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# Charming CPV

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# The start of charm CPV

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The big news from 3/2019

**LHCb found CPV in charm**

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- It is just the start of charm CPV
- We have many SM predictions to test
- We can probe BSM
- We can learn about QCD

# What next for charm CPV?

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In this talk

- Is the LHCb signal a hint for BSM?
  - The LHCb signal is well explained in the SM
  - We learn about QCD
- Can we make predictions for time-dependent CPV?
  - We predict approximate universality

# A few references

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Not the full list

- YG, Kagan, Nir, arXiv:hep-ph/0609178
- YG, Nir, Perez, arXiv:0904.0305
- Bobrowski, Lenz, Riedl, Rohrwild, arXiv:1002.4794
- Khodjamirian, Petrov, arXiv:1706.07780
- Chala, Lenz, Rusov, Scholtz, arXiv:1903.10490
- YG, Schacht, arXiv:1903.10952
- Kagan, Silvestrini, arXiv:2001.07207
- YG et al. in preparation

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# The effective 2-gen SM

# The 2-generation SM

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- Kaon and charm physics: only the first two generation are on-shell
- In many cases we can forget about the 3rd generation
- In some cases, like for CPV, we cannot do it
- The effective 2-generation model: We work with an EFT with two generation that is valid below  $m_b$
- There are two main effects for CPV
  - The  $2 \times 2$  CKM is not unitary
  - There are NR terms, like four Fermi operators

$$(\bar{s}_L \gamma_\mu d_L)(\bar{s}_L \gamma^\mu d_L)$$

# The effective $2 \times 2$ CKM

- We think about a  $2 \times 2$  CKM that is not unitary

$$V \approx \begin{pmatrix} \cos \theta_C & \sin \theta_C \\ -\sin \theta_C + \cos \theta_C \Delta e^{i\delta_{\text{KM}}} & \cos \theta_C + \sin \theta_C \Delta e^{i\delta_{\text{KM}}} \end{pmatrix}$$

- Non Unitarity (NU) is given by  $\Delta$

$$\Delta = |V_{cb}V_{ub}| \sim \lambda^5$$

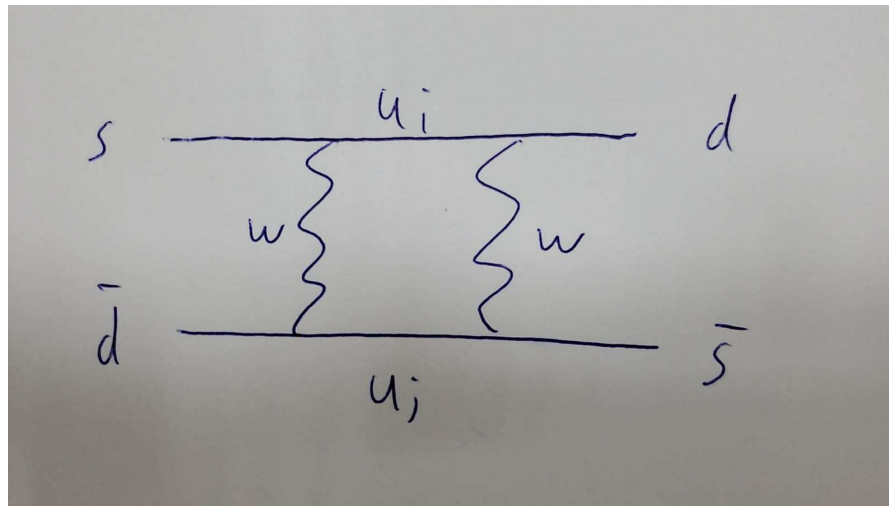
- We also define

$$\lambda_i = V_{ci}^* V_{ui}, \quad \lambda_s + \lambda_d = \Delta e^{i\delta_{\text{KM}}} \quad \lambda_s - \lambda_d = 2 \sin \theta_C \cos \theta_C$$

$$\varepsilon_{\text{NU}} \equiv \frac{\lambda_s + \lambda_d}{\lambda_s - \lambda_d} \approx 6 \times 10^{-4}$$

# The NR operators

- For example  $K - \bar{K}$  mixing from  $(\bar{s}_L \gamma_\mu d_L)(\bar{s}_L \gamma^\mu d_L)$
- In the SM it comes from



- Integrating out the  $W$  and top gives the NR operator
- The top contributions is CKM suppressed but GIM enhanced compared to the charm



# GIM vs CKM

3rd generation terms vs 2nd generation term

- CKM ratio:  $\frac{V_{ts}V_{td}}{V_{cs}V_{cd}} \sim \frac{V_{cb}V_{ub}}{V_{cs}V_{us}} \sim \lambda^4 \sim 10^{-3}$

- GIM ratio:  $K : \frac{m_t^2}{m_c^2} \sim 10^4 \quad D : \frac{m_b^2}{m_s^2} \sim 10^2$

- $K$ : GIM wins and thus NR is more important

- $D$ : CKM wins and thus NU is more important

In charm we only care about the NU of the  $2 \times 2$  CKM

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# CPV in charm

# The small parameters for charm

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All the observables depends on the following small parameters

- Non-unitarity of the  $2 \times 2$  CKM:  $\varepsilon_{\text{NU}} \sim 10^{-3}$
  - SU(3) flavor and U-spin breaking:  $\varepsilon_{\text{SU}(3)} \sim 0.2$
  - The Wolfenstein parameter of the CKM:  $\lambda \sim 0.2$
  - For example
    - $x_{\text{th}} \sim y_{\text{th}} \sim \lambda^2 \varepsilon_{\text{SU}(3)}^2 \sim 0.2\%$
    - $x_{\text{ex}} \sim y_{\text{ex}} \sim 0.5\%$
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We classify all CPV observables in terms of  $\lambda$ ,  $\varepsilon_{\text{SU}(3)}$ ,  $\varepsilon_{\text{NU}}$

# Time integrated CP asymmetry

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The time integrated CP asymmetry to leading order in  $x, y$

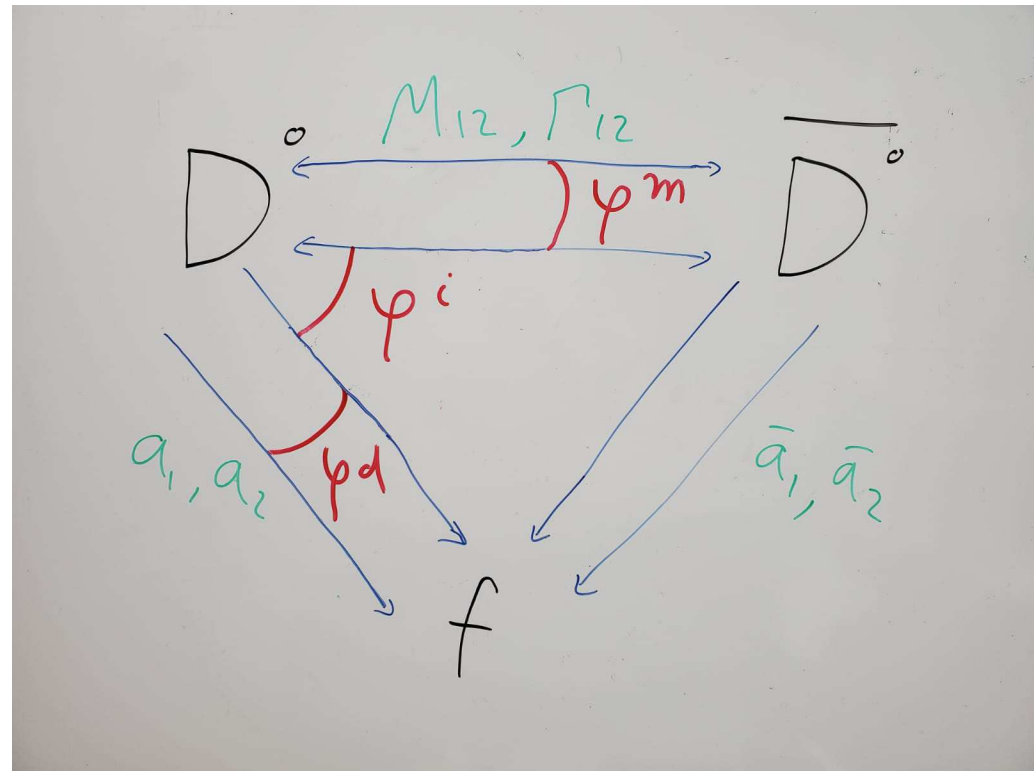
$$a_f \equiv \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})} \approx a_f^d + a^m + a_f^i$$

1.  $a_f^d \sim r_f \sin \varphi_f^d$
  2.  $a^m \sim y \sin \varphi^m$
  3.  $a_f^i \sim x \sin \varphi_f^i$
- $a^m$  is universal but  $a_f^d$  and  $a_f^i$  depend on  $f$
  - Using time dependence we can separate the three terms. Each is a separate observable

# What are the phases

All the weak phases depend on  $\varepsilon_{\text{NU}}$

1.  $a_f^d \sim r_f \sin \varphi_f^d$
2.  $a_f^m \sim y \sin \varphi_f^m$
3.  $a_f^i \sim x \sin \varphi_f^i$



# Magnitudes of the asymmetries

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## There is a pattern

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1.  $a_f^d$ . For SCS

$$a_f^d \sim O(1)_f \times \varepsilon_{\text{NU}} \sim 10^{-3}$$

2.  $a^m$ . Universal

$$a^m \sim y \frac{\varepsilon_{\text{NU}}}{\varepsilon_{\text{SU}(3)}} \sim \varepsilon_{\text{NU}} \times \varepsilon_{\text{SU}(3)} \sim 10^{-4}$$

3.  $a_f^i$ . Approximate universality

$$a_f^i \sim x \frac{\varepsilon_{\text{NU}}}{\varepsilon_{\text{SU}(3)}} \times \left[ 1 + O(\varepsilon_{\text{SU}(3)})_f \right] \sim 10^{-4} \pm 10^{-5}$$

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# Direct CPV in charm

# The LHCb Measurement

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$$\Delta A_{CP} \equiv a_{K^+K^-} - a_{\pi^+\pi^-}$$

Data show a signal that is above  $5\sigma$

$$\Delta A_{CP} = (-15.4 \pm 2.9) \times 10^{-4}$$

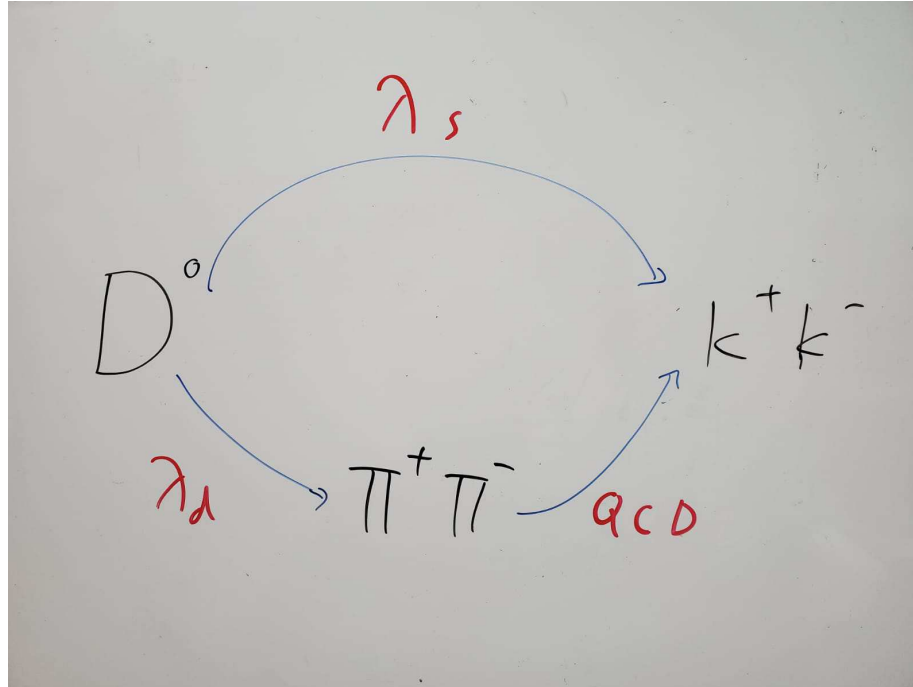
- Recall:  $a_f = a_f^d + a^m + a_f^i$
- Roughly speaking

$$\Delta A_{CP} \sim 2a_{KK}^d$$

- What the SM predicts?



# What interferes? Rescattering



- Interference of trees with  $\lambda_s$  and  $\lambda_d$
- We do not talk about penguins
- There are many more intermediate states

# The factors

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$$\frac{\mathcal{A}(D \rightarrow \text{“}\pi\pi\text{”} \rightarrow KK)}{\mathcal{A}(D \rightarrow KK)} = (r_{\text{QCD}} e^{i\delta}) (r_{\text{CKM}} e^{i\varphi})$$

$$a^d = 2(r_{\text{CKM}} \sin \varphi)(r_{\text{QCD}} \sin \delta)$$

- $r_{\text{QCD}}$ : ratio of rescattering amplitudes
- $\sin \delta = O(1)$ : strong phase
- $r_{\text{CKM}} = 1$ : ratio of CKM factors,  $|\lambda_d/\lambda_s|$
- $\sin \varphi \sim \varepsilon_{\text{NU}} \sim 10^{-3}$ : deviation from  $2 \times 2$  unitarity

$$a^d \sim \varepsilon_{\text{NU}} \times r_{\text{QCD}} \sim 10^{-3} \times r_{\text{QCD}}$$

# The ratios

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$$a^d \sim 10^{-3} \times r_{\text{QCD}} \quad r_{\text{QCD}} \sim \left| \frac{\mathcal{A}(D \rightarrow \text{“}\pi\pi\text{”} \rightarrow KK)}{\mathcal{A}(D \rightarrow KK)} \right|$$

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## What is $r_{\text{QCD}}$ ?

- Light Cone Sum Rules (LCSR)

Khodjamirian, Petrov, 2017

$$r_{\text{QCD}} \sim O\left(\frac{\alpha_s}{\pi}\right) \sim 10^{-1}$$

- Low energy QCD, rescattering is  $O(1)$

$$r_{\text{QCD}} \sim O(1)$$

# What we learn from direct CPV

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$$a_{\text{th}}^d \sim 10^{-3} \times r_{\text{QCD}} \quad a_{\text{ex}}^d \sim 10^{-3}$$

We conclude

- Within the SM the data imply  $r_{\text{QCD}} \sim 1$
- $r_{\text{QCD}} \sim 1$  from large rescattering agrees with the data
- It is hard to argue that the LHCb result requires BSM
- Yet, BSM can still be present
- There are more evidences that rescattering is  $O(1)$  in charm from  $D \rightarrow \pi\pi$  decays

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# CPV involving mixing

# What are the phases in mixing

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$$a_f \approx a_f^d + a^m + a_f^i$$

We care about  $a^m$  and  $a_f^i$

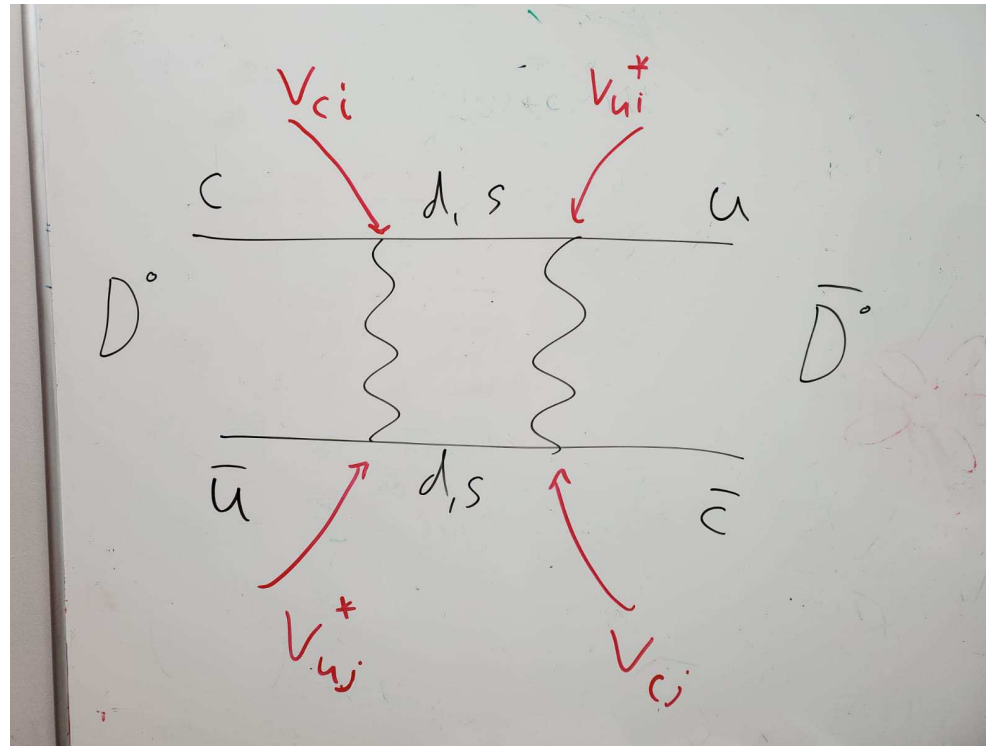
1.  $a^m \sim y \sin \varphi^m$  with

$$\sin^2 \varphi^m = \frac{x^2}{x^2 + y^2} \arg \left( \frac{\Gamma_{12}}{M_{12}} \right)$$

2.  $a_f^i \sim x \sin \varphi_f^i$  with  $\varphi_f^i$  is roughly the phase between the decay and the mixing amplitudes

# The mixing amplitude

$$M_{12} \propto \lambda_s^2 f_{ss} + 2\lambda_s \lambda_d f_{sd} + \lambda_d^2 f_{dd}$$



We cannot calculate  $f_{ij}$  reliably

# Evaluation of the mixing amplitude

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$$M_{12} \propto \lambda_s^2 f_{ss} + 2\lambda_s \lambda_d f_{sd} + \lambda_d^2 f_{dd}$$

- Same for  $\Gamma_{12}$  but with  $f_{ij} \rightarrow g_{ij}$
- The SU(3) properties are as follows

$$f_{ss} - f_{sd} \sim f_{dd} - f_{sd} \sim \varepsilon_{\text{SU}(3)} \quad f_{ss} + f_{dd} - 2f_{sd} \sim \varepsilon_{\text{SU}(3)}^2$$

- Recall

$$\lambda_s - \lambda_d \sim \lambda \quad \frac{\lambda_s + \lambda_d}{\lambda_s - \lambda_d} \sim \varepsilon_{\text{NU}}$$

- We get

$$M_{12}, \Gamma_{12} \sim \lambda^2 \left[ \varepsilon_{\text{SU}(3)}^2 + 2\varepsilon_{\text{SU}(3)}\varepsilon_{\text{NU}} + \varepsilon_{\text{NU}}^2 \right]$$



# The phases of the mixing

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$$M_{12}, \Gamma_{12} \sim \lambda^2 \left[ \varepsilon_{\text{SU}(3)}^2 + 2\varepsilon_{\text{SU}(3)}\varepsilon_{\text{NU}} + \varepsilon_{\text{NU}}^2 \right]$$

- The CPV phase enters with  $\varepsilon_{\text{NU}}$
- We can neglect the  $\varepsilon_{\text{NU}}^2$  term
- The phases are

$$\arg(M_{12}) \sim \arg(\Gamma_{12}) \sim \frac{\varepsilon_{\text{NU}}}{\varepsilon_{\text{SU}(3)}}$$

- The phases of the decays are  $O(\varepsilon_{\text{NU}})$
- The relevant phases are

$$\phi^m \sim \frac{\varepsilon_{\text{NU}}}{\varepsilon_{\text{SU}(3)}} \quad \phi_f^i \sim \frac{\varepsilon_{\text{NU}}}{\varepsilon_{\text{SU}(3)}} + (\varepsilon_{\text{NU}})_f \quad \phi_f^d \sim (\varepsilon_{\text{NU}})_f$$

# The predictions

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To leading order in SU(3) breaking the time dependent asymmetries are universal

$$\phi^m \sim \frac{\varepsilon_{\text{NU}}}{\varepsilon_{\text{SU}(3)}} \quad \phi_f^i \sim \frac{\varepsilon_{\text{NU}}}{\varepsilon_{\text{SU}(3)}} \left[ 1 + O(\varepsilon_{\text{SU}(3)})_f \right]$$

- Numerically, it is only a rough prediction
- Can be tested, hopefully soon
- We will learn something
  - If it fail, we found BSM
  - If it is confirmed, we will understand QCD better

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# Conclusion

# There is a pattern

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1.  $a_f^d$ . For SCS

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2.  $a^m$ . Universal

$$a^m \sim y \frac{\varepsilon_{\text{NU}}}{\varepsilon_{\text{SU}(3)}} \sim \varepsilon_{\text{NU}} \times \varepsilon_{\text{SU}(3)} \sim 10^{-4}$$

3.  $a_f^i$ . Approximate universality

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