



Recent results from charged-current semileptonic B decays at LHCb

Dawid Gerstel on behalf of the LHCb Collaboration

Aix Marseille Univ, CNRS/IN2P3, CPPM, Marseille, France

8-12 June '20, Conference on Flavour Physics and CP violation, Illa da Toxa, Spain

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Introduction

Motivation

- Precisely measure CPV in quark sector & test CKM unitarity (New Physics?)
- long-standing **discrepancy between inclusive and exclusive** measurements:

$$|V_{cb}|^{\text{incl}} = (42.19 \pm 0.78) \times 10^{-3}$$

► HFLAV Summer '19 incl. V_{cb}

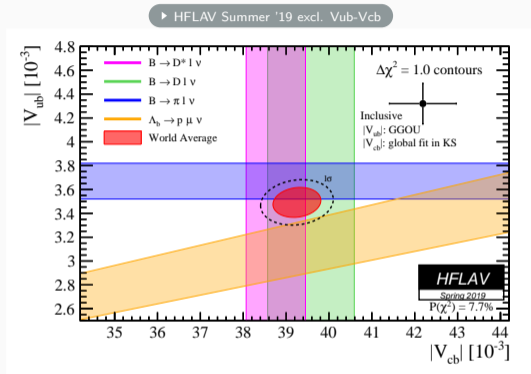
$$|V_{cb}|^{\text{excl}} = (39.25 \pm 0.56) \times 10^{-3}$$

► HFLAV Summer '19 excl. V_{ub} - V_{cb}

$\approx 3\sigma$ tension

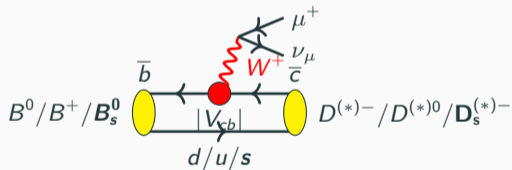
Analyses covered in this talk:

- Measurement of $|V_{cb}|$ with $B_s^0 \rightarrow D_s^{(*)-} \mu^+ \nu_\mu$ decays [► PhysRevD.101.072004](#) [► arXiv:2001.03225](#)
- Measurement of the shape of the $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu$ differential distribution [► arXiv:2003.08453](#)



**Measurement of $|V_{cb}|$ with
 $B_s^0 \rightarrow D_s^{(*)-} \mu^+ \nu_\mu$ decays**

- $\bar{b} \rightarrow \bar{c} \ell^+ \nu_\ell$ transitions: cleanest probe for $|V_{cb}|$
- So far $|V_{cb}|$ has been measured with B^0 and B^+ decays ▶ HFLAV Summer '19 excl. V_{ub} - V_{cb}
- Extending the study to B_s^0 decays might shed light on the discrepancy
- Advantages:
 - **Theoretically:** better precision in Lattice QCD (heavy spectator quark)
 - **Experimentally:** less contamination from D_s^{**} feeddown



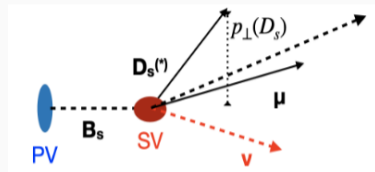
$$\frac{d^4\Gamma(B_{(s)} \rightarrow D_{(s)}^* \mu \nu)}{dw d\cos\theta_\mu d\cos\theta_D d\chi} = \frac{3m_B^3 m_{D^*}^2 G_F^2}{16(4\pi)^4} \eta_{EW}^2 |V_{cb}|^2 |\mathcal{A}(w, \theta_\mu, \theta_D, \chi)|^2,$$

$$\frac{d\Gamma(B_{(s)} \rightarrow D_{(s)} \mu \nu)}{dw} = \frac{G_F^2 m_D^3}{48\pi^3} (m_B + m_D)^2 \eta_{EW}^2 |V_{cb}|^2 (w^2 - 1)^{3/2} |\mathcal{G}(w)|^2.$$

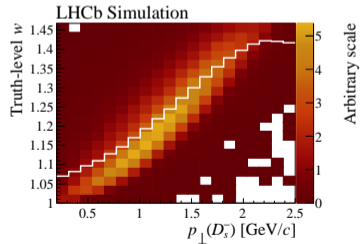
Target

From form-factors
(CLN & BGL)

- **Target-1:** Measure $|V_{cb}|$ and form factors of $B_s^0 \rightarrow D_s^{(*)-} (\rightarrow [K^+ K^-]_{\phi(1020)} \pi^-) \mu^+ \nu_\mu$ using $B^0 \rightarrow D^{(*)-} (\rightarrow [K^+ K^-]_{\phi(1020)} \pi^-) \mu^+ \nu_\mu$ as a normalisation.
- **Target-2** Measure $\mathcal{R}^{(*)} \equiv \frac{\mathcal{B}(B_s^0 \rightarrow D_s^{(*)-} \mu^+ \nu_\mu)}{\mathcal{B}(B^0 \rightarrow D^{(*)-} \mu^+ \nu_\mu)}$
- **Target-3** Determine $\mathcal{B}(B_s^0 \rightarrow D_s^{(*)-} \mu^+ \nu_\mu)$
- ✓ more precise in LQCD
- ✓ less background than $B^{0,+}$: less contamination from D_s^{**} (only $D_{s1}(2460)^-$ decays to $D_s^{*-} X$)
- ✓ suppress efficiency biases: same final state and similar kinematics between signal and normalisation
- recoil variable,
 $w = v_B \cdot v_{D^*} = (m_B^2 + m_{D^*}^2 - q^2)/(2m_B m_{D^*})$
- Use proxy variable: $p_\perp(D_{(s)})$ correlated with w

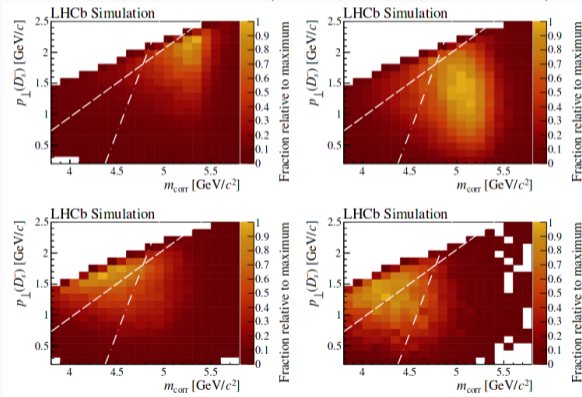


For $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu$:



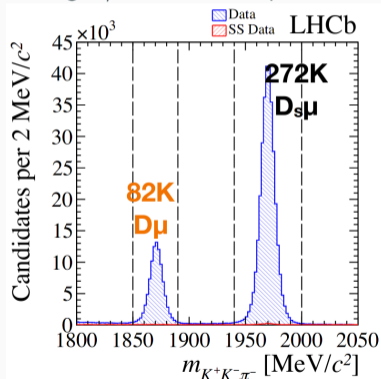
Exploiting the corrected mass, $m_{\text{corr}} \equiv \sqrt{m^2(D_s^- \mu^+) + p_{\perp}^2(D_s^- \mu^+) + p_{\perp}(D_s^- \mu^+)}$

Top: (left) $B_s^0 \rightarrow D_s^- \mu^+ \nu_{\mu}$ and (right) $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_{\mu}$

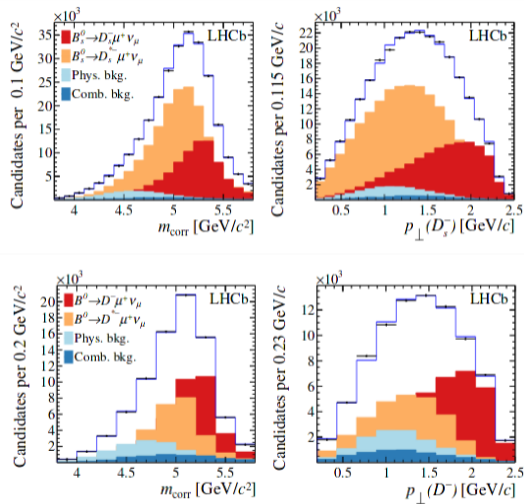


Bottom: (left) B_s^0 feed-down & doubly-charmed backgrounds, and (right) B^0 cross-feed & semitauonic B_s^0 decays

Signal/normalisation separation



- Simultaneous least-squares fit to $p_{\perp}(D_s^+)$ and m_{corr} for signal (top) and normalisation (bottom) from inclusive $D_{(s)}^-(\rightarrow K^+K^-\pi^-)\mu^+$



$\mathcal{R}^{(*)}$ is a free parameter in the fit, exploiting:

$$N_{\text{sig}}^{(*)} = N_{\text{ref}}^{(*)} \xi^{(*)} \mathcal{K}^{(*)} \underbrace{\frac{\mathcal{B}(B_s^0 \rightarrow D_s^{+(*)-} \mu^+ \nu_\mu)}{\mathcal{B}(B^0 \rightarrow D^{(*)-} \mu^+ \nu_\mu)}}_{\mathcal{R}^{(*)}},$$

where

$$\mathcal{K} \equiv \frac{f_s}{f_d} \frac{\mathcal{B}(D_s^- \rightarrow K^+ K^- \pi^-)}{\mathcal{B}(D^- \rightarrow K^+ K^- \pi^-)},$$

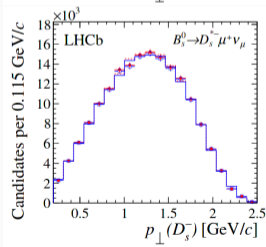
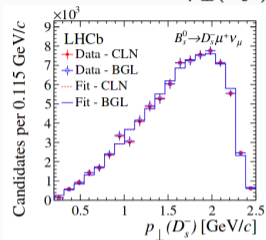
$$\mathcal{K}^* \equiv \frac{f_s}{f_d} \frac{\mathcal{B}(D_s^- \rightarrow K^+ K^- \pi^-)}{\mathcal{B}(D^{*-} \rightarrow D^- X) \mathcal{B}(D^- \rightarrow K^+ K^- \pi^-)},$$

Obtaining $|V_{cb}|$: expand the signal BF and $|V_{cb}|$ as a free parameter in the fit; use decay rate formula (slide 3)

$$N_{\text{sig}}^{(*)} = \frac{N_{\text{ref}}^{(*)} \xi^{(*)} \mathcal{K}^{(*)}}{\mathcal{B}(B^0 \rightarrow D^{(*)-} \mu^+ \nu_\mu)} \underbrace{\tau \int \frac{d\Gamma(B_s^0 \rightarrow D_s^{+(*)-} \mu^+ \nu_\mu)}{d\zeta} d\zeta}_{\mathcal{B}(B_s^0 \rightarrow D_s^{+(*)-} \mu^+ \nu_\mu)},$$

- There are several models (parametrisations) to describe the FF
- **BGL**: the most general; expresses FF with series expansions with arbitrary number of parameters
- **CLN**: the most used in the past; reduces the number of free parameters exploiting more theoretical constraints
- Recent theoretical works: CLN **could be problematic** at current precision
- → It's important to test the value of $|V_{cb}|$ obtained against the use of the **different parametrisations**
- This is done in the most recent results from Belle and BaBar, and it's done also in **this analysis**
- **See Backup** for details on the CLN&BGL formalism

CLN & BGL fits to $p_{\perp}(D_s^-)$



$$\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu) =$$

$$(2.49 \pm 0.12 \text{ (stat)} \pm 0.14 \text{ (syst)} \pm 0.16 \text{ (ext)}) \times 10^{-2},$$

$$\mathcal{B}(B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu) =$$

$$(5.38 \pm 0.25 \text{ (stat)} \pm 0.46 \text{ (syst)} \pm 0.30 \text{ (ext)}) \times 10^{-2},$$

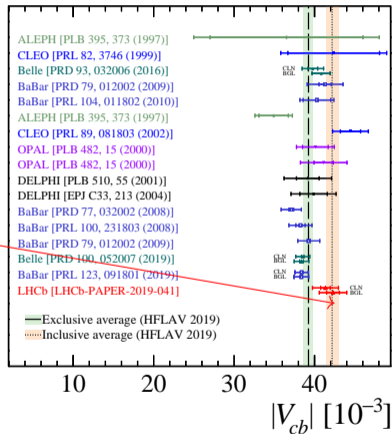
$$|V_{cb}|_{CLN} =$$

$$(41.4 \pm 0.6 \text{ (stat)} \pm 0.9 \text{ (syst)} \pm 1.2 \text{ (ext)}) \times 10^{-3}$$

$$|V_{cb}|_{BGL} =$$

$$(42.3 \pm 0.8 \text{ (stat)} \pm 0.9 \text{ (syst)} \pm 1.2 \text{ (ext)}) \times 10^{-3}$$

- CLN and BGL are compatible between each other accounting for their correlation; $|V_{cb}|$ in agreement with previous excl. & incl. determinations
- Uncertainty dominated by external inputs: f_s/f_d , B 's of B^0 and $D_{(s)}^-$ decays
- **First $|V_{cb}|$ exclusive determination from hadron collider and from B_s^0 decay**



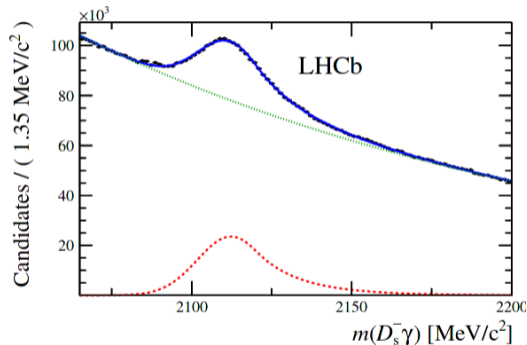
**Measurement of the shape of
the $B_S^0 \rightarrow D_S^{*-} \mu^+ \nu_\mu$ differential
distribution**

- **Motivation:** exclusive determination of $|V_{cb}|$ relies heavily on FF determination (esp. near zero-recoil, $w = 0$, *i.e.* maximum q^2 transfer); lack of experimental input; **crucial for $R(D_s^*)$**
- **Goal:** Measure leading hadronic form factors for the transition $B_s^0 \rightarrow D_s^{*-}$ using $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu$ decays; determine the differential decay rate in bins of w

- Fully reconstruct

$D_s^{*-} \rightarrow D_s^- (\rightarrow K^- K^+ \pi^-) \gamma$ and match with a μ^+

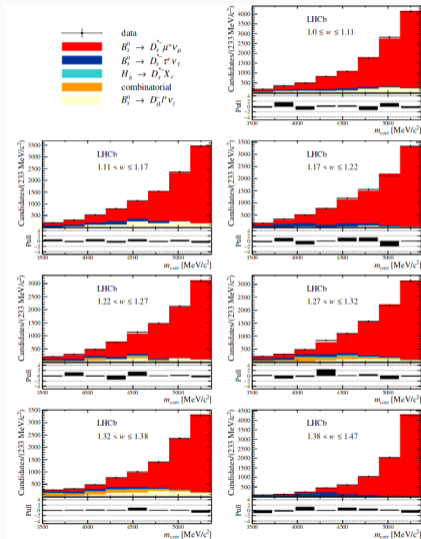
- Neural network used to separate γ from D_s^{*-} and π^0
- Gauss + power-tail for signal (D_s^{*-})
- exponential for background
- *sPlot* technique to remove combinatorial photons
- Backgrounds: semitauonic B_s^0 decays; double charm; feed-down from excited D_s^+ ; combinatorial



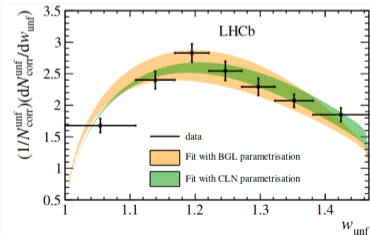
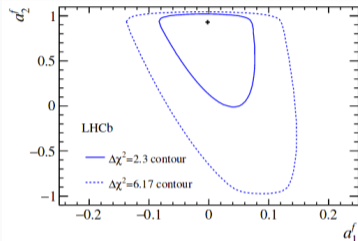
- Fit (binned max-likelihood) the corrected mass in 7 bins of w and extract the yield; fit efficiency-corrected decay distribution using CLN and BGL param.
- Templates from simulation

uncertainties:

Source	$\sigma(\rho^2)$	$\sigma(a_1^f)$	$\sigma(a_2^f)$
Simulation sample size	0.053	0.036	+0.04 -0.35
Sample sizes for efficiencies and corrections	0.020	0.016	+0.02 -0.16
SVD unfolding regularisation	0.008	0.004	-
Radiative corrections	0.004	-	-
Simulation FF parametrisation	0.007	0.005	-
Kinematic weights	0.024	0.013	-
Hardware-trigger efficiency	0.001	0.008	-
Software-trigger efficiency	0.004	0.002	-
D_s^- selection efficiency	-	0.008	-
D_s^- weights	0.002	0.014	-
External parameters in fit	0.024	0.002	0.04
Total systematic uncertainty	0.068	0.046	+0.06 -0.38
Statistical uncertainty	0.052	0.034	+0.05 -0.20



- **Leading FF using CLN and BGL** parametrisations: CLN:
 $\rho^2 = 1.16 \pm 0.05$ (stat) ± 0.07 (syst)
 BGL:
 $a_1^f = -0.002 \pm 0.034$ (stat) ± 0.046 (syst)
 BGL: $a_2^f = 0.93_{-0.20}^{+0.05}$ (stat) $_{-0.38}^{+0.06}$ (syst)
- Both results **within 1σ from HFLAV**, as expected by SU(3) symmetry between B^0 and B_s^0
- Result consistent with parametrisations from just discussed ▶ PhysRevD.101.072004
- Uncertainties dominated by systematics, mostly due to the simulation statistics
- **First unfolded normalised differential rate as a function of the recoil**

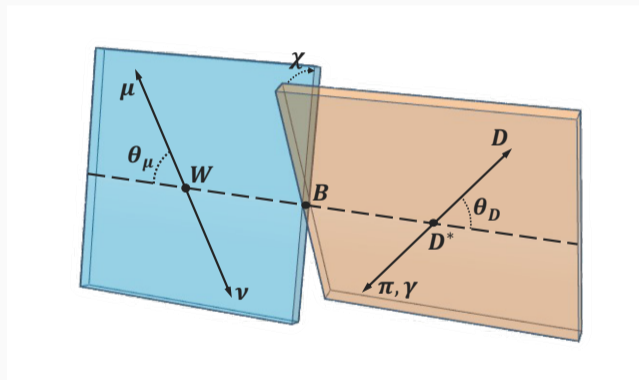


Conclusions and prospects

Conclusions and prospects

- Two recent papers from LHCb on the exclusive $|V_{cb}|$, form factors and the shape of the $B_s^0 \rightarrow D_s^{*+} \mu^- \bar{\nu}_\mu$ differential distribution in the recoil variable w
- For the **first time** $|V_{cb}|$ at hadron collider and first time with B_s^0
- $|V_{cb}|$ compatible with both exclusive and inclusive measurements
- CLN and BGL parametrisations give compatible results for (i) $|V_{cb}|$ and (ii) the differential distributions in w
- Similar techniques can be used for other b-hadrons:
“Measurement of $|V_{cb}|$ with $B^0 \rightarrow D^{*-} \mu^+ \nu_\mu$ decays at LHCb” ongoing

Backup



$$\frac{d^4\Gamma(B \rightarrow D^* \mu \nu)}{dw \, d\cos\theta_\mu \, d\cos\theta_D \, d\chi} = \frac{3m_B^3 m_{D^*}^2 G_F^2}{16(4\pi)^4} \eta_{EW}^2 |V_{cb}|^2 |\mathcal{A}(w, \theta_\mu, \theta_D, \chi)|^2, \quad (1)$$

$$|\mathcal{A}(w, \theta_\mu, \theta_D, \chi)|^2 = \sum_i^6 \mathcal{H}_i(w) k_i(\theta_\mu, \theta_D, \chi), \quad (2)$$

i	$\mathcal{H}_i(w)$	$k_i(\theta_\mu, \theta_D, \chi)$	
		$D^* \rightarrow D\gamma$	$D^* \rightarrow D\pi^0$
1	H_+^2	$\frac{1}{2}(1 + \cos^2\theta_D)(1 - \cos\theta_\mu)^2$	$\sin^2\theta_D(1 - \cos\theta_\mu)^2$
2	H_-^2	$\frac{1}{2}(1 + \cos^2\theta_D)(1 + \cos\theta_\mu)^2$	$\sin^2\theta_D(1 + \cos\theta_\mu)^2$
3	H_0^2	$2\sin^2\theta_D \sin^2\theta_\mu$	$4\cos^2\theta_D \sin^2\theta_\mu$
4	$H_+ H_-$	$4\sin^2\theta_D \sin^2\theta_\mu \cos 2\chi$	$-2\sin 2\theta_D \sin^2\theta_\mu \cos 2\chi$
5	$H_+ H_0$	$\sin 2\theta_D \sin\theta_\mu(1 - \cos\theta_\mu) \cos\chi$	$-2\sin 2\theta_D \sin\theta_\mu(1 - \cos\theta_\mu) \cos\chi$
6	$H_- H_0$	$-\sin 2\theta_D \sin\theta_\mu(1 + \cos\theta_\mu) \cos\chi$	$2\sin 2\theta_D \sin\theta_\mu(1 + \cos\theta_\mu) \cos\chi$

$$\frac{d^4\Gamma(B_{(s)} \rightarrow D_{(s)}^* \mu \nu)}{dw d\cos\theta_\mu d\cos\theta_D d\chi} = \frac{3m_B^3 m_{D^*}^2 G_F^2}{16(4\pi)^4} \eta_{EW}^2 |V_{cb}|^2 |\mathcal{A}(w, \theta_\mu, \theta_D, \chi)|^2,$$

$$|\mathcal{A}(w, \theta_\mu, \theta_D, \chi)|^2 = \sum_i^6 \mathcal{H}_i(w) k_i(\theta_\mu, \theta_D, \chi),$$

The helicity amplitudes are expressed by **three form factors**, $h_{A_1}(w)$, $R_1(w)$ and $R_2(w)$:

$$H_{\pm/0}(w) = 2 \frac{\sqrt{m_B m_{D^*}}}{m_B + m_{D^*}} (1 - r^2) (w + 1) (w^2 - 1)^{1/4} h_{A_1}(w) \tilde{H}_{\pm/0}(w),$$

with $r = m_{D^*}/m_B$ and

$$\tilde{H}_\pm(w) = \frac{\sqrt{1 - 2wr + r^2}}{1 - r} \left[1 \mp \sqrt{\frac{w - 1}{w + 1}} R_1(w) \right],$$

$$\tilde{H}_0(w) = 1 + \left[(w - 1) \left(1 - R_2(w) \right) \right] / (1 - r).$$

CLN (Caprini-Lellouch-Neubert) parametrisation uses based on Heavy Quark Effective Theory, dispersion relations, reinforced unitarity bounds

$$h_{A_1}(w) = h_{A_1}(1) \left[1 - 8\rho^2 z + (53\rho^2 - 15)z^2 - (231\rho^2 - 91)z^3 \right],$$

$$R_1(w) = R_1(1) - 0.12(w-1) + 0.05(w-1)^2,$$

$$R_2(w) = R_2(1) - 0.11(w-1) - 0.06(w-1)^2,$$

where the conformal variable z is defined as

$$z \equiv \frac{\sqrt{w+1} - \sqrt{2}}{\sqrt{w+1} + \sqrt{2}}.$$

The form factors depend only on **four parameters**: $h_{A_1}(1)$, ρ^2 , $R_1(1)$ and $R_2(1)$

- BGL (Boyd-Grinstein-Lebed) parametrisation follows from more general arguments based on dispersion relations, analyticity, and crossing symmetry
- FFs are written in terms of three functions, $f(w)$, $g(w)$ and $\mathcal{F}_1(w)$:

These functions are expanded as convergent power series of z as

$$\begin{aligned}
 h_{A_1}(w) &= \frac{f(w)}{\sqrt{m_B m_{D^*}}(1+w)}, \\
 R_1(w) &= (w+1)m_B m_{D^*} \frac{g(w)}{f(w)}, \\
 R_2(w) &= \frac{w-r}{w-1} - \frac{\mathcal{F}_1(w)}{m_B(w-1)f(w)}.
 \end{aligned}$$

$$\begin{aligned}
 f(z) &= \frac{1}{P_{1+}(z)\phi_f(z)} \sum_{n=0}^{\infty} b_n z^n, \\
 g(z) &= \frac{1}{P_{1-}(z)\phi_g(z)} \sum_{n=0}^{\infty} a_n z^n, \\
 \mathcal{F}_1(z) &= \frac{1}{P_{1+}(z)\phi_{\mathcal{F}_1}(z)} \sum_{n=0}^{\infty} c_n z^n.
 \end{aligned}$$

Parameters: series a_n , b_n and c_n

$$\frac{d\Gamma(B_{(s)} \rightarrow D_{(s)}\mu\nu)}{dw} = \frac{G_F^2 m_D^3}{48\pi^3} (m_B + m_D)^2 \eta_{EW}^2 |V_{cb}|^2 (w^2 - 1)^{3/2} |\mathcal{G}(w)|^2.$$

CLN:

$$\mathcal{G}(z) \leftarrow \mathcal{G}(0) \left[1 - 8\rho^2 z + (51\rho^2 - 10)z^2 - (252\rho^2 - 84)z^3 \right].$$

→ parameters: $\mathcal{G}(0)$ and ρ^2

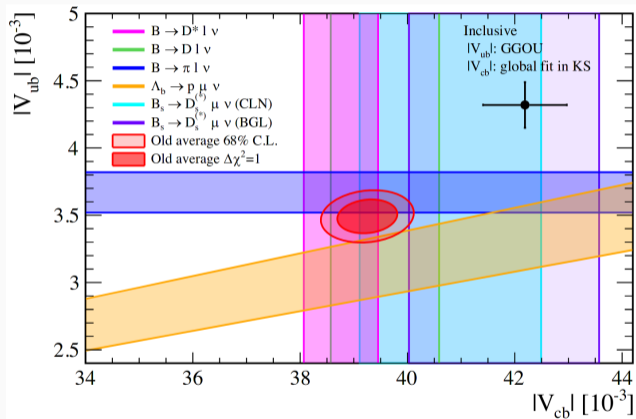
BGL:

$$|\mathcal{G}(z)|^2 = \frac{4r}{(1+r)^2} |f_+(z)|^2,$$

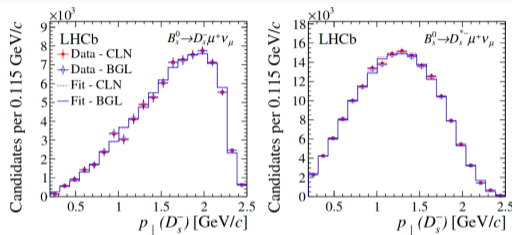
with $r = m_D/m_B$ and

$$f_+(z) = \frac{1}{P_{1-}(z)\phi(z)} \sum_{n=0}^{\infty} d_n z^n.$$

→ parameters: series d_n



Differential distributions for (left) $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$ and (right) $B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu$



(left) CLN and (right) BGL parameters:

Parameter	Value			
$ V_{cb} [10^{-3}]$	41.4	± 0.6	(stat) ± 1.2	(ext)
$\mathcal{G}(0)$	1.102	± 0.034	(stat) ± 0.004	(ext)
$\rho^2(D_s^-)$	1.27	± 0.05	(stat) ± 0.00	(ext)
$\rho^2(D_s^{*-})$	1.23	± 0.17	(stat) ± 0.01	(ext)
$R_1(1)$	1.34	± 0.25	(stat) ± 0.02	(ext)
$R_2(1)$	0.83	± 0.16	(stat) ± 0.01	(ext)

Parameter	Value			
$ V_{cb} [10^{-3}]$	42.3	± 0.8	(stat) ± 1.2	(ext)
$\mathcal{G}(0)$	1.097	± 0.034	(stat) ± 0.001	(ext)
d_1	-0.017	± 0.007	(stat) ± 0.001	(ext)
d_2	-0.26	± 0.05	(stat) ± 0.00	(ext)
b_1	-0.06	± 0.07	(stat) ± 0.01	(ext)
a_0	0.037	± 0.009	(stat) ± 0.001	(ext)
a_1	0.28	± 0.26	(stat) ± 0.08	(ext)
c_1	0.0031	± 0.0022	(stat) ± 0.0006	(ext)