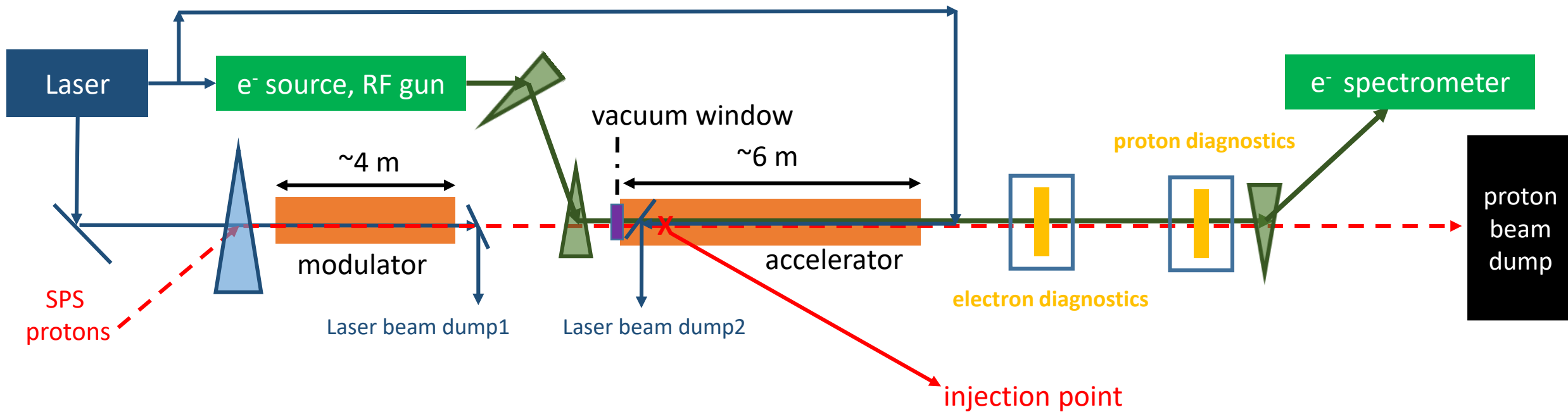


# Run2 layout



- %-level energy spread → beam loading

- emittance preservation → blowout regime

} beam matching is a necessary condition

**Matching: wakefield focusing force exactly compensates beam divergence.**

In the blowout:  $E_r = \frac{n_e e r}{2 \epsilon_0}$   $\xrightarrow{\text{eq. motion}}$   $\frac{d^2 r}{dt^2} = q E_r$

$$r(t) = r_0 e^{i \frac{\omega_p}{\sqrt{2} \gamma} t} = r_0 e^{i K t}$$

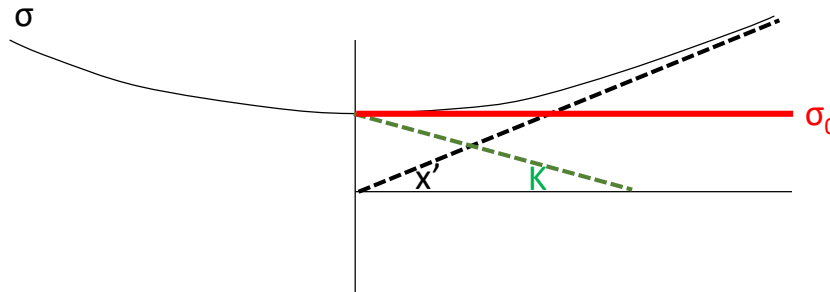
envelope equation:  $\sigma'' + \left( K^2 \sigma - \frac{\varepsilon^2}{\sigma^3} \right) = 0$

= 0, if beam is matched

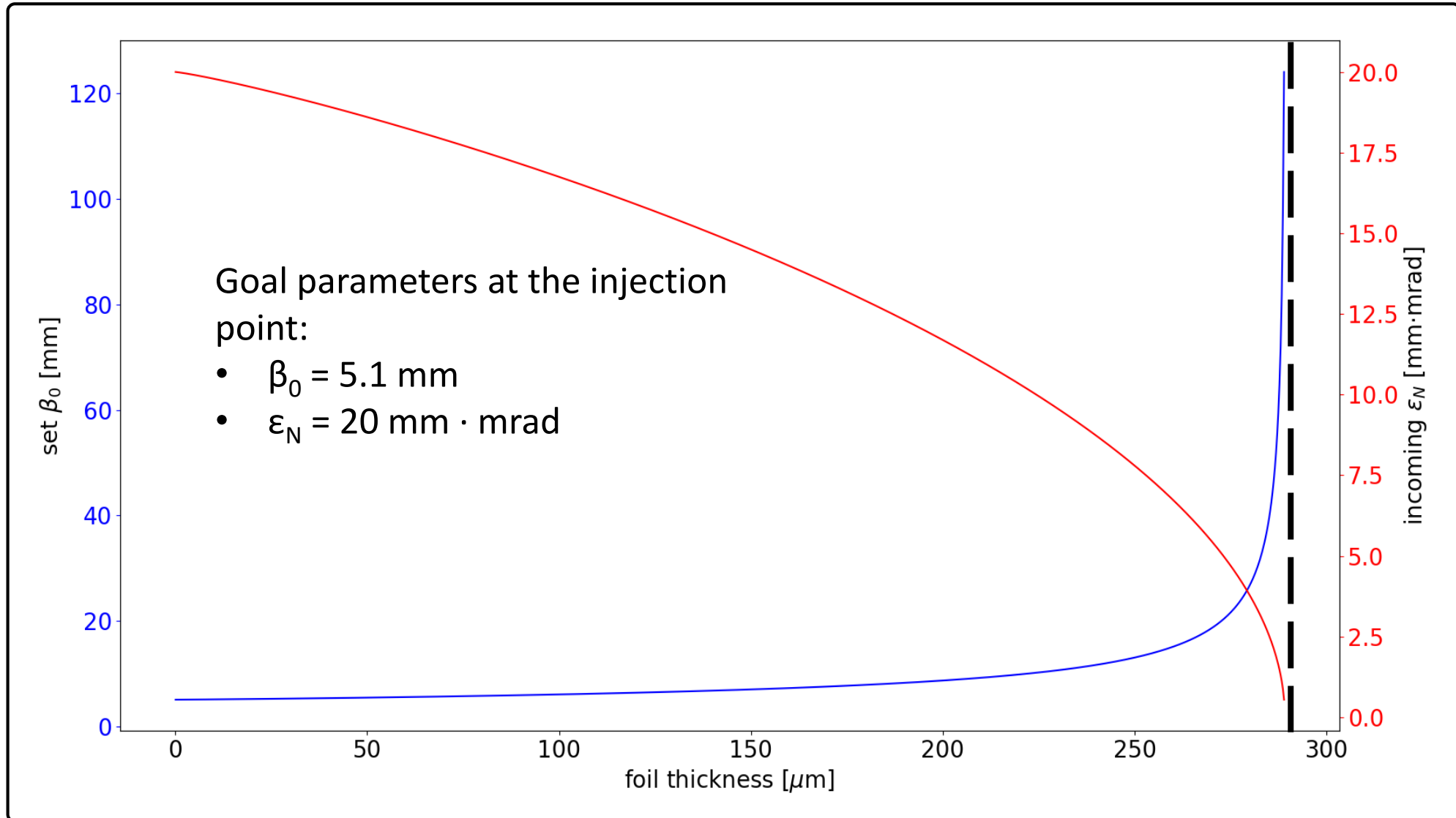
$$\beta_0 = \sqrt{\frac{2 \varepsilon_0 m_e c^2 \gamma}{n_e e^2}}$$

**matching is only  
β dependent!**

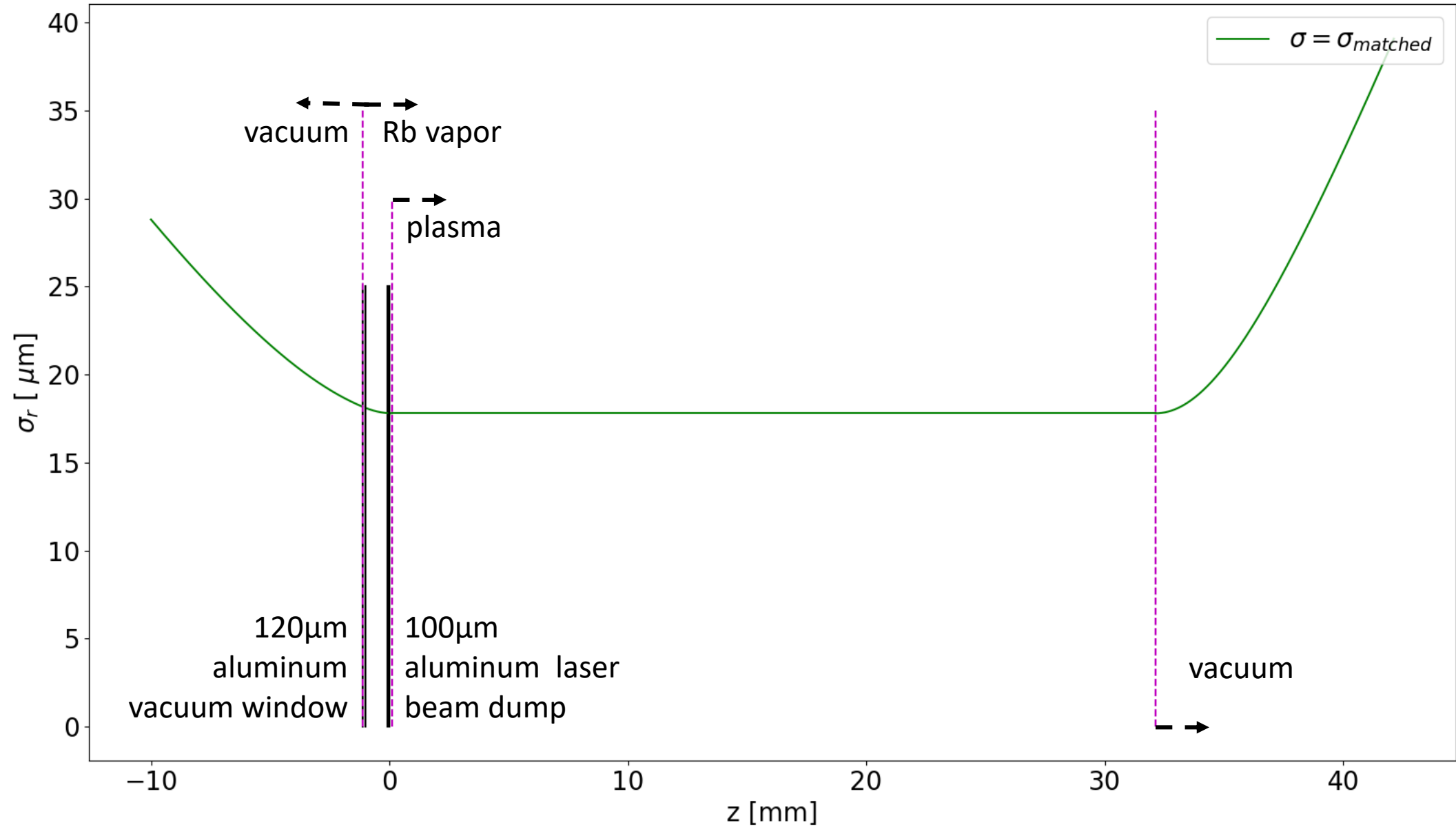
if the beam is injected at the waist ( $\sigma'_0 = 0$ ) with a spot size  $\sigma_0$ ,  
the beam size can be preserved along the plasma



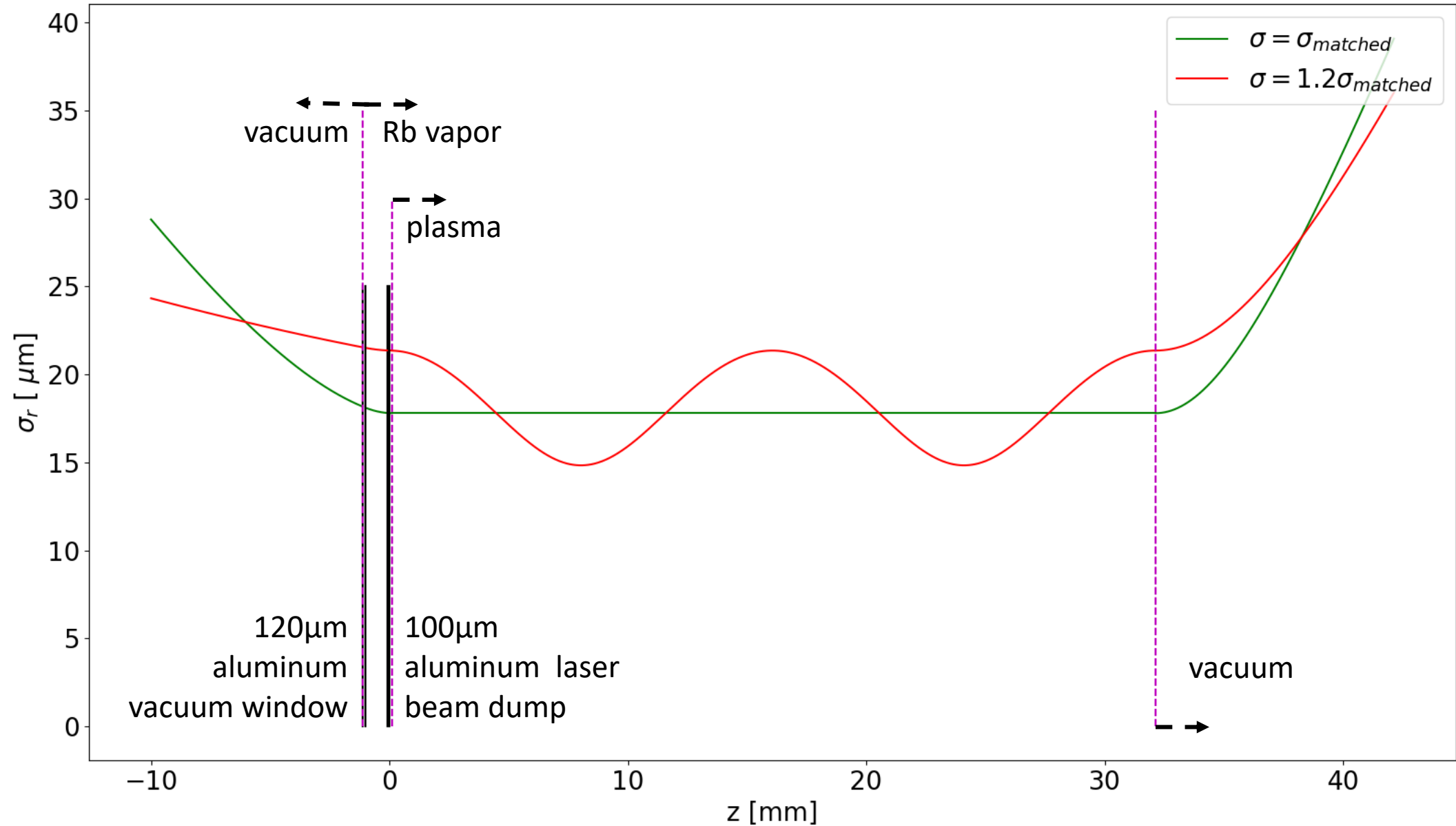
Foils increase emittance and shorten beta function  
→ calculate backwards the incoming parameters



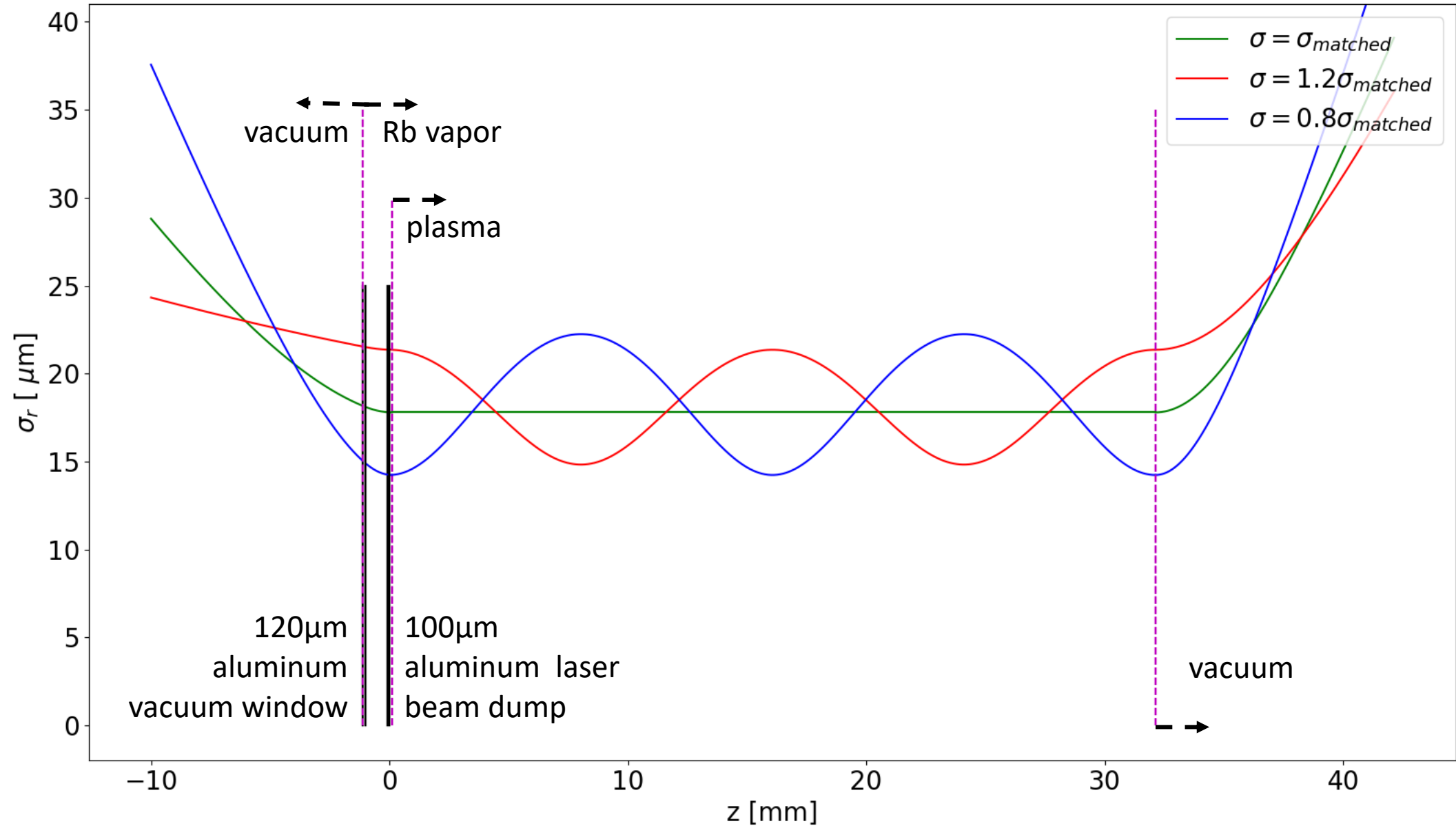
for  $E = 165 \text{ MeV}$  and  $n_e = 7\text{E}+14 \text{ cm}^{-3}$ ,  $\beta_0 = 5.1 \text{ mm}$



for  $E = 165 \text{ MeV}$  and  $n_e = 7\text{E}+14 \text{ cm}^{-3}$ ,  $\beta_0 = 5.1 \text{ mm}$



for  $E = 165 \text{ MeV}$  and  $n_e = 7E+14 \text{ cm}^{-3}$ ,  $\beta_0 = 5.1 \text{ mm}$



# Next:

- How do we include energy spread in matching?
- What if we don't inject exactly at the waist?
- How do we check we are (not) matched, looking at the accelerated beam?
- How do we measure the incoming beam parameters?

**Stay tuned!**