

# CMS Draft Analysis Note

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## Measurement of the top quark mass with single top events at 13 TeV

T. Aziz<sup>1</sup>, R. Karnam<sup>1</sup>, M. Kumar<sup>1</sup>, S. Mitra<sup>2</sup>, G.B. Mohanty<sup>1</sup>, and T. Müller<sup>2</sup>

<sup>1</sup> Tata Institute of Fundamental Research

<sup>2</sup> Karlsruhe Institute of Technology

### Abstract

A measurement of the top quark mass is performed with single top events using  $35.9 \text{ fb}^{-1}$  of proton-proton collision data collected at  $\sqrt{s} = 13 \text{ TeV}$  by the CMS experiment during 2016. The analysis is performed in the  $t \rightarrow bW \rightarrow b\ell\nu$  decay channel. Signal events are selected by requiring an isolated energetic muon or electron, large missing transverse momentum, and at least two hadronic jets. One of the jets is identified to originate from a bottom quark or antiquark, whereas the other results from the hadronization of a light-flavor quark within the pseudorapidity range  $|\eta| \leq 4.7$ . The masses of top quark and antiquark (along with their difference) are determined separately depending on the charge of the lepton in the final state. The analysis is in progress in a "blind" way and the final result is expected soon.

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## 1 Introduction

The top quark mass is one of the most important parameters of the standard model (SM) of particle physics. Its precise measurement is of profound importance, both for theory and experiment. It constitutes a major input to the global electroweak fits, used to verify the self-consistency of the SM. Its value is also directly related to the stability of electroweak vacuum, because among all SM particles it is the largest contributor in terms of radiative corrections to the mass and self-coupling [1] of the Higgs boson. From the experimental perspective, it provides an ideal benchmark to determine the calibration and performance of the detector as well as of reconstruction algorithms. The latest world average of the top mass [2], based on measurements performed with top pair ( $t\bar{t}$ ) events, from ATLAS, CMS, CDF and D0 collaborations, is :

$$m_t = 173.34 \pm 0.27 \text{ (stat)} \pm 0.71 \text{ (syst)} \text{ GeV} \quad (1)$$

Top quarks are produced copiously in proton-proton (pp) collisions at the Large Hadron Collider (LHC). Here,  $t\bar{t}$  events are dominantly produced via gluon-gluon fusion followed by quark-antiquark annihilation. A good number of single top quark events are also produced through charged-current interaction via the exchange of a  $W$  boson. Single top production, at leading order (LO) in the SM, can be realized in three modes, the  $t$ -channel, the  $tW$ -channel and the  $s$ -channel, ordered according to their cross sections. Feynman diagrams of these three production modes are shown in Figure 1. The  $t$ -channel is the most dominant single-top production mode in pp collisions at the LHC, with a total cross section of 217 pb calculated at next-to-leading order (NLO) with HATHORv2.1 [3, 4].

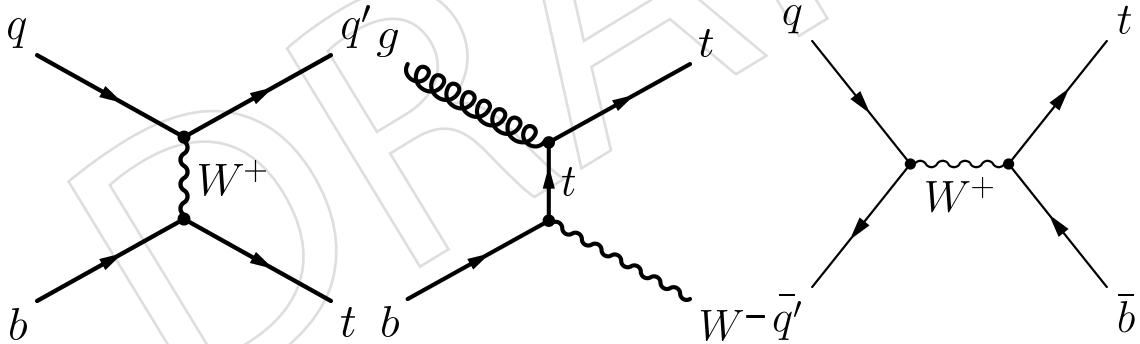


Figure 1: Feynman diagrams of single top production in the SM:  $t$ -channel (left) ,  $tW$ -channel (middle) and  $s$ -channel (right).

As alluded earlier, most of the top-quark mass measurements till date have been obtained with  $t\bar{t}$  events. Single top process provides an independent statistical sample to measure the same quantity. This process occurs at a lower energy scale compared to  $t\bar{t}$ . Further, it enriches the range of available measurements with systematics being partially uncorrelated from those considered for  $t\bar{t}$  events. The distinct production mechanism of the  $t$ -channel single top process dictates color connection only between the top quark and the proton, from which the initial  $b$ -quark is coming and not to the whole event as observed in  $t\bar{t}$  [5]. Such measurements therefore provide a useful check for any large unknown systematic effects arising due to the modeling of non-perturbative QCD processes in Monte Carlo (MC) simulations. Previous measurements of

the top quark mass with single top events were performed by both CMS and ATLAS using full Run-1 data collected at a centre-of-mass energy  $\sqrt{s} = 8$  TeV [6, 7]; the respective results are:

$$m_t = 172.95 \pm 0.77 \text{ (stat.) } {}_{-0.93}^{+0.97} \text{ (syst.) GeV,} \quad (2)$$

$$m_{\bar{t}} = 172.2 \pm 0.7 \text{ (stat.) } \pm 2.0 \text{ (syst.) GeV} \quad (3)$$

In the analysis reported here, a measurement of the top quark mass is performed with  $t$ -channel single top events using  $35.9 \text{ fb}^{-1}$  data collected at  $\sqrt{s} = 13$  TeV by the CMS experiment during 2016. A striking feature of this channel is the presence of a light-flavor quark in the final state, recoiling against the top quark (antiquark) in the high pseudorapidity ( $\eta$ ) region. The produced top quark (antiquark) almost exclusively decays to a bottom quark (antiquark) and a  $W^\pm$  boson. This analysis is focused on the muon and electron final states arising from direct and cascade (via  $\tau$  lepton) decays of the  $W^\pm$  boson, originating from the top quark (antiquark) decay. The outgoing bottom quark (antiquark) hadronizes to a jet that can be identified (“b-tagged”) using its characteristic signature inside the CMS detector. The four-momenta of the decay products of the top quark (antiquark) including the neutrino are either directly measured or estimated to calculate the invariant mass of the  $\ell\nu b$  system. An event selection based on the multivariate analysis (MVA) technique is designed to obtain a high-purity signal sample for the measurement. We measure the masses of top quark and antiquark separately by selecting events with positively and negatively charged leptons, respectively, in order to determine their mass difference as a test of the CPT invariance.

## 2 Data and MC Samples

### 2.1 Data samples

The analysis is based on the data recorded by CMS experiment, corresponding to a total integrated luminosity ( $L_{\text{int}}$ ) of  $35.9 \text{ fb}^{-1}$ . Table 1 lists the different run periods used for each dataset. Only luminosity sections certified as good according to the so-called *Golden JSON* file `Cert_271036-284044_13TeV_23Sep2016ReReco_Collisions16_JSON.txt` are considered. Luminosities are quoted from the pixel cluster counting method and are known with an uncertainty of 2.5% [8].

Table 1: List of data samples over different run periods.

Run period	Run range	Dataset name	$L_{\text{int}}$ ( $\text{fb}^{-1}$ )
Run B	272007–275376	/SingleMuon(Electron)/Run2016B-03Feb2017_ver2-v2/MINIAOD	5.8
Run C	275657–276283	/SingleMuon(Electron)/Run2016C-03Feb2017-v1/MINIAOD	2.6
Run D	276315–276811	/SingleMuon(Electron)/Run2016D-03Feb2017-v1/MINIAOD	4.2
Run E	276831–277420	/SingleMuon(Electron)/Run2016E-03Feb2017-v1/MINIAOD	4.1
Run F	277772–278808	/SingleMuon(Electron)/Run2016F-03Feb2017-v1/MINIAOD	3.1
Run G	278820–280385	/SingleMuon(Electron)/Run2016G-03Feb2017-v1/MINIAOD	7.5
Run H	280919–284044	/SingleMuon(Electron)/Run2016H-03Feb2017_ver{2,3}-v1/MINIAOD	8.6
Total	272007–284044		35.9

### 2.2 Signal and Background MC samples

The  $t$ -channel single top quark and antiquark events are generated using the NLO generator POWHEG [9–11] within the four-flavor scheme and the parton distribution function (PDF) set NNPDF3.0 [12]. Several SM background processes are considered in the analysis. The  $t\bar{t}$  process and production of single top quark and antiquark in association with a  $W^\mp$  boson ( $tW$ ) are generated with POWHEG. The latter is simulated within the five-flavor scheme. The value

of the top quark mass used in these simulated samples is 172.5 GeV. The production of W or Z bosons in association with jets is generated using the MG5\_aMC@NLO [13] event generator and the FxFx merging scheme [14]. For all these samples, PYTHIA 8 [15] is used to model the showering process. To validate the data-driven method for estimating the multijet background, QCD events are generated with PYTHIA8. In Table 11, various simulation samples used in this analysis are listed. All generated events undergo a full simulation of the detector response according to an implementation of the CMS detector within GEANT4 [16, 17]. Additional pp interactions (pileups) are included in the simulation with the same frequency of occurrence as observed in data.

Table 2: List of signal and background MC samples.

Process	$\sigma(\times BR)[\text{pb}]$	Dataset name	$N_{\text{events}}$
<i>t</i> -channel, top, inclusive decays	136.02 (NLO) [18]	ST_t-channel_top_4f_inclusiveDecays_13TeV-powhegV2-madspin-pythia8_TuneCUETP8M1	67240808
<i>t</i> -channel, anti-top, inclusive decays	80.95 (NLO) [18]	ST_t-channel_antitop_4f_inclusiveDecays_13TeV-powhegV2-madspin-pythia8_TuneCUETP8M1	38811017
<i>s</i> -channel, top+anti-top, leptonic decays	$10.32(\times 0.324)$ (NNLL) [18]	ST_s-channel_4f_leptonDecays_13TeV-amcatnlo-pythia8_TuneCUETP8M1	1000000
<i>tW</i> -channel, top, inclusive decays	35.6 (NNLL) [18]	ST_tW_top_5f_inclusiveDecays_13TeV-powheg-pythia8_TuneCUETP8M2T4	992024
<i>tW</i> -channel, anti-top, inclusive decays	35.6 (NNLL) [18]	ST_tW_antitop_5f_inclusiveDecays_13TeV-powheg-pythia8_TuneCUETP8M1	998276
$t\bar{t}$ , inclusive decays	831.76 (NNLO+NNLL) [18]	TT_TuneCUETP8M2T4_13TeV-powheg-pythia8	77229341
$W(\rightarrow \ell\nu)+0$ jet	50132 (NNLO)	WToLNu_0J_13TeV-amcatnloFXFX-pythia8	49141548
$W(\rightarrow \ell\nu)+1$ jet	8426 (NNLO)	WToLNu_1J_13TeV-amcatnloFXFX-pythia8	92024405
$W(\rightarrow \ell\nu)+2$ jets	3173 (NNLO)	WToLNu_2J_13TeV-amcatnloFXFX-pythia8	102093848
$Z/\gamma^*(\rightarrow \ell^+\ell^-)+\text{jets}$ ( $M_{\ell\ell} > 50$ GeV)	5765.4 (NNLO)	DYJetsToLL_M-50_TuneCUETP8M1_13TeV-amcatnloFXFX-pythia8	28968252
$WW \rightarrow 1\ell 1\nu 2q$	45.85 (NLO)	WWTo1L1Nu2Q_13TeV-amcatnloFXFX_madspin-pythia8	5176114
$WW \rightarrow 2\ell 2\nu$	12.178 (NLO)	WWTo2L2Nu_13TeV-powheg	1999000
$WZ \rightarrow 1\ell 1\nu 2q$	10.71 (NLO)	WZTo1L1Nu2Q_13TeV-amcatnloFXFX_madspin-pythia8	24221923
$WZ \rightarrow 2\ell 2q$	5.595 (NLO)	WZTo2L2Q_13TeV-amcatnloFXFX_madspin-pythia8	26517272
$ZZ \rightarrow 2\ell 2q$	3.22 (NLO)	ZZTo2L2Q_13TeV-amcatnloFXFX_madspin-pythia8	15345572
$\mu$ -enriched QCD	302672.16 (LO)	QCD_Pt-20toInf_MuEnriched_Pt15_TuneCUETP8M1_13TeV_pythia8	22094081
EM-enriched QCD	5352960 (LO)	QCD_Pt-20to30_EMEnriched_TuneCUETP8M1_13TeV_pythia8	9218954
	9928000 (LO)	QCD_Pt-30to50_EMEnriched_TuneCUETP8M1_13TeV_pythia8	6768384
	2890800 (LO)	QCD_Pt-50to80_EMEnriched_TuneCUETP8M1_13TeV_pythia8	23474171
	350000 (LO)	QCD_Pt-80to120_EMEnriched_TuneCUETP8M1_13TeV_pythia8	41853504
	62964 (LO)	QCD_Pt-120to170_EMEnriched_TuneCUETP8M1_13TeV_pythia8	41954035
	18810 (LO)	QCD_Pt-170to300_EMEnriched_TuneCUETP8M1_13TeV_pythia8	11540163
	1350 (LO)	QCD_Pt-300toInf_EMEnriched_TuneCUETP8M1_13TeV_pythia8	7373633

### 3 Object Selection

Various objects used in the analysis are reconstructed with information from all CMS subdetectors based on the particle-flow (PF) algorithm [19].

#### 3.1 Trigger

Events are required to pass the high-level trigger (HLT) criteria for each of the leptonic final states.

- For events containing a muon in the final state, a logical OR of the trigger decisions `HLT_IsoMu24` and `HLT_IsoTkMu24` needs to be satisfied, which demands the presence of at least one isolated "global muon" (reconstructed with information from the inner tracker as well as the muon chambers) OR "tracker muon" (reconstructed with information from the inner tracker and minimal information from the muon chambers) candidate with transverse momentum,  $p_T > 24$  GeV.
- For events with an electron in the final state, `HLT_Ele32_eta2p1_WPTight_Gsf` needs to be satisfied, which demands the presence of at least one electron with  $p_T > 32$  GeV and  $|\eta| < 2.1$  passing the tight identification criteria.

#### 3.2 Primary Vertex

Primary vertices are reconstructed by means of the standard deterministic-annealing clustering algorithm [20]. The first vertex in the collection (the one with largest sum of  $p_T^2$  for the associ-

ated clustered objects [21]) is required to be within a cylinder of radius 2 cm around the beam axis and its z-coordinate must satisfy  $|z| < 24$  cm. In addition, the reconstruction algorithm must not mark the vertex as *fake* and must assign it at least four degrees of freedom, which roughly corresponds to the requirement of at least four tracks being associated with the vertex. The vertices that satisfy the above requirements are exploited to mitigate the deleterious effects of pileup based on the charged-hadron subtraction scheme [22]. In this scheme, if a PF candidate is identified as a charged hadron and is associated to any but the first of these vertices, the candidate is removed from the event.

### 3.3 Tight Muons

Muons are reconstructed as `global muons`. Events with exactly one muon with  $p_T > 26$  GeV and within  $|\eta| < 2.4$  are selected. These selected high- $p_T$  muon objects are required to pass additional quality requirements to be identified as tight muons" [23]. Further, the muon must be well isolated in terms of the PF-based " $\Delta\beta$ "-corrected relative isolation:

$$I_{\text{rel}} = \frac{I^{\text{ch}} + \max.[(I^\gamma + I^{\text{nh}} - 0.5 \times I^{\text{PU}}), 0]}{p_T^\mu} \quad (4)$$

where  $I^{\text{ch}}$ ,  $I^\gamma$  and  $I^{\text{nh}}$  are the sum of the transverse energies of charged hadrons, photons and neutral hadrons, respectively, in a cone size of  $\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} = 0.4$  around the muon direction.  $I^{\text{PU}}$  is the  $\sum p_T^{\text{PU}}$  of charged hadrons associated to the vertices other than the primary vertex. It is used to estimate the contribution of neutral particles from pileup vertices, where the factor 0.5 takes into account the neutral-to-charged particle ratio. For the tight muon, our selection requires  $I_{\text{rel}} < 0.06$ .

### 3.4 Tight Electrons

Similar to the case of muons, "tight" electrons are required for the events with electron final state. Such an electron must pass the tight working point of the cut-based identification criteria [24] and must not be identified as originating from a photon conversion. The "tight" electron must have  $p_T > 35$  GeV and  $|\eta| < 2.1$ , excluding the transition region between the barrel and endcap of the electromagnetic calorimeter, given by  $1.4442 < |\eta_{\text{sc}}| < 1.5660$ , where  $\eta_{\text{sc}}$  is the pseudorapidity of the supercluster associated to the electron track. Additional requirements on the transverse and longitudinal impact parameters ( $d_{xy}$  and  $d_z$ ) are applied separately for the barrel and endcap regions. In the barrel region ( $|\eta| \leq 1.479$ ), electrons are required to pass  $d_{xy} < 0.05$  cm and  $d_z < 0.1$  cm criteria, whereas in the endcap region ( $|\eta| > 1.479$ ), they need to satisfy  $d_{xy} < 0.1$  cm and  $d_z < 0.2$  cm.

### 3.5 Loose Muons

Events with additional muons are vetoed. The requirements for having one or more additional muon in the event are loosened. Events having another muon with  $p_T > 10$  GeV within  $|\eta| < 2.4$  that satisfies the "global muon" OR "tracker muon" criteria (muons reconstructed in the inner tracker having at least one segment in the muon chambers) and  $I_{\text{rel}} < 0.2$ , are rejected.

### 3.6 Veto Electrons

Events with one or more electrons along with the tight lepton, described in Sections 3.3 and 3.4, are vetoed. Any event which contains additional electron(s) with  $E_T > 15$  GeV within  $|\eta| < 2.5$  passing the cut-based "veto" identification criteria is rejected.

### 3.7 Jets

Jets are reconstructed using the anti- $k_T$  algorithm [25] with a cone size of 0.4, taking PF candidates as inputs after rejecting charged hadrons associated to pileup vertices (slimmedJets). We require at least two jets having  $p_T > 40$  GeV and  $|\eta| < 4.7$ . To reduce the contamination of fake jets from pileup vertices or detector noise, a set of  $|\eta|$ -dependent “loose” identification criteria [26] are applied. Jets are also required to have  $\Delta R > 0.4$  relative to the selected tight lepton described earlier.

Once the jets are reconstructed, a number of corrections [27] are applied to their measured energy. Sequentially, we apply `L1FastJet`, `L2Relative` and `L3Absolute` corrections from payload `Summer16_23Sep2016V4` to both data and simulation, in order to reduce contribution from pileup as well as to account for the nonlinear calorimetric response and detector mismodeling depending on  $p_T$  and  $|\eta|$  of the jet. The `L2L3Residual` corrections are applied to data only, while the jet energy in simulated samples is smeared to account for the  $p_T$  difference observed between the reconstructed and associated generated jet in data to those in the simulations [28] corresponding to the tag `Summer16_25ns_v1`.

### 3.8 B-tagging

As the lifetime of a b-flavored hadron is large, it travels certain distance before decaying. Within CMS various techniques have been explored to identify jets that originate from bottom quarks or antiquarks using the secondary vertex and lifetime information. For this study, a combined MVA algorithm (“cMVA<sub>v2</sub>”) [29] has been used which collects track-based lifetime information together with secondary vertices inside the jet to provide an optimal MVA discriminator for b-jet identification. We apply a “tight” threshold on the discriminator value ( $> 0.9432$ ) that corresponds to an average b-tagging efficiency of  $\approx 55\%$  with a light-flavor misidentification probability of 0.1%.

### 3.9 Missing Transverse Momentum

The missing transverse momentum vector  $\vec{p}_T^{\text{miss}}$  is defined as the projection of the negative vector sum of the momenta of all reconstructed PF objects in an event onto the plane perpendicular to the beam axis:

$$\vec{p}_T^{\text{miss}} = - \sum_i \vec{p}_{T,i} \quad (5)$$

where  $i$  refers to the  $i$ -th PF candidate. Its magnitude is referred to as  $p_T^{\text{miss}}$ . To account for possible misreconstructed high- $p_T$  muons in the 2016 data, the `slimmedMETsMuEGClean` collection instead of the default `slimmedMETs` is used for the missing transverse momentum calculation [30].

### 3.10 Transverse W-boson Mass

The transverse W-boson mass is defined as:

$$m_T^W = \sqrt{(p_{T,\ell} + p_T^{\text{miss}})^2 - (p_{x,\ell} + p_x^{\text{miss}})^2 - (p_{y,\ell} + p_y^{\text{miss}})^2} \quad (6)$$

158 where,  $p_{x,\ell}$  and  $p_{y,\ell}$  are the x and y-component of the tight lepton momentum and  $\cancel{p}'_x$  and  $\cancel{p}'_y$  are  
 159 the same components of  $\vec{p}'_T$ . As  $m_T^W$  is very sensitive to the processes with prompt leptons from  
 160 the leptonically decaying W boson, a cut of  $m_T^W > 50$  GeV is applied to suppress contributions  
 161 from processes with nonprompt muons in the case of  $\mu$ +jets events.

### 162 3.11 MC Correction Factors

163 A number of correction factors are applied to MC simulation to match with data. They are  
 164 described below.

- 165 • **Pileup Reweighting:** The pileup profile used in the MC simulation does not agree  
 166 exactly with that in data where the latter is derived from the (effective) total cross  
 167 section of inelastic pp scattering and the measured instantaneous luminosity. To cor-  
 168 rect for this difference, MC events are reweighted based on the *true* number of pileup  
 169 interactions, as suggested by the standard prescription [31], assuming a minimum-  
 170 bias cross section of 69.2 mb for the pileup reweighting [32]. An additional system-  
 171 atic uncertainty is introduced by varying this cross section by  $\pm 4.6\%$ .
- 172 • **Lepton Efficiencies:** The correction of the muon efficiencies encompasses separate  
 173 scale factors for the muon identification and tracker efficiencies. The correction fac-  
 174 tors are provided by the Muon POG [33], which are derived with tag-and-probe  
 175 methods [34] at the  $J/\psi$  and Z boson resonances. As the official muon isolation and  
 176 trigger scale factors are not suitable for this analysis owing to the tight isolation cri-  
 177 terion on  $I_{\text{rel}} < 0.06$ , privately produced correction factors [35] are applied instead.  
 178 Simulated electron efficiencies for the reconstruction as well as cut-based identifi-  
 179 cation are also corrected [36]. The correction factors are provided by the EGamma  
 180 POG that have been determined on large  $Z \rightarrow e^+e^-$  samples with the tag-and-probe  
 181 procedure [37]. The correction of the electron trigger efficiency is applied too; since  
 182 the EGamma POG does not provide this efficiency, the privately produced correc-  
 183 tion scale factors [35] are used.  
 184 The determination of these lepton scale factors depends on the available amount of  
 185 data and simulated events. Hence, the statistical uncertainty of each scale factor is  
 186 used as an additional source of systematic uncertainty.
- 187 • **B-tagging Efficiency:** In order to account for differences in b-tagging efficiency of  
 188 the cMVA<sub>v2</sub> algorithm between data and simulations, MC simulated events are  
 189 reweighted following the method described in Ref. [38]. The probability of having  
 190  $n$  b-tagged jets and  $m$  not-b-tagged (untagged) jets in simulation and data are given  
 191 by:

$$P(\text{MC}) = \prod_{i=\text{tagged}}^n \epsilon_i \prod_{j=\text{untagged}}^m (1 - \epsilon_j), \quad (7)$$

$$P(\text{Data}) = \prod_{i=\text{tagged}}^n \text{SF}_i \epsilon_i \prod_{j=\text{untagged}}^m (1 - \text{SF}_j \epsilon_j), \quad (8)$$

where  $\epsilon_i$  is the b-tagging efficiency in simulation and  $\text{SF}_i$  are the scale factors for the cMVA<sub>v2</sub> algorithm that are provided by the BTV POG [39]. Both the scale factors and b-tagging efficiencies depend on the jet flavor,  $p_T$  and  $\eta$ . The event weight is then given by

$$w = \frac{P(\text{Data})}{P(\text{MC})} \quad (9)$$



## 4 Event Categorization: Signal and Control Regions

The  $t$ -channel single top production mode has one light quark recoiling against the virtual  $W$  boson and one  $b$ -quark arising from the top quark decay. There is a second  $b$ -quark in the final state due to the initial gluon splitting at NLO. The  $p_T$ -spectrum of the latter  $b$ -quark is softer compared to the one coming from the top quark. It also has large  $|\eta|$  as opposed to the  $b$ -quark originating from top that goes more centrally within the detector. As a result, the jet due to the second  $b$ -quark in the final state is often either rejected by the jet  $p_T$ -threshold ( $> 40$  GeV) applied during selection or not identified as a  $b$ -tagged jet due to limited tracker acceptance ( $|\eta| < 2.4$ ). Hence, the region with two jets, with one of them being  $b$ -tagged, has the largest fraction of signal events.

Depending on the number of jets and the number of  $b$ -tagged jets, we define several event categories in addition to the signal-enriched region. These are used to validate the normalization and modeling of dominant background processes. A generic nomenclature “ $nJmT$ ” is attributed to the events having “ $n$ ” jets and “ $m$ ”  $b$ -tagged jets. In addition to the signal-enriched 2J1T region; 2J0T, 3J1T and 3J2T regions have been extensively studied as various control regions.

### 4.1 2J1T Region

This is the region with highest signal fraction. The  $b$ -tagged jet is identified to originate from the  $b$ -quark due to the top decay, while the untagged jet is identified to recoil against the top quark. The sideband defined by  $I_{\text{rel}} > 0.2$  is used to estimate the QCD contribution in 2J1T as explained in Section 7.2. An MVA technique is used in this region to reduce the electroweak and top backgrounds as described in Section 8. Kinematic plots of the final state objects in the 2J1T region before applying  $m_T^W$  cut are shown in Figures 2 to 5.

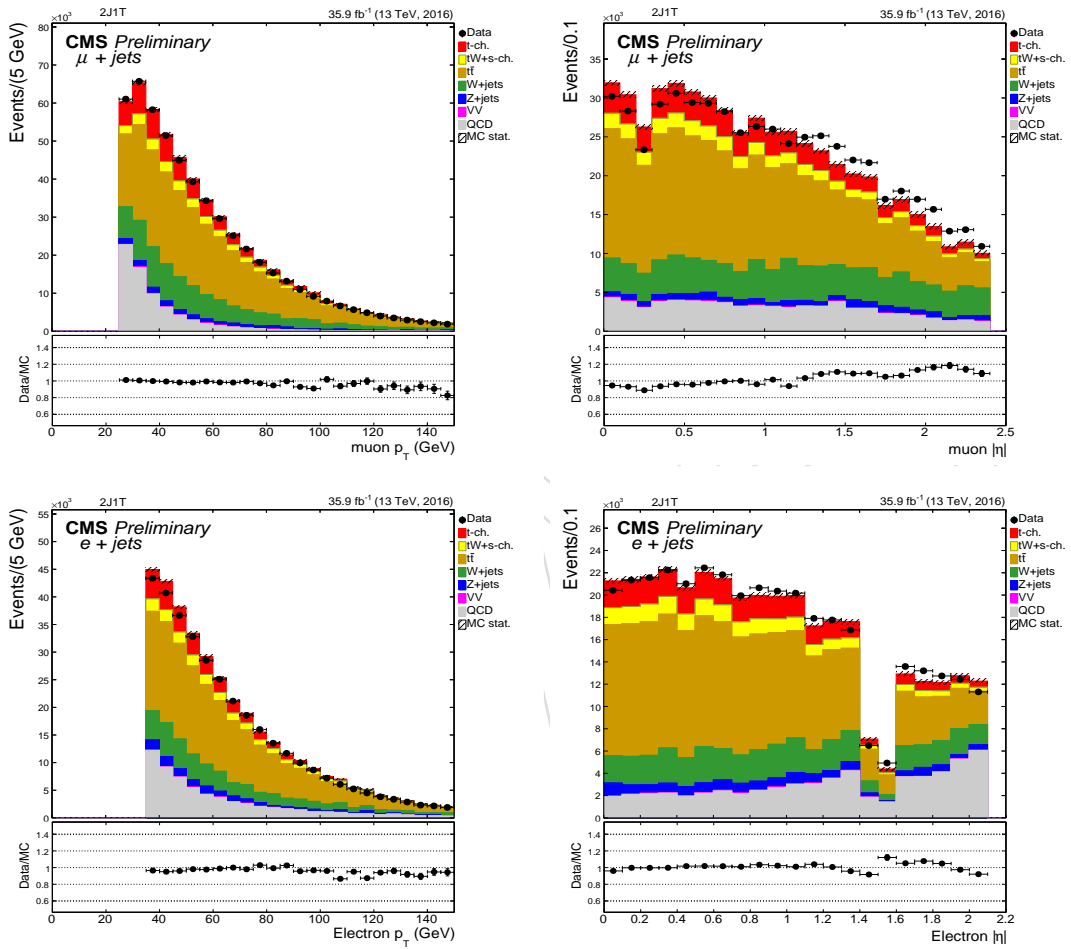


Figure 2: Data-MC comparison of  $p_T$  (left) and  $|\eta|$  (right) corresponding to muon (top) and electron (bottom) final states in 2J1T.

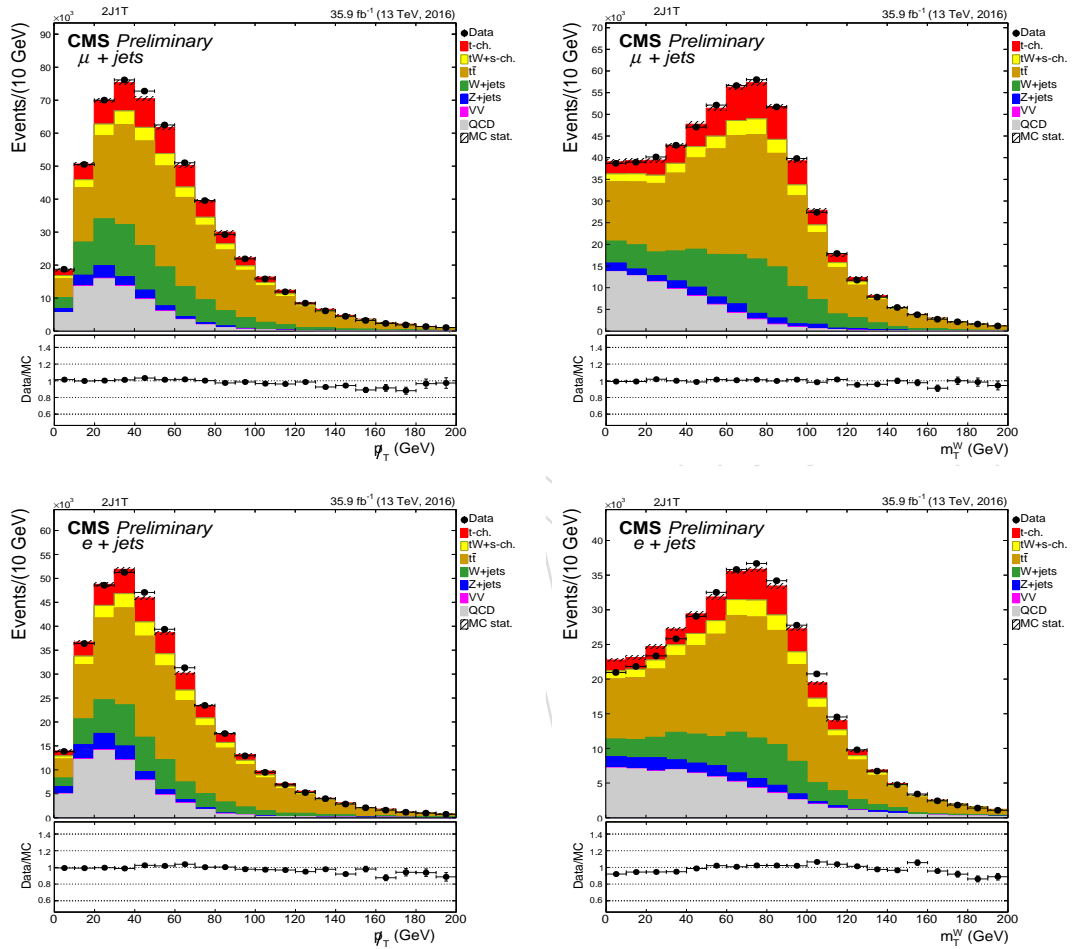


Figure 3: Data-MC comparison of  $p_T$  (left) and  $m_T^W$  (right) corresponding to muon (top) and electron (bottom) final states in 2J1T.

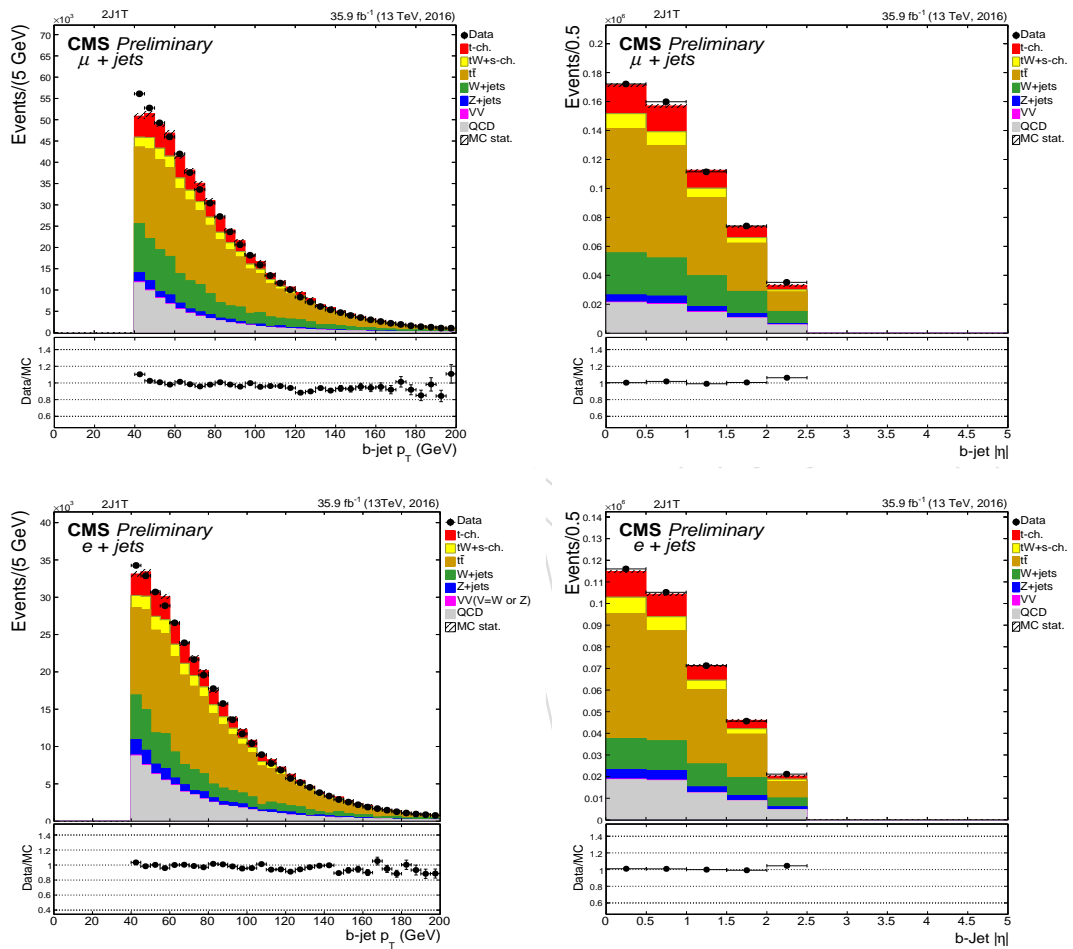


Figure 4: Data-MC comparison of b-jet  $p_T$  (left) and  $|\eta|$  (right) corresponding to muon (top) and electron (bottom) final states in 2J1T.

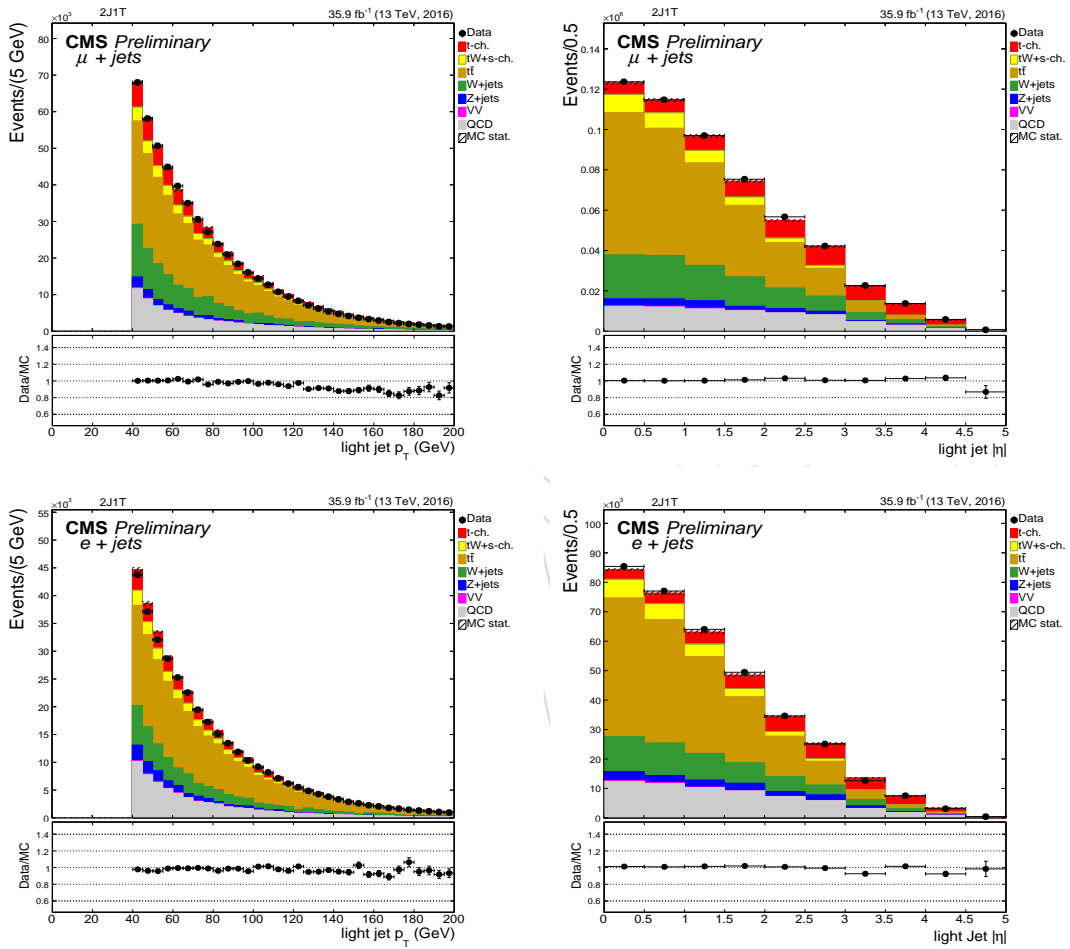


Figure 5: Data-MC comparison of light-flavor jet  $p_T$  (left) and  $|\eta|$  (right) corresponding to muon (top) and electron (bottom) final states in 2J1T.

## 215 4.2 2J0T Region

216 This region is selected by requiring none of the two jets pass the tight b-tagging criteria. How-  
 217 ever, one of the jets is designated as the b-jet from top quark decay using the definitions in  
 218 Section 6. The 2J0T region is dominated by W+light-flavor jets and QCD background. High  
 219 QCD statistics in this region, which is adjacent but orthogonal to the signal region, serves well  
 220 to validate the technique of QCD estimation to be applied to the signal region. The basic kine-  
 matic plots in the 2J0T region before applying cut to  $m_T^W$  is shown in Figures 6 to 9.

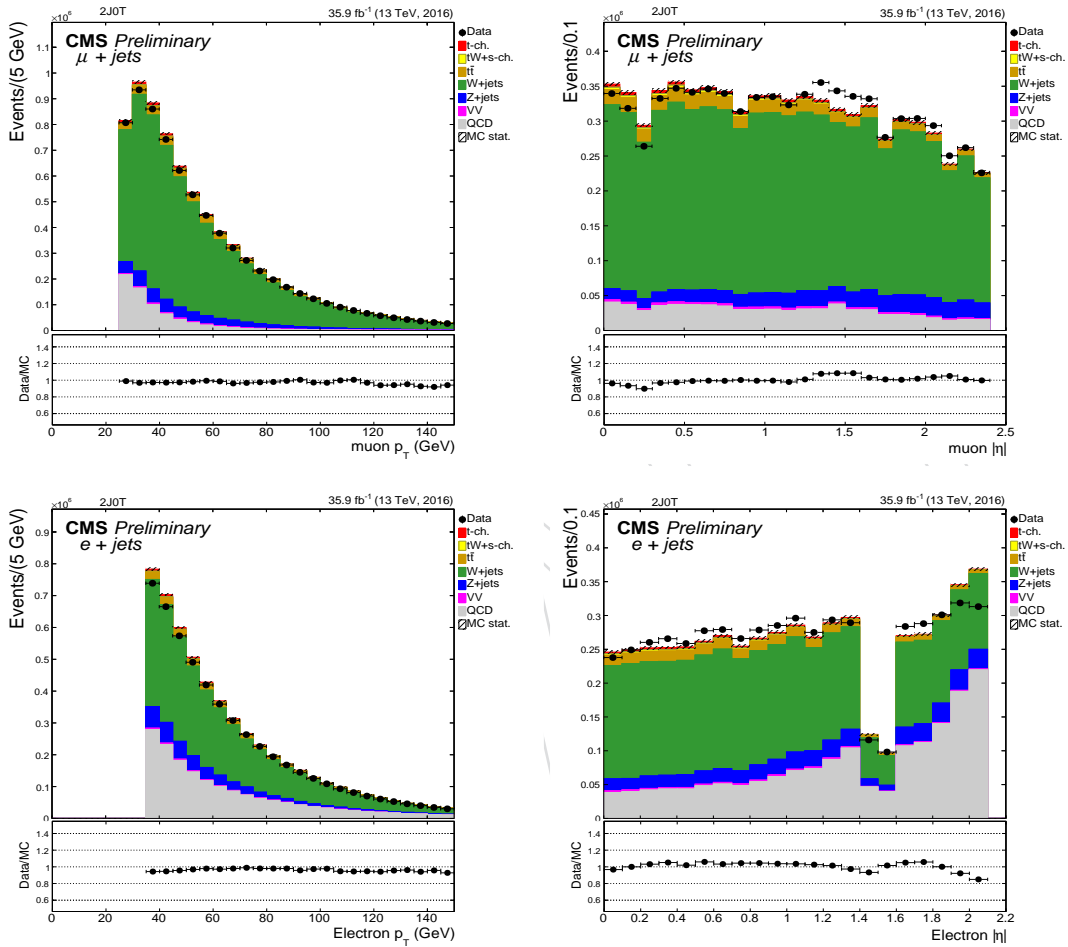


Figure 6: Data-MC comparison of lepton  $p_T$  (left) and  $|\eta|$  (right) corresponding to muon (top) and electron (bottom) final states in 2J0T.

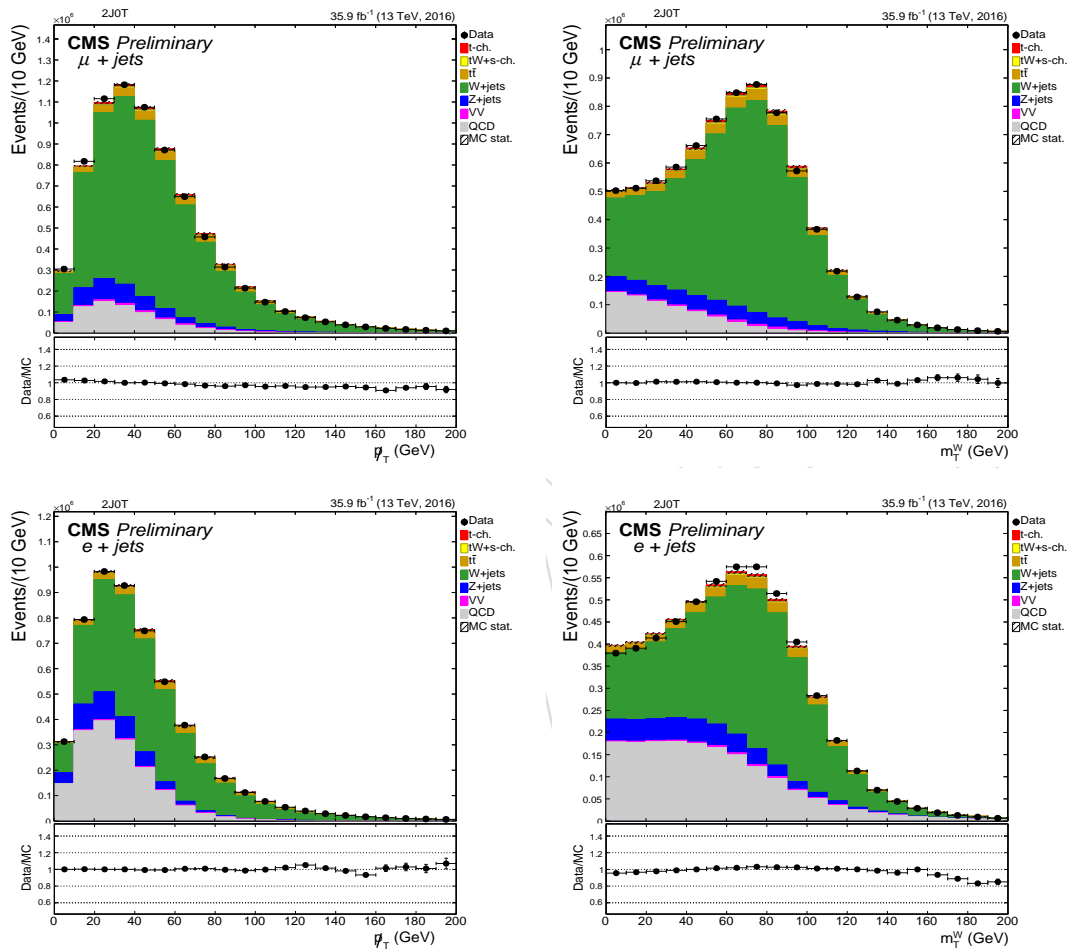


Figure 7: Data-MC comparison of  $p_T$  (left) and  $m_T^W$  (right) corresponding to muon (top) and electron (bottom) final states in 2J0T.

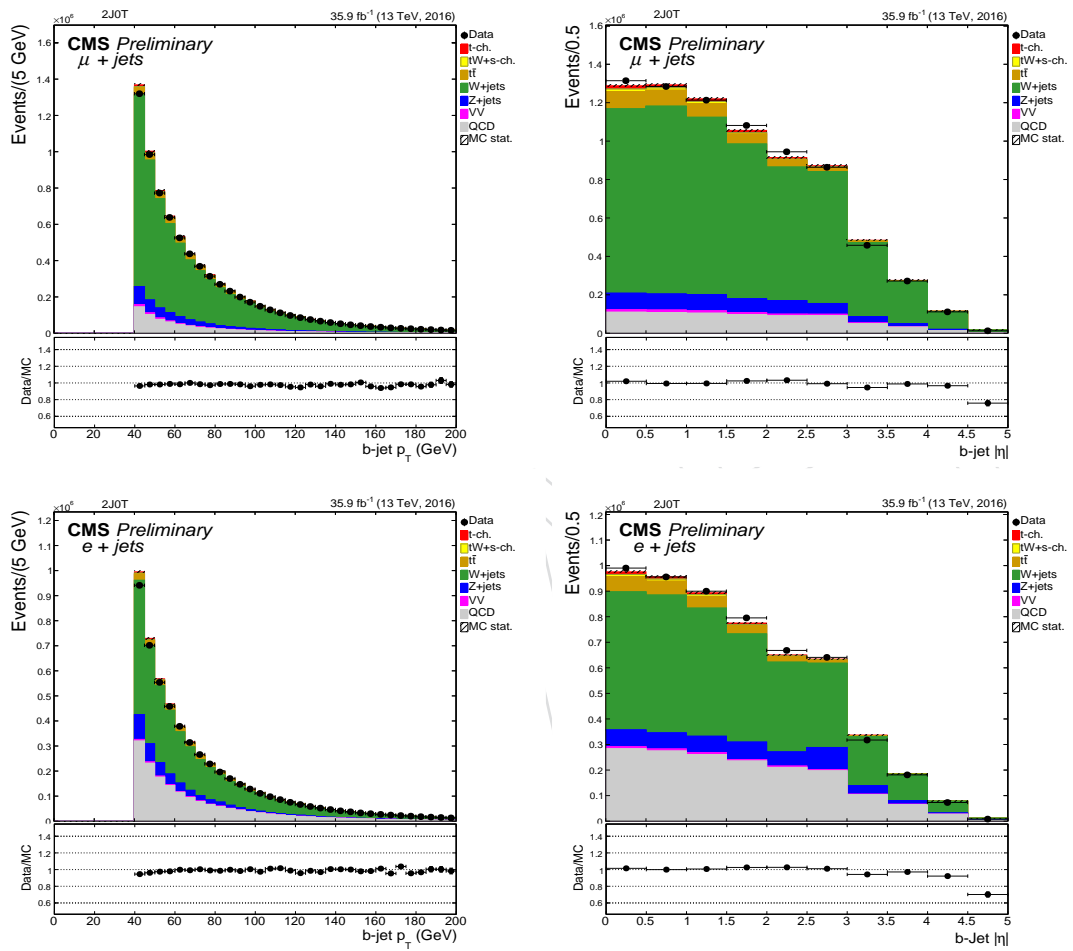


Figure 8: Data-MC comparison of b-jet  $p_T$  (left) and  $|\eta|$  (right) corresponding to muon (top) and electron (bottom) final states in 2J0T.



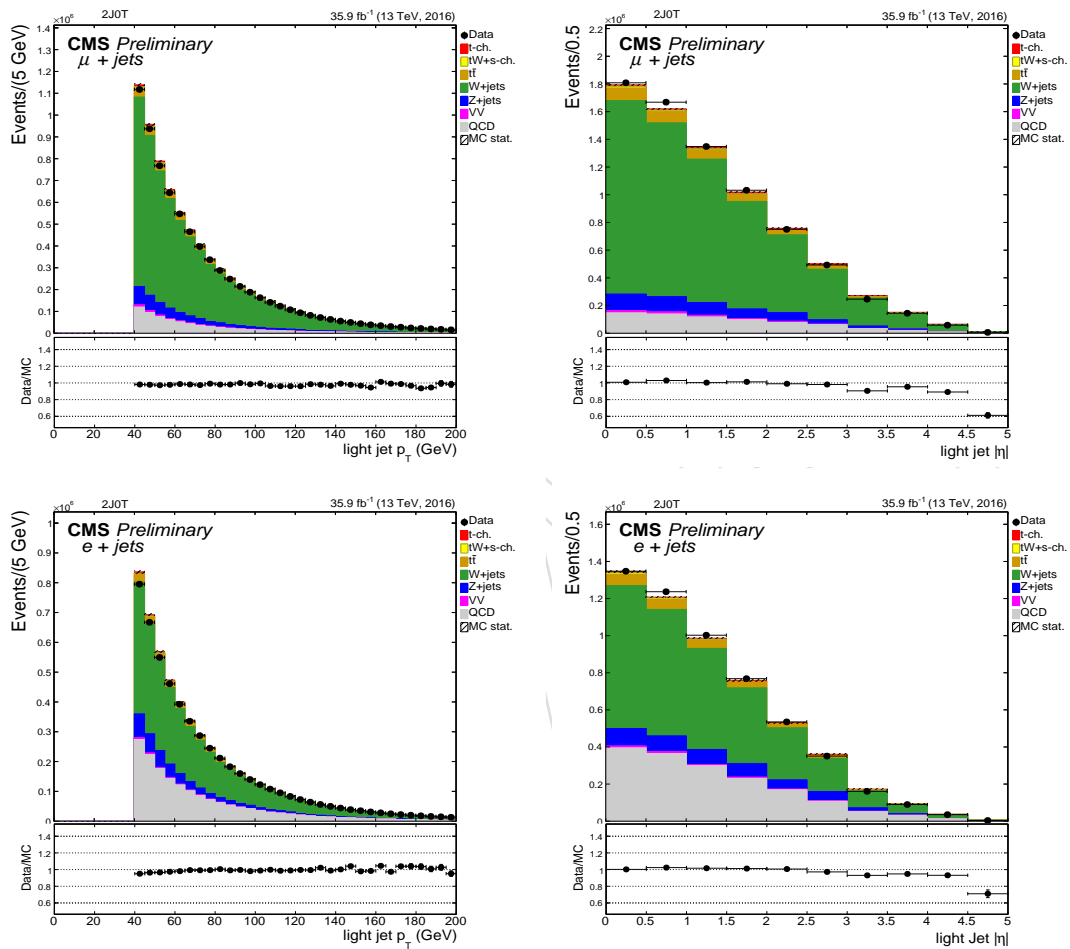


Figure 9: Data-MC comparison of light-flavor jet  $p_T$  (left) and  $|\eta|$  (right) corresponding to muon (top) and electron (bottom) final states in 2J0T.

### 222 4.3 3J1T Region

223 This region is selected by requiring three jets passing the jet selection criteria, one of them being  
 224 b-tagged. The 3J1T region is mostly dominated by  $t\bar{t}$  background and has similar heavy flavor  
 225 content as the signal region (2J1T). Therefore, this region is used to validate the modeling and  
 226 normalization of events having a W boson produced in association with heavy flavor quarks.  
 The basic kinematic plots before applying the  $m_T^W$  cut are shown in Figures 11 to 13.

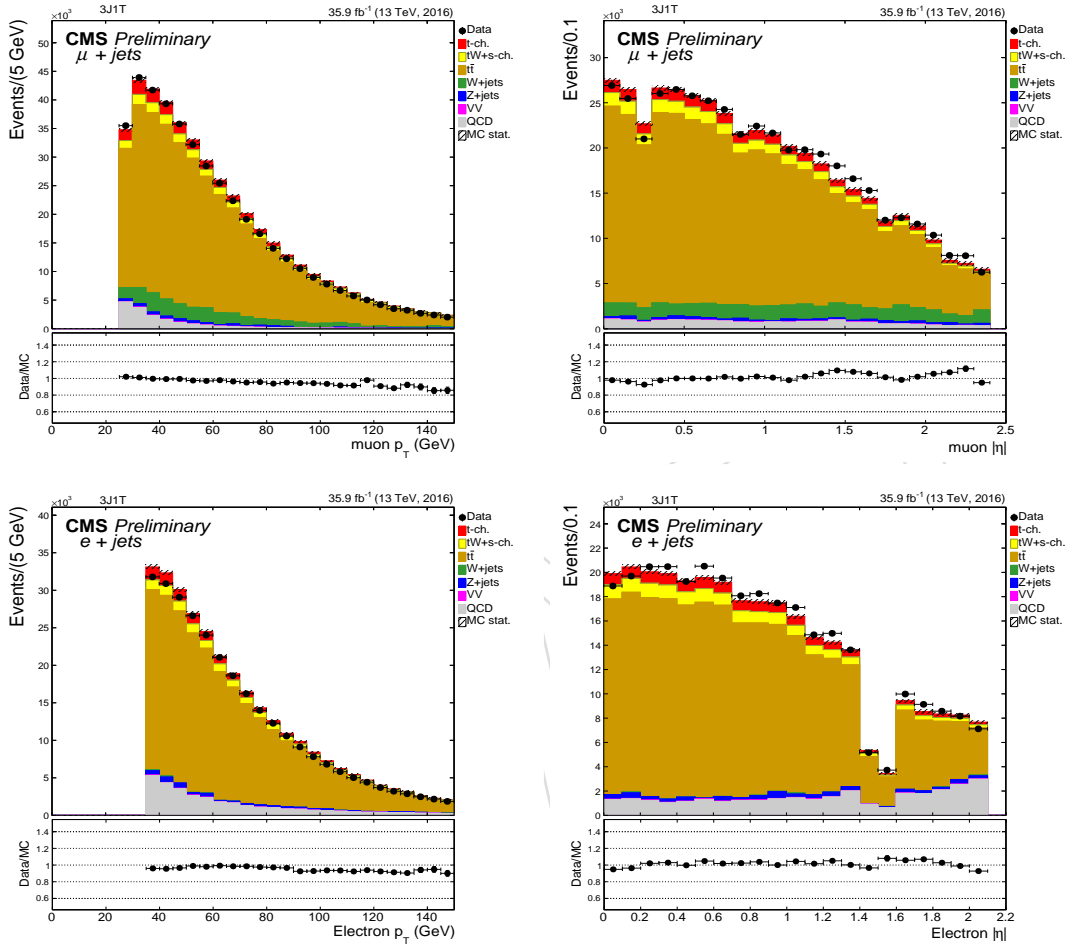


Figure 10: Data-MC comparison of lepton  $p_T$  (left) and  $|\eta|$  (right) corresponding to muon (top) and electron (bottom) final states in 3J1T.

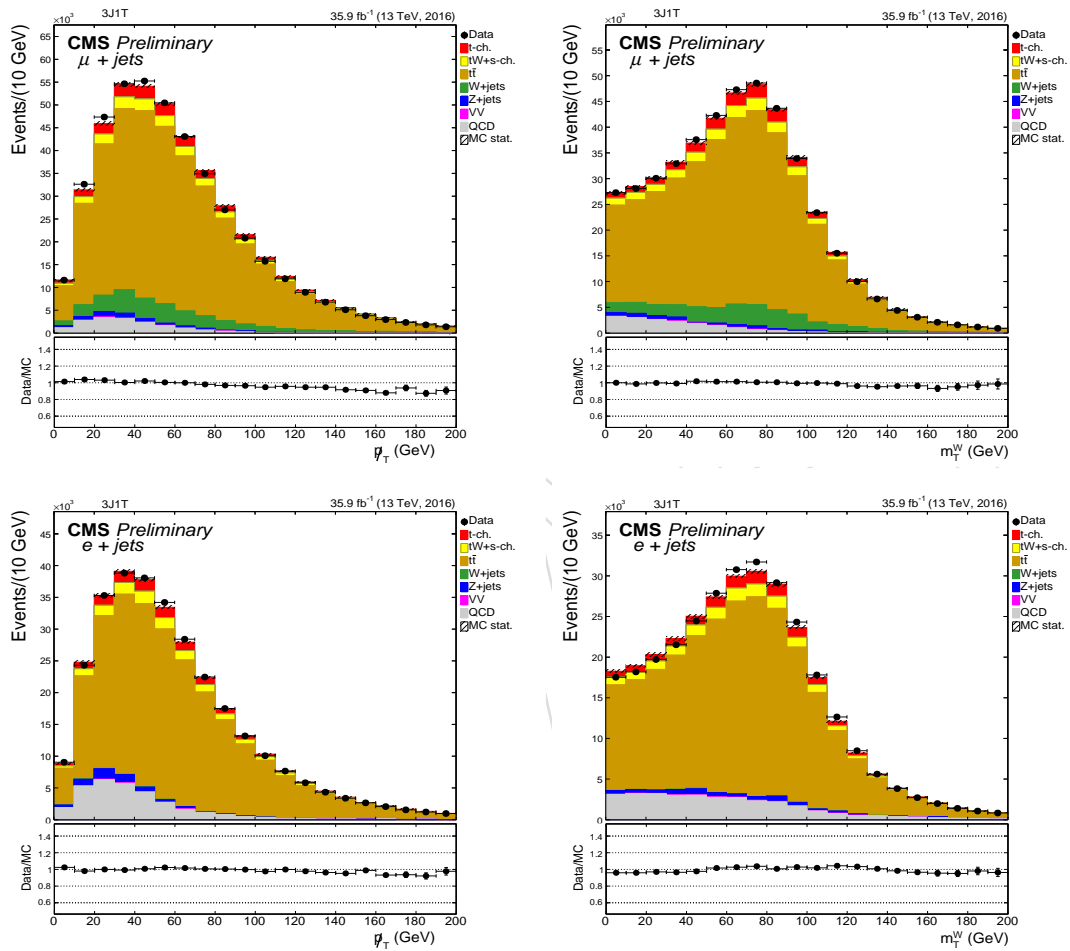


Figure 11: Data-MC comparison of  $p_T$  (left) and  $m_T^W$  (right) corresponding to muon (top) and electron (bottom) final states in 3J1T.

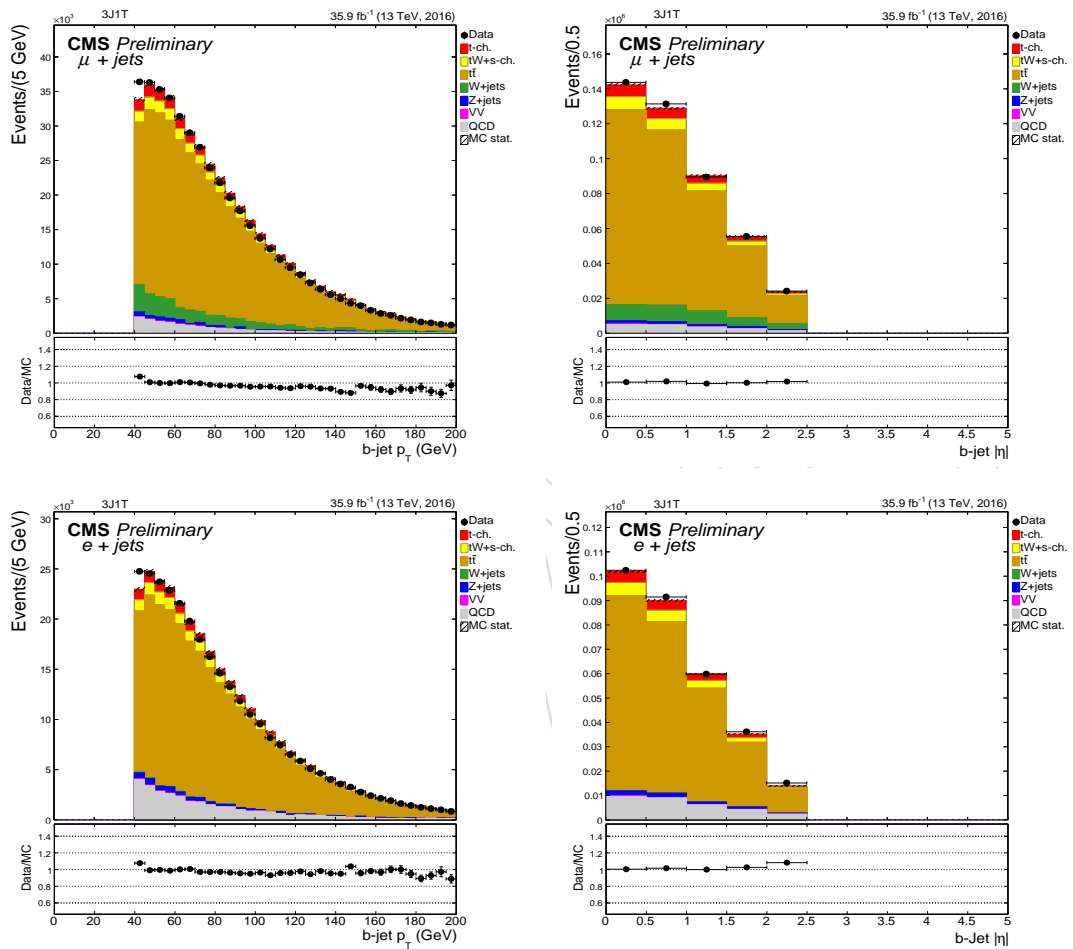


Figure 12: Data-MC comparison of b-jet  $p_T$  (left) and  $|\eta|$  (right) corresponding to muon (top) and electron (bottom) final states in 3J1T.

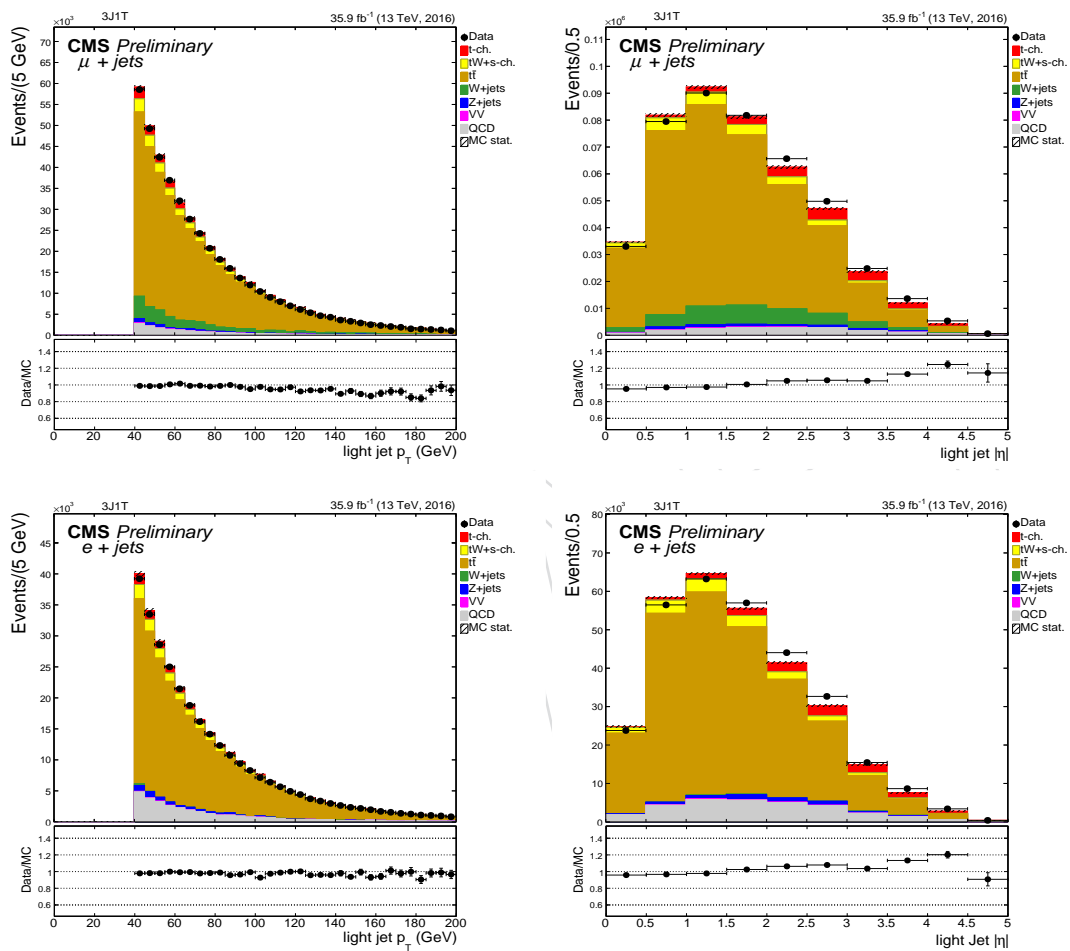


Figure 13: Data-MC comparison of light-flavor jet  $p_T$  (left) and  $|\eta|$  (right) corresponding to muon (top) and electron (bottom) final states in 3J1T.

#### 228 4.4 3J2T region

229 This region is selected by requiring three jets passing the jet selection criteria, two of them being  
 230 b-tagged. The untagged jet is considered as the light-flavor jet. The jet due to the b-quark from  
 231 top quark decay is identified as described in Section 6. This region is completely dominated  
 232 by  $t\bar{t}$  background. Therefore, 3J2T is used to validate the modeling and normalization of  $t\bar{t}$   
 233 background. The basic kinematic plots in the 3J2T region before applying the  $m_T^W$  cut are shown  
 in Figures 14 to 17.

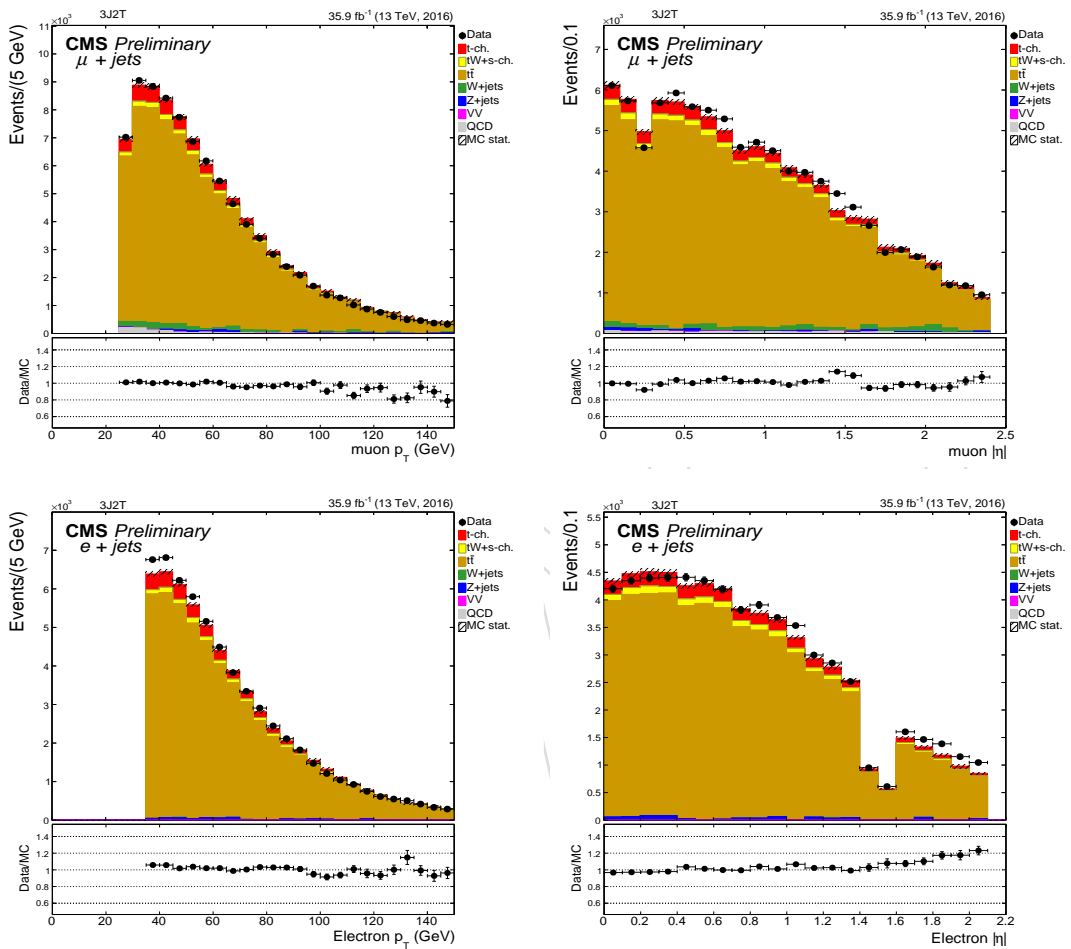


Figure 14: Data-MC comparison of lepton  $p_T$  (left) and  $|\eta|$  (right) corresponding to muon (top) and electron (bottom) final states in 3J2T.

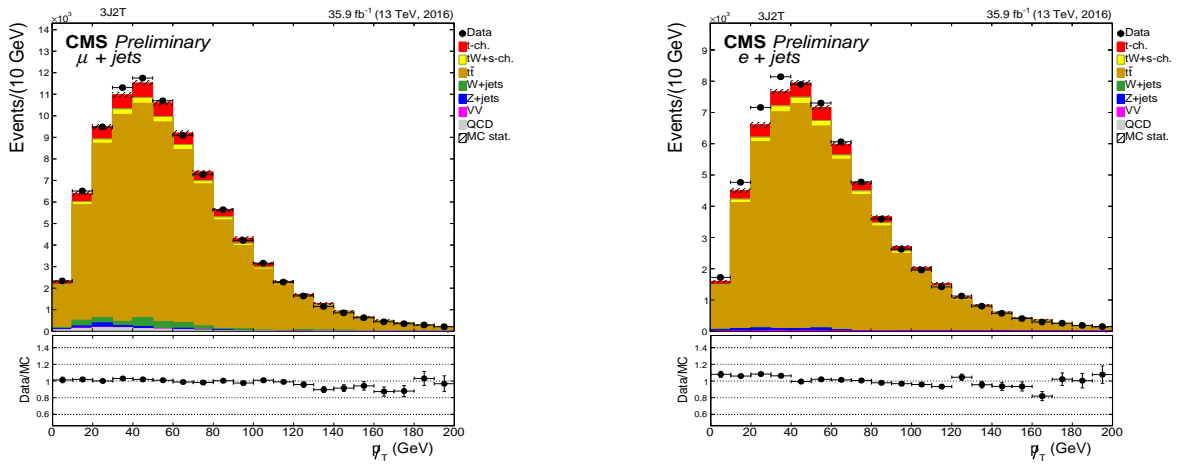


Figure 15: Data-MC comparison of  $p_T$  corresponding to muon (top) and electron (bottom) final states in 3J2T.

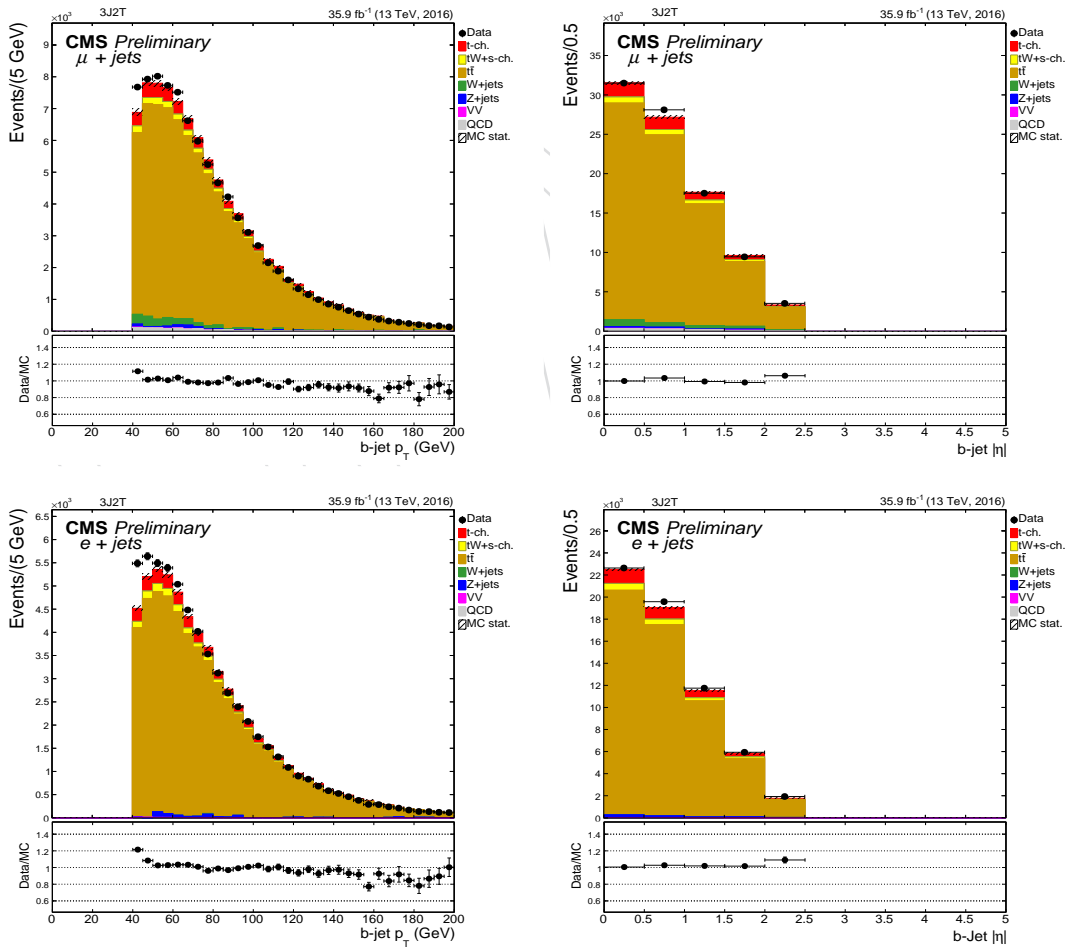


Figure 16: Data-MC comparison of b-jet  $p_T$  (left) and  $|\eta|$  (right) in corresponding to muon (top) and electron (bottom) final states 3J2T.

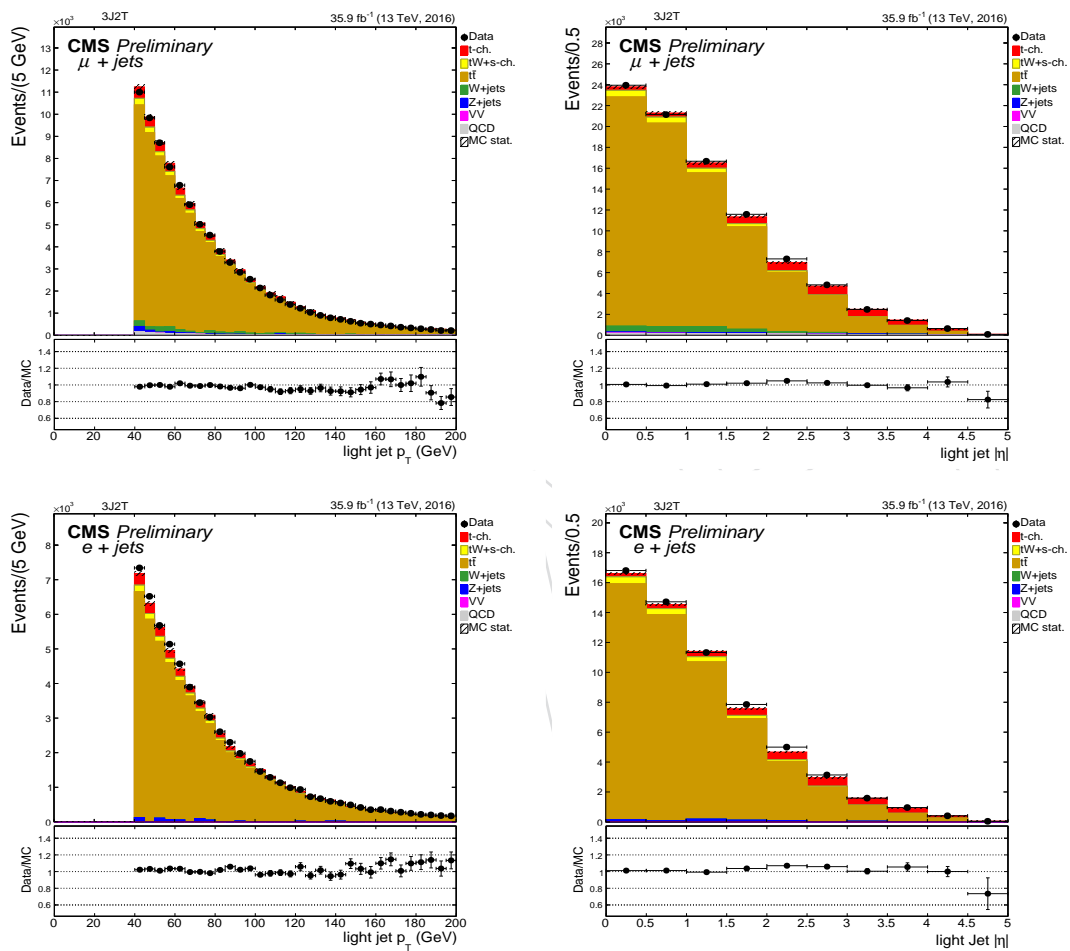


Figure 17: Data-MC comparison of light-flavor jet  $p_T$  (left) and  $|\eta|$  (right) corresponding to muon (top) and electron (bottom) final states in 3J2T.



## 5 Cut Flow

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236 Tables 3 and 4 summarizes the step-by-step event yields for simulated signal and background  
 237 events as well as in data in the signal-enriched 2J1T region, when the selection criteria are  
 238 applied sequentially.

Table 3: Cut flow for events with the muon final state.

Cut	t-ch.	tW + s-ch.	t $\bar{t}$	W+jets	Z+jets	di-boson	QCD	Total MC	Data	Data/MC(%)
No cut	7778510	2922066	2.98178e+07	2.20583e+09	2.06715e+08	2780995	1.08515e+010	13307344371	786809782	5.91
Trigger	522403	431879.5	4.03312e+06	3.09301e+08	4.46127e+07	576838.2	1.56223e+08	515700940.7	469761390	91.09
1 tight isolated $\mu$	406617	331738	2.97164e+06	2.33916e+08	2.28107e+07	434859.5	2.47365e+07	285608054.5	258382120	90.47
Loose $\mu$ veto	404505	319712.8	2.84126e+06	2.33563e+08	1.29449e+07	406448.96	2.38424e+07	274322226.76	245109050	89.35
e veto	402917	292559.1	2.56513e+06	2.33386e+08	1.28375e+07	375387.93	2.38121e+07	273671594.03	244545880	89.36
2 jets	151988.9	105039.5	695845	6.60088e+06	590102	81312.9	1.46003e+06	9685198.3	8000147	82.60
1 b-tag	64472.5	39140.78	278100	103099	18926.7	2160.19	150628	656527.18	544798	82.98
$m_{\ell\ell}^W > 50$ GeV	44946.6	26523.49	191354	74884.2	9781.65	1407.99	36526.1	385424.04	340453	88.33

239

Table 4: Cut flow for events with the electron final state.

Cut	t-ch.	tW + s-ch.	t $\bar{t}$	W+jets	Z+jets	di-boson	QCD	Total MC	Data	Data/MC(%)
No cut	7717690	2924052	30895200	2.17e+09	2.08e+08	2783180	6.41e+11	6.44e+11	843398435	0.1
Trigger	309594	288290.9	2660710	1.42e+08	2.72e+07	353090.5	9.71e+07	2.70e+08	292170629	108.2
1 Tight isolated e	229830.3	220699.3	2019920	8.60e+07	1.42e+07	251417.7	1.21e+07	1.15e+08	117287424	102.0
Loose e veto	229067.5	211554.3	1920620	8.60e+07	5752430	228387.7	1.21e+07	1.06e+08	108316594	101.8
$\mu$ veto	227904.9	190603.3	1711180	8.58e+07	5709520	208425.8	1.21e+07	1.06e+08	107856987	101.8
2 jets	86035.3	68740.7	456275	2929229	529504	48973.8	1356662.3	5475420.1	5918361	108.1
1 b-tag	36664.9	25065.9	182395	49618.5	16016.1	1331.1	28739.4	339830.9	359251	105.7
$p_{\ell\ell}^W > 30$ GeV	27782.1	19327.2	148045	35952.9	7676.3	966.4	16778.2	256528	260515	101.6

## 6 Top Quark Reconstruction

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241 The four-momentum of the top quark is calculated from the available kinematic information  
 242 in an event. The top quark decays to a b-tagged jet, a charged lepton and a neutrino, whose  
 243 transverse momentum can be inferred from  $\vec{p}_{\ell\ell}^T$ . The longitudinal momentum of the neutrino,  
 244  $p_{z,\nu}$  is determined from the kinematic constraint, namely the W boson mass,  $m_W = 80.4$  GeV  
 245 [40]. Assuming energy-momentum conservation at the  $W \rightarrow \mu\nu$  vertex, one can obtain the  
 246 expression for  $p_{z,\nu}$  as:

$$p_{z,\nu} = \frac{\Lambda p_{z,\ell}}{p_{T,\ell}^2} \pm \frac{1}{p_{T,\ell}^2} \sqrt{\Lambda^2 p_{z,\ell}^2 - p_{T,\ell}^2 (E_{\ell}^2 p_{\ell}^2 - \Lambda^2)}, \text{ where } \Lambda = \frac{m_W^2}{2} + \vec{p}_{T,\ell} \cdot \vec{p}_T^{\prime} \quad (10)$$

247 Two cases can arise for the solution, as following.

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- If the discriminant, i.e., the square root term in Eq.(10), is negative, it leads to complex solutions for  $p_{z,\nu}$ . In this case, the imaginary part is eliminated by setting  $m_W^T = m_W$ , while still respecting the  $m_W$  constraint. This sets the discriminant to 0. This condition gives a quadratic relation between  $p_{x,\nu}$  and  $p_{y,\nu}$  with two possible solutions, and one remaining degree of freedom. The solution corresponding to the minimal distance between  $p_{T,\nu}$  and  $\vec{p}_T^{\prime}$  is chosen.
- For a positive discriminant, the solution corresponding to the smallest absolute value of  $p_{z,\nu}$  is chosen [41, 42].

256 This implies that the four-momentum of the W boson candidate can be completely determined.  
 257 In the 2J1T and 3J1T regions, the b-tagged jet is assumed to come from the top quark decay.  
 258 In the 3J1T region, the most forward jet is considered to be the one stemming from the light  
 259 quark recoiling against the top. In the 3J2T region, the b-tagged jet corresponding to the lowest  
 260 difference between the reconstructed top quark mass and 172.5 GeV (top quark mass used in  
 261 simulation for the nominal sample) is attributed to stem from the b-quark from the top decay,  
 262 while the untagged jet is identified to originate from the light quark. In the 2J0T region, the  
 263 following three cases are considered.

- 264 • If both jets pass b-tagging algorithm, but do not satisfy the tight criterion, then the jet  
 265 with the higher b-tagging discriminant value is attributed to the b-quark originating  
 266 from the top.
- 267 • If only one of the two jets passes the b-tagging algorithm but does not satisfy the  
 268 b-tagging discriminator tight criterion, then that jet is identified as the b-jet due to  
 269 top quark decay.
- 270 • In the case where none of the jets pass the b-tagging algorithm, the one with lower  
 271  $|\eta|$  is assigned as the b-jet from the decay of the top quark.

272 A detailed study of the jet-to-parton assignment in signal and control regions can be found in  
 273 Ref. [35]. The four-momentum of the W boson is then added to that of the b-jet candidate to  
 274 obtain the four-momentum of the mother top quark.

## 275 7 QCD Background Estimation

276 QCD multijet has a huge production cross section in pp collisions. However, only a small  
 277 fraction of these events can mimic the lepton+jets final state of the applied event selection in  
 278 this analysis. Thus, the selection efficiency for QCD multijet events is tiny. The large cross  
 279 section coupled with very small efficiency would require the generation of an extremely large  
 280 MC sample for this process in order to retain sufficient events surviving our event selection  
 281 to ensure a reliable description of QCD modeling in the signal region. An alternative and  
 282 pragmatic way is to define a sideband (SB) in data that is enriched in QCD events and to use  
 283 the distributions of relevant kinematic variables directly from this region. In the following  
 284 subsections, the definition of the QCD enriched SB and the estimation of QCD contribution to  
 285 the signal region (SR) by means of a binned maximum-likelihood (ML) fit are discussed. The  
 286  $m_T^W$  and  $\cancel{p}_T$  are used as the fit variables for this purpose in the  $\mu$ +jets and e+jets final states,  
 287 respectively. As the available QCD statistics is larger in the 2J0T control region, this region has  
 288 been used as a proof-of-concept of the method, which is later applied to the signal-enriched  
 289 2J1T region.

### 290 7.1 Modeling and Estimation of QCD Background in 2J0T

291 The 2J0T control region is dominated by QCD and W+light-flavor jets events. The fraction  
 292 of QCD events in this region can be significantly increased by inverting the isolation or iden-  
 293 tification criterion for the muon or electron, e.g.,  $I_{\text{rel}} > 0.2$  or cut-based “veto” identification  
 294 criteria. Figure 18 shows a comparison between QCD templates in the SR and SB for  $m_T^W$ . A  
 295 good agreement between the two orthogonal regions is observed. Using simulated samples for  
 296 all relevant signal and background processes, the QCD purity of the SB has been estimated to  
 297 be  $\approx 93\%$ . Therefore, small contributions from nonQCD processes in SB can be neglected.

298 The  $m_T^W$  and  $\cancel{p}_T$  variables provide a good discrimination between QCD and nonQCD processes  
 299 with prompt muons or electrons, respectively in the  $\mu$ +jets and e+jets events. Therefore,  $m_T^W$

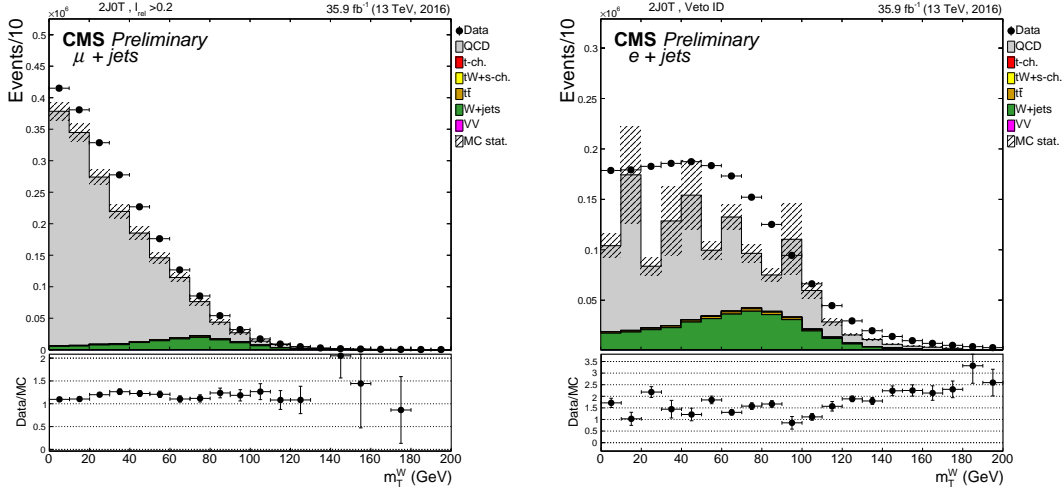


Figure 18: Data-MC comparison for  $m_T^W$  in the SB (left) and comparison of the QCD  $m_T^W$  templates between SR and SB of 2J0T (right).

300 ( $\cancel{p}_T$ ) is chosen to be the fit variable, represented by  $X$ , in the final state containing muon (elec-  
 301 tron). A binned extended ML fit with two parameters is performed to the distribution of  $X$  in  
 302 the 2J0T region. We assume that the distribution of  $X$  in data,  $F(X)$ , can be modeled as:

$$F(X) = N_{\text{QCD}} \cdot Q(X) + N_{\text{nonQCD}} \cdot W(X) \quad (11)$$

303 where  $Q(X)$  stands for the QCD template taken from the SB as described earlier and  $W(X)$   
 304 represents the combined template for all nonQCD processes obtained by adding up MC con-  
 305 tributions of the individual processes in the SR, weighted according to their respective cross  
 306 sections. Both templates are normalized to an integral of 1.0. The fit parameters  $N_{\text{QCD}}$  and  
 307  $N_{\text{nonQCD}}$  represent the yields of QCD and nonQCD processes, respectively; they are allowed to  
 308 float freely during the fit. Figures 19 and 20 show the postfit distributions in  $\mu$ +jets and  $e$ +jets  
 309 final states, respectively. The fit is repeated with different QCD templates obtained from MC  
 310 events in SR and SB, as well as a data-driven (DD) template derived in SB by subtracting the  
 311 contribution of nonQCD processes from data. The entire range of the fit variable distribution is  
 312 fitted. From the resulting QCD yield, we estimate the QCD contribution in the SR for  $m_T^W$  ( $\cancel{p}_T$ )  
 313  $> 50$  (30) GeV by calculating the integral of the  $m_T^W$  ( $\cancel{p}_T$ )-distributions of QCD, normalized  
 314 to the fit-result, in  $m_T^W$  ( $\cancel{p}_T$ )  $> 50$  (30) GeV. The QCD template is derived from data in the SB,  
 315 as described above, while the actual fit is performed in the SR. The postfit yields with different  
 316 QCD templates are summarized in Table 5. Overall good agreement, within uncertainties, is  
 317 observed among results from fits based on different QCD templates, in case of both  $m_T^W$  and  $\cancel{p}_T$ .  
 318 The largest difference between the yields for  $m_T^W$  ( $\cancel{p}_T$ )  $> 50$  (30) GeV is taken as uncertainty in  
 319 the QCD normalization for the final state containing muon (electron).

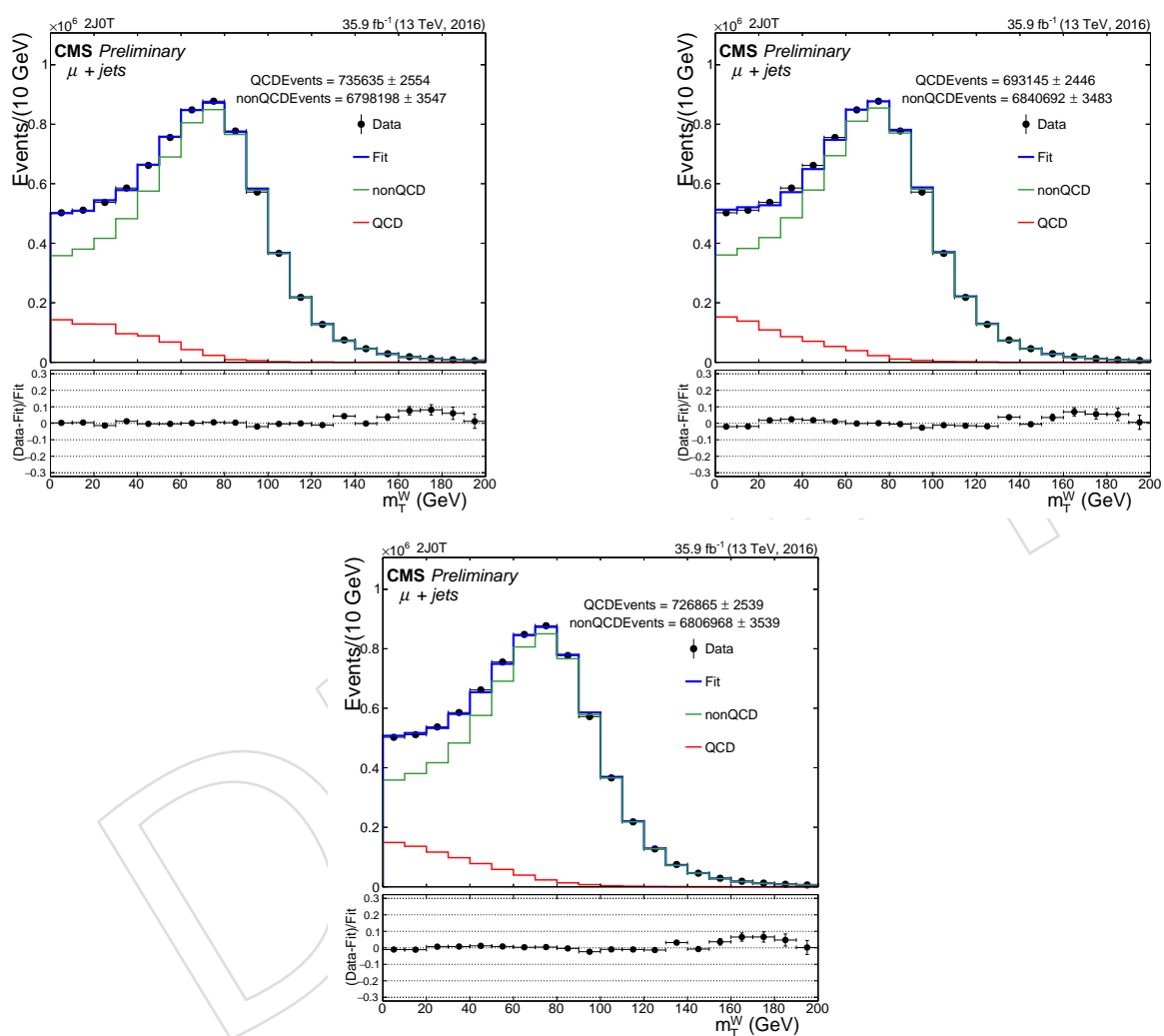


Figure 19: Postfit distribution of  $m_T^W$  with different QCD templates: MC templates from SR (top left) and SB (top right), and DD template from SB (bottom).

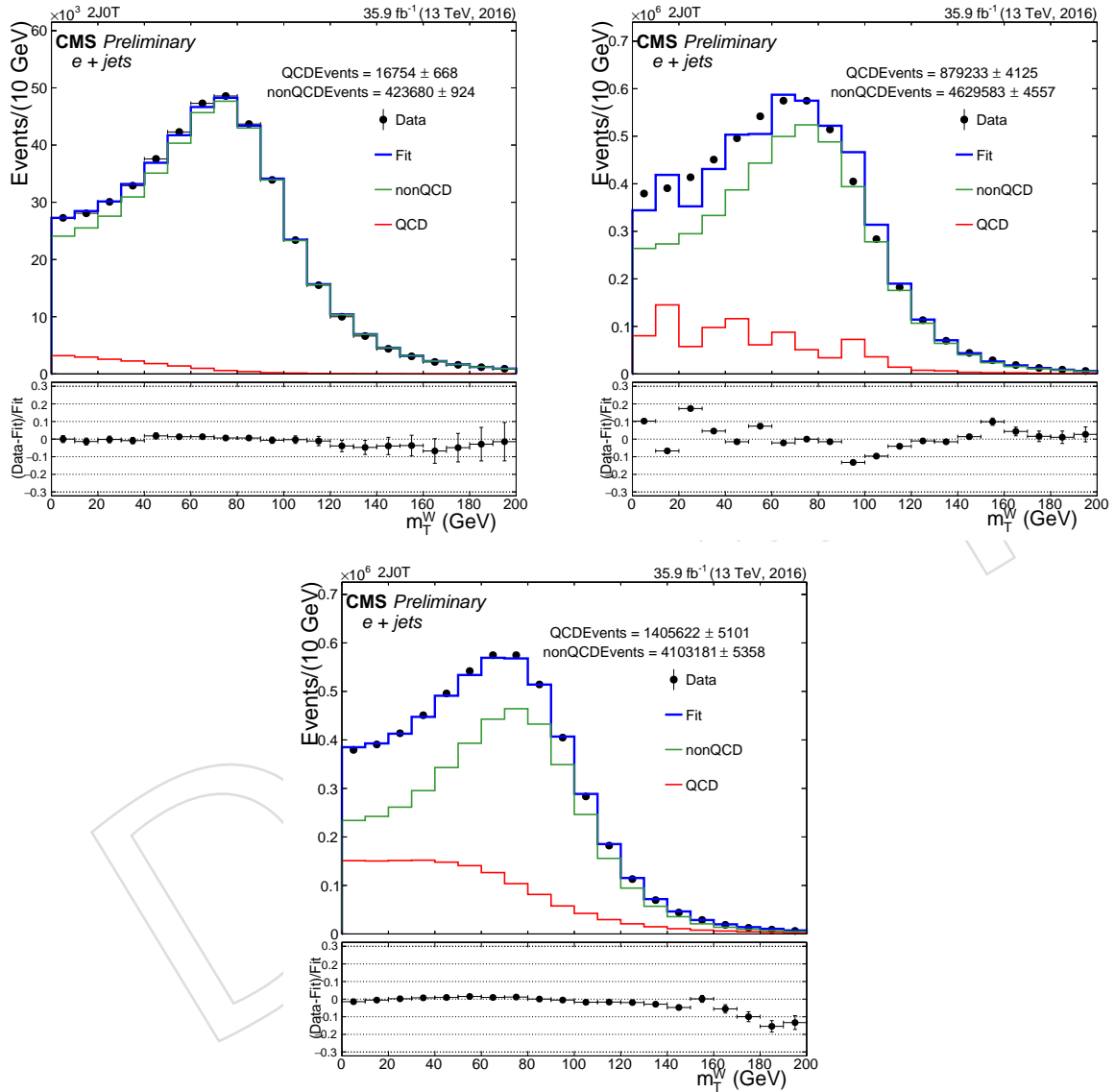


Figure 20: Postfit distribution of  $m_T^W$  with different QCD templates: MC template from SR (top left) and SB (top right), and DD template from SB (bottom).

Table 5: QCD estimation in the 2J0T region.

Variable	QCD template	Process	Fitted yield (full range)	Yield for $m_T^W(\cancel{p}_T) > 50$ (30) GeV
$m_T^W$	MC template from SB	QCD	$635688 \pm 2415$	$122417 \pm 465$
		nonQCD	$6763128 \pm 3457$	$4546640 \pm 2324$
	Data-driven template from SB	QCD	$674599 \pm 2538$	$131951 \pm 527$
		nonQCD	$6724217 \pm 3533$	$4520480 \pm 2375$
	MC template from SR	QCD	$674471 \pm 2524$	$136613 \pm 511$
		nonQCD	$6724343 \pm 3524$	$4520570 \pm 2369$
$\cancel{p}_T$	MC template from SB	QCD	$1677676 \pm 3713$	$724528 \pm 1603$
		nonQCD	$4732461 \pm 4103$	$3250420 \pm 2818$
	Data-driven template from SB	QCD	$2038996 \pm 4340$	$951068 \pm 2024$
		nonQCD	$4371114 \pm 4597$	$3002240 \pm 3157$
	MC template from SR	QCD	$1813942 \pm 3979$	$815706 \pm 1789$
		nonQCD	$4596206 \pm 4314$	$3156840 \pm 2963$

## 320 7.2 Estimation of QCD Background in 2J1T

### 321 7.2.1 Inclusive of lepton charge

322 The binned ML fit procedure used in the 2J0T control region is applied in the signal-enriched  
 323 2J1T region to the fit variable  $X$  ( $X = m_T^W$  or  $\cancel{p}_T$ ). The template  $W(X)$  is again derived from  
 324 MC simulation by summing up the individual contributions of different processes, weighted  
 325 according to their respective cross sections, while the QCD template,  $Q(X)$ , is derived from the  
 326 SB. Figure 21 shows the data-MC comparison for  $m_T^W$  in the SB as well as a comparison of QCD  
 $m_T^W$ -templates from SR and SB in the  $\mu$ +jets final state.

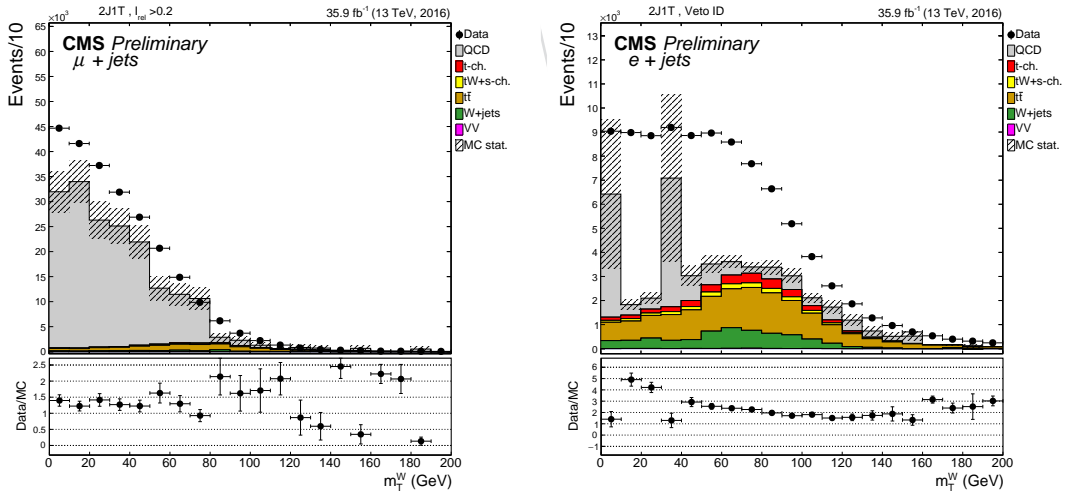


Figure 21: Data-MC comparison for  $m_T^W$  in the SB (left) and comparison between the QCD  $m_T^W$ -templates derived from SR and SB of 2J1T (right).

327

328 As discussed in Section 7.1, the entire  $m_T^W(\cancel{p}_T)$ -distribution is fitted and the QCD contribution  
 329 in the SR for  $m_T^W(\cancel{p}_T) > 50$  (30) GeV is estimated from the postfit  $m_T^W(\cancel{p}_T)$ -distribution, nor-  
 330 malized to the fit result. Figures 22 and 23 show the postfit distributions for the SR in the  $\mu$ +jets

Table 6: QCD estimation in the 2J1T region.

Variable	Process	Fitted Yield (full range)	Yield above $m_T^W(\cancel{p}_T) > 50(30)$ GeV
$m_T^W$	QCD	$67928 \pm 713$	$14983 \pm 157$
	nonQCD	$475257 \pm 957$	$322496 \pm 649$
$\cancel{p}_T$	QCD	$63226 \pm 819$	$31659 \pm 410$
	nonQCD	$293416 \pm 949$	$225532 \pm 729$

Table 7: QCD estimation in the 2J1T region separated by charge.

	Process	Fitted yield (full range)	Yield for $m_T^W(\cancel{p}_T) > 50(30)$ GeV
$\mu^+$	QCD	$32975 \pm 511$	$7217 \pm 112$
	nonQCD	$250244 \pm 692$	$169756 \pm 469$
$\mu^-$	QCD	$34997 \pm 496$	$7778 \pm 110$
	nonQCD	$224971 \pm 661$	$152710 \pm 448$
$e^+$	QCD	$32109 \pm 593$	$16201 \pm 299$
	nonQCD	$151958 \pm 686$	$116842 \pm 528$
$e^-$	QCD	$31156 \pm 564$	$15477 \pm 280$
	nonQCD	$141419 \pm 655$	$108661 \pm 503$

331 and e+jets final states, respectively. Table 6 reports the postfit QCD and nonQCD yields.

### 332 7.2.2 Separation by lepton charge

333 The same binned ML fit as before is applied to the  $m_T^W(\cancel{p}_T)$  distribution in the 2J1T region, but  
334 separately for the positively and negatively charged leptons. This is necessary as the final mass  
335 measurement will be separately performed for positively and negatively charged leptons. The  
336 templates for the nonQCD processes are again derived from MC simulation by summing up  
337 the individual contributions from different processes, weighted according to their respective  
338 cross sections. The QCD templates are derived from the SB in data, as discussed before. The  
339 entire  $m_T^W(\cancel{p}_T)$ -distribution in the SR is fitted and the QCD contribution in the SR for  $m_T^W$   
340  $(\cancel{p}_T) > 50(30)$  GeV is estimated from the postfit  $m_T^W(\cancel{p}_T)$ -distributions normalized to the fit  
341 result. Table 7 lists the QCD and nonQCD yields obtained from various fits corresponding to  
342 positively and negatively charged leptons. The postfit distributions are shown in Figures 22  
343 and 23 for  $\mu$ +jets and e+jets final states, respectively.

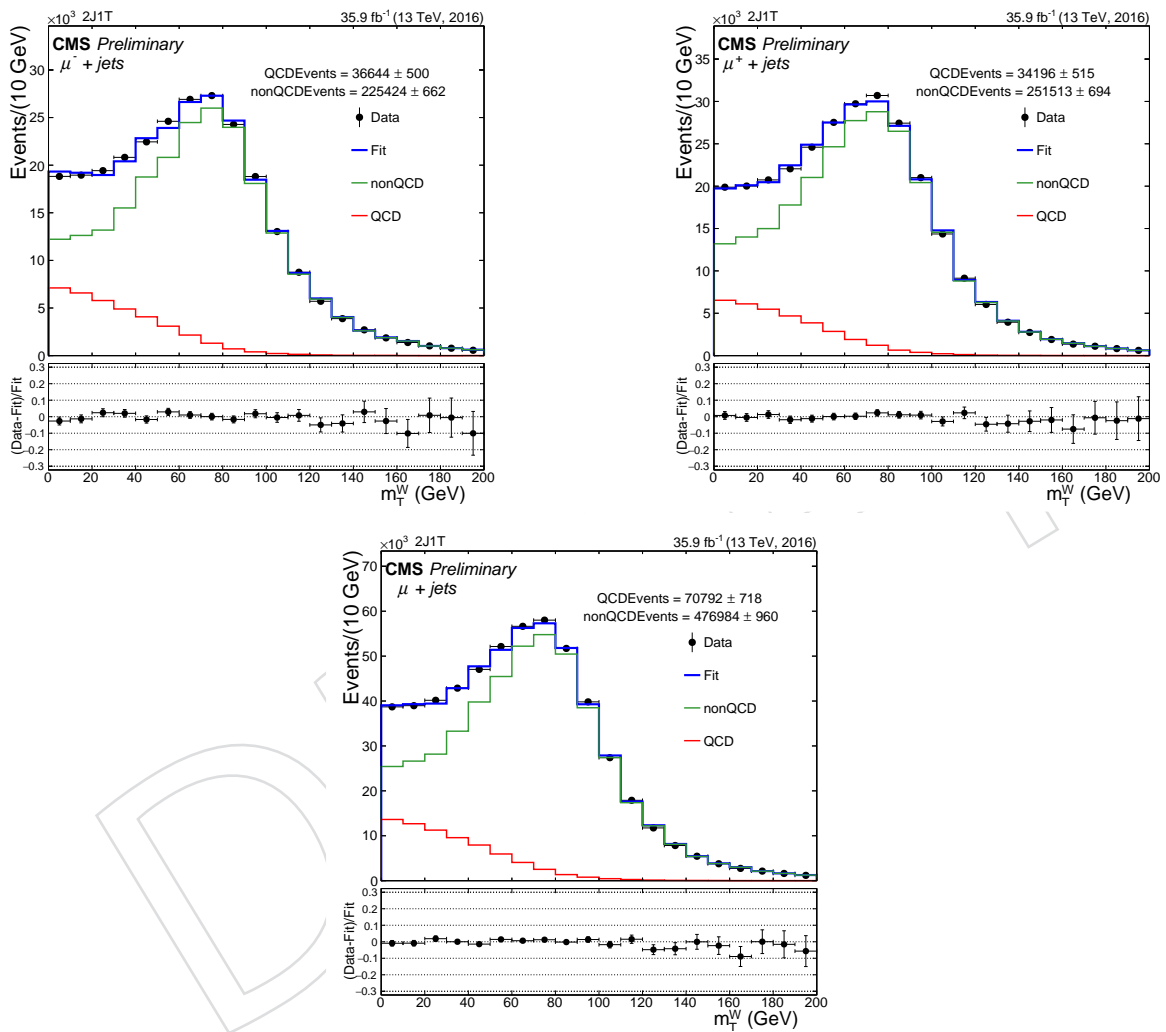


Figure 22: Fit in the SR using data-driven QCD  $m_T^W$  template from the SB for  $\mu^-$  (top left),  $\mu^+$  (top right) and inclusive (bottom) cases in the  $\mu$ +jets final state.



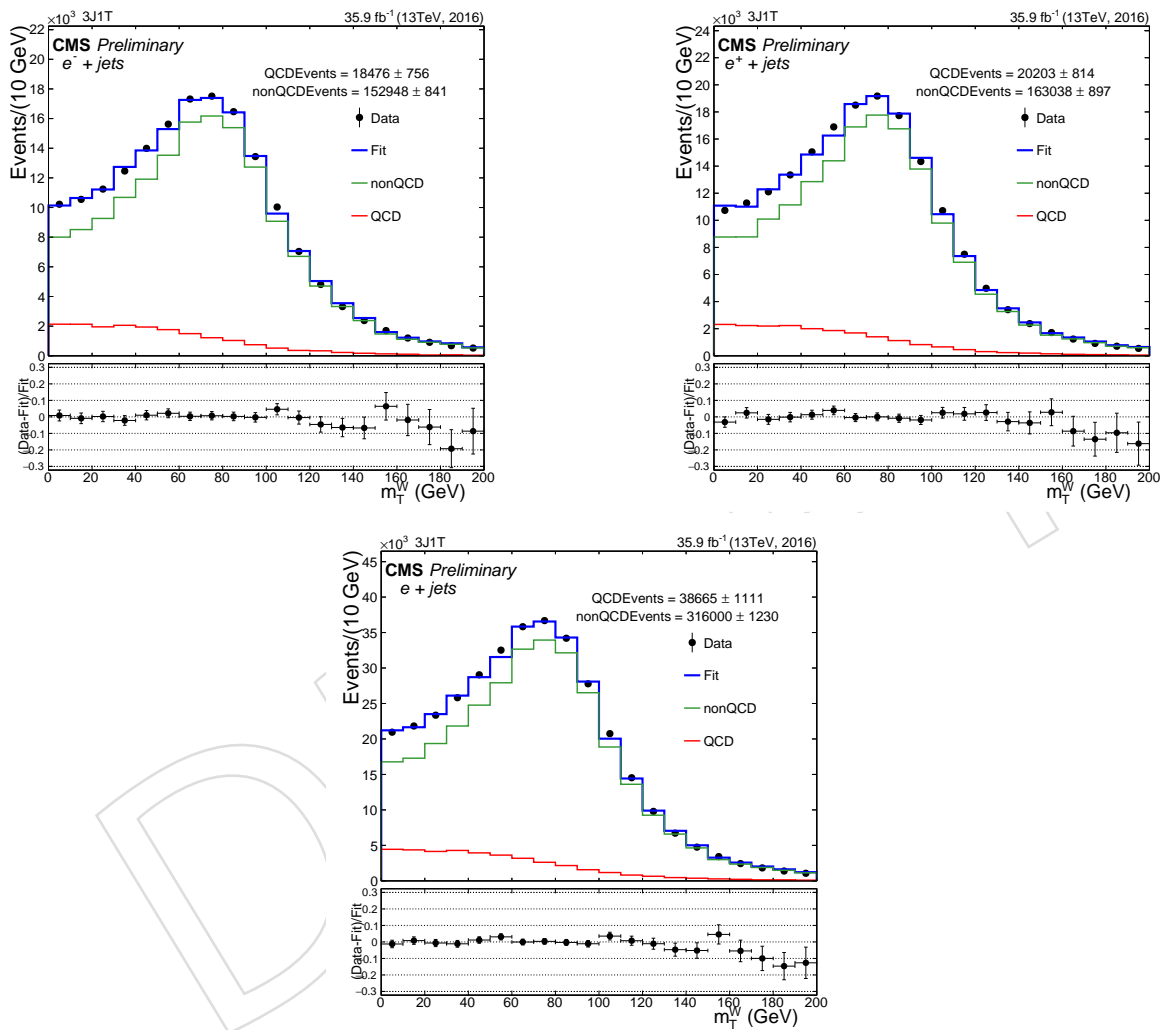


Figure 23: Fit in the SR using data-driven QCD  $p_T$ -template from SB region for  $e^-$  (top left),  $e^+$  (top right) and inclusive (bottom) cases in the  $e+$  jets final state.

## 344 8 Multivariate Discriminator

345 Several input variables can be combined into a single MVA discriminator to achieve a better  
 346 separation between the signal and backgrounds. The correlations among various input vari-  
 347 ables can also be taken into account while calculating the discriminator. In this analysis, two  
 348 separate boosted decision trees (BDTs) are developed using the input variables listed in Tables 8  
 349 and 9 for the  $\mu$ +jets and e+jets final states, respectively. The TMVA package [43] built into ROOT  
 has been used for this purpose.

Table 8: Input variables to BDT ranked according to their separation power for the muon final state.

Rank	Variable	Separation power
1	$\Delta R(\text{b-jet, light jet})$	2.090e-01
2	light jet $ \eta $	2.056e-01
3	$m_{b\bar{b}}$	1.656e-01
4	$\cos\theta^*$	6.769e-02
5	$m_T^W (>50 \text{ GeV})$	4.497e-02
6	$\Delta\eta(\mu, \text{b-jet})$	1.343e-02
7	b-jet $p_T$ + light jet $p_T$	7.352e-03
8	$ \eta $ of $\mu$	3.584e-04

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Table 9: Input variables to BDT ranked according to their separation power for electron final state.

Rank	Variable	Separation power
1	light jet $ \eta $	2.045e-01
2	$m_{b\bar{b}}$	1.764e-01
3	$\Delta R(\text{b-jet, light jet})$	6.444e-02
4	$\cos\theta^*$	2.342e-02
6	b-jet $p_T$ + light jet $p_T$	1.443e-02
5	$\Delta\eta(\text{e, b-jet})$	4.716e-03
7	$ \eta $ of e	2.450e-04

351 All input variables are validated by comparing data and MC distributions. The  $t$ -channel single  
 352 top signal is trained against  $t\bar{t}$  and electroweak ( $V$ +jets and  $VV$ ,  $V = W$  or  $Z$ ) processes in the  
 353 2J1T region with QCD mixed in, after applying the  $m_T^W$  ( $p_T$ ) cut for the muon (electron) final  
 354 state. During training, signal and background processes are weighted according to their purity  
 355 in the 2J1T region. The BDT setup is checked for overtraining by dividing the MC samples into  
 356 two independent subsamples, one for BDT training and the other to evaluate its performance.  
 357 The result is shown in Figure 24, which depicts no overtraining. The input variables are so  
 358 chosen that the correlation between the reconstructed  $m_t$  and the BDT response is as low as  
 359 possible in both muon and electron final states. This ensures that any cut on the BDT response  
 360 minimally impacts the reconstructed  $m_t$  distribution. The distributions of the BDT response in  
 361 data as well as in simulation in the 2J1T region for muon and electron final states are shown in  
 362 Figure 25.

363 A cut on the BDT response is applied to select a sample enriched in  $t$ -channel single top events.  
 364 The cut is optimized by studying signal and background efficiencies as well as signal purity of

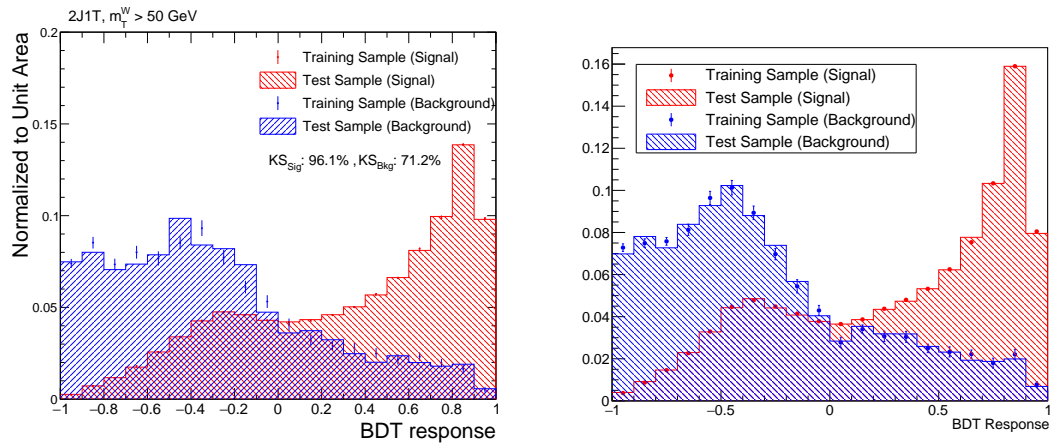


Figure 24: Overtraining check of BDT discriminator between test and training sample for muon (left) and electron (right) final states.

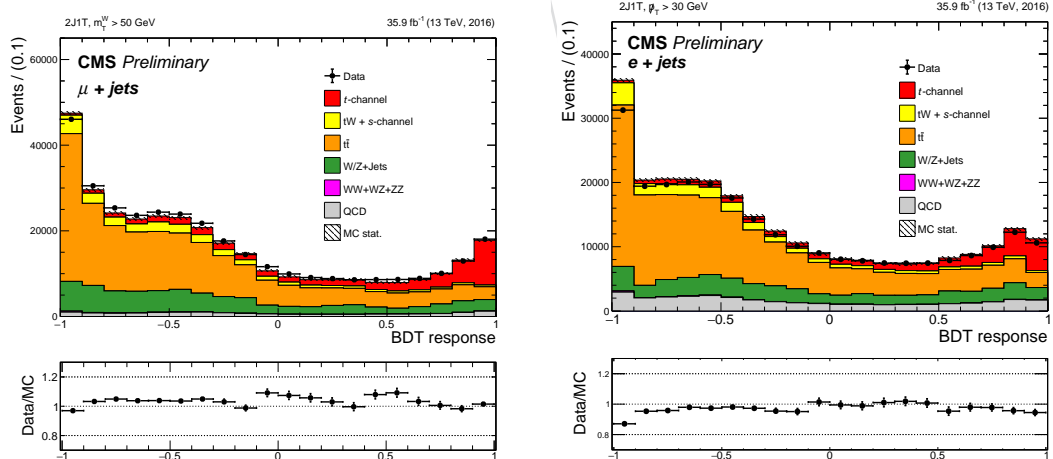


Figure 25: Data-MC comparison of BDT response in 2J1T for muon (left) and electron (right) final states.

365 the resulting sample after cut, as shown in Figure 27. Based on this study, BDT response  $> 0.8$   
 366 is chosen so that the resulting sample has enough signal and background statistics, and more  
 367 importantly, the cut corresponds to 60.7% (53.1%) signal purity and a signal-to-background  
 368 ratio of 1.55 (1.13), for the  $t$ -channel single top process in the muon and electron final states, re-  
 369 spectively. The resulting  $m_t$  distributions after applying BDT selection are shown in Figure 27.

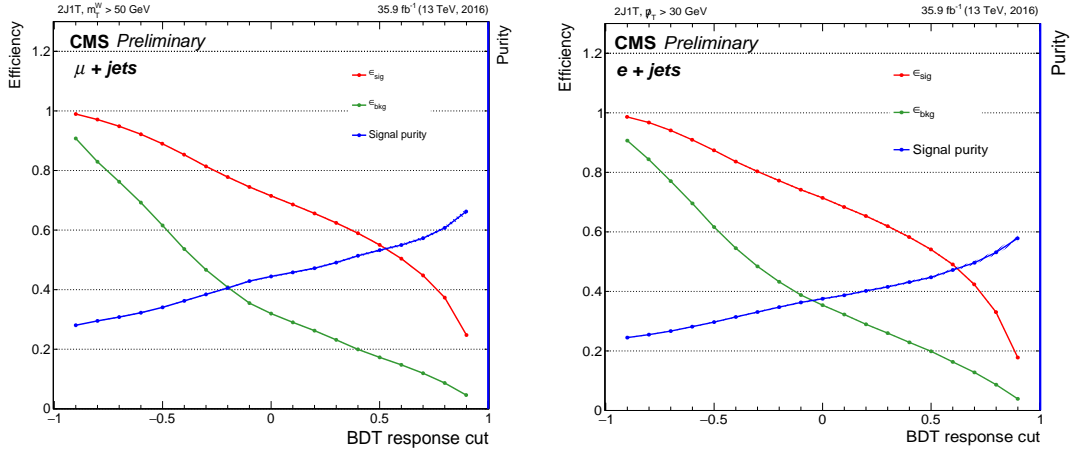


Figure 26: Study of signal and background efficiencies and signal purity as a function of cut on the BDT response for the muon (left) and electron (right) final states.

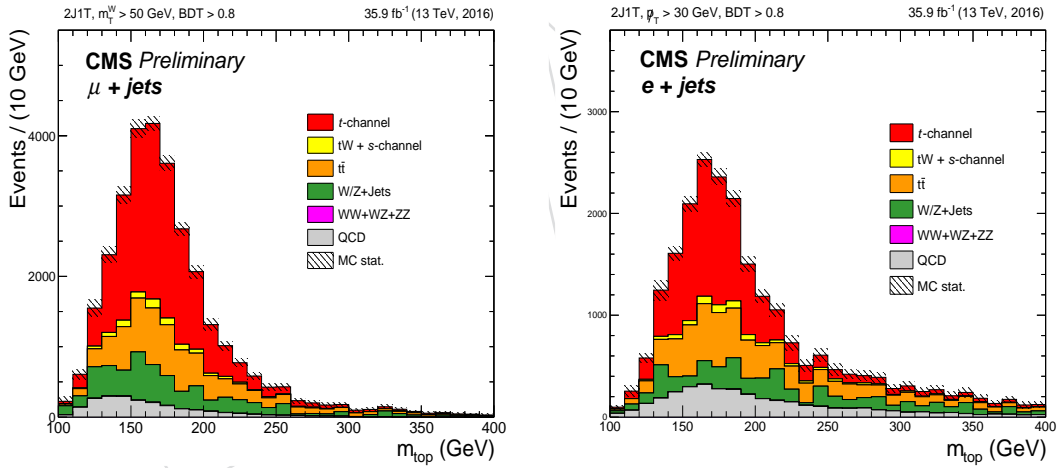


Figure 27:  $m_t$  distribution in 2J1T from simulation after applying BDT response  $> 0.8$  for muon (left) and electron (right) final states.

## 9 Top Mass Extraction

A variety of parametric templates have been tried to model signal and background components in the  $m_t$  distribution using the respective MC samples. High skewness of the distribution as well as lower background rate after BDT selection pose a considerable challenge to obtain stable and appropriate parametric templates for both signal and backgrounds. Instead, a suitable alternative is found in the form of the natural logarithm of  $m_t$ , i.e.,  $y = \ln m_t$ . It has been observed that, by taking the natural logarithm, the skewness can be significantly reduced [44, 45] for a positive random variable such as  $m_t$ , which is skewed to the right. This happens due to the fact that the logarithm *pulls in* more extreme values on the right relative to the mode of the original distribution, whereas the extreme values on left of the mode are *stretched back* farther away from the mode, thus reducing the overall skewness. Also, the logarithm being a monotonic function, the transformed probability density functions are well behaved.

Henceforth,  $y = \ln m_t$  distributions from signal and background processes are used for parametric modeling. Figure 28 shows these distributions in simulated events in the 2J1T region after applying the BDT selection. The  $y$  distributions obtained from the muon and electron final states are simultaneously considered in the fit. The top quark mass is determined by taking the exponential of the parameter that denotes the peak position ( $y_0$ ) of the distribution. The parametric 1D template used to simultaneously model in the muon and electron final state can be described as:

$$F(y = \ln m_t) = f_{t\text{-ch}} \cdot F_{t\text{-ch}}(y_0) + f_{\text{Top}} \cdot F_{\text{Top}}(y_0) + f_{\text{EWK}} \cdot F_{\text{EWK}}, \quad (12)$$

where  $F_{t\text{-ch}}$ ,  $F_{\text{Top}}$  and  $F_{\text{EWK}}$  represent the parametric templates for the signal, top ( $t\bar{t}$ ,  $tW$  and  $s$ -channel) and electroweak ( $V$ +jets and  $VV$  with  $V = W$  or  $Z$ ) backgrounds, respectively. The signal template,  $F_{t\text{-ch}}$ , is a sum of an asymmetric Gaussian and Landau functions [46] with unequal peaks. The top background template,  $F_{\text{Top}}$ , is a Crystal ball function [47] and the electroweak background template,  $F_{\text{EWK}}$ , is modeled with a Novosibirsk function [48]. The  $y_0$  value of the combined  $t$ -channel and top background templates along with the normalization scale factor for the  $t$ -channel single top ( $f_{t\text{-ch}}$ ) process are allowed float during the fit. The normalization scale factors for the top ( $f_{\text{Top}}$ ) and electroweak ( $f_{\text{EWK}}$ ) backgrounds are constrained using log-normal priors with 10% and 30% uncertainties, respectively, to account for uncertainties in the measurement of their respective cross sections at 13 TeV [49–52]. Other shape parameters of the templates comprising the model are tested on simulated samples and each of them is found to agree within a good level of accuracy. Therefore, these shape parameters are kept fixed to the values obtained during nominal fits to the respective MC distributions.

The output of the fit framework behaves linearly as shown in Figure 30 when checked against alternate top mass hypotheses using dedicated signal and  $t\bar{t}$  samples. The extracted mass is calibrated with respect to the *true* mass in simulation, and an offset correction is applied to the value obtained from fit to account for the differences between two masses. The deviation of the slope (p1) of the red line shown in Figure 30 from unity can be attributed mostly to resolutions of the  $b$ -tagged jet and  $\cancel{p}_T$  which go directly as inputs to the reconstructed  $m_t$ . Very little dependence is observed on  $f_{t\text{-ch}}$  with different top mass hypotheses. Pseudoexperiments are performed to test the robustness of the fit and check for any preset bias in the fit parameters. The respective pull distributions are observed to follow a Gaussian function with mean at zero and unit width, as shown in Figure 31. Pseudoexperiments are also used to determine the expected statistical uncertainty in  $m_t$ ; its value is obtained to be  $\pm 0.28$  GeV.

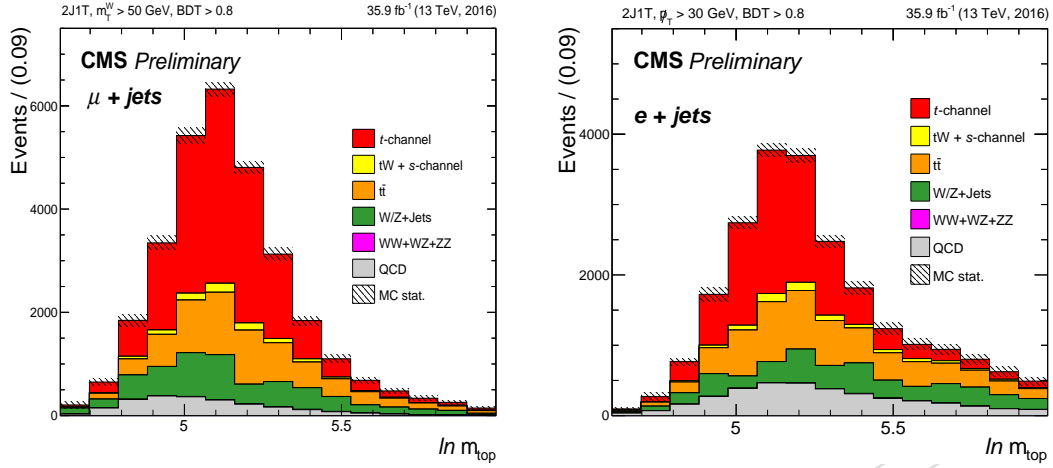


Figure 28: Distribution of  $\ln m_t$  after BDT selection in 2J1T using simulated samples for muon (left) and electron (right) final states.

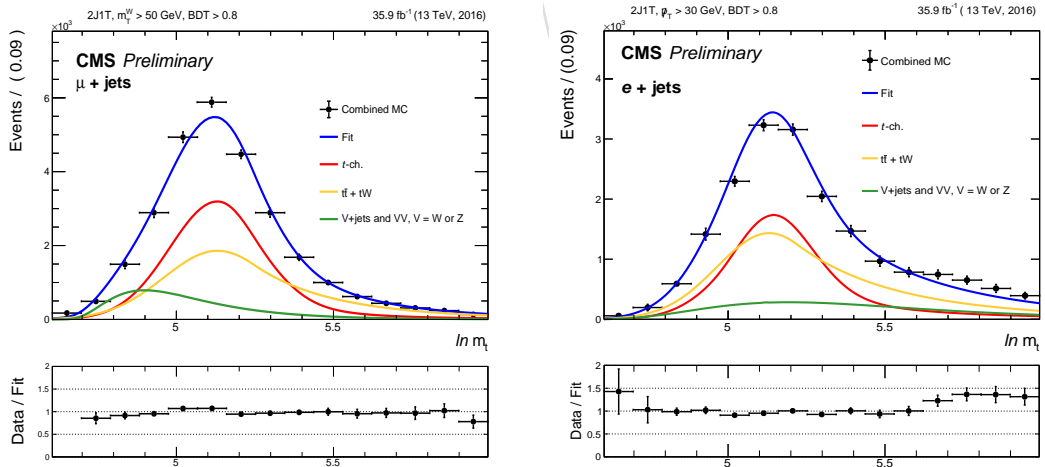
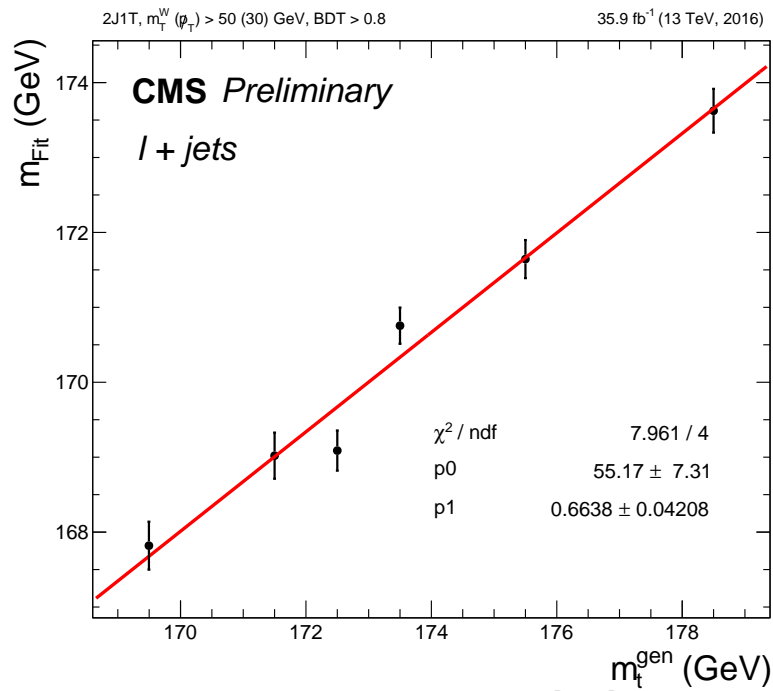
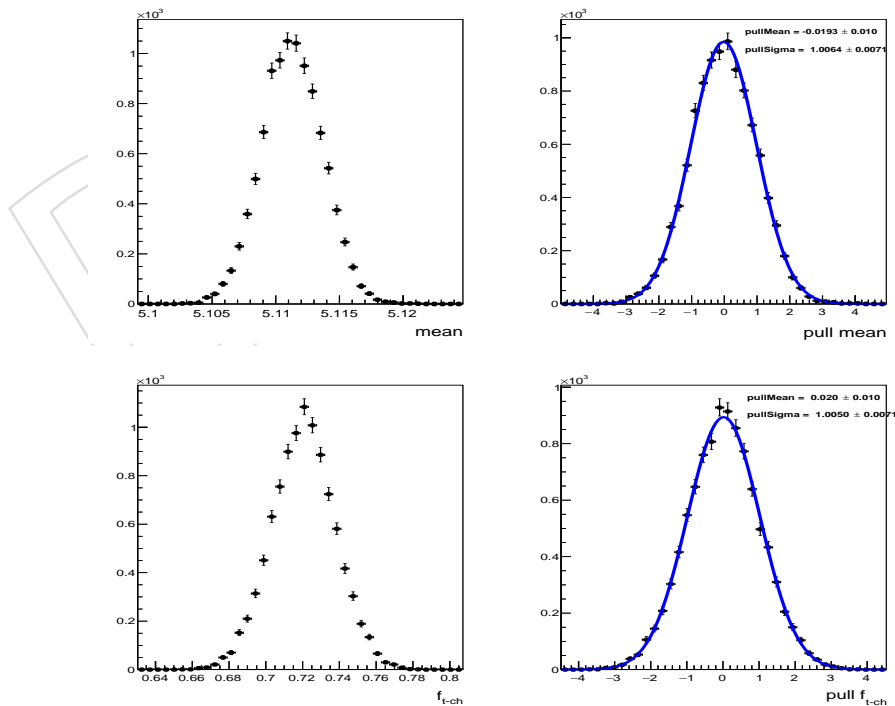


Figure 29: Parametric model for the  $\ln m_t$  distribution along with its components in MC events corresponding to muon (left) and electron (right) final states.

Figure 30: Linearity check of the  $m_t$  extracted from fit relative to the true  $m_t$ .Figure 31: Postfit distribution of fit parameters and their pulls in pseudoexperiments:  $y_0$  (top),  $f_{t\text{-ch}}$  (bottom).

## 10 Systematic Uncertainties

413

414 Various sources of systematic uncertainty that can affect the measured value of the top-quark  
 415 mass are considered. Uncertainties are calculated from the difference between the offset-corrected  
 416 postfit value of  $m_t$  corresponding to the nominal and varied templates using pseudoexper-  
 417 iments. The uncertainties can be grouped into two categories, experimental and modeling  
 418 uncertainties, depending on the nature of systematic source. The impact owing to individual  
 419 sources are listed in Table 10.

### 420 Experimental Uncertainties

421 • **Jet energy scale:** Energies of all reconstructed jets in simulated events are simulta-  
 422 neously scaled up and down according to their  $p_T$  and  $\eta$ -dependent uncertainties  
 423 [53], split into correlation groups, namely `InterCalibration`, `MPFInSitu` and  
 424 `Uncorrelated` according to the procedure in Ref. [54]. These variations are also  
 425 propagated to  $\cancel{p}_T$ .

426 • **Flavor-dependent jet energy corrections:** The Lund string fragmentation imple-  
 427 mented in PYTHIA 6.422 [55] is compared to the cluster fragmentation of HER-  
 428 WIG++ 2.4 [56]. Each model relies on a large set of tuning parameters that allow to  
 429 modify the individual fragmentation of jets initiated from gluons, light and b quarks.  
 430 Therefore, the difference in jet energy response between PYTHIA 6 and HERWIG++  
 431 is determined for each jet flavor [53] and then are added in quadrature.

432 • **Jet energy resolution:** To account for the difference in the jet energy resolution be-  
 433 tween data and simulation, a dedicated smearing is applied [53] that increases or  
 434 decreases the resolutions within their uncertainties.

435 • **Unclustered energy:** The contributions of unclustered particles to  $\cancel{p}_T$  are varied  
 436 within their respective energy resolutions [57].

437 • **Muon and electron efficiencies:** The efficiencies of the lepton identification and  
 438 isolation, of the used trigger paths as well as of the detector response are determined  
 439 with a “tag-and-probe” method [58] from Drell-Yan events falling into the Z boson  
 440 mass window. The uncertainties in the efficiency correction factors are varied in  
 441 bins of  $p_T$  and  $|\eta|$ .

442 • **Pileup:** The uncertainty in the average expected number of pileup interactions is  
 443 propagated as a systematic uncertainty by varying the minimum-bias cross section  
 444 by  $\pm 4.6\%$  [59].

445 • **b-tagging:** The scale factors used to calculate the efficiency corrections of the cM-  
 446 VAv2 b-tagging algorithm are varied up and down within their uncertainties. From  
 447 these up and down varied scale factors, up- and down-shifted efficiency corrections  
 448 are calculated and applied to the simulation.

449 • **Luminosity:** The relative uncertainty in the integrated luminosity is determined to  
 450 be  $\pm 2.5\%$  [8]. This is propagated as uncertainties in the expected rate of signal and  
 451 background processes except for QCD, which is determined from data.

### 452 Modeling Uncertainties

453 • **Offset correction:** The offset correction, i.e., the difference between the mass ob-  
 454 tained from fit and the true mass is considered to be a function of the mass obtained  
 455 from fit, using dedicated MC samples with alternate top mass hypotheses (Figure 32).  
 456 The band about the central line represents  $\pm 1$  standard deviation owing to statistical  
 457 fluctuations of the signal and  $t\bar{t}$  samples with different mass hypotheses. The offset



correction is obtained from the central value while the corresponding uncertainty is determined from the band and considered as an independent source of uncertainty.

- **Background normalizations:** The contribution of QCD multijet background as estimated by the data-driven method (Section 7) is first subtracted from data. In order to account for the differences in the QCD-estimate using different templates, a  $\pm 50\%$  uncertainty in the estimated QCD normalization is considered. The corresponding uncertainty in the measurement is obtained from the difference in fit results due to the varied templates. The uncertainties  $\pm 10\%$  and  $\pm 30\%$  in the rates of the top and electroweak backgrounds, respectively, are propagated by considering their rates as nuisance parameters in the fit.

- **Signal modeling:** To determine the influence of possible mismodeling of the signal process, several sources are considered which are listed below.

**Parton shower (PS) scale:** The nominal signal sample is compared with dedicated samples generated with a PS scale shifted by  $\pm 1$  standard deviation. The uncertainty is estimated from the difference in the fit results due varied samples relative to the nominal one.

**ME/PS matching scale:** The model parameter  $h_{\text{damp}} = 1.58^{+0.66}_{-0.59}$  (with  $m_t = 172.5$  GeV) [60] used in POWHEG to control the matching of the matrix element to the parton shower (ME-PS matching) and to regulate the high- $p_T$  radiation in the simulation, is varied within its uncertainties.

**Renormalization/Factorization ( $\mu_R/\mu_F$ ) scale:** The uncertainties caused by variations in the renormalization and factorization scales ( $\mu_R/\mu_F$ ) are considered by applying weights [61], corresponding to simultaneously doubled or halved renormalization and factorization scales with the nominal value set to 172.5 GeV, on the  $y = \ln m_t$  distributions.

**PDF:** The impact due to the choice of PDFs is studied using reweighted templates that are derived from all PDF sets of NNPDF 3.0 [62].

- **$t\bar{t}$  modeling:** The impacts due to variation of the ISR and FSR-PS scales,  $h_{\text{damp}}$  parameter,  $\mu_R/\mu_F$  scale and PDF for the  $t\bar{t}$  process are considered by using either dedicated samples or reweighted templates, according to the uncertainty source. The uncertainty is determined from the difference in the fit results obtained from the varied  $t\bar{t}$  templates for each source relative to the nominal one. The contributions from individual sources are summed in quadrature to obtain the total uncertainty due to  $t\bar{t}$  modeling.
- **Electroweak background modeling:** The impacts due to variations of the  $\mu_R/\mu_F$  scales and PDF for the electroweak processes are considered by using reweighted templates according to the uncertainty source. The impact due to individual sources are again summed in quadrature to obtain the total uncertainty due to electroweak modeling.
- **Top quark  $p_T$ :** In differential measurements of the top quark  $p_T$  in  $t\bar{t}$  events, the predicted  $p_T$  spectrum is found to be harder than the observed spectrum [63]. To account for this mismodeling, postfit mass obtained using the default simulation for  $t\bar{t}$  is compared to the one based on simulated  $t\bar{t}$  events that are reweighted according to the observed difference between data and simulation in Ref. [63].
- **Color reconnection Tune:** The uncertainties that arise from ambiguities in modeling color reconnection effects are estimated by comparing among the default model in PYTHIA 8 with two alternative models of color reconnection, one with string for-

506 mation beyond leading color (QCD inspired) [64] and the other in which the gluons  
 507 can be moved to another string (gluon move) [5]. In addition, the effects of color  
 508 reconnection on the top decay products is considered by enabling early resonance  
 509 decays (ERD) in PYTHIA 8. All models are tuned to measurements of the underlying  
 510 event [65] and simultaneous variations of different tunes in  $t$ -channel single top  
 511 signal and  $t\bar{t}$  are considered. The largest observed shift are quoted as the systematic  
 512 uncertainty.

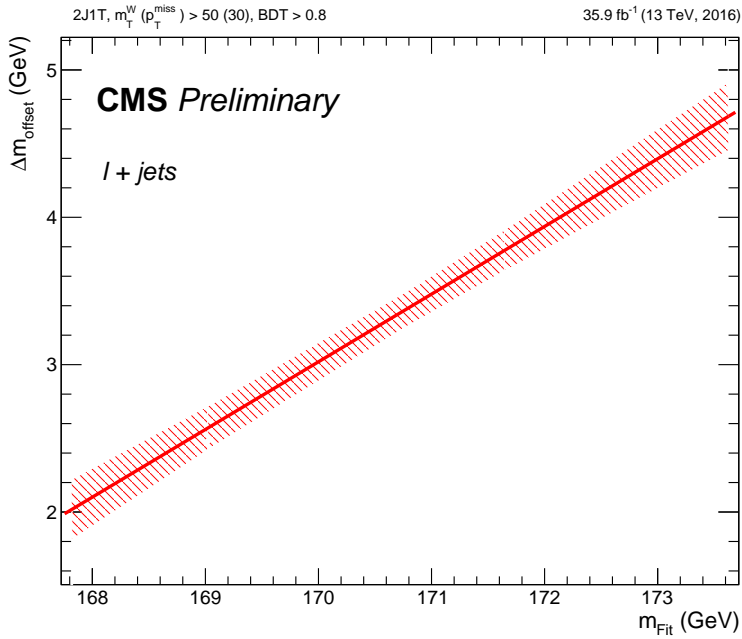


Figure 32: Offset correction as a function of the postfit mass.

Table 10: Summary of systematic uncertainties.

Source	$\delta m$ (GeV)	
muon efficiencies	identification	$\pm 0.01$
	isolation	$< \pm 0.01$
	trigger	$< \pm 0.01$
	total	$\pm 0.01$
electron efficiencies	identification	$\pm 0.02$
	trigger	$\pm 0.03$
	total	$\pm 0.04$
b-tagging	b-tagging efficiency	$\pm 0.22$
	misidentification probability	$\pm 0.03$
	total	$\pm 0.22$
pileup	$\pm 0.03$	
offset correction	$\pm 0.14$	
top $p_T$ reweighting	$-0.01$	
color reconnection tune	"gluon move" with ERD vs default with ERD	$+0.09$
	"QCD inspired" vs "gluon move"	$-0.05$
	$\pm 0.09$	
Luminosity	$\pm 0.01$	
Total syst.	$\pm 0.28$	
stat. + bkg. norm.	$\pm 0.27$	
Grand total	$\pm 0.39$	

## 11 Results

Based on a blind analysis with MC simulated events having *true*  $m_t$  set at 172.5 GeV, the value of the top quark mass measured with single top events in  $t$ -channel, obtained from the postfit  $\ln m_t$  distribution followed by offset correction, is given by:

$$m_t = 172.69 \pm 0.27(\text{stat} + \text{bkg. norm.}) \pm 0.28(\text{syst}) \text{ GeV} = 172.69 \pm 0.39 \text{ GeV} \quad (13)$$

The first uncertainty is due to the combined effect of uncertainties due to statistics and background normalizations, whereas the second denotes the total systematic uncertainty obtained so far. A total uncertainty of 0.39 GeV is obtained by adding the two uncertainties in quadrature.

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DRAFT



683 **A Systematic Samples**

Table 11: List of signal and background systematics samples.

Process	$\sigma(\times BR)[\text{pb}]$	Dataset name	$N_{\text{events}}$
$t$ -channel, top, hdamp up/down	136.02	ST.t-channel_top_4f_hdampup_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	6000000
		ST.t-channel_top_4f_hdampdown_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	6000000
$t$ -channel, anti-top, hdamp up/down	80.95	ST.t-channel_antitop_4f_hdampup_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	4000000
		ST.t-channel_antitop_4f_hdampdown_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	3999346
$t$ -channel, top, PS-scale up/down	136.02	ST.t-channel_top_4f_scaleup_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	5709148
		ST.t-channel_top_4f_scaledown_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	5946672
$t$ -channel, anti-top, PS-scale up/down	80.95	ST.t-channel_antitop_4f_scaleup_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	3970546
		ST.t-channel_antitop_4f_scaledown_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	3894778
$tW$ -channel, top, PS-scale up/down	35.6	ST.tW_top_5f_scaleup_inclusiveDecays.13TeV-powheg-pythia8.TuneCUETP8M1	997880
		ST.tW_top_5f_scaledown_inclusiveDecays.13TeV-powheg-pythia8.TuneCUETP8M1	993640
$tW$ -channel, anti-top, PS-scale up/down	35.6	ST.tW_antitop_5f_scaleup_inclusiveDecays.13TeV-powheg-pythia8.TuneCUETP8M1	1000000
		ST.tW_antitop_5f_scaledown_inclusiveDecays.13TeV-powheg-pythia8.TuneCUETP8M1	999068
$t\bar{t}$ , FSR up/down	831.76	TT.TuneCUETP8M2T4.13TeV-powheg-fsrup-pythia8	56168970
		TT.TuneCUETP8M2T4.13TeV-powheg-fsrdn-pythia8	29636416
$t\bar{t}$ , ISR up/down	831.76	TT.TuneCUETP8M2T4.13TeV-powheg-isrup-pythia8	29938880
		TT.TuneCUETP8M2T4.13TeV-powheg-isrdn-pythia8	59037234
$t$ -channel, top, alternate mass	136.02	ST.t-channel_top_4f_mtop1695_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	5802500
		ST.t-channel_top_4f_mtop1715_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	5839700
		ST.t-channel_top_4f_mtop1735_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	5930600
		ST.t-channel_top_4f_mtop1755_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	5930600
		ST.t-channel_top_4f_mtop1785_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	6084480
$t$ -channel, anti-top, alternate mass	80.95	ST.t-channel_antitop_4f_mtop1695_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	3891200
		ST.t-channel_antitop_4f_mtop1715_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	3948000
		ST.t-channel_antitop_4f_mtop1735_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	3927600
		ST.t-channel_antitop_4f_mtop1755_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	3962100
		ST.t-channel_antitop_4f_mtop1785_inclusiveDecays.13TeV-powhegV2-madspin-pythia8	3917400
$t\bar{t}$ , alternate mass	831.76	TT.TuneCUETP8M2T4.mtop1695.13TeV-powheg-pythia8	9954200
		TT.TuneCUETP8M2T4.mtop1715.13TeV-powheg-pythia8	19578812
		TT.TuneCUETP8M2T4.mtop1735.13TeV-powheg-pythia8	19419050
		TT.TuneCUETP8M2T4.mtop1755.13TeV-powheg-pythia8	29459232
		TT.TuneCUETP8M2T4.mtop1785.13TeV-powheg-pythia8	16377176
$t$ -channel, top, color reconnection tune	136.02	ST.t-channel_top_4f_CRTune_erdON.13TeV-powhegV2-madspin-pythia8	5935400
		ST.t-channel_top_4f_GluonMoveCRTune.13TeV-powhegV2-madspin-pythia8	5931424
		ST.t-channel_top_4f_GluonMoveCRTune_erdON.13TeV-powhegV2-madspin-pythia8	5965500
		ST.t-channel_top_4f_QCDBasedCRTune_erdON.13TeV-powhegV2-madspin-pythia8	5952488
$t$ -channel, anti-top, color reconnection tune	80.95	ST.t-channel_antitop_4f_CRTune_erdON.13TeV-powhegV2-madspin-pythia8	3971999
		ST.t-channel_antitop_4f_GluonMoveCRTune.13TeV-powhegV2-madspin-pythia8	3958536
		ST.t-channel_antitop_4f_GluonMoveCRTune_erdON.13TeV-powhegV2-madspin-pythia8	3934164
		ST.t-channel_antitop_4f_QCDBasedCRTune_erdON.13TeV-powhegV2-madspin-pythia8	3959800
$t\bar{t}$ , color reconnection tune	831.76	TT.TuneCUETP8M2T4_erdON.13TeV-powheg-pythia8	29938880
		TT.TuneCUETP8M2T4_GluonMoveCRTune.13TeV-powheg-pythia8	59037234
		TT.TuneCUETP8M2T4_GluonMoveCRTune_erdON.13TeV-powheg-pythia8	56168970
		TT.TuneCUETP8M2T4_QCDBasedCRTune_erdON.13TeV-powheg-pythia8	29636416