

SPIN OBSERVABLES IN pN - and pd - ELASTIC AND QUASI-ELASTIC SCATTERING AT ENERGIES OF SPD NICA

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PLAN:

pN- elastic scattering . Data and parametrizations of pp amplitudes <3 GeV, >3 GeV

Glauber theory of pd- elastic scattering at 0.1-3 GeV

Results of Glauber calculations of spin observables pd-elastic scattering at 3-50 GeV/c

Quasielastic scattering pd- \rightarrow {pp}(1S0)+n and complete polarization experiment

Spin-dependent pN-amplitudes in search of T-invariance violation in pd-scattering

Conclusion

NN-forces is a basis of nuclear physics .
It is important to study all their components,
including spin-dependent terms at low and high
energies **via the spin amplitudes of the NN**
elastic scattering

PP elastic scattering

For identical spin $\frac{1}{2}$ particles under Lorentz and P-,T- invariance:

spin non-flip $\phi_1(s, t) = \langle ++ | M | ++ \rangle$

double spin-flip $\phi_2(s, t) = \langle ++ | M | -- \rangle$

spin non-flip $\phi_3(s, t) = \langle +- | M | +- \rangle$

double spin-flip $\phi_4(s, t) = \langle +- | M | -+ \rangle$

single spin-flip $\phi_5(s, t) = \langle ++ | M | +- \rangle$.

For non-identical (pn) nucleons one has 6 amplitudes,

T-reversal non-invariance provides two additional amplitudes.

All spin-observables of NN elastic scattering are described in terms of ϕ_i

$$d\sigma/dt = N[|\phi_1|^2 + |\phi_2|^2 + |\phi_3|^2 + |\phi_4|^2 + 4|\phi_5|^2],$$

$$A_N \sim \text{Im}[(\phi_1 + \phi_2 + \phi_3 - \phi_4)\phi_5^*]$$

$$A_{NN} \sim 2|\phi_5|^2 + \text{Re}(\phi_1^*\phi_2 - \phi_3^*\phi_4)$$

...

Number of linearly independent non-zero spin observables:

single-spin (asymmetries A_i , polarizations P_i) – 2

double-spin (A_{ii}, \dots) – 12

triple-spin – 9

four- spin – 2

Complete polarization experiment

for pp-elastic requires 9 independent observables.

PWA GWU is performed for pp-elastic up to 3.8 GeV/c (SAID

webpage:<http://gwdac.phys.gwu.edu>.

R.A. Arndt, I.I. Strakovsky, B.L. Workman PRC 56, 3005 (1997);

PWA for pn- elastic – up 1.2 GeV/c

Concerning SPD NICA, above 3 GeV/c $d\sigma/dt$ and mainly A_N (up to 50 GeV/c) and A_{NN}, C_{LL} (up to 6 GeV/c, 12 GeV/c) are measured. Data on double-spin observables D_{NN}, K_{NN} are rather poore in the region of forward angles.

Parametrizations (fit) of the pp- data:

Regge: W.P. Ford, J.W. Van Orden, Phy.Rev. **C87** (2013) 014004;

A. Sibirtsev et al. Eur.Phys.J. **A 45** (2010) 357;

Eikonal: S. Wakaizumi, M. Sawamoto, Prog. Theor. Phys. v.64 (1980) 1699

$$\phi_{ai}(s, t) = \pi \beta_{ai}(t) \frac{\xi_i(s, t)}{\Gamma(\alpha(t))}; i = \rho, \omega, a_2, f_2, P; a = 1 - 5;$$

$$\xi_i(t, s) = \frac{1 + S_i \exp[-i\pi\alpha(t)]}{\sin[\pi\alpha_i(t)]} \left[\frac{s}{s_0} \right]^{\alpha_i(t)},$$

$$\alpha_i(t) = \alpha_i^0 + \alpha_i' t,$$

$$\beta_{1i}(t) = c_{1i} \exp(b_{1i} t),$$

$$\beta_{2i}(t) = c_{2i} \exp(b_{2i} t) \frac{-t}{4m_N^2},$$

$$\beta_{3i}(t) = c_{3i} \exp(b_{3i} t),$$

$$\beta_{4i}(t) = c_{4i} \exp(b_{4i} t) \frac{-t}{4m_N^2},$$

$$\beta_{5i}(t) = c_{5i} \exp(b_{5i} t) \left[\frac{-t}{4m_N^2} \right]^{1/2}.$$

A. Sibirtsev et al, EPJ A 45 (2010) 357

Helicity amplitudes in Regge formalism

A systematic analysis of pp elastic scattering from COSY-EDDA, SATURNE, GZS ANL

A. Sibirtsev, J. Haidenbauer, H.-W. Hammer et al. EPJA 45 (2010) 357

ω, ρ, f_2, a_2 Regge exchanges and the Pomeron for P_L from 3 GeV/c up to 50 GeV/c.

Isospin structure and G-parity relations allow to obtain the $\bar{p}p$ -, pn - and $\bar{p}n$ elastic amplitudes from the pp amplitudes (J.R. Pelaez, 2006):

$$\phi(pp) = -\phi_\omega - \phi_\rho + \phi_{f_2} + \phi_{a_2} + \phi_P$$

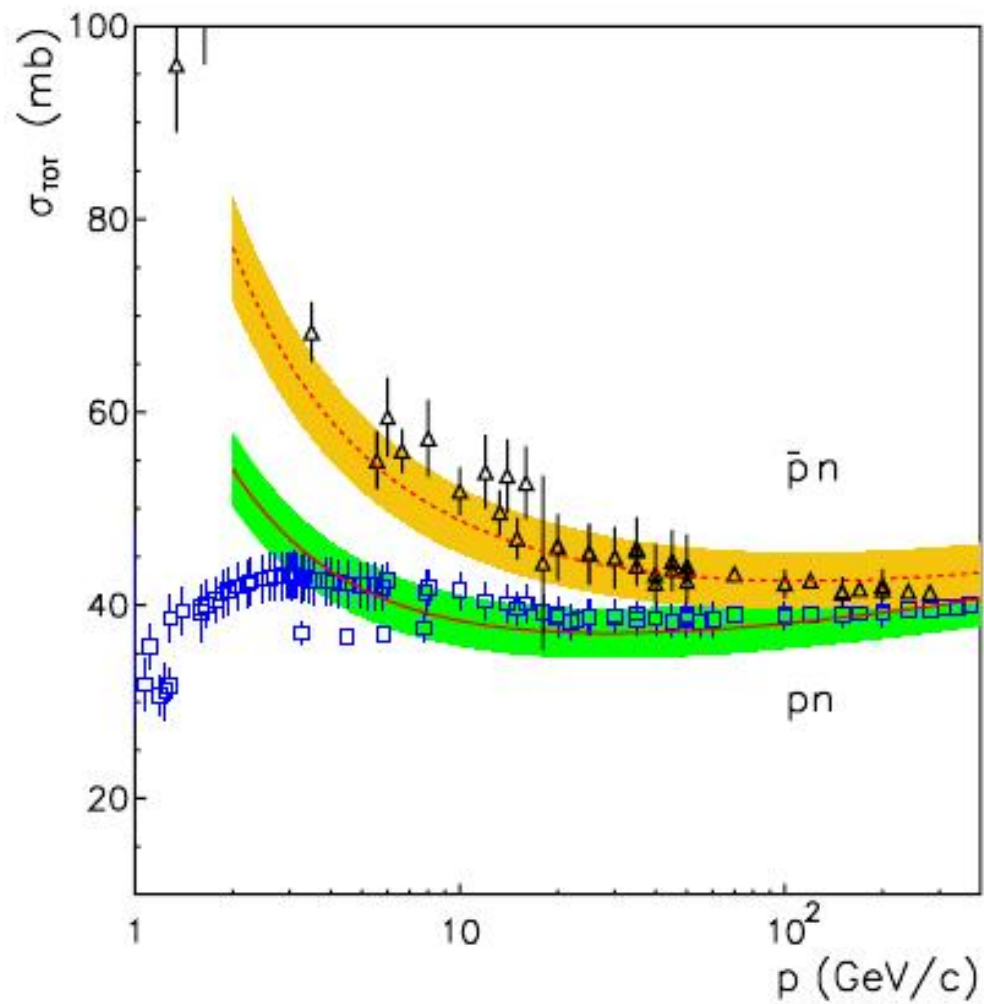
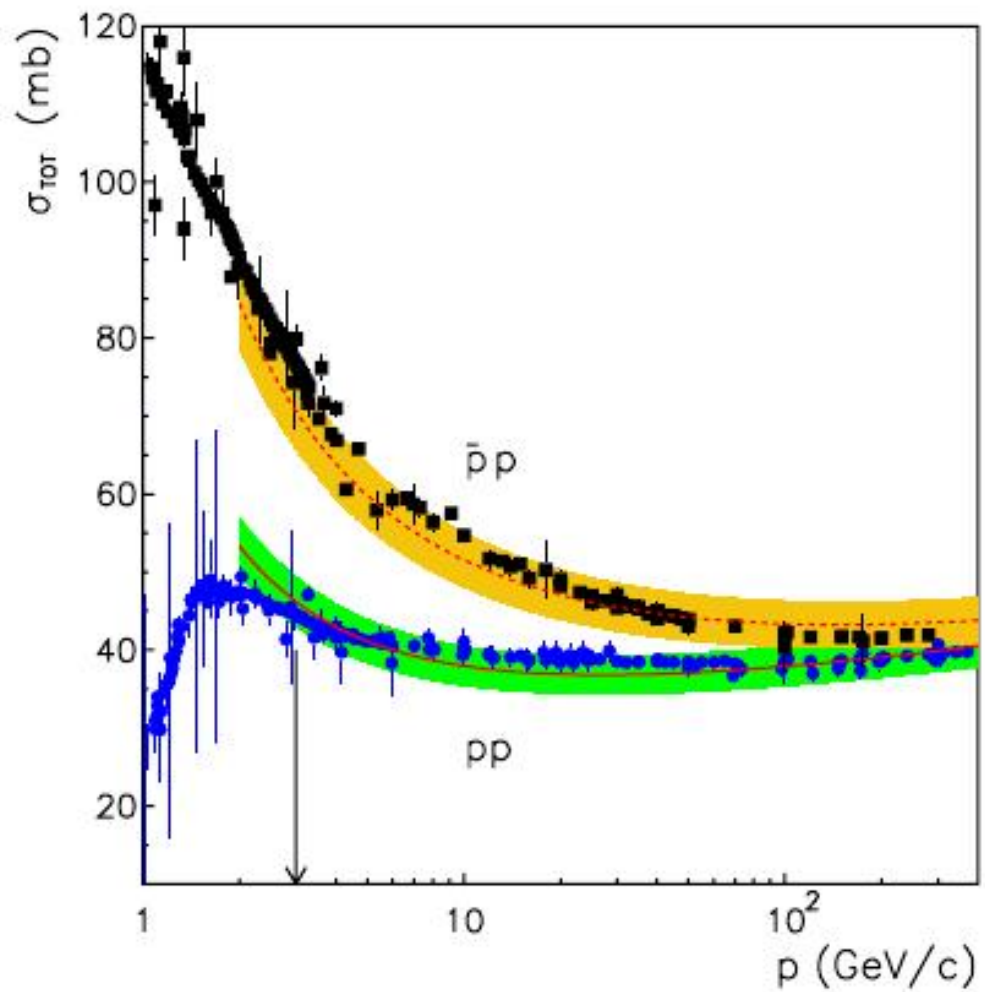
$$\phi(\bar{p}p) = \phi_\omega + \phi_\rho + \phi_{f_2} + \phi_{a_2} + \phi_P$$

$$\phi(pn) = -\phi_\omega + \phi_\rho + \phi_{f_2} - \phi_{a_2} + \phi_P$$

$$\phi(\bar{p}n) = \phi_\omega - \phi_\rho + \phi_{f_2} - \phi_{a_2} + \phi_P$$

However, not all available data

($C_{NN}, C_{LL}, C_{SS}, C_{LS}, D_{NN}, D_{SS}, D_{LS}, K_{NN}, \Delta\sigma_T, H_{SNS}$... measured by ANL at 6 GeV/c, and some at 12 GeV/c) were included into the fit.



A. Sibirtsev et al, EPJA (2010): full line – pp, dashed – antip p.

PROBLEMS

A. Sibirtsev et al, EPJA (2010) 357

R- real-to-imaginary part ratio.
A problem with antip-p theory: no zero

Other problems, see O.V. Selyugin, PRD 91 (2015);
PEPA Letters 13 (2016) 116.

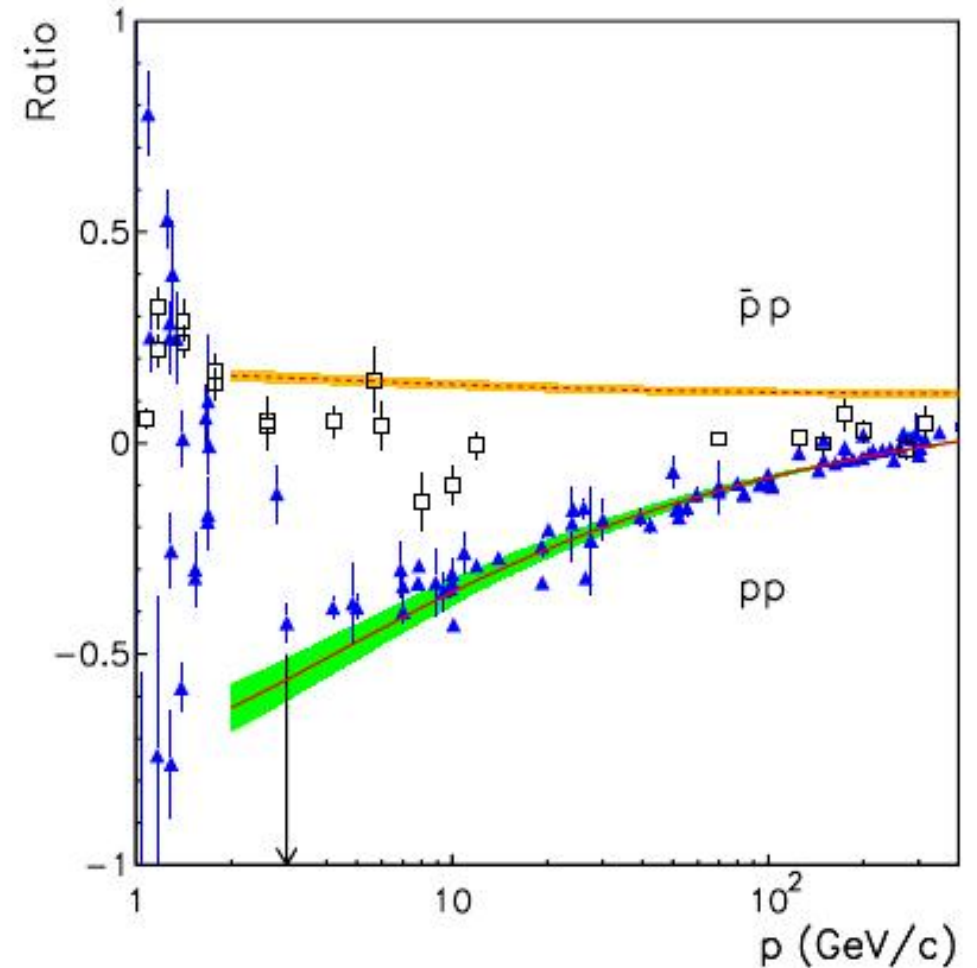
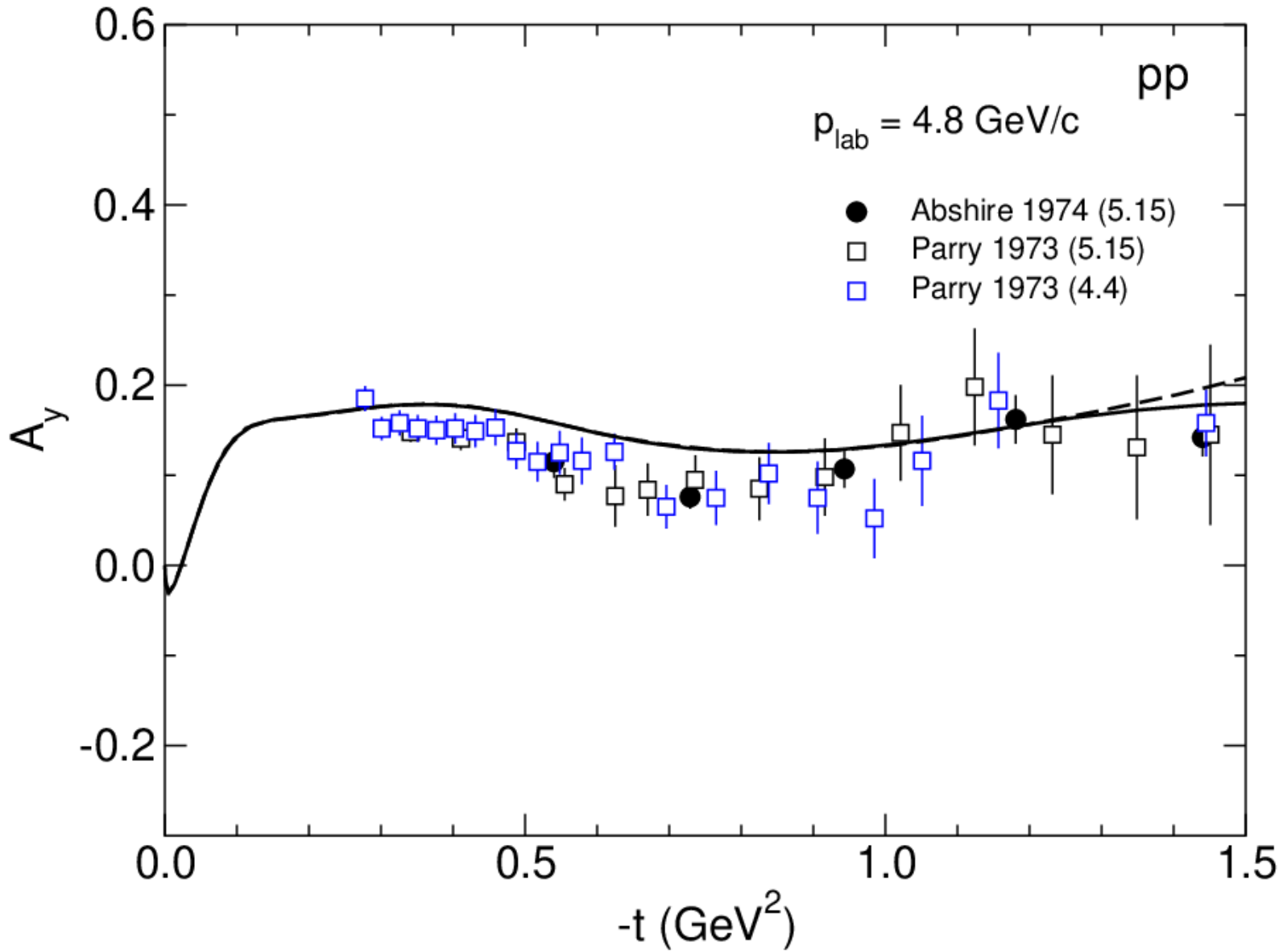


Fig. 16. Ratio of the real-to-imaginary parts of the forward amplitudes for pp (triangles, solid line) and $\bar{p}p$ (squares, dashed line), respectively. The data are taken from the PDG [32].

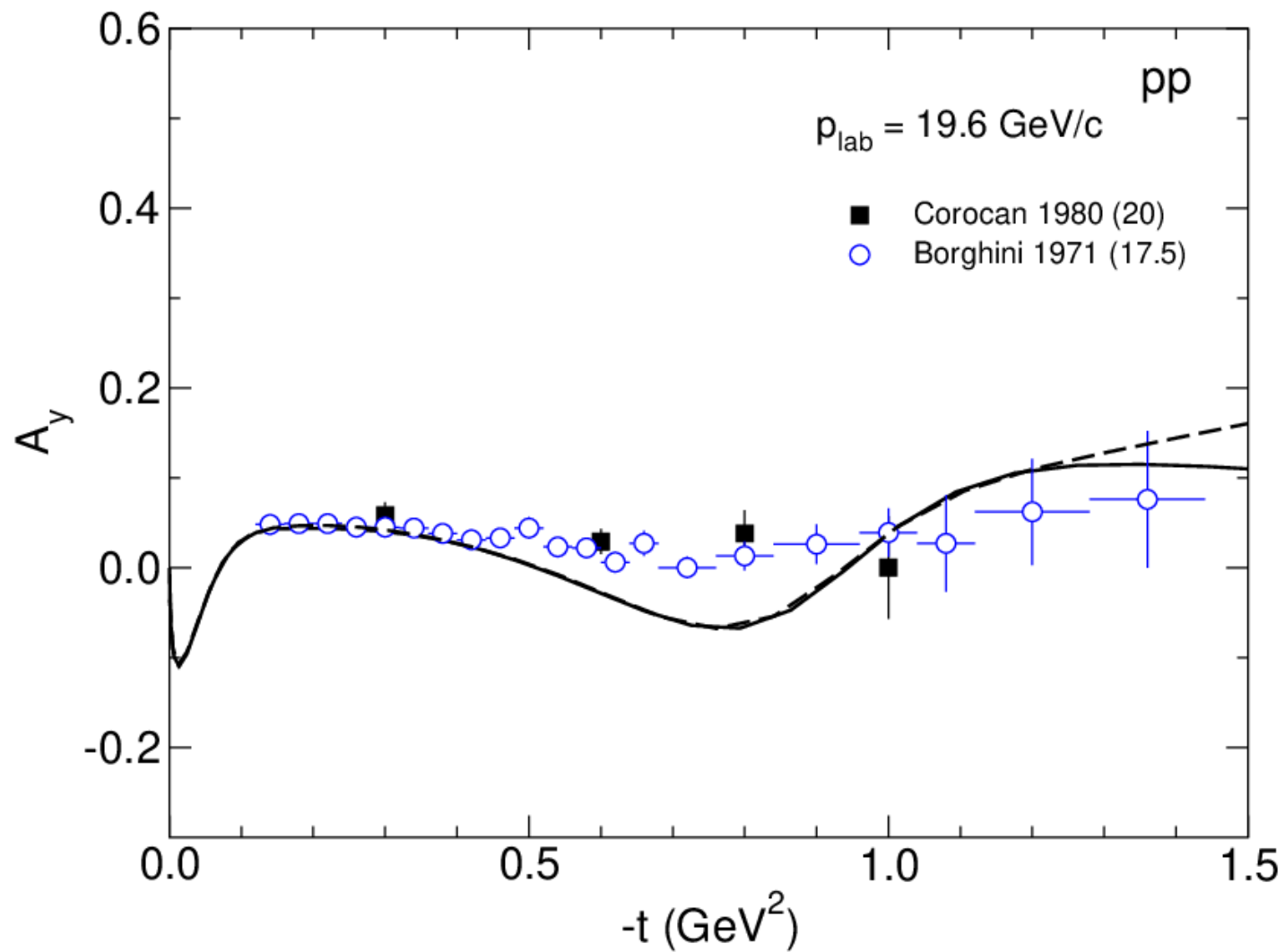


pp- helicity amplitudes
by A.Sibirtsev:
Regge parametrization
Gaussian (dashed)

pp- helicity amplitudes

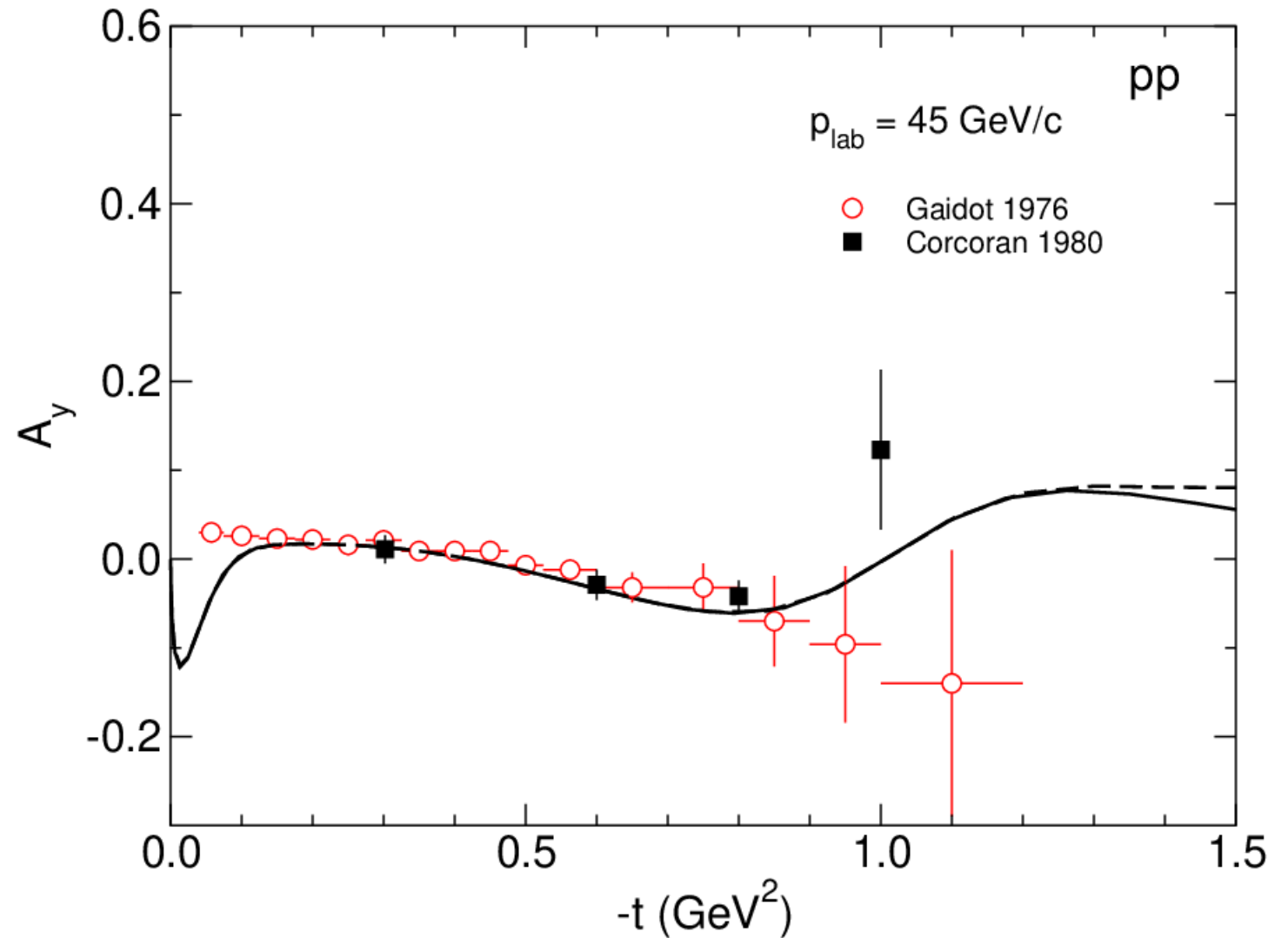
A.Sibirtsev:

Regge parametrization;
Gaussian (dashed)



A.Gaidat et al. Phys.Lett.
B61 (1976) 103

pp- helicity amplitudes
A.Sibirtsev: Regge
parametrization (full);
Gaussians (dashed)



pd elastic scattering

Phenomenology of the $pd \rightarrow pd$ transition

$$\frac{1}{2} + 1 \rightarrow \frac{1}{2} + 1$$

$(2 + 1)^2(2\frac{1}{2} + 1)^2 = 36$ transition amplitudes

P-parity \implies 18 independent amplitudes

T-invariance \implies 12 independent amplitudes

At $\theta_{cm} = 0 \implies$ 4 (for T-inv. P-inv.) + 1 (T- viol. P-inv.)

Elastic $pd \rightarrow pd$ transitions

$$\begin{aligned} \hat{M}(\mathbf{q}, \mathbf{s}) = & \exp\left(\frac{1}{2}i\mathbf{q} \cdot \mathbf{s}\right)M_{pp}(\mathbf{q}) + \exp\left(-\frac{1}{2}i\mathbf{q} \cdot \mathbf{s}\right)M_{pn}(\mathbf{q}) + \\ & + \frac{i}{2\pi^{3/2}} \int \exp(i\mathbf{q}' \cdot \mathbf{s}) \left[M_{pp}(\mathbf{q}_1)M_{pn}(\mathbf{q}_2) + p \leftrightarrow n \right] d^2\mathbf{q}'. \end{aligned}$$

On-shell elastic pN scattering amplitude (**T-even, P-even**)

$$\begin{aligned} M_{pN} = & A_N + (C_N\boldsymbol{\sigma}_1 + C'_N\boldsymbol{\sigma}_2) \cdot \hat{\mathbf{n}} + B_N(\boldsymbol{\sigma}_1 \cdot \hat{\mathbf{k}})(\boldsymbol{\sigma}_2 \cdot \hat{\mathbf{k}}) + \\ & + (G_N - H_N)(\boldsymbol{\sigma}_1 \cdot \hat{\mathbf{n}})(\boldsymbol{\sigma}_2 \cdot \hat{\mathbf{n}}) + (G_N + H_N)(\boldsymbol{\sigma}_1 \cdot \hat{\mathbf{q}})(\boldsymbol{\sigma}_2 \cdot \hat{\mathbf{q}}) \end{aligned}$$

M. Platonova, V. Kukulín, PRC **81** (2010) 014004:

Phenomenology of the $pd \rightarrow pd$ transition

$\hat{\mathbf{q}} = (\mathbf{p} - \mathbf{p}')$, $\hat{\mathbf{k}} = (\mathbf{p} + \mathbf{p}')/k$, $\hat{\mathbf{n}} = [\mathbf{k} \times \mathbf{q}]$ – unit vect. ($Z \uparrow\uparrow \hat{\mathbf{k}}$, $X \uparrow\uparrow \hat{\mathbf{q}}$, $Y \uparrow\uparrow \hat{\mathbf{n}}$)

$$M = (A_1 + A_2 \boldsymbol{\sigma} \hat{\mathbf{n}}) + (A_3 + A_4 \boldsymbol{\sigma} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{q}})^2 + (A_5 + A_6 \boldsymbol{\sigma} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{n}})^2 + A_7(\boldsymbol{\sigma} \hat{\mathbf{k}})(\mathbf{S} \hat{\mathbf{k}}) + A_8(\boldsymbol{\sigma} \hat{\mathbf{q}}) [(\mathbf{S} \hat{\mathbf{q}})(\mathbf{S} \hat{\mathbf{n}}) + (\mathbf{S} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{q}})] + (A_9 + A_{10} \boldsymbol{\sigma} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{n}}) + A_{11}(\boldsymbol{\sigma} \hat{\mathbf{q}})(\mathbf{S} \hat{\mathbf{q}}) + A_{12}(\boldsymbol{\sigma} \hat{\mathbf{k}}) [(\mathbf{S} \hat{\mathbf{k}})(\mathbf{S} \hat{\mathbf{n}}) + (\mathbf{S} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{k}})]$$

$$+ (T_{13} + T_{14} \boldsymbol{\sigma} \hat{\mathbf{n}}) [(\mathbf{S} \hat{\mathbf{k}})(\mathbf{S} \hat{\mathbf{q}}) + (\mathbf{S} \hat{\mathbf{q}})(\mathbf{S} \hat{\mathbf{k}})] + T_{15}(\boldsymbol{\sigma} \hat{\mathbf{q}})(\mathbf{S} \hat{\mathbf{k}}) + T_{16}(\boldsymbol{\sigma} \hat{\mathbf{k}})(\mathbf{S} \hat{\mathbf{q}}) + T_{17}(\boldsymbol{\sigma} \hat{\mathbf{k}}) [(\mathbf{S} \hat{\mathbf{q}})(\mathbf{S} \hat{\mathbf{n}}) + (\mathbf{S} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{q}})] + T_{18}(\boldsymbol{\sigma} \hat{\mathbf{q}}) [(\mathbf{S} \hat{\mathbf{k}})(\mathbf{S} \hat{\mathbf{n}}) + (\mathbf{S} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{k}})]$$

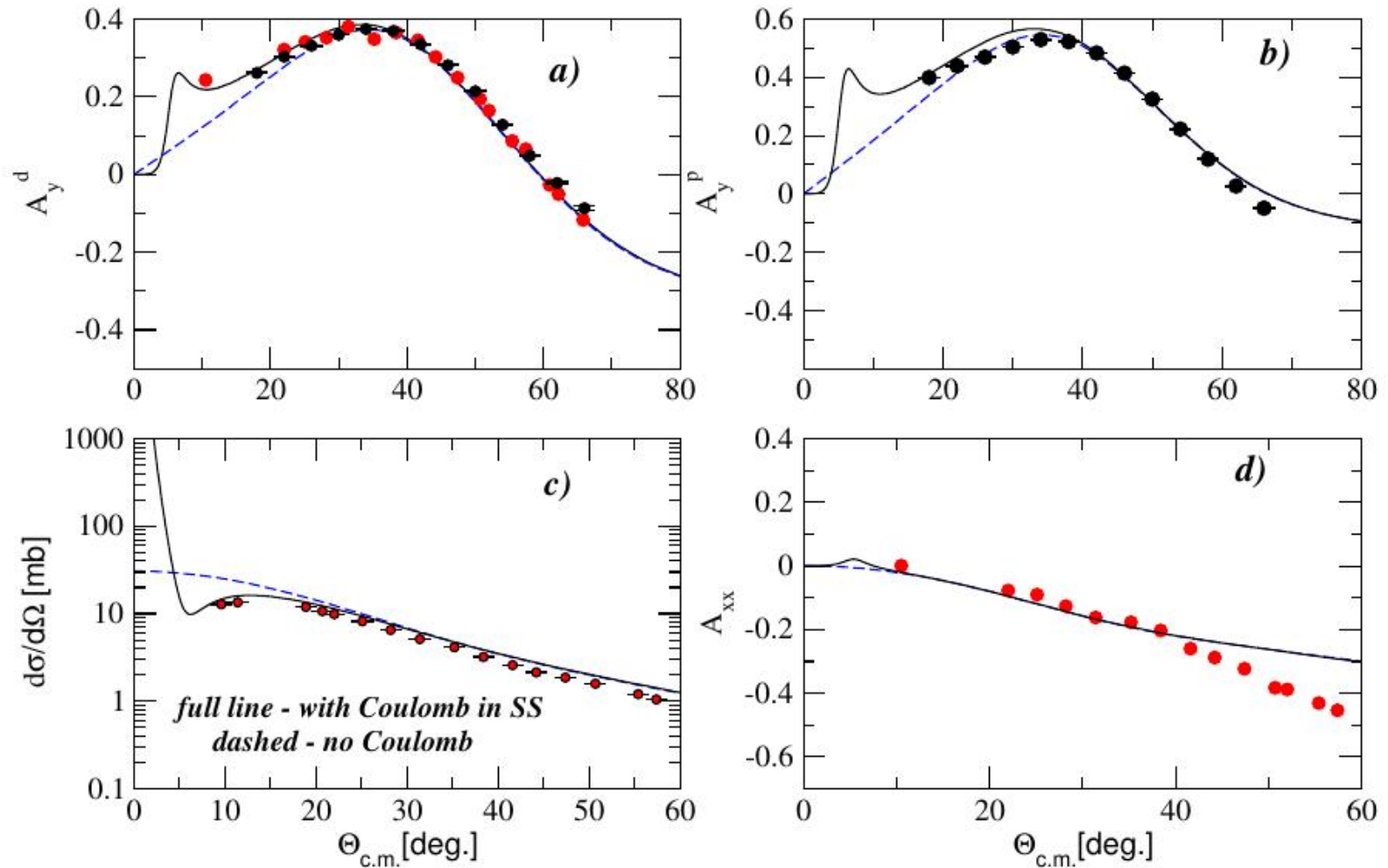
T-even P-even: $A_1 \div A_{12}$
 (see M. Platonova, V.I. Kukulin, PRC **81** (2010) 014004)

$T_{13} \div T_{18} : \text{TVPC}$

The polarized elastic differential pd cross section

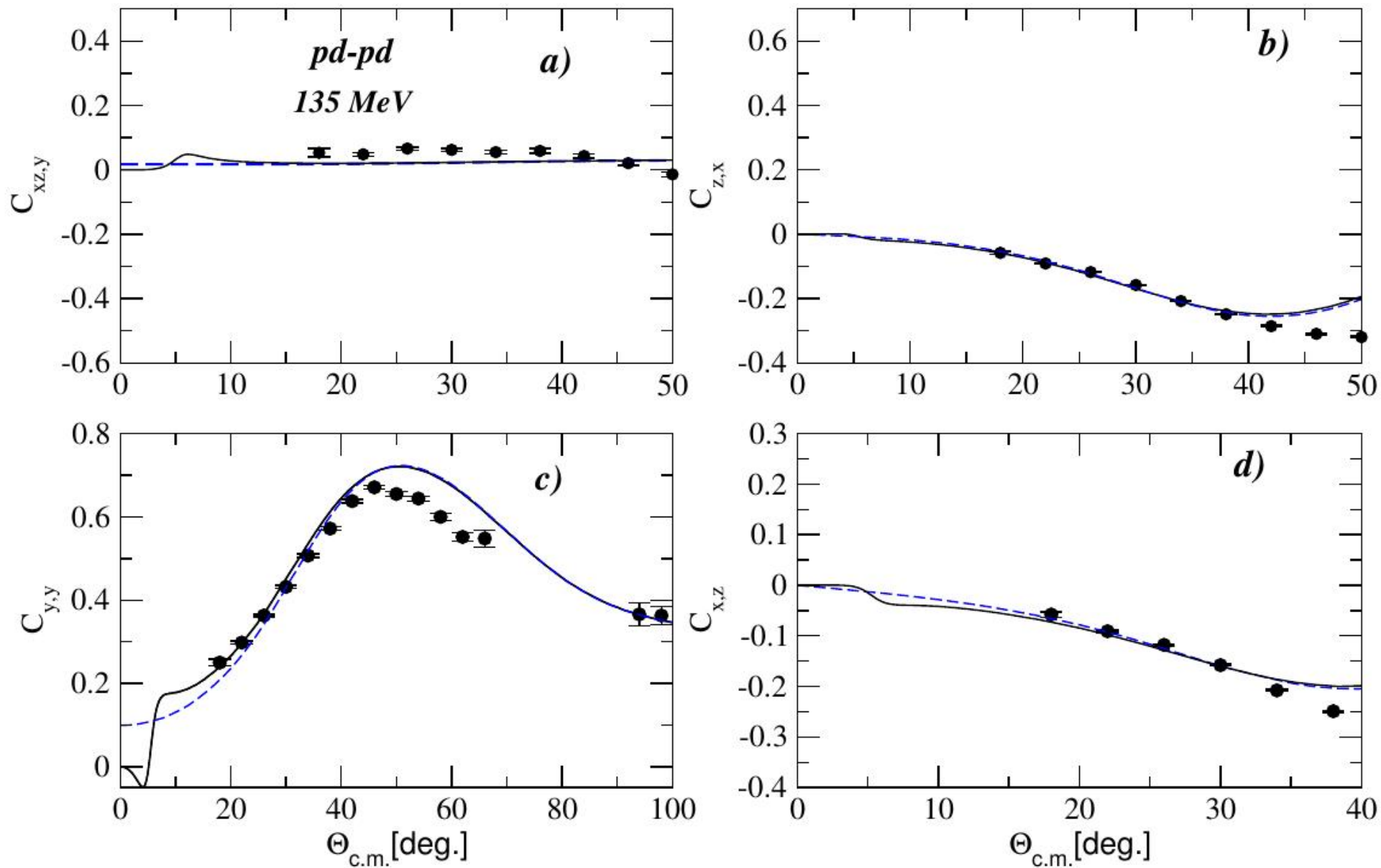
$$\left(\frac{d\sigma}{d\Omega} \right)_{pol} = \left(\frac{d\sigma}{d\Omega} \right)_0 \left[1 + \frac{3}{2} p_j^p p_i^d C_{j,i} + \frac{1}{3} P_{ij}^d A_{ij} + \dots \right]. \quad (2)$$

$$C_{y,y} = Tr M S_y \sigma_y M^+ / Tr M M^+, \quad \dots \quad (3)$$



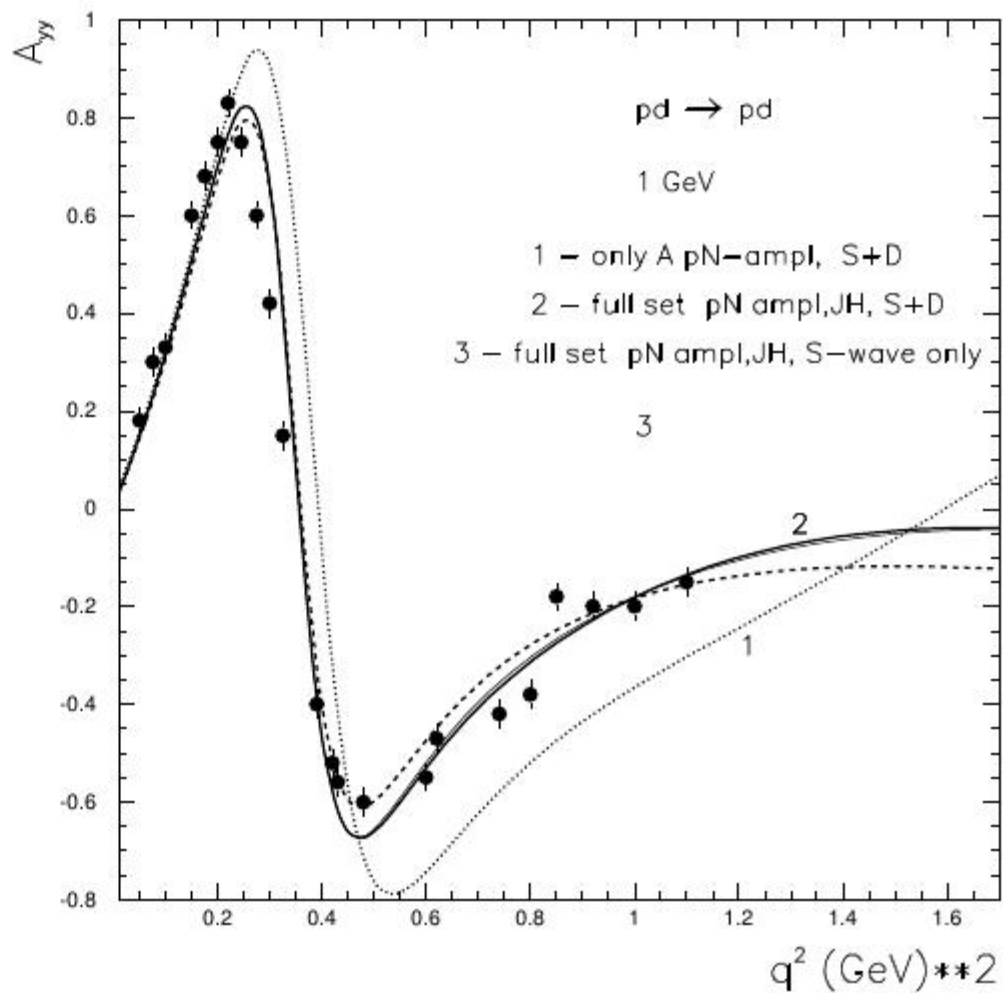
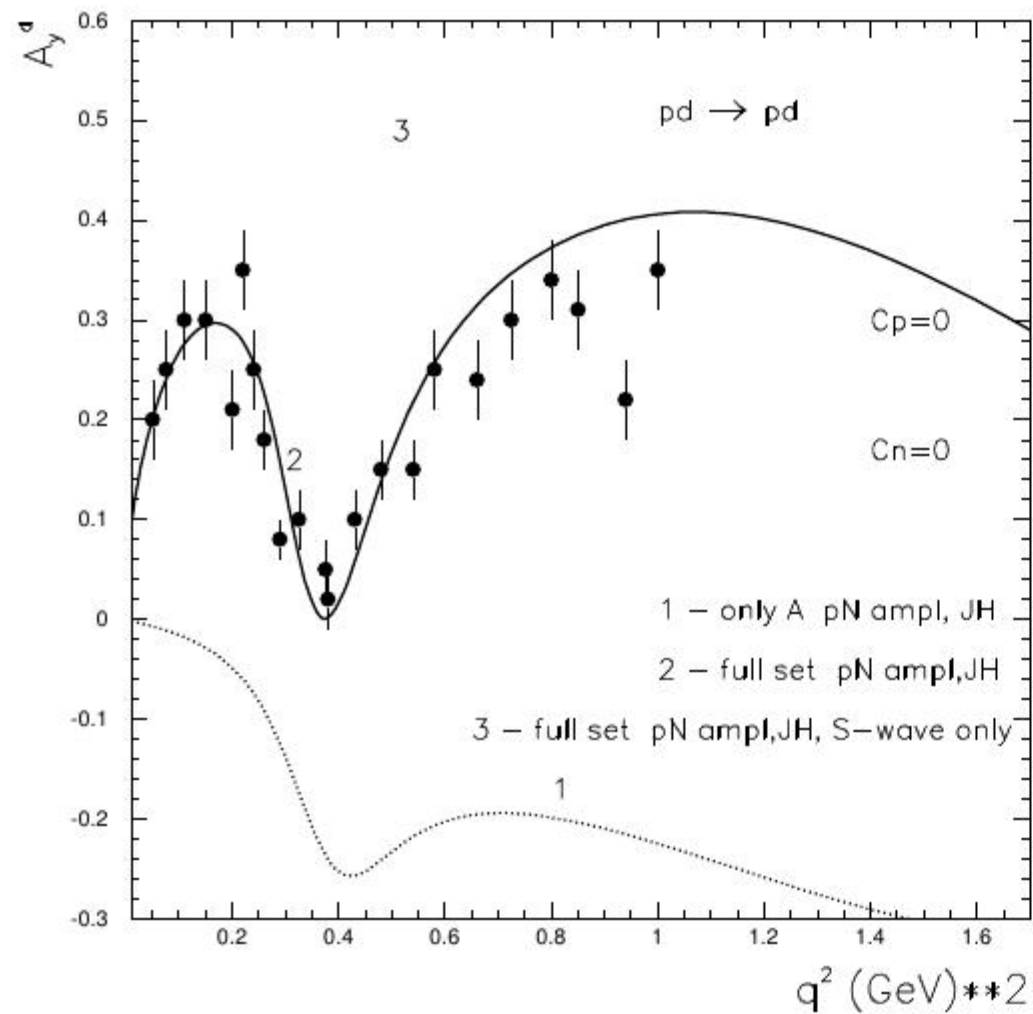
Data: K. Sekiguchi et al. PRC (2002); B. von Przewoski et al. PRC (2006)

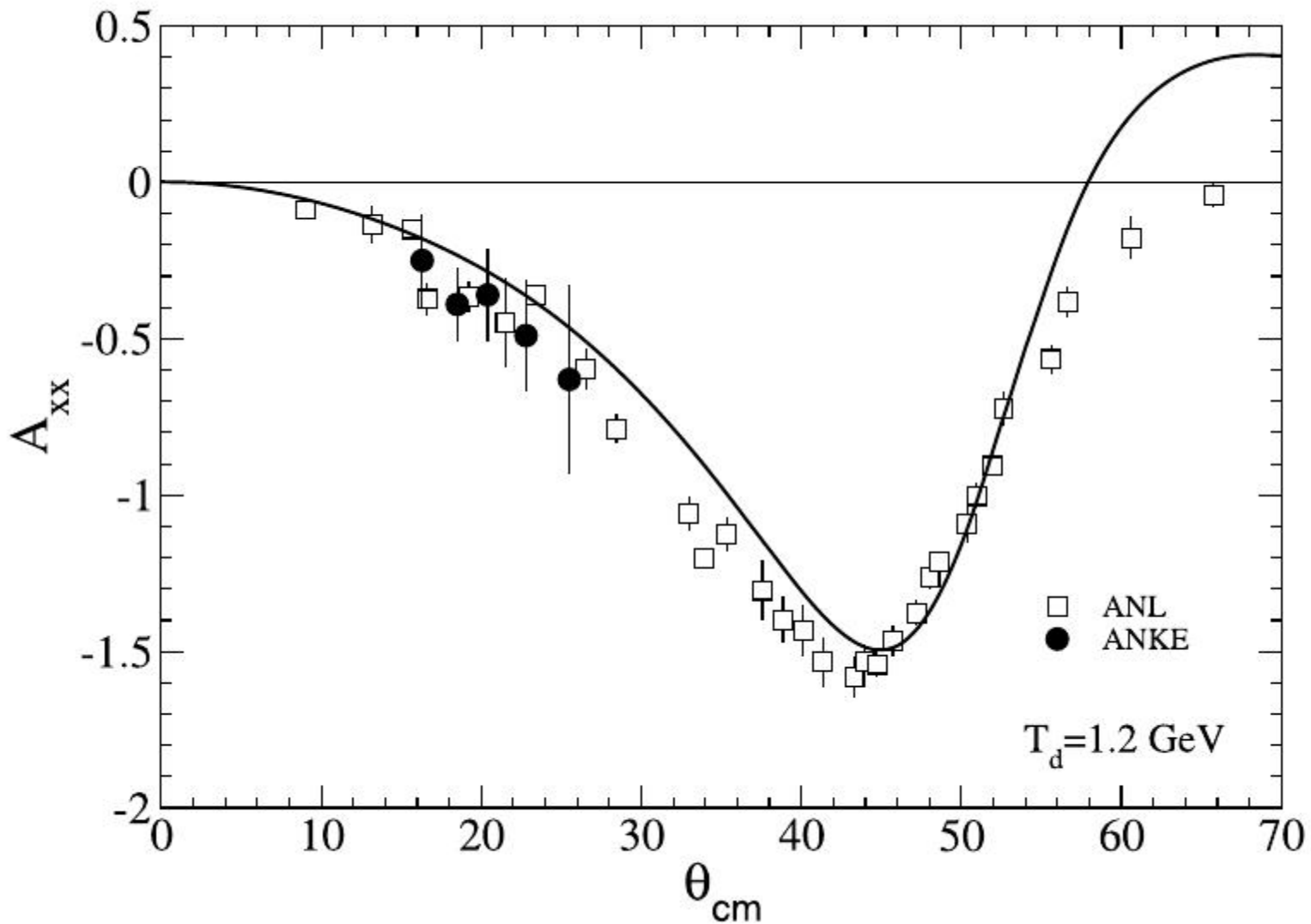
See also Faddeev calculations: A.Deltuva, A.C. Fonseca, P.U. Sauer, PRC 71 (2005) 054005.

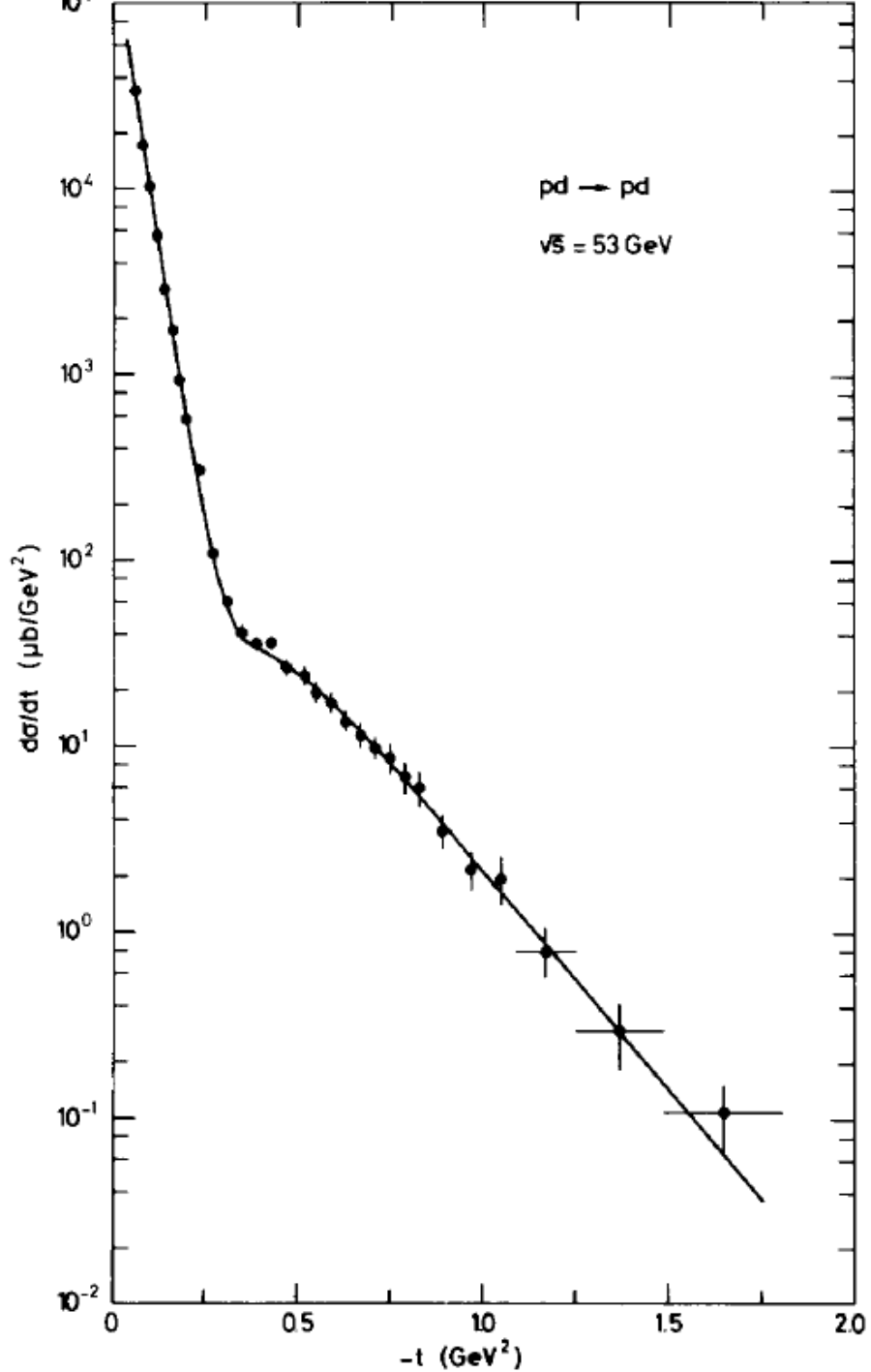


Curves: the modified Glauber model; A.A. Temerbayev, Yu.N.Uzikov, *Yad. Fiz.* **78** (2015) 38
 Data: von B.Przewoski et al. *PRC* 74 (2006) 064003

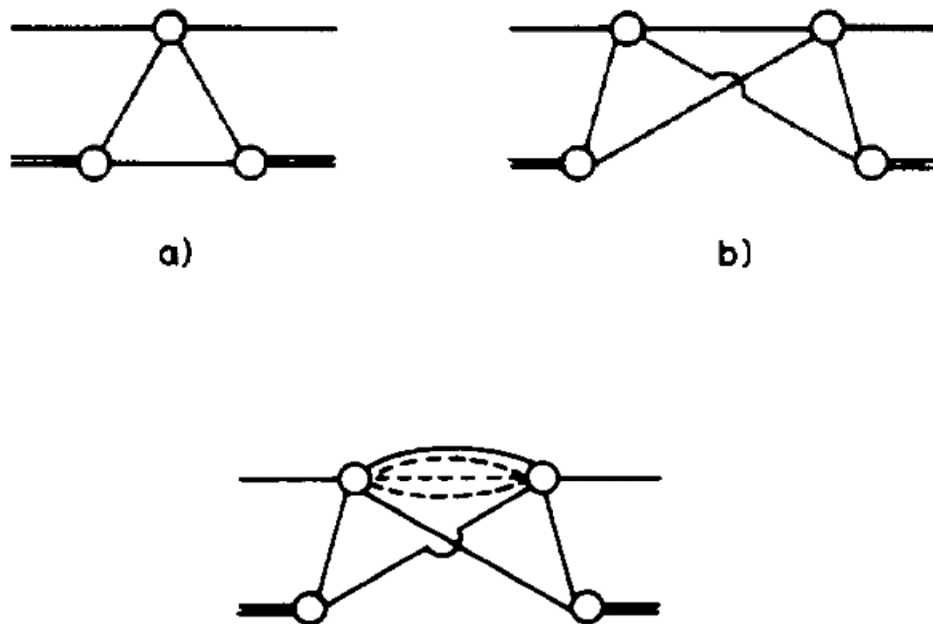
Test calculations: pd elastic scattering at 1 GeV







Glauber calculations of the $d\sigma/dt$ for pd-elastic at ISR energies $\sqrt{s}=53$ and 63 GeV
 G.Goggi et al. Nucl. Phys. B149 (1979) 381



$$R = A_y^d / A_y^p$$

Yu.N.U, C. Wilkin, Phys. Lett. B793 (2019) 224,

$R \neq 2/3$ is sensitive to spin-spin NN terms

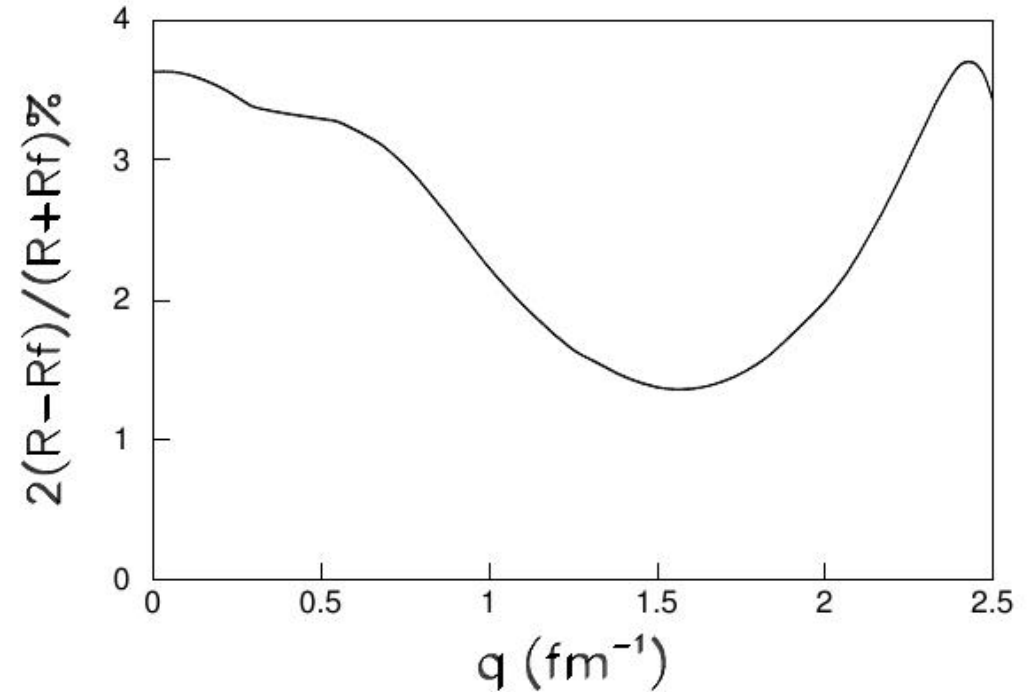
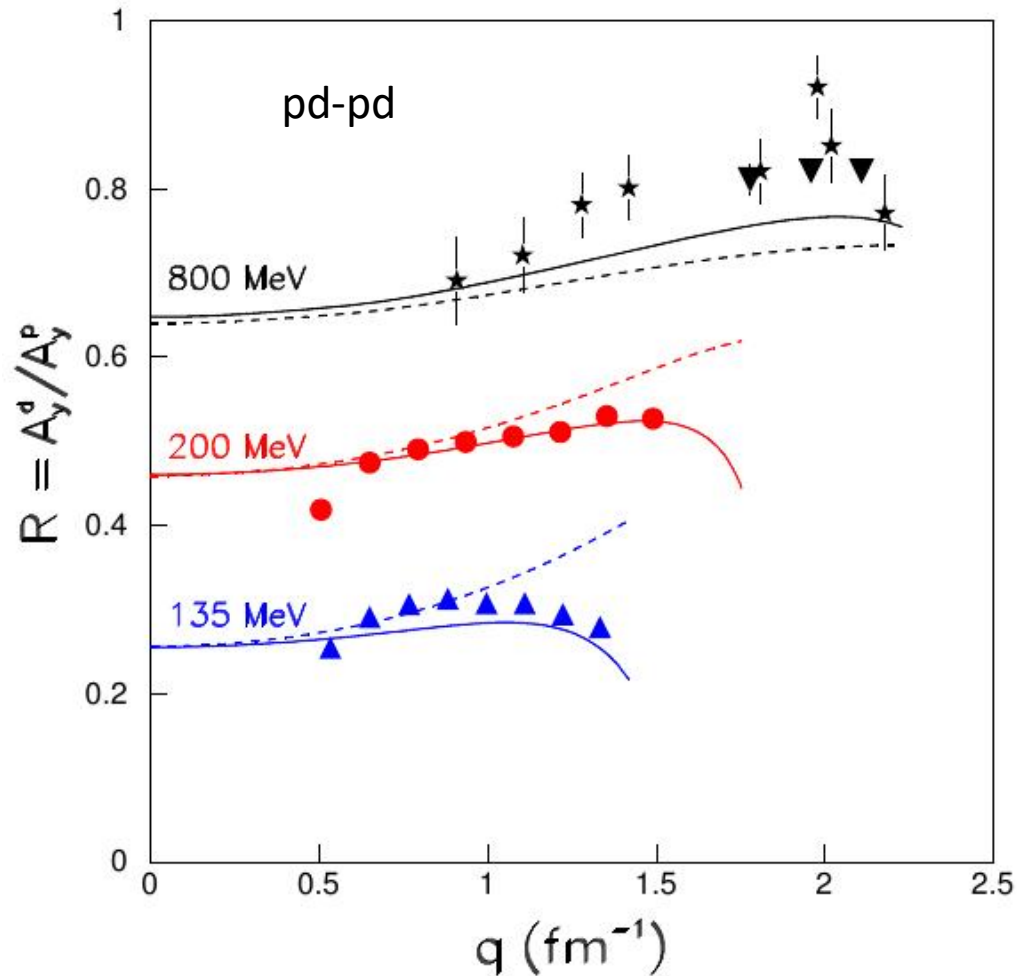


Figure 2: Difference between the predictions of the refined Glauber model [10](#) without (R) and with (Rf) the NN spin-spin contribution at 800 MeV expressed as a percentage of their average.

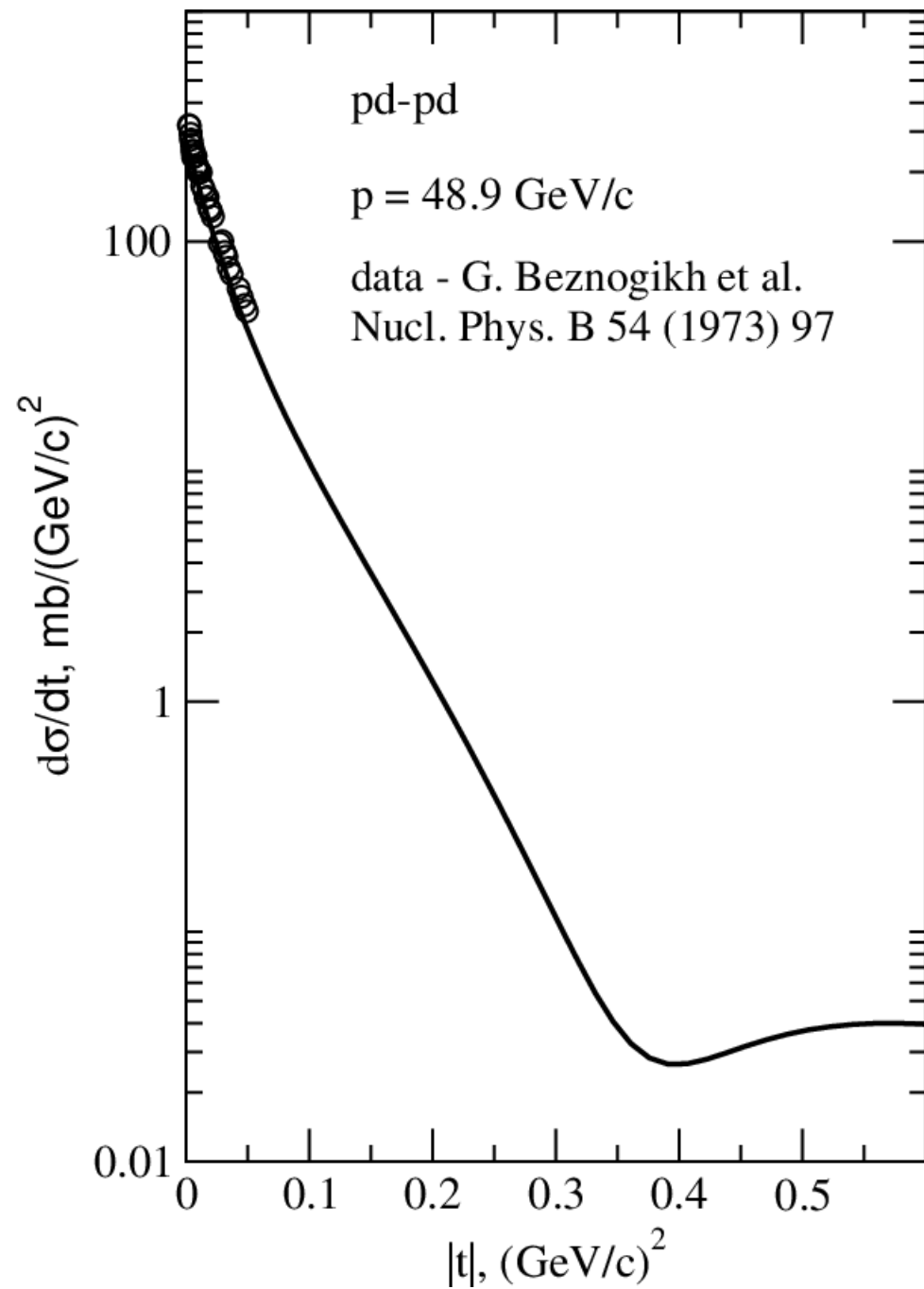
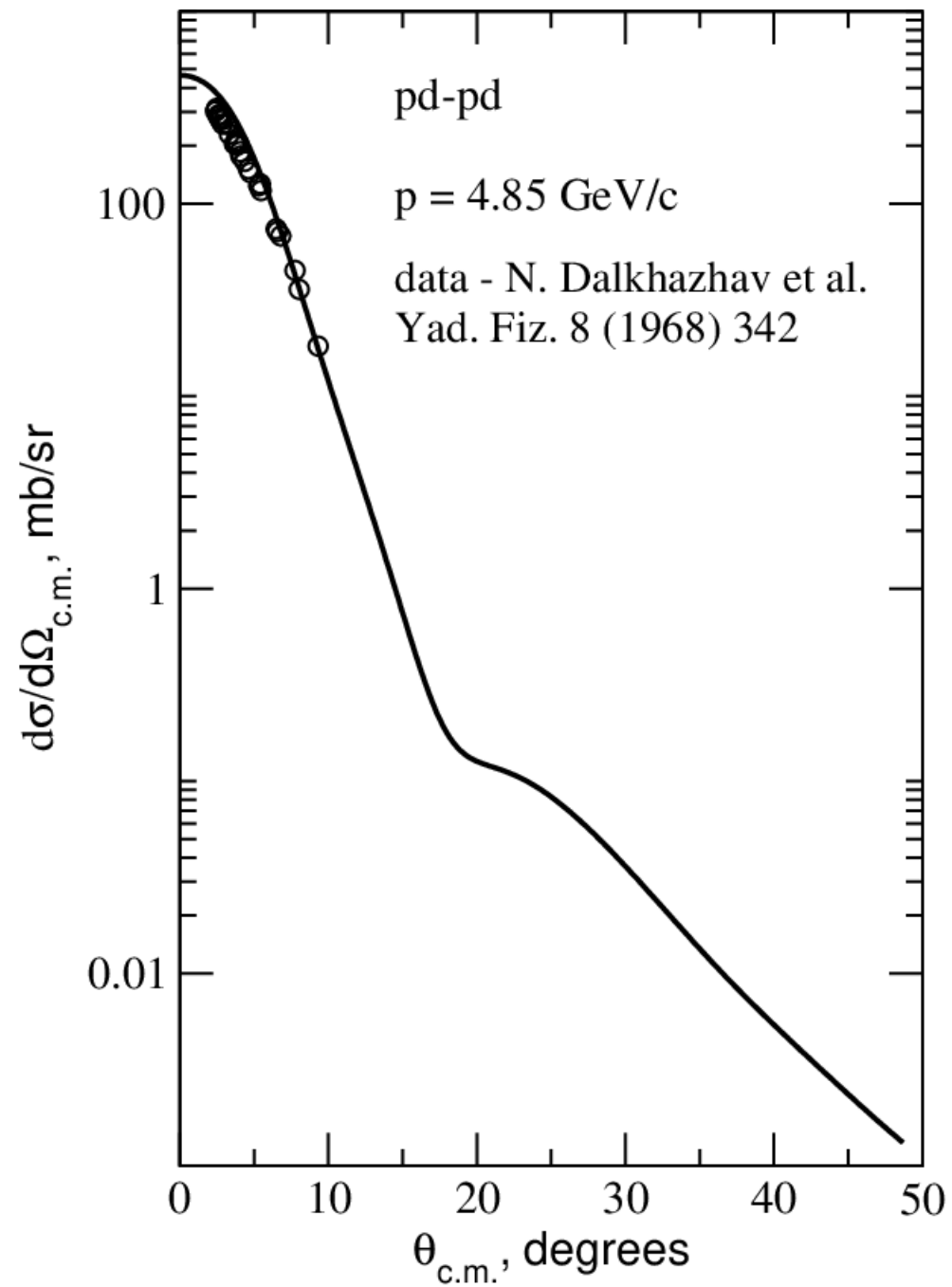
RESULTS OF pd-pd CALCULATIONS within THE GLAUBER THEORY FOR SPD NICA

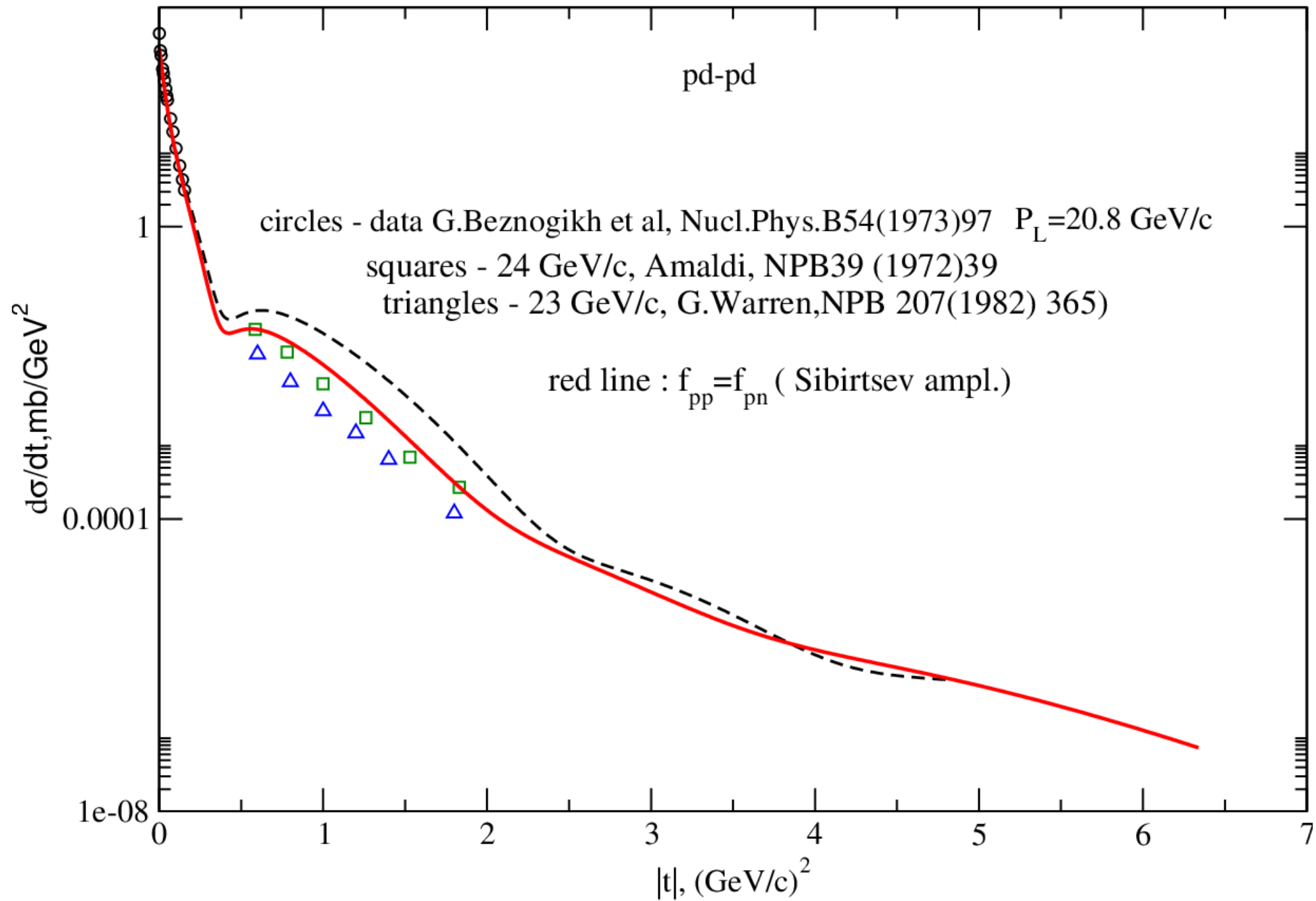
pp $\sqrt{s_{NN}} = 3.4 - 27 GeV$

dd $\sqrt{s_{dd}} = 6.7 - 28 GeV$

pd $\sqrt{s_{pd}} = 4.76 - 15.3 GeV$

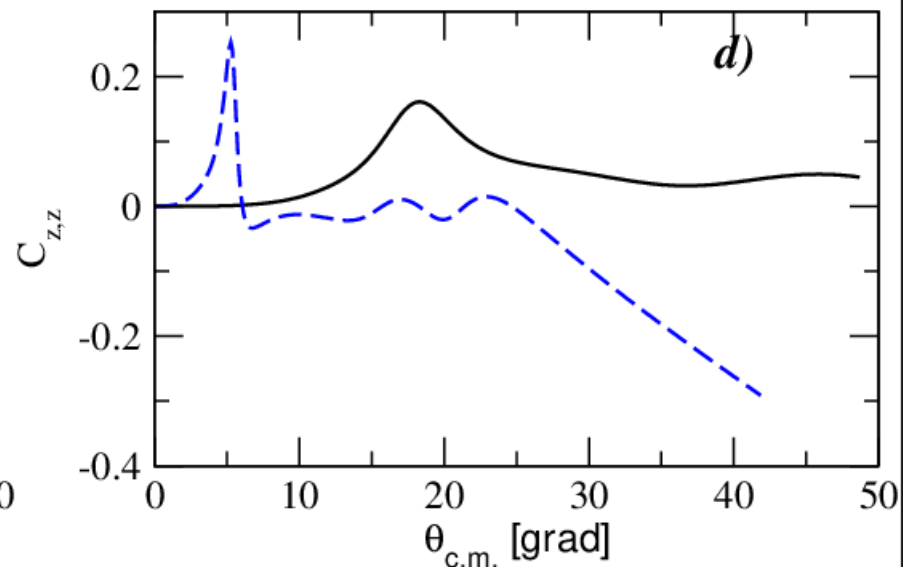
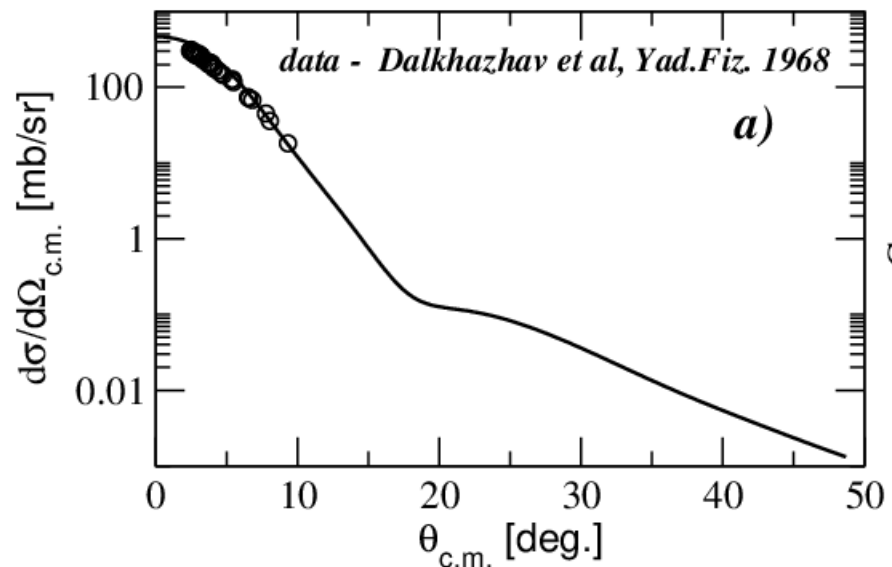
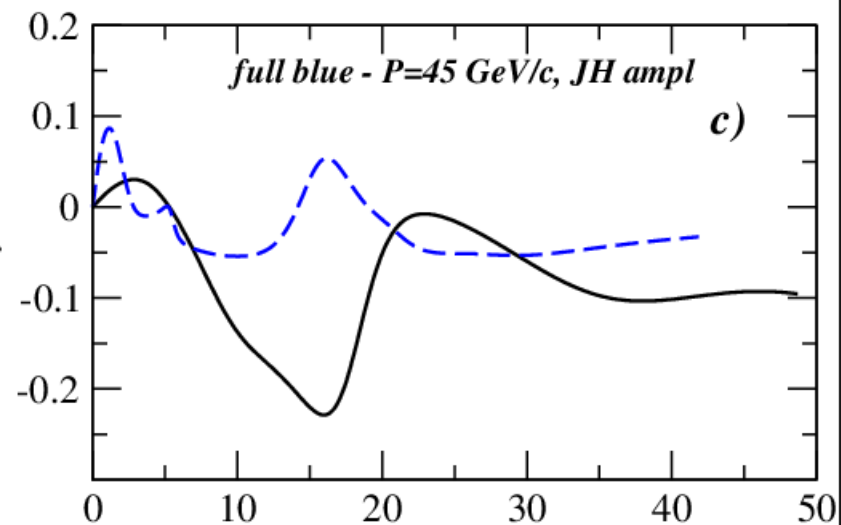
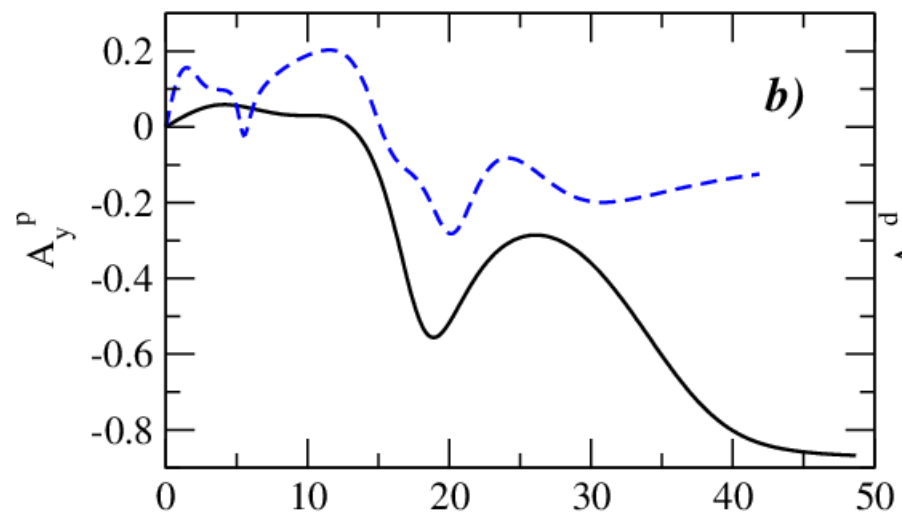
$$L \sim 10^{27} - 10^{32} cm^{-2} s^{-1}$$





pd- elastic

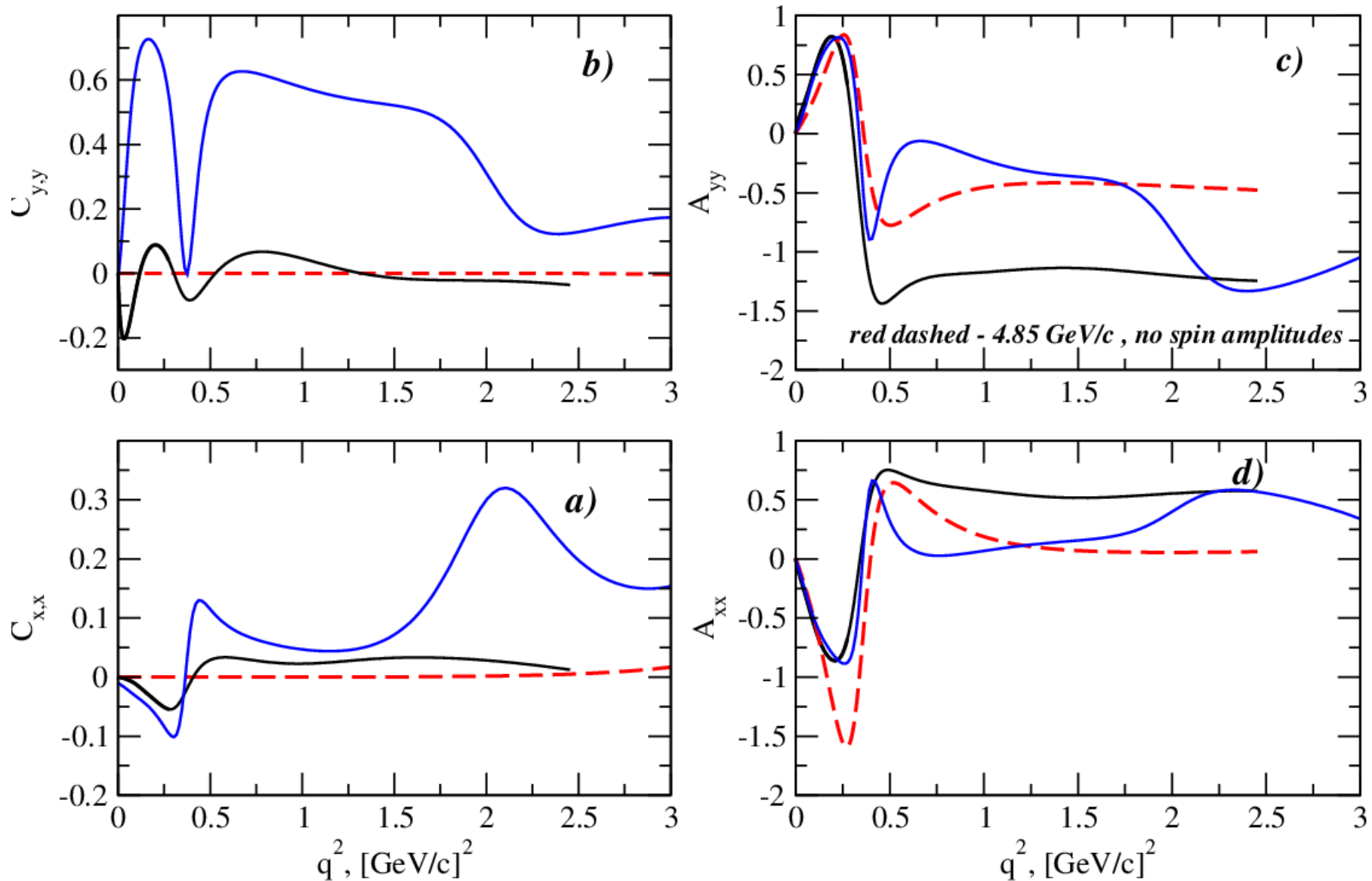
full black - $P_L=4.85$ GeV/c with JH; dashed blue - 45 GeV/c with JH-3 ampl.



pd- elastic

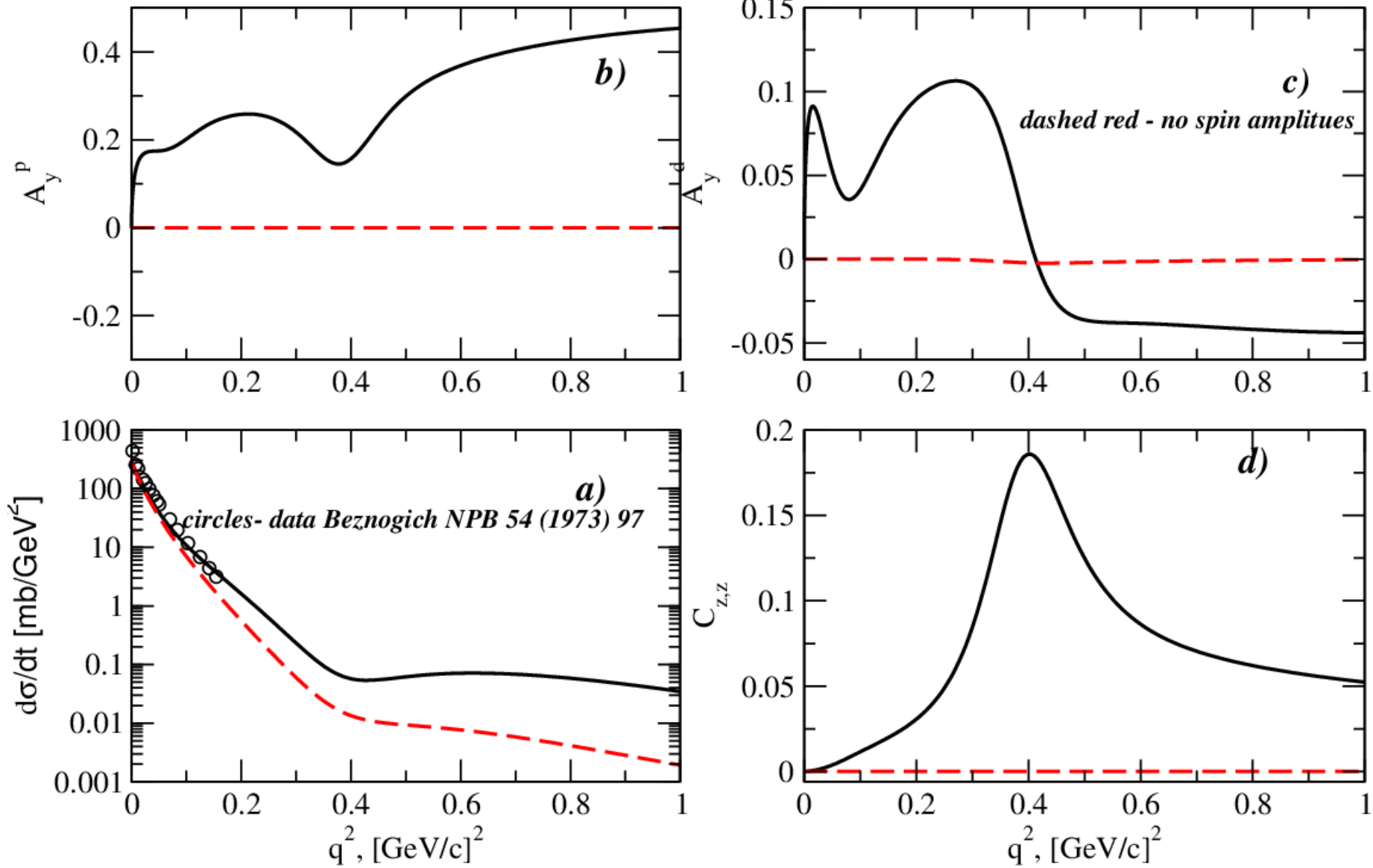
full black - $P_L=4.85$ GeV/c with Sibirtsev amplitudes; full blue - 45 GeV/c (JH)

dashed red - 4.85 GeV/c without spin dependent pN amplitudes



pd- elastic

full black - $P_L=20.4$ GeV/c with Sibirtsev amplitudes



Quasielastic scattering



$$p + d \rightarrow \{pp\}_s + n$$

$$\mathcal{F} = \mathcal{A}(\mathbf{e} \cdot \mathbf{k})(\boldsymbol{\sigma} \cdot \mathbf{k}) + \mathcal{B}\mathbf{e} \cdot \boldsymbol{\sigma},$$

$$p + n \rightarrow n + p$$

$$f_{12}^{collin} = \alpha + \beta(\boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2) + (\epsilon - \beta)(\boldsymbol{\sigma}_1 \cdot \mathbf{k})(\boldsymbol{\sigma}_2 \cdot \mathbf{k}).$$

$$\mathcal{A} = (\epsilon - \beta)S(Q/2), \quad \mathcal{B} = \beta S(Q/2)$$

$$d\sigma_0 = \frac{1}{3} \mathcal{K} \{ |\varepsilon|^2 + 2|\beta|^2 \},$$

$$T_{20} = \frac{1}{\sqrt{2}} A_{zz} = \sqrt{2} \frac{|\beta|^2 - |\varepsilon|^2}{|\varepsilon|^2 + 2|\beta|^2},$$

$$C_{x,x} = C_{y,y} = -2 \frac{\operatorname{Re} \varepsilon \beta^*}{|\varepsilon|^2 + 2|\beta|^2}, \quad C_{xz,y} = -C_{yz,x} = 3 \frac{\operatorname{Im} \beta \varepsilon^*}{|\varepsilon|^2 + 2|\beta|^2}.$$

Complete polarization experiment gives: $|\varepsilon|, |\beta|, \operatorname{Re} \varepsilon \beta^*, \operatorname{Im} \varepsilon \beta^*$

Search for T-invariance violation in double polarized pd - scattering

Yu.N. U. , J. Haidenbauer, PRC 94 (2016) 035501

Yu. N. U., A. Temerbayev , PRC 92 (2015) 014002

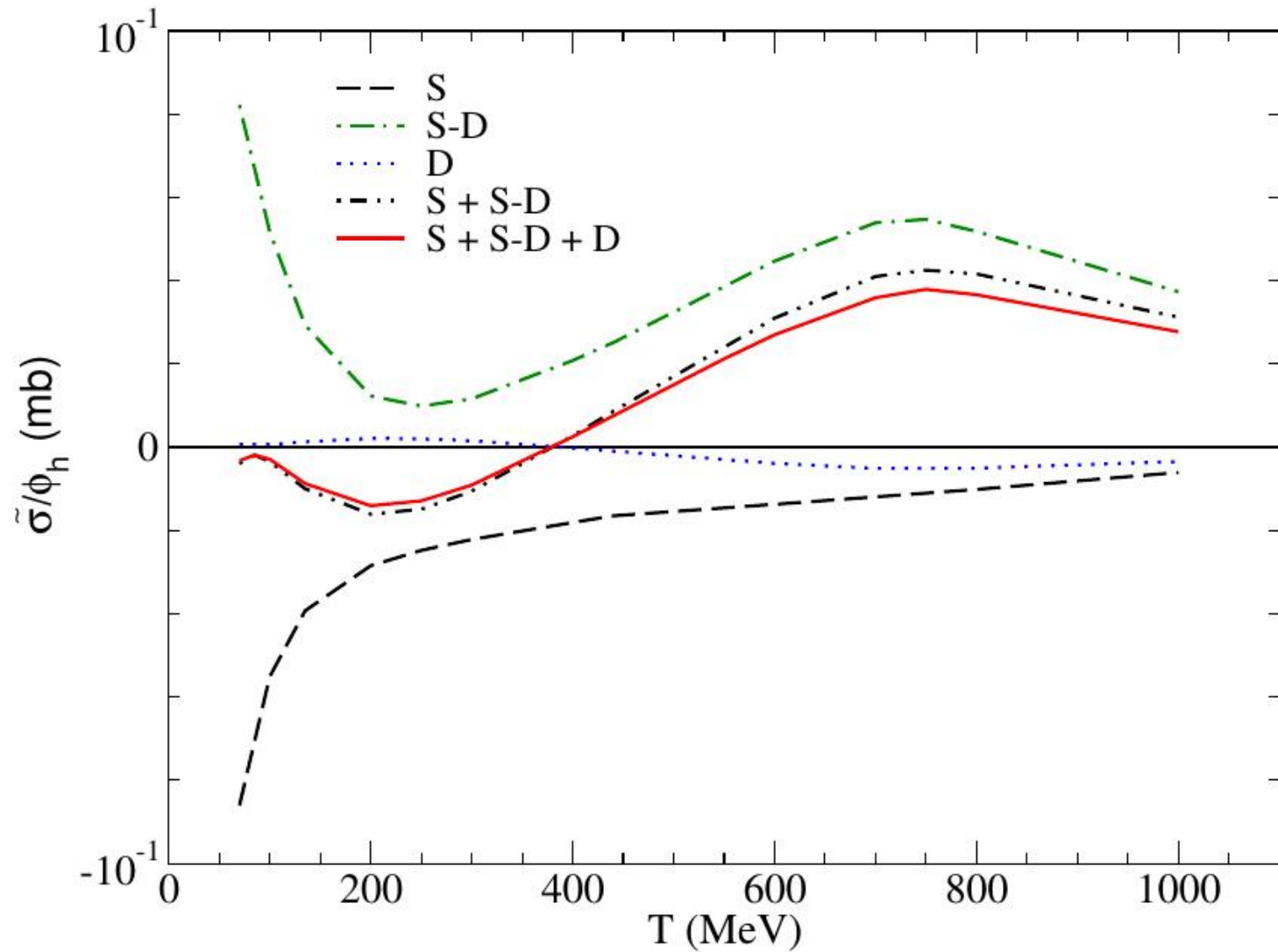
N. Nikolaev, F.Rathman, A. Silenko, Yu.N. Uzikov, [2004.09943](#) [nucl-th]

$$C' \approx i\phi_5 + iq/2m(\phi_1 + \phi_3)/2$$

Yu.N.U., A.A. Temerbayev, PRC 92 (2015) 014002;

Yu.N.U., J. Haidenabuer, PRC 94 (2016) 035501.

$$\sigma_{tot} = \underbrace{\sigma_0 + \sigma_1 \mathbf{p}^p \cdot \mathbf{P}^d + \sigma_2 (\mathbf{p}^p \cdot \hat{\mathbf{k}})(\mathbf{P}^d \cdot \hat{\mathbf{k}}) + \sigma_3 P_{zz}}_{T\text{-even}, P\text{-even}} + \underbrace{\tilde{\sigma}_{tvpc} p_y^p P_{xz}^d}_{T\text{-odd}, P\text{-even}}$$



CONCLUSION

- Spin-dependent Glauber theory of pd- elastic scattering works well in describing of pd spin observables at moderate energies 0.1-3 GeV. Hopefully, this theory should work also at higher energies, 3-50 GeV .
- Existing data on pp- and especially pn- elastic spin amplitudes above 3 GeV are rather poor, although different phenomenological parametrizations are available.
- Test of T-invariance in pd double polarized scattering at NICA energies requires knowledge of pN-spin amplitudes.
- Measurement of single and *double spin observables of pd- elastic and quasielastic scattering at SPD NICA energies and comparison with our results of the Glauber calculations* will give a clean test for pp- and pn- amplitudes.

Thank you for attention!

APPENDIX

T-even P-even

$$M_N(\mathbf{p}, \mathbf{q}; \boldsymbol{\sigma}, \boldsymbol{\sigma}_N)$$

$$= A_N + C_N \boldsymbol{\sigma} \hat{\mathbf{n}} + C'_N \boldsymbol{\sigma}_N \hat{\mathbf{n}} + B_N (\boldsymbol{\sigma} \hat{\mathbf{k}}) (\boldsymbol{\sigma}_N \hat{\mathbf{k}}) \\ + (G_N + H_N) (\boldsymbol{\sigma} \hat{\mathbf{q}}) (\boldsymbol{\sigma}_N \hat{\mathbf{q}}) + (G_N - H_N) (\boldsymbol{\sigma} \hat{\mathbf{n}}) (\boldsymbol{\sigma}_N \hat{\mathbf{n}})$$

T-odd P-even , M.Simonius,PRL 1997

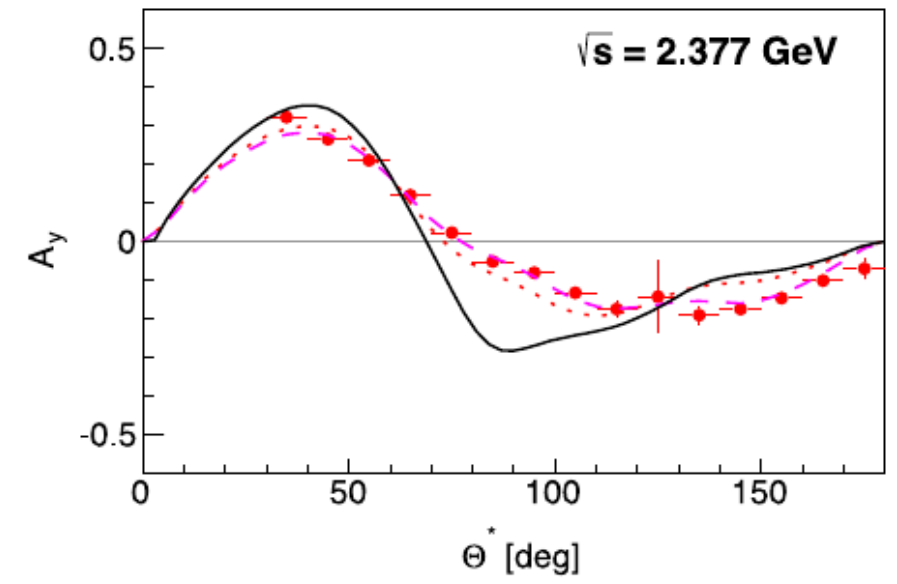
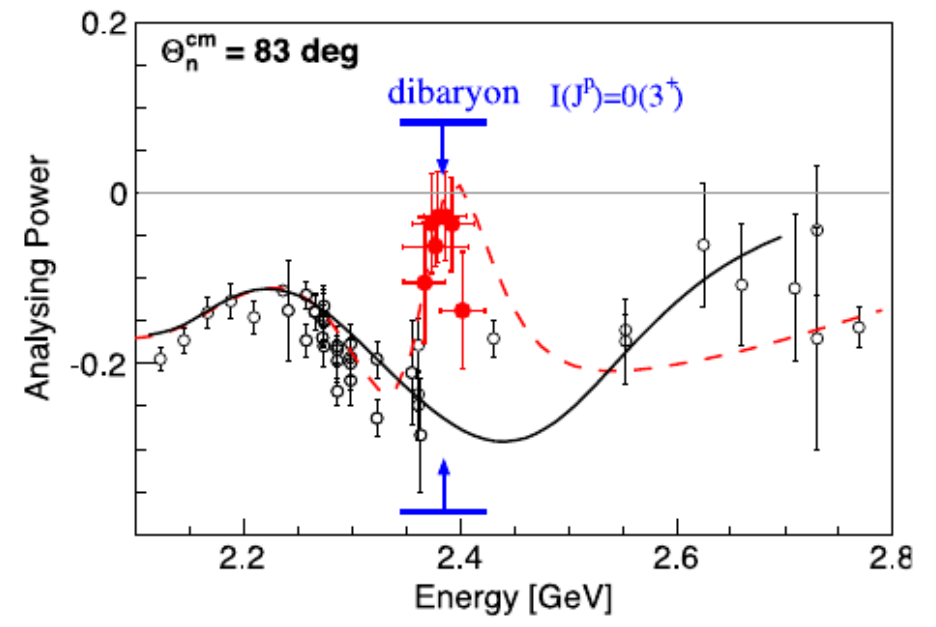
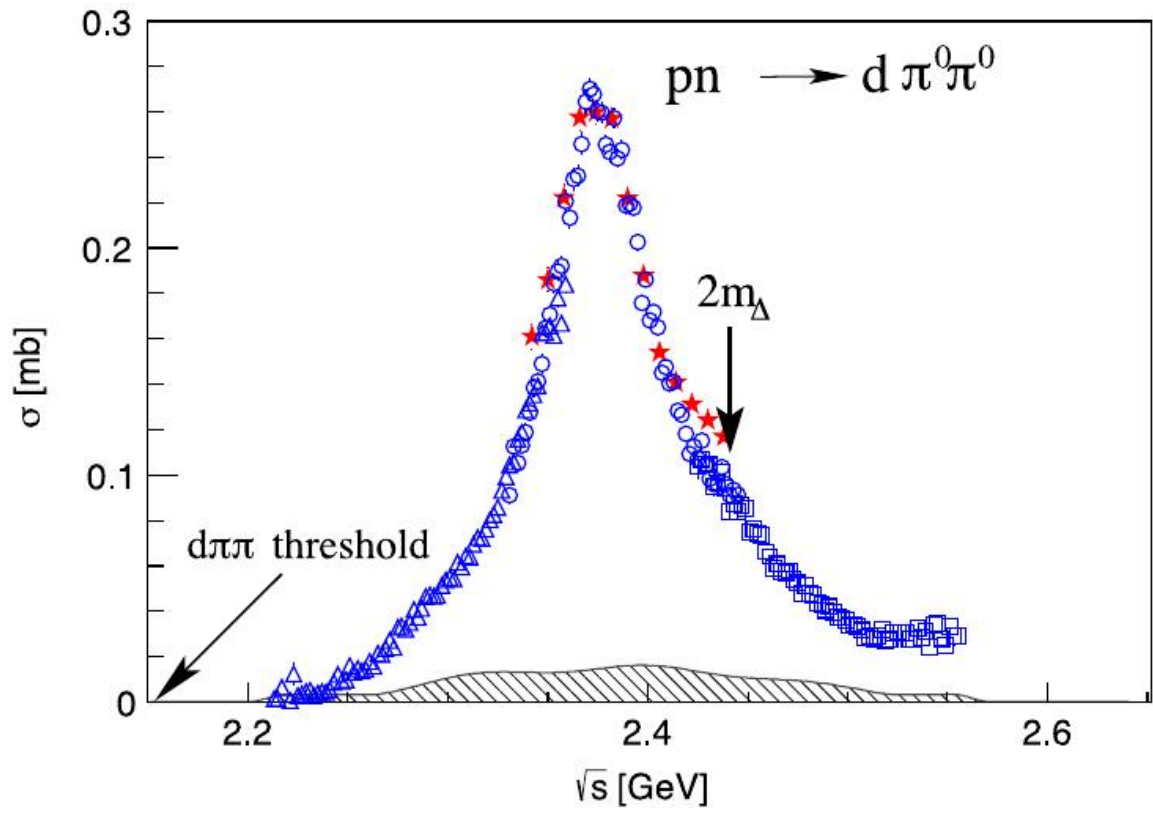
$$t_{pN} = h_N [(\boldsymbol{\sigma} \cdot \mathbf{k})(\boldsymbol{\sigma}_N \cdot \mathbf{q}) + (\boldsymbol{\sigma}_N \cdot \mathbf{k})(\boldsymbol{\sigma} \cdot \mathbf{q}) \\ - \frac{2}{3} (\boldsymbol{\sigma}_N \cdot \boldsymbol{\sigma})(\mathbf{k} \cdot \mathbf{q})] / m_p^2 \\ + g_N [\boldsymbol{\sigma} \times \boldsymbol{\sigma}_N] \cdot [\mathbf{q} \times \mathbf{k}] [\boldsymbol{\tau} - \boldsymbol{\tau}_N]_z / m_p^2 \\ + g'_N (\boldsymbol{\sigma} - \boldsymbol{\sigma}_N) \cdot i [\mathbf{q} \times \mathbf{k}] [\boldsymbol{\tau} \times \boldsymbol{\tau}_N]_z / m_p^2.$$

Null-test signal:

$$\tilde{g} = \frac{i}{4\pi m_p} \int_0^\infty dq q^2 \left[S_0^{(0)}(q) - \sqrt{8} S_2^{(1)}(q) - 4 S_0^{(2)}(q) \right. \\ \left. + \sqrt{2} \frac{4}{3} S_2^{(2)}(q) + 9 S_1^{(2)}(q) \right] [-C'_n(q) h_p + C'_p(q) (g_n - h_n)]$$

d*(2380) dybarion $J^P = 3^+$

H. Clement / Progress in Particle and Nuclear Physics 93 (2017) 195–242



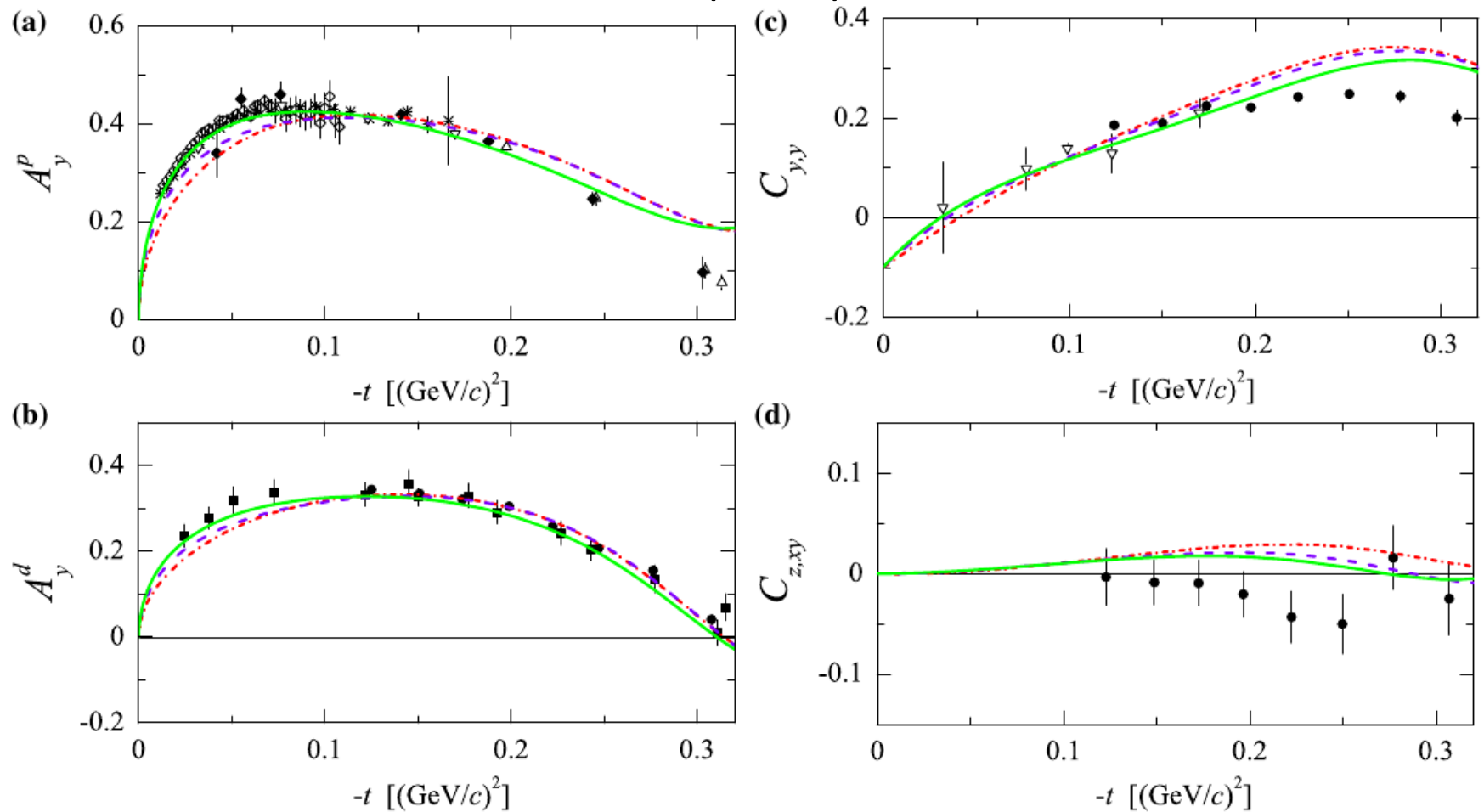


Fig. 8 Proton analyzing power A_y^p (a), deuteron analyzing power A_y^d (b), vector spin-correlation parameter $C_{y,y}$ (c) and tensor spin-correlation parameter $C_{z,xy}$ (d) in pd (dp) elastic scattering at the incident (equivalent) proton energy $T_p = 800$ MeV. Dash-dotted (red),

dashed (violet) and solid (green) lines show the refined Glauber model calculations with NN amplitudes corresponding to the SAID PWA solution SM16 [35,41], with the modified amplitude C_p and with modified amplitudes C_p and C_n (see Fig. 6), respectively. Experimental data at $T_p = 796$ and 800 MeV are the same as in Figs. 2, 4 and 5

– *Planned experiments to search for CP violation beyond the SM*

- Detecting a non-zero **EDM** of elementary fermion (neutron, atoms, charged particles). The current experimental limit

$$|d_n| \leq 2.9 \times 10^{-26} e cm$$

is much less as compared the SM estimation (B.H.J. McKellar et al. PLB 197 (1987))

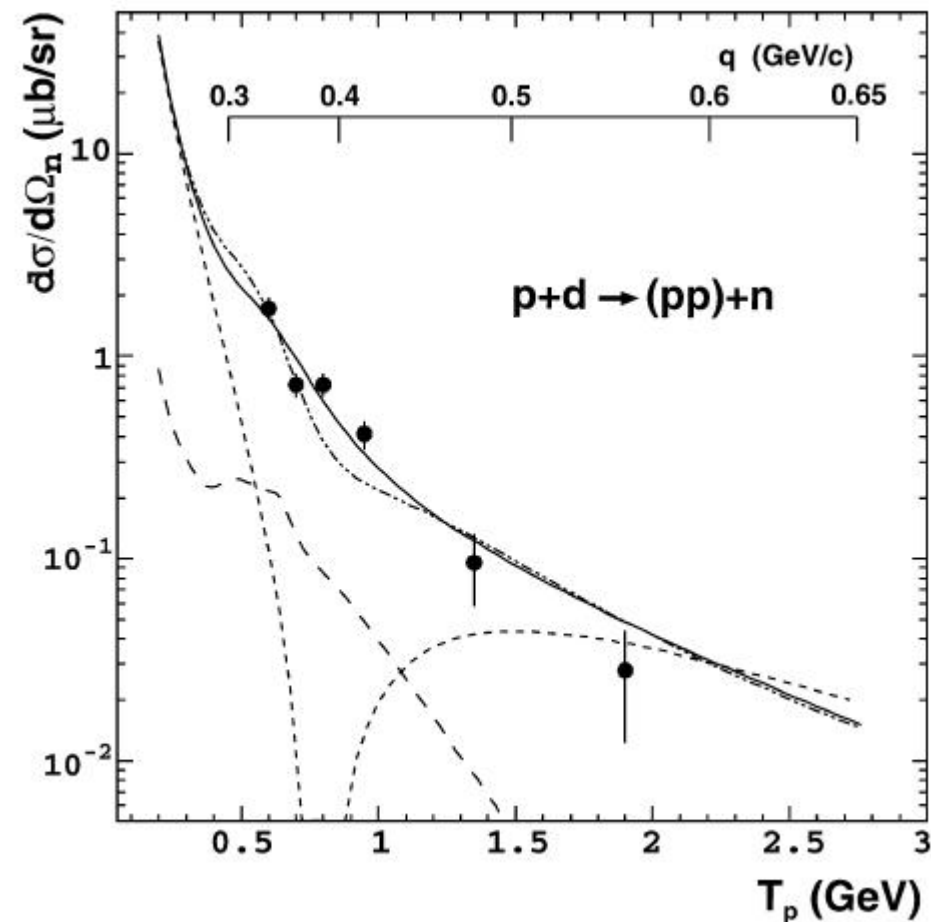
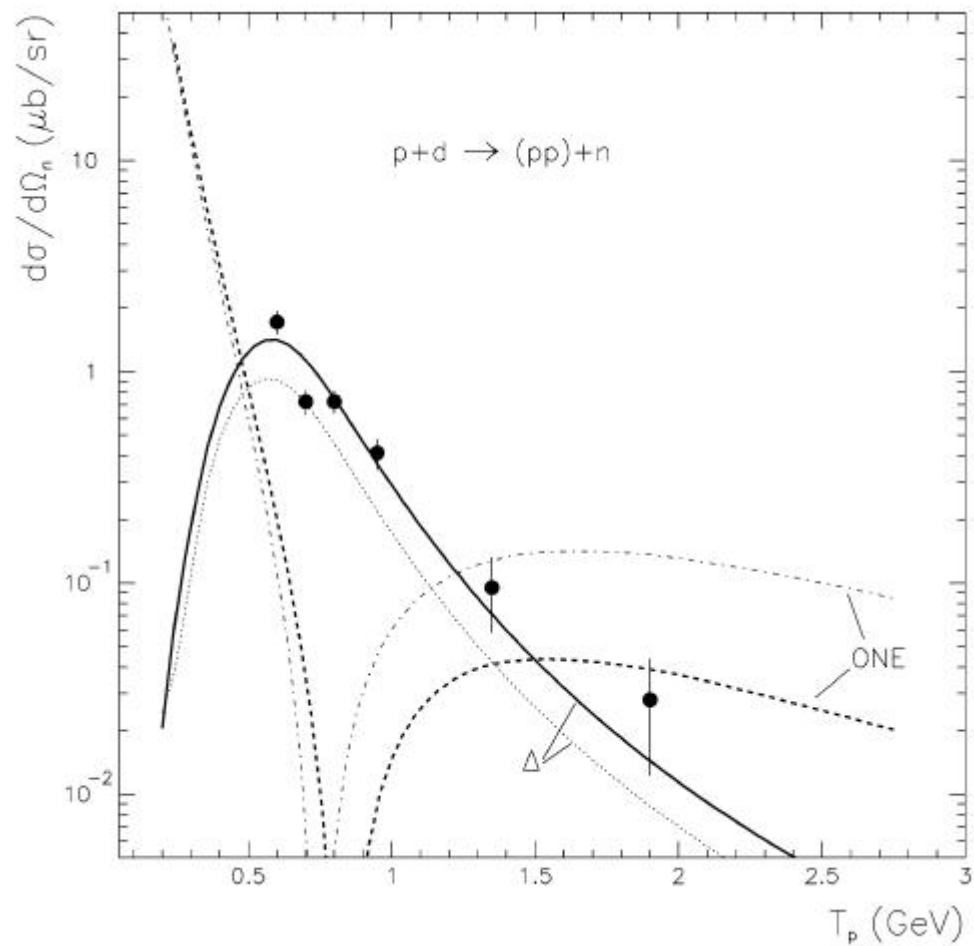
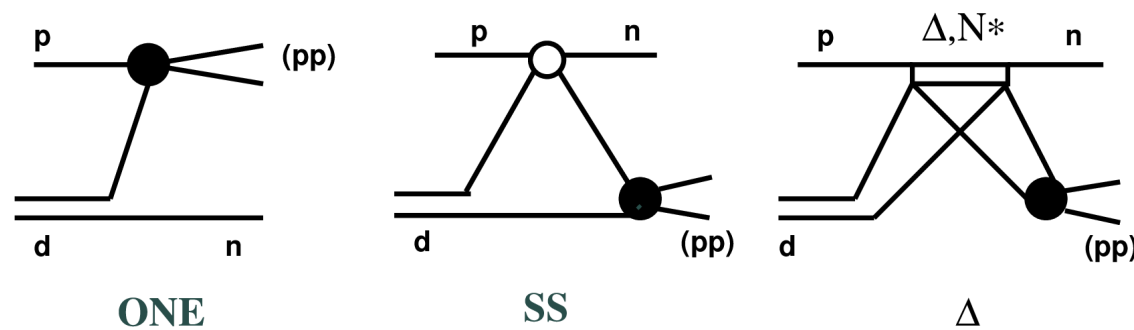
$$1.4 \times 10^{-33} e cm \leq |d_n| \leq 1.6 \times 10^{-31} e cm$$

- Search for CP violation in the **neutrino sector** ($\theta_{13} \neq 0$, then generation of lepton asymmetry and via $B - L$ conservation to get the BAU).

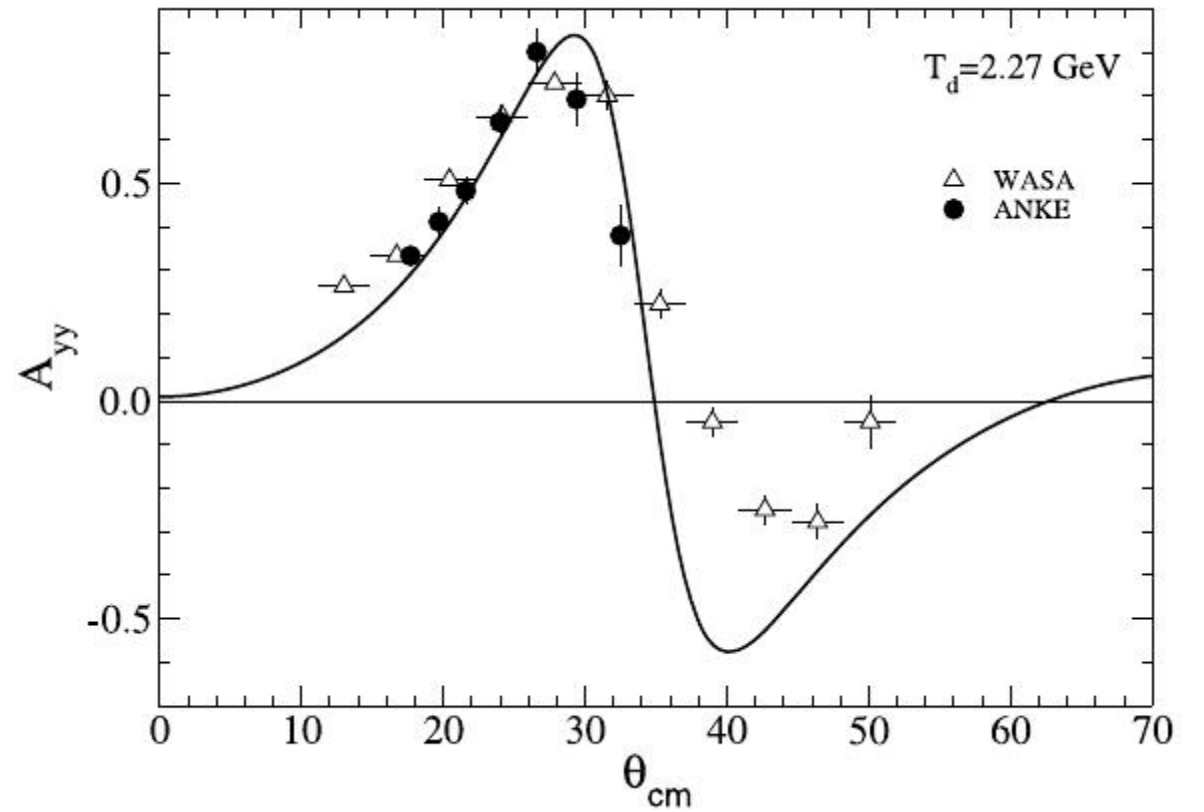
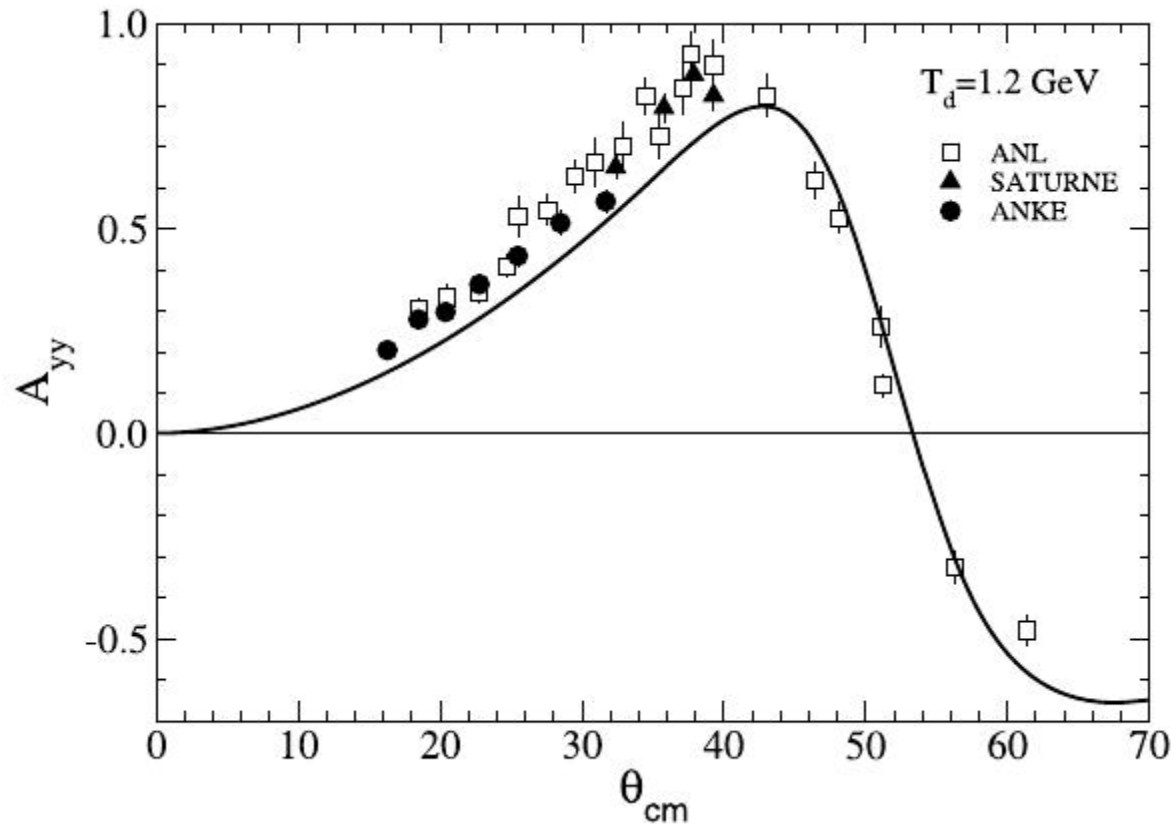
Those are T-violating and Parity violating (**TVPV**) effects.

Much less attention was paid to T-violating P-conserving (TVPC) flavor conserving effects.

J. Haidenbauer, Yu. Uzikov, PLB (2003)



D. Mchedlishvili et al. Nucl.Phys. A 977 (2018) 14 , pd-elastic



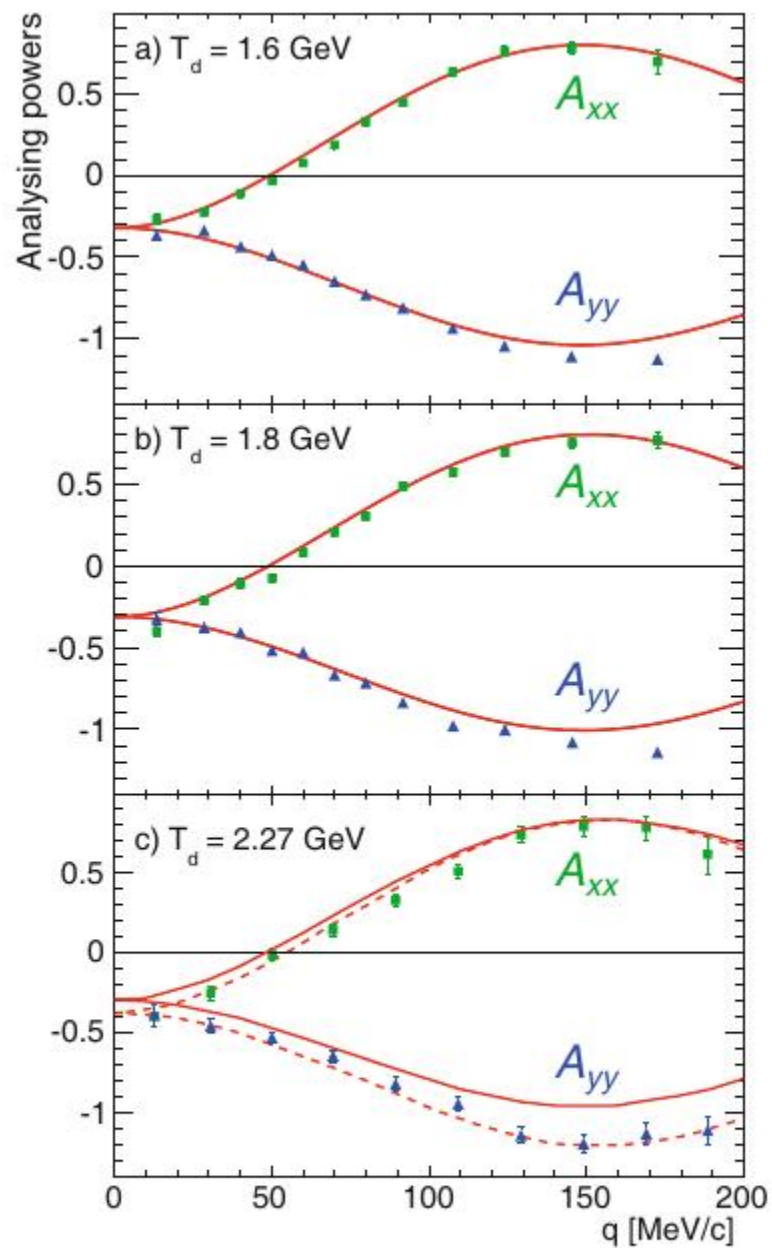
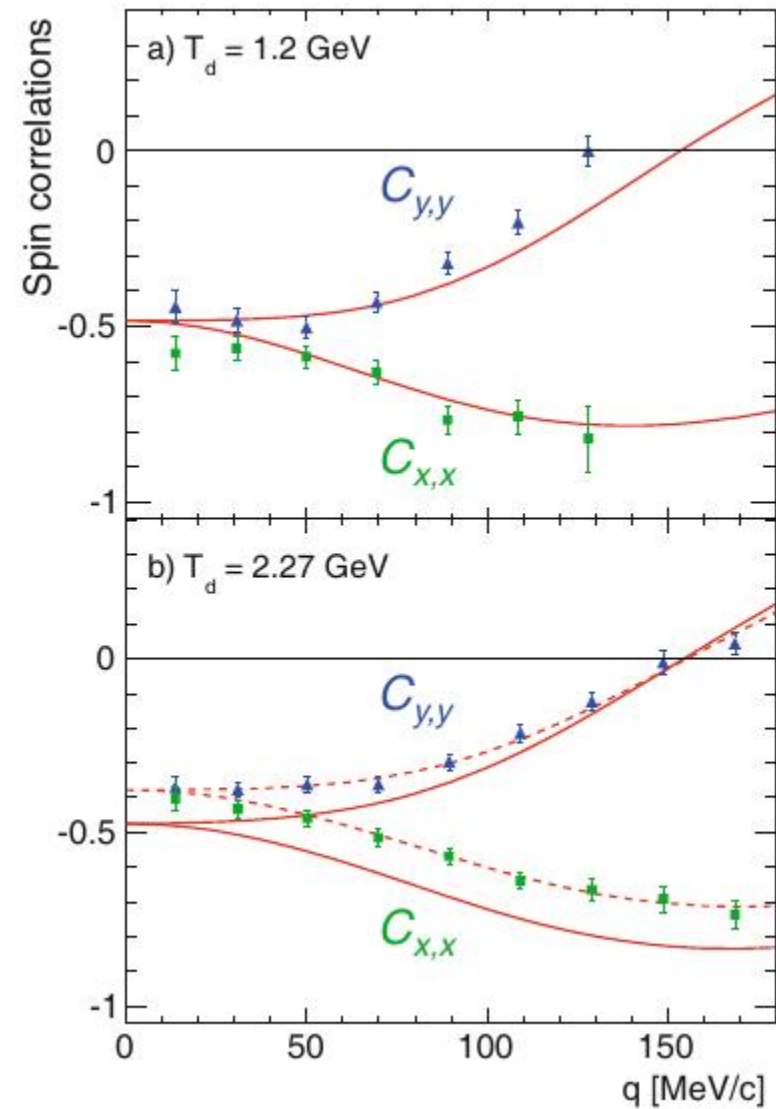
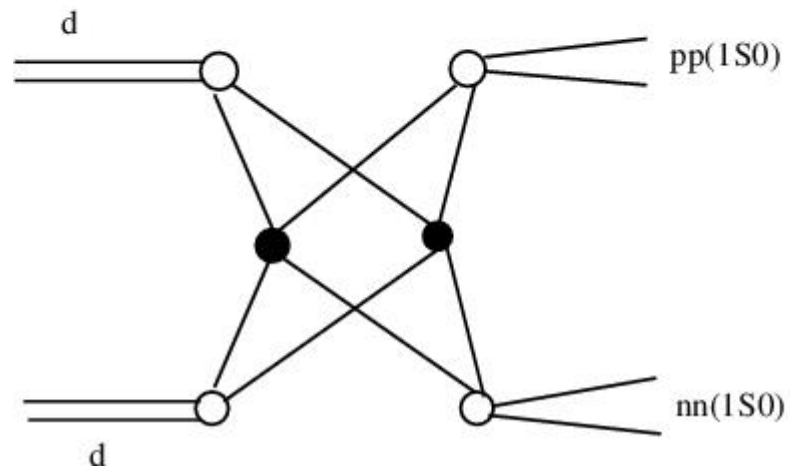
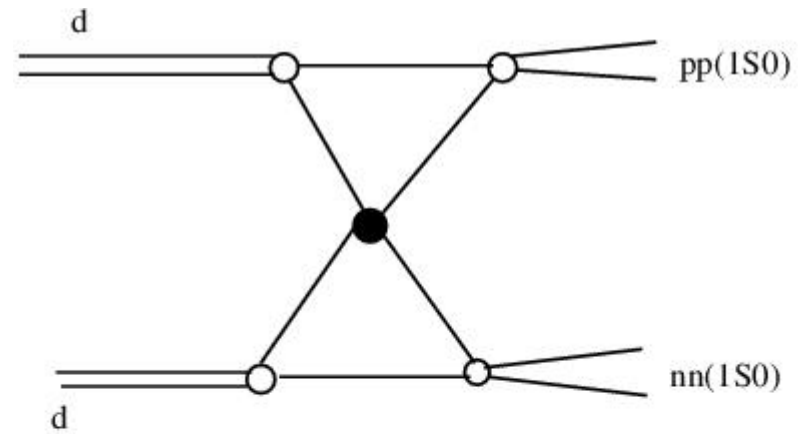


Fig. 8. Tensor analysing powers A_{xx} (squares) and A_{yy} (triangles) of the $\vec{d}p \rightarrow \{pp\}_s n$ reaction at three beam energies for low diproton excitation energy, $E_{pp} < 3 \text{ MeV}$, compared to im-



pd- \rightarrow (pp)+n, $E_{pp} < 3 \text{ MeV}$, 150 ANKE
 D. Mchedlishvili, et al. EPJA 49 (2013)

dd- elastic and quasi-elastic scattering



$$Del = \frac{d\sigma / dt_{data.} - d\sigma / dt_{theor-exp.}}{d\sigma / dt_{theor-exp.}}$$

**P. Gauron, B. Nicolescu, O.V. Selyugin, PLB
397 (1997)**

