## Novel Physics Opportunities at the LHeC



# Stan Brodsky 든느를 NATIONAL ACCELERATOR LABORATORY 

ELECTRONS FOR THE LHC: Workshop on the LHeC, FCC-eh and PERLE
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## The LHeC

$s_{e p}=\left(p_{e}+p_{p}\right)^{2}=4 E_{e} E_{p}=4 \times 60 \mathrm{GeV} \times 7 \mathrm{TeV} \simeq 1.7 \mathrm{Te} V^{2}$
Equivalent to an e-p collider in the CM:

$$
E_{e}^{C M}=E_{p}^{C M} \simeq 650 \mathrm{GeV} \quad \sqrt{s}_{e p} \simeq 1.3 \mathrm{TeV}
$$

Equivalent to SLAC Fixed-Target DIS with $E_{e}^{F T} \simeq 900 \mathrm{TeV}$

## (A SLAC Linear Accelerator: 60,000 Mïles Long!)

$$
x_{b j}=\frac{Q^{2}}{2 q \cdot p}>10^{-7} \text { for } Q^{2}>1 G e V^{2}
$$

Novel High-Energy Electron-Proton Collider Physics at the LHeC

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Precise Higgs Factory

## Test Higgs Emission from the W at the LHeC


$W^{-} u \rightarrow H d$

$W^{-} c \rightarrow H b$

Intrinsic Charm at high $x$


Test $\gamma b \rightarrow H b^{\prime}$

## $b(x, Q)$ at high $x$ (Intrinsic Bottom)

## Crucial Physics for the LHeC

## Test for Lepton/Quark Compositeness at the LFeC



Measure $\frac{d \sigma}{d t}\left(e q \rightarrow e^{\prime} q^{\prime}\right)$ at very high $Q^{2}$

Test for Lepto-Quarks at the LHeC

s - channel resonance : $e q \rightarrow[\ell q] \rightarrow e^{\prime} q^{\prime}$ at $\hat{s}=m_{\ell q}^{2}$

## Radiation-A mplitude Zero at the LHeC

$$
\gamma W^{+} \rightarrow c \bar{b}
$$



$$
\begin{aligned}
& \frac{d \sigma}{d t}\left(W^{+} \gamma \rightarrow c \bar{b}\right)=0 \\
& \text { at } \cos \theta=\frac{e_{\bar{b}}}{e_{W^{+}}}=\frac{1}{3} \\
& \text { Tests } g_{W}=g_{q}=2
\end{aligned}
$$

## Fundamental Standard Model Physics Tests at the LFteC

## Elimination of Scale Ambiguities!

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## An Important Theoretical Physics Advance for the LHeC

## BLM/PMC Principle of Maximum Conformality

$$
\alpha_{s}\left(q^{2}\right) \text { sums all } \beta \text { terms }
$$

- Eliminates renormalization scale ambiguities for PQCD and SM predictions
- Predictions are independent of scheme and initial scale choice
- Convergent conformal series: No "renormalons" $C_{n} \sim \alpha_{s}^{n} \beta_{o}^{n} n$ !
- Consistent with Gell-Mann Low for QED

$$
\alpha(t)=\frac{\alpha\left(t_{o}\right)}{1-\Pi\left(t, t_{0}\right)}
$$

- Eliminates many outstanding conflicts of pQCD with experiment
- Maximizes sensitivity of LHeC measurements to new physics

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T. Gehrmann, N. H'afliger, P. F. Monni


Renormalization scale depends on the thrust

T. Gehrmann, N. H'afliger, P. F. Monni


S.-Q. Wang, L. Di Giustino,
X.-G. Wu, sjb
S.-Q. Wang, L. Di Giustino, X.-G. Wu, sjb


Principle of Maximum Conformality (PMC)

S.-Q.Wang, L. Di Giustino, X.-G. Wu, SJB

The Renormalization Scale Ambiguity for Top-Pair Production Eliminated Using the 'Principle of Maximum Conformality' (PMC)


Top quark forward-backward asymmetry predicted by pQCD NNLO within $1 \sigma$ of CDF/DO measurements using $P M C / B L M$ scale setting

## BLM-PMC

- Test QCD to maximum precision
- High precision determination of $\alpha_{s}\left(Q^{2}\right)$ at all scales
- Relate observable to observable --no scheme or scale ambiguity
- Eliminate renormalization scale ambiguity in a schemeindependent manner
- Relate renormalization schemes without ambiguity
- Maximize sensitivity to new physics


## The QCD pomeron with optimal renormalization

Stanley J. Brodsky (SLAC), Victor S. Fadin (Novosibirsk, IYF), Victor T. Kim (St. Petersburg, INP \& lowa State U., IITAP), Lev N. Lipatov (St. Petersburg, INP), Grigorii B. Pivovarov (Moscow, INR \& lowa State U., IITAP). Dec 1998. 11 pp.
Published in JETP Lett. 70 (1999) 155-160
SLAC-PUB-8037, IITAP-98-010
DOI: 10.1134/1.568145
e-Print: hep-ph/9901229 | PDF

## BFKLP

Based on BLM/PMC

$$
x=\frac{k^{+}}{P^{+}}=\frac{k^{0}+k^{3}}{P^{0}+P^{3}}
$$

生

Measurements of hadron LF wavefunction are at fixed LF time Fixed $\tau=t+z / c$

Like aflash photograph

$$
x_{b j}=x=\frac{k^{+}}{P^{+}}
$$

Invariant under boosts! Independent of $P^{11}$

## The LHeC :

Key Measurements of Hadron Dynamics and Structure

Fixed $\tau=t+z / c$


## Light Front Wavefunctions: Boost Invariant, Causal

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## Advantages of the Dirac's Front Form for Hadron Physics

 Poincare' InvariantPhysics Independent of Observer's Motion

- LHeC Measurements are made at fixed $\tau$
- Causality is automatic
- Structure Functions are squares of LFWFs
- Form Factors are overlap of LFWFs
- LFWFs are frame-independent: no boosts, no pancakes!


## Penrose, Terrell, Weisskopf

- Same structure function measured at an ep collider and in the proton rest frame
- No dependence of hadron structure on observer's frame
- LF Holography: Dual to AdS space
- LF Vacuum trivial -- no vacuum condensates!
- Profound implications for Cosmological Constant

Roberts, Shrock, Tandy, sjb


$$
\left|p, S_{z}>=\sum_{n=3} \Psi_{n}\left(x_{i}, \vec{k}_{\perp i}, \lambda_{i}\right)\right| n ; \vec{k}_{\perp_{i}}, \lambda_{i}>
$$

sum over states with $n=3,4, \ldots$ constituents
The Light Front Fork State Wavefunctions

$$
\Psi_{n}\left(x_{i}, \vec{k}_{\perp i}, \lambda_{i}\right)
$$

are boost invariant; they are independent of the hadron's energy and momentum $P^{\mu}$.

The light-cone momentum fraction

$$
x_{i}=\frac{k_{i}^{+}}{p^{+}}=\frac{k_{i}^{0}+k_{i}^{z}}{P^{0}+P^{z}}
$$

are boost invariant.

$$
\sum_{i}^{n} k_{i}^{+}=P^{+}, \sum_{i}^{n} x_{i}=1, \sum_{i}^{n} \vec{k}_{i}^{\perp}=\overrightarrow{0}^{\perp}
$$

> Intrinsic heavy quarks
> $s(x), c(x), b(x)$ at high $x$ !

$$
\begin{aligned}
& \bar{s}(x) \neq s(x) \\
& \bar{u}(x) \neq \bar{d}(x)
\end{aligned}
$$



Fixed LF time $\tau=t+z / c$

$$
\bar{d}(x) / \bar{u}(x) \text { for } 0.015 \leq x \leq 0.35
$$

■ E866/NuSea (Drell-Yan)

$$
\bar{d}(x) \neq \bar{u}(x)
$$

Interactions of quarks at same rapidity in 5-quark Fock state

Intrinsic sea quarks


## Fixed LF time

Proton Self Energy Intrinsic Heavy Quarks


Probability $(\mathrm{QED}) \propto \frac{1}{M_{\ell}^{\text {t }}}$
Collins, Ellis, Gunion, Mueller, sjb
M. Polyakov

## Fixed LF time

Proton 5-quark Fock State:
Intrinsic Heavy Quarks


$$
x_{Q} \propto\left(m_{Q}^{2}+k_{\perp}^{2}\right)^{1 / 2}
$$

QCD predicts
Intrinsic Heavy Quarks at high x!

## Minimal off-shellness

Maximum at Equal rapidity!
Probability $(\mathrm{QED}) \propto \frac{1}{M_{\ell}^{4}} \quad$ Probability $(\mathrm{QCD}) \propto \frac{1}{M_{Q}^{2}}$

Rigorous OPE
Analysis

Collins, Ellis, Gunion, Mueller, sjb
Polyakov, et al.


Two Components (separate evolution):
$c\left(x, Q^{2}\right)=c\left(x, Q^{2}\right)_{\text {extrinsic }}+c\left(x, Q^{2}\right)_{\text {intrinsic }}$

$c\left(x, Q^{2}\right)=c\left(x, Q^{2}\right)_{\text {extrinsic }}+c\left(x, Q^{2}\right)_{\text {intrinsic }}$
$p \bar{p} \rightarrow \gamma+Q+X$

$$
\frac{\Delta \sigma(\bar{p} p \rightarrow \gamma c X)}{\Delta \sigma(\bar{p} p \rightarrow \gamma b X)}
$$

Ratio is insensitive to gluon PDF, scales
$g c \rightarrow \gamma c$

## Signal for

 significant intrinsic charmMesropian, Bandurin
LHC: $p p \rightarrow Z^{0}{ }_{c} X$
Boettcher, Itten, Williams

## Intrinsic Heavy-Quark Fock

- Rigorous prediction of QCD, OPE
- Color-Octet Color-Octet Fock State

- Probability $\quad P_{Q \bar{Q}} \propto \frac{1}{M_{Q}^{2}} \quad P_{Q \bar{Q} Q \bar{Q}} \sim \alpha_{S}^{2} P_{Q \bar{Q}} \quad P_{c \bar{c} / p} \simeq 1 \%$
- Large Effect at high x
- Greatly increases kinematics of colliders such as Higgs production !!
- Underestimated in conventional parameterizations of heavy quark distributions
- Many EIC, LHeC tests


Produce charm hadrons at high x
Charm not a reliable signal for the high - glwon distribution

$$
e p \rightarrow e^{\prime} c g X, e p \rightarrow e^{\prime} b g X
$$



LHeC: Measure $c(x, Q), b(x, Q)$ at large $x$


Test $\gamma c \rightarrow Z^{0} c^{\prime}$
$c(x, Q)$ at high $x$ (Intrinsic Charm)


Test $\gamma c \rightarrow W^{+} b^{\prime}$
$c(x, Q)$ at high $x$ (Intrinsic Charm)

## Test Higgs-strahlung from Heary Quarks at the LHeC



Test $\gamma b \rightarrow H b^{\prime}$
$b(x, Q)$ at high $x$ (Intrinsic Bottom)

## "Hadronization at the Amplitude Level"



## Fixed LF time

Proton 5-quark Fock State:
Intrinsic Heavy Quarks


$$
x_{Q} \propto\left(m_{Q}^{2}+k_{\perp}^{2}\right)^{1 / 2}
$$

QCD predicts
Intrinsic Heavy Quarks at high x!

## Minimal off-shellness

Maximum at Equal rapidity!
Probability $(\mathrm{QED}) \propto \frac{1}{M_{\ell}^{4}} \quad$ Probability $(\mathrm{QCD}) \propto \frac{1}{M_{Q}^{2}}$

Rigorous OPE
Analysis

Collins, Ellis, Gunion, Mueller, sjb
Polyakov, et al.

## "Hadronization at the Amplitude Level"



Collinear heavy quarks and heavy hadrons at same rapidity as proton

Barger, Halzen, Keung PRD 25 (198I)


## Coalesece of comovers produces high-XF heavy hadrons



Spectator counting rules

$$
\frac{d N}{d x_{F}} \propto\left(1-x_{F}\right)^{2 n_{\text {spect }}-1}
$$

Coalescence of Comoving Charm and Valence Quarks Produce $J / \psi, \Lambda_{c}$ and other Charm Hadrons at High $x_{F}$

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- EMC data: $c\left(x, Q^{2}\right)>30 \times$ DGLAP $Q^{2}=75 \mathrm{GeV}^{2}, x=0.42$
- High $x_{F} p p \rightarrow J / \psi X$

Rules out color drag model (Pythia)

- High $x_{F} p p \rightarrow J / \psi J / \psi X$
- High $x_{F} p p \rightarrow \wedge_{c} X$


## Evidence for IQ

- High $x_{F} p p \rightarrow \Lambda_{b} X$
- High $x_{F} p p \rightarrow$ 三( $c c d$ ) $X$ (SELEX)

Explain Tevatron anomalies: $p \bar{p} \rightarrow \gamma c X, Z c X$
Interesting spin, charge asymmetry, threshold, spectator effects
Important corrections to B decays; Quarkonium decays
Gardner, Karliner, sjb

## Fixed Target



## Use LHeC 60 GeV Electron Ring in Fixed-Target Mode

HERMES (HERA), SMOG(LHCb)
Complimentary to LHeC Program Nuclear and Polarized ProtonTargets Large-x Domain of DIS

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Coalescence maximal at matching rapidities

$$
\operatorname{High} x_{\Lambda_{b}}^{F}
$$

LHeC: Measure heary hadrons produced at high $x_{F}$

Light-Front Wavefunctions and Heavy-Quark Electroproduction


Coalescence of comovers produces $Z_{c}^{+}$tetraquark

## Why is Intrinsic Heavy Quark Phenomenon Important?

- Test Fundamental QCD predictions OPE, Non-Abelian QCD Non-Abelian: $P_{Q \bar{Q}} \propto \frac{1}{M_{Q \bar{Q}}^{2}}$ Abelian: $P_{Q \bar{Q}} \propto \frac{1}{M_{Q \bar{Q}}^{4}}$
- Test non-perturbative effects
- Important for correctly identifying the gluon distribution
- High-xf open and hidden charm and bottom; discover exotic states
- Explain anomalous high pT charm jet + $\gamma$ data at Tevatron
- Important source of high energy $\mathbf{v}$ at IceCube

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$$
\gamma * p \rightarrow c \bar{c}+p^{\prime}
$$



Odderon-Pomeron Interference gives $c$ vs. $\bar{c}$ asymmetry Rathsman, Merino, sj

Deep Inelastic Electron-Proton Scattering


Conventional wisdom:
Final-state interactions of struck quark can be neglected

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Final-State Gluonic Interactions

$$
\begin{aligned}
& \text { Produce Diffractive Deep } \\
& \text { Inelastic Scattering (DDIS) }
\end{aligned}
$$



# Quark Rescattering in Final State 

Hoyer, Marchal, Peigne, Sannino, SJB (BHMPS)

Enberg, Hoyer, Ingelman, SJB

Hwang, Schmidt, SJB

Leading Twist: Bj Scaling
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Low-Nussinov model of Pomero

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SIne

## QCD Mechanism for Rapidity Gaps



Reproduces lab-frame color dipole approach
DDIS: Crucial Input for leading-twist nuclear shadowing
DDIS: Diffractive Deep Inelastic Scattering

Remarkable observation at HERA

are
diffractive!


Fraction $r$ of events with a large rapidity gap, $\eta_{\max }<1.5$, as a function of $Q_{\mathrm{DA}}^{2}$ for two ranges of $x_{\mathrm{DA}}$. No acceptance corrections have been applied.
M. Derrick et al. [ZEUS Collaboration], Phys. Lett. B 315, 481 (1993)

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H1: de Roeck, et al.

## Diffractive Structure Function $F_{2}{ }^{D}$



## Diffractive inclusive cross section

$\frac{\mathrm{d}^{3} \sigma_{N C}^{\text {diff }}}{\mathrm{d} x_{\mathbb{P}} \mathrm{d} \beta \mathrm{d} Q^{2}} \propto \frac{2 \pi \alpha^{2}}{x Q^{4}} F_{2}^{D(3)}\left(x_{\mathbb{P}}, \beta, Q^{2}\right)$
$F_{2}^{D}\left(x_{\mathbb{P}}, \beta, Q^{2}\right)=f\left(x_{\mathbb{P}}\right) \cdot F_{2}^{\mathbb{P}}\left(\beta, Q^{2}\right)$
extract DPDF and $x g(x)$ from scaling violation
Large kinematic domain $3<Q^{2}<1600 \mathrm{GeV}^{2}$
Precise measurements sys $5 \%$, stat $5-20 \%$
About 15\% of DIS events are
 diffractive!


DDIS: Diffractive Deep Inelastic Scattering

Integration over on-shell domain produces phase i
Need Imaginary Phase to Generate Pomeron
Also: Need Imaginary Pbase to Generate "Sivers Effect" T-Odd Single-Spin Asymmetry

Physics of FSI not in LF Wavefunction of Target
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90\% of proton momentum carried off by final state p' in $15 \%$ of events!

Gluon momentum fraction misidentified!

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Physics at the LHeC

## Anti-Shadowing



## Nuclear Shadowing in QCD



Shadowing depends on understanding leading twist-diffraction in DIS Nuclear Shadowing not included in nuclear LFWF !

Dynamical effect due to virtual photon interacting in nucleus
Diffraction via Reggeon gives constructive interference!
Anti-shadowing not universal


Diffraction via Pomeron gives destructive interference!

## Shadowing

## Reggeon <br> Exchange

Phase of two-step amplitude relative to one step:
$\frac{1}{\sqrt{2}}(1-i) \times i=\frac{1}{\sqrt{2}}(i+1)$

Constructive Interference

Depends on quark flavor!

Thus antishadowing is not universal

Different for couplings of $\gamma^{*}, Z^{0}, W^{ \pm}$

## Criticaltests: Tagged SIDIS, Drell-Yan



The one-step and two-step processes in DIS on a nucleus.

Coherence at small Bjorken $x_{B}$ :
$1 / M x_{B}=2 \nu / Q^{2} \geq L_{A}$.


## Regge

If the scattering on nucleon $N_{1}$ is via exchange, the one-step and two-step amplitudes are oppesite in phase, thus diminishing the $\bar{q}$ flux reaching $N_{2}$.
constructive in phase thus increasing the flux reaching $\mathrm{N}_{2}$

## Reggeon DDIS produces nuclear flavor-dependent anti-shadowing

## Anti-shadowing



Nuclear Antishadowing not universal!

Shadowing and Antishadowing in Lepton-Nucleus Scattering

- Shadowing: Destructive Interference of Two-Step and One-Step Processes Pomeron Exchange
- Antishadowing: Constructive Interference of Two-Step and One-Step Processes! Reggeon and Odderon Exchange
- Antishadowing is Not Universal!

Electromagnetic and weak currents: different nuclear effects!
Potentially significant for NuTeV Anomaly\}

Jian-Jun Yang Ivan Schmidt Hung Jung Lu sjb

## Crucial LHeC Tests

$$
\gamma^{*} p \rightarrow n X
$$



Charge-Exchange Diffractive Deep Inelastic Scattering CEDDIS

## $\gamma^{*} A \rightarrow \gamma^{*} A \quad$ Nuclear Forward DVCS

$q^{+}=0 \quad q_{\perp}^{2}=Q^{2}=-q^{2}$
Illustrates the


$$
A-1
$$

Front-Face Nucleon $N_{1}$ struck
Front-Face Nucleon $N_{1}$ not struck One-Step / Two-Step Interference
Study Double Virtual Compton Scattering $\gamma^{*} A \rightarrow \gamma^{*} A$
cannot reduce to real phase matrix element of local operator! No Sum Rules!
I. Schmidt, S. Liuti, sjb

## Nuclear PDFs

- Shadowing from destructive interference of 2-step and I-step processes

Gribov-Glauber, Stodolsky

- Anti-Shadowing from constructive interference of 2 -step and I -step processes
H. Lu, sjb
- Diffractive DIS and Charge-Exchange DDIS crucial inputs
- Handbag amplitude for nuclear DVCS not applicable
- OPE and Sum Rules inapplicable to nuclear pdfs!
I. Schmidt, S. Liuti, sjb
- Multiple scattering effects in high density proton pdf at low x. Nonlinear QCD.


## Ridge Formation

## Two particle correlations: CMS results



- Ridge: Distinct long range correlation in $\eta$ collimated around $\Delta \Phi \approx 0$ for two hadrons in the intermediate $1<\mathrm{p}_{\mathrm{T}}, \mathrm{q}_{\mathrm{T}}<3 \mathrm{GeV}$ High Multiplicity Events


## Origin of same-side CMS ridge in $p$ p Collisions

## Collision of Flux Tubes

Bjorken, Goldhaber, sjb


$$
\vec{V}=\sum_{i=1}^{N}\left[\cos 2 \phi_{i} \hat{x}+\sin 2 \phi_{i} \hat{y}\right]
$$

## LFHQD Light-Front Holographic QCD

- Predicts Hadron Spectra and Dynamics (LFWFs)
- Color Confinement; Universal Mass Scale
- Illuminates Supersymmetric Features of Hadron Physics: Equal-Mass Mesons, Baryons and Tetraquarks for Light and Heavy Quarks
- Universal Regge Trajectories: in n and L
- Massless composite pion for $\mathrm{m}_{\mathrm{q}}=0$
- Predicts Running QCD coupling at all scales: $\alpha_{s}\left(Q^{2}\right)$

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The leading Regge trajectory: $\Delta$ resonances with maximal J in a given mass range. Also shown is the Regge trajectory for mesons with $J=L+S$.
E. Klempt and B. Ch. Metsch

## 6. $M^{2}\left(\mathrm{GeV}^{2}\right)$ <br> $\rho-\Delta$ superpartner trajectories <br>  <br> fermions <br> BARYONS <br> [qqq] <br> $L_{M}=L_{B}+1$ <br> Dosch, de Teramond, sjb <br> L (Orbital Angular Momentum)

Superconformal Algebra

## 2X2 Hadronic Multiplets

Bosons, Fermions with Equal Mass! Meson

Baryon

$\phi_{M}, L_{B}+1 \quad \underset{\substack{\psi_{B+}, L_{B} \\ \text { Baryon }}}{L_{B}}$

$$
\begin{array}{r}
R_{\lambda}^{\dagger} \bar{q} \rightarrow[q q] \\
\overline{3}_{C} \rightarrow \overline{3}_{C}
\end{array}
$$

$$
\begin{array}{r}
R_{\lambda}^{\dagger} q \rightarrow[\bar{q} \bar{q}] \\
3_{C} \rightarrow 3_{C}
\end{array}
$$



Proton: lu[ud]> Quark + Scalar Diquark Equal Weight: L=0, L=1

Superconformal Quantum Mechanics Light-Front Holography

$$
\frac{M^{2}}{4 \kappa^{2}}
$$

de Tèramond, Dosch, Lorcè, sjb
$M^{2}\left(n, L_{B}\right)=4 \kappa^{2}\left(n+L_{B}+1\right) N_{-}^{7-}$

Same slope

$$
N \frac{5^{+}}{2}(1680)
$$

$$
b_{3}
$$

$\lambda=\kappa^{2}$
de Tèramond, Dosch, Lorce', sjb

$$
m_{u}=m_{d}=46 \mathrm{MeV}, m_{s}=357 \mathrm{MeV}
$$



Fit to the slope of Regge trajectories, including radial excitations
Same Regge Slope for Meson, Baryons:
Supersymmetric feature of hadron physics

## Supersymmetry across the light and heavy-light spectrum



## Supersymmetry across the light and heavy-light spectrum



Heavy bottom quark mass does not break supersymmetry

## Supersymmetry in QCD

- A hidden symmetry of Color SU(3) in hadron physics
- QCD: No squarks or gluinos!
- Emerges from Light-Front Holography and Super-Conformal Algebra
- Color Confinement
- Massless Pion in Chiral Limit
- QCD coupling $\alpha_{s}\left(Q^{2}\right)$ in non-perturbative domain

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## AdS/QCD

Soft-Wall Model

$$
e^{\varphi(z)}=e^{+\kappa^{2} z^{2}}
$$

$$
\left[-\frac{d^{2}}{d \zeta^{2}}-\frac{1-4 L^{2}}{4 \zeta^{2}}+U(\zeta)\right] \psi(\zeta)=M^{2} \psi(\zeta)
$$

Light-Front Schrödinger Equation

$$
U(\zeta)=\kappa^{4} \zeta^{2}+2 \kappa^{2}(L+S-1)
$$

Single variable $\zeta$

Unique
Confinement Potential!
Conformal symmetry of the action

## Confinement scale: $\kappa \simeq 0.5 \mathrm{GeV}$

- de Alfaro, Fubini, Furlan:
- Fubini, Rabinovici:

Scale can appear in Hamiltonian and EQM without affecting conformal invariance of action!

GeV units external to QCD: Only Ratios of Masses Determined

## Meson Spectrum in Soft Wall Model

## Massless pion!

$$
m_{\pi}=0 \text { if } m_{q}=0
$$

Pion: Negative term for $J=0$ cancels positive terms from $L F K E$ and potential

- Effective potential: $U\left(\zeta^{2}\right)=\kappa^{4} \zeta^{2}+2 \kappa^{2}(J-1)$
- LF WE

$$
\left(-\frac{d^{2}}{d \zeta^{2}}-\frac{1-4 L^{2}}{4 \zeta^{2}}+\kappa^{4} \zeta^{2}+2 \kappa^{2}(J-1)\right) \phi_{J}(\zeta)=M^{2} \phi_{J}(\zeta)
$$

- Normalized eigenfunctions $\langle\phi \mid \phi\rangle=\int d \zeta \phi^{2}(z)^{2}=1$

$$
\phi_{n, L}(\zeta)=\kappa^{1+L} \sqrt{\frac{2 n!}{(n+L)!}} \zeta^{1 / 2+L} e^{-\kappa^{2} \zeta^{2} / 2} L_{n}^{L}\left(\kappa^{2} \zeta^{2}\right)
$$

- Eigenvalues

$$
\mathcal{M}_{n, J, L}^{2}=4 \kappa^{2}\left(n+\frac{J+L}{2}\right)
$$

$$
\vec{\zeta}^{2}=\vec{b}_{\perp}^{2} x(1-x)
$$

G. de Teramond, H. G. Dosch, sjb

## Bound States in Relativistic Quantum Field Theory:

Light-Front Wavefunctions
Dirac's Front Form: Fixed $\tau=t+z / c$
Fixed $\tau=t+z / c$

$$
\psi\left(x_{i},{\overrightarrow{k_{\perp}}}_{i}, \lambda_{i}\right)_{x=\frac{k^{+}}{P^{+}}=\frac{k^{0}+k^{3}}{P^{0}+P^{3}}}
$$

Invariant under boosts. Independent of $P^{\boldsymbol{\mu}}$

$$
\mathrm{H}_{L F}^{Q C D}\left|\psi>=M^{2}\right| \psi>
$$

Direct connection to QCD Lagrangian Off-shell in invariant mass

Remarkable new insights from AdS/CFT, the duality between conformal field theory and Anti-de Sitter Space

Prediction from AdS/QCD: Meson LFWF

$$
e^{\varphi(z)}=e^{+\kappa^{2} z}
$$

$x$

$$
0.80 .6^{0.40 .2}
$$

$$
\psi_{M}\left(x, k_{\perp}^{2}\right)^{0}
$$

Note coupling

$$
k_{\perp}^{2}, x
$$

de Teramond, Cao, sjb
"Soft Wall" model

massless quarks

$$
\psi_{M}\left(x, k_{\perp}\right)=\frac{4 \pi}{\kappa \sqrt{x(1-x)}} e^{-\frac{k^{2}}{2 \kappa^{2} x(1-x)}} \quad \phi_{\pi}(x)=\frac{4}{\sqrt{3} \pi} f_{\pi} \sqrt{x(1-x)}
$$

$$
f_{\pi}=\sqrt{P_{q q}} \frac{\sqrt{3}}{8} \kappa=92.4 \mathrm{MeV} \quad \text { Same as DSE! c. D. Roberts et al. }
$$

Provides Connection of Confinement to Hadron Structure

## AdS/QCD Holographic Wave Function for the $\rho$ Meson

 and Diffractive $\rho$ Meson Electroproduction

## Spacelike Paulí Form Factor

From overlap of $L=1$ and $L=0$ LFWFs


Using $S U(6)$ flavor symmetry and normalization to static quantities



Comparison for $x q(x)$ in the proton from LFHQCD (red bands) and global fits: MMHT2014 (blue bands) [5], CT14 [6] (cyan bands), and NNPDF3.0 (gray bands) [77]. LFHQCD results are evolved from the initial scale $\mu_{0}=1.06 \pm 0.15 \mathrm{GeV}$.

Universality of Generalized Parton Distributions in Light-Front Holographic QCD
Guy F. de Téramond, Tianbo Liu, Raza Sabbir Sufian, Hans Günter Dosch, Stanley J. Brodsky, and Alexandre Deur PHYSICAL REVIEW LETTERS 120, 182001 (2018)


Helicity asymmetries of $u(x)+\bar{u}(x)$ and $d(x)+\bar{d}(x)$ compared with measurements.

Guy F. de Téramond, Tianbo Liu, Raza Sabbir Sufian, Hans Günter Dosch, Stanley J. Brodsky, and Alexandre Deur

## Bjorken sum rule defines effective charge $\alpha_{g 1}\left(Q^{2}\right)$

$$
\int_{0}^{1} d x\left[g_{1}^{e p}\left(x, Q^{2}\right)-g_{1}^{e n}\left(x, Q^{2}\right)\right] \equiv \frac{g_{a}}{6}\left[1-\frac{\alpha_{g 1}\left(Q^{2}\right)}{\pi}\right]
$$

- Can be used as standard QCD coupling
- Well measured
- Asymptotic freedom at large $\mathbf{Q}^{\mathbf{2}}$
- Computable at large $\mathbf{Q}^{\mathbf{2}}$ in any pQCD scheme
- Universal $\boldsymbol{\beta}_{0}, \boldsymbol{\beta}_{\text {I }}$


## Analytic, defined at all scales, IR Fixed Point



AdS/QCD dilaton captures the higher twist corrections to effective charges for $\mathbf{Q}<\mathbf{I} \mathbf{G e V}$

$$
e^{\varphi}=e^{+\kappa^{2} z^{2}}
$$

Deur, de Teramond, sjb
$m_{\rho}=\sqrt{2} \kappa$ $m_{p}=2 \kappa$

## All-Scale QCD Coupling

Deur, de Tèramond, sjb Fit to $\mathrm{Bj}+\mathrm{DHG}$ Sum Rules:


## Light-Front Holography: First Approximation to QCD

- Color Confinement, Analytic form of confinement potential
- Retains underlying conformal properties of QCD despite mass scale (DeAlfaro-Fubini-Furlan Principle)
- Massless quark-antiquark pion bound state in chiral limit, GMOR
- QCD coupling at all scales
- Connection of perturbative and nonperturbative mass scales
- Poincarè Invariant
- Hadron Spectroscopy-Regge Trajectories with universal slopes in n, L
- Supersymmetric 4-Plet: Meson-Baryon -Tetraquark Symmetry
- Light-Front Wavefunctions
- Form Factors, Structure Functions, Hadronic Observables
- OPE: Constituent Counting Rules
- Hadronization at the Amplitude Level: Many Phenomenological Tests
- Systematically improvable: Basis LF Quantization (BLFQ)

> Novel High-Energy Electron-Proton Collider Physics at the LHeC

- Testing a New Approach to Color Confinement, Hadron Spectroscopy, Light-Front Dynamics: Light-Front Holographic QCD
- Exotic Hadron Production
- Ridge Production from Flux Tube Collisions: Novel Azimuthat Correlations
- Hadronization at the Amplitude Level
- Heavy Quark and Flavor Dynamics: Intrinsic Distributions
- Novel Nuclear Structure Phenomena: Breakdown of Sum Rules for Nuclear PDFs, Flawor-Dependent Antishadowing, Hidden Color, Color Transparency,
- Violation of Factorization Theorems: Initial EFFinal-State Interactions, Novel Spín Phenomena
- Elimination of Scale Ambiguities:Princíple of Maximum Conformality


## Novel Physics Opportunities at the LHeC


(10)

