# **Trilinear Couplings** — global interpretation —

Ultimate Precision at Hadron Colliders Institut Pascal, December 3, 2019







# The importance of being cubic...

## The Higgs self-coupling plays important roles

- **I)** linked to **naturalness/hierarchy** problem
- 2) controls the **stability** of the EW vacuum (... like many other BSM parameters)
- 3) dictates the dynamics of EW phase transition and potentially conditions the generation
  - of (1) matter-antimatter imbalance via **EW baryogenesis** & (2) a stochastic **GW** background

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## **Does it need to be measured with high accuracy?**

Only a few new physics scenarios (but they exist) that will be revealed in the measurements of h<sup>3</sup> But this measurement is the only way to understand the dynamics of EWSB (Cooper pair or elementary scalar?)

What sort of precision should we aim for? M. McCullough DESY'18 95% confidence it exists: Around 50% accuracy 5σ discovery: Around 20% accuracy. Quantum structure: Around 5% accuracy.

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## Window to early universe: GW - Colliders



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Huang, Long, Wang '16

# Which Higgs couplings?

Within the SM, all the Higgs couplings are uniquely fixed by known quantities (G<sub>F</sub>, m<sub>V</sub>, m<sub>Z</sub>, m<sub>quark</sub>, m<sub>lepton</sub>)

This is a curse (nothing more to learn) and a blessing (can asses the inconsistency of the SM)



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M. Mangano

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### Two approaches to go BSM

Study specific models





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# M. Mangano

### Try to introduce continuous deformations of the SM

# Which Higgs couplings?

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# M. Mangano

### Try to introduce continuous deformations of the SM

At LHC: EW/VV precision strong enough not to interfere with Higgs measurements (at least if Higgs part of EW doublet)

Not necessarily true at future colliders Need a more global strategy

# **Higgs/BSM Primaries**

How many SM deformations are not affecting precisely measured observables outside Higgs physics?

As many as parameters in the SM: 8 for one family (assuming CP-conservation)  $|H|^2 G^A_{\mu\nu} G^{A\mu\nu}$  $\mathbf{g}_{\mathbf{s}}$ **GGh** coupling  $|H|^2 B_{\mu\nu} B^{\mu\nu}$ hyy coupling g  $\mathbf{g}'$  $|H|^2 W^a_{\mu\nu} W^{\mu\nu\,a}$ hZγ coupling  $|H|^2 |D_\mu H|^2$  $\mathbf{m}_{\mathbf{W}}$ hVV\* (custodial invariant) h<sup>3</sup> coupling  $H|^6$  $\mathbf{m}_{\mathbf{h}}$  $|H|^2 \overline{f}_L H f_R + h.c.$   $\longrightarrow$  htt, hbb, h $\tau\tau$  $\mathbf{m_{f}}$  $(f=t,b,\tau)$ 

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Pomarol, Riva'13 Elias-Miro et al '13 Gupta, Pomarol, Riva '14

# **Higgs/BSM Primaries**

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# Synergy Higgs and diboson

In EFT<sub>(dim-6)</sub>

8 deformations affecting Higgs physics alone

2 deformations affecting Higgs and diboson data

diboson (1%) are a priori more constraining than Higgs (10%)

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- Is there any value in doing a global fit?

# Synergy Higgs and diboson



(TGC+Higgs)>(TGC)∪(Higgs)

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# Synergy Higgs and diboson



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Impact of HL-LHC WW data? we assumed 1% syst. and also studied the impact of this assumption

## Importance of WW run

## (TGC+Higgs)>(TGC)U(Higgs)



Durieux, Grojean, Gu, Wang '17

## **Beware of TGC dominance assumption**

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### EAA Cimultaneous Fit

J. De Blas, G. Durieux, C. Grojean, J. Gu, A. Paul 1907.04311

Beware of TGC dominance as sure of would need five

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precision

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The distributions used in the combined fit are multi-dimensional distributions of the appendix of the dimensional distributions of the dimensional distribution. Filling a five-dimensional distribution leads to poor statistics for the single bins and does not appear to be a convenient chorde. It was therefore decided to move to three-dimensional distributions, using 0!9

## h<sup>3</sup> Extraction @ LHC

Notoriously difficult in particular because of strong interference



$$A_{\Box} = \frac{\alpha_s}{4\pi} y_t^2, \qquad A_{\Delta} = \lambda_3 \frac{\alpha_s}{4\pi} y_t^2 \frac{m_h^2}{\hat{s}} \left( \log \frac{m_t^2}{\hat{s}} + \frac{\sigma(pp \to hh)}{\sigma(pp \to h)} \sim 10^{-3} \right)$$

Note 1: The two diagrams have different energy behaviour: look at differential distributions

Note 2: also: 2% uncertainty on tth  $\rightarrow$  5% uncertainty on h<sup>3</sup>. Good control of parametric uncertainties is needed

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$$(-i\pi)^2$$

## h<sup>3</sup> from HH



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## h<sup>3</sup> from hh@LHC now



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### See E. Petit talk yesterday

# h³ from hh@HL/HE-LHC



 $\bullet$  HL-LHC can test the Higgs trilinear with O(50%) precision  $0.57 \le \kappa_{\lambda} \le 1.5$  at 68% C.L.

 $\bullet$  HE-LHC could test the Higgs trilinear with O(15-30%) precision (projections vary significantly between different analyses)

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### HL/HE-LHC Higgs WG report

## h<sup>3</sup> from h@NLO@HL-LHC

M. McCullough '14

At 240 GeV:  

$$\sigma_{Zh} = \begin{vmatrix} \mathbf{e} & \mathbf{z} \\ \mathbf{e} & \mathbf{h} \end{vmatrix}^{2} \mathcal{L} = \mathcal{L}_{SM} \int \mathcal{L} = \mathcal{L}_{SM} \mathcal{Z} - \frac{1}{3!} \delta_{h}^{*} A_{SM} h^{3} \\ + 2 \operatorname{Re} \int \mathcal{L} = \mathcal{L}_{SM} \mathcal{L} = \mathcal{L}_{SM} \int \mathcal{L} = \mathcal{L} = \mathcal{L}_{SM} \int \mathcal{L} = \mathcal{L} = \mathcal{L} + \mathcal{L} = \mathcal{L} + \mathcal{$$

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 $\cdots -h$ 







$$\kappa_{\lambda} \in [-0.7, 4.2]$$

cwith massless fermion lines, which is equivalent to including an ly transversal gauge-boson



Worse than direct determination via double Higgs production but different systematics and "easier" analysis





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Worse than direct determination via double Higgs production but different systematics and "easier" analysis

## Make h<sup>3</sup> great again: Higgs portal models

 $\mathcal{L} \supset \theta g_* m_* H^{\dagger} H \varphi - \frac{m_*^4}{g_*^2} V(g_* \varphi/m_*)$ 



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$$\begin{split} \mathbf{Make h^{3} great again: Higgs power of the formula of the fo$$

Global determination 14

## rtal models



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Global determination 14





Global determination 14







5 main production modes: ggF,VBF, WH, ZH, ttH 5 main decay modes: ZZ, WW, γγ, ττ, bb



Global determination 15

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# h<sup>3</sup> @NLO vs h @ LO in global fit

### Good sensitivity (O(5-10-20)%) on 16 channels @ HL-LHC

Process		Combination	Theory	Experimental
$H \to \gamma \gamma$	ggF	0.07	0.05	0.05
	VBF	0.22	0.16	0.15
	$t\overline{t}H$	0.17	0.12	0.12
	WH	0.19	0.08	0.17
	ZH	0.28	0.07	0.27
$H \rightarrow ZZ$	ggF	0.06	0.05	0.04
	VBF	0.17	0.10	0.14
	$t\overline{t}H$	0.20	0.12	0.16
	WH	0.16	0.06	0.15
	ZH	0.21	0.08	0.20
$H \rightarrow WW$	ggF	0.07	0.05	0.05
	VBF	0.15	0.12	0.09
$H \to Z\gamma$	incl.	0.30	0.13	0.27
$H  o b \bar{b}$	WH	0.37	0.09	0.36
	ZH	0.14	0.05	0.13
$H \to \tau^+ \tau^-$	VBF	0.19	0.12	0.15

Estimated relative uncertainties on the determination of single-Higgs production channels at the HL-LHC(14 TeV center of mass energy, 3/ab integrated luminosity and pile-up 140 events/bunch-crossing). ATL-PHYS-PUB-2016-008 ATL-PHYS-PUB-2016-018

ATL-PHYS-PUB-2014-016

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a priori up to **25** measurements

but for an on-shell particles, at most **10** physical quantities since only products  $\sigma xBR$  are measured  $\Rightarrow$  only 9 independent constraints

$$\mu_i^f = \mu_i \times \mu^f = \frac{\sigma_i}{(\sigma_i)_{\rm SM}} \times \frac{{\rm BR}[f]}{({\rm BR}[f])_{\rm SM}}$$

 $\mu_i \to \mu_i + \delta$ 

$$\mu_i^f \simeq 1 + \delta \mu_i + \delta_i$$

linearized BSM perturbations

$$\mu^f 
ightarrow \mu^f {-} \delta_{+}$$

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- $u^{f}$

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cannot determine univocally 10 EFT parameters!

## one flat direction is expected!

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- $\mu^{f}$



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# h<sup>3</sup> @NLO vs h @ LO in global fit



HL-LHC I $\sigma$  bound on related parameter

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# h<sup>3</sup> @NLO vs h @ LO in global fit



HL-LHC I $\sigma$  bound on related parameter

The particular structure of this flat direction tells that adding new data on diboson or  $h \rightarrow Z\gamma$  won't help much

cannot determine univocally 10 EFT parameters!

## one flat direction is expected!

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# Does h<sup>3</sup> modify the fit to other couplings?



Figure 3. Constraints in the planes  $(\delta y_t, \hat{c}_{gg})$  (left panel) and  $(\delta y_b, \hat{c}_{\gamma\gamma})$  (right panel) obtained from a global fit on the single-Higgs processes. The darker regions are obtained by fixing the Higgs trilinear to the SM value  $\kappa_{\lambda} = 1$ , while the lighter ones are obtained through profiling by restricting  $\delta \kappa_{\lambda}$  in the ranges  $|\delta \kappa_{\lambda}| \leq 10$  and  $|\delta \kappa_{\lambda}| \leq 20$  respectively. The regions correspond to 68% confidence level (defined in the Gaussian limit corresponding to  $\Delta \chi^2 = 2.3$ ).

In models with parametrically large h<sup>3</sup>, fit with  $\kappa_{\lambda}$  @ NLO can differ from LO fit by a factor 2. But this concerns only particular BSM models, in most models  $\kappa_{\lambda} \sim \kappa_i$  and NLO effects are negligible. Furthermore, HL-LHC will already measure h<sup>3</sup> at 50%, so even in the extreme case, the NLO effects are limited to 20-30%

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DiVita et al '17

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1 main production mode (ZH) & 1 subdominant production (VBF) + access to full angular distributions (4) and/or beam polarizations (2) 7 (+2) accessible decay modes: ZZ, WW,  $\gamma\gamma$ ,  $Z\gamma$ ,  $\tau\tau$ , bb, gg, (cc,  $\mu\mu$ )

## **No flat direction is expected!**



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M. Peskin in HH white paper '19

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## Future prospects for h<sup>3</sup> measurements



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### ECFA Higgs @FC WG '19

Inst. Pascal, Dec. 3, 2019