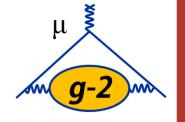


INO-CNR Istituto Nazionale di Ottica



#### The muon g-2 Experiment



Carlo Ferrari CNR-INO & INFN Italy & CERN

on behalf of the g-2 collaboration

IPA2022, Vienna 8 September 2022

Istituto Nazionale di Fisica Nucleare



www.ino.cnr.it

### The muon g-2 Experiment at Fermilab

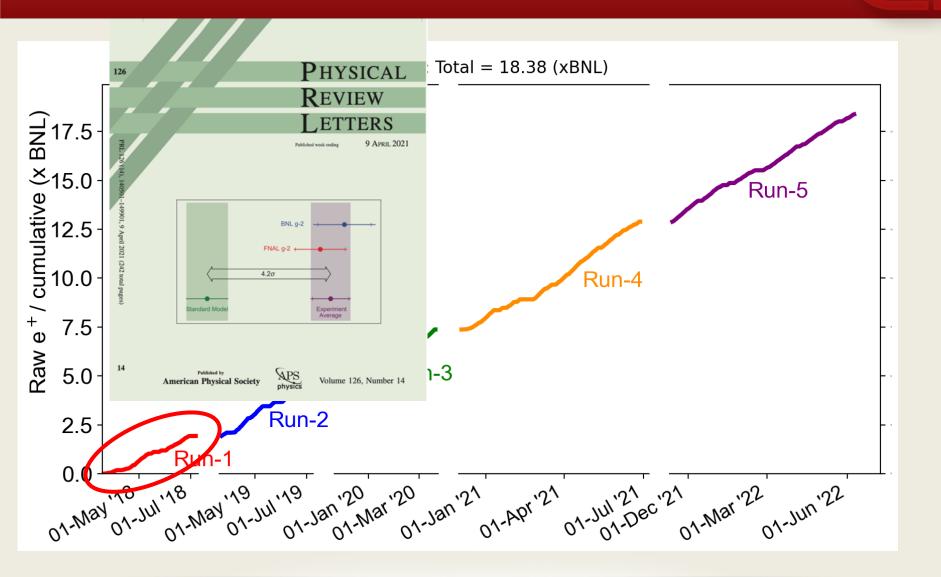


- Low energy, high Intensity experiment
- Small scale detectors and collaborations, very high statistics
- Precision measurements, looking for deviations from theory

Outline:

- Brief introduction to a<sub>u</sub>
- Experiment description
- Calculating the a<sub>u</sub>
- Status and outlook

### The data



### 1948: Triumph of QED

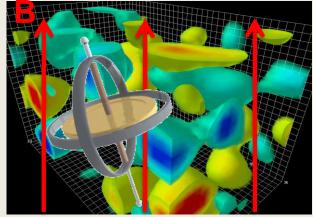
g is the proportionality factor between spin and magnetic moment for particle p:

- Classical physics: g = 1
- Relativistic quantum mechanics prediction for a point-like particle (Dirac, 1928): g = 2
- For electron, experimentally found to be (Foley & Kush, 1948): g<sub>e</sub> = 2.00119(5)
- Schwinger figured out why: QED

$$a = \frac{(g-2)}{2} = \frac{\partial}{2\rho} = 0.001161$$

$$\overrightarrow{\mu_p} = -g_p \frac{e}{2m_p} \vec{S}$$

Image Credits: Derek Leinweber



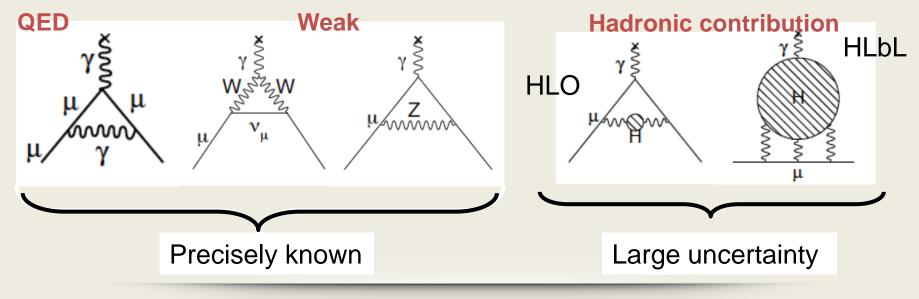


### 1948: Triumph of Quantum Field Theory

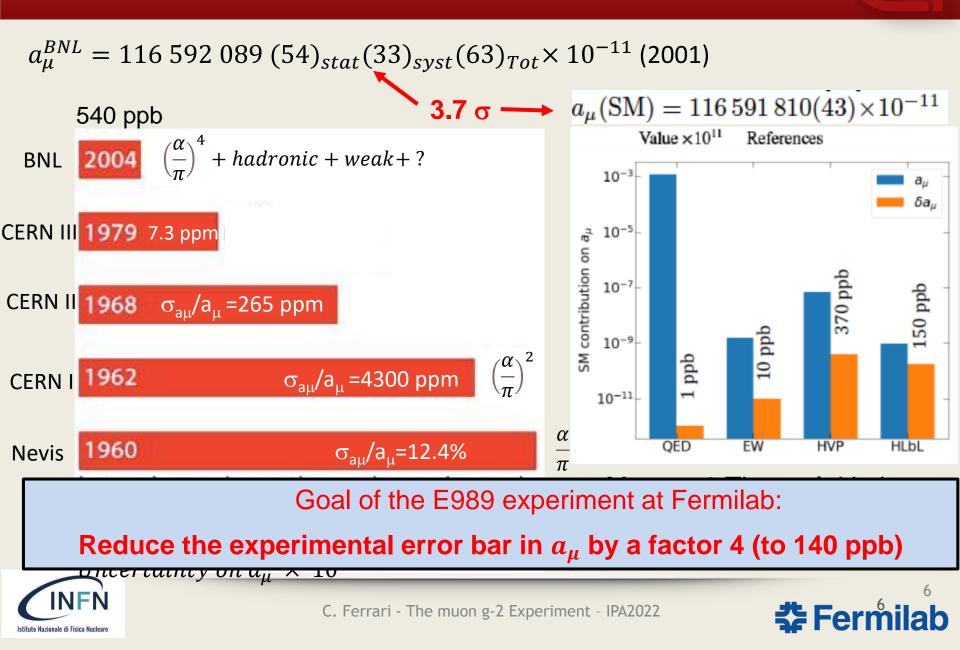
#### g<sub>e,meas</sub> = 2.00231930436182(52) [0.25 ppt]

The most precise prediction ever confirmed by experiment [Rev.Mod. Phys. 88, 035009] Weak and hadronic interaction have small impact on the ge result

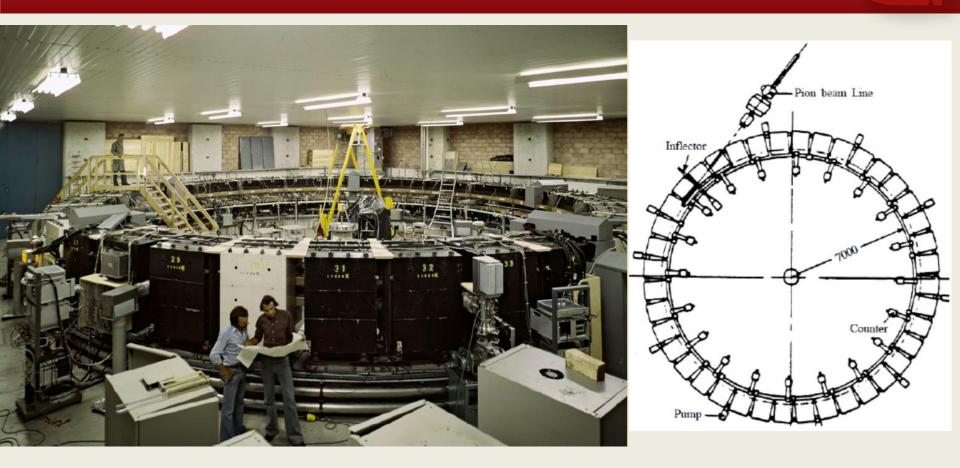
Muons: most interactions are proportional to  $(m_{\mu} / m_{e})^{2} \approx 43.000$  $a_{\mu}$  is a better probe for new physics



### Muon g-2 experiments



### g-2 muon experiment at CERN (CERN III)



Pions injection, magic momentum, vertical confinement with E field

 $a_{\mu} = 1.165.924 \,(8.5) \times 10^{-9} \,(7 \,\mathrm{ppm}).$ 



C. Ferrari - The muon g-2 Experiment - IPA2022



### g-2 muon experiment at Brookhaven (2000's)

Muons injection, magic momentum, vertical confinement with E field

 $a_{\mu}^{BNL} = 116\ 592\ 089\ (54)_{stat}(33)_{syst}(63)_{Tot} \times 10^{-11}$ 

Nazionale di Fisica Nuclear

C. Ferrari - The muon g-2 Experiment - IPA2022

**Fermilab** 

### The Big Move of the Ring (2013)

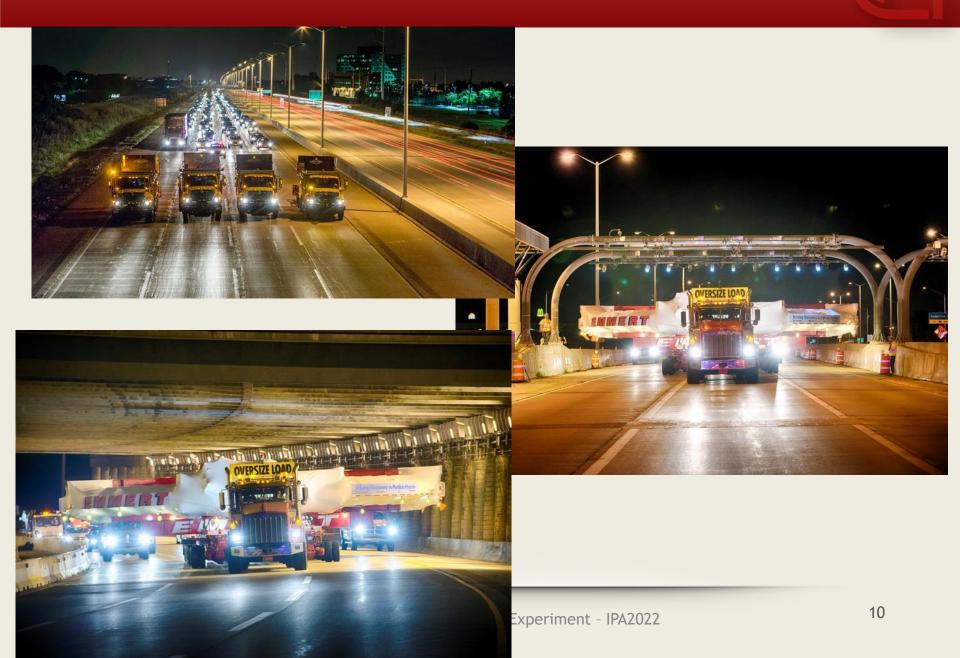








### Including 30 miles of Chicago suburbs



### Photos

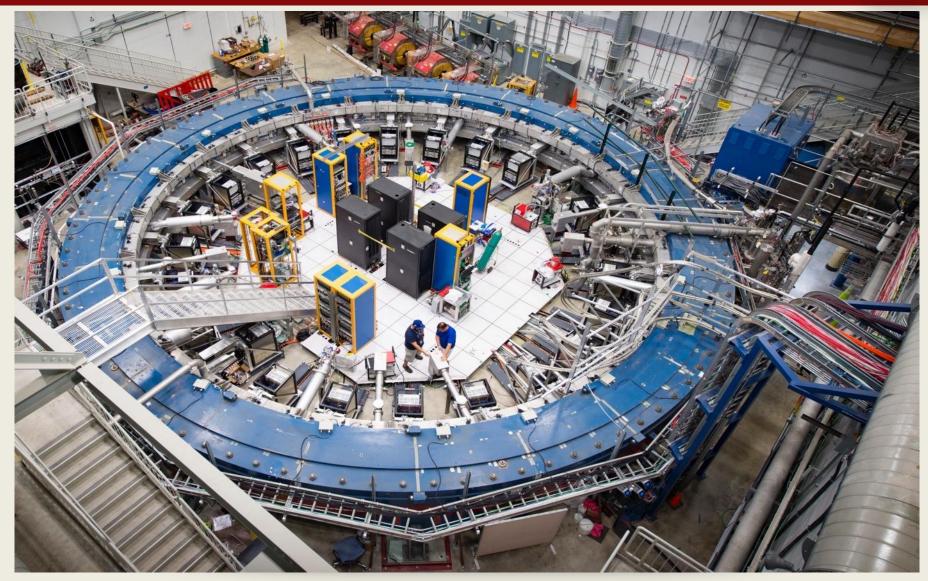








### Muon g-2 Storage Ring at Fermilab



### Key ingredients

1) Polarized muons (parity violation in weak decays)  $\nu \leftrightarrow \pi^+ \leftrightarrow \mu^+$ ~97% polarized for forward decay

 $a_{\mu} = \left(\frac{m}{2}\right)$ 

Time (µs) modulo 100 µs

2) Anomalous precession in a B field, proportional to (g-2)

Measure 2 quantities

3)  $P_m$  magic momentum = 3.09 GeV/c

$$\bar{\omega}_a = \frac{e}{mc} \left[ a_{\mu} \bar{B} - \left( a_{\mu} - \frac{1}{\gamma^2 - 1} \right) \bar{\beta} \times \bar{E} \right]$$

#### *E* field doesn't affect muon spin when $\gamma = 29.3$

 $=\omega_{spin}-\omega_{cyclotron}=$ 

 High energy decay e<sup>+</sup> are emitted preferably in spin direction of the muon

$$\mu^+ \rightarrow e^+ \nu_e \overline{\nu}_\mu$$

#### E821 at Brookhaven

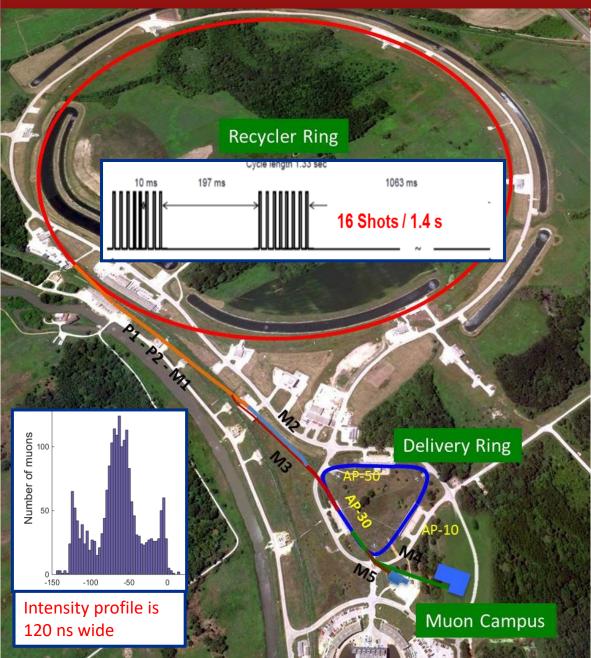
$$\begin{array}{l} \sigma_{\text{stat}} = \pm \ 460 \ \text{ppb} \\ \sigma_{\text{syst}} = \pm \ 280 \ \text{ppb} \end{array} \right\} \sigma = \pm \ 540 \ \text{ppb} \ \end{array}$$

E989 at Fermilab

$$\begin{array}{l} \sigma_{stat} = \pm \ 100 \ ppb \\ \sigma_{syst} = \pm \ 100 \ ppb \end{array} \right\} \sigma = \pm \ 140 \ ppb \ \end{array}$$

- More statistic (positrons x21)
- Improved beam (much less hadronic contamination)
- Improved detectors (segmented calorimeters, SiPM, trackers)
- Laser calibration system (SiPMs gain changes at 1 part in 10<sup>4</sup>)
- 800 MHz waveform digitizers sample (twice the rate BNL)
- Simulation tools (Ringsim, GEANT4, COSY, BMAD)
- Magnetic field measurement

### **Muon beam production**



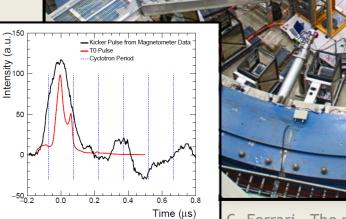
- 10<sup>12</sup> protons per pulse (~ 9 GeV) batch into Recycler Ring
- hit the production target
- Pion production
- Pion decay to Muons:  $\pi^+ \rightarrow \mu^+ \nu_\mu$
- p/π/m beam enters DR;
   protons kicked out
- Fermilab's Muon
   Campus beamlines
   transport ~ 3.1 GeV/c
   muons to storage ring
- μ enter storage ring and decay to e<sup>+</sup>, 700 μs fill, at 15 Hz



**3 Magnetic kickers** 

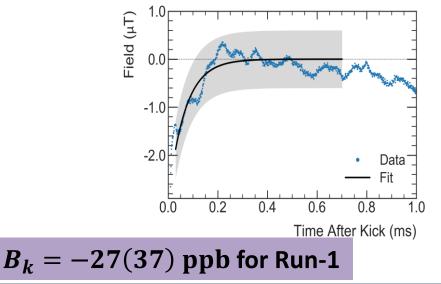


Kickers aim to align muons with storage region (11 mrad deflection) Off after the first turn (< 149 ns) Run1 = 125-142 kV, 220 G (-> 165 kV)

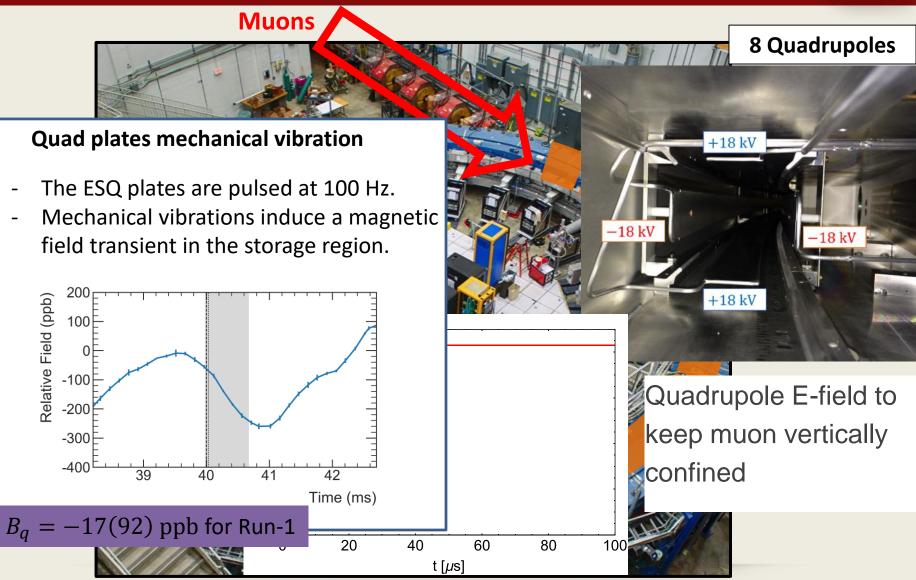


#### **Kicker transient field**

- Fast kicker pulses impedance mismatch induces Eddy currents.
- Faraday magnetometer using fibers measured the kicker transient field (laser polarization rotates in TGG crystal in presence of the magnetic field).



C. Ferrari - The muon g-2 Experiment - IPA2022

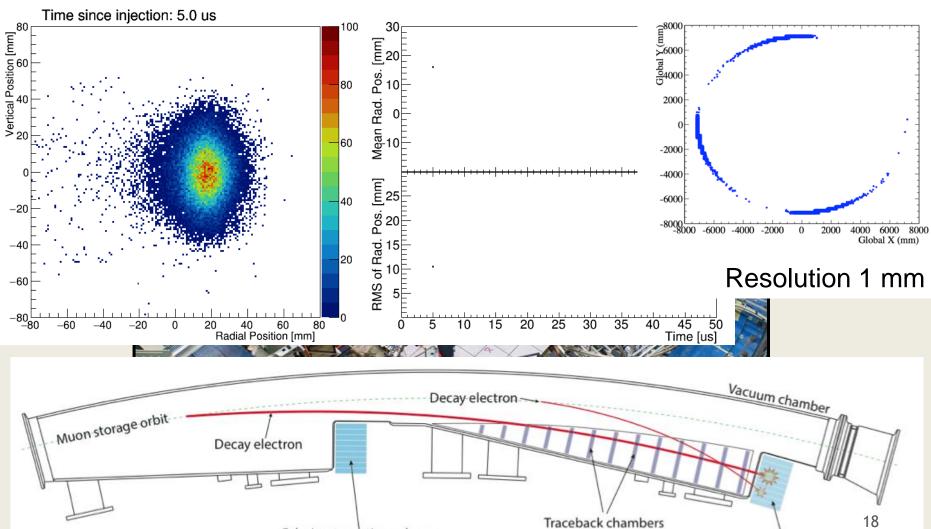


C. Ferrari - The muon g-2 Experiment - IPA2022

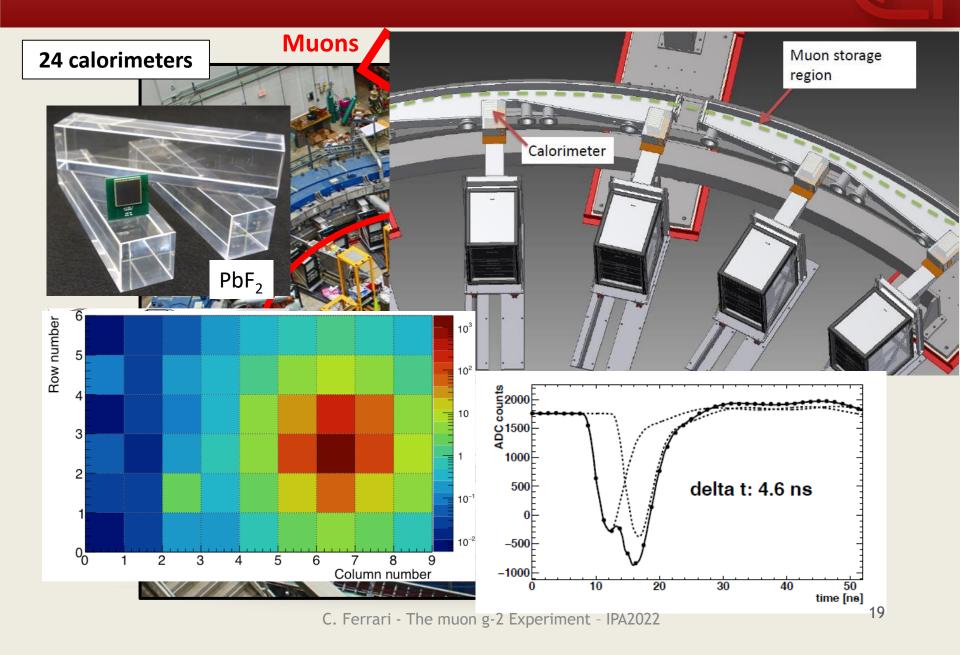
2 Trackers

Muons

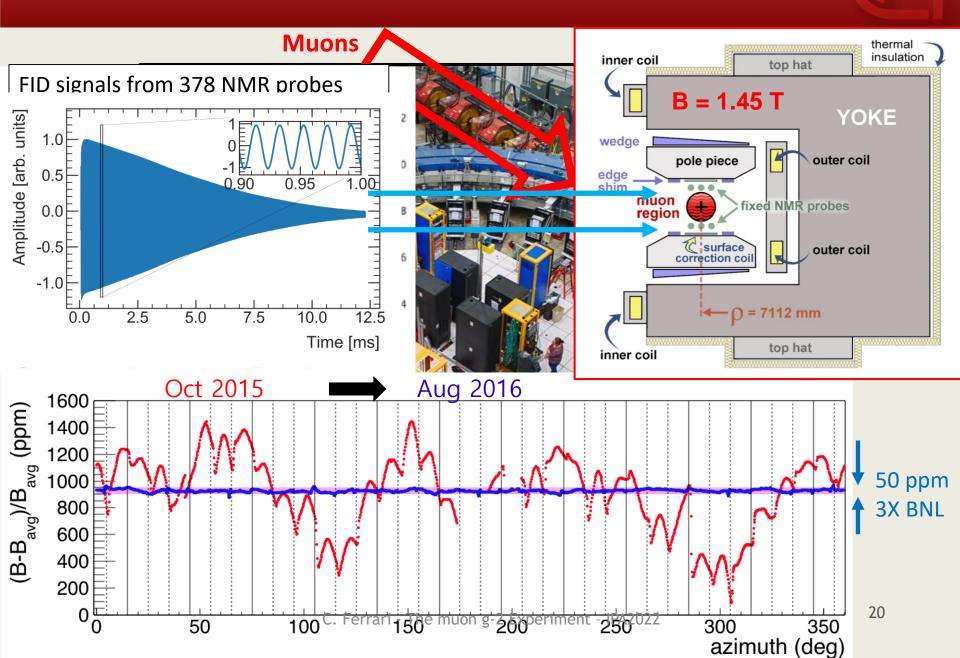
Calorimeter active volume



hambers Calorimeter active volume

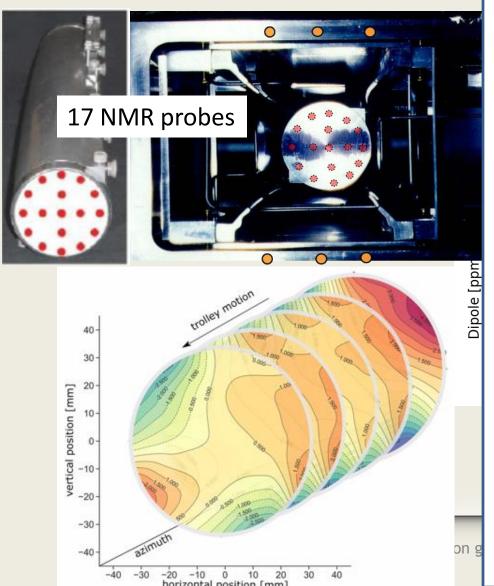


### The magnet

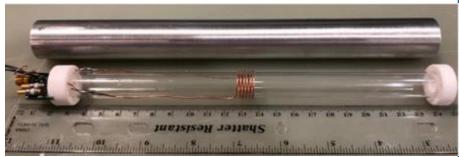


### The NMR probes calibration

#### NMR trolley maps field every 3 days



#### Trolley absolute calibration: plunging probe with water sample



#### Absolute probes all crosscalibrated at the ANL test magnet





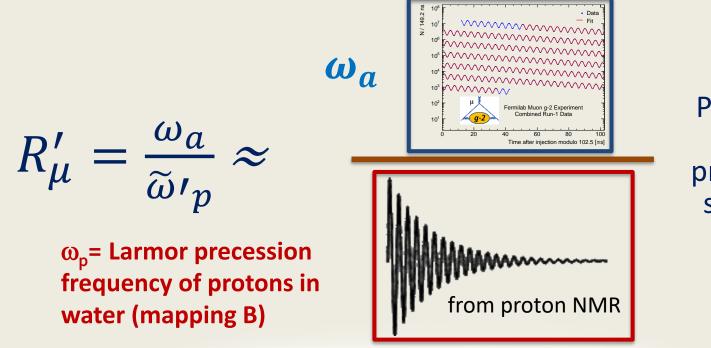
Consistent with BNL probe to 6<sup>1</sup>ppb and with new <sup>3</sup>He probe to 38 ppb

### The magnetic anomaly $a_{\mu} = (g - 2)/2$

$$a_{\mu} = \underbrace{\frac{\omega_a}{\tilde{\omega}_p'(T, T_r)}}_{\mu_e(H)} \frac{\mu_p'(T_r)}{\mu_e(H)} \frac{\mu_e(H)}{\mu_e} \frac{m_{\mu}}{m_e} \frac{g_e}{2}$$

**Measured quantities** 

External data, total uncertainties: 25 ppb



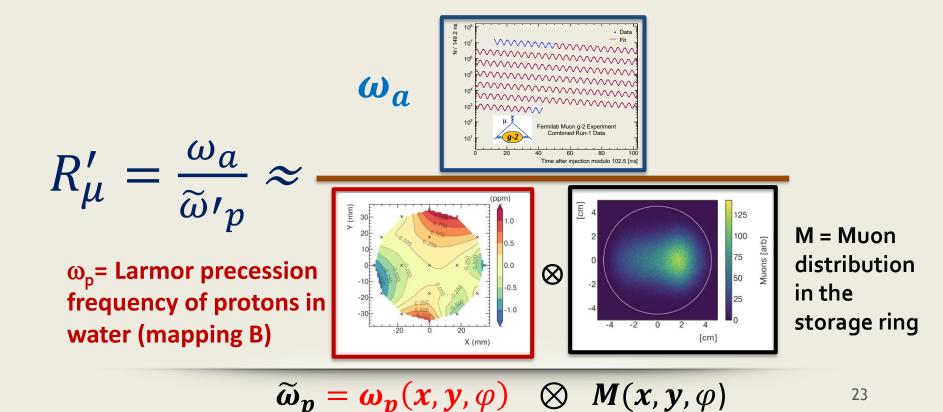
Precession of muons and protons in the same B field

### The magnetic anomaly $a_{\mu} = (g - 2)/2$

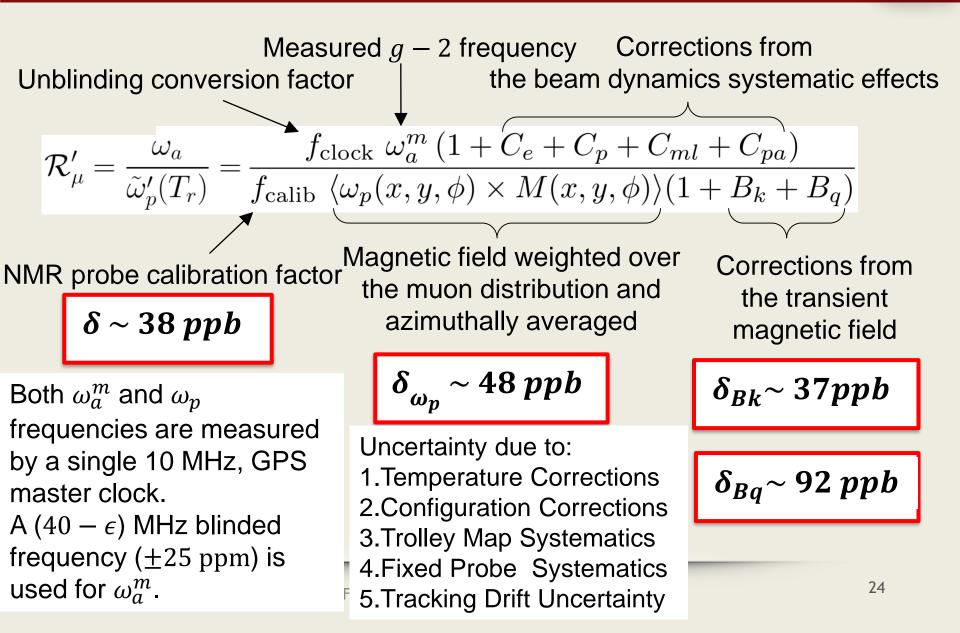
$$a_{\mu} = \underbrace{\frac{\omega_a}{\tilde{\omega}'_p(T, T_r)}}_{\mu_e(H)} \frac{\mu'_p(T_r)}{\mu_e(H)} \frac{\mu_e(H)}{\mu_e} \frac{m_{\mu}}{m_e} \frac{g_e}{2}$$

**Measured quantities** 





### The master formula



## The $\omega_a^m$ analysis strategy

- 6 independent analysis groups using different Reconstruction algorithms and different Fit methods
- Q-method is completely different from all others: it has a larger error → used as crosscheck
- 2 Independent Reconstruction algorithms developed (East, West)

Team	Reconstruction	Analysis
CU (Cornell)	East	Т, Е
UW (Washington)	West	Т, А
Europa (INFN+UK)	West/Europa	Т, А
SJTU (Shangai)	West	Т, Е
BU (Boston)	West	T, R
Uky (Kentucky)	Q	Q

T-method: count all positrons with E>1.7GeV and plot them vs time to get the *«Wiggle plot»*; reference method

E-method (Energy binned): fit each energy slice, combine the resulting values for  $\omega_{\text{a}}$ 

**A-method** (Asimmetry weighted): weight each event with its own contribution to asimmetry A(E). From the statistical point of view, this method uses most information.

**Ratio method**: randomly split dataset in 2 subsets shifted by ±half a g-2 period, build combinations of the 2 subsets which eliminates the exponential behavior and leaves just a sinusoidal term

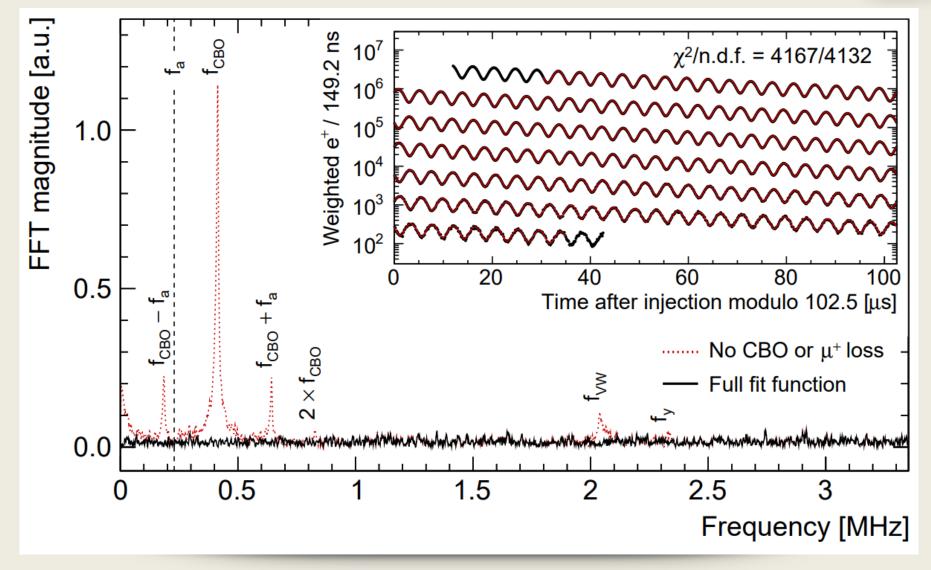
**Q method** No clustering: just integrate energy above threshold. The total energy per event fluctuates with  $\omega_a$  frequency

### The $\omega_a^m$ fit equation (22 parameters)

$$\begin{split} N_{0} e^{-\frac{t}{\tau \tau}} \left(1 + A \cdot A_{BO}(t) \cos(\omega_{a} t + \phi \cdot \phi_{BO}(t))\right) \cdot N_{\text{CBO}}(t) \cdot N_{\text{VW}}(t) \cdot N_{y}(t) \cdot N_{2\text{CBO}}(t) \cdot J(t) \\ A_{\text{BO}}(t) &= 1 + A_{A} \cos(\omega_{\text{CBO}}(t) + \phi_{A}) e^{-\frac{t}{\tau \text{CBO}}} \\ \phi_{\text{BO}}(t) &= 1 + A_{\phi} \cos(\omega_{\text{CBO}}(t) + \phi_{\phi}) e^{-\frac{t}{\tau \text{CBO}}} \\ N_{\text{CBO}}(t) &= 1 + A_{\text{CBO}} \cos(\omega_{\text{CBO}}(t) + \phi_{\text{CBO}}) e^{-\frac{t}{\tau \text{CBO}}} \\ N_{2\text{CBO}}(t) &= 1 + A_{2\text{CBO}} \cos(2\omega_{\text{CBO}}(t) + \phi_{2\text{CBO}}) e^{-\frac{t}{\tau \text{CBO}}} \\ N_{2\text{CBO}}(t) &= 1 + A_{2\text{CBO}} \cos(2\omega_{\text{CBO}}(t) + \phi_{2\text{CBO}}) e^{-\frac{t}{\tau \text{VW}}} \\ \text{Red} &= \text{free parameters} \\ \text{Blue= fixed parameters} \\ Blue &= \text{fixed parameters} \\ J(t) &= 1 + A_{y} \cos(\omega_{y}(t)t + \phi_{y}) e^{-\frac{t}{\tau y}} \\ J(t) &= 1 - k_{LM} \int_{t_{0}}^{t} \Lambda(t) dt \qquad \text{Muon Loss term} \\ \omega_{\text{CBO}}(t) &= \omega_{0}t + A e^{-\frac{t}{\tau A}} + B e^{-\frac{t}{\tau B}} \\ \omega_{y}(t) &= F \omega_{\text{CBO}(t)} \sqrt{2\omega_{c}/F \omega_{\text{CBO}}(t) - 1} \\ \omega_{\text{VW}}(t) &= \omega_{c} - 2\omega_{y}(t) \end{split}$$

 $\omega_{\text{y}},\,\omega_{\text{vw}}$  vertical oscillations  $\omega_{CBO,}\,\omega_{2CBO,}\,$  radial oscillation

### The $\omega_a^m$ fit equation: residuals



### The $\omega_a^m$ Run 1 results

- First beam injected into ring on May 31, 2017
- Run 1 (FY18): Total statistics = 8.2B e<sup>+</sup> ~ 1.2 x BNL
- Conditions not stable, fragmented data sets taken in different Quad and Kicker conditions, while optimizing Storage Ring operations

T. ALBAHRI et al.

PHYS. REV. D 103, 072002 (2021)

Run-1 dataset	1a	1b	1c	1d
$\omega_a^m/2\pi \ (\mathrm{s}^{-1})$	229 080.957	229 081.274	229 081.134	229 081.123
$\Delta \left( \omega_a^m / 2\pi \right) (\mathrm{s}^{-1})$	0.277	0.235	0.189	0.155
Statistical uncertainty (ppb)	1207	1022	823	675
Gain changes (ppb)	<ul> <li>434 ppb statistical uncertainty (compare to 460 ppb for BNL)</li> <li>56 ppb systematic uncertainty</li> </ul>			
Pileup (ppb) CBO (ppb) Time randomization (ppb) Early-to-late effect (ppb)	4 (Co	ompare to 4	60 ppb for E	BNL)
CBO (ppb) Time randomization (ppb)	4 (Co	ompare to 4	60 ppb for E	BNL)

TABLE VII. The combination result for each dataset when using a staged approach.

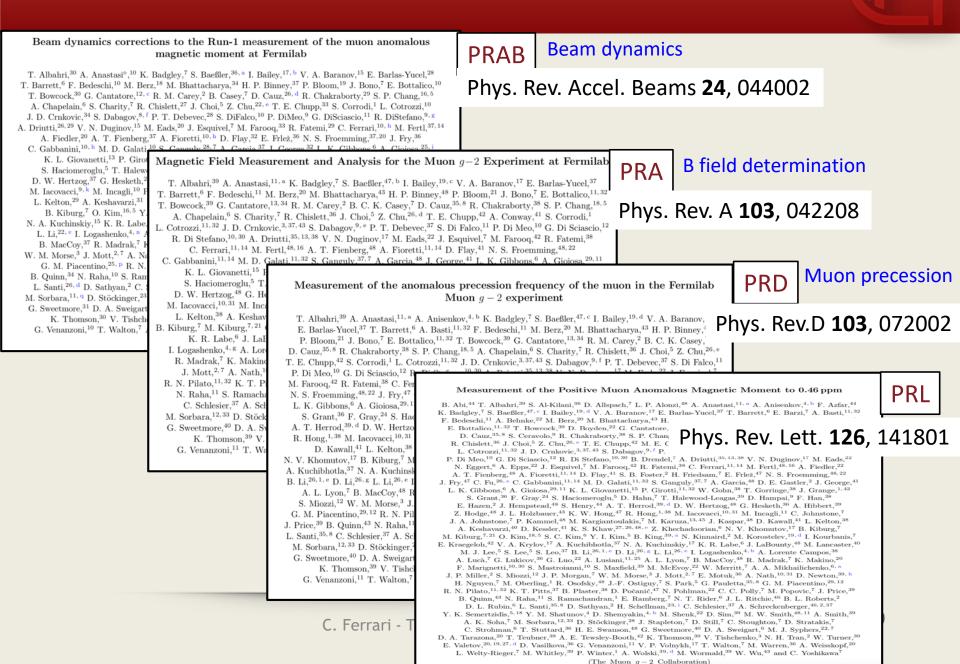
C. Ferrari - The muon g-2 Experiment - IPA2022

# The $a_{\mu}$ Run 1 results

Taking into account	the other corrections: $a_{\mu}(FN)$	$AL) = 116592040(54) \times$	$10^{-11}$
	Quantity	Correction Terms Une	certainty
		(ppb)	(ppb)
	$\omega_a$ (statistical)	_	434
	$\omega_a$ (systematic)	_	56
E-field correction	$C_e$	489	53
Pitch correction	$C_p$	180	13
Muon loss	$C_{ml}$	-11	5
Phase-Acceptance	$C_{pa}$	-158	75
·	$f_{calib}\langle \omega_p'(x,y,\phi) \times M(x,y,\phi) \rangle$	)) –	56
	$B_q$	-17	92
•	$B_k$	-27	37
Enhanced by the	$\mu_{p}'(34.7^{\circ})/\mu_{e}$	_	10
Run 1 conditions	$m_{\mu}/m_e$	_	22
	$g_e/2$	_	0
	Total	_	462

#### 434 ppb stat ⊕ 157 ppb syst error

### References



### Comparison with theory

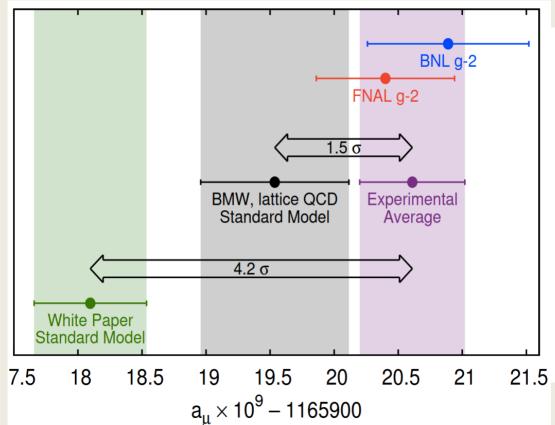
Combining BNL/FNAL and comparing to e+e- based theory by the Theory Initiative  $\rightarrow$  4.2 $\sigma$  tension with the SM

Lattice QCD (blue band) are becoming competitive

Recent evaluation(s) of HVP from lattice (BMW20) in tension with the  $e^+e^-$  evaluation (WP20), at  $2\sigma$ 

Data-driven evaluation (R-ratio) on firm ground. Unlikely to be wrong...

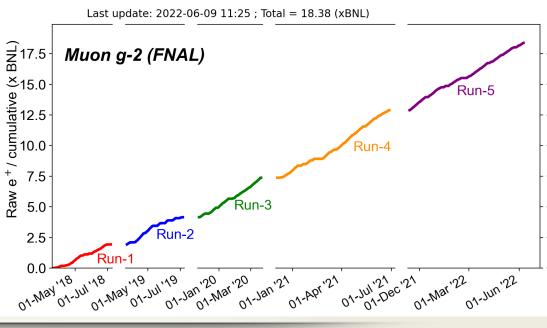
New experiment: MUonE



### Conclusion

- We have determined  $a_{\mu}$  to an unprecedented 460 ppb precision
- The Run 1 result  $a_{\mu}(\text{FNAL}) = 116\,592\,040(54) \times 10^{-11}$ 
  - 6% of ultimate data sample
  - confirm the BNL experimental results
  - 15% smaller error than BNL
  - 3.3 $\sigma$  tension with e+e- SM
- Next year release of Run 2&3
- Analysis of Run 4&5 ongoing
- Run 6 (opportunistic) approved
- New experiment: J-PARC

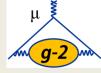
#### We have collected ~19 x BNL over the last 5 years







### The g-2 Collaboration (experiment E989)







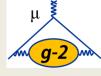
Thank you for your attention

C. Ferrari - The muon g-2 Experiment – IPA2022





**Backup slides** 



# Backup



C. Ferrari - Laser Calibration System for the Muon g-2 experiment at Fermilab

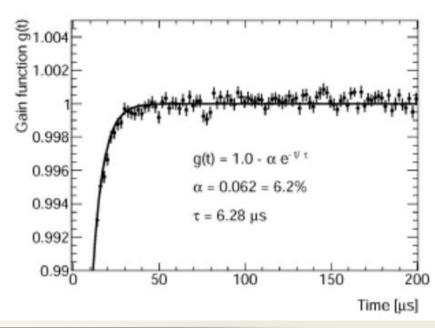


### Laser calibration system

			BNL	FNAL
	Systematic	Improvements	[ppb]	[ppb]
C	Gain changes	Laser gain calibration	120	20
	Pileup	Segmented Čerenkov calorimeter	80	40
	Lost Muons	Beam Collimation	90	20
	Betatron Oscillations	High n value, beamline match	70	<30
	E-field and Pitch	Better tracking, improved simulation	50	30
-	Quadrature sum		180	70

SiPM gain issues:

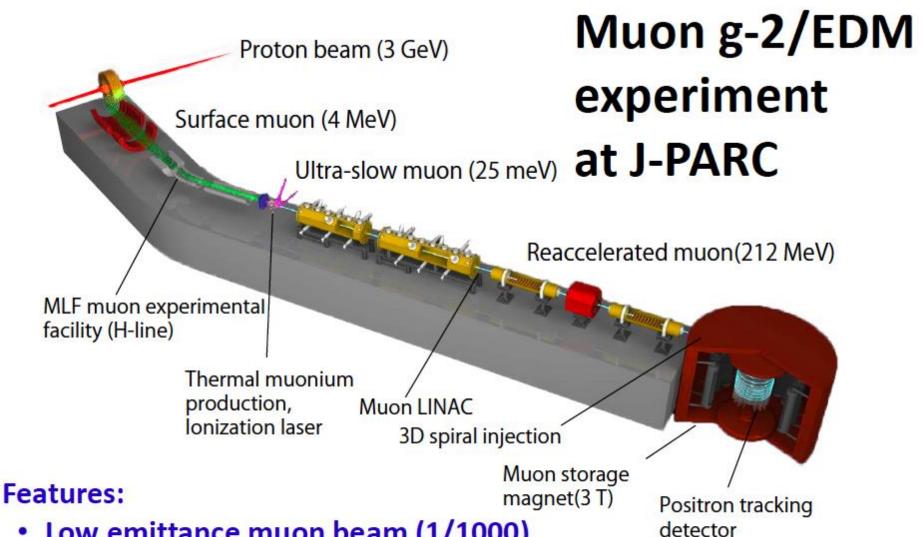
- Gain sag at the beginning of the fill (beam splash) ~ μs
- Pixel recovery after one hit ~ ns
- SiPM aging and temperature/bias voltage slow drift (affect energy threshold)



35

**Ferm** 





- Low emittance muon beam (1/1000)
- No strong focusing (1/1000) & good injection eff. (x10)
- Compact storage ring (1/20)
- Tracking detector with large acceptance
- Completely different from BNL/FNAL method

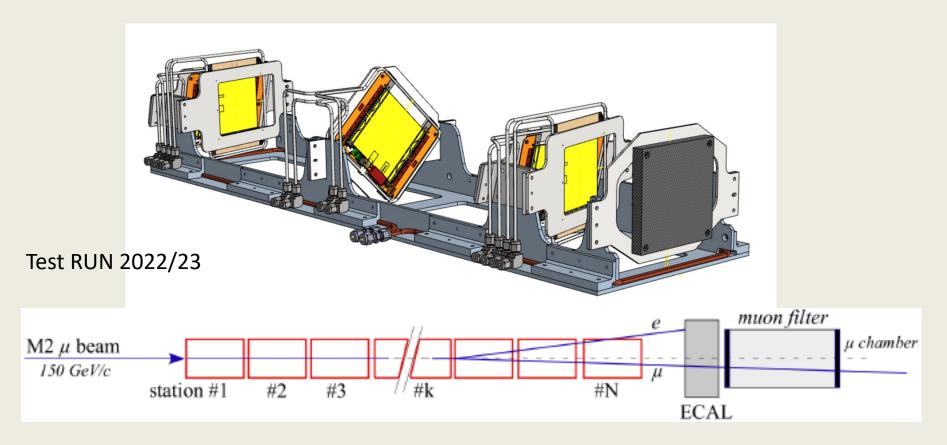
# Comparison of g-2 experiments

Prog. Theor. Exp. Phys. 2019, 053C02 (2019)

	BNL-E821	Fermilab-E989	Our experiment	
	DINL-LO21	Femma0-1.909	Our experiment	
Muon momentum	3.09 GeV/c		300 MeV/c	
Lorentz $\gamma$	29.3		3	
Polarization	100%		50%	
Storage field	B = 1.45  T		B = 3.0  T	
Focusing field	Electric quadrupole		Very weak magnetic	
Cyclotron period	149 ns		7.4 ns	
Spin precession period	$4.37~\mu$	ιs	$2.11 \ \mu s$	
Number of detected $e^+$	$5.0 \times 10^{9}$	$1.6 \times 10^{11}$	$5.7 \times 10^{11}$	
Number of detected $e^-$	$3.6 \times 10^{9}$	_	_	
$a_{\mu}$ precision (stat.)	460 ppb	100 ppb	450 ppb	
(syst.)	280 ppb	100 ppb	<70 ppb	
EDM precision (stat.)	$0.2 imes 10^{-19}~e\cdot{ m cm}$	_	$1.5  imes 10^{-21} \ e \cdot \mathrm{cm}$	
(syst.)	$0.9  imes 10^{-19} e \cdot \mathrm{cm}$	_	$0.36 \times 10^{-21} e \cdot \mathrm{cm}$	

Completed	Running	In preparation
-----------	---------	----------------

#### A third way for HVP...MUonE at CERN



#### Alternative measurement of HVP for $a_{\mu}$

-C. M. Carloni Calame et al PLB 746 (2015) 325 -G. Abbiendi et al Eur.Phys.J.C 77 (2017) 3, 139 -Lol https://cds.cern.ch/record/2677471/files/SPSC-I-252.pdf