac{Q^4}{\Lambda^4} \right) \times (u(x, Q^2) + \bar{u}(x, Q^2))$$

Precise predictions



$$d\sigma^{pp \rightarrow ab} \underset{\ni \text{LHC}}{=} \sum_{i,j} \overset{\text{SMEFT}}{f_i} \otimes \overset{\text{SMEFT}}{f_j} \otimes \overset{\text{SMEFT}}{d\hat{\sigma}^{ij \rightarrow ab}} + \dots$$

$f_i(x, \mu)$

SMEFT ← **data**

PDF are process universal **but model dependent**

EFT and PDF

Procedure

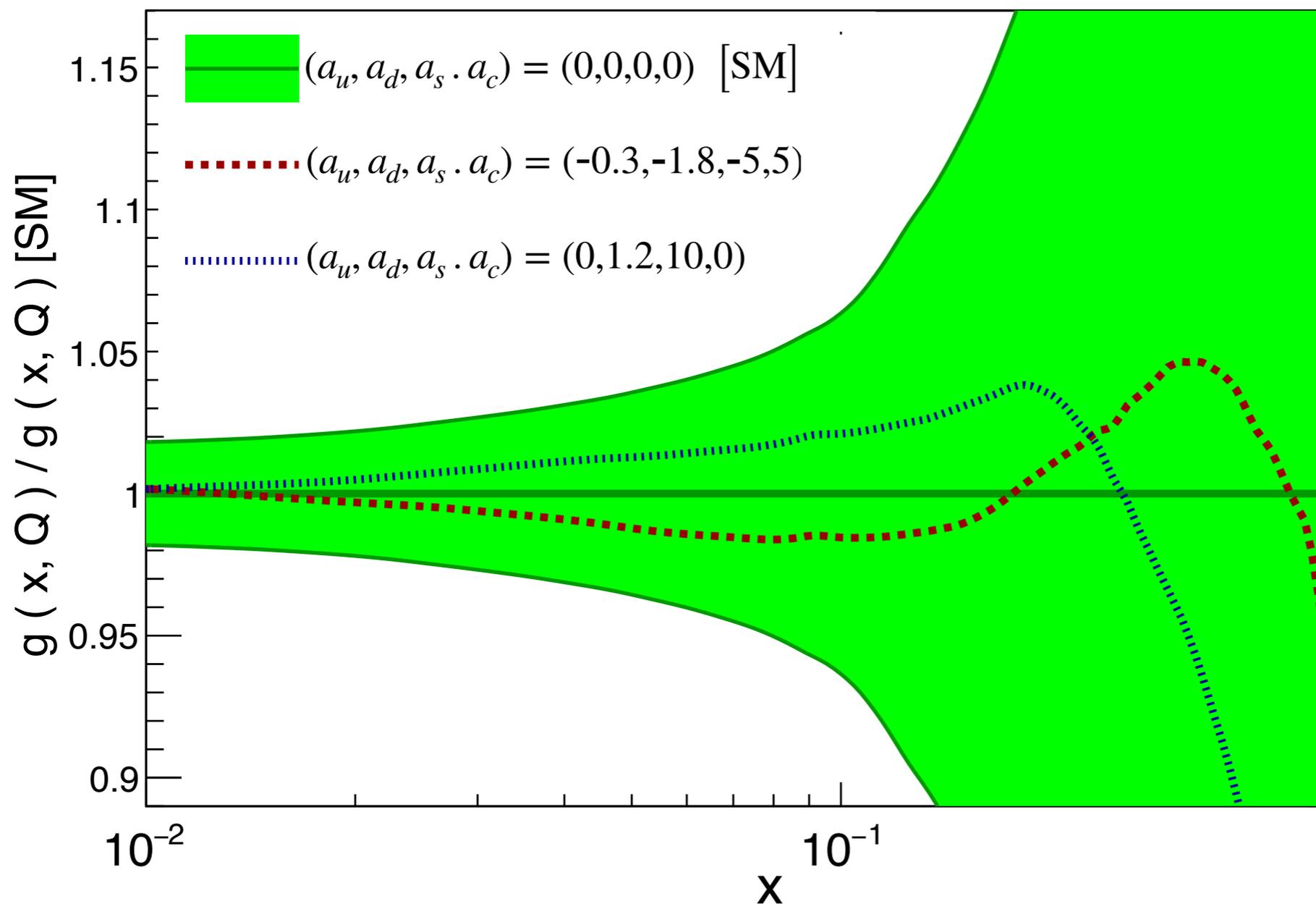
- A few operators $\mathcal{O}_{lq} = (\bar{l}_R \gamma^\mu l_R) (\bar{q}_R \gamma_\mu q_R)$, $q = u, d, s, c$,

$$\sigma^{LEP} = \sigma^{SM} + (a_u + a_c)\sigma^u + (a_d + a_s)\sigma^d$$

- DIS data
- PDF for each BP
- χ^2 for each BP
- Combine with 'PDF independent' constraints (LEP diet + Parity)

EFT and PDF

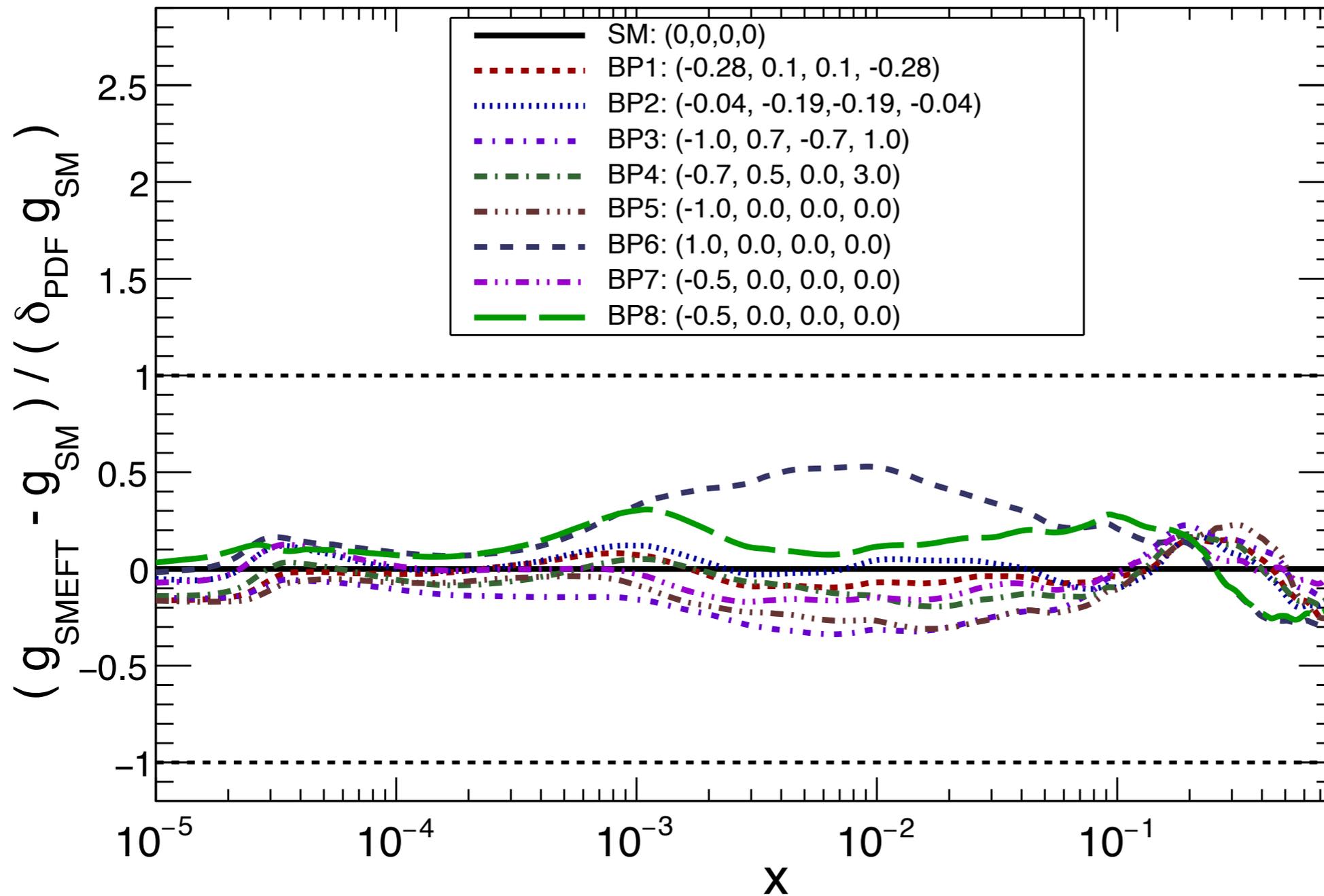
NNPDF3.1 DIS-only, $Q = 10$ GeV



Deviation
within uncer.
but large
uncertainty
(DIS only)

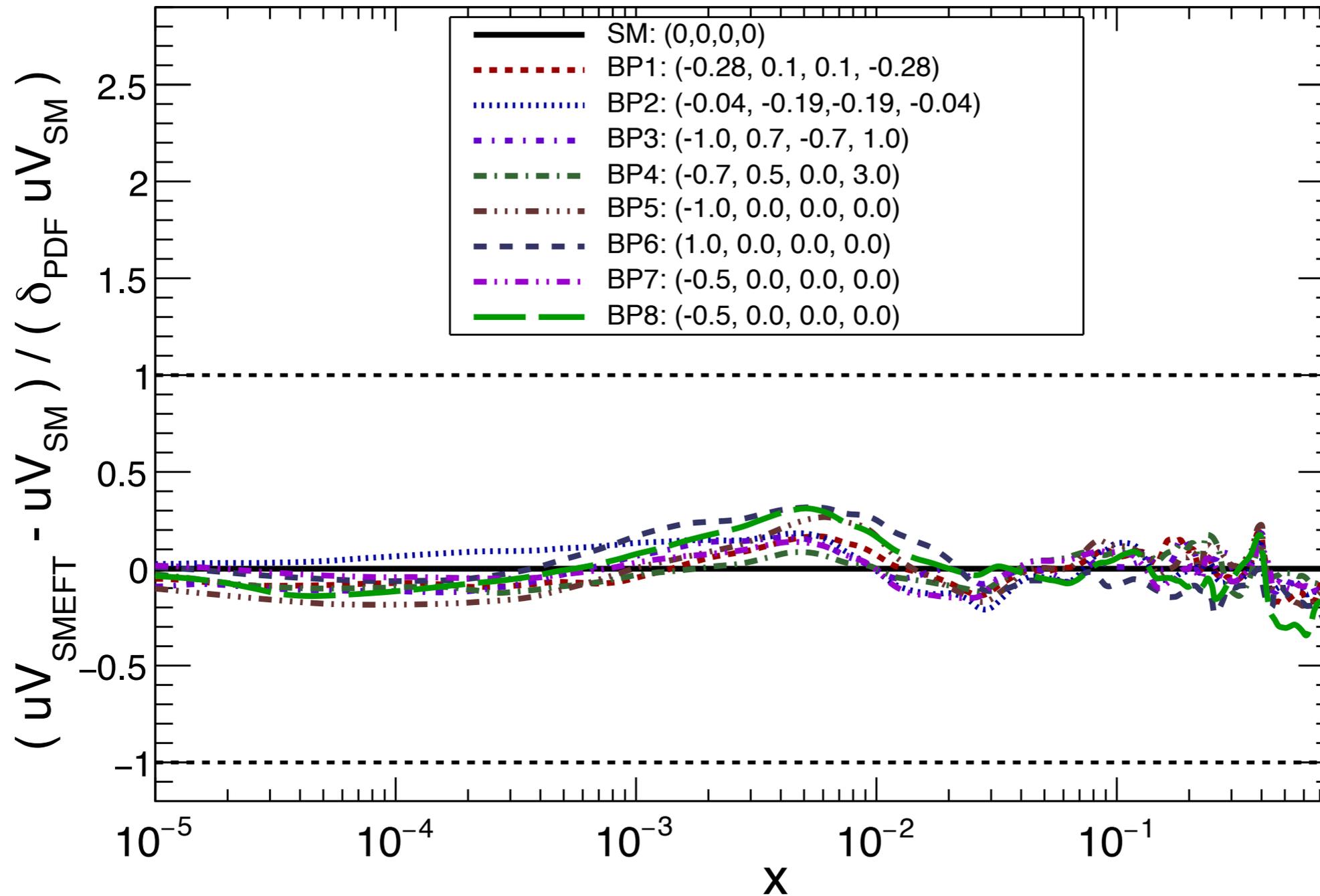
Effect on gluon PDF

NNPDF3.1 NLO DIS-only, $Q = 10$ GeV

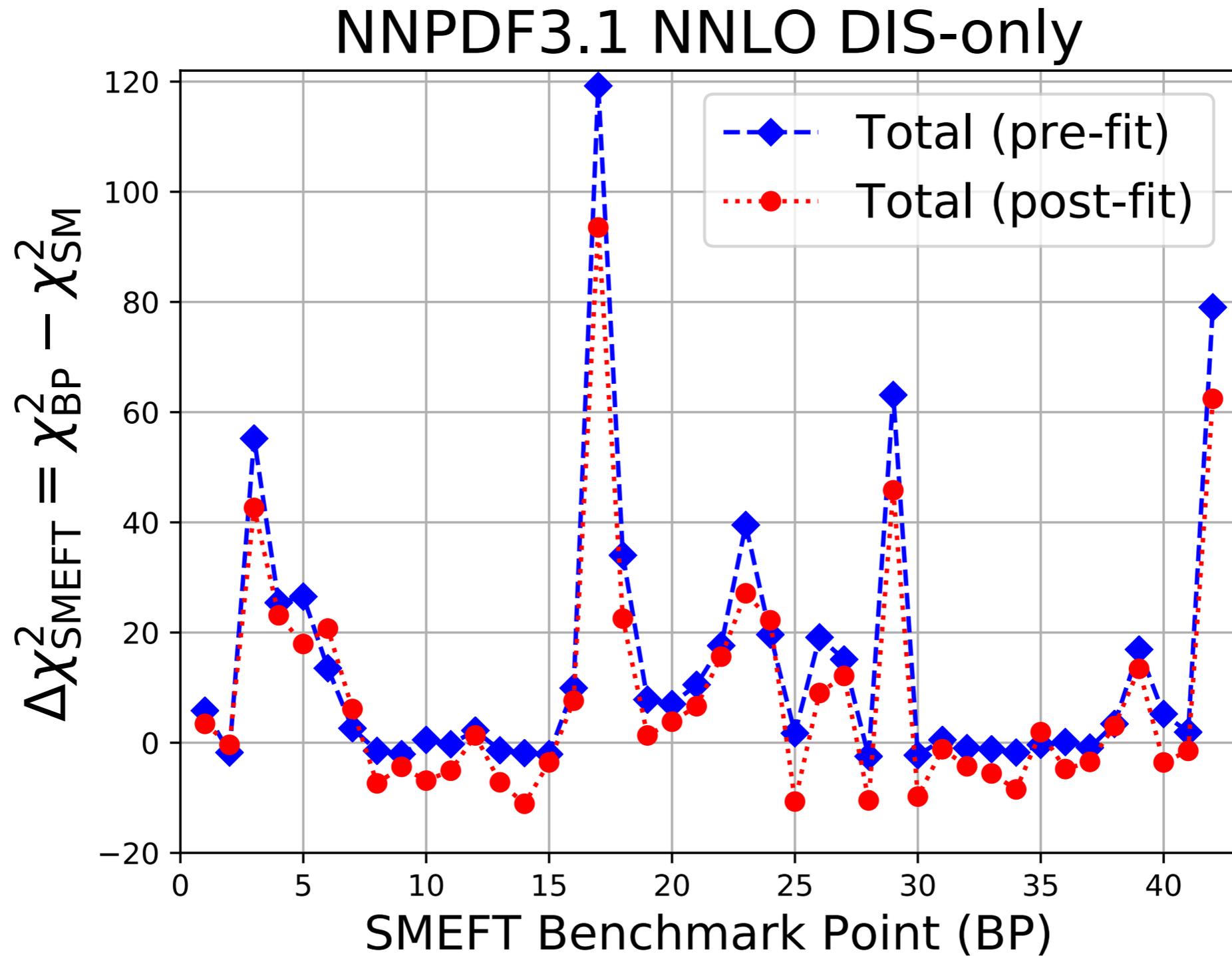


Effect on quarks PDF

NNPDF3.1 NLO DIS-only, Q = 10 GeV

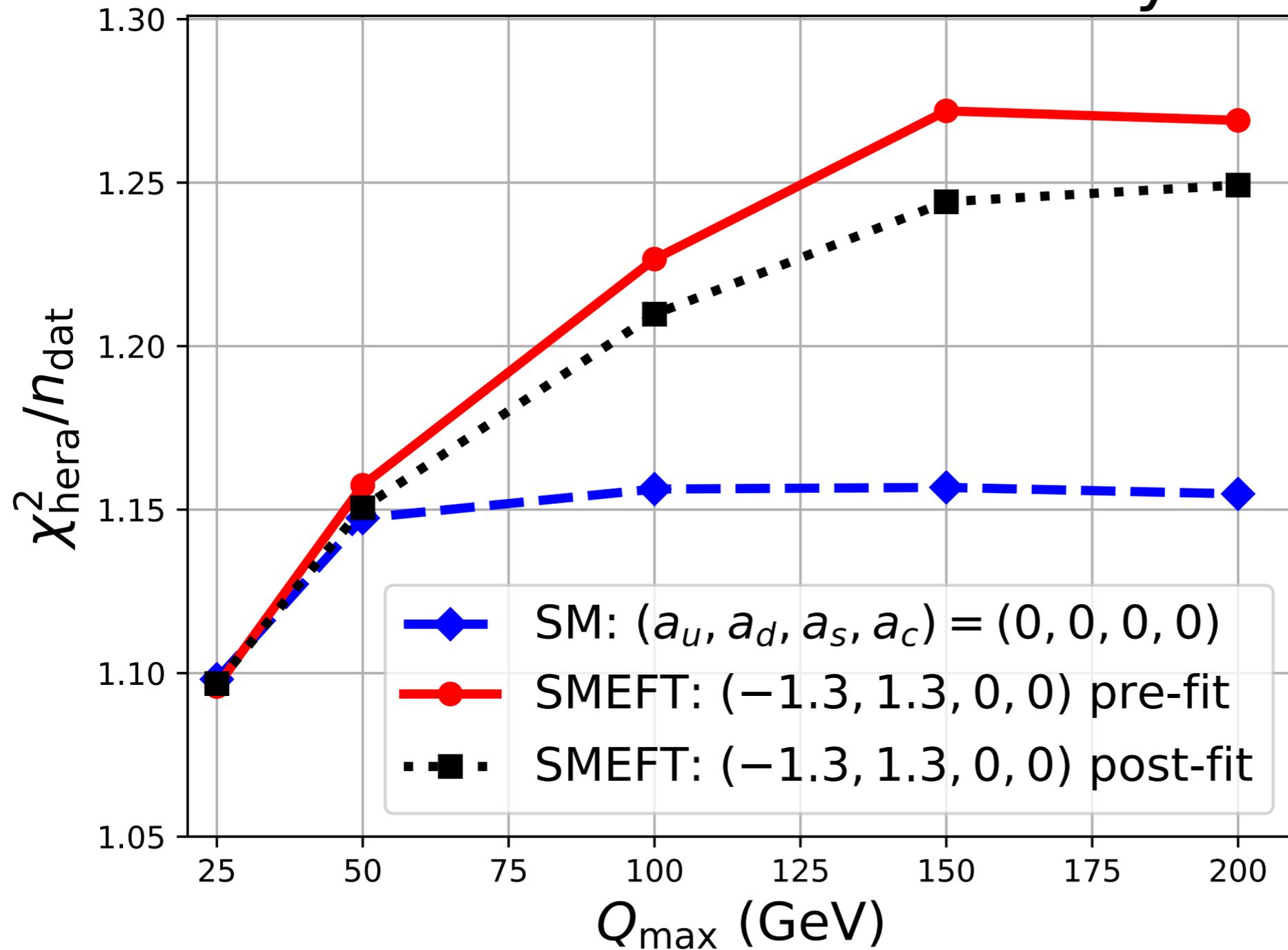


PDF fit for each SMEFT BP



SM vs SMEFT

NNPDF3.1 NNLO DIS-only

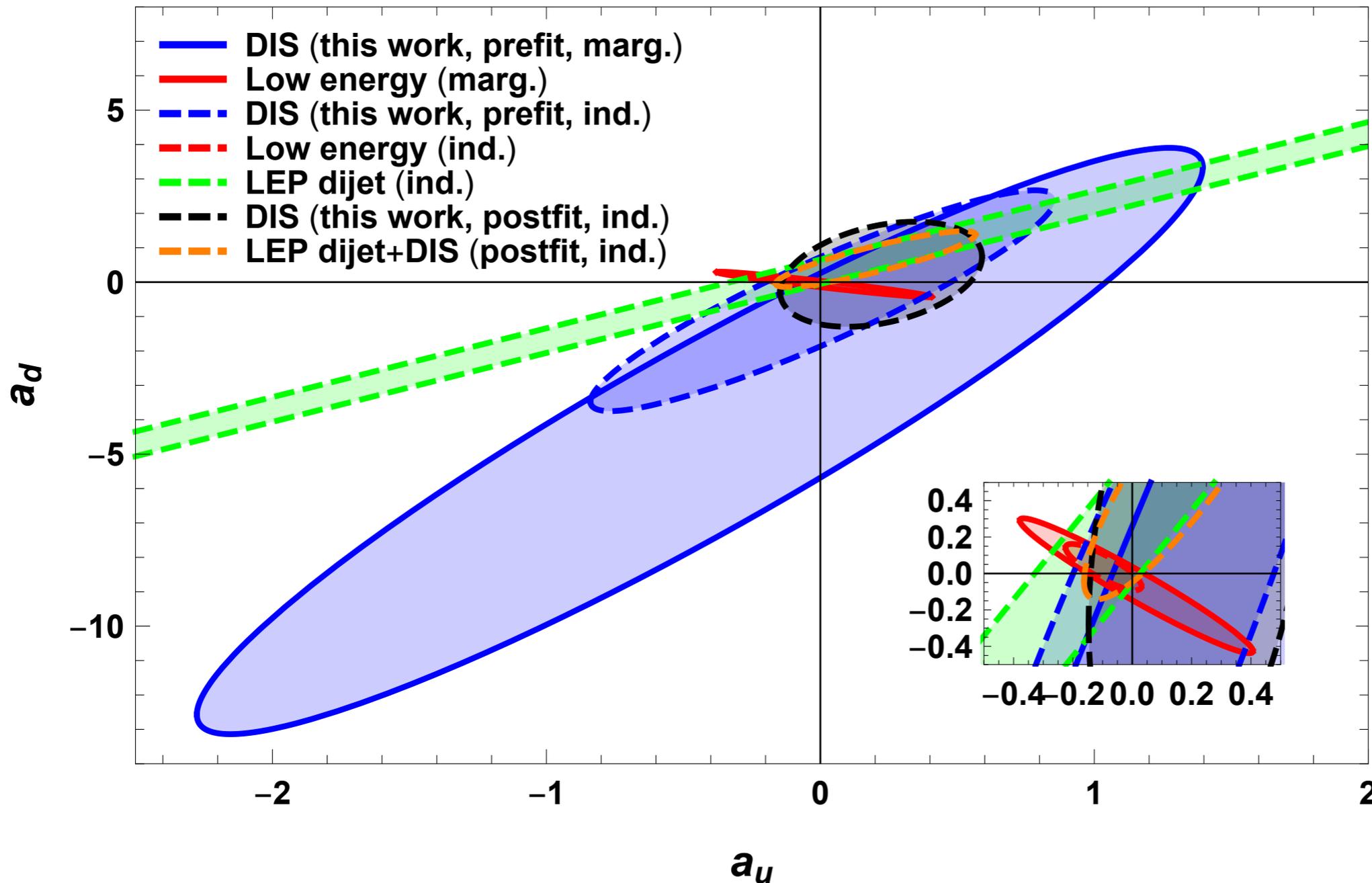


Operator
dependent

$$\sigma_{4F} \sim \sigma_{SM} \times \frac{s}{\Lambda^2}$$

EFT and PDF

90%CL allowed region



Parity
 $p=2u+d$
 $n=2d+u$
 or
 PDF at
 $Q^2 \ll 1 \text{ GeV}^2$

LEP correlations only between x-section at different energies

Outlook

Looking for new physics



Summary

- EFT provide guidance (which observable)
- EFT is multi-channel/observable
- Global fit with a large number of parameters/multiple data
- Interplay between PDF and EFT
 - add more operators
 - add more data
 - full fit with both PDF and SMEFT

Summary



Thank you