

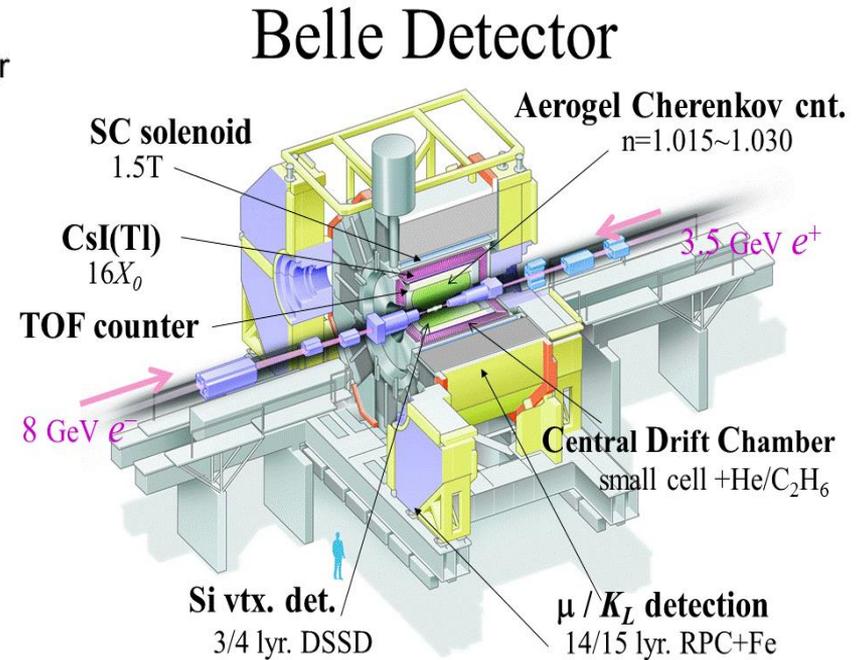
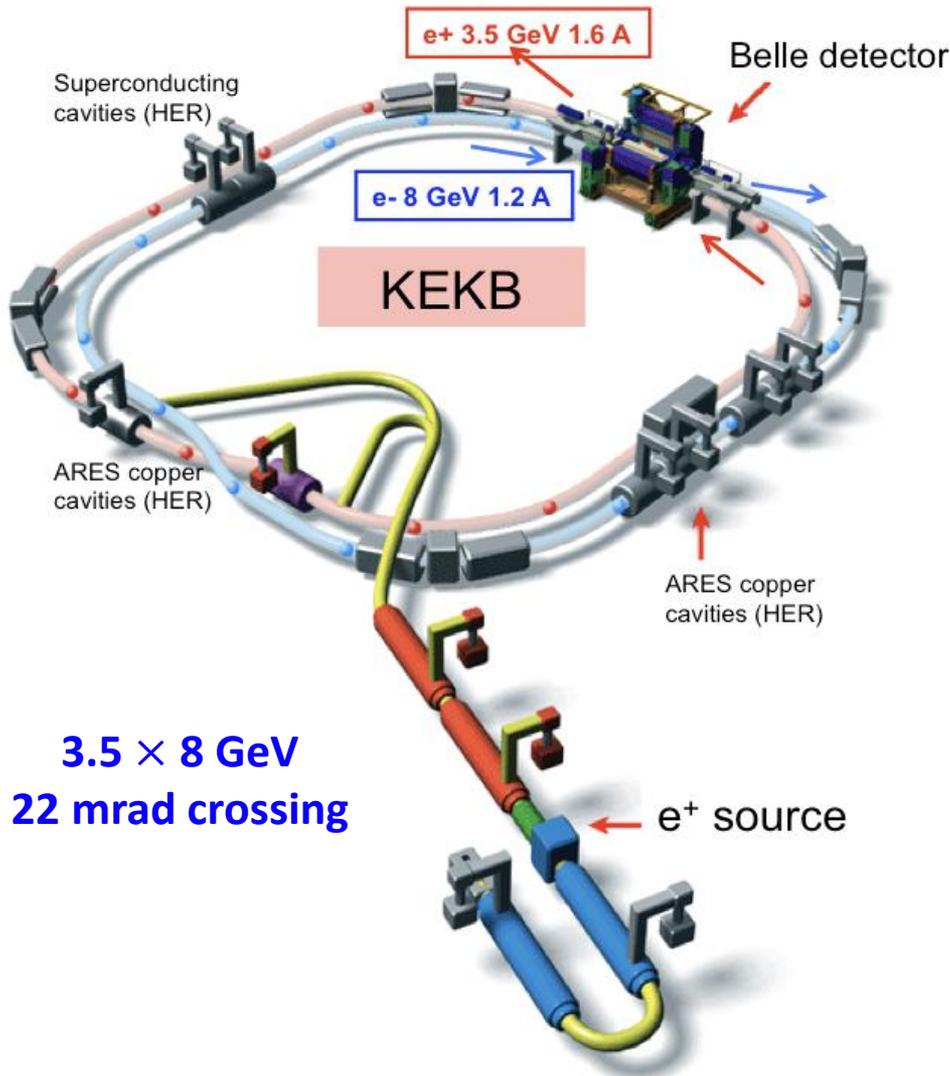


# Charmonium(like) states at Belle

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On behalf of Belle Collaboration**

**The 14<sup>th</sup> International Workshop on Heavy Quarkonium  
Mar 15~19, 2021**

# Belle experiment and data samples



Data taking: 1999 – 2010  
 On/off/Scan  $\Upsilon(nS)$  peaks  
 Total luminosity:  $980 \text{ fb}^{-1}$   
 772M  $B\bar{B}$  events @ $\Upsilon(4S)$

# Outline

- *Search for  $\eta_{c2}(1D)$  in B decays*
- *$Y(4626): e^+ e^- \rightarrow D_s^+ D_{s1}(2536)^- / D_s^+ D_{s2}^*(2573)^- + c.c.$*
- *Search for a doubly-charged DDK bound state*
- *Study of  $e^+ e^- \rightarrow K^+ K^- J/\psi$  via initial state radiation*
- *Summary*

# Search for $\eta_{c2}(1D)$ in $B$ decays

## Motivation:

[JHEP 05, 034 (2020)]

- Evidence for the  $\psi_2(1D)$  was first found by Belle in  $B^+ \rightarrow \psi_2(1D)(\rightarrow \chi_{c1}(\rightarrow J/\psi\gamma)\gamma)K^+$  [1].
- The masses of the  $\psi_2(1D)$  and  $\eta_{c2}(1D)$  are very close [2-5].
- The  $\eta_{c2}(1D)$  is expected to decay predominantly via E1 transition to  $h_c\gamma$  [6-9].
- The  $B(B^+ \rightarrow \eta_{c2}(1D)K^+) \times B(\eta_{c2}(1D) \rightarrow \gamma h_c)$  is expected to be  $1.0 \times 10^{-5}$  [9].

## Reconstruction:

- $B^+ \rightarrow \eta_{c2}(1D)K^+$ ,  $B^0 \rightarrow \eta_{c2}(1D)K_S^0$ ,  $B^0 \rightarrow \eta_{c2}(1D)\pi^-K^+$ , and  $B^+ \rightarrow \eta_{c2}(1D)\pi^+K_S^0$
- $\eta_{c2}(1D) \rightarrow h_c\gamma$  and  $h_c \rightarrow \eta_c\gamma$
- $\eta_c$  is reconstructed in the ten decay channels:  $K^+K_S^0\pi^-$ ,  $K^+K^-\pi^0$ ,  $K_S^0K_S^0\pi^0$ ,  $K^+K^-\eta$ ,  $K^+K^-K^+K^-$ ,  $\eta'(\rightarrow \eta\pi^+\pi^-)\pi^+\pi^-$ ,  $p\bar{p}$ ,  $p\bar{p}\pi^0$ ,  $p\bar{p}\pi^+\pi^-$ , and  $\Lambda\bar{\Lambda}$ .

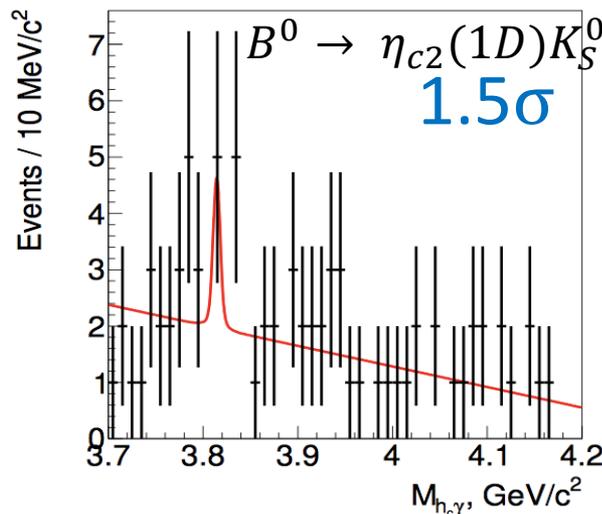
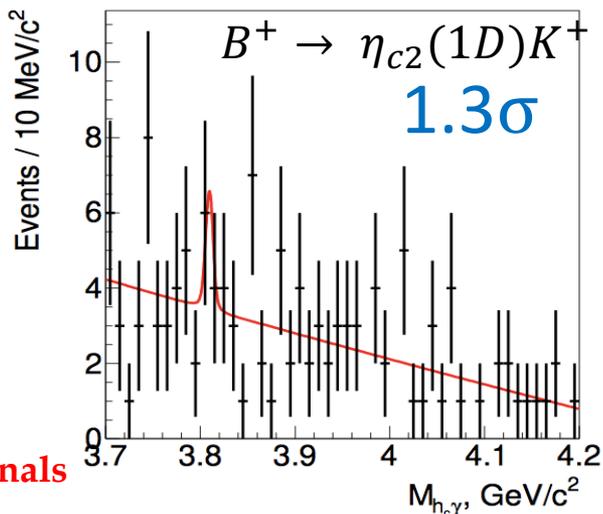
Data sample:  $772 \times 10^6 B\bar{B}$  pairs

## Analysis strategy:

- The multivariate analysis using the multilayer perceptron neural network.
- A global optimization is performed.

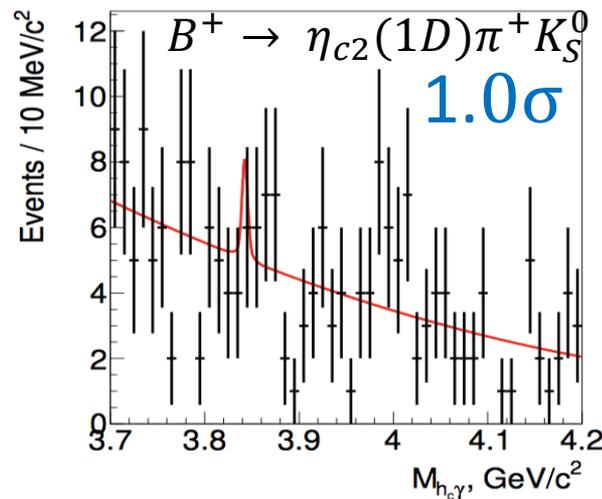
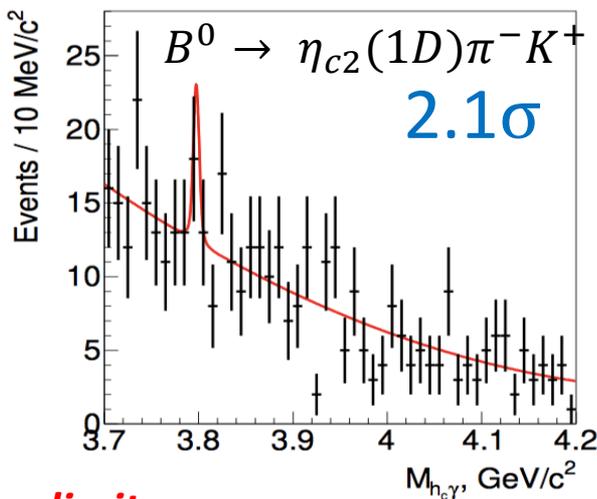
$$F_{\text{opt}} = \frac{\sum_i N_{\text{sig}}^{(i)}}{\frac{a}{2} + \sqrt{\sum_i N_{\text{bg}}^{(i)}}}$$

[1] PRL 111, 032001 (2013). [2] PRD 32, 189 (1985). [3] PRD 44, 2079 (1991). [4] PRD 52, 5229 (1995). [5] PRD 67, 014027 (2003). [6] PRL 89, 162002 (2002). [7] PRD 72, 054026 (2005). [8] PRD 80, 014001 (2009). [9] PRD 94, 034005 (2016).



$\eta_{c2}(1D)$  mass region:  
(3.795 – 3.845)  $\text{GeV}/c^2$

Signal shape: Breit-Wigner  $\otimes$  double asymmetric Gaussians  
Background: 1<sup>st</sup> or 2<sup>nd</sup> Polynomial



The  $\eta_{c2}(1D)$  width is fixed at 500 keV.  
[PRD 80 (2019) 014001]

No  $\eta_{c2}(1D)$  signals are observed.

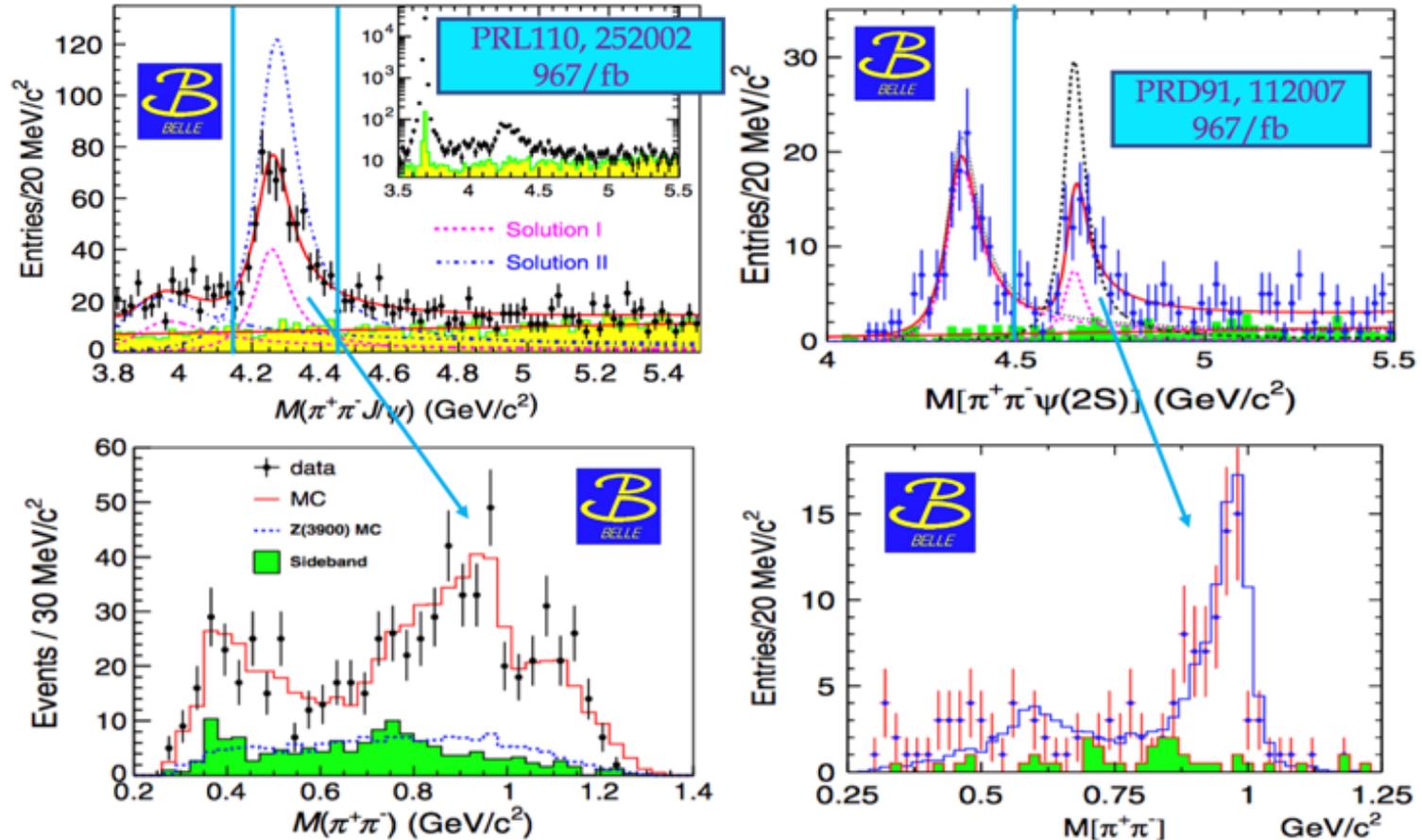
90% C.L. upper limits:

|  |                      |  |                      |
|--|----------------------|--|----------------------|
| $\mathcal{B}(B^+ \rightarrow \eta_{c2}(1D)K^+)\mathcal{B}(\eta_{c2}(1D) \rightarrow h_c\gamma)$      | $3.7 \times 10^{-5}$ | $\mathcal{B}(B^0 \rightarrow \eta_{c2}(1D)K_S^0)\mathcal{B}(\eta_{c2}(1D) \rightarrow h_c\gamma)$      | $3.5 \times 10^{-5}$ |
| $\mathcal{B}(B^0 \rightarrow \eta_{c2}(1D)\pi^-K^+)\mathcal{B}(\eta_{c2}(1D) \rightarrow h_c\gamma)$ | $1.0 \times 10^{-4}$ | $\mathcal{B}(B^+ \rightarrow \eta_{c2}(1D)\pi^+K_S^0)\mathcal{B}(\eta_{c2}(1D) \rightarrow h_c\gamma)$ | $1.1 \times 10^{-4}$ |

[theoretical prediction:  $\mathcal{B}(B^+ \rightarrow \eta_{c2}(1D)K^+) \times \mathcal{B}(\eta_{c2}(1D) \rightarrow \gamma h_c) = 1.0 \times 10^{-5}$ ]

$$Y(4626): e^+ e^- \rightarrow D_s^+ D_{s1} (2536)^- / D_s^+ D_{s2}^* (2573)^- + \text{c.c.}$$

## Motivation:



- $Y(4260) \rightarrow f_0(980)(\rightarrow \pi^+ \pi^-) J/\psi$ ,  $Y(4660) \rightarrow f_0(980)(\rightarrow \pi^+ \pi^-) \psi(2S)$   
 $f_0(980)$  has a  $s\bar{s}$  component, and  $J/\psi$  has a  $c\bar{c}$  component.
- It is natural to search for such  $Y$  states with quark component of  $(c\bar{s})(\bar{c}s)$ , e. g.,  
 $D_s \bar{D}_{s1}(2536)$  and  $D_s \bar{D}_{s2}^*(2573)$ .

# Analysis method

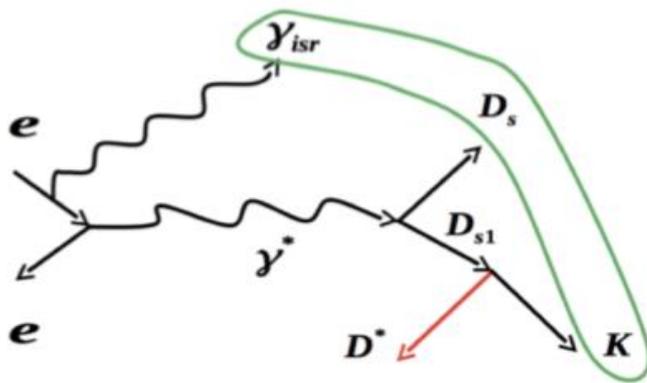
$$e^+e^- \rightarrow \gamma_{ISR} D_S^+ D_{s1}(2536)^- (\rightarrow \bar{D}^{*0} K^- / D^{*-} K_S^0)$$

We require full reconstruction of the  $\gamma_{ISR}$ ,  $D_S^+$ , and  $K^- / K_S^0$ .

- $D_S^+ \rightarrow \phi\pi^+, \bar{K}^{*0}K^+, K_S^0K^+, K^+K^-\pi^+\pi^0, K_S^0\pi^0K^+, K^{*+}K_S^0, \eta\pi^+$ , and  $\eta'\pi^+$
- For the signals, the spectrum of the mass recoiling against the  $D_S^+K^- \gamma_{ISR}$  system should be accumulated at the  $\bar{D}^{*0}/D^{*-}$  nominal mass.

$$M_{\text{rec}}(\gamma_{ISR} D_S^+ K^- / K_S^0) = \sqrt{(E_{\text{c.m.}}^* - E_{\gamma_{ISR} D_S^+ K^- / K_S^0}^*)^2 - (p_{\gamma_{ISR} D_S^+ K^- / K_S^0}^*)^2}$$

- To improve the  $M_{\text{rec}}(\gamma_{ISR})$  resolution,  $M_{\text{rec}}(\gamma_{ISR} D_S^+ K^- / K_S^0)$  is constrained to be the nominal mass of the  $\bar{D}^{*0}/D^{*-}$ .



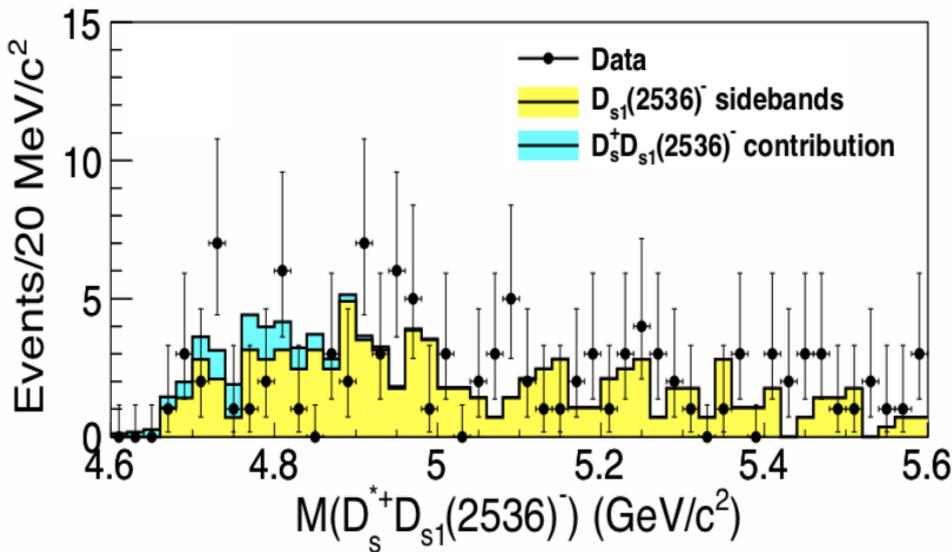
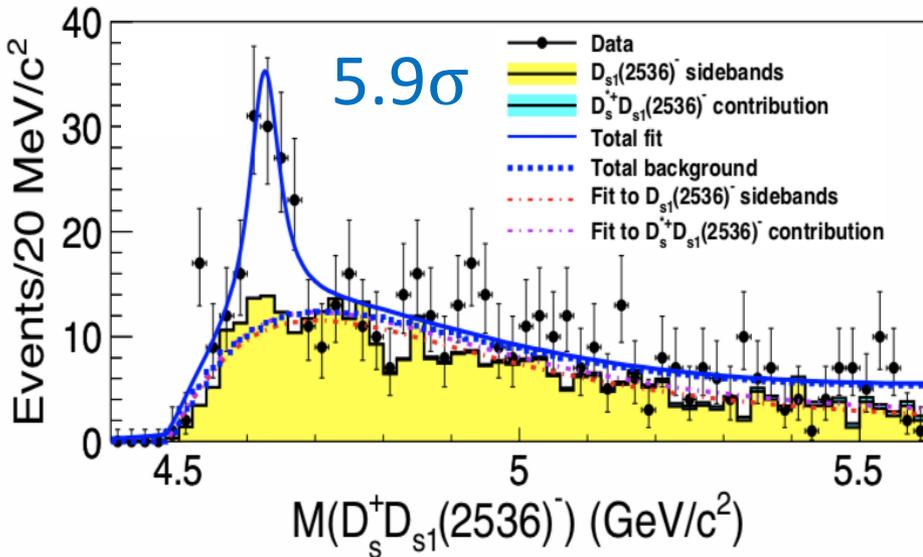
Data samples:

| $\sqrt{s}$ (GeV) | Luminosity (fb <sup>-1</sup> ) |
|------------------|--------------------------------|
| 10.52            | 89.5±1.3                       |
| 10.58            | 711±10                         |
| 10.867           | 121.4±1.7                      |
| Total            | 921.9±12.9                     |

- For the study of  $e^+e^- \rightarrow \gamma_{ISR} D_S^+ D_{s2}(2573)^- (\rightarrow \bar{D}^0 K^-)$ , the same analysis method is used.

# $M(D_s^+ D_{s1}(2536)^-)$

[PRD 100, 111103(R) (2019)]



An unbinned simultaneous likelihood fit:

- **Signal:** a  $BW$  convolved with a Gaussian function, then multiplied by an efficiency function
- **A non-resonant contribution:** a two-body phase space form
- $D_{s1}(2536)^-$  mass sidebands: a threshold function
- $e^+e^- \rightarrow D_s^{*+} D_{s1}(2536)^-$  background contribution: a threshold function

$$M = (4625.9^{+6.2}_{-6.0}(\text{stat.}) \pm 0.4(\text{syst.}) \text{ MeV}/c^2$$

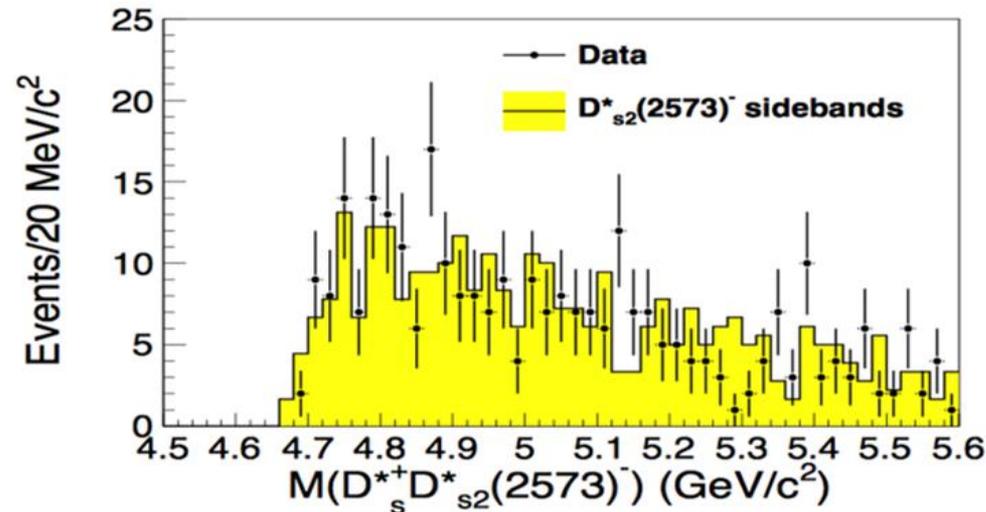
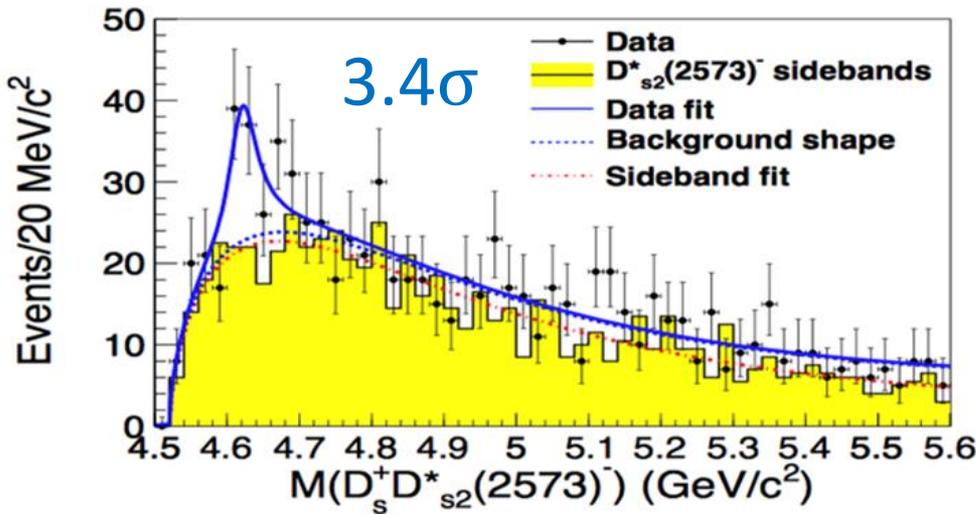
$$\Gamma = (49.8^{+13.9}_{-11.5}(\text{stat.}) \pm 4.0(\text{syst.}) \text{ MeV}$$

$$\Gamma_{ee} \times \mathcal{B}(Y \rightarrow D_s^+ D_{s1}(2536)^-) \times \mathcal{B}(D_{s1}(2536)^- \rightarrow \bar{D}^{*0} K^-) = (14.3^{+2.8}_{-2.6}(\text{stat.}) \pm 1.5(\text{syst.}) \text{ eV}$$

- One possible background is from  $e^+e^- \rightarrow D_s^{*+} (\rightarrow D_s^+ \gamma) D_{s1}(2536)^-$ .

# $M(D_s^+ D_{s2}^*(2573)^-)$

[PRD 101, 091101(R) (2020)]



An unbinned simultaneous likelihood fit:

- **Signal:** a BW convolved with a Gaussian function, then multiplied by an efficiency function
- **A non-resonant contribution:** a two-body phase space form
- **$D_{s2}^*(2573)^-$  mass sidebands:** a threshold function

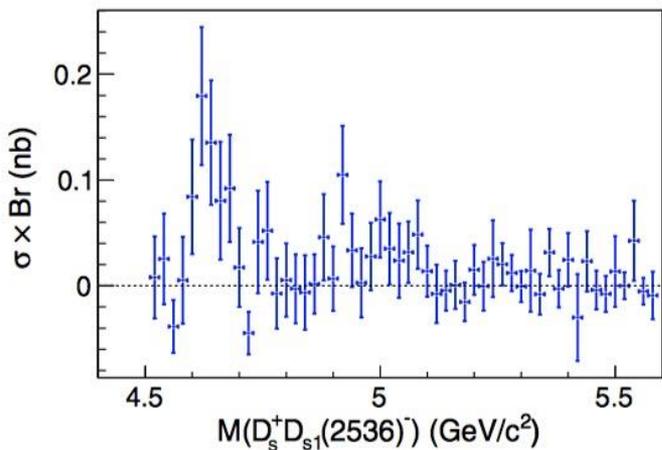
$$M = (4619.8_{-8.0}^{+8.9}(\text{stat.}) \pm 2.3(\text{syst.}) \text{ MeV/c}^2$$

$$\Gamma = (47.0_{-14.8}^{+31.3}(\text{stat.}) \pm 4.6(\text{syst.}) \text{ MeV}$$

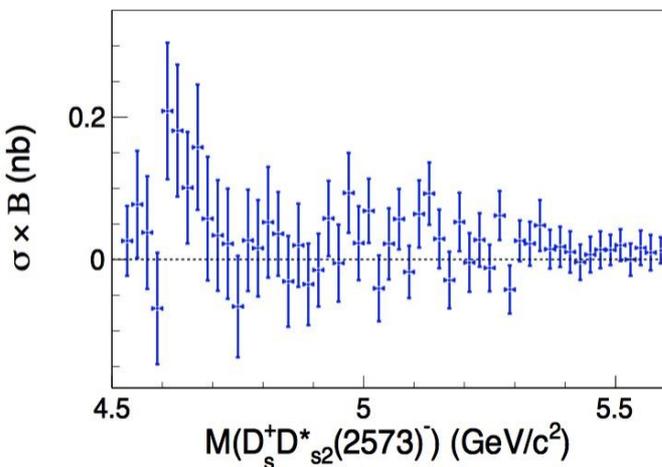
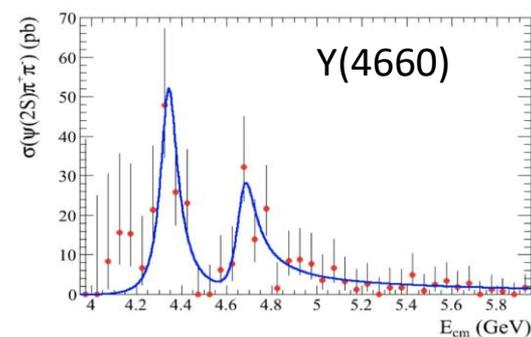
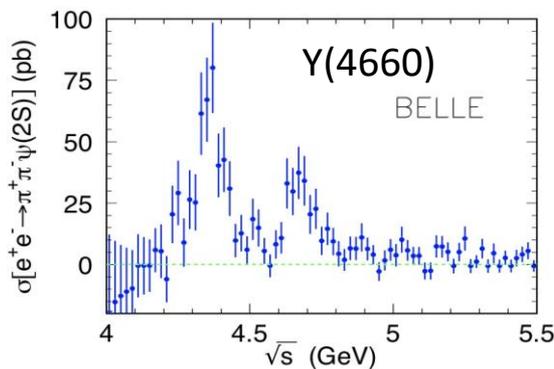
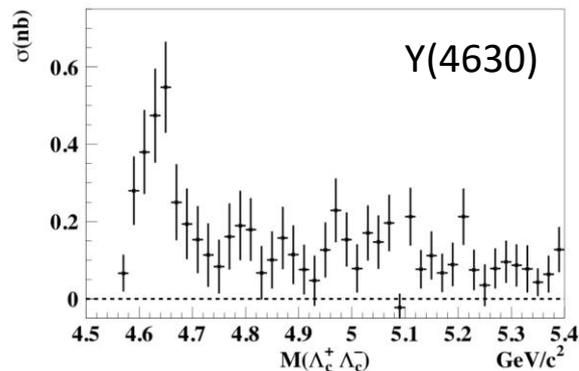
$$\Gamma_{ee} \times \mathcal{B}(Y \rightarrow D_s^+ D_{s2}^*(2573)^-) \times \mathcal{B}(D_{s2}^*(2573)^- \rightarrow \bar{D}^0 K^-) = (14.7_{-4.5}^{+5.9}(\text{stat.}) \pm 3.6(\text{syst.}) \text{ eV}$$

- One possible background is from  $e^+ e^- \rightarrow D_s^{*+} (\rightarrow D_s^+ \gamma) D_{s2}^*(2573)^-$ .

# Y(4626)=Y(4630)=Y(4660)?



$$\sigma(e^+e^- \rightarrow D_s^+ D_{s1}(2536)^-) \times B(D_{s1}(2536) \rightarrow \bar{D}^0 K^-)$$

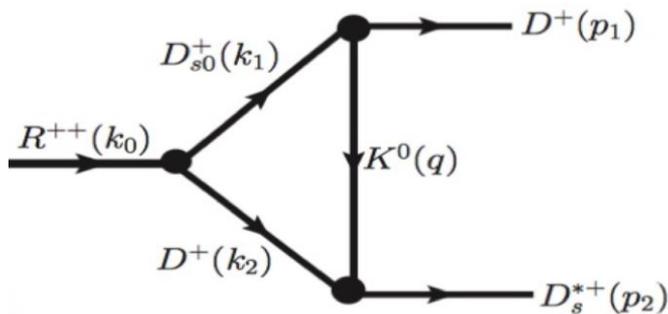


$$\sigma(e^+e^- \rightarrow D_s^+ D_{s2}^*(2573)^-) \times B(D_{s2}^*(2573) \rightarrow \bar{D}^0 K^-)$$

| Experiment                       | Mass (MeV)             | Width (MeV)              |
|----------------------------------|------------------------|--------------------------|
| Belle, $\Lambda_c^+ \Lambda_c^-$ | $4634^{+8+5}_{-7-8}$   | $92^{+40+10}_{-24-21}$   |
| Belle, $\pi^+ \pi^- \psi(2S)$    | $4652 \pm 10 \pm 8$    | $68 \pm 11 \pm 1$        |
| BaBar, $\pi^+ \pi^- \psi(2S)$    | $4669 \pm 21 \pm 3$    | $104 \pm 48 \pm 10$      |
| Belle, $D_s^+ D_{s1}(2536)^-$    | $4626^{+7}_{-7} \pm 1$ | $49.8^{+14}_{-12} \pm 4$ |
| Belle, $D_s^+ D_{s2}^*(2573)^-$  | $4620^{+9}_{-9} \pm 3$ | $47.0^{+32}_{-15} \pm 5$ |

# Search for a doubly-charged $DDK$ bound state

- A doubly-charged and doubly-charmed molecule  $R^{++}$  decays to  $D^+ D_s^{*+}$  with modest rates according to Refs. [PRD 99, 076017 (2019), PRD 101, 014022 (2020)].
- The mass of  $R^{++}$  is predicted to be in the range of 4.13 to 4.17  $\text{GeV}/c^2$ ; the width is (2.30–2.49) MeV.
- A state decaying to  $D^+ D_s^{*+}$  is also a good candidate for a doubly-charged tetraquark according to Ref. [PRL 119, 202001 (2017)].

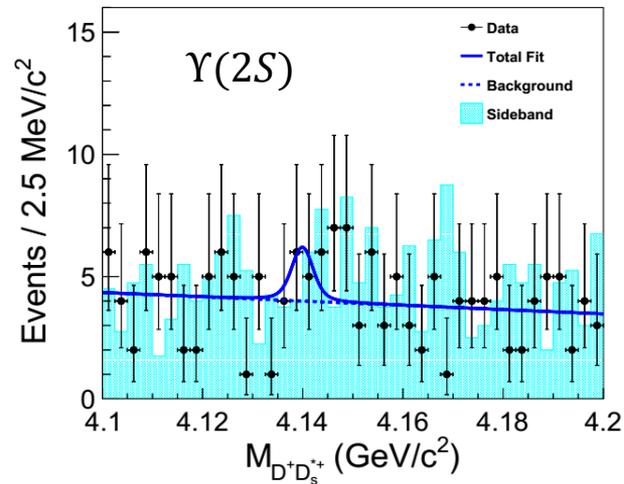
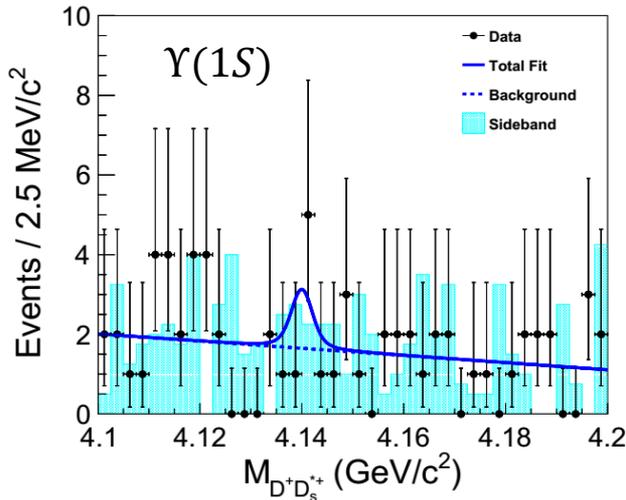


- $D^+ \rightarrow K^- \pi^+ \pi^- / K_S^0 (\rightarrow \pi^+ \pi^-) \pi^+$
- $D_s^{*+} \rightarrow D_s^+ \gamma$
- $D_s^+ \rightarrow \phi \pi^+ / \bar{K}^{*0} K^-$

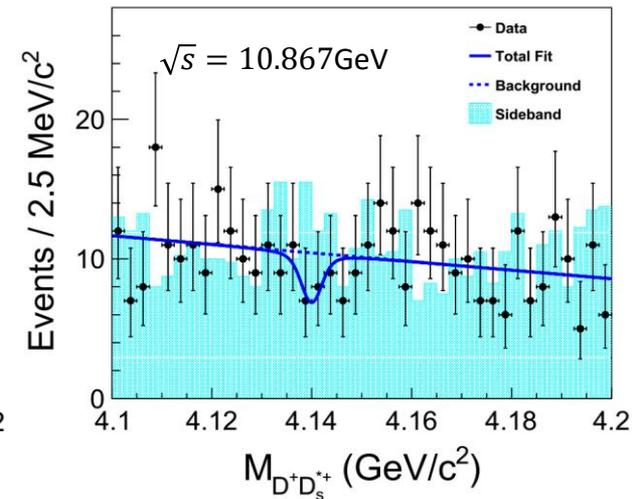
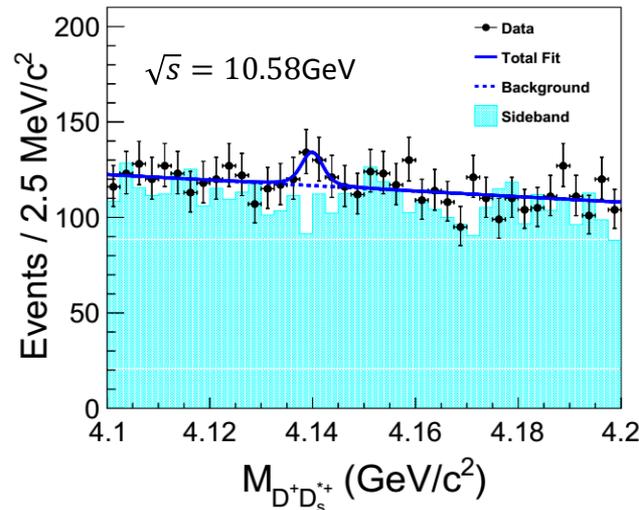
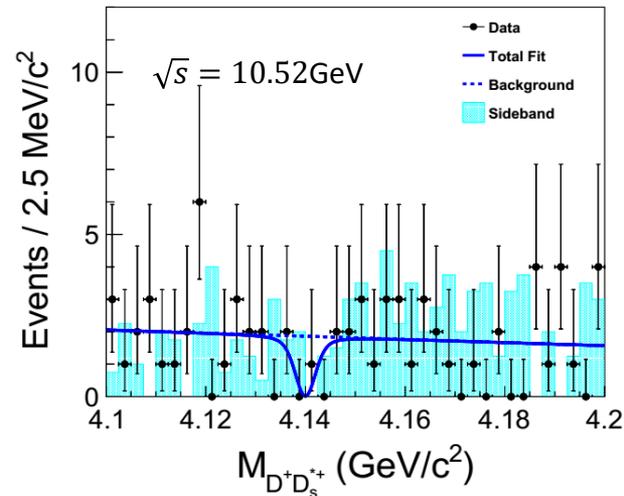
## Data samples:

| $\sqrt{s}$ (GeV) | Luminosity ( $\text{fb}^{-1}$ ) | Events                |
|------------------|---------------------------------|-----------------------|
| 9.46 [Y(1S)]     | $5.74 \pm 0.09$                 | (102 $\pm$ 3) million |
| 10.023 [Y(2S)]   | $24.91 \pm 0.35$                | (158 $\pm$ 4) million |
| 10.52            | $89.5 \pm 1.3$                  | -                     |
| 10.58 [Y(4S)]    | $711 \pm 10$                    | -                     |
| 10.867 [Y(5S)]   | $121.4 \pm 1.7$                 | -                     |

# $M(D^+D_s^{*+})$

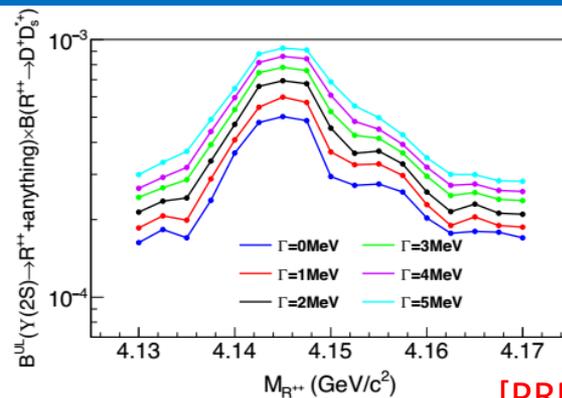
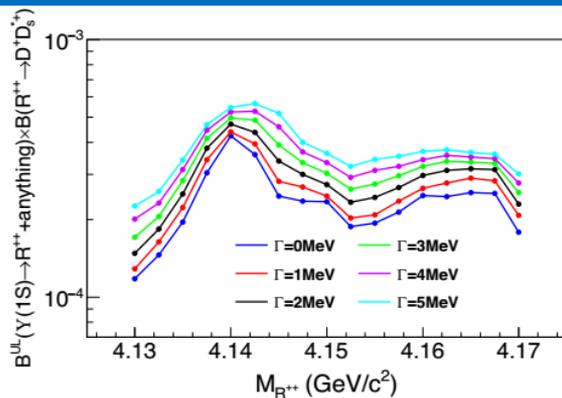


**No  $R^{++}$  signals are observed.**

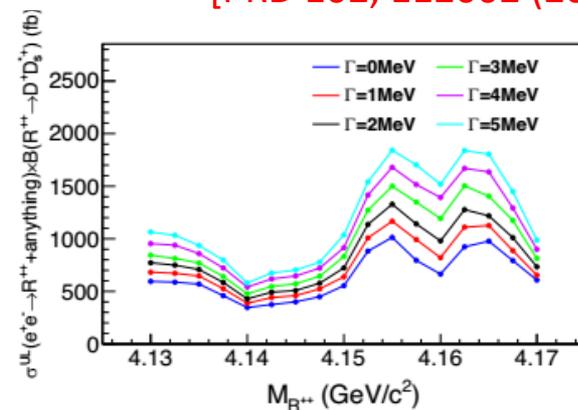
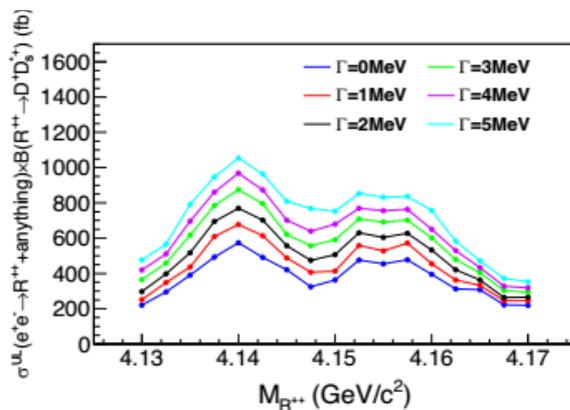
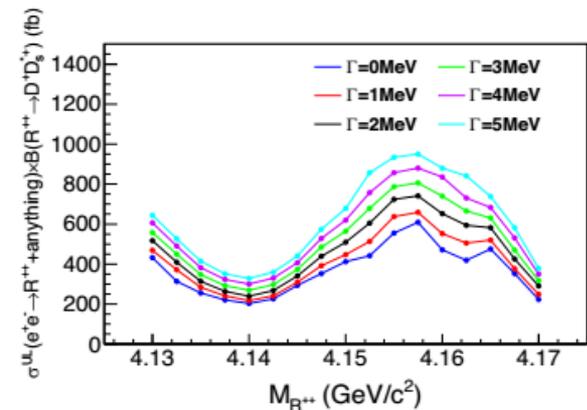


➤ The fitted results with the  $R^{++}$  mass fixed at  $4.14 \text{ GeV/c}^2$  and width fixed at  $2 \text{ MeV}$ .

# 90% C.L. upper limits



[PRD 102, 112002 (2020)]



90% C. L. Upper limits [ $M(R^{++})$  varying from 4.13 to 4.17  $\text{GeV}/c^2$ ,  $\Gamma(R^{++})$  varying from 0 to 5 MeV]

$$\mathcal{B}(Y(1S) \rightarrow R^{++} + \text{anything})\mathcal{B}(R^{++} \rightarrow D^+ D_s^{*+}) < (1.18 - 5.65) \times 10^{-4}$$

$$\mathcal{B}(Y(2S) \rightarrow R^{++} + \text{anything})\mathcal{B}(R^{++} \rightarrow D^+ D_s^{*+}) < (1.63 - 9.27) \times 10^{-4}$$

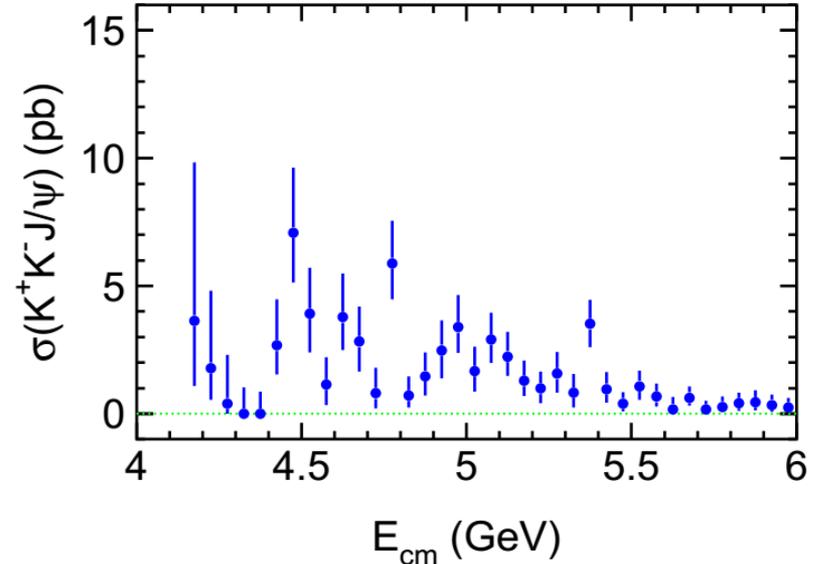
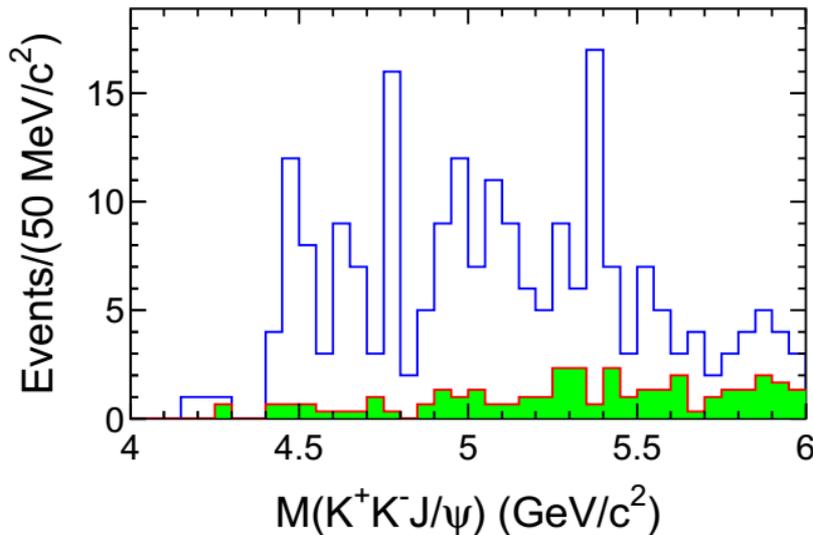
$$\sigma(e^+ e^- \rightarrow R^{++} + \text{anything})\mathcal{B}(R^{++} \rightarrow D^+ D_s^{*+}) < (202.8 - 950.6) \text{ fb at } \sqrt{s} = 10.52 \text{ GeV}$$

$$\sigma(e^+ e^- \rightarrow R^{++} + \text{anything})\mathcal{B}(R^{++} \rightarrow D^+ D_s^{*+}) < (218.9 - 1054.0) \text{ fb at } \sqrt{s} = 10.58 \text{ GeV}$$

$$\sigma(e^+ e^- \rightarrow R^{++} + \text{anything})\mathcal{B}(R^{++} \rightarrow D^+ D_s^{*+}) < (346.6 - 1841.7) \text{ fb at } \sqrt{s} = 10.867 \text{ GeV}$$

# Study of $e^+e^- \rightarrow K^+K^-J/\psi$

- Very recently,  $Z_{cs}(3985)^-(\rightarrow (D_s^-D^{*0} + D_s^{*-}D^0))$  and  $Z_{cs}(4000)^-(\rightarrow K^-J/\psi)$  were observed by BESIII and LHCb, respectively. [PRL.126.102001 (2021), arXiv: 2103.01803]
- The process  $e^+e^- \rightarrow K^+K^-J/\psi$  via initial state radiation was studied by Belle. [PRD 77, 011105(R) (2008); PRD 89, 072015 (2014)]

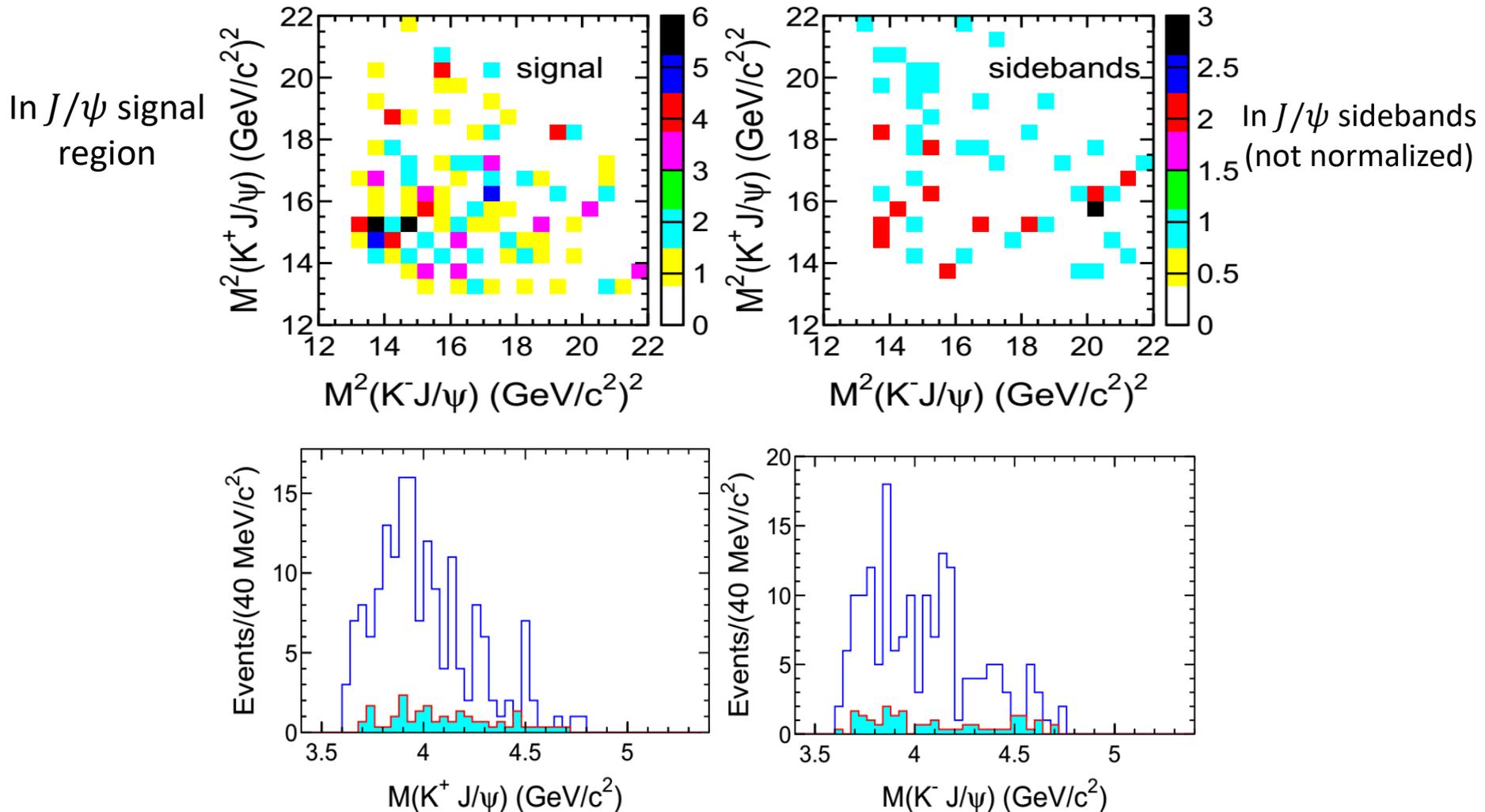


- The  $K^+K^-J/\psi$  invariant mass distribution shows a broad enhancement around 4.4 – 5.5 GeV/c<sup>2</sup>; the green shaded histogram represents the normalized  $J/\psi$  sideband.
- The  $e^+e^- \rightarrow K^+K^-J/\psi$  cross section at each energy point is calculated using

$$\sigma_i = \frac{n_i^{\text{obs}} - f \times n_i^{\text{bkg}}}{\mathcal{L}_i \cdot \epsilon_i \cdot \mathcal{B}(J/\psi \rightarrow \ell^+\ell^-)}$$

# Study of $e^+e^- \rightarrow K^+K^-J/\psi$

- A search for resonant structures and associated intermediate states is performed.



- Neither  $Z_{cs}(3985)^\pm$  nor  $Z_{cs}(4000)^\pm$  was seen in the  $K^\pm J/\psi$  system.

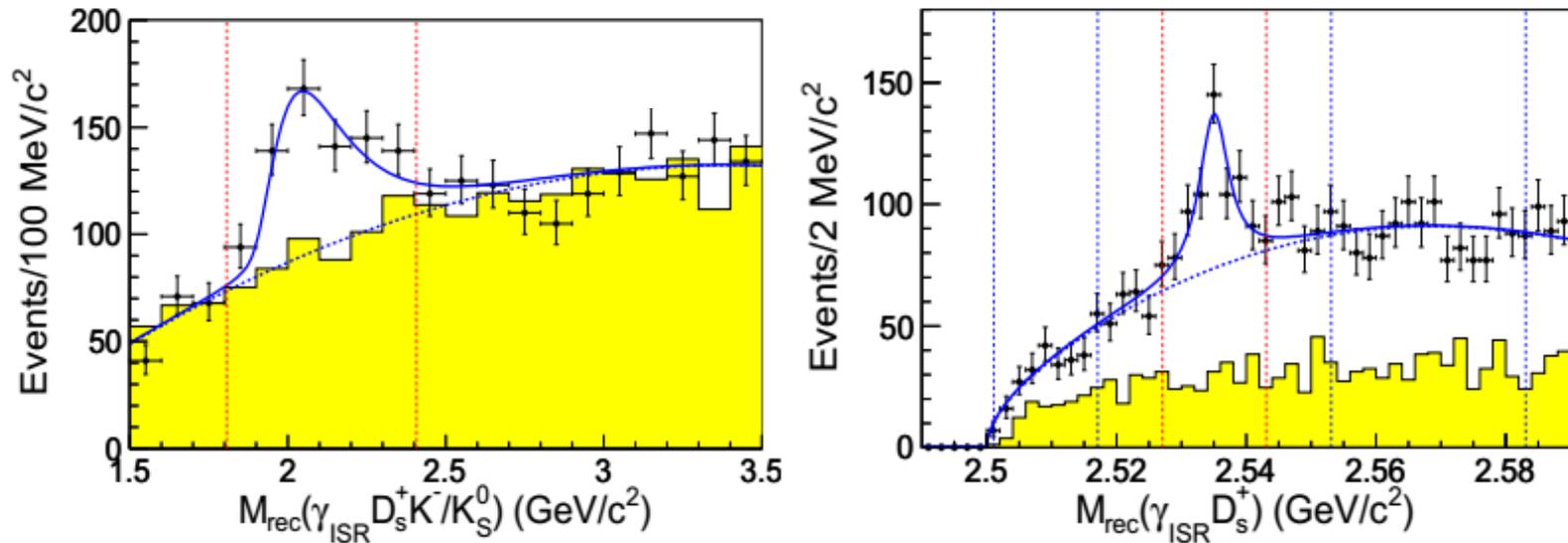
# Summary

- We first search for the  $\eta_{c2}(1D)$  in the  $B \rightarrow K\eta_{c2}(1D)$  and  $B \rightarrow K\pi\eta_{c2}(1D)$  decays. No significant signal is found.
- We report the first vector charmonium-like state decaying to the charmed-antistrange and anticharmed-strange meson pairs  $D_s^+ D_{s1}^-(2536)$  and  $D_s^+ D_{s2}^*(2573)$ . The masses and widths are close to those of the  $Y(4660)$ .
- We report the results of a first search for a doubly charged DDK bound state, called the  $R^{++}$ . No significant signal is observed in all studied modes. The 90% C.L. upper limits on the production ratio under different assumptions of  $R^{++}$  masses and widths are obtained.
- We ever studied the process  $e^+e^- \rightarrow K^+K^-J/\psi$  via initial state radiation. No obvious structures are observed in the  $K^\pm J/\psi$  system.
- Belle II will reach  $50 \text{ ab}^{-1}$ , which will provide greater sensitivity and precise measurements in charmonium(like) states.

*Thanks for your attentions!*

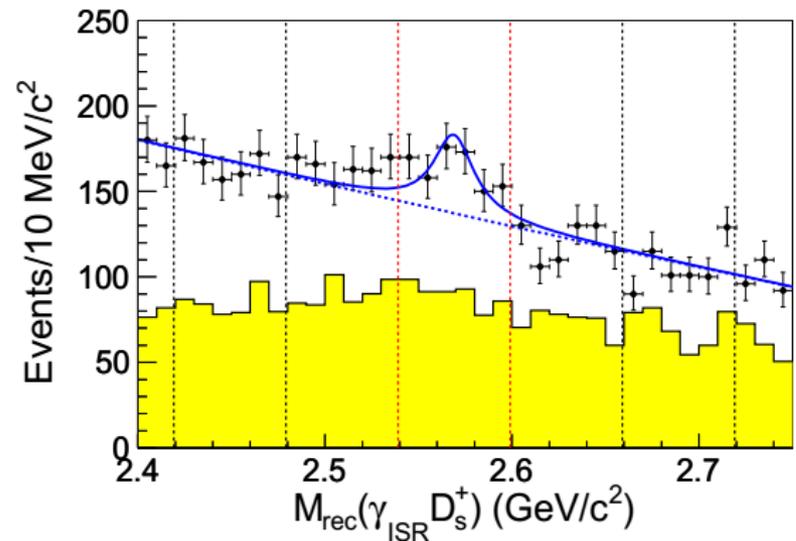
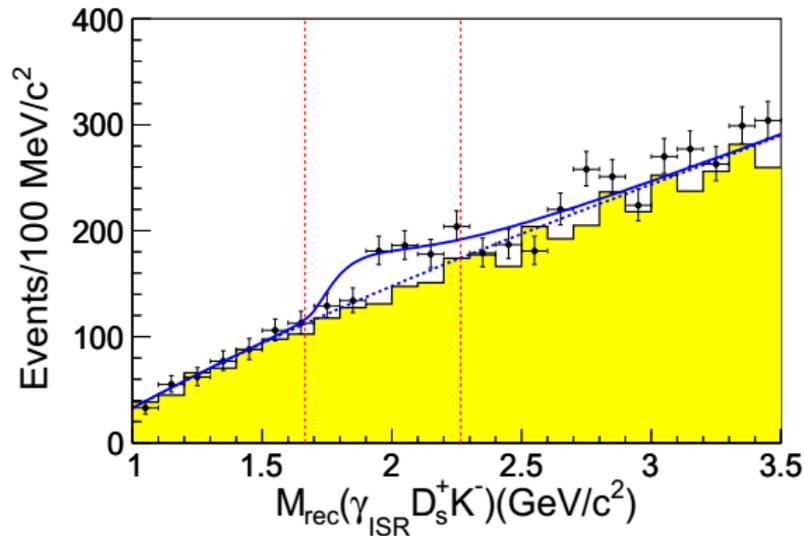
# Backup

# Backup



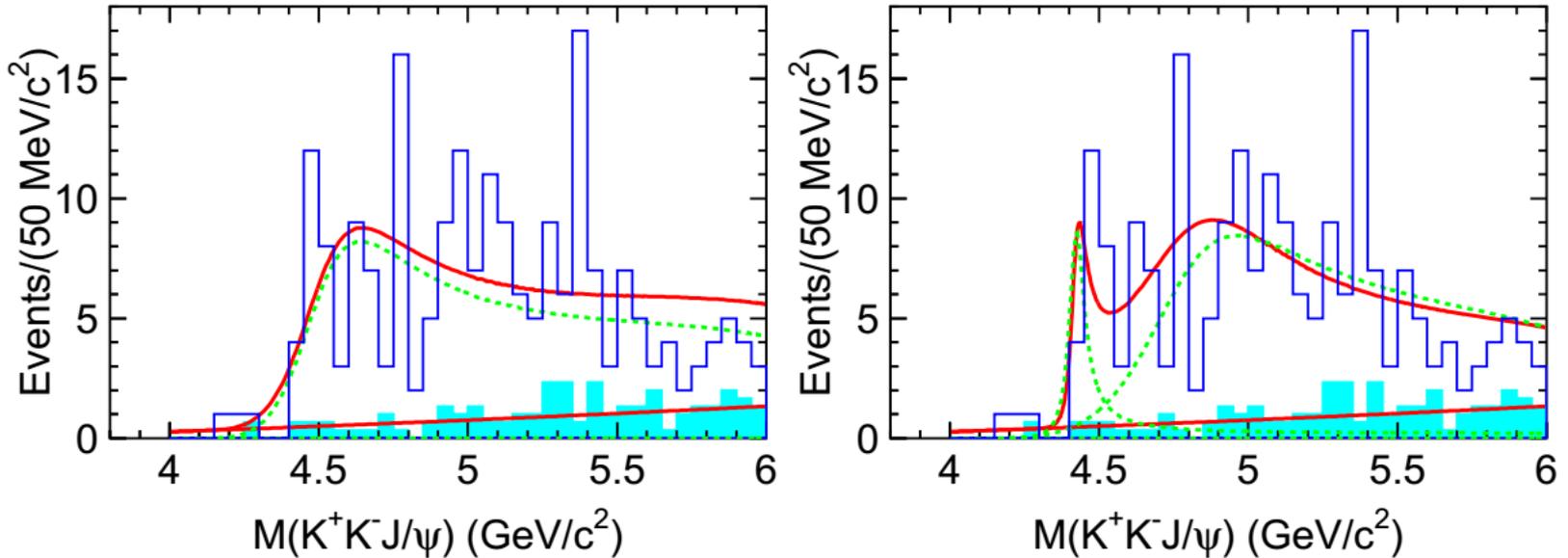
- $M_{\text{rec}}(\gamma_{\text{ISR}} D_s^+ K^- / K_S^0)$  and  $M_{\text{rec}}(\gamma_{\text{ISR}} D_s^+)$  distribution is making **before** applying the  $\bar{D}^{*0} / D^{*-}$  mass constraint.
- The yellow histograms show the normalized  $D_{s1}(2536)^-$  mass sidebands (left plot) and the normalized  $D_s^+$  mass sidebands (right plot).
- Due to the poor mass resolution, the  $\bar{D}^{*0} / D^{*-}$  signal is very wide.

# Backup



- $M_{\text{rec}}(\gamma_{\text{ISR}} D_s^+ K^-)$  and  $M_{\text{rec}}(\gamma_{\text{ISR}} D_s^+)$  distribution is making **before** applying the  $\bar{D}^0$  mass constraint.
- The yellow histograms show the normalized  $D_{s2}^*(2573)^-$  mass sidebands (left plot) and the normalized  $D_s^+$  mass sidebands (right plot).
- The  $\bar{D}^0$  signal is wide and asymmetric due to the asymmetric resolution function of the ISR photon energy and higher order ISR corrections

# Backup



$$\sigma(s) = \frac{M^2}{s} \frac{12\pi\Gamma_{e^+e^-} \mathcal{B}(R \rightarrow f) \Gamma_{\text{tot}}}{(s - M^2)^2 + M^2\Gamma_{\text{tot}}^2} \frac{\rho(\sqrt{s})}{\rho(M)}$$

**Model 1:** a single BW function plus a background term,

Fitted mass and width:  $M = (4482 \pm 45) \text{ MeV}/c^2$ ,  $\Gamma_{\text{tot}} = (432 \pm 56) \text{ MeV}$ ;

**Model 2:** a coherent sum of a BW function and a  $\psi(4415)$  component with mass and width fixed at their world average values plus a background term,

Fitted mass and width:  $M = (4747 \pm 117) \text{ MeV}/c^2$ ,  $\Gamma_{\text{tot}} = (671 \pm 86) \text{ MeV}$ .