

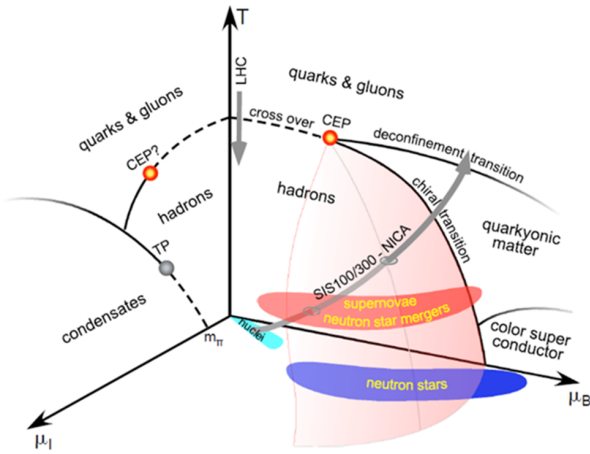
# Anisotropic Flow in Heavy Ion Collisions

Viktor Klochkov



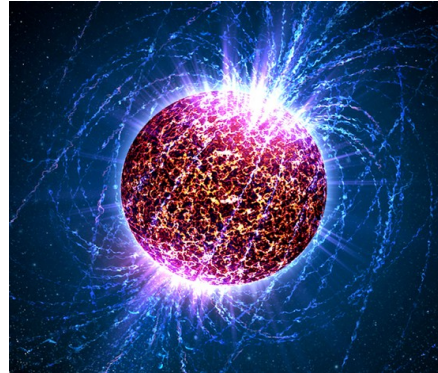
Arbeitstreffen Kernphysik 2020  
Schleching, 28.02

# Dense Baryonic Matter



NUPECC Long Range Plan 2017

## Neutron stars

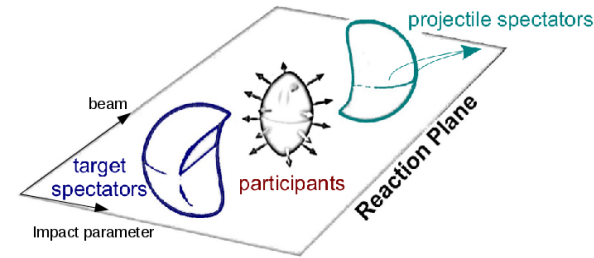


## Neutron star merger



GW170817

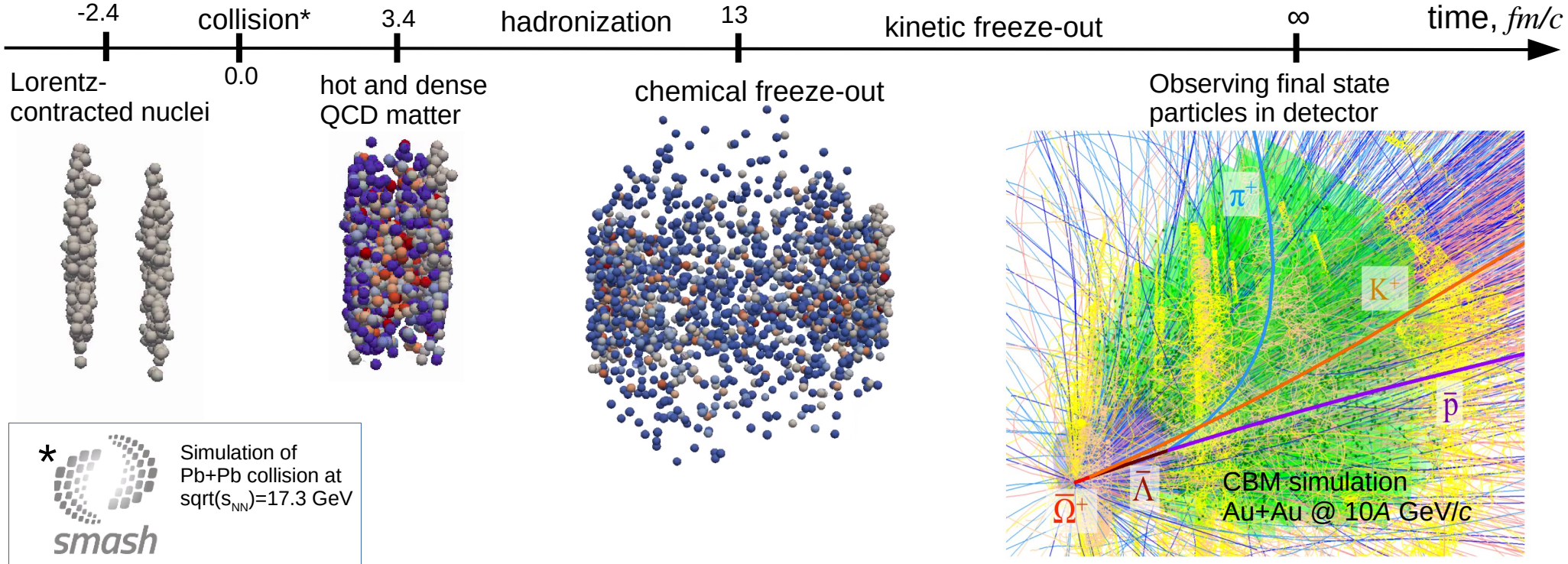
## Heavy-ion collisions



at intermediate energies

Temperature ( $T$ )	$< 10 \text{ MeV}$	$\sim 10\text{-}100 \text{ MeV}$	$< 120\text{-}200 \text{ MeV}$
Density ( $\rho$ )	$< 10 \rho_0$	$< 2\text{-}6 \rho_0$	$< 10 \rho_0$
Lifetime / Reaction time ( $t$ )	$\infty$	$\sim 10 \text{ ms}$	$\sim 10^{-23} \text{ s}$

# Relativistic heavy-ion collision evolution



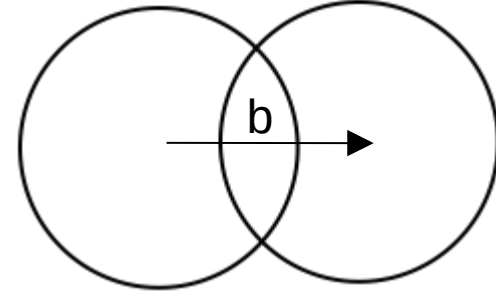
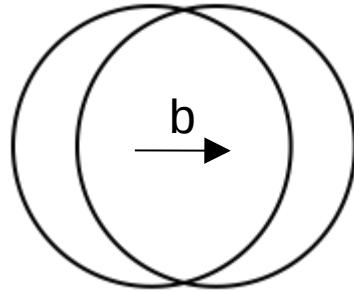
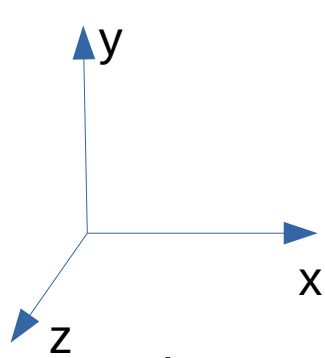
## Experimental challenge at intermediate collision energies:

reconstruct hot and dense QCD matter properties by measuring only final state particles



- Collision geometry and initial state fluctuations
- Interaction with “spectators”
- Medium evolution (equation of state)
- Hadronization and freeze-out

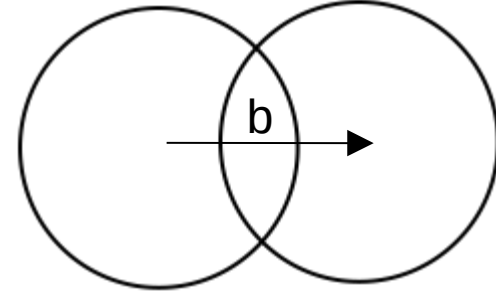
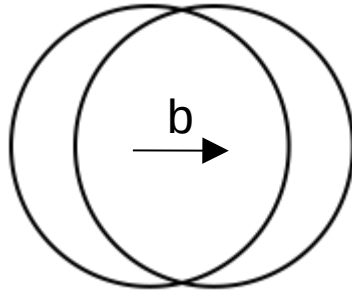
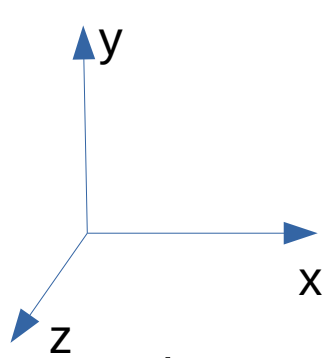
# Collision geometry



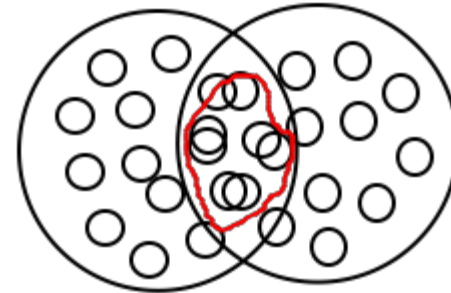
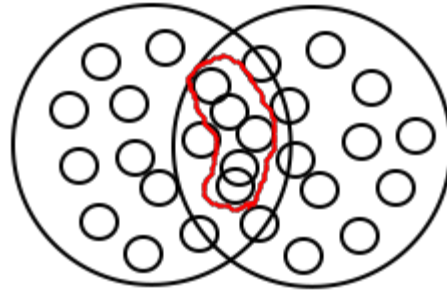
impact parameter  $\leftrightarrow$  energy density of the interacting matter



# Collision geometry

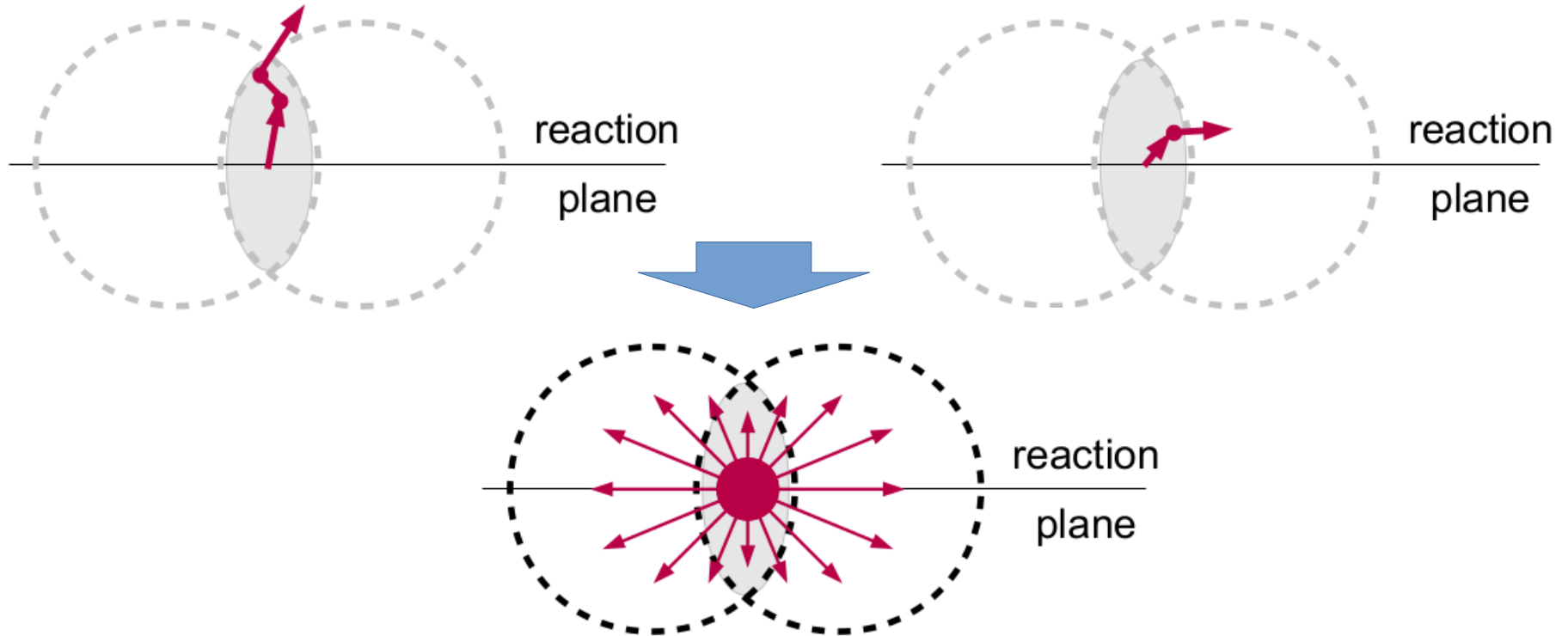


impact parameter  $\leftrightarrow$  energy density of the interacting matter



spatial asymmetry of the overlap region  $\leftrightarrow$  asymmetry of energy distribution

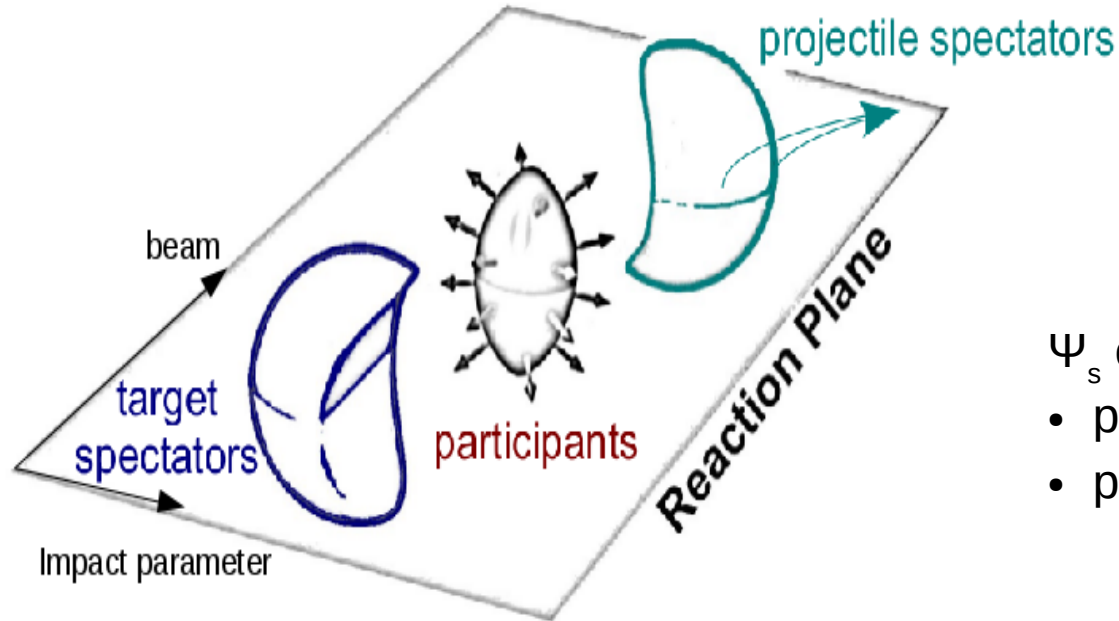
# Anisotropic transverse flow



Asymmetry in initial coordinate space converts due to interaction into final momentum asymmetry with respect to the symmetry plane

# Anisotropic transverse flow

Final state asymmetry is sensitive to the collision evolution and QCD matter properties



$$\rho(\varphi) = \frac{1}{2\pi} \left[ 1 + 2 \sum_{n=1}^{\infty} v_n \cos(n(\varphi - \Psi_s)) \right]$$

$$v_n = \langle \cos(n[\varphi - \Psi_s]) \rangle$$

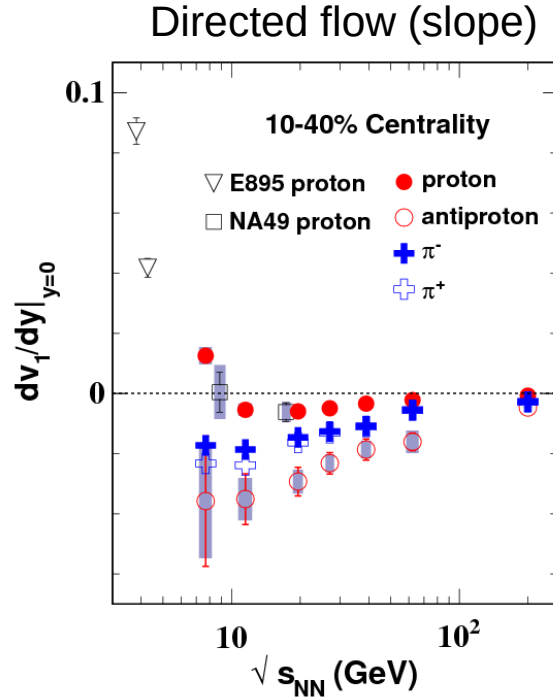
$\Psi_s$  can be estimated from

- produced particles ( $\Psi_{pp}$ )
- projectile (target) spectators  $\Psi_{proj}$  ( $\Psi_{targ}$ )

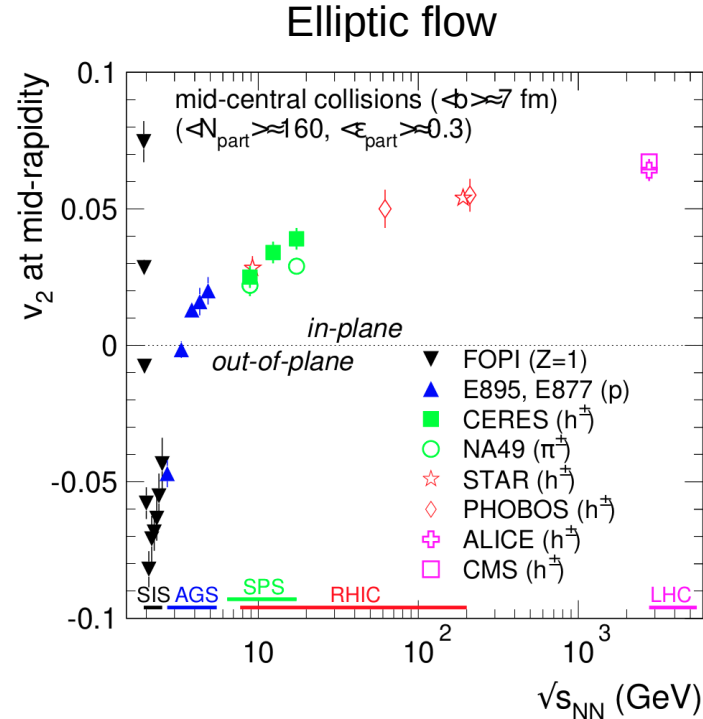
Important to measure flow coefficient relative both to spectators and produced particles symmetry planes

# Collective flow measurements

STAR Collaboration  
PRL 112 (2014) 162301



Non-trivial behavior of directed flow associated with the change of EoS



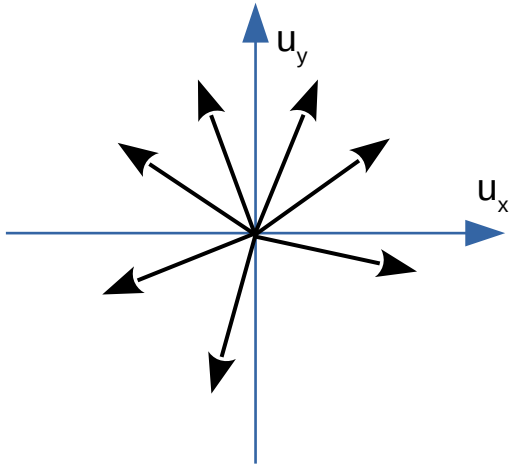
Elliptic flow changes sign (sensitive to collision dynamics)

More results are coming soon at high  $\mu_B$  region from BES-II@RHIC, NA61/SHINE@SPS and in future from CBM@FAIR MPD@NICA, ...

# Flow vectors and event plane angle

u and Q-vectors:

$$\vec{u}_n = \begin{pmatrix} \cos n\varphi \\ \sin n\varphi \end{pmatrix}$$

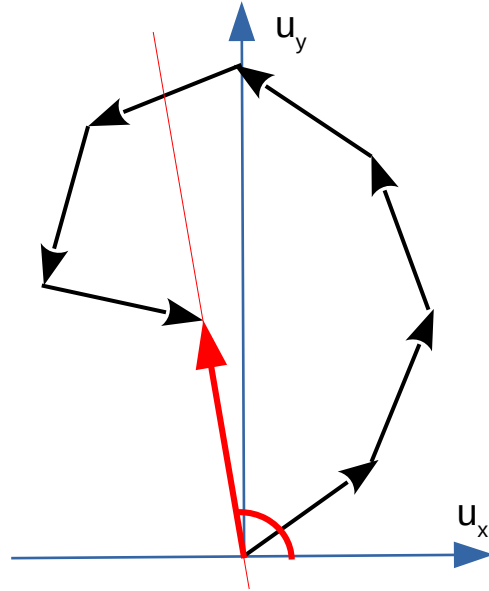


event plane method:

$$\vec{Q}_n = \frac{1}{Q_n} \sum_{j=1}^{j \leq M} w_j \vec{u}_n^j$$

scalar product:

$$\vec{Q}_n = \frac{1}{M} \sum_{j=1}^{j \leq M} w_j \vec{u}_n^j$$

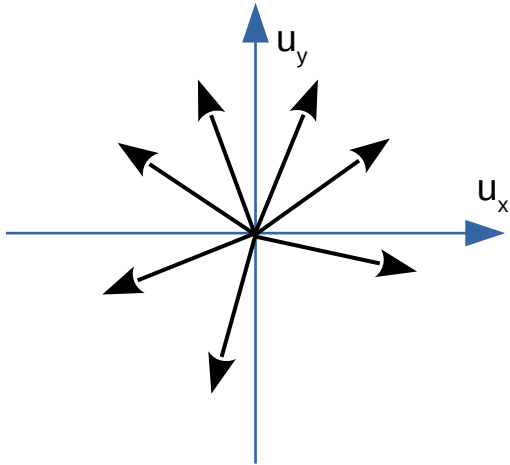




# Flow vectors and event plane angle

u and Q-vectors:

$$\vec{u}_n = \begin{pmatrix} \cos n \varphi \\ \sin n \varphi \end{pmatrix}$$

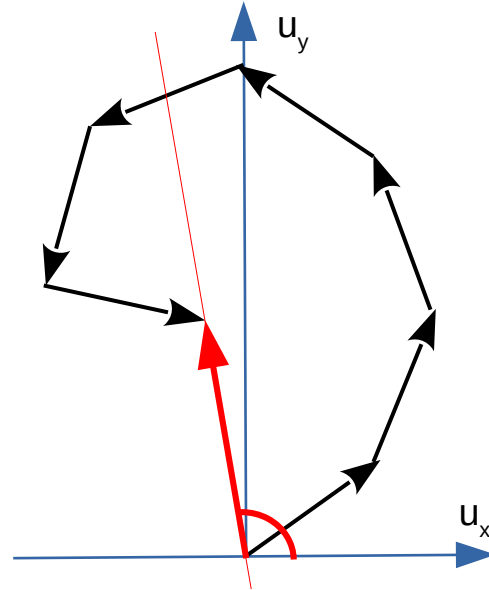


event plane method:

$$\vec{Q}_n = \frac{1}{Q_n} \sum_{j=1}^{j \leq M} w_j \vec{u}_n^j$$

scalar product:

$$\vec{Q}_n = \frac{1}{M} \sum_{j=1}^{j \leq M} w_j \vec{u}_n^j$$



Participants event plane:

- measured with tracks
- $w_j = 1, p_T$

Spectators event plane

- usually is measured with forward calorimeters
- $w_j =$  energy deposition in a module

# Flow vectors and event plane angle

u and Q-vectors:

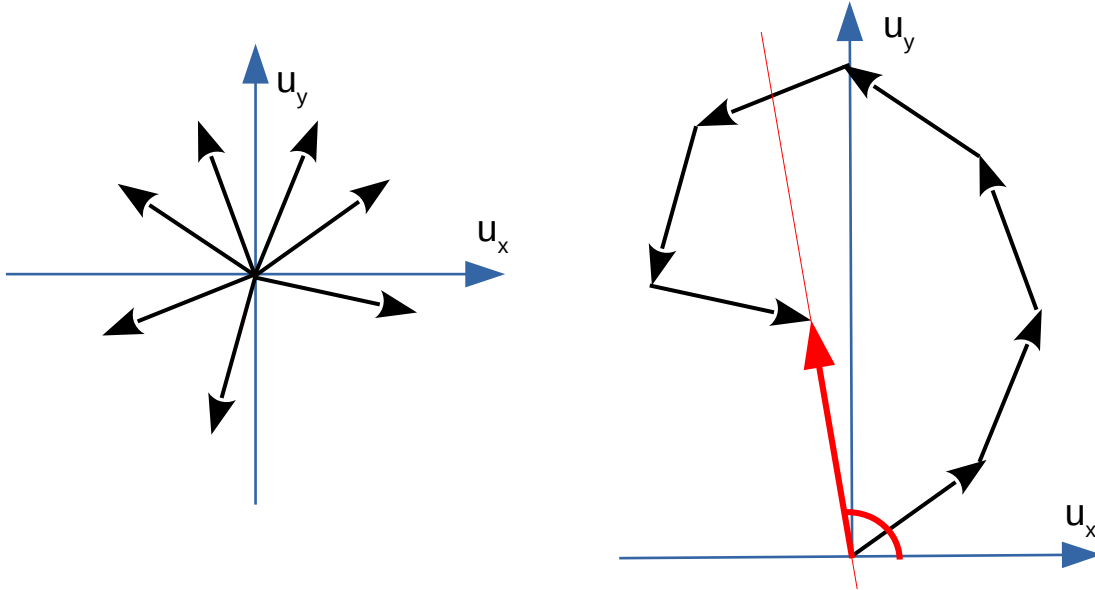
$$\vec{u}_n = \begin{pmatrix} \cos n \varphi \\ \sin n \varphi \end{pmatrix}$$

event plane method:

$$\vec{Q}_n = \frac{1}{Q_n} \sum_{j=1}^{j \leq M} w_j \vec{u}_n^j$$

scalar product:

$$\vec{Q}_n = \frac{1}{M} \sum_{j=1}^{j \leq M} w_j \vec{u}_n^j$$



$$v_n = \langle \cos(n[\varphi - \Psi_s]) \rangle$$

Directed flow:

$$v_1 \propto \langle 2u_{1,i} Q_{1,i} \rangle$$

Elliptic flow:

$$v_2 \propto \langle 2u_{2,i} Q_{2,i} \rangle \approx \langle 4u_{2,i} Q_{1,j}^A Q_{1,k}^B \rangle$$

$$(i, j, k = [x, y])$$

# Resolution correction

$$v_n = \langle \cos(n[\varphi - \Psi_s]) \rangle = \frac{1}{R_{n,i}} \langle 2u_{n,i} Q_{i,n} \rangle$$

$$R_{n,i} = \langle \cos[n(\Psi_{RP} - \Psi_{EP})] \rangle$$

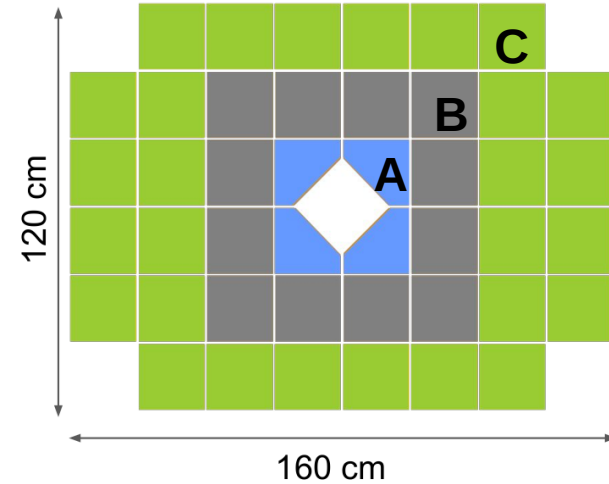
Correction factor (resolution)  $R_{1,i}^A$  is calculated via correlations  $\rightarrow$  3-subevent method:

$$R_{1,i}^A[B, C] = \sqrt{2 \frac{\langle Q_{1,i}^A Q_{1,i}^B \rangle \langle Q_{1,i}^A Q_{1,i}^C \rangle}{\langle Q_{1,i}^B Q_{1,i}^C \rangle}}$$

mixed harmonics:

$$R_{1,i}^A[B, C, D] \propto \sqrt{\frac{\langle Q_{1,i}^A Q_{1,i}^B \rangle \langle Q_{1,i}^A Q_{1,i}^C Q_{2,i}^D \rangle}{\langle Q_{1,i}^B Q_{1,i}^C Q_{2,i}^D \rangle}}$$

CBM Projectile Spectators Detector (PSD)

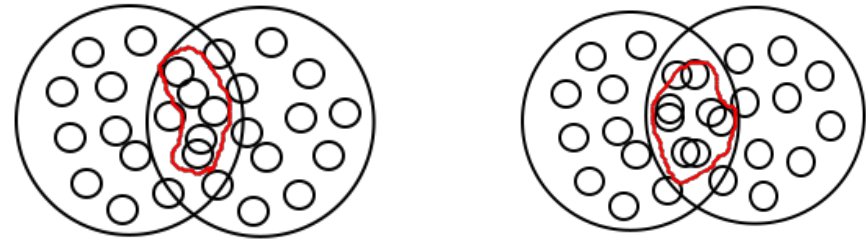
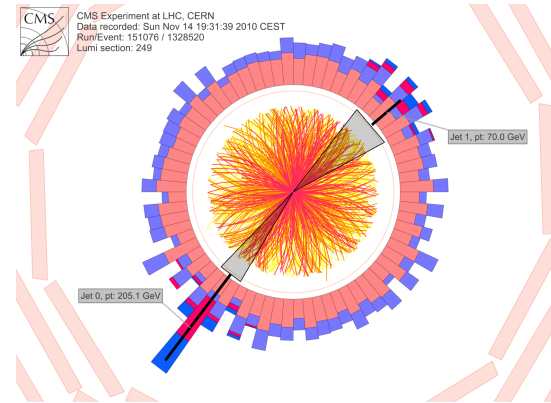
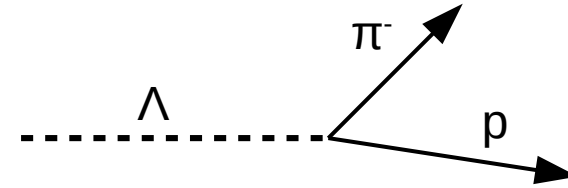


subevent A = 4 central modules

Resolution reflects the sensitivity of subevent A to initial symmetry plane

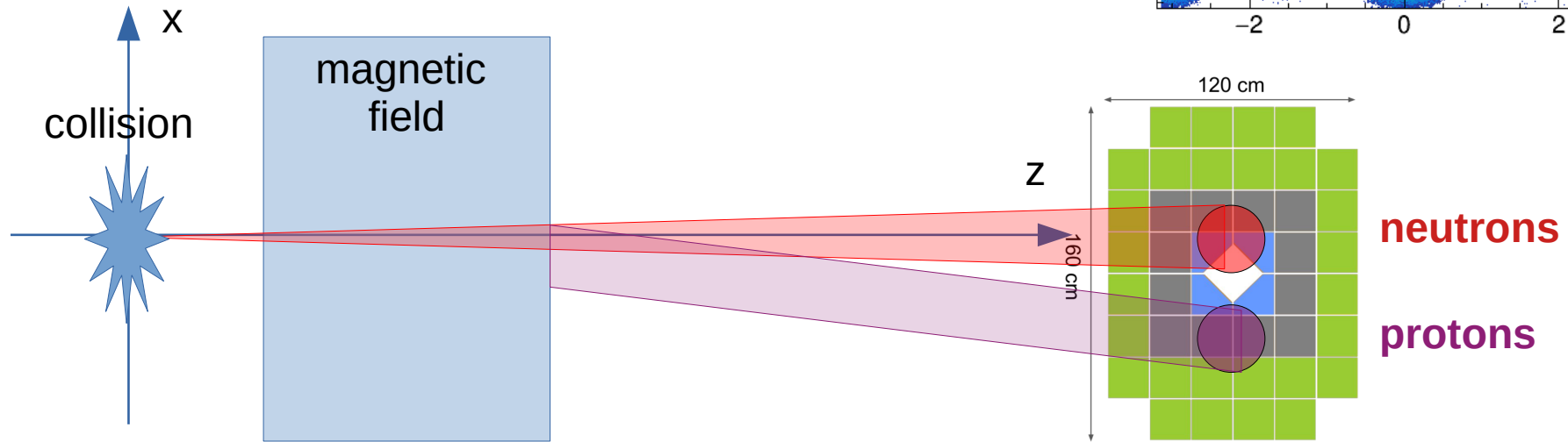
# Non-flow and flow fluctuations

- Resonance decays
  - for example, correlation between proton and pion from the lambda decay
- Jets (at high enough energies)
- Global momentum conservation
- Flow fluctuations
  - different initial state shapes for the same impact parameter value



# Detector biases

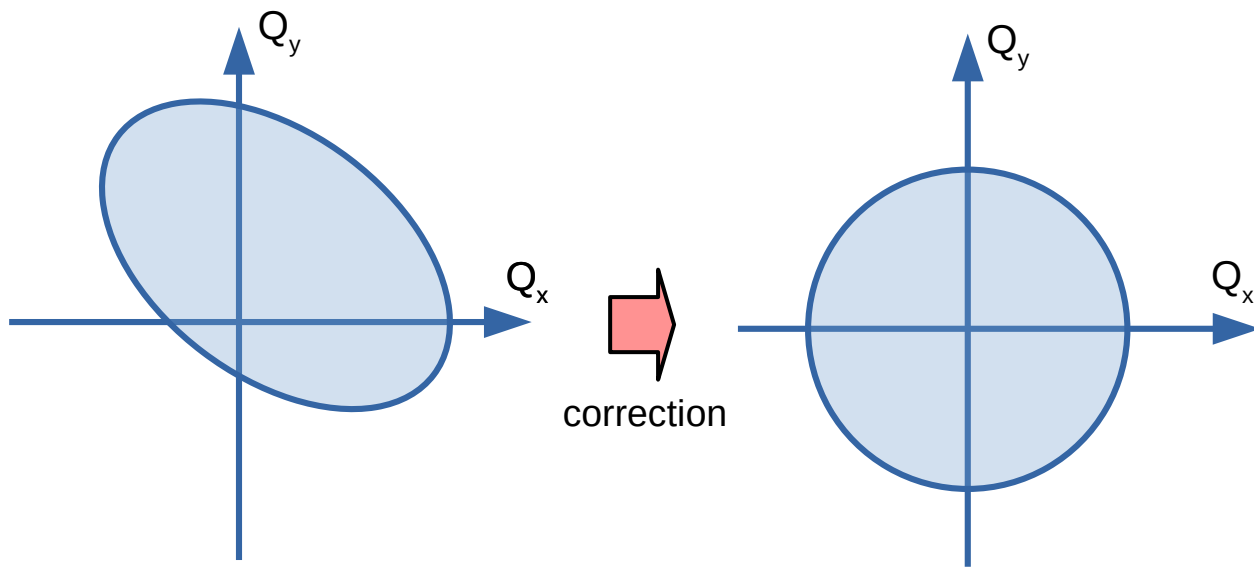
- Anisotropic detector acceptance and/or efficiency
- Magnetic field
- Tracking artefacts (track splitting etc)



Detector anisotropy introduce biases into measured azimuthal distribution



# Correction for detector non-uniformity



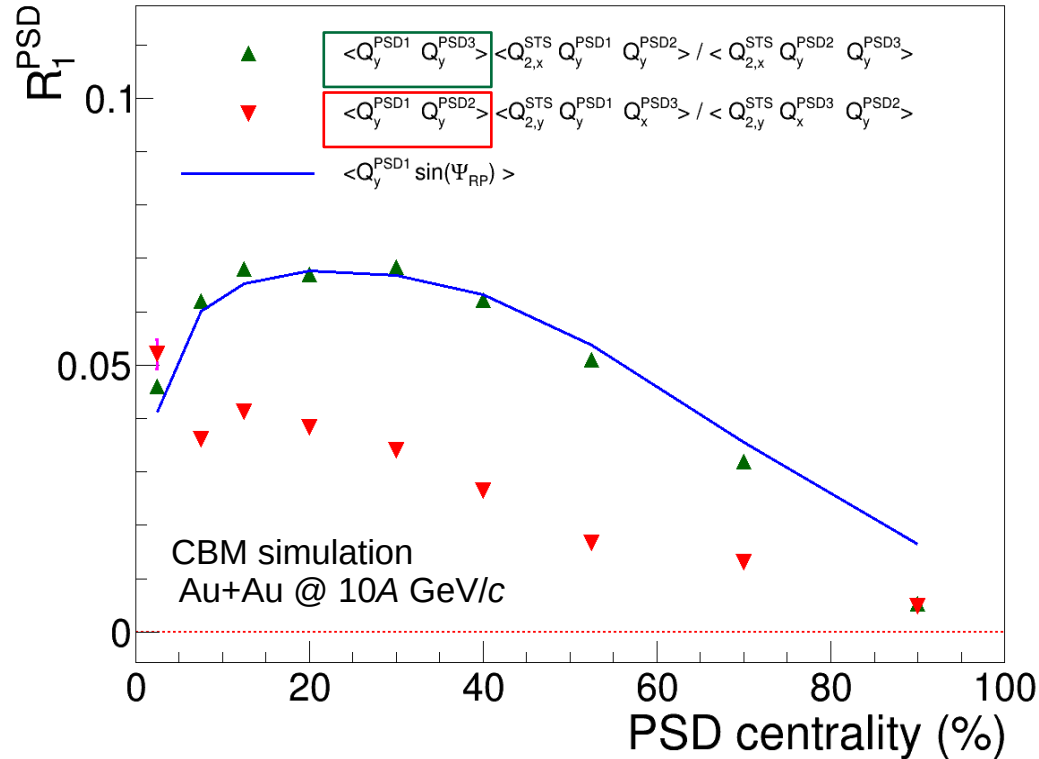
Data driven corrections for azimuthal acceptance non-uniformity

I. Selyuzhenkov and S. Voloshin  
[PRC77 034904 (2008)]

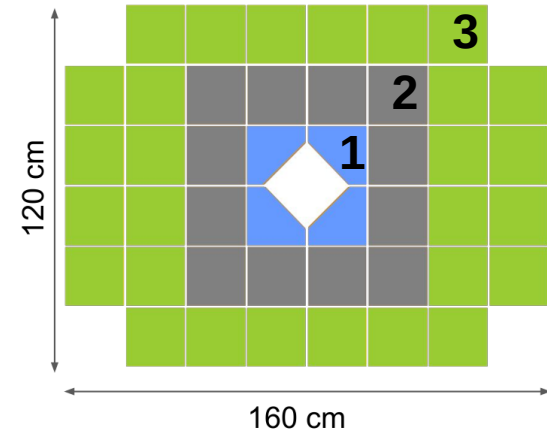
- Gain equalization
- Recentering
- Twist
- Rescaling

Correction procedure for Q-vectors is needed to recover isotropic distribution in azimuthal angle

# PSD resolution correction factor

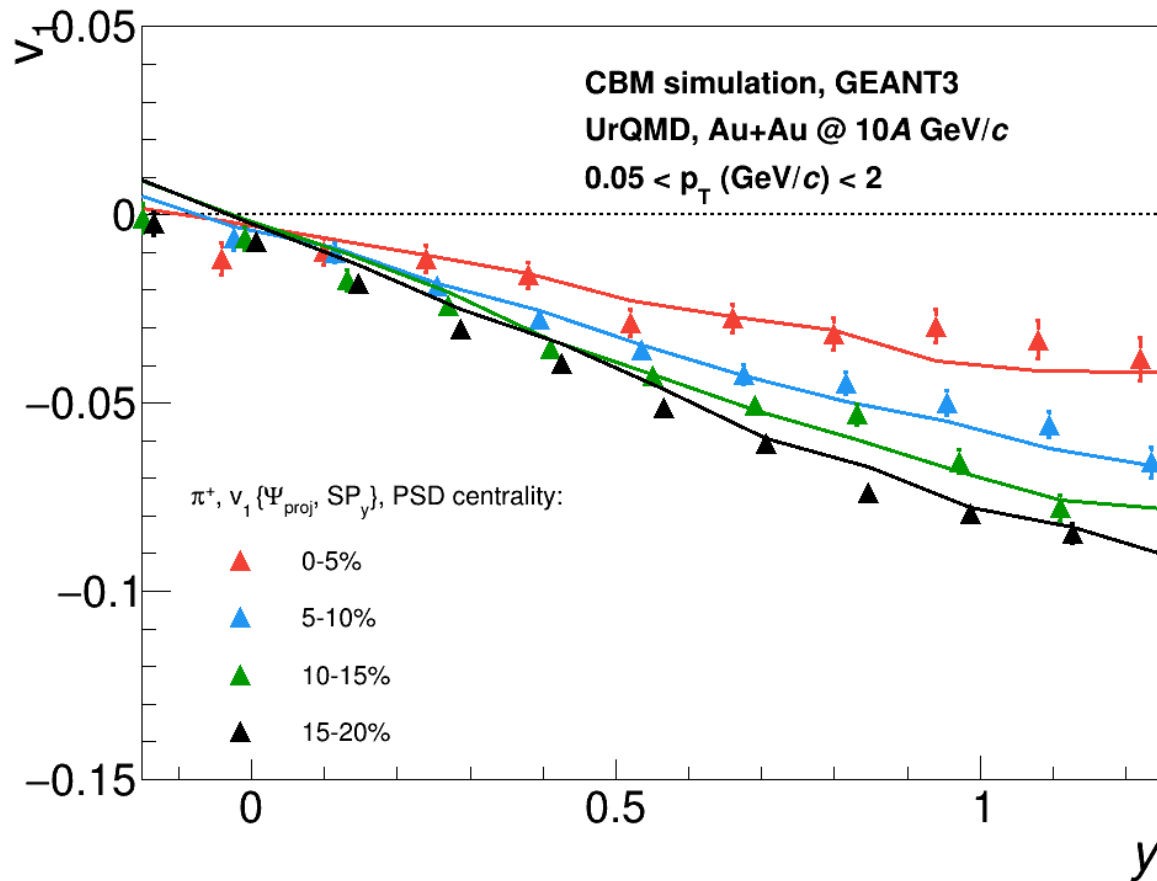


Neighboring PSD subevents correlation are distorted due to autocorrelations → mixed harmonics



After corrections we are able to reconstruct MC-true resolution correction factor

# PSD performance for directed flow measurements



- Directed flow of positively charged pions relative to spectators plane
- Centrality is defined using energy of the projectile spectators
- Reconstructed and simulated results are consistent in all centrality bins

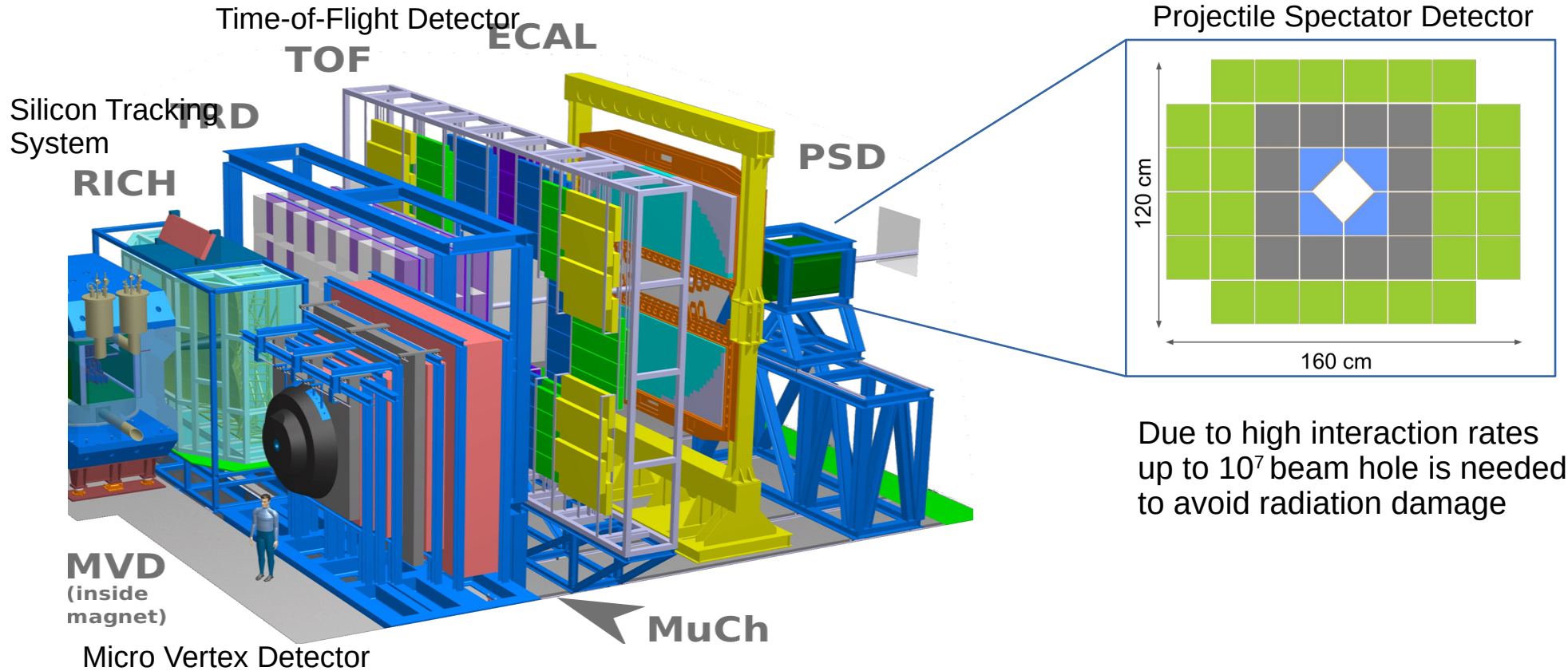
# Summary

- Anisotropic transverse flow allows to study evolution of heavy-ion collisions and properties of QCD matter
- It is important to measure flow coefficient relative to both participants and spectators symmetry plane
- Flow measurement techniques allow for precise extraction of flow coefficients with a complicated (non-uniform) detector setup
- More results are coming soon at high  $\mu_B$  region from BES-II@RHIC, NA61/SHINE@SPS and in future from CBM@FAIR MPD@NICA, ...





# CBM experiment @ FAIR



Simulation setup:  
UrQMD/DCM-QGSM-SMM models,  
Au+Au @ 10A GeV/c

# Resolution correction

$$v_n = \langle \cos(n[\varphi - \Psi_s]) \rangle = \frac{1}{R_{n,i}} \langle 2u_{n,i} Q_{i,n} \rangle \quad R_{n,i} = \langle \cos[n(\Psi_{RP} - \Psi_{EP})] \rangle$$

Observables:

Directed flow:

$$v_1 = \frac{\langle 2u_{1,i} Q_{1,i} \rangle}{R_{1,i}}$$

Elliptic flow:

$$v_2 = \frac{4 \langle u_{2,i} Q_{1,j}^A Q_{1,k}^B \rangle}{R_{1,j}^A R_{1,k}^B}$$

$$i, j, k = [x, y]$$

Correction factor (resolution)  $R_{1,i}^A$  is calculated via correlations → 3-subevent method:

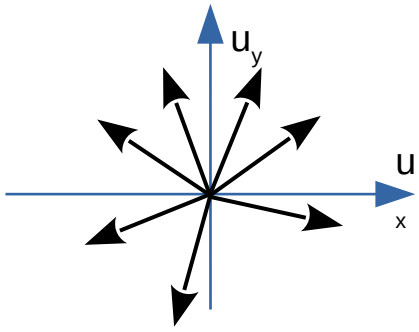
$$R_{1,i}^A[B, C] = \sqrt{2 \frac{\langle Q_{1,i}^A Q_{1,i}^B \rangle \langle Q_{1,i}^A Q_{1,i}^C \rangle}{\langle Q_{1,i}^B Q_{1,i}^C \rangle}}$$

mixed

harmonics:

$$R_{1,i}^A[B, C, D] \propto \sqrt{\frac{\langle Q_{1,i}^A Q_{1,i}^B \rangle \langle Q_{1,i}^A Q_{1,i}^C Q_{2,i}^D \rangle}{\langle Q_{1,i}^B Q_{1,i}^C Q_{2,i}^D \rangle}}$$

Resolution shows the sensitivity of subevent A to initial symmetry plane



# Multiparticles azimuthal correlations

$$v_n = \langle \cos n(\varphi - \Psi_n) \rangle$$

- Estimating flow harmonics with 2-particle correlation:

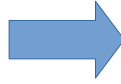
$$\begin{aligned}
 \text{event average} \rightarrow \langle \langle e^{in(\varphi_1 - \varphi_2)} \rangle \rangle &= \langle \langle e^{in(\varphi_1 - \Psi_n - (\varphi_2 - \Psi_n))} \rangle \rangle \\
 \text{particle average} \rightarrow &= \langle \langle e^{in(\varphi_1 - \Psi_n)} \rangle \langle e^{-in(\varphi_2 - \Psi_n)} \rangle \rangle \\
 &= v_n^2
 \end{aligned}$$

- The 'trick' works for any number of particles in the correlator

Ante

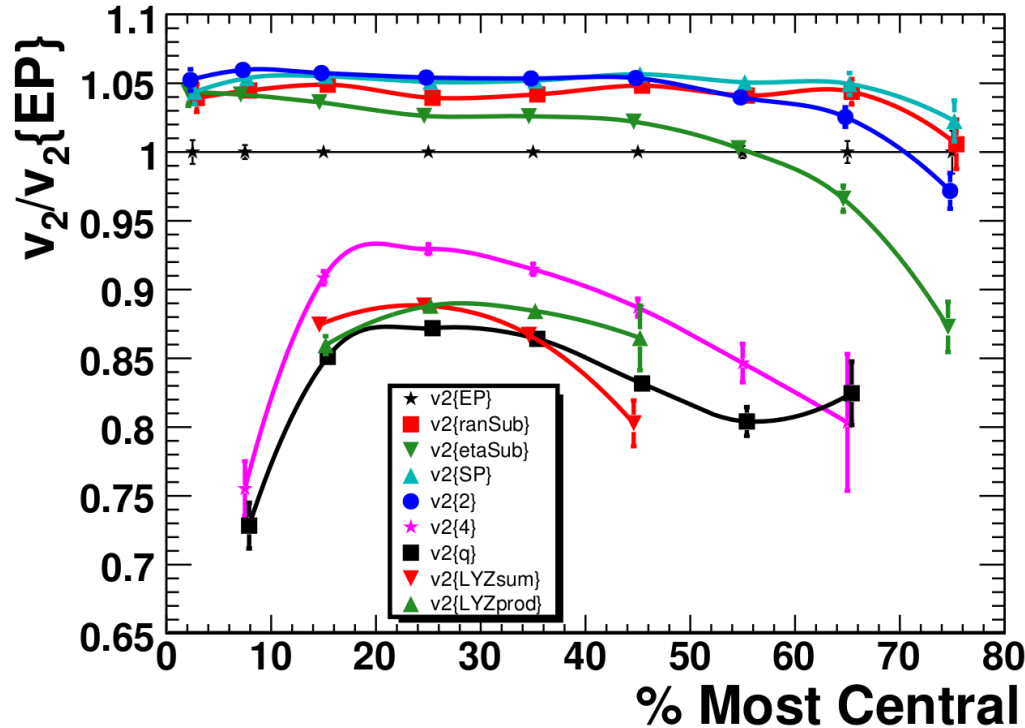
# Methods comparison

$$\vec{Q}_n = \frac{1}{Q_n} \sum_{j=1}^{j \leq M} \vec{u}_n^j$$



$$\vec{Q}_n = \frac{1}{M} \sum_{j=1}^{j \leq M} \vec{u}_n^j$$

different sensitivity  
to non-flow



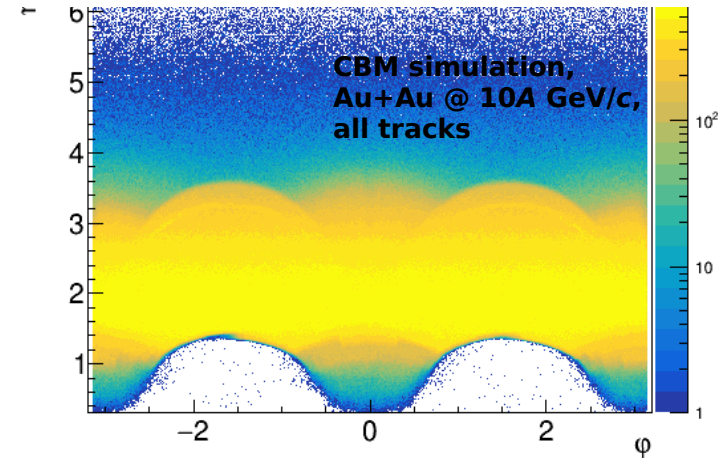
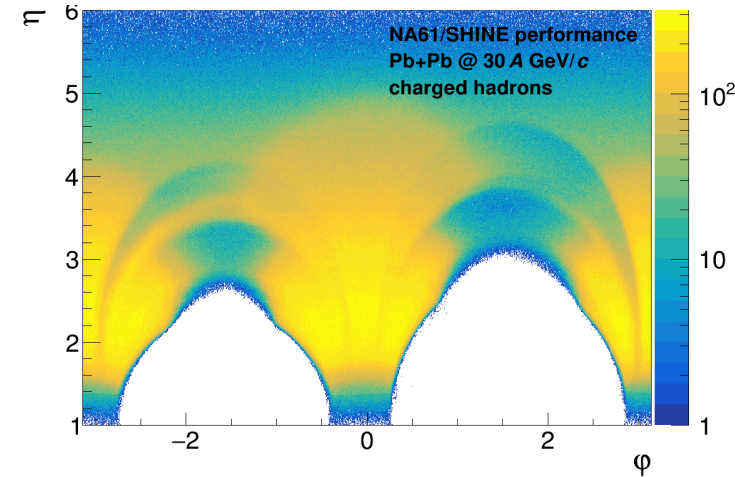
Upper band → two-particle correlation

- averages along the participant plane with nonflow and fluctuation contributions

Lower band → multi-particle correlation

- averages along the reaction plane mostly free of nonflow and fluctuation contributions

# Framework for detector azimuthal non-uniformity corrections and analysis



## QnVector Corrections Framework

- Data driven corrections for azimuthal acceptance non-uniformity  
I. Selyuzhenkov and S. Voloshin [PRC77 034904 (2008)]
- QnVector Corrections Framework (used by ALICE)  
J. Onderwaater, V. Gonzalez, I. Selyuzhenkov  
<https://github.com/jonderwaater/FlowVectorCorrections>
- Recentering, twist, and rescaling corrections applied  
time dependent (run-by-run) and as a function of centrality



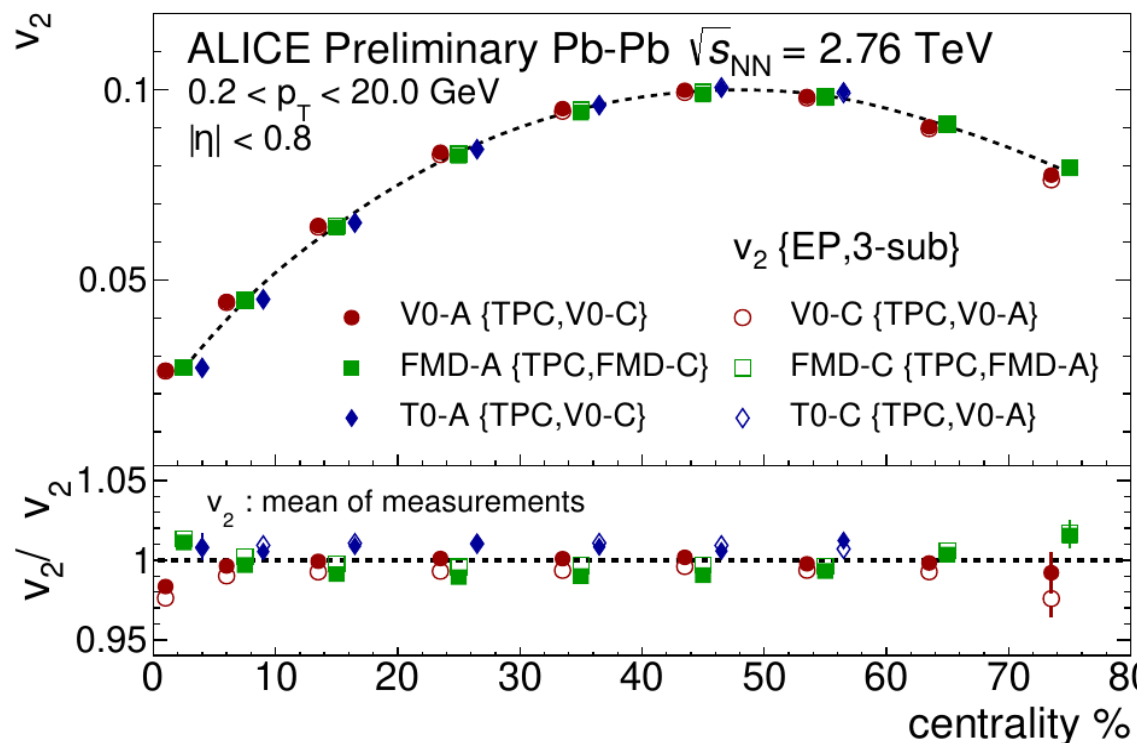
## Flow Analysis Framework

- Extended  $Q_n$ -vector corrections for  $p_T/y$ -differential
- Multi-dimensional correlations of  $u$  and  $Q$ -vectors  
L. Kreis (GSI / Heidelberg) and I. Selyuzhenkov (GSI / MEPHI)

Interfaced to CBM and NA61/SHINE analysis environment



# Framework for detector azimuthal non-uniformity corrections



- After corrections, the elliptic flow measurements with different event plane estimators are fully consistent with each other

QnVector Corrections Framework (ALICE)  
J. Onderwaater, V. Gonzalez, I. Selyuzhenkov

<https://github.com/jonderwaater/FlowVectorCorrections>