



# Multiplicity correlations with strongly intensive quantities

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3-7 June 2019



# Outline

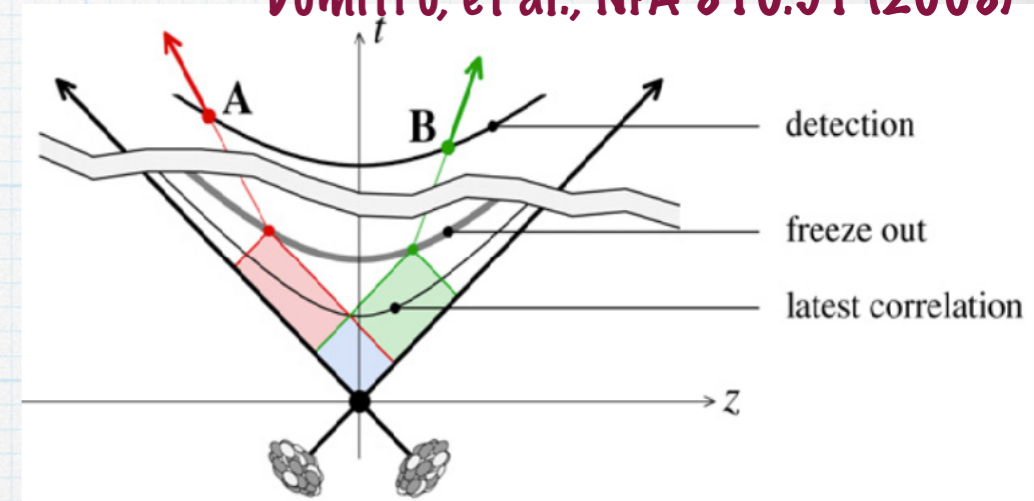
- \* Forward-backward multiplicity correlations
- \* Strongly intensive quantity  $\Sigma$
- \* Independent quark-gluon strings model calculations for LHC energies
- \* Collectivity/string fusion
- \* ALICE Pb-Pb results vs. event generators
- \* LHC->RHIC->SPS->NICA

# Forward-backward multiplicity correlations

Dumitru, et al., NPA 810:91 (2008)

Causality requires appearance of long-range rapidity correlations at early stages of evolution.

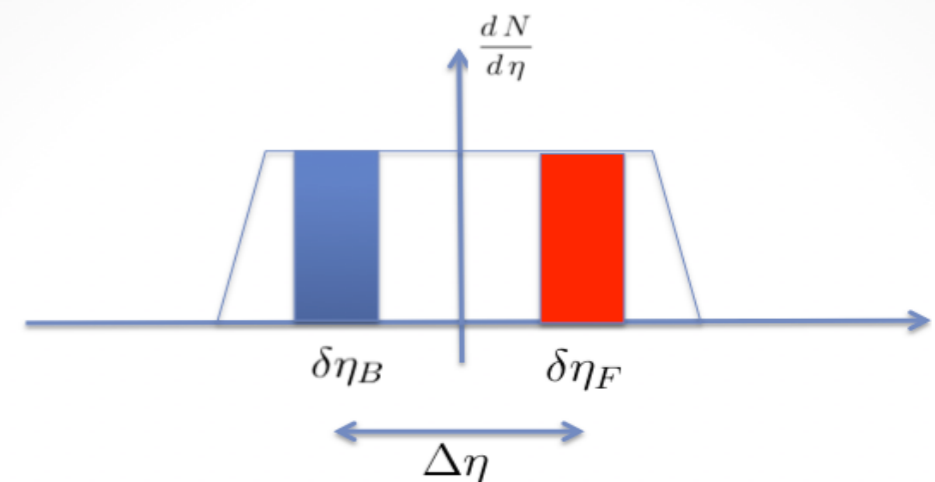
Long-range correlations originate from fluctuations in the number of particle sources (initial stage)+ other effects (jets, etc)



Quantified by the correlation coefficient:

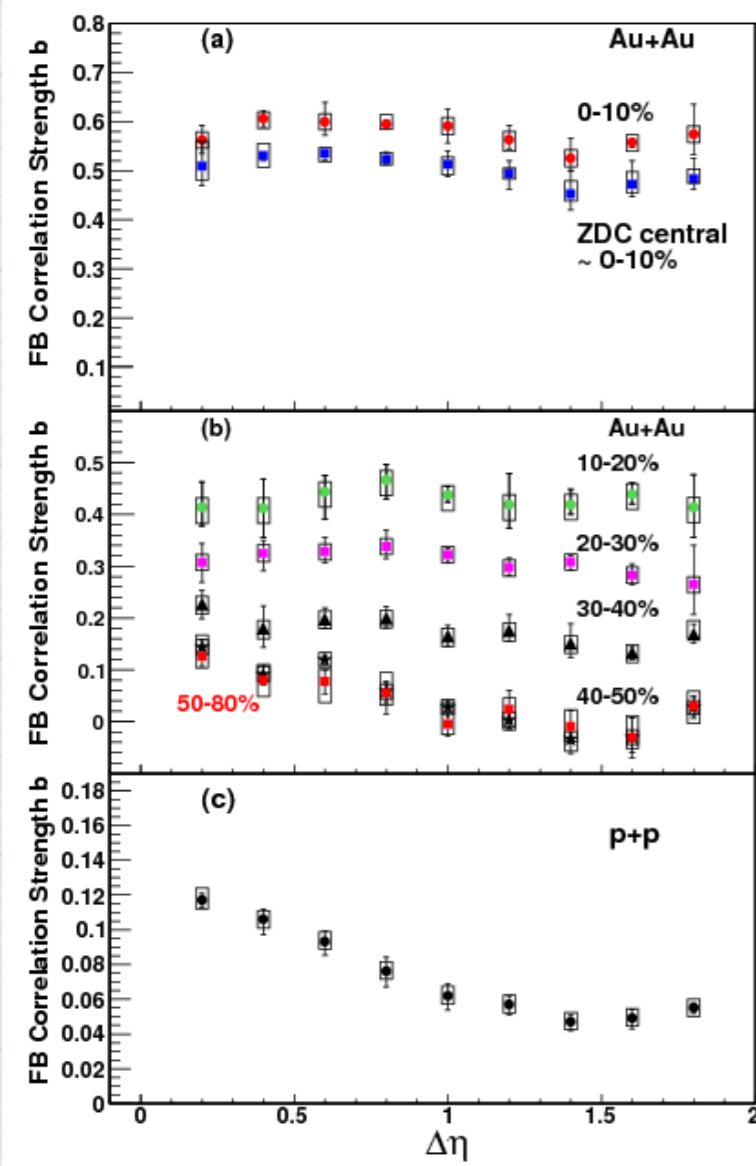
$$b_{corr} = \frac{\langle B \cdot F \rangle - \langle B \rangle \cdot \langle F \rangle}{\langle F^2 \rangle - \langle F \rangle^2}$$

Choose as B and F multiplicities in two separated rapidity intervals

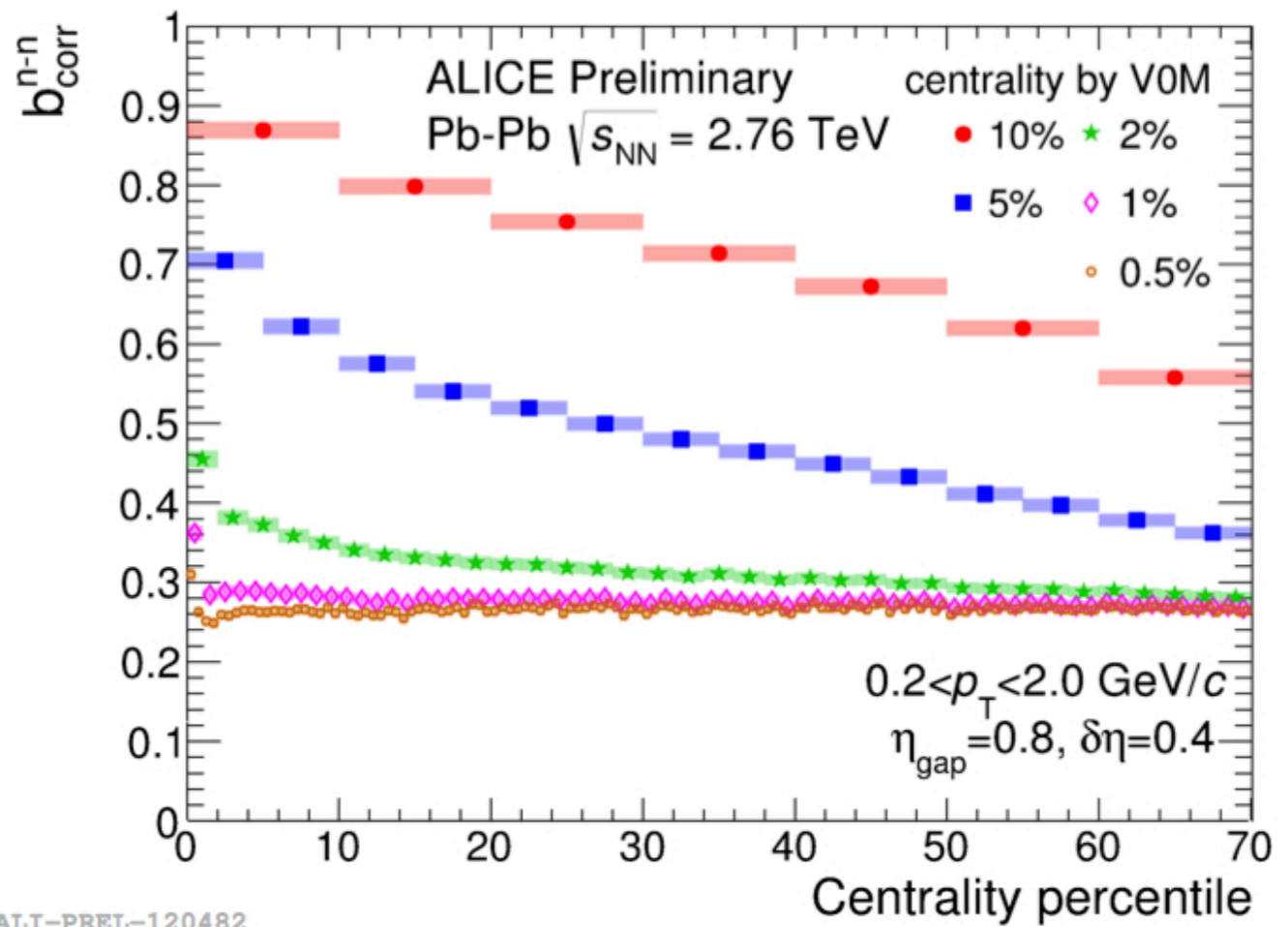


# Forward-backward multiplicity correlations

Huge sensitivity to centrality selection/volume fluctuations



STAR, PRL 103: 172301 (2009)



ALI-PREL-120482

I. Altsybeev (for ALICE), KnE Energy&Physics 3:304 (2018)



# Strongly intensive quantity

For a pair of extensive (proportional to volume) observables  $A$  and  $B$ :

$$\Sigma[A, B] = \frac{\langle B \rangle \omega[A] + \langle A \rangle \omega[B] - \text{cov}(A, B)}{C_\Sigma}$$

M. Gorenstein, M. Gazdzicki,  
PRC 84:014904 (2011)

- \* Independent of  $\langle W \rangle$  and  $\omega[W]$  in the Wounded Nucleon Model
- \*  $\Sigma=1$  for independent particle production model
- \*  $\Sigma=0$  in case of absence of fluctuations

Can be applied for F-B multiplicity correlations!

E.A., TMPH 185:383 (2015)

$$\Sigma[n_F, n_B] = \frac{\langle n_B \rangle \omega[n_F] + \langle n_F \rangle \omega[n_B] - \text{cov}(n_F, n_B)}{\langle n_F \rangle + \langle n_B \rangle}$$

# Independent strings model

1) The number of strings,  $N$ , fluctuates around the mean value  $\langle N \rangle$  with the scaled variance  $\omega[N] = \frac{\langle N^2 \rangle - \langle N \rangle^2}{\langle N \rangle}$

2) The fragmentation of each string contributes event-by-event to the forward and backward rapidity windows the  $\mu_F$  and  $\mu_B$  charged particles

3)  $P(\mu_F, \mu_B)$  is identical for all strings

$$\Sigma[n_F, n_B] = \Sigma[\mu_F, \mu_B] \quad \text{for independent sources}$$

E.A., TMPH 185:383 (2015)

# Independent strings model

## Two-particle correlation function

$$C_2(\eta_1, \eta_2) = \frac{\rho_2(\eta_1, \eta_2)}{\rho(\eta_1)\rho(\eta_2)} - 1 \quad \rho(\eta) = \frac{dn_{ch}}{d\eta} \quad \rho_2(\eta_1, \eta_2) = \frac{d^2n_{ch}}{d\eta_1 d\eta_2}$$

For string:

$$\Lambda(\eta_1, \eta_2) = \frac{\lambda_2(\eta_1, \eta_2)}{\lambda(\eta_1)\lambda(\eta_2)} - 1$$

$$C_2(\eta_1, \eta_2) = \frac{\omega[N] + \Lambda(\eta_1, \eta_2)}{\langle N \rangle}$$

V. Vechernin, NPA 939:21 (2015)

Translational invariance assumption:

$$\lambda(\eta) = \mu_0 \quad \lambda_2(\eta_1, \eta_2) = \lambda_2(\eta_1 - \eta_2) = \lambda_2(\Delta\eta)$$

For small symmetric observation windows ( $\delta\eta \ll \eta_{corr}$ ):

$$\Sigma[n_F, n_B](\Delta\eta) = 1 + \mu_0 \delta\eta (\Lambda(0) - \Lambda(\Delta\eta))$$

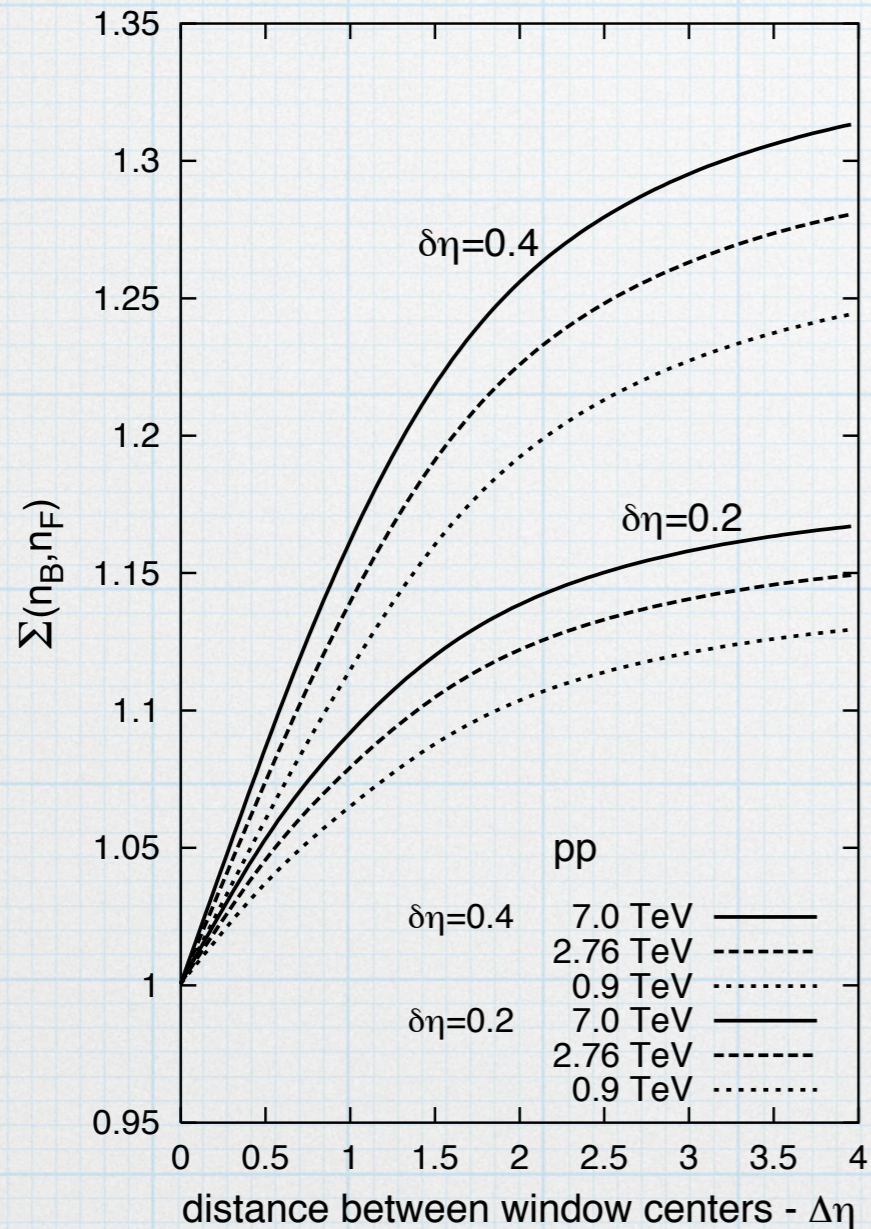
V. Vechernin, WPCF2017  
E.A., V. Vechernin, EPJA 55(1):14 (2019)

Strongly intensive quantity is entirely described by  
string two-particle correlation function

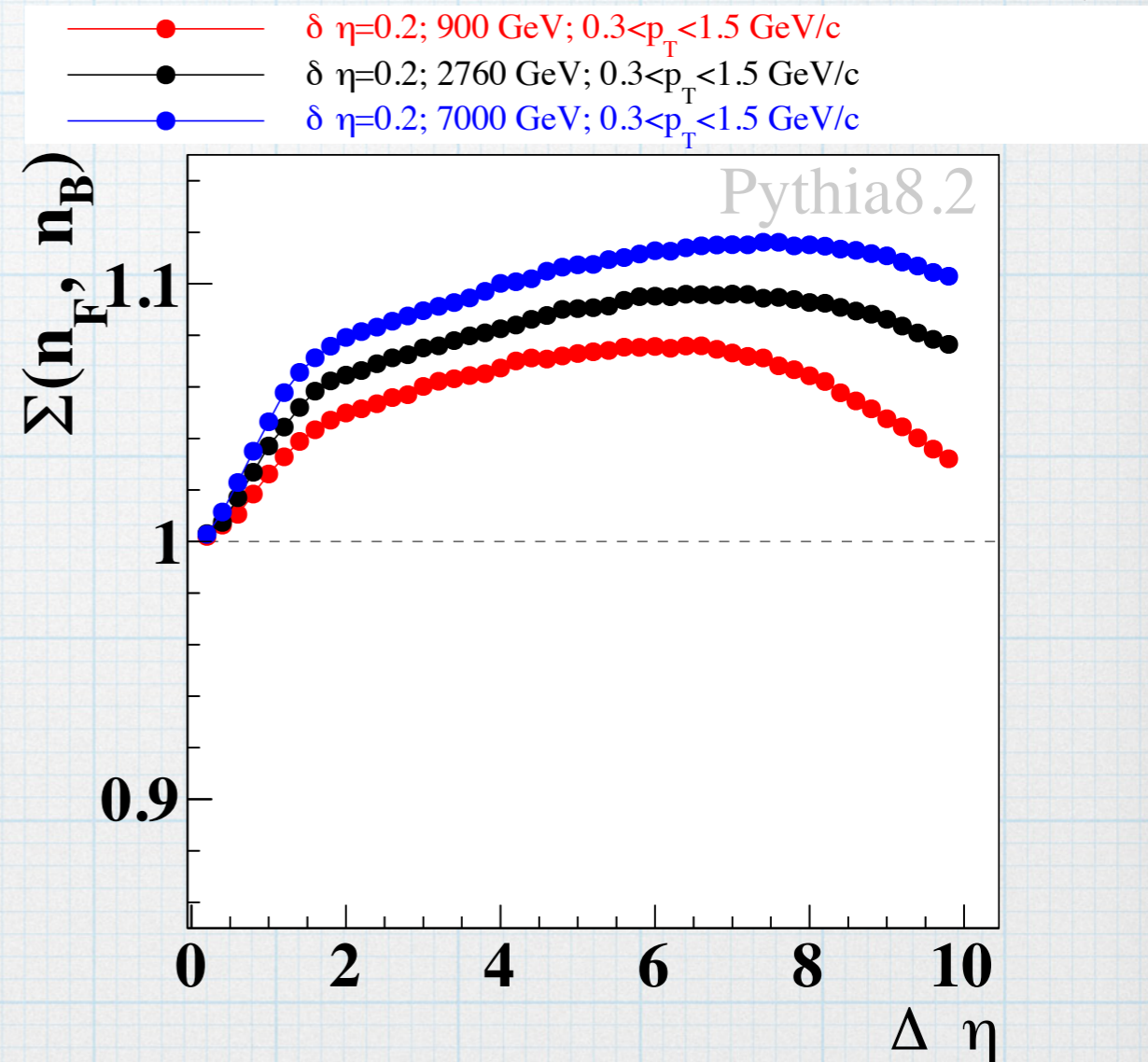
# Strongly intensive quantity

With parametrisation of  $\Lambda(\Delta\eta)$  from V. Vechernin, NPA 939:21 (2015)

v.8.235



E.A., V. Vechernin, EPJA 55(1):14 (2019)



T. Sjöstrand, et al., Comp.Phys.Comm. 191:159 (2015)



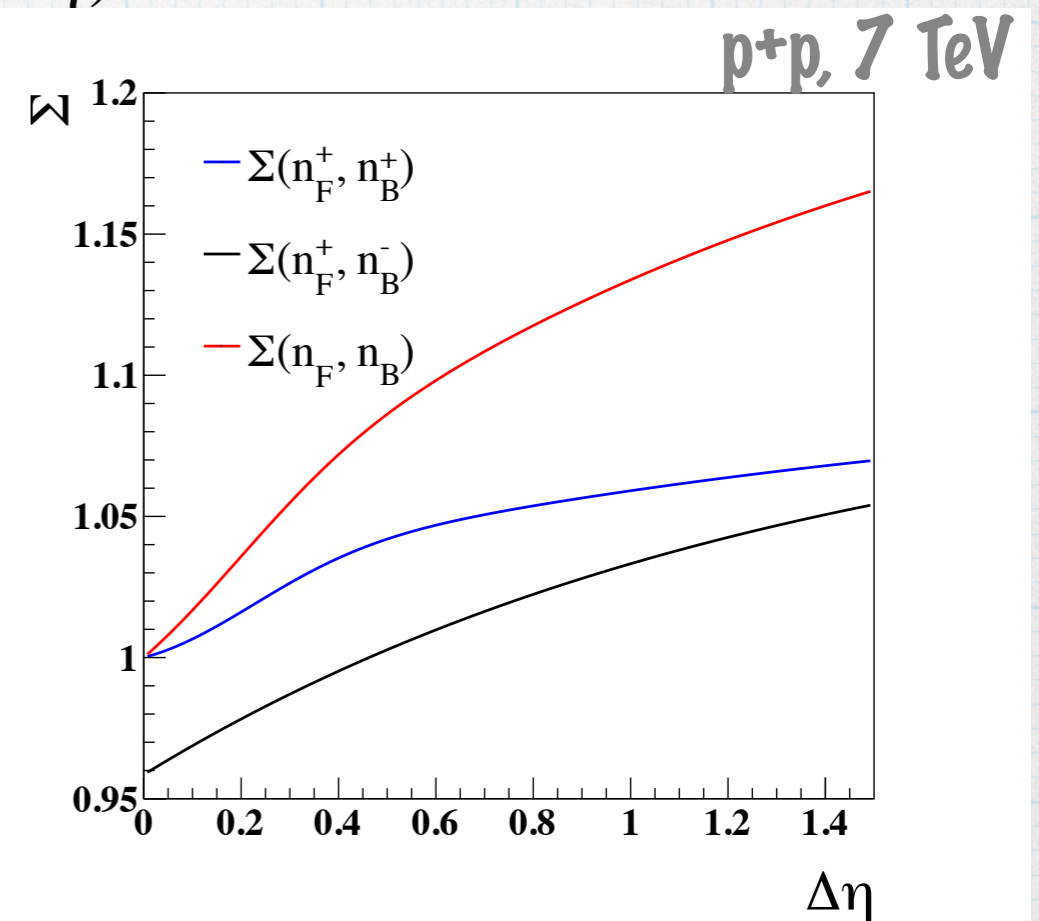
# Electric charge

$$\Sigma[n_F, n_B] = \Sigma[n_F^+, n_B^+] + \Sigma[n_F^-, n_B^+] - \Sigma[n_F^+, n_F^-]$$

By fitting balance functions from **ALICE, PRL 110:152301 (2013)**  
we find parametrisation for  $\Lambda^{++}(\Delta\eta), \Lambda^{+-}(\Delta\eta)$

Oversimplified approach

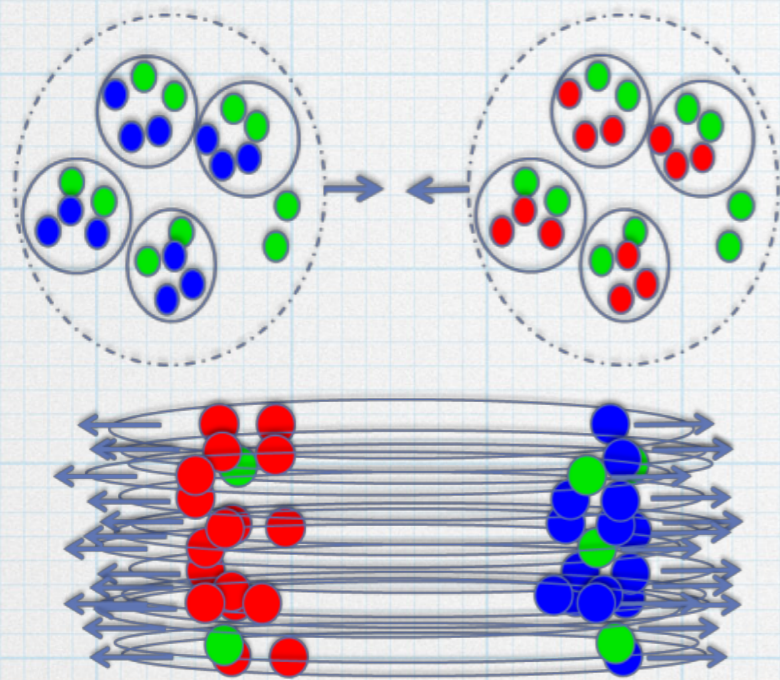
Should be modified by taking into account  
short-range correlations of particles  
originating from different strings



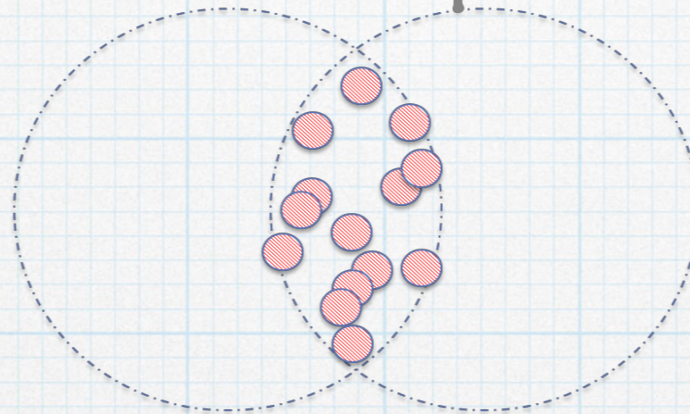
E.A., V. Vechernin, EPJA 55(1):14 (2019)



# Interaction of strings



Transverse plane



● Single string

$$\Sigma[n_F, n_B](\Delta\eta) = 1 + \mu_0 \delta\eta (\Lambda(0) - \Lambda(\Delta\eta))$$

● Cluster of k strings

$$\Sigma_k[n_F, n_B](\Delta\eta) = 1 + \mu_{0k} \delta\eta (\Lambda_k(0) - \Lambda_k(\Delta\eta))$$

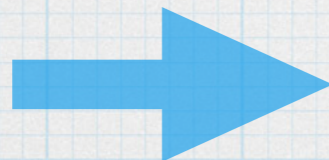
Set of string clusters

$$\Sigma[n_F, n_B](\Delta\eta) = \sum_{k=1}^{\infty} \alpha_k \Sigma_k[n_F, n_B](\Delta\eta)$$

$$\alpha_k = \frac{\langle n \rangle_k}{\langle n \rangle}$$

$$\mu_{0k} > \mu_0$$

$$n_{corr,k} < n_{corr}$$



$$\Sigma^{fusion}[n_F, n_B](\Delta\eta) > \Sigma^{no-fusion}[n_F, n_B](\Delta\eta)$$

Abramovskii, et al., Pisma Zh.Eksp.Theor.Fiz. 47(6):281 (1988)

Braun,Pajares, PLB 287:154 (1992); NPB 390:542 (1993); PRL 85:4684 (2000)

Bierlich, NPA 982:499 (2019)

E.A., V. Vechernin, EPJA 55(1):14 (2019)

# Interaction of strings

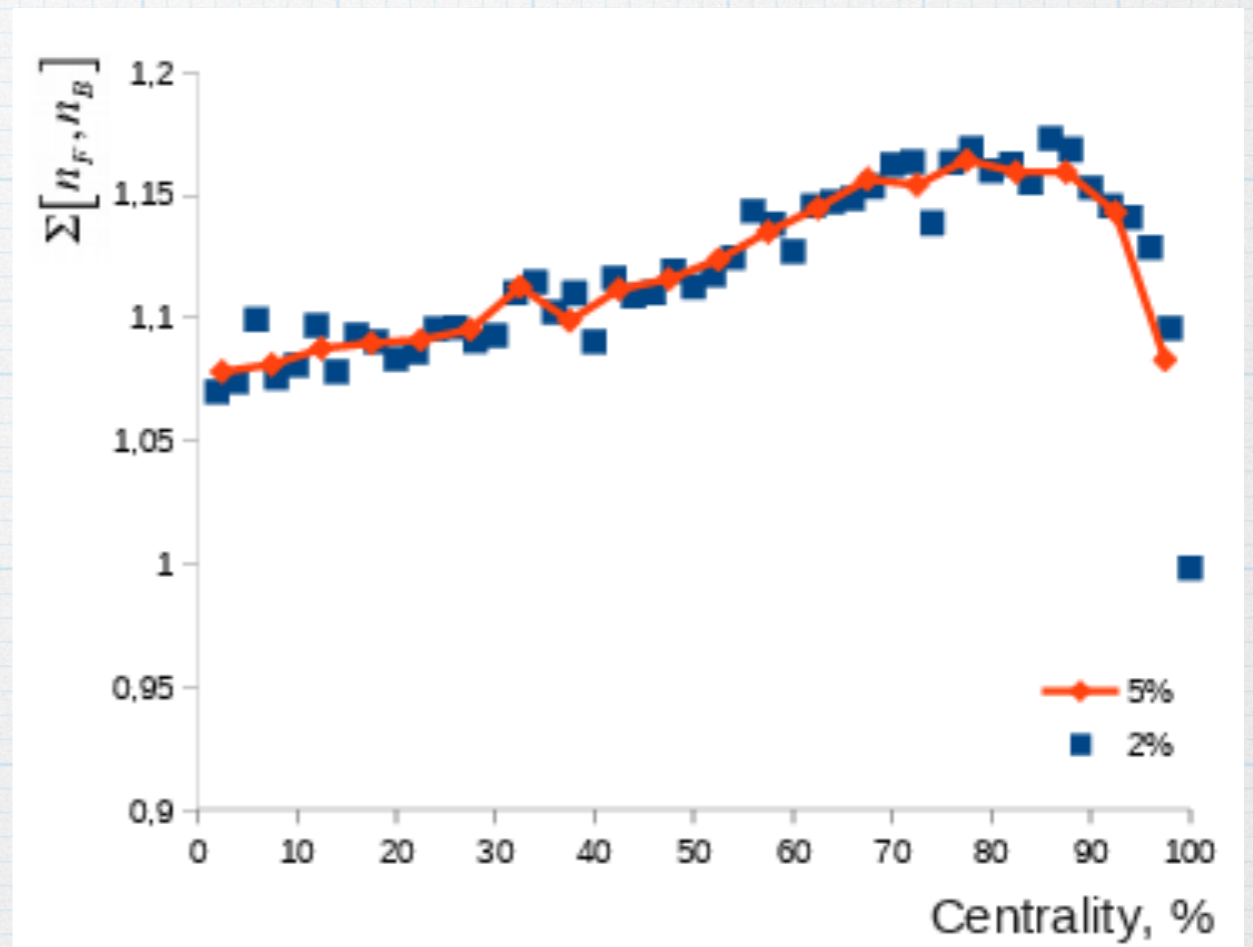
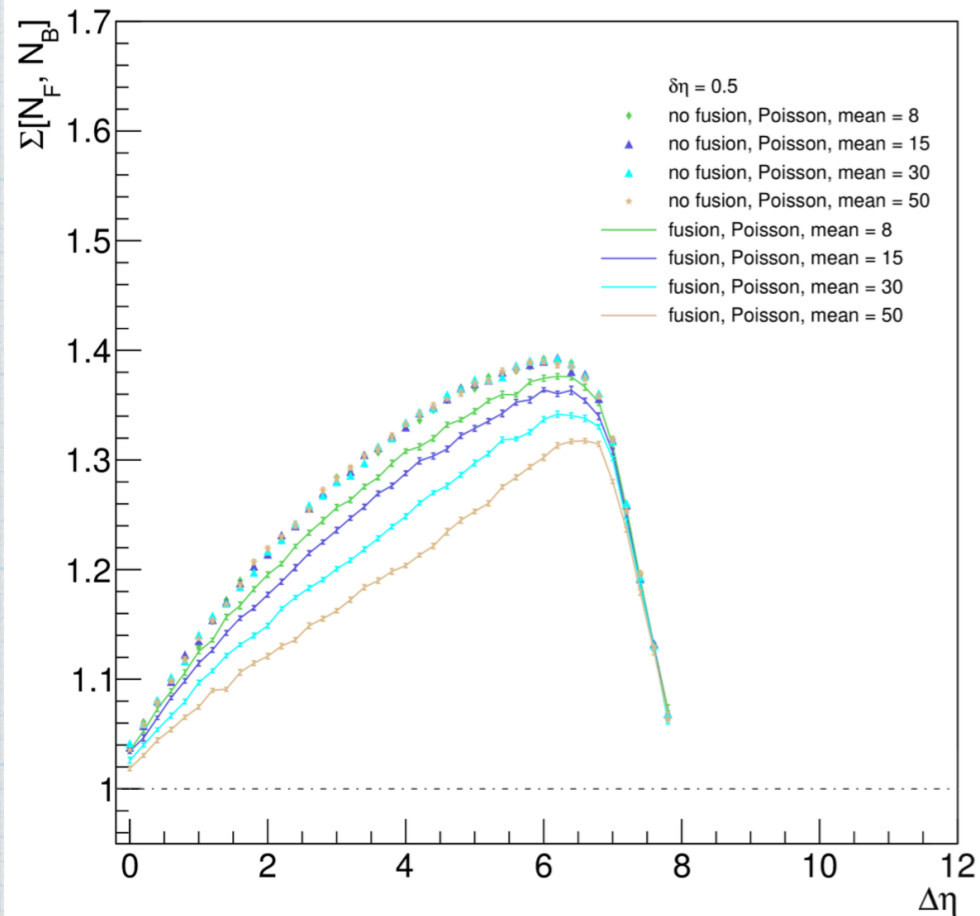
Pb+Pb

(-3.8;-3) and (3;3.8) windows  
non-monotonic dependence

model with interacting strings from color dipoles

Suppression due to string fusion

$\Sigma[N_F, N_B]$  from different strings

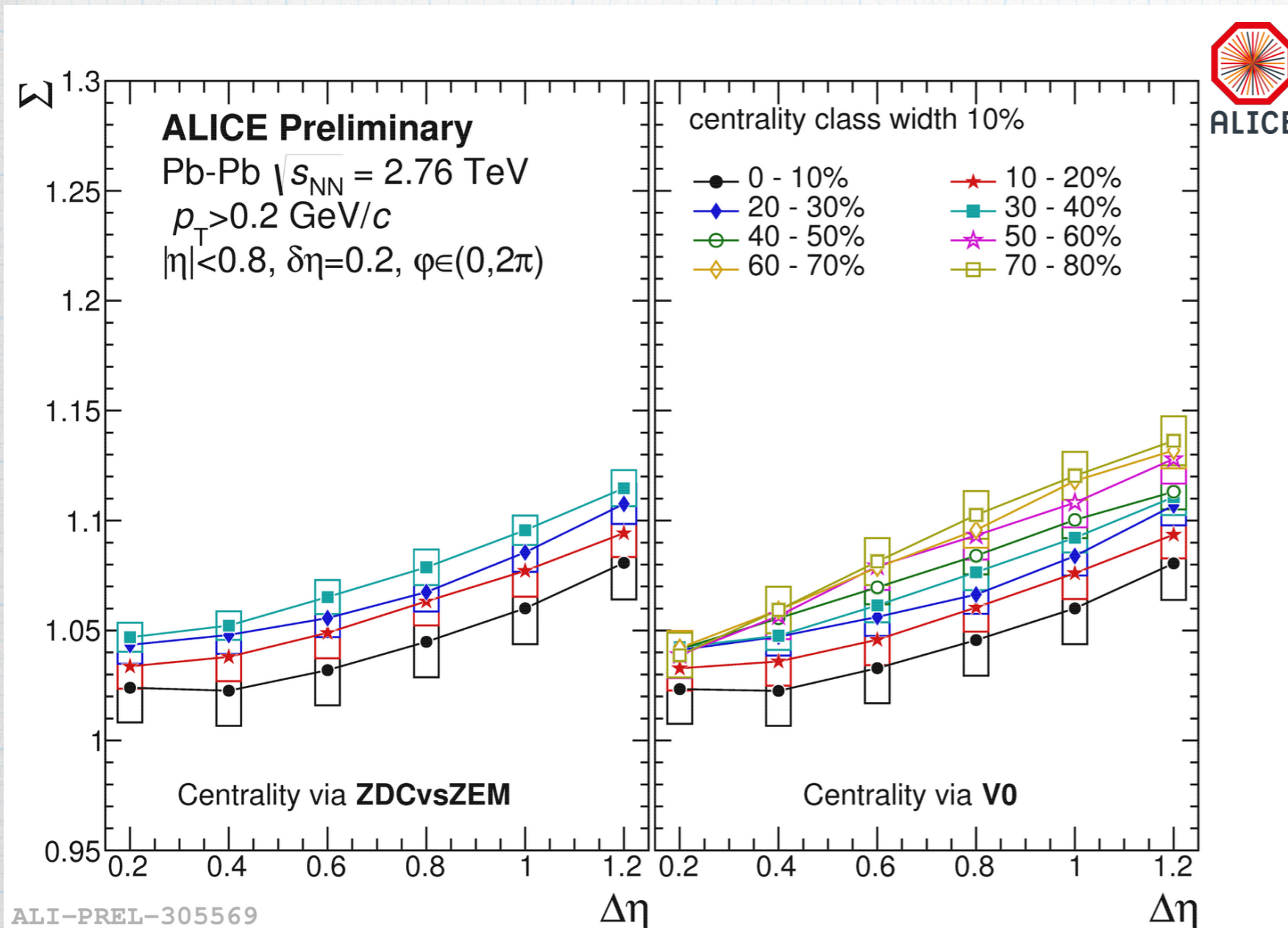


D. Prokhorova, this workshop

V. Kovalenko, EPJWCConf 204:03006 (2019)

# PbPb

I.Sputowska(for ALICE) MDPI Proc. 10(1):14 (2019)



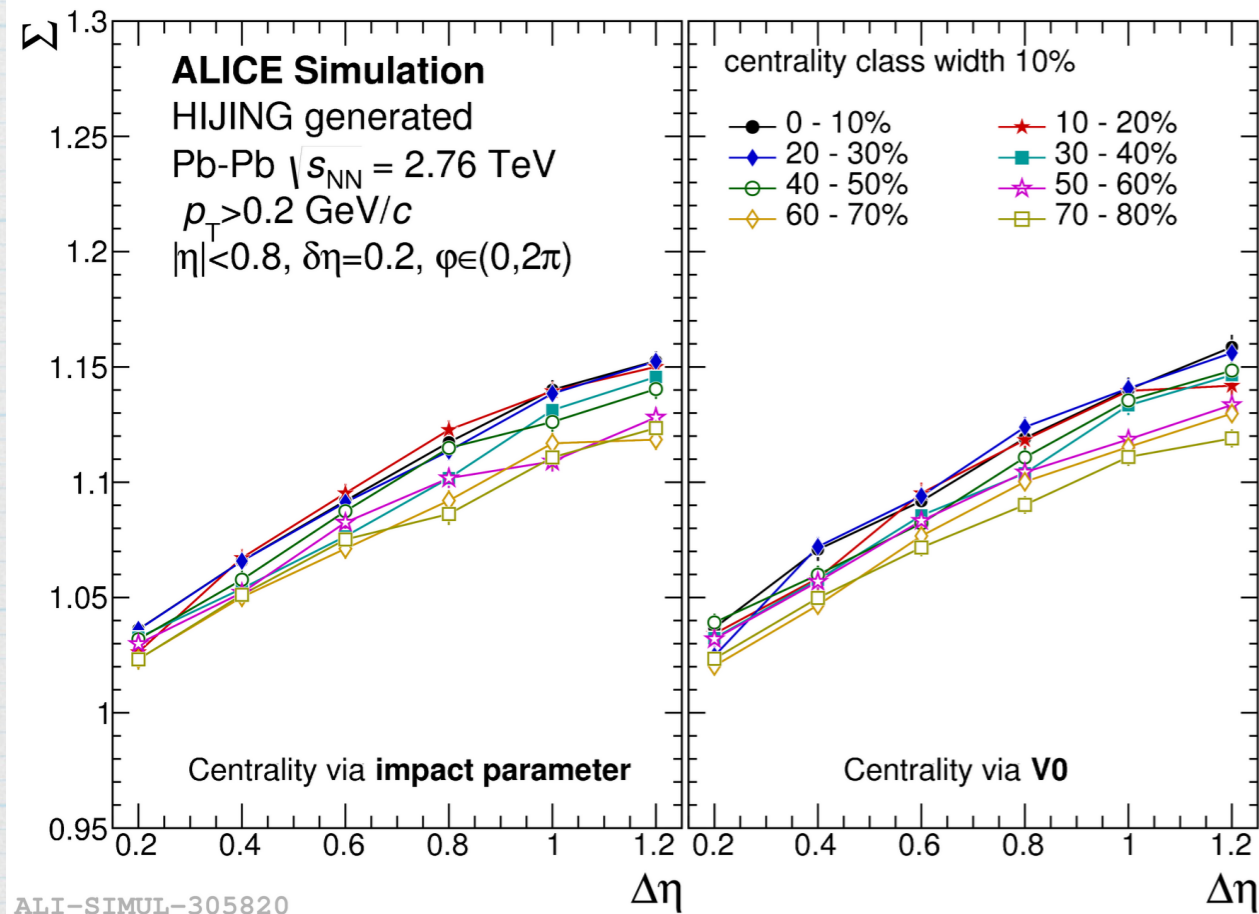
\* almost no dependence on centrality selection procedure

\* decreasing trend when going to more central collisions -> collectivity signal?

# PbPb in models

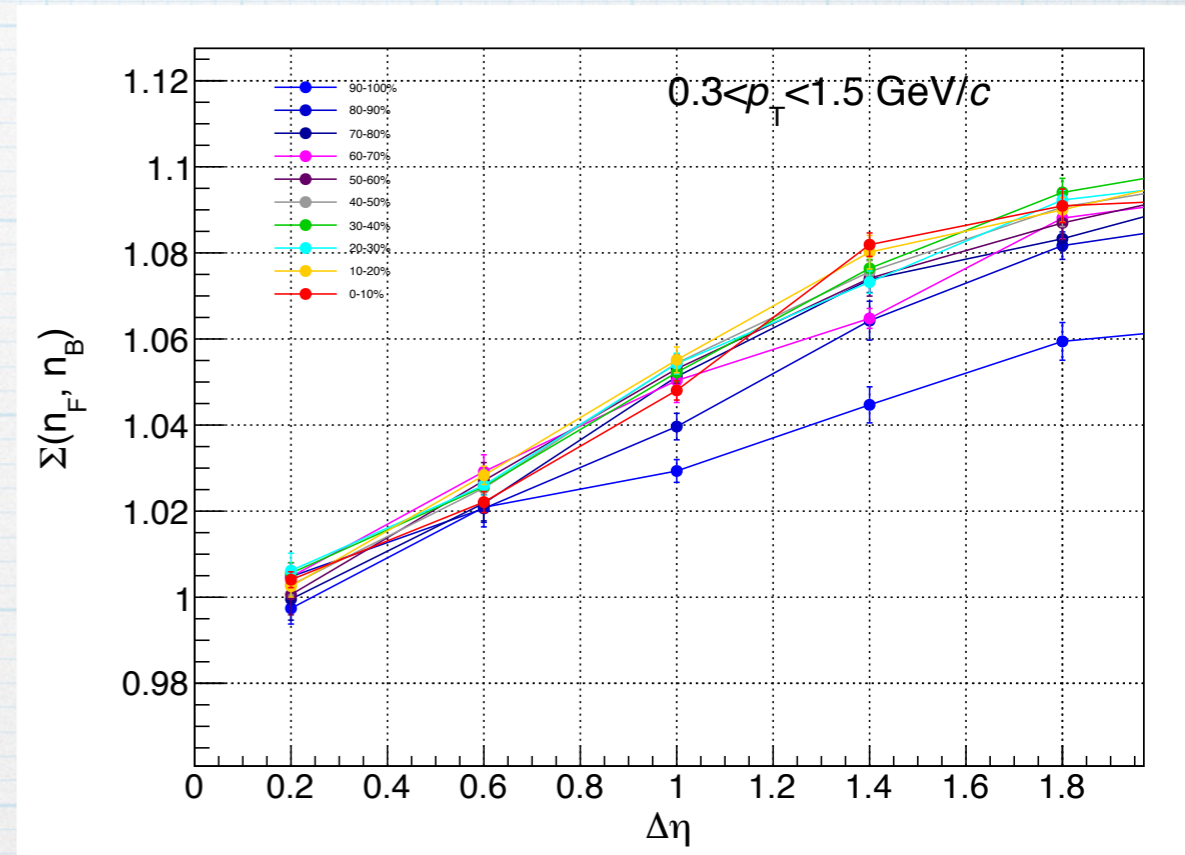
HIJING

M.Gyulassy, X.-N.Wang, *Comp.Phys.Comm.* 83:307 (1994)



Increasing trend when going to more central collisions

Angantyr (PYTHIA extension for AA)  
 C.Bierlich, et al., *JHEP* 1810:134 (2018)



Almost independent on centrality

# History lesson

Fluctuations of asymmetry parameter,  $C$ , have been studied at RHIC

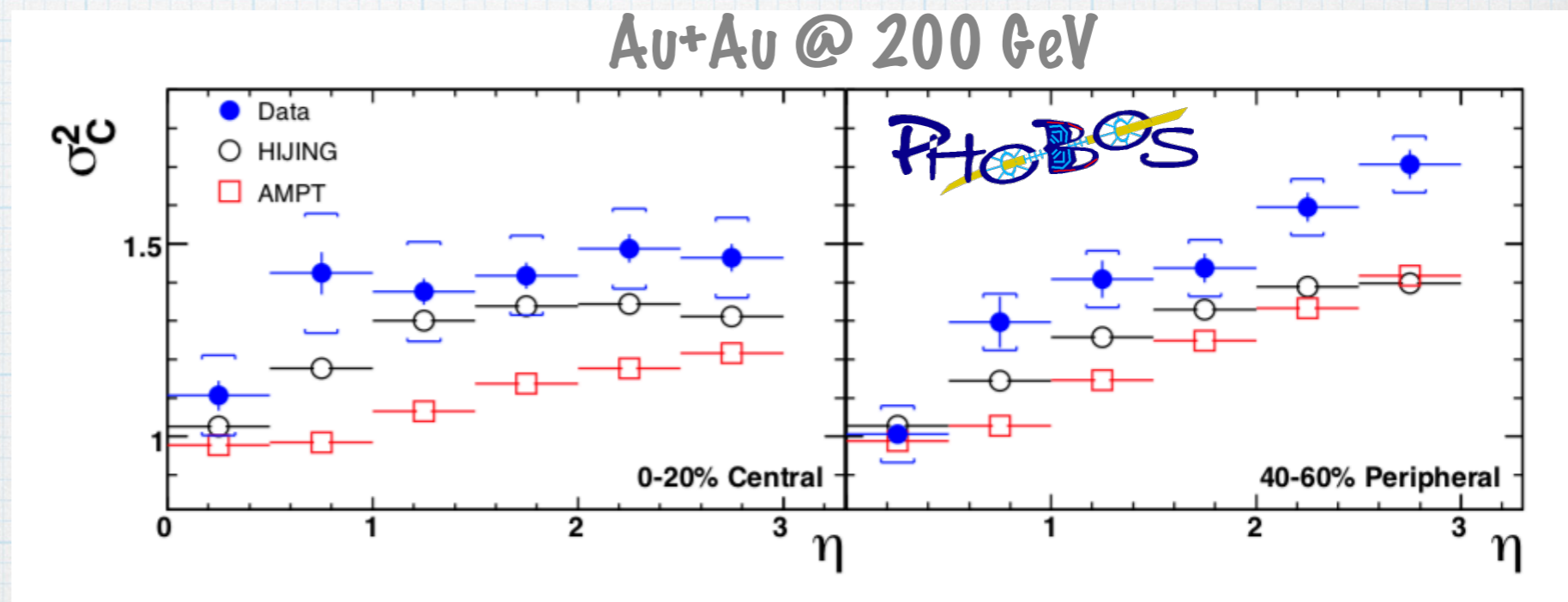
$$C = \frac{n_F - n_B}{\sqrt{n_F + n_B}} \quad \sigma^2(C) = \left\langle \frac{(n_F - n_B)^2}{n_F + n_B} \right\rangle - \left\langle \frac{n_F - n_B}{\sqrt{n_F + n_B}} \right\rangle^2$$

$\sigma^2(C) \approx \Sigma[n_F, n_B]$  under assumptions:

$$\langle n_F \rangle = \langle n_B \rangle$$

$$\left\langle \frac{n_F - n_B}{\sqrt{n_F + n_B}} \right\rangle^2 = \frac{\langle n_F - n_B \rangle^2}{\langle n_F + n_B \rangle}$$

$$\left\langle \frac{(n_F - n_B)^2}{n_F + n_B} \right\rangle = \frac{\langle (n_F - n_B)^2 \rangle}{\langle n_F + n_B \rangle}$$



PHOBOS, PRC 74: 011901 (2006)

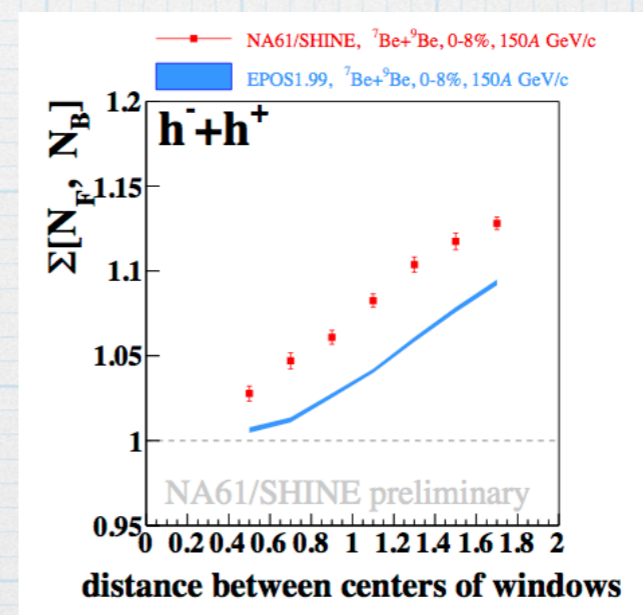
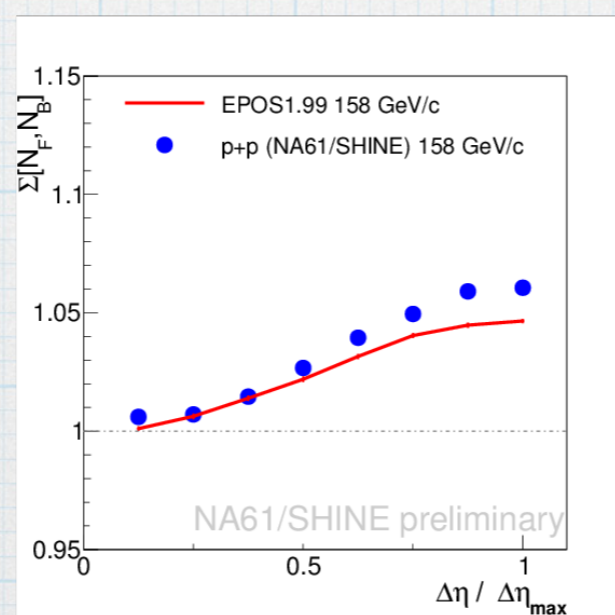
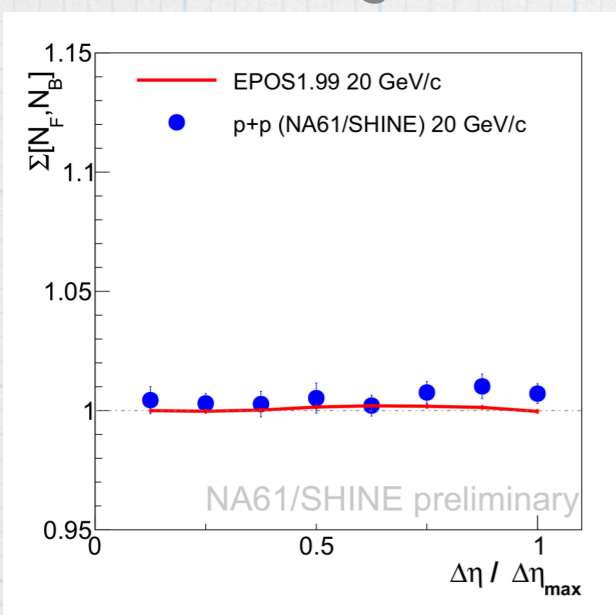
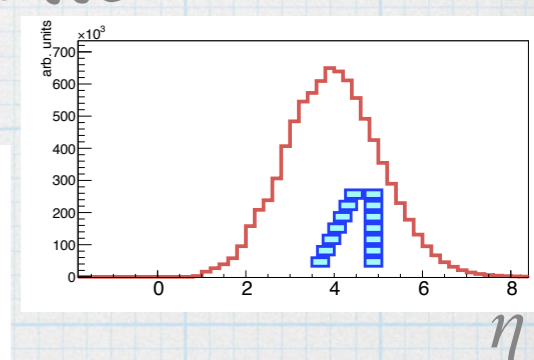
- \* Similar behaviour with  $\Delta\eta$
- \* No centrality dependence visible

# Going to lower energies



E.A., WPCF2017  
 E.A., EPJ Web Conf. 191:05002 (2018)  
 D.Prokhorova, EPJ Web Conf. 204:07013 (2019)  
 see also A. Seryakov, this workshop

- \* Fixed target experiment at the CERN SPS
- \* Have to take both rapidity windows in forward hemisphere
- \* Results for p+p and Be+Be collisions with the same increasing trend (consistent with EPOS)

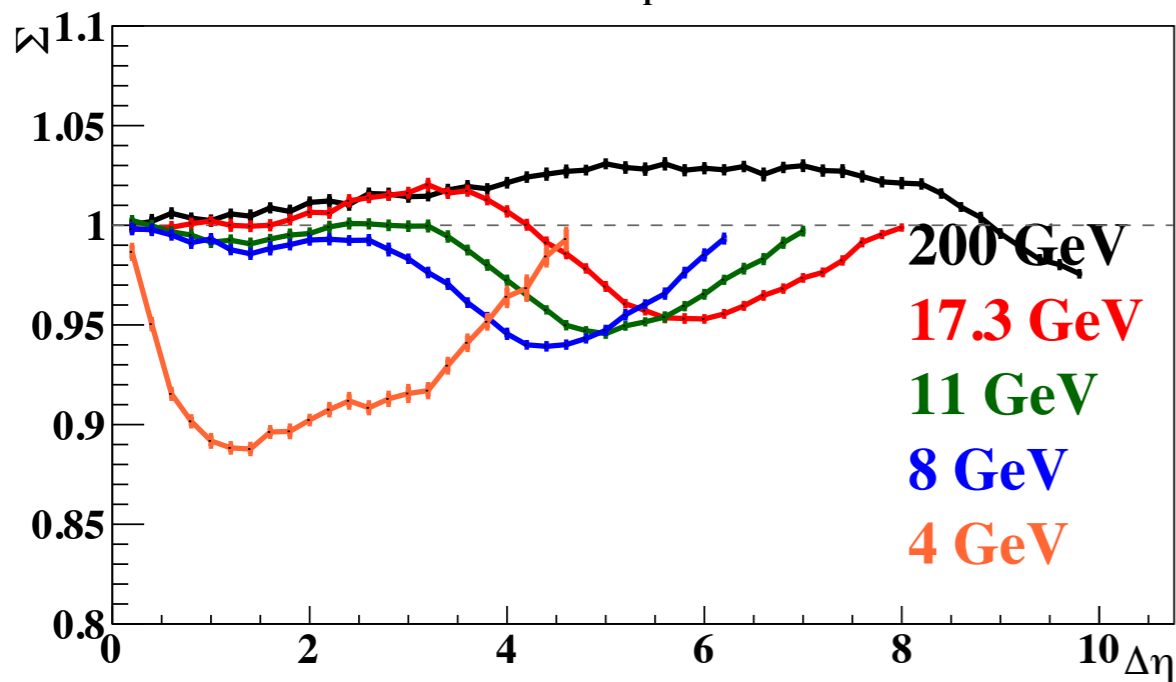


# RHIC->SPS->NICA



Test of strongly intensive quantity in SMASH event generator (transport code)

SMASH, p+p,  $0.3 < p_T < 1.5$  GeV/c,  $\delta\eta=0.2$



IM events for each energy

SMASH

J. Weil, et al., PRC 94: 054905 (2016)

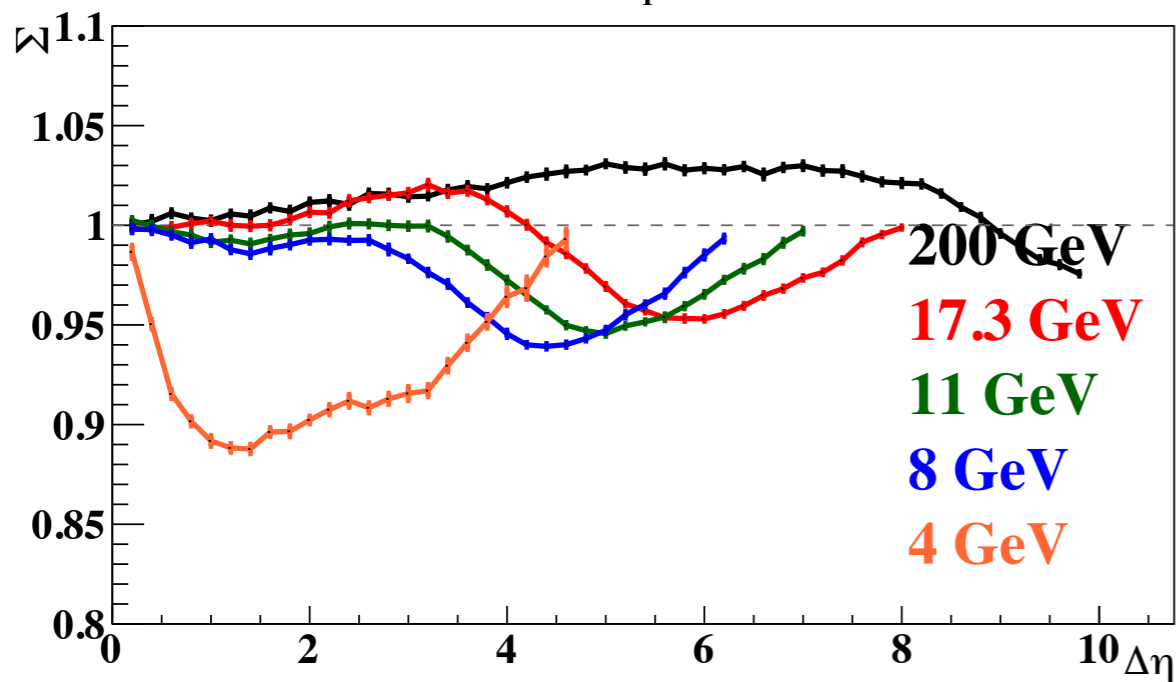


# RHIC->SPS->NICA

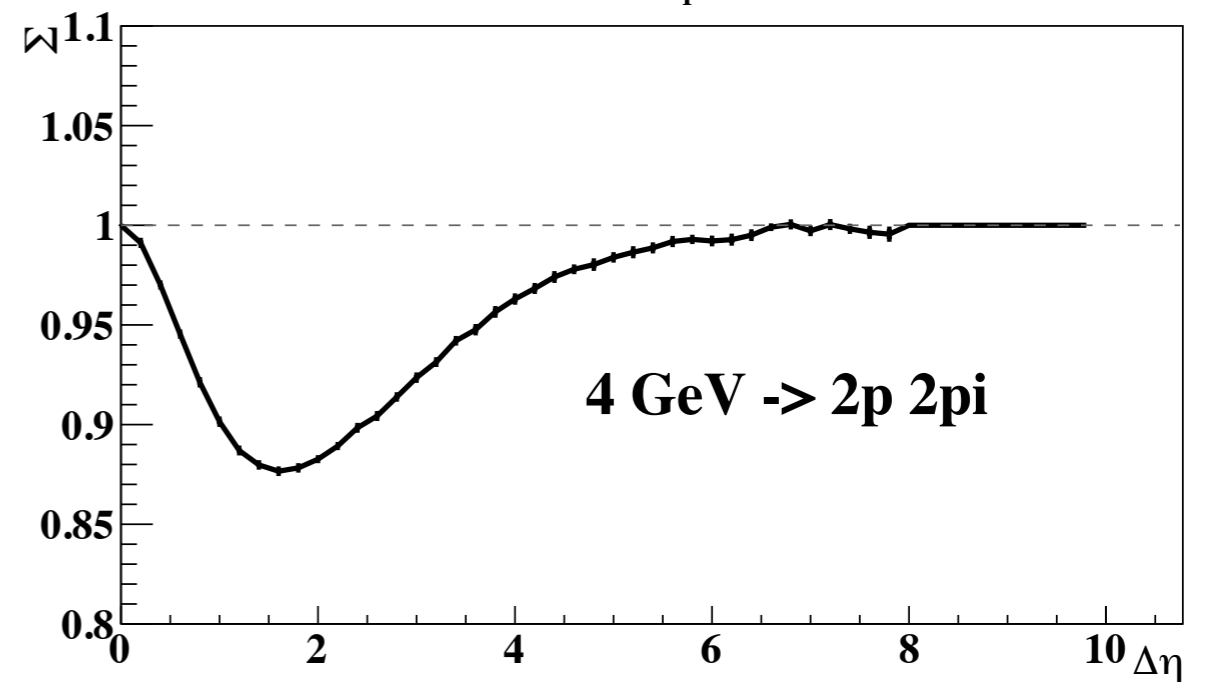


Test of strongly intensive quantity in SMASH event generator (transport code)

SMASH, p+p,  $0.3 < p_T < 1.5$  GeV/c,  $\delta\eta=0.2$



REGGAE, 4 GeV,  $0.3 < p_T < 1.5$  GeV/c,  $\delta\eta=0.2$



IM events for each energy

SMASH

J. Weil, et al., PRC 94: 054905 (2016)

Energy-momentum conservation code

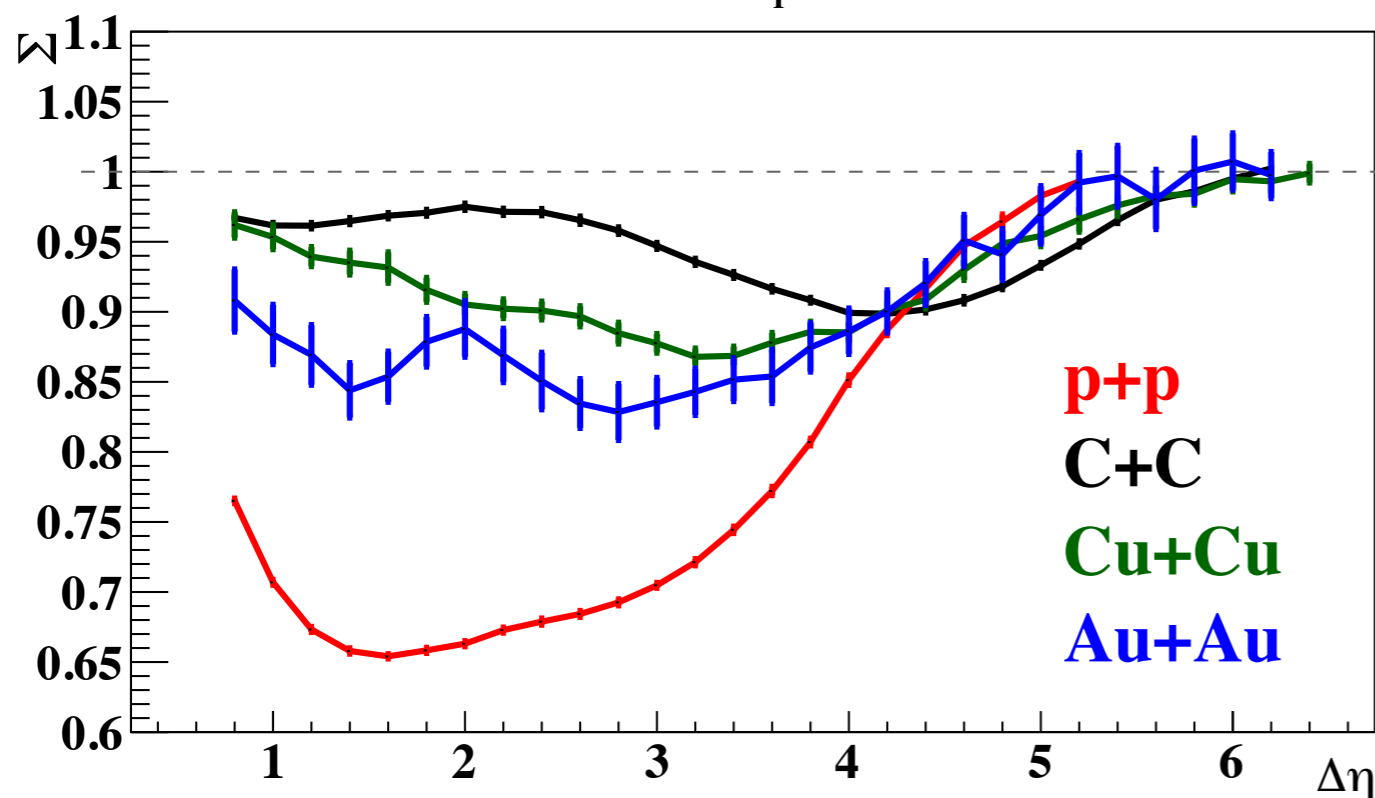
REGGAE

M. Meres, et al., Comp.Phys.Comm. 182:2561 (2011)



# NICA, system size scan?

SMASH, 4 GeV,  $0.3 < p_T < 1.5$  GeV/c,  $\delta\eta = 0.8$



$b=0$  fm

pp: 1M events

C+C: 300k

CuCu: 30k

AuAu: 5k

nuclei deformation and clustered structure are not taken into account

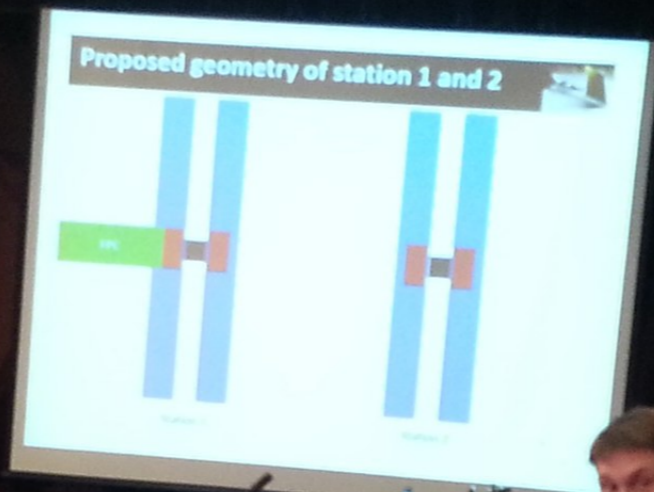
SMASH

J. Weil, et al., PRC 94: 054905 (2016)

# Conclusions and plans

- \* The string model enables to understand the main features of the behaviour of the strongly intensive observable  $\Sigma(n_F, n_B)$  at LHC energies
- \* Collectivity (string fusion) leads to deviation from the baseline of the model with independent sources. Creation of homogeneous long-range sources increases  $\Sigma(n_F, n_B)$ . Inhomogeneity in rapidity leads to decrease of  $\Sigma(n_F, n_B)$ .
- \* Modification of the  $\Sigma(n_F, n_B)$  behaviour at NICA collision energies (change from string decays to resonances decays). Role of global energy-momentum conservation.
- \* Plans - make use of MPDRoot, perform simulations in different event generators with the real detector geometry response

5 years ago





# Thank you!

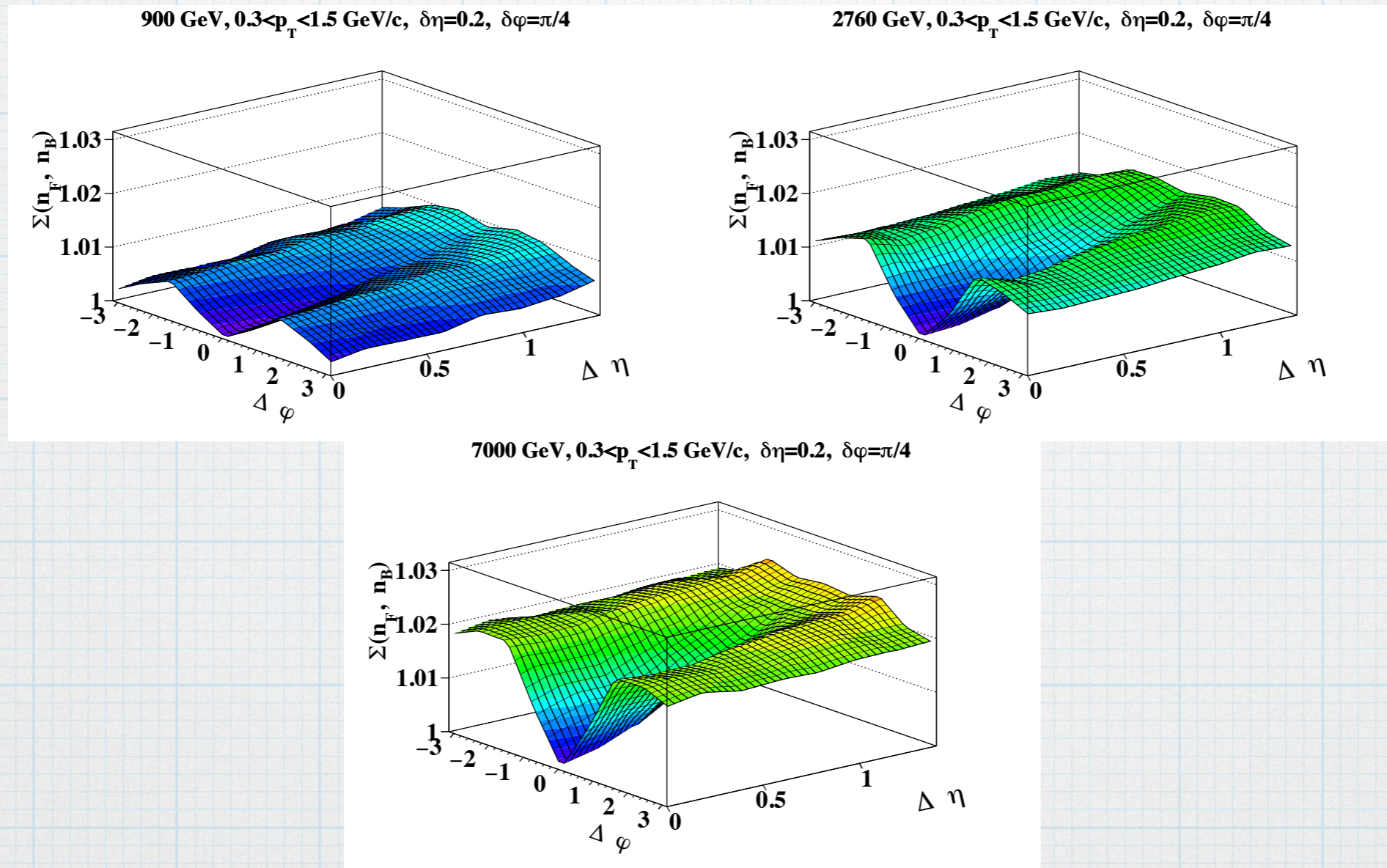
The reported study was funded by RFBR according to the research project No. 18-02-00041

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[evgeny.andronov@cern.ch](mailto:evgeny.andronov@cern.ch)

Back-up

# Strongly intensive quantity

With parametrisation of  $\Lambda(\Delta\eta, \Delta\phi)$  from **V. Vechernin, NPA 939:21 (2015)**

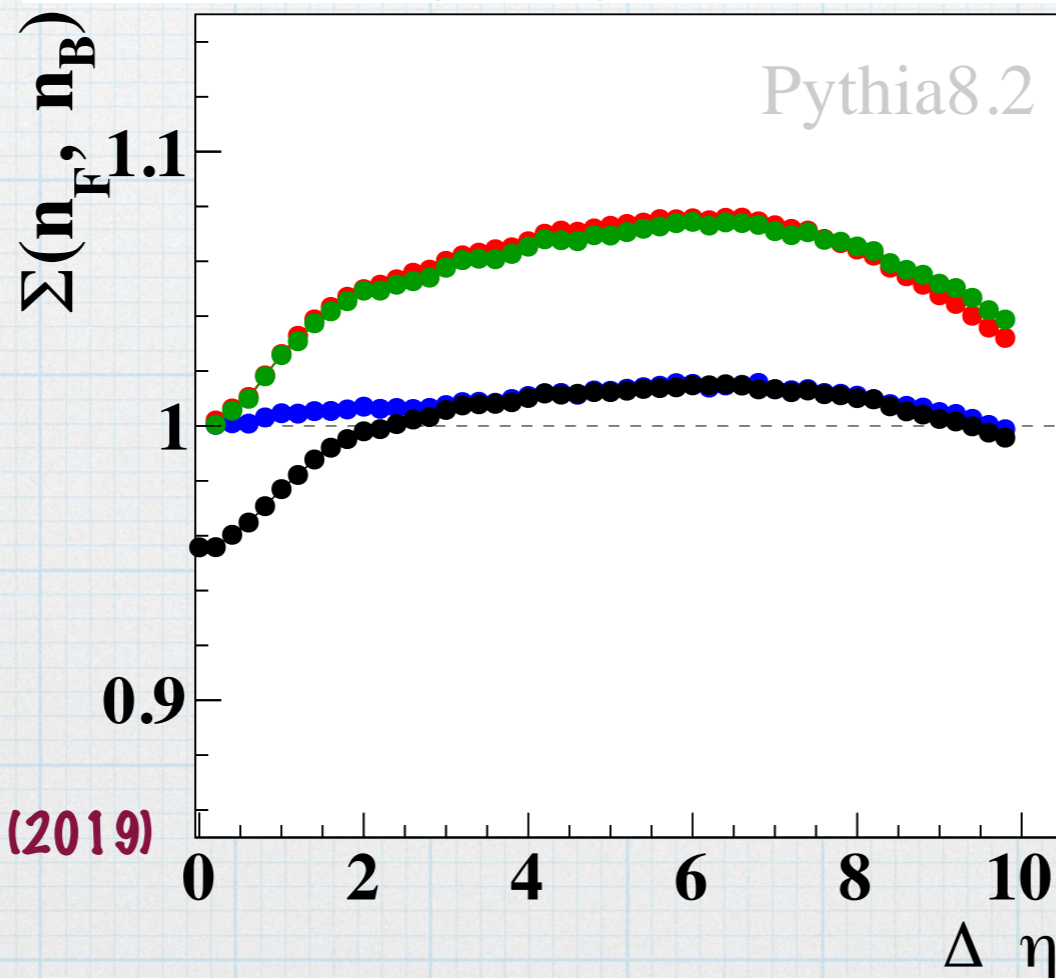


**E.A., V. Vechernin, EPJA 55(1):14 (2019)**

# Electric charge

$$\Sigma[n_F, n_B] = \Sigma[n_F^+, n_B^+] + \Sigma[n_F^-, n_B^+] - \Sigma[n_F^+, n_B^-]$$

- $\delta \eta=0.2; 900 \text{ GeV}; 0.3 < p_T < 1.5 \text{ GeV}/c, \text{all}_B - \text{all}_F$
- $\delta \eta=0.2; 900 \text{ GeV}; 0.3 < p_T < 1.5 \text{ GeV}/c, \text{pos}_B - \text{pos}_F$
- $\delta \eta=0.2; 900 \text{ GeV}; 0.3 < p_T < 1.5 \text{ GeV}/c, \text{neg}_B - \text{pos}_F$
- $\Sigma^{++}(\Delta \eta) + \Sigma^+(\Delta \eta) - \Sigma^+(\emptyset)$

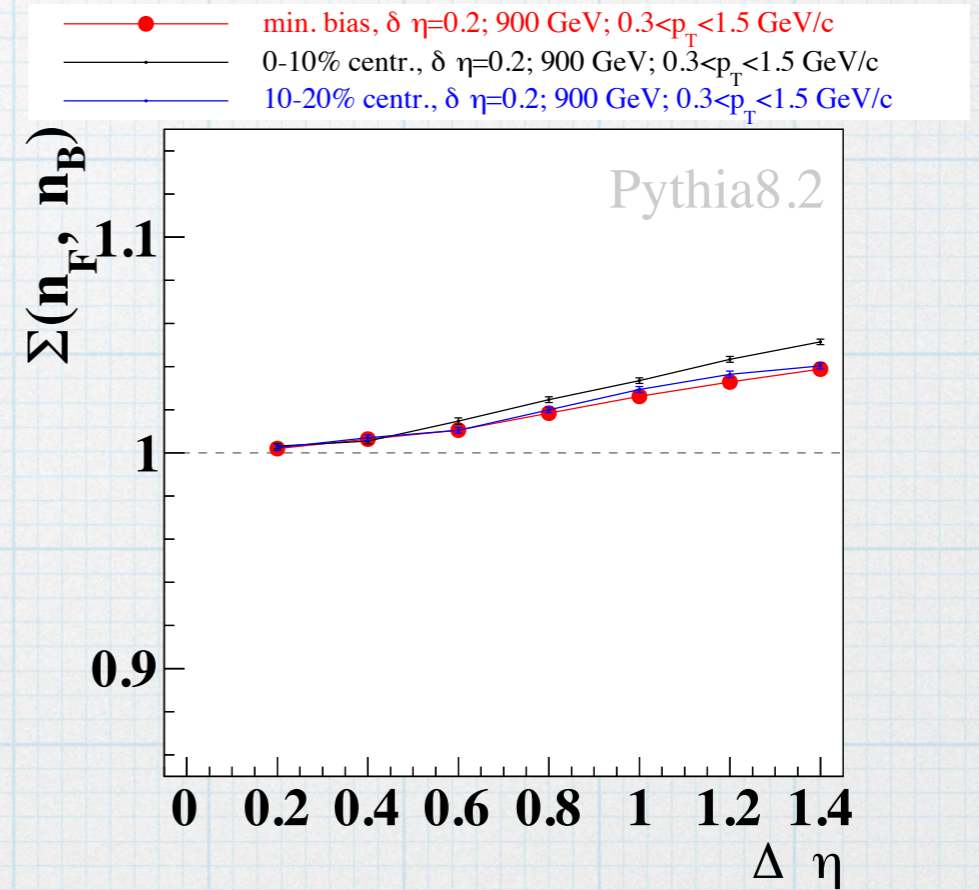
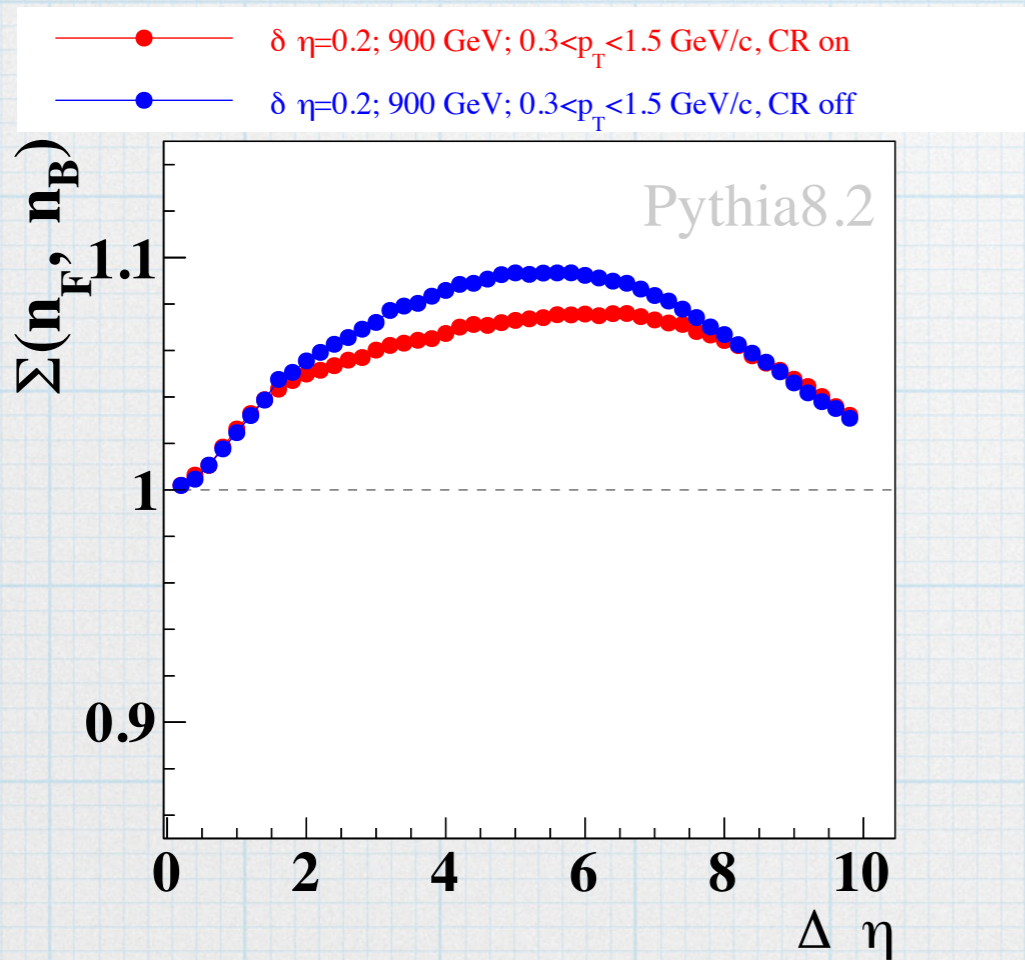


E.A., V. Vechernin, EPJA 55(1):14 (2019)



# PYTHIA tests

v.8.235



T. Sjöstrand, et al., *Comp.Phys.Comm.* 191:159 (2015)