

# Contribution of tensor forces to formation of Gamow-Teller Resonance and its overtone in closed-shell parent nuclei

S.Yu. Igashov<sup>1</sup>, G.V. Kolomiytsev<sup>2</sup>, M.H. Urin<sup>2</sup>

<sup>1</sup>*The Federal State Unitary Enterprise Dukhov Automatics Research Institute (VNIIA), 127055, Russia, Moscow*

<sup>2</sup>*National Research Nuclear University "MEPhI" (Moscow Engineering Physics Institute), 115409, Russia, Moscow*

A mean-field and interaction in the particle-hole (p-h) channel are the input quantities for any RPA-based approach to describing Gamow-Teller Resonance and its overtone — Isovector Giant Spin-Monopole Resonance in the  $\beta^{(-)}$ -channel (GTR and IVGSMR<sup>(-)</sup>, respectively). The recent example of such an approach is given in Ref. [1], where main properties of mentioned resonances in <sup>208</sup>Bi are described within the continuum-RPA-based semimicroscopic p-h dispersive optical model. A realistic partially self-consistent phenomenological mean field and Landau-Migdal p-h interaction have been used in this study. Provided that dimensionless strength  $g'$  of the spin-isospin part of the mentioned interaction is adjusted to reproduce in calculations of the GT strength function the observable GTR energy, the calculated IVGSMR<sup>(-)</sup> energy is found to be less (on about 3 MeV) than respective experimental value. In the present study, we attempt to resolve this puzzle by taking into account tensor forces, which lead to mixing  $1^+$  spin-monopole and spin-quadrupole excitations. In applying to describing GT strength distribution, tensor forces have been considered in Ref. [2]. Mentioned mixing takes place due to both the spin-orbit term in a mean field (so-called nonsymmetric or non-diagonal approximation in RPA-based approaches employing central forces [3] and non-central (tensor) forces. Using the mentioned continuum-RPA-based analysis of Ref. [1] as a starting point, we resolved the above-described puzzle related to evaluation of the IVGSMR<sup>(-)</sup> energy by taking tensor forces into account. As expected, the strength parameter of the spin-isospin part of non-central forces  $g'_T$  is found to be less than the Landau-Migdal parameter  $g'$ .

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2. A. P. Severyukhin and H. Sagawa, *Prog. Theor. Exp. Phys.* 103D03 (2013).
3. M.G. Urin, "Relaxation of nuclear excitations". Moscow, Energoatomizdat, 1991 (in Russian).

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External field (probing operator)

$$V_{JLSM}^{(-)}(\mathbf{r}) = V_{JLS}^{(-)}(r) T_{JLSM}(\mathbf{n}), \quad J=1, S=1, L=0, L=2$$

$$\tilde{V}_{J=1,L=0,S=1}^{(-)}(r) = \begin{cases} V_{GT} = 1 \\ V_{SM}(r) = r^2 - \eta \end{cases}$$

$$T_{JLSM}(\mathbf{n}) = \sum_{m\mu} \langle Lm, S\mu | JM \rangle Y_{Lm} \cdot \boldsymbol{\sigma}_{S,M}$$

$$T_{J=1,L=0,S=1,M} = Y_{00} \cdot \boldsymbol{\sigma}_{1,M}$$

Effective field

$$\tilde{V}_{J=1,M}^{(-)}(\mathbf{r}, \omega) = \tilde{V}_{J=1,L=0,S=1}^{(-)}(r, \omega) T_{J=1,L=0,S=1,M}(\mathbf{n}) + \tilde{V}_{J=1,L=2,S=1}^{(-)}(r, \omega) T_{J=1,L=2,S=1,M}(\mathbf{n})$$

Set of eqs. for the radial effective fields:

$$\begin{aligned} \tilde{V}_{J,L=0,S}^{(-)}(r, \omega) = V_{J,L=0,S}^{(-)}(r) + \frac{2G'}{r^2} \int_0^\infty A_{J;L=0,L=0,S,S}^{(-)}(r, r', \omega) \tilde{V}_{J,L=0,S}^{(-)}(r', \omega) dr' + \\ + \frac{2G'}{r^2} \int_0^\infty A_{J;L=0,L=2,S,S}^{(-)}(r, r', \omega) \tilde{V}_{J,L=2,S}^{(-)}(r', \omega) dr' \end{aligned}$$

$$\begin{aligned} \tilde{V}_{J,L=2,S}^{(-)}(r, \omega) = \frac{2G'}{r^2} \int_0^\infty A_{J;L=2,L=0,S,S}^{(-)}(r, r', \omega) \tilde{V}_{J,L=0,S}^{(-)}(r', \omega) dr' + \\ + \frac{2G'}{r^2} \int_0^\infty A_{J;L=2,L=2,S,S}^{(-)}(r, r', \omega) \tilde{V}_{J,L=2,S}^{(-)}(r', \omega) dr' \end{aligned}$$

$$\begin{aligned} A_{J;L=0,L=2,S,S}^{(-)}(r, r', \omega) = \sum_{(\pi), \nu} n_\nu t_{(\pi)(\nu)}^{J,L=0,S} t_{(\pi)(\nu)}^{J,L=2,S} \chi_\nu(r) \chi_\nu(r') g_{(\pi)}(r, r', E = E_\nu + \omega) + \\ + \sum_{(\nu), \pi} n_\pi t_{(\nu)(\pi)}^{J,L=0,S} t_{(\nu)(\pi)}^{J,L=2,S} \chi_\pi(r) \chi_\pi(r') g_{(\nu)}(r, r', E = E_\pi - \omega) \end{aligned}$$

$$t_{(\nu)(\lambda)} = \frac{\langle j_\nu l_\nu \| T_{JLS} \| j_\lambda l_\lambda \rangle}{\sqrt{2J+1}}$$

Polarizability

$$\begin{aligned} P^{(-)}\left(\left[\tilde{V}_{J,L=0,S}^{(-)}\right], \omega\right) = \int_0^\infty \int_0^\infty V_{J,L=0,S}^{(-)}(r) \left\{ A_{J;L=0,L=0,S,S}^{(-)}(r, r', \omega) \tilde{V}_{J,L=0,S}^{(-)}(r', \omega) + \right. \\ \left. A_{J;L=0,L=2,S,S}^{(-)}(r, r', \omega) \tilde{V}_{J,L=2,S}^{(-)}(r', \omega) \right\} dr dr' \end{aligned}$$

Strength function

$$S\left(\left[\tilde{V}_{J,L=0,S}^{(-)}\right], \omega\right) = -\frac{1}{\pi} \text{Im} P^{(-)}\left(\left[\tilde{V}_{J,L=0,S}^{(-)}\right], \omega\right)$$