

# Göttingen report

SHERPA Annual Meeting  
Milan, 7 January 2020

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Enrico Bothmann

# The Göttingen group these days ...



[@Email](#)

Prof. Dr. Steffen Schumann



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Dr. Vincent Michel Theeuwes



[@Ema](#)

Dr. Enrico Bothmann

## PhD students:



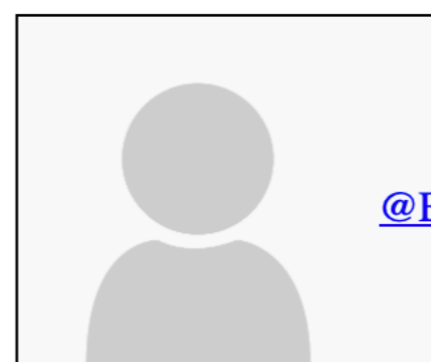
Stephan Bräuer



Daniel Reichelt



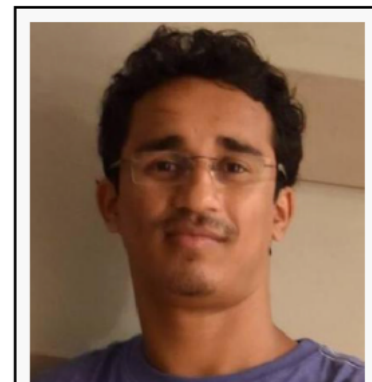
Timo Janssen



[@E](#)

Simon Luca Villani

## MCnet short-term student from ALICE



Suman Deb

# Topics 2019 and ongoing

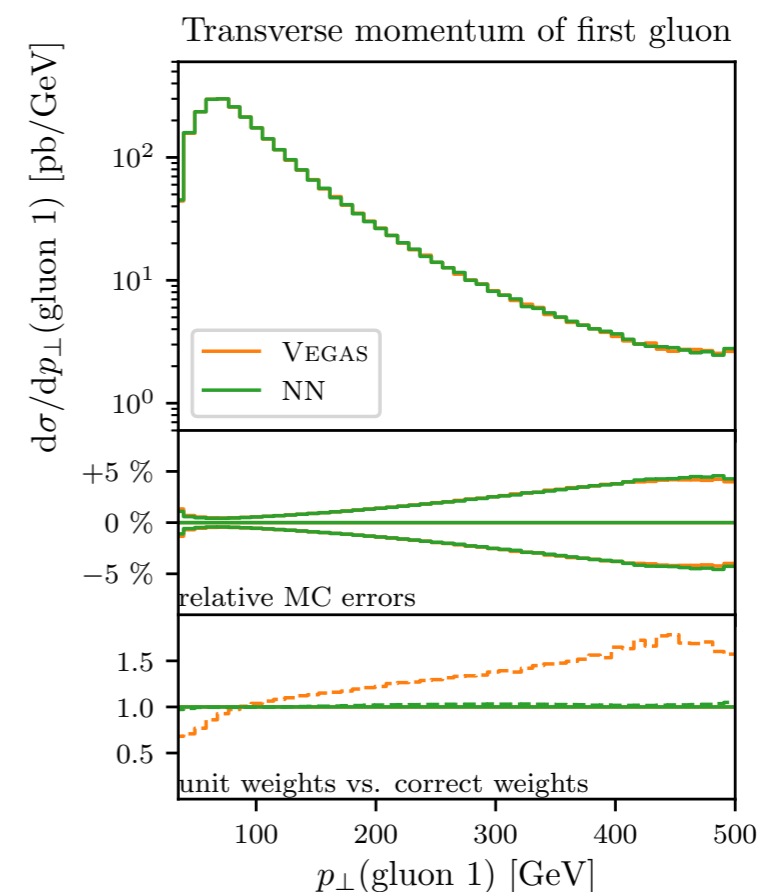
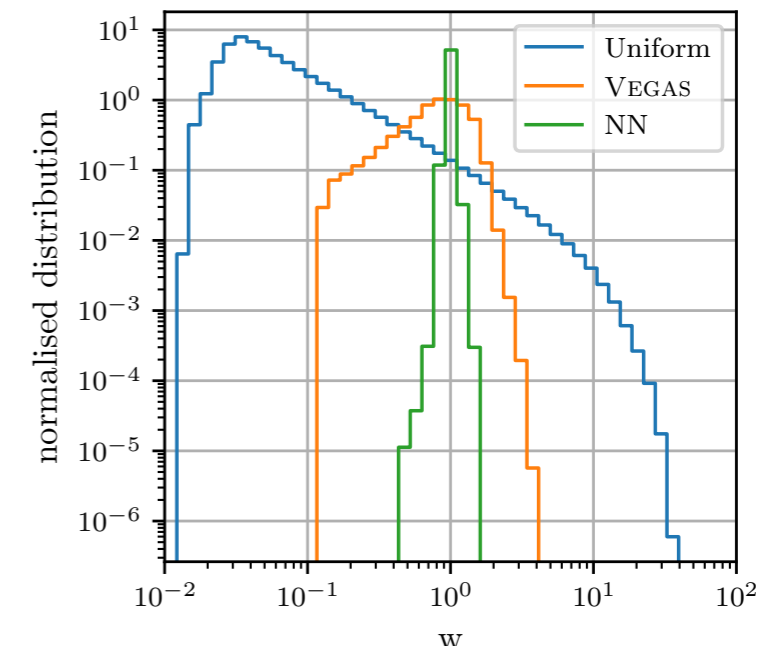
- explore phase space with Neural Importance Sampling  
Steffen, Enrico, → **Timo**
- resummation & automated CAESAR plug-in  
Steffen, → **Daniel**, Vincent
  - ee soft-drop Thrust @ NLO+NLL → apply to  $\alpha_s$  fit
  - ee Durham jet resolutions @ NLO+NLL' →  $N_{\text{jets}} \leq 6$
- loop-induced processes  
Steffen, Enrico, → **Simon**
  - use EXTAMP ME interface to calculate LI  $gg \rightarrow VV$  @ NLO+PS
- electro-weak corrections  
Steffen, Enrico, Stephan
  - calculation of QCD+EW NLO 3-jet production → apply to  $R_{32}$
  - $WW(j)$  @ MEPS@NLO+EWvirt
  - ongoing development of EW Sudakov corrections

# Neural importance sampling

[EB, Timo Janßen, Max Knobbe, Tobias Schmale, Steffen Schumann, TBP]

- train a NN to propose points
  - replace VEGAS as channel optimiser
- NN architecture guarantees ...
  - full phase-space coverage
  - cheap weight calculation (Jacobians  $\mathcal{O}(D)$ )
- inspired by methods developed for light transport simulation (3D rendering)  
[Müller et al., Disney Research, 1808.03856]
- proof-of-principle study for:
  - top decays & leptonic  $t\bar{t}$  production
  - $gg \rightarrow 3g/4g$
- coordinated with complementary study focusing on scaling behaviour in  $pp \rightarrow W + n \text{ jets}$   
[Stefan Höche et al., TBP]

→ Timo

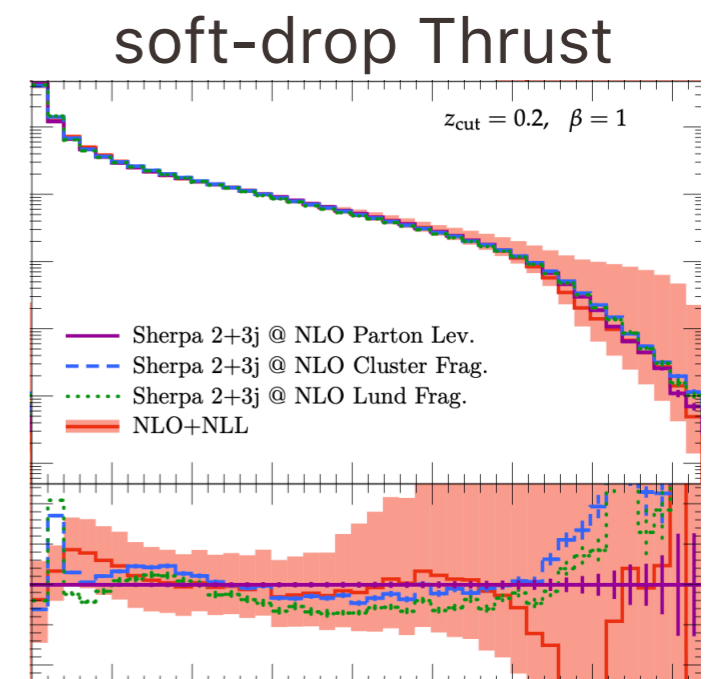
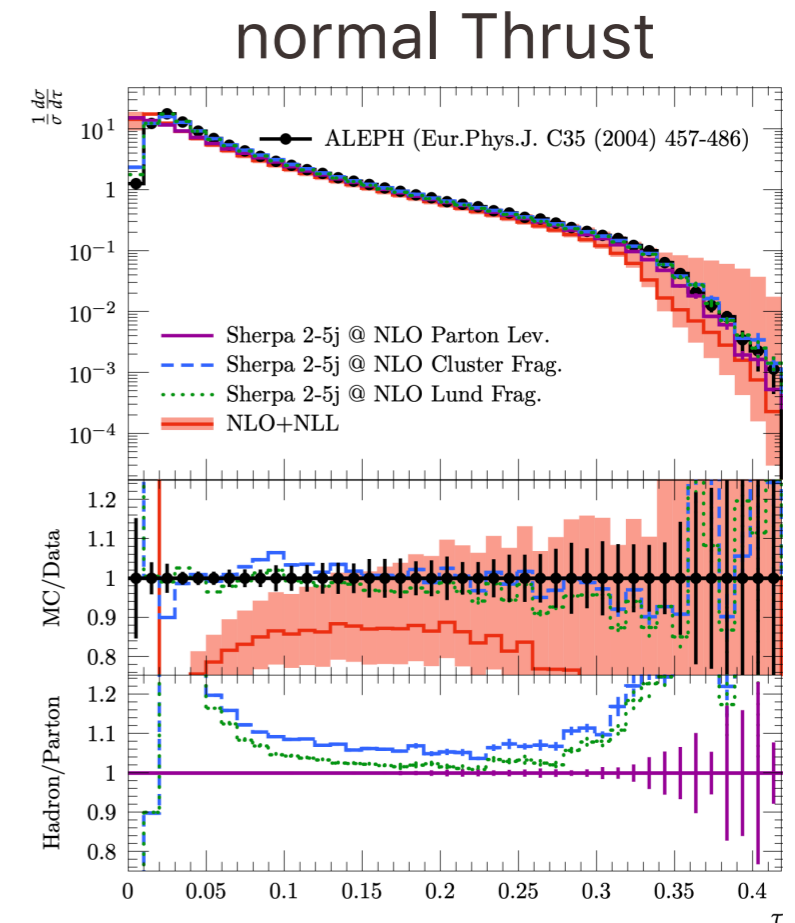


# Resummation I: soft-drop Thrust for $\alpha_s$ fits

[Simone Marzani, Daniel Reichelt, Steffen Schumann, Gregory Soyez, Vincent Theeuwes, 1906.10504]

- ▶ use soft-drop to reduce hadronisation effects in Thrust at LEP to improve  $\alpha_s$  fit
- ▶ MEPS@NLO SHERPA+OPENLOOPS simulated data (there is no experimental analysis)
- ▶ NLO+NLL prediction  
[Baron, Marzani, Theeuwes, 1803.04719]
- ▶ validated by automated CAESAR-based SHERPA plug-in  
[Gerwick, Höche, Marzani, Schumann, 1411.7325]
- ➔ reduced shift by hadronisation (very broadly speaking  $\sim 20\% \rightarrow \lesssim 10\%$ , flatter shape)
- ➔ possibility of extending fit range to smaller values of  $\tau = 1 - T$ , while retaining perturbativity
- ▶ proof-of-principle study, precision extraction would require NNLO+NNLL (and experimental analysis)
- ▶ ongoing study for hadronic event shapes with soft-drop, where also UE comes into play

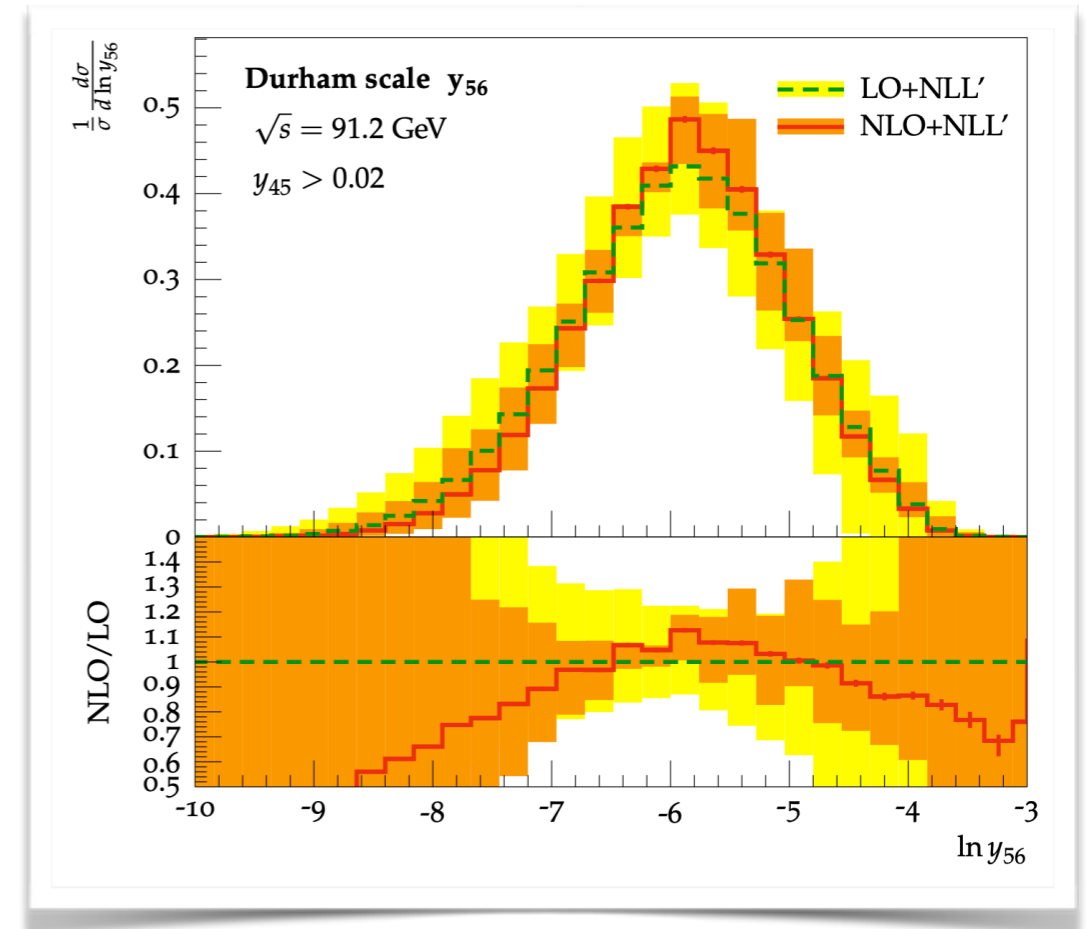
➔ Daniel



# Resummation II: Durham jet resolutions

[Nick Baberuxki, Christian T Preuss, Daniel Reichelt, Steffen Schumann, 1912.09396]

- ▶ Jet resolution scales at NLO+NLL' for ee
- ▶ first time up to  $N_{\text{Jets}} = 6$
- ▶ resummation by CAESAR plug-in (virtualls from OPENLOOPS & RECOLA)
- ▶ multi-emission contribution numerically challenging
- ▶ comparison between LC, improved LC (shower-like) and full colour
  - ➔ improved LC very good approximation
- ▶ sub-leading colour contributions smaller than differences observed when comparing resummation and parton-shower results
  - ➔ other ambiguities must be more important: recoil scheme, phase-space constraints, sub-leading  $\alpha_s$  running ...
- ▶ comparison to data not possible due to  $y_{\text{cut}} = 0.02$  requirement, would require re-evaluation by LEP

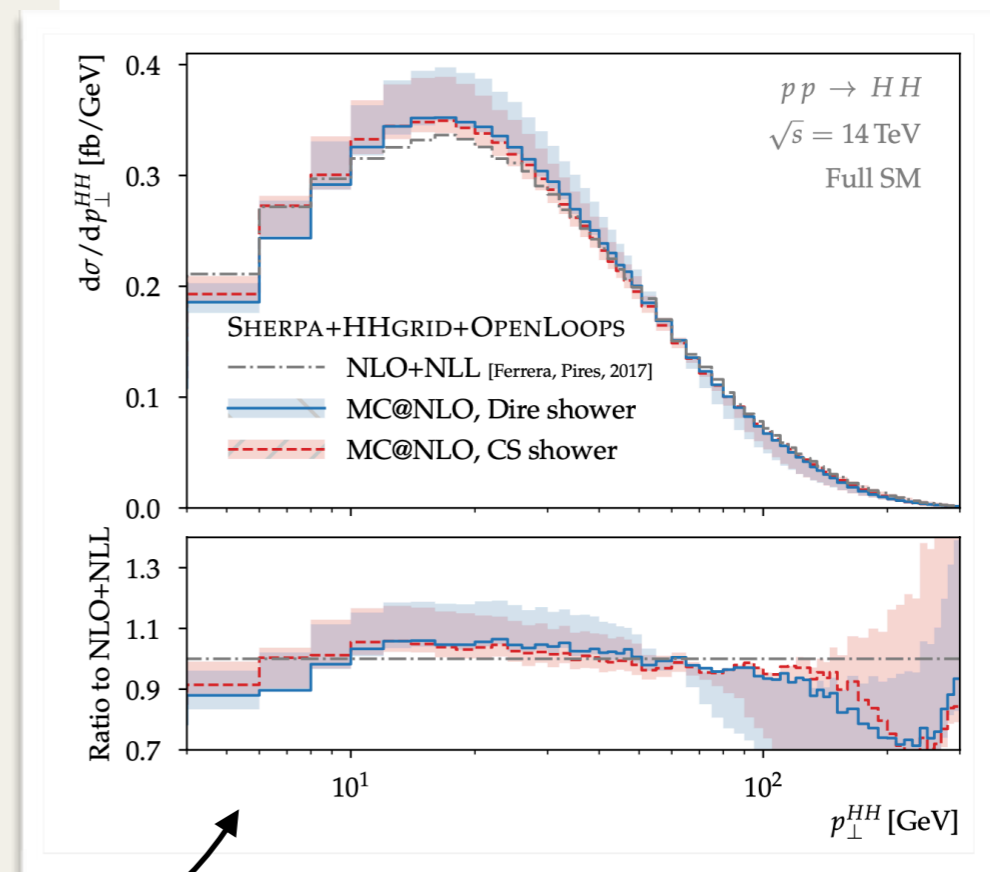


➔ Daniel

# Loop-induced processes

[Jones, Kuttimalai, 1711.03319]

- ▶ in principle, (fully generic) support for LI processes at MC@NLO in SHERPA by EXTAMP module which ...
  - ▶ interfaces external libs for double-virtual ME
  - ▶ implements Catani–Seymour NLO subtraction
  - ▶ performs MC@NLO parton-shower matching
- ▶ proof-of-principle study for  $gg \rightarrow HH$
- ▶ manual steps to add more processes: make sure conventions agree (schemes, prefactors, ...), slow double-virtual potentially requires interpolation, validation
- ▶ first attempt after reproduction of  $gg \rightarrow HH$ :  $gg \rightarrow VV$  with double virtuals from VVAMP code [Manteuffel, Tancredi, 1503.08835]



[EB, Simon Luca Villani, Steffen Schumann]

→ Simon

# EW corrections I: fixed-order

- corrections to (differential) 3-jet production @ QCD+EW NLO

[Max Reyer, Marek Schönherr, Steffen Schumann, 1902.01763]

- observe compensations between Sudakov-type suppression and sub-leading contributions

→ accidental, but illustrates importance of including all contributions

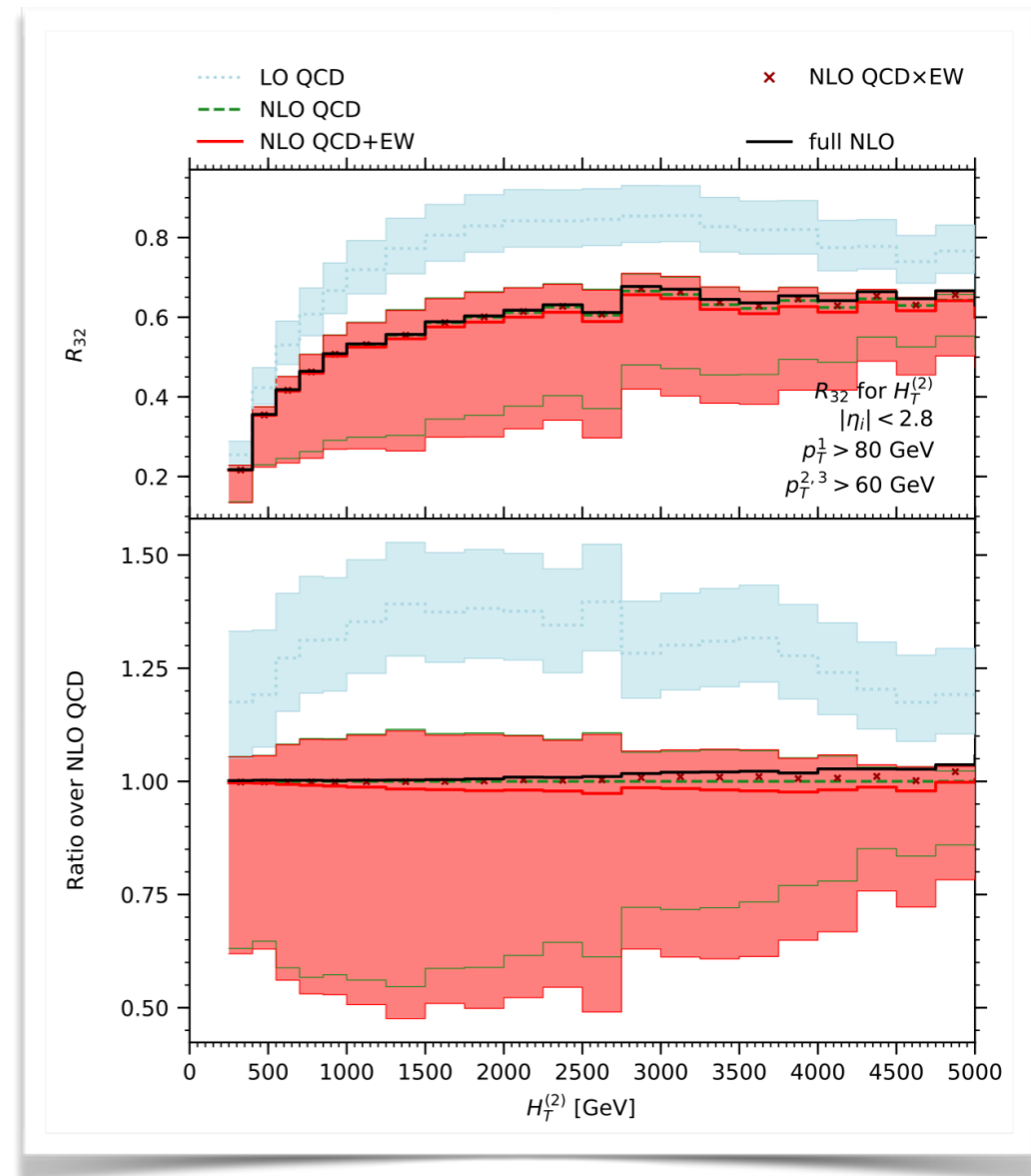
- application: 3-to-2 jet ratio  $R_{23}$

▸ found to be stable against EW corrections:  $\leq 5\%$  even for large  $p_T$

→ "confirms particular usefulness of  $R_{23}$  for determination of the strong coupling"

- WW(j) @ MEPS@NLO+EWvirt → study EWvirt validation/applicability

[Bräuer, Pellen, Schönherr, Schumann]



→ Marek (?)



# EW corrections II: Sudakov logs

[EB, Davide Napoletano]

- ▶ Implement Sudakov logs in high-energy (HE) limit within SHERPA
  - ▶ approximate EW corrections, capturing dominant contributions
  - ▶ as universal ME-level corrections: directly applicable to full machinery
- ▶ Fully general calculation for physical fields [\[Denner, Pozzorini \(2001\) hep-ph/0010201\]](#)
  - ▶ checked exact reproduction of their explicit log coefficients in HE limit (only PR missing)

Double/Single logs:

$$\text{DL} \sim \frac{\alpha}{4\pi s_W^2} \log^2 \frac{s}{M_W^2}$$

$$\text{SL} \sim \frac{\alpha}{4\pi s_W^2} \log \frac{s}{M_W^2}$$

$$K = \frac{\sum_s \sum_j (1 + 2\text{Re} \delta_s^j) |\mathcal{M}_s|^2}{\sum_i |\mathcal{M}_s|^2}$$

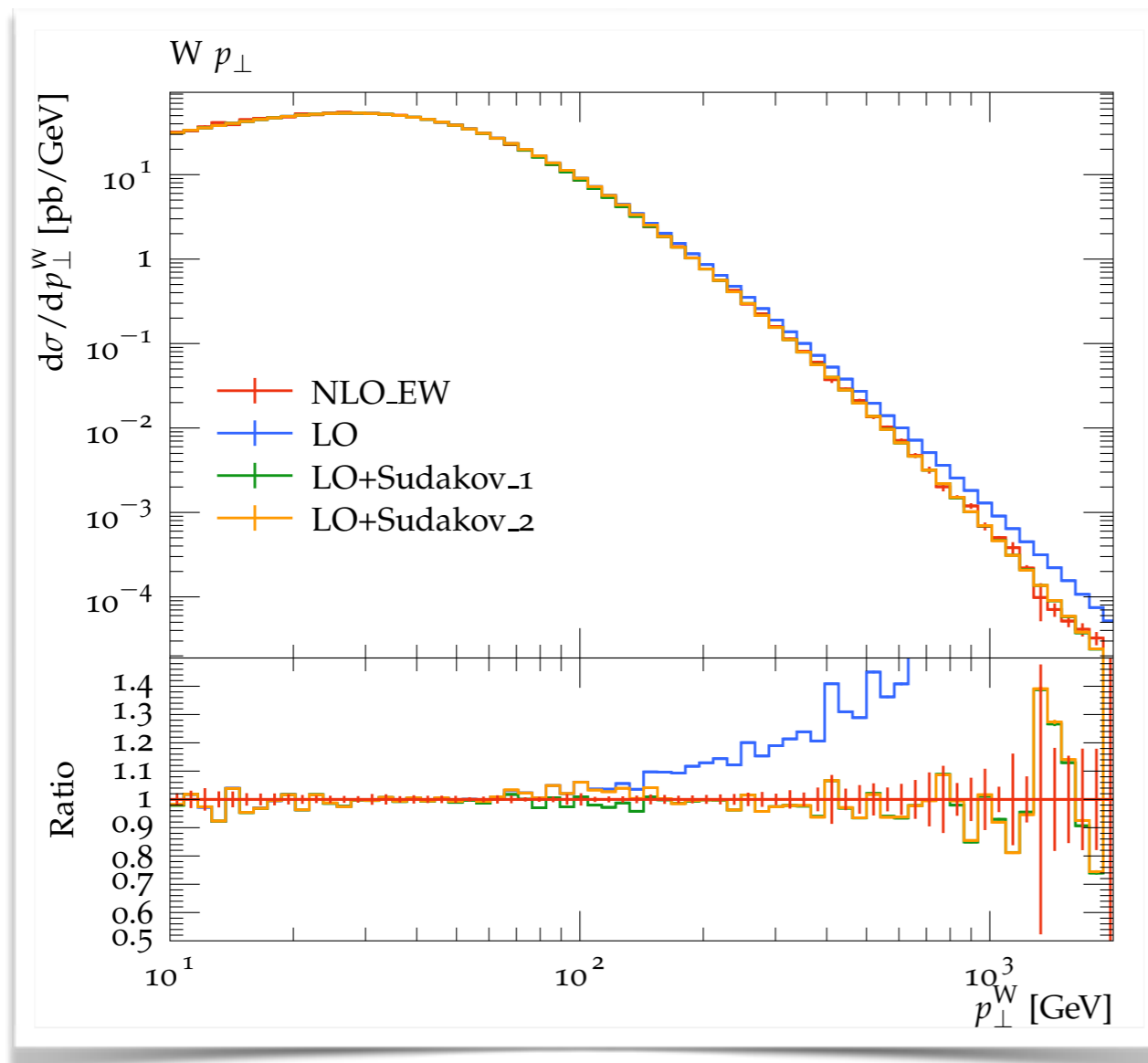
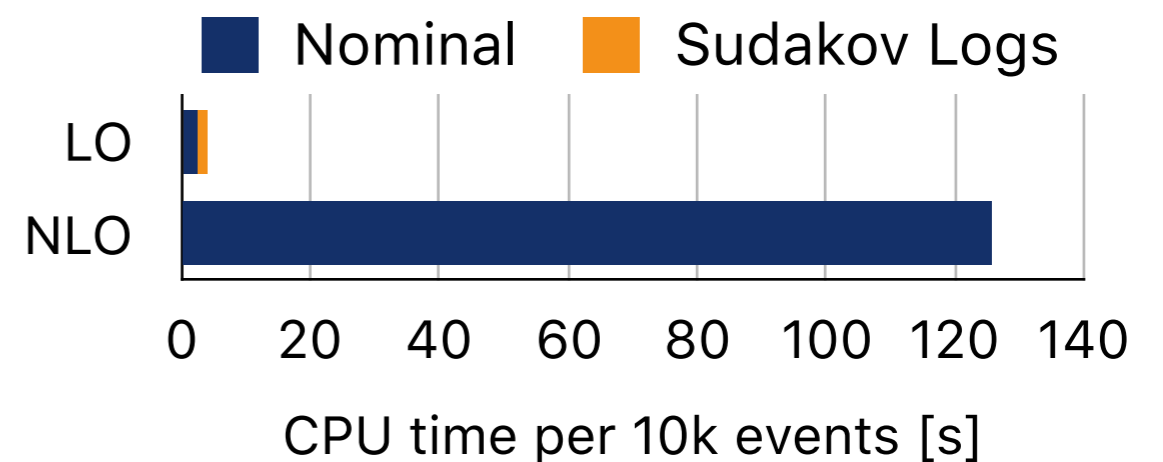
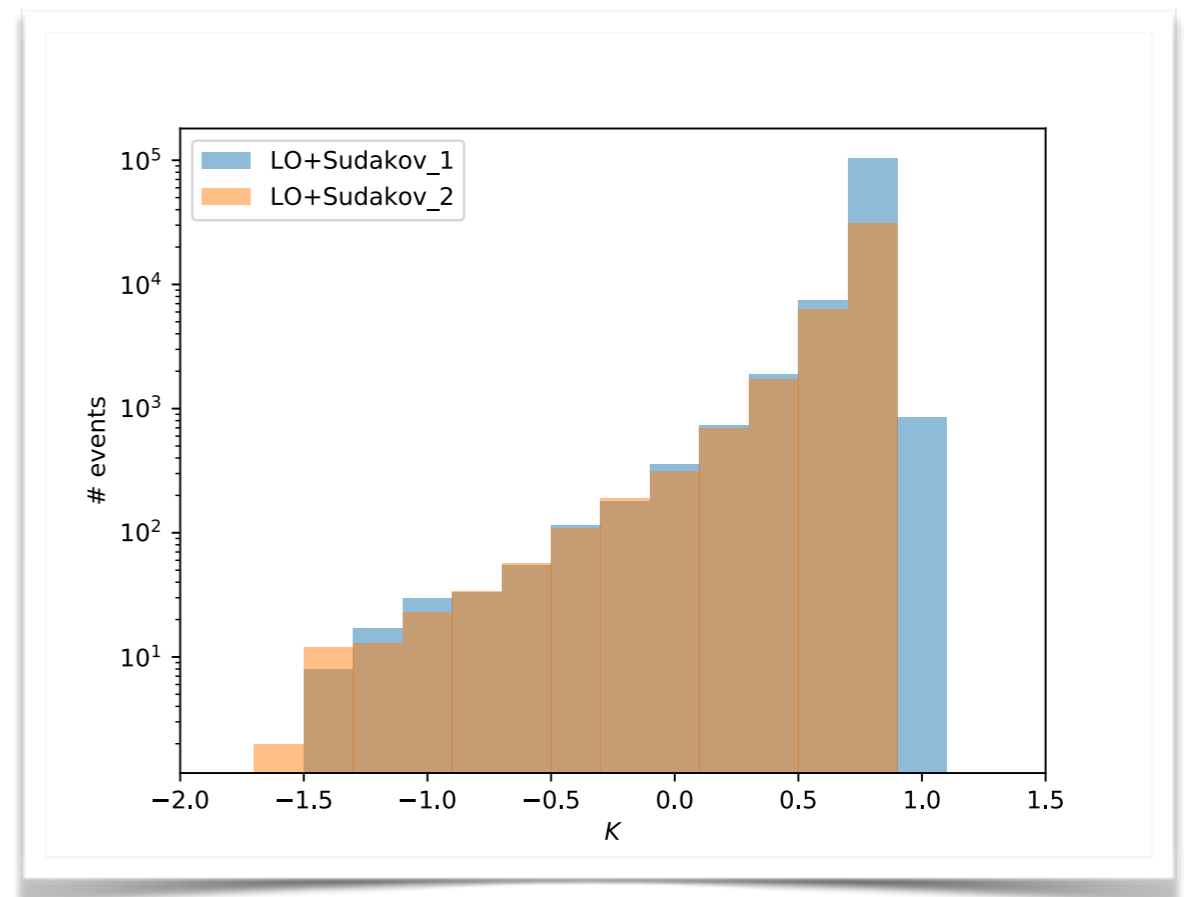
E.g. VBS WZ: “The corrections [to  $\sigma$ ] reach  $-16\%$  in the chosen fiducial region and are driven by Sudakov logarithms [...]”

[\[Denner et al. \(2019\) 1904.00882\]](#)

# EW corrections II: Sudakov logs

[EB, Davide Napoletano]

- ▶ Example:  $pp \rightarrow W^+W^-$  (on-shell)
  - ▶ FCC-pp:  $\sqrt{s} = 100$  TeV
  - ▶ no PR, no SSC (numerical issues!)
  - ▶ HE threshold:  $1, 2 m_W$



- ▶ **phase-space:**  
neural importance sampling
- ▶ **resummation / CAESAR plug-in:**  
soft-drop applications & jet resolutions
- ▶ **Loop-induced processes:**  
gg  $\rightarrow$  VV at MC@NLO
- ▶ **EW corrections:**  
3-jet calculation, WW(j) & Sudakov logs

Thanks

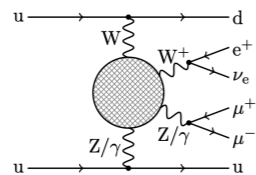
Backup

# Motivation: EW Sudakovs

- ALPGEN implementation

- [Chiesa et al. (2013) 1305.6837]
- proof-of-principle for  $Z[\nu\nu]+1,2,3$  jets
- fully general, BUT missing longitudinal V corrections
- "two is one and one is none"

- E.g. VBS WZ



- "The corrections [to  $\sigma$ ] reach  $-16\%$  in the chosen fiducial region and are driven by Sudakov logarithms that are large and negative and grow in size in the high-energy limit." [Denner et al. (2019) 1904.00882]
- VBS same-sign WW [Biedermann, Denner, Pellen (2017) 1708.00268]

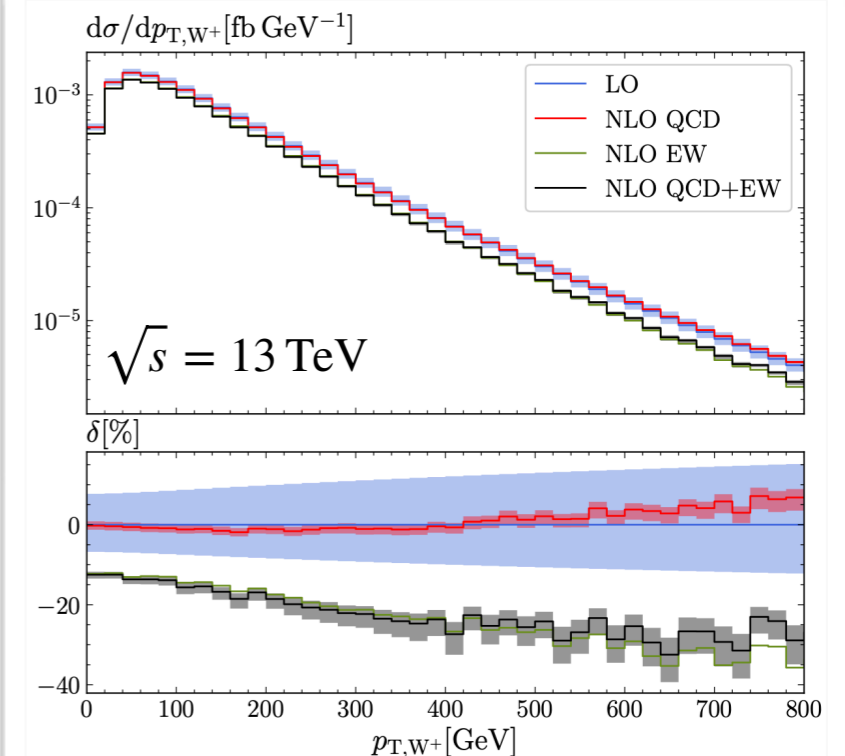
## Why not use NLO EW?:

NLO (QCD+)EW is ...

... not available for arbitrary procs / multiplicities

... not yet automated for precision event samples ( $\rightarrow$  matching/merging)

... time-consuming



# EW Sudakov Theory: Overview

- DL
  - soft+coll. V loops between pairs of ext. legs
- SL
  - purely coll. virtual V emission from ext. leg
  - field renormalisation constants
- Parameter renormalisation
  - charge and weak mixing angle, Yukawa and scalar self couplings
  - SL from UV region
- All shown to factorise from ME as a matrix:
  - $\delta \mathcal{M}^{i_1 \dots i_n}(p_1, \dots, p_n) = \mathcal{M}_0^{i'_1 \dots i'_n}(p_1, \dots, p_n) \delta_{i'_1 i_1 \dots i'_n i_n}$

High-energy limit (HE):

All invariants much larger than V masses:

$$r_{kl} = (p_k + p_l)^2 \sim 2p_k p_l \gg M_W^2$$

i.e.  $d\sigma$  better not dominated by resonances

Write logs in terms of:

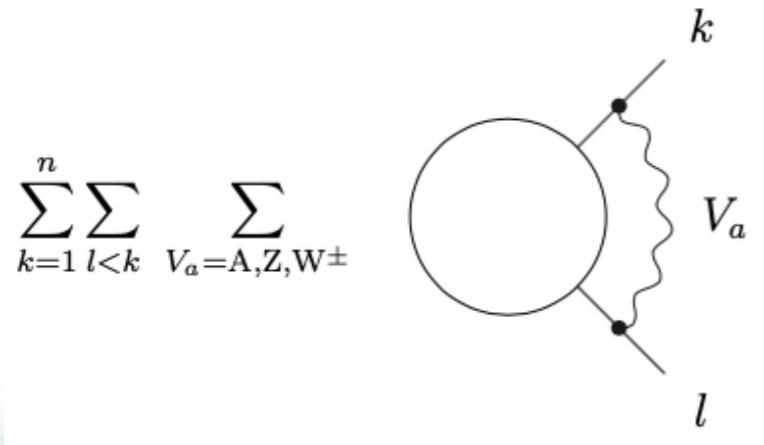
$$L\left(|r_{kl}|, M^2\right) := \frac{\alpha}{4\pi} \log^2 \frac{r_{kl}}{M^2}$$

$$l(r_{kl}, M^2) := \frac{\alpha}{4\pi} \log \frac{r_{kl}}{M^2}$$

$$L(s) := L(s, M_W^2), \quad l(s) := l(s, M_W^2)$$

log. approximation:  
omit terms  $\propto \log(\mathcal{O}(1))$

# EW Sudakov Theory: DL corrections I



$$\sum_{k=1}^n \sum_{l < k} \sum_{V_a = A, Z, W^\pm}$$

gauge bosons/couplings:

$$V_a = A, Z, W^\pm, \quad ieI_{i_k i_k}^{V_a}(k)$$

eikonal approx:  
set masses in numerator = 0

$$\delta \mathcal{M}^{i_1 \dots i_n} = \sum_{k=1}^n \sum_{l < k} \sum_{V_a = A, Z, W^\pm} \int \frac{d^4 q}{(2\pi)^4} \frac{-4ie^2 p_k p_l I_{i_k i_k}^{V_a}(k) I_{i_l i_l}^{V_a}(l) \mathcal{M}_0^{i_1 \dots i_k \dots i_l \dots i_n}}{(q^2 - M_{V_a}^2) [(p_k + q)^2 - m_{k'}^2] [(p_l - q)^2 - m_{l'}^2]}$$

logarithmic approx:  
region where \$V\_a\$ both soft and collinear to one leg

$$\delta \mathcal{M}^{i_1 \dots i_n} = \frac{1}{2} \sum_{k=1}^n \sum_{l \neq k} \sum_{V_a = A, Z, W^\pm} I_{i_k i_k}^{V_a}(k) I_{i_l i_l}^{\bar{V}_a}(l) \mathcal{M}_0^{i_1 \dots i_k \dots i_l \dots i_n} \left[ L(|r_{kl}|, M_{V_a}^2) - \delta_{V_a A} L(m_k^2, \lambda^2) \right]$$

$$L(|r_{kl}|, M^2) = \underbrace{L(s, M^2)}_{\text{LSC}} + \underbrace{2l(s, M^2) \log \frac{|r_{kl}|}{s}}_{\text{"angular" SSC}} + \cancel{L(|r_{kl}|, s)}$$

# EW Sudakov Theory: DL corrections II: LSC

$$\delta^{\text{LSC}} \mathcal{M}^{i_1 \dots i_n} = \frac{1}{2} \sum_{k=1}^n \sum_{l \neq k} \sum_{V_a=A, Z, W^\pm} I_{i'_k i_k}^{V_a}(k) I_{i'_l i_l}^{\bar{V}_a}(l) \mathcal{M}_0^{i_1 \dots i'_k \dots i'_l \dots i_n} L(s, M^2)$$

use invariance under global  $SU(2) \times U(1)$  transformations:

$$0 = \delta_{V_a} \mathcal{M}^{i_1 \dots i_n} = ie \sum_l I_{i'_l i_l}^{V_a}(l) \mathcal{M}_0^{i_1 \dots i'_l \dots i_n}$$

$$= \sum_{k=1}^n \delta_{i'_k i_k}^{\text{LSC}}(k) \mathcal{M}_0^{i_1 \dots i'_k \dots i_n} \quad \rightarrow \text{factorise as a matrix for each leg!}$$

W/Z mass gap

$$\delta_{i'_k i_k}^{\text{LSC}}(k) = -\frac{1}{2} \left[ C_{i'_k i_k}^{\text{ew}}(k) L(s) - 2 (I^Z(k))_{i'_k i_k}^2 \log \frac{M_Z^2}{M_W^2} l(s) + \delta_{i'_k i_k} Q_k^2 L^{\text{em}}(s, \lambda^2, m_k^2) \right]$$

(nearly) symmetric ew part

$$C^{\text{ew}} := \sum_{V_a=A, Z, W^\pm} I^{V_a} I^{\bar{V}_a}$$

purely em part:  
not meaningful w/o  
adding real radiation!



# EW Sudakov Theory: DL corrections II: SSC

- also factorise as a matrix, for each leg pair:

$$\delta^{\text{SSC}} \mathcal{M}^{i_1 \dots i_n} = \sum_{k=1}^n \sum_{l < k} \sum_{V_a=A, Z, W^\pm} \delta_{i'_k i'_l}^{V_a, \text{SSC}}(k, l) \mathcal{M}_0^{i_1 \dots i'_k \dots i'_l \dots i_n}$$

A loops:

$$\delta_{i'_k i'_l}^{A, \text{SSC}}(k, l) = 2 \left[ l(s) + \text{purely em } l(M_W^2, \lambda^2) \right] \log \frac{|r_{kl}|}{s} I_{i'_k i'_k}^A(k) I_{i'_l i'_l}^A(l)$$

Z loops:

non-diagonal in neutral sector ( $h_0 ZZ$ )

$$\delta_{i'_k i'_l}^{Z, \text{SSC}}(k, l) = 2l(s) \log \frac{|r_{kl}|}{s} I_{i'_k i'_k}^Z(k) I_{i'_l i'_l}^Z(l)$$

W loops:

non-diagonal everywhere

$$\delta_{i'_k i'_l}^{\pm, \text{SSC}}(k, l) = 2l(s) \log \frac{|r_{kl}|}{s} I_{i'_k i'_k}^\pm(k) I_{i'_l i'_l}^{\mp}(l)$$

# Interlude: GBET

Derivation of gauge invariance from high-energy unitarity bounds on the  $S$  matrix\*

John M. Cornwall,<sup>†</sup> David N. Levin, and George Tiktopoulos  
Department of Physics, University of California at Los Angeles, Los Angeles, California 90024  
(Received 21 March 1974)

- Set masses to zero in loop integrand numerator  
→ Feynman rules should have no inverse powers of  $M_{V_a}$

- BUUUT what about the HE limit of longitudinal polarisation vectors!?

$$\epsilon_L^\mu(p) = \frac{p^\mu}{M} + \mathcal{O}\left(\frac{M}{p^0}\right)$$

→ derivation so far not applicable!

- Use the Goldstone-Boson Equivalence Theorem (GBET)

$$\mathcal{M}_0^{\dots W_L^\pm} = \mathcal{M}_0^{\dots \phi^\pm}$$

$$\mathcal{M}_0^{\dots Z_L \dots} = i \mathcal{M}_0^{\dots \chi \dots}$$

→ ALPGEN does not support GB, hence no  $V_a^L$  corrections

one-loop corrections of the GBET:

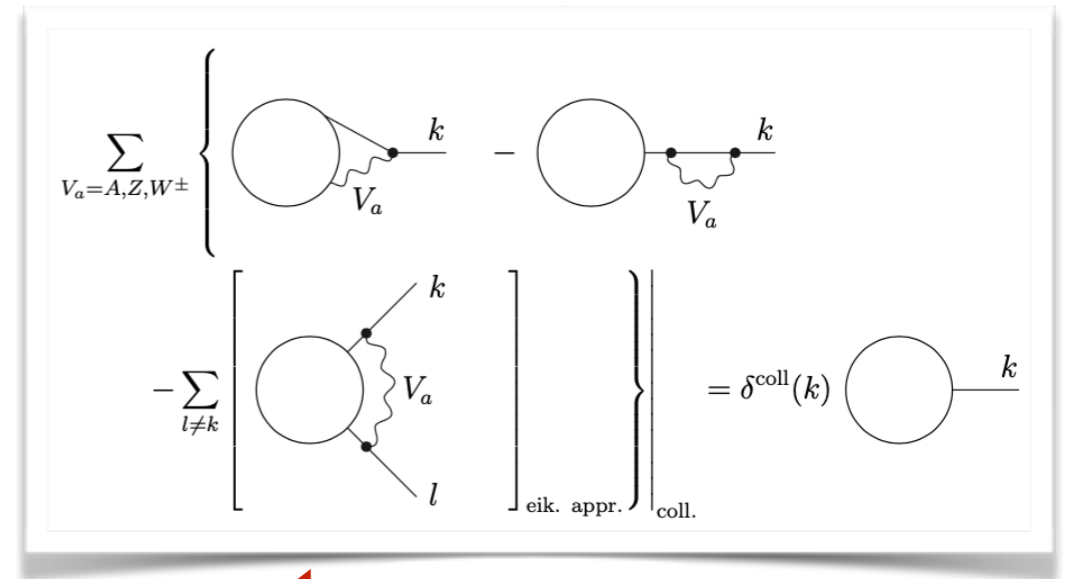
- do not contain DL
- DL corrections can use Born approximation on the left

Tackling this w/o GB?:

- [Cuomo, Vecchi, Wulzer (2019) 1911.12366]

# EW Sudakov Theory: SL corrections

- Two sources of soft OR coll. logs
  - field renormalisation constants give  $\delta Z_\varphi/2$  for each leg, soft and coll. contribs
  - coll. limit of loop diagrams where one leg splits into two internal lines (incl. one  $V_a$ )



$$\delta^C \mathcal{M}^{i_1 \dots i_n} = \sum_{k=1}^n \delta_{i'_k i_k}^C(k) \mathcal{M}_0^{i_1 \dots i'_k \dots i_n}$$

$$\delta_{i'_k i_k}^C(k) = \delta^{\text{coll}}(k) + \left. \frac{1}{2} \delta Z_{i'_k i_k}^\varphi \right|_{\mu^2=s}$$

- Example result for chiral fermions:

$$\delta_{f_\sigma f'_\sigma}^C(f^k) = \delta_{\sigma\sigma'} \left\{ \left[ \frac{3}{2} C_{f^k}^{\text{ew}} - \frac{1}{8s_W^2} \left( (1 + \delta_{kR}) \frac{m_{f_\sigma}^2}{M_W^2} + \delta_{kL} \frac{m_{f_{-\sigma}}^2}{M_W^2} \right) \right] l(s) + Q_{f_\sigma}^2 l^{\text{em}}(m_{f_\sigma}^2) \right\}$$

Yukawa terms:  
large contribs for (t, b) doublet

# EW Sudakov Theory: PR corrections

- From renormalisation of dimensionless parameters
  - charge
  - ew mixing angle  $c_w = \cos \theta_w$
  - Yukawa and Higgs self-couplings

- Logs are therefore related UV divergences

- Option 1: explicitly calculate logarithms:

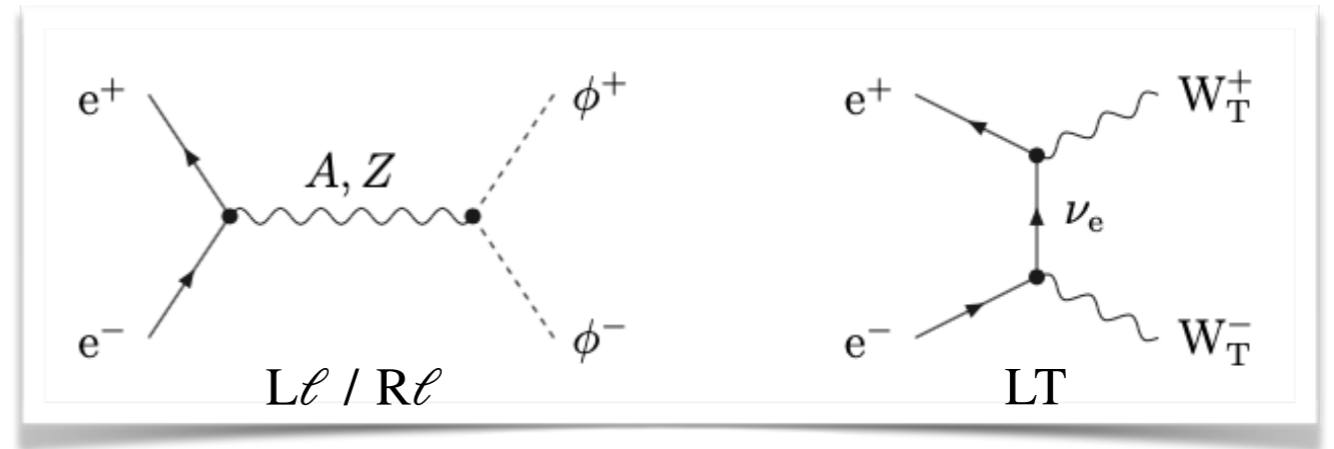
$$\delta^{\text{PR}} \mathcal{M} = \frac{\delta \mathcal{M}_0}{\delta e} \delta e + \frac{\delta \mathcal{M}_0}{\delta c_w} \delta c_w + \frac{\delta \mathcal{M}_0}{\delta h_t} \delta h_t + \frac{\delta \mathcal{M}_0}{\delta h_H} \delta h_H^{\text{eff}} \Big|_{\mu^2=s}$$

$$\text{e.g. } \frac{\delta c_w^2}{c_w^2} = \frac{s_w}{c_w} b_{AZ}^{\text{ew}l}(\mu^2)$$

- Option 2: Just let the parameters run and evaluate ME at the HE scale

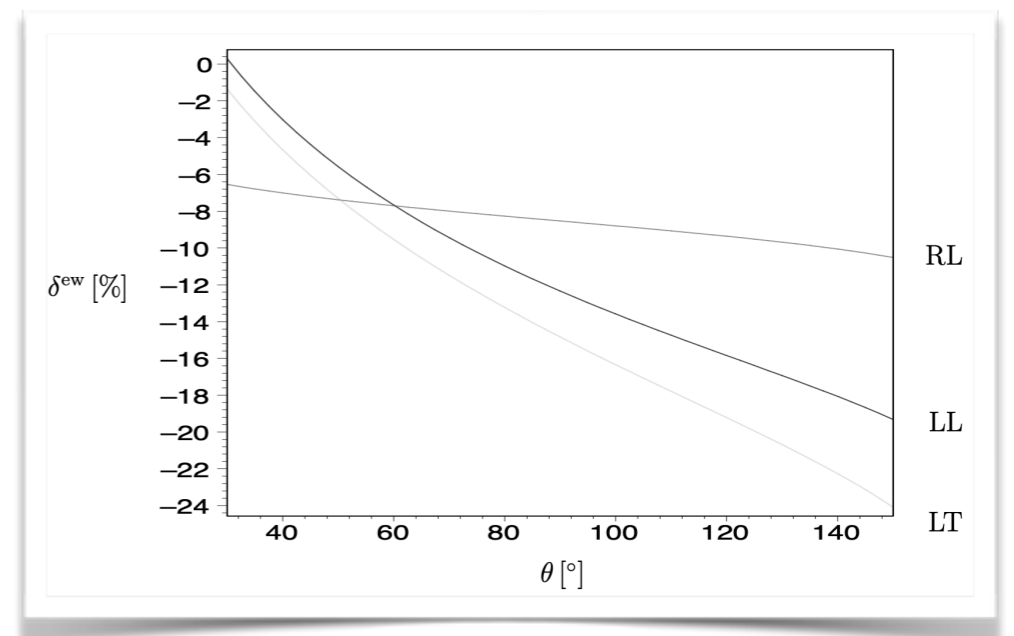
# EW Sudakov Example: $e_{\kappa}^{+} e_{\kappa}^{-} \rightarrow W_{\lambda_{+}}^{+} W_{\lambda_{-}}^{-}$

- $\kappa = R, L$
- $\lambda_{\pm} = \ell, \pm$ , but non-suppressed in HE only: both  $\ell$  ( $\ell$ ) or oppositely transverse (T)
- results independently verified



$\kappa\lambda_{\pm}$	DL: LSC	DL: LSC Z mass gap	DL: SSC (angular)	C	C: Yuk	PR
$L\ell$	-7.35	0.45	$5.76 \log t/u + 13.9 \log  t /s$	25.7	-31.8	-9.03
$R\ell$	-4.96	0.37	$-2.58 \log t/u$	18.6	-31.8	8.80
LT	-12.6	1.98	$-8.95(\log t/u + (1 - t/u)\log  t /s)$	25.2	—	-14.2
log	$L(s)$	$l(s)$	$l(s)$	$l(s)$	$l(s)$	$l(s)$

- left-handed fermion gives large negative DL and PR
- $W_T$ : no Yukawa, but other coeffs larger
- however, for  $\sqrt{s} = 1$  TeV, overall corrections similar for each helicity config



# EW Sudakov: Implementation

- Implementation within the SHERPA 3.0 framework
- well-documented and follow closely notation in [Denner, Pozzorini (2001) hep-ph/0010201]
- Generalised Standard Model definition to include GB
  - easy to calculate any ME value needed
- Calculate  $K$ -factor for each Monte-Carlo event
  - check HE limit, e.g.  $(p_i + p_j)^2 \geq xm_W$
  - put momenta on-shell for transformed MEs
  - calculate contributions to  $K$

```

Coeff_Value Sudakov::LsCoeff()
{
  Coeff_Value coeff{0.0};
  const auto& base_ampl = m_ampls.BaseAmplitude(m_current_spincombination);
  for (size_t i{0}; i < m_current_spincombination.size(); ++i) {
    const Flavour flav{base_ampl.Leg(i)->Flav()};
    const auto diagonal =
      -m_ewgroupconsts.DiagonalCew(flav, m_current_spincombination[i]) / 2.0;
    coeff += diagonal;
    if (flav.IsVector() && flav.Charge() == 0) {
      // special case of neutral transverse gauge bosons, they mix and hence
      // non-diagonal terms appear, cf. e.g. eq. (6.30);
      // assume they are actually transverse, because we have already
      // replaced longitudinal ones with Goldstone bosons when calling
      // BaseAmplitude() above
      assert(m_current_spincombination[i] != 2);
      const kf_code newkf = (flav.Kfcode() == kf_Z) ? kf_photon : kf_Z;
      const auto prefactor = -m_ewgroupconsts.NondiagonalCew() / 2.0;
      // we can use amplitudes without replacing longitudinal gauge bosons
      // here, because of (i) eq. (3.4) and (ii) Goldstone boson correction
      // terms are diagonal (hence we only need to pass the right flavour above
      // when using DiagonalCew())
      const auto transformed =
        TransformedAmplitudeValue({{i, newkf}}, m_current_spincombination);
      auto amplratio = transformed / m_current_me_value;
      coeff += prefactor * amplratio;
    }
  }
  return coeff;
}

```

$$\frac{1}{L(s)} \delta_s^{\text{LSC}} = \frac{1}{L(s)} \sum_{k'} \frac{\delta_{i_k i_k}^{\text{LSC}}(k) \mathcal{M}_s^{\dots k \dots}}{L(s) \mathcal{M}_s^{\dots k \dots}} = -\frac{1}{2} \left[ \sum_{k'} \frac{C_{i_k i_k}^{\text{ew}}(k) \mathcal{M}_s^{\dots k \dots}}{\mathcal{M}_s^{\dots k \dots}} \right]$$

Sudakov log of type  $j$  for helicities  $i$

$$K = \frac{\sum_s \sum_j (1 + 2\text{Re} \delta_s^j) |\mathcal{M}_s|^2}{\sum_i |\mathcal{M}_s|^2}$$

# EW Sudakov: Validation

$\kappa\lambda_{\pm}$	DL: LSC	DL: LSC Z mass gap	DL: SSC (angular)	C	C: Yuk	PR
$L\ell$	-7.35	0.45	$5.76 \log t/u + 13.9 \log  t /s$	25.7	-31.8	-9.03
$R\ell$	-4.96	0.37	$-2.58 \log t/u$	18.6	-31.8	8.80
LT	-12.6	1.98	$-8.95(\log t/u + (1 - t/u)\log  t /s)$	25.2	—	-14.2
<b>log</b>	$L(s)$	$l(s)$	$l(s)$	$l(s)$	$l(s)$	$l(s)$

- Check *exact* reproduction of log coefficients for any HE kinematics (test-driven development)

→ for all explicit results in [Denner, Pozzorini (2001)]:

$$ee \rightarrow W^+W^-, ZZ, ZA, AA, \mu^+\mu^-, u\bar{u}, d\bar{d}, b\bar{b}, t\bar{t}$$

- TODO: Parameter Renormalisation implementation still missing

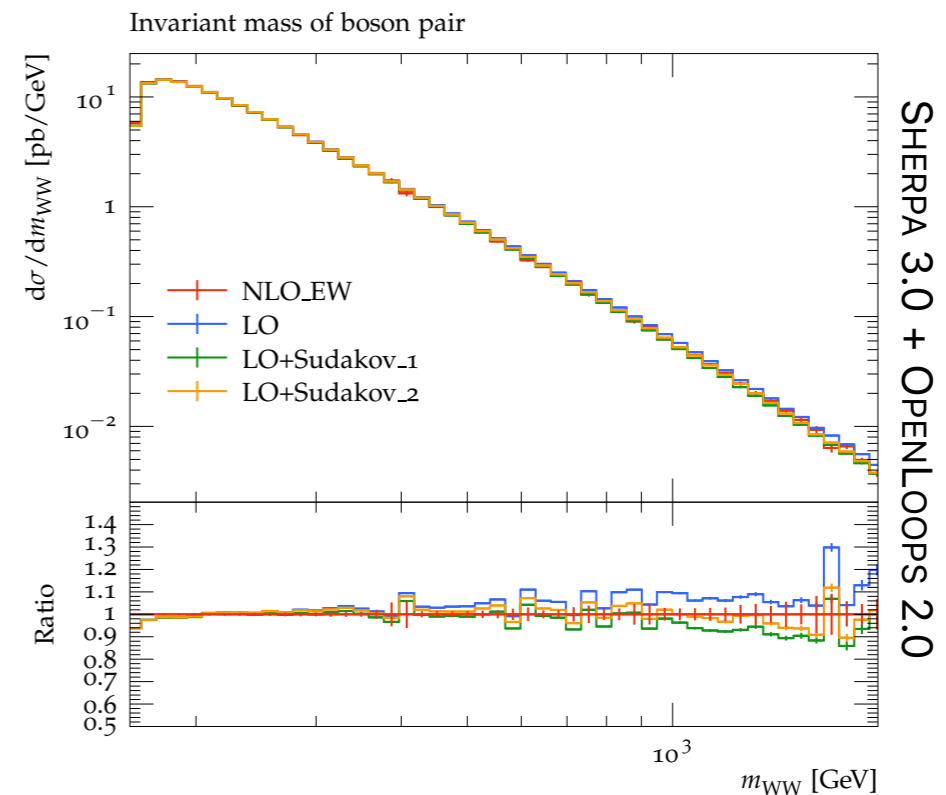
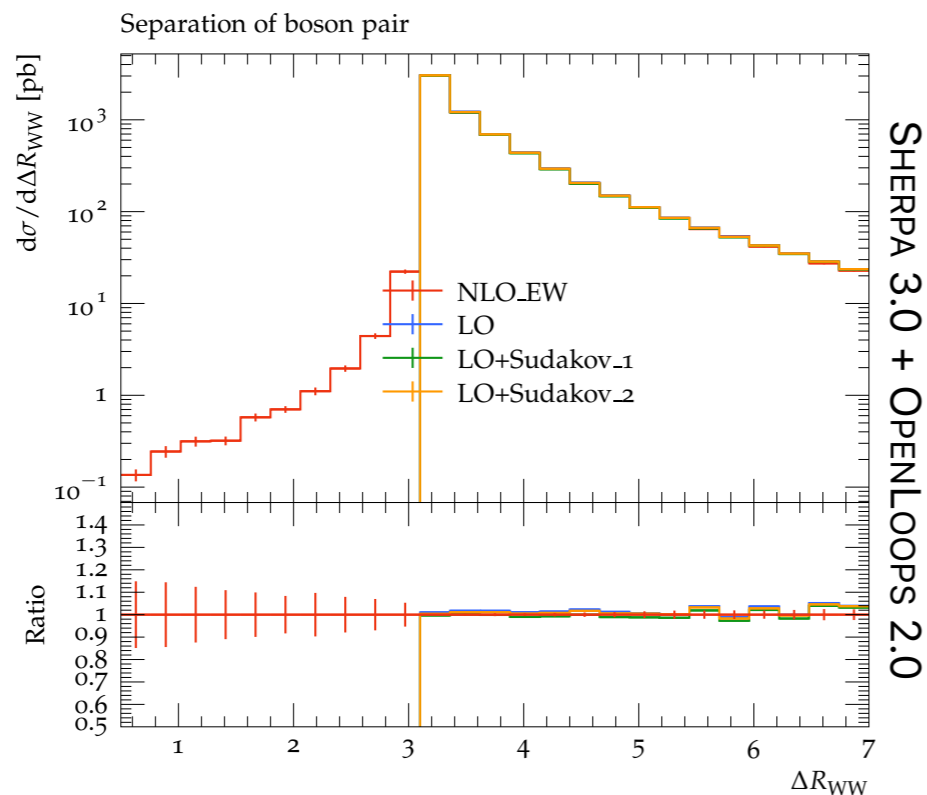
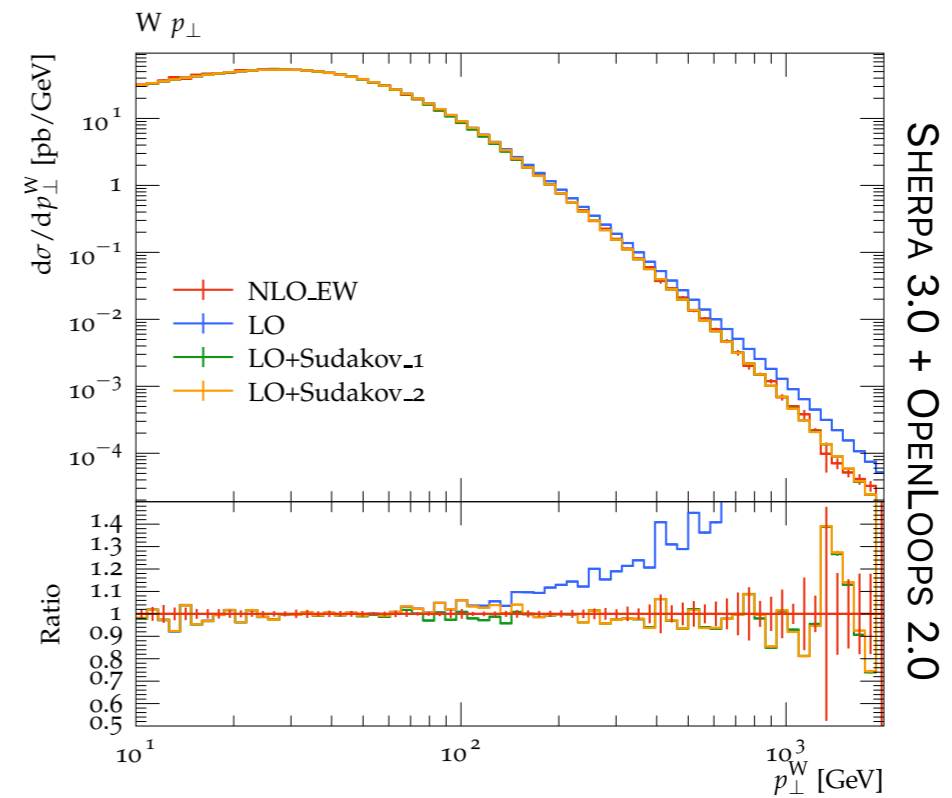
minus sign hunt due to different conventions:

$$D_{\mu} = \partial_{\mu} - igA_{\mu}^a T^a - ig'YB_{\mu} \quad (\text{Peskin/Schroeder, Sherpa})$$

$$D_{\mu} = \partial_{\mu} - igA_{\mu}^a T^a + ig'YB_{\mu} \quad (\text{Boehm/Denner, [Denner, Pozzorini(2001)])}$$

# EW Sudakov Example: $pp \rightarrow W^+W^-$

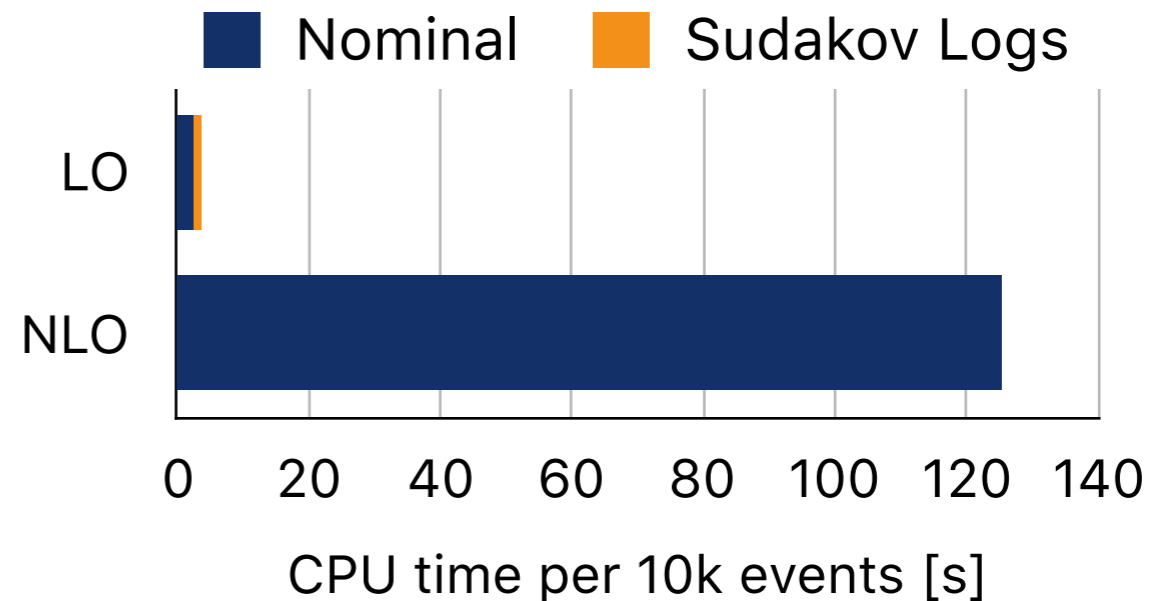
- FCC-pp:  $\sqrt{s} = 100 \text{ TeV}$
- on-shell diboson production
- no PR, no SSC (numerical issues)
- HE threshold:  $1, 2 m_W$





# EW Sudakov Example: $pp \rightarrow W^+W^-$

- CPU time per 10k weighted events
  - LO: 2.5 s
  - LO+Sudakov: 3.4 s (+ 36 %)
  - NLO: 125.5 s ( $\times 50$  /  $\times 35$ )  
(NOTE: on top of that need 20 % more events for same total  $\sigma$  accuracy)



- Weights shifted to smaller values
  - Sudakov suppression

