

Space-time Colour Reconnection in Herwig 7

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in collaboration with J. Bellm, C. Duncan, S. Gieseke, M. Myska
based on EPJC 79 (2019) no.12, 1003.



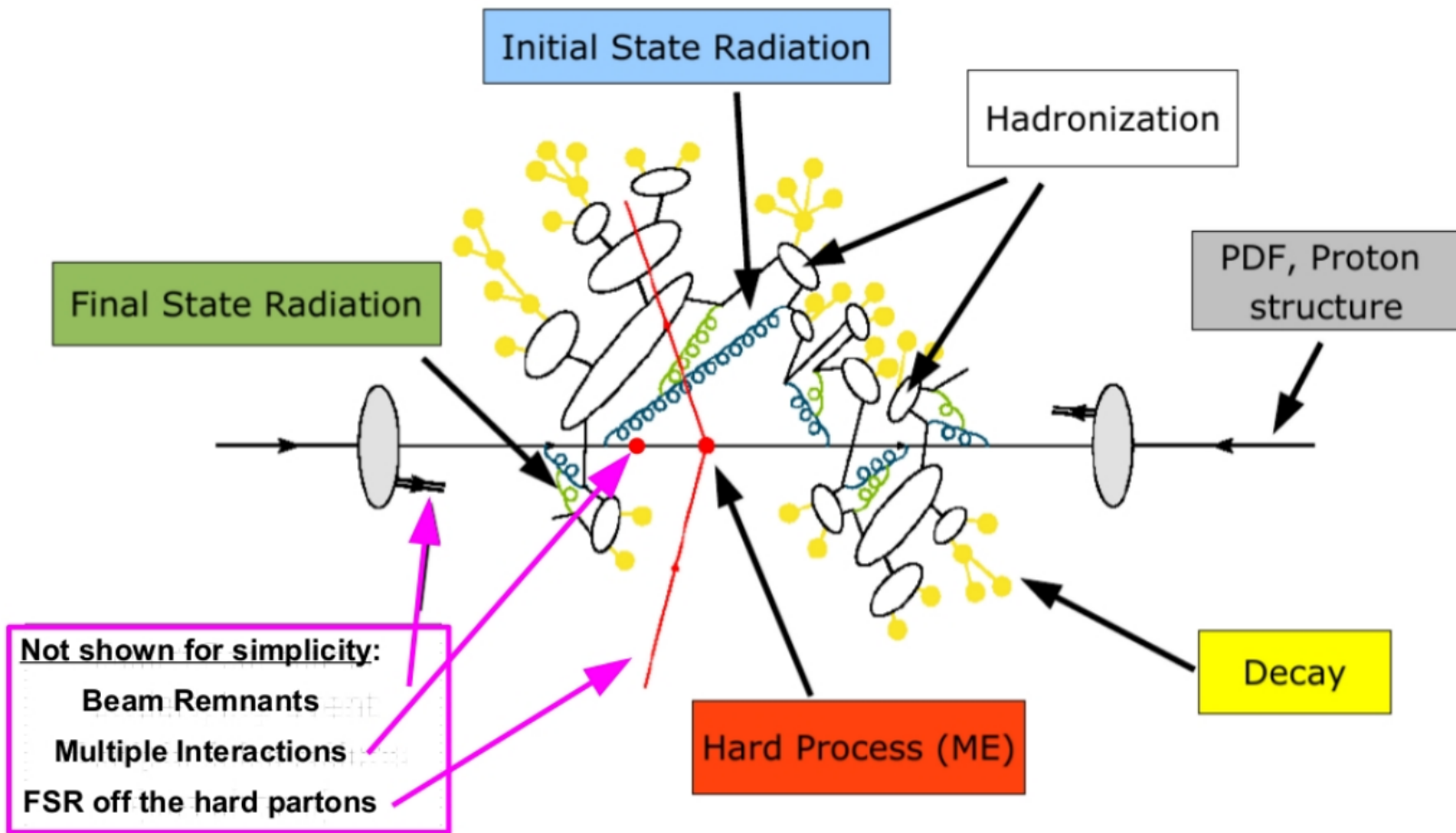
THE HENRYK NIEWODNICZAŃSKI
INSTITUTE OF NUCLEAR PHYSICS
POLISH ACADEMY OF SCIENCES



PARTICLEFACE 2020, 11 February 2020, Cracow

1. Motivation and introduction
2. Space time position of Multi-Parton Interactions (MPI)
3. Space time position from Parton Shower evolution
4. Colour reconnection based on space-time information
5. Numerical results
6. Summary and outlook

Motivation - Monte Carlo Event Generators



taken from Stefan Gieseke[©]

The general approach is the same in different programs but the models and approximations used are different.

Motivation. How do we know MPI exists?

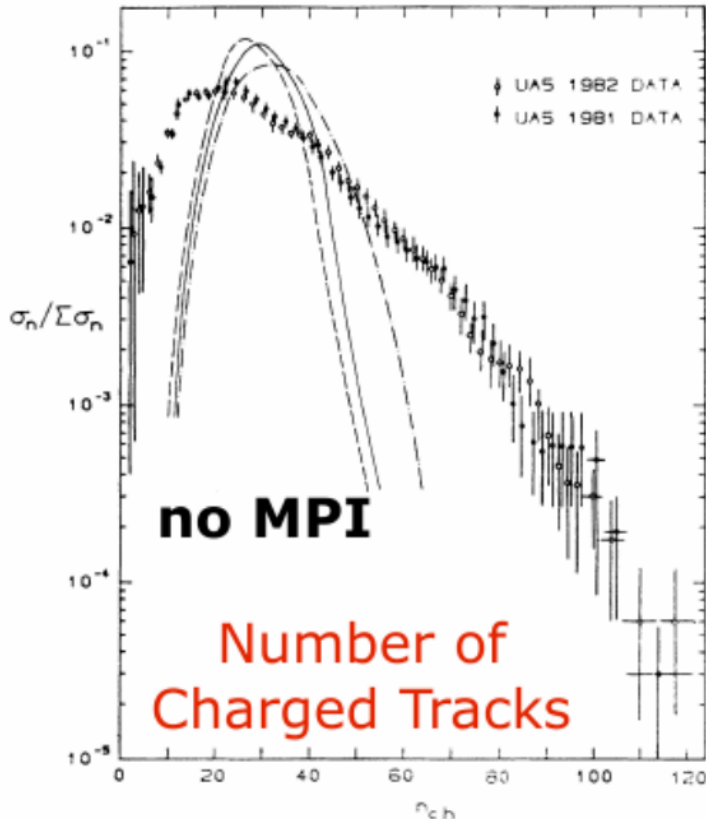


FIG. 3. Charged-multiplicity distribution at 540 GeV, UA5 results (Ref. 32) vs simple models: dashed low p_T only, full including hard scatterings, dash-dotted also including initial- and final-state radiation.

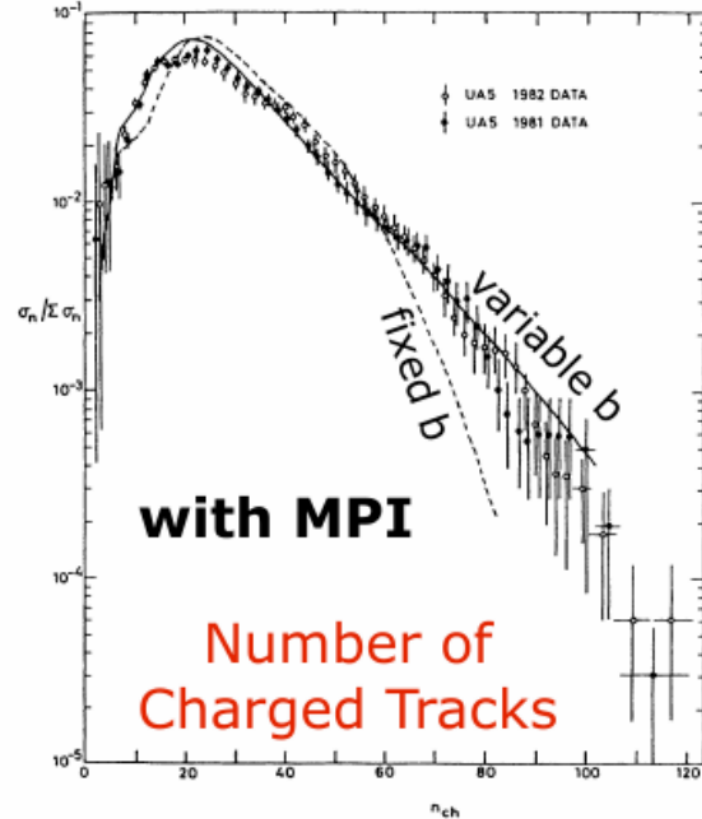
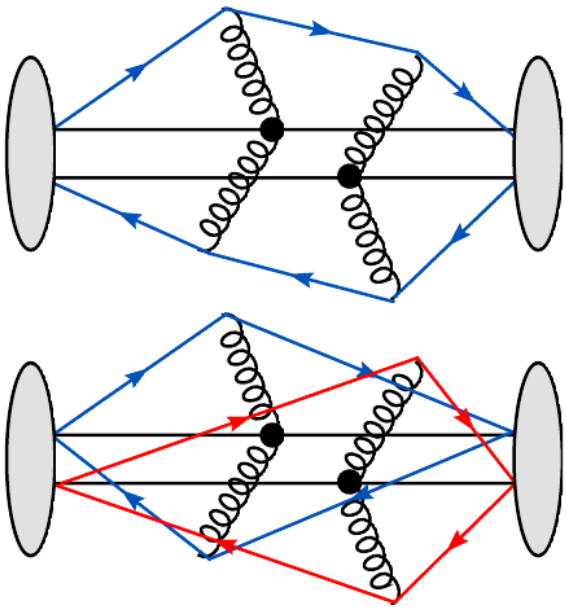


FIG. 12. Charged-multiplicity distribution at 540 GeV, UA5 results (Ref. 32) vs multiple-interaction model with variable impact parameter: solid line, double-Gaussian matter distribution; dashed line, with fix impact parameter [i.e., $\bar{O}_0(b)$].

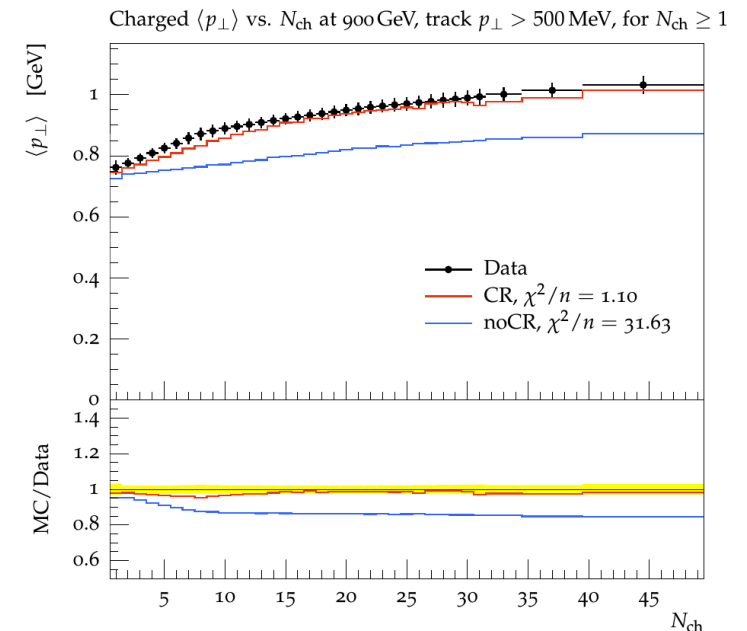
Sjöstrand & v. Zijl,
Phys.Rev.D36(1987)2019

Motivation. Is it really important?

- Better control of perturbative corrections (“**NLO revolution**”) → more often LHC measurements are limited by non-perturbative components (hadronization or multiparton interactions):
 - W mass measurement using a new method [Freytsis et al. JHEP 1902 (2019) 003]
 - extraction of the strong coupling in [M. Johnson, D. Maître, Phys.Rev. D97 (2018) no.5, 054013].
 - the top mass [S. Argyropoulos, T. Sjöstrand, JHEP 1411 (2014) 043] precision dominated by so called **colour reconnection**.
- **Colour reconnection** – the least understood component of MPI models



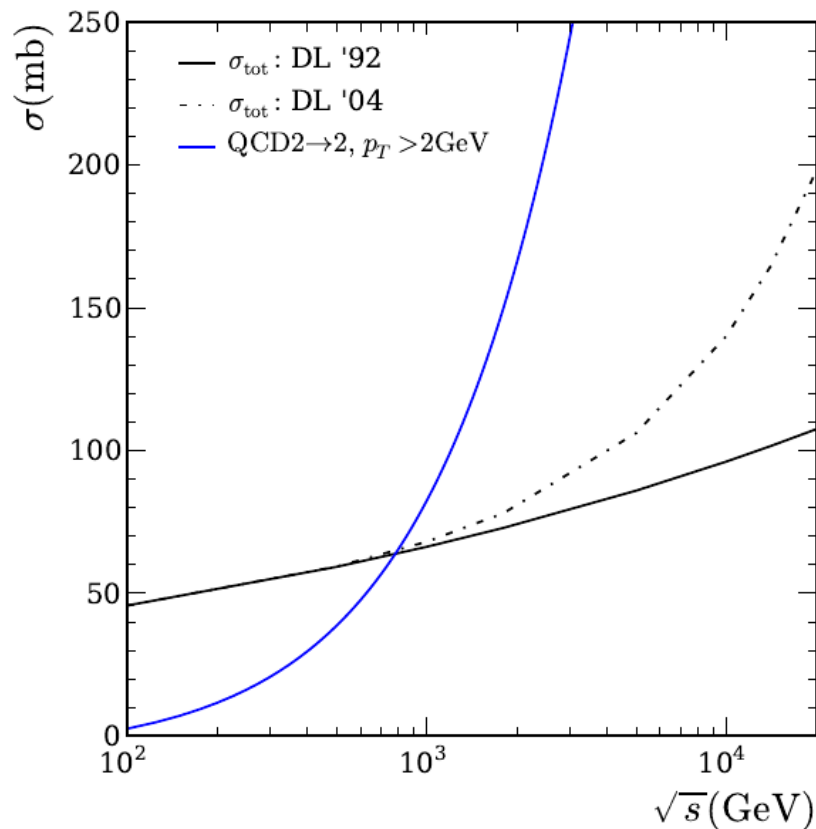
required by data



MPI models in Monte Carlo Event Generators

Inclusive hard jet cross section in pQCD:

$$\sigma^{\text{inc}}(s, p_t^{\text{min}}) = \sum_{i,j} \int_{p_t^{\text{min}^2}^2} dp_t^2 \int dx_1 dx_2 f_i(x_1, Q^2) f_j(x_2, Q^2) \frac{d\hat{\sigma}_{ij}}{dp_t^2}$$



$\sigma^{\text{inc}} > \sigma_{\text{tot}}$ eventually

Interpretation:

- ▶ σ^{inc} counts **all** partonic scatters in a single pp collision
- ▶ more than a single interaction

$$\sigma^{\text{inc}} = \langle n_{\text{dijets}} \rangle \sigma_{\text{inel}}$$

Assumptions:

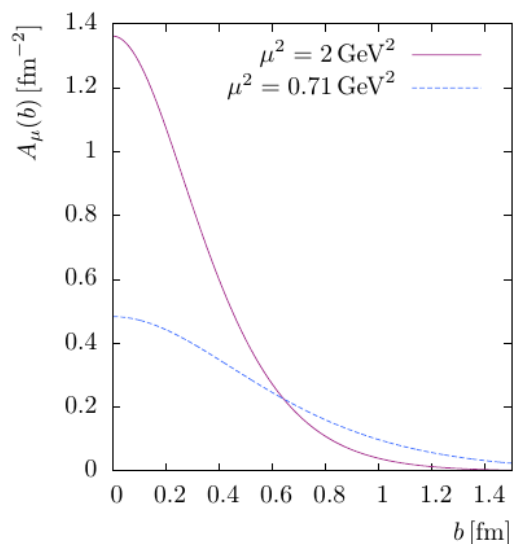
- ▶ the distribution of partons in hadrons factorizes with respect to the b and x dependence \Rightarrow average number of parton collisions:

$$\begin{aligned}
 \bar{n}(\vec{b}, s) &= L_{\text{partons}}(x_1, x_2, \vec{b}) \otimes \sum_{ij} \int dp_t^2 \frac{d\hat{\sigma}_{ij}}{dp_t^2} \\
 &= \sum_{ij} \frac{1}{1 + \delta_{ij}} \int dx_1 dx_2 \int d^2\vec{b}' \int dp_t^2 \frac{d\hat{\sigma}_{ij}}{dp_t^2} \\
 &\quad \times D_{i/A}(x_1, p_t^2, |\vec{b}'|) D_{j/B}(x_2, p_t^2, |\vec{b} - \vec{b}'|) \\
 &= \sum_{ij} \frac{1}{1 + \delta_{ij}} \int dx_1 dx_2 \int d^2\vec{b}' \int dp_t^2 \frac{d\hat{\sigma}_{ij}}{dp_t^2} \\
 &\quad \times f_{i/A}(x_1, p_t^2) G_A(|\vec{b}'|) f_{j/B}(x_2, p_t^2) G_B(|\vec{b} - \vec{b}'|) \\
 &= A(\vec{b}) \sigma^{\text{inc}}(s; p_t^{\text{min}}) .
 \end{aligned}$$

- ▶ at fixed impact parameter b , individual scatterings are independent (leads to the Poisson distribution)

MPI model in Herwig 7 – key components

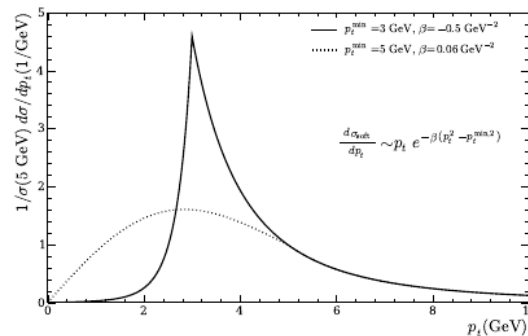
Matter distribution (μ^2)



Based on electromagnetic form factor
(radius of the proton free parameter)

Extension to soft MPI

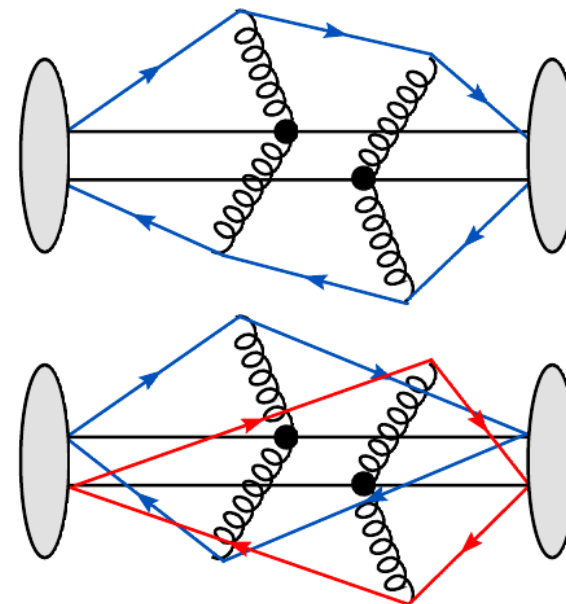
($p_t < p_t^{\min}$)



Gaussian extension below p_t^{\min}

Energy dependent p_t^{\min}

Colour structure

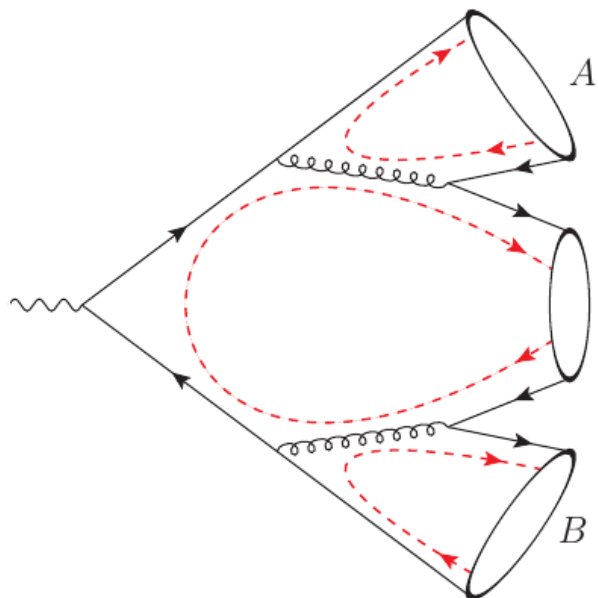


Possibility of change of color structure
(color reconnection)

Main parameters:

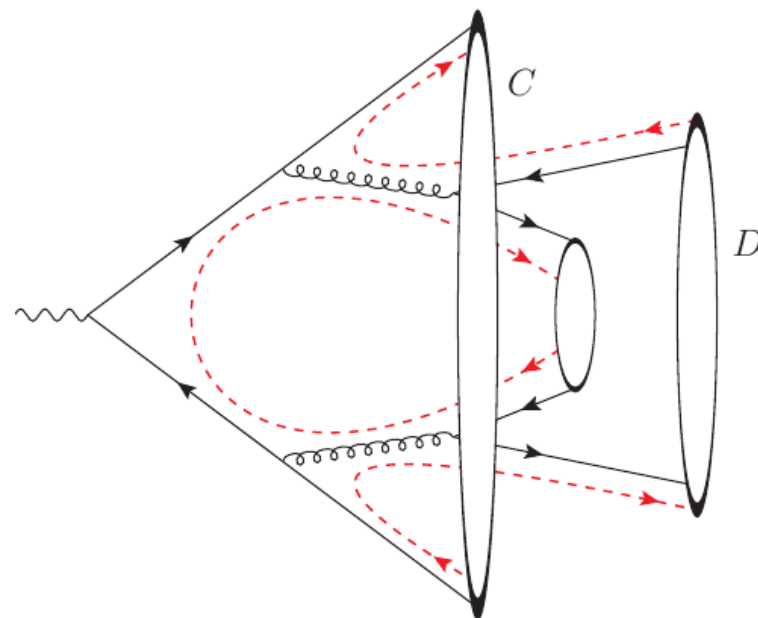
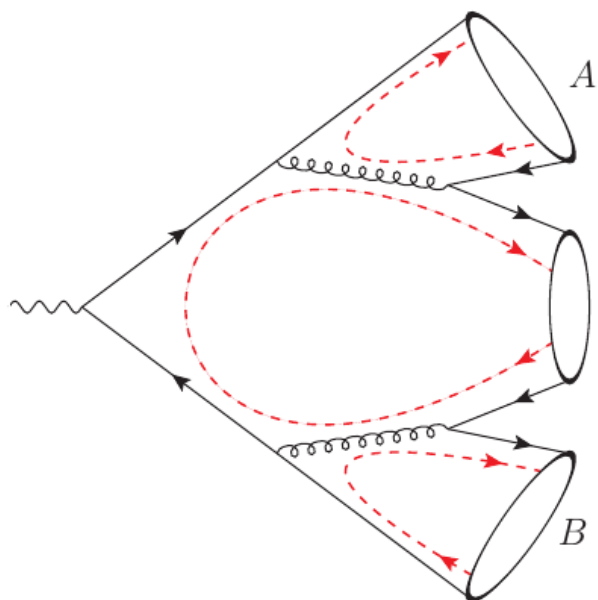
- ▶ μ^2 - inverse hadron radius squared (parametrization of overlap function)
- ▶ p_t^{\min} - transition scale between soft and hard components $\Rightarrow p_t^{\min} = p_{t,0}^{\min} \left(\frac{\sqrt{s}}{E_0}\right)^b$
- ▶ p_{reco} - colour reconnection

Cluster hadronization [Webber, Nucl. Phys. B238 (1984) 492]



- ▶ perturbative QCD provides *preconfinement* [Amati, Veneziano, Phys. Lett. B83 (1979) 87]
- ▶ colour-singlet pairs end up close in phase space and form highly excited hadronic states, the *clusters*

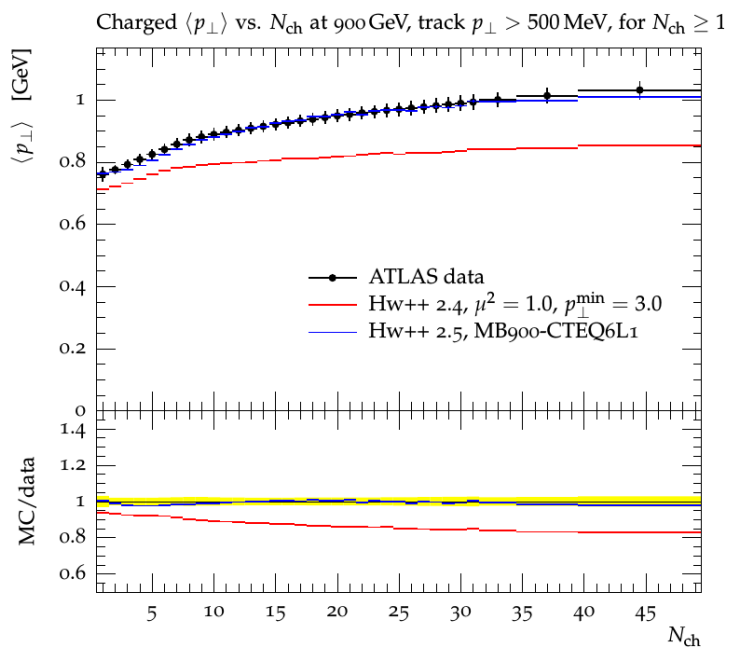
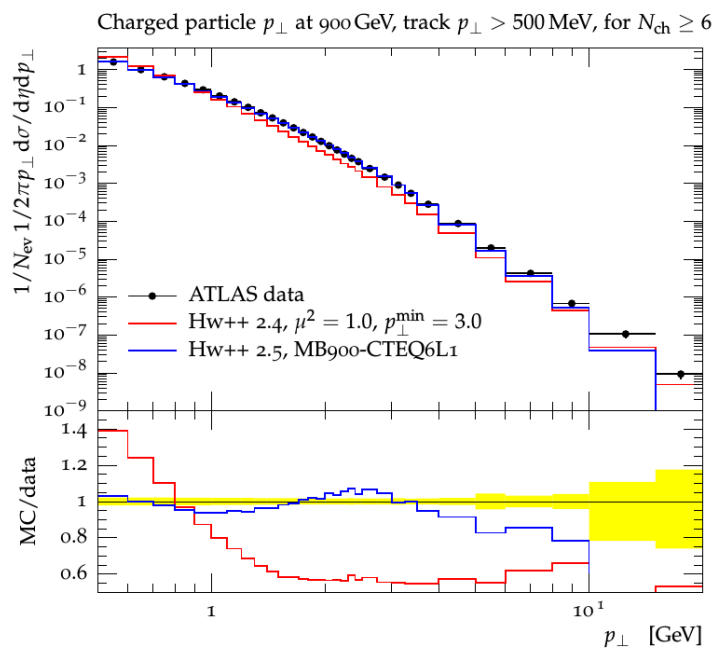
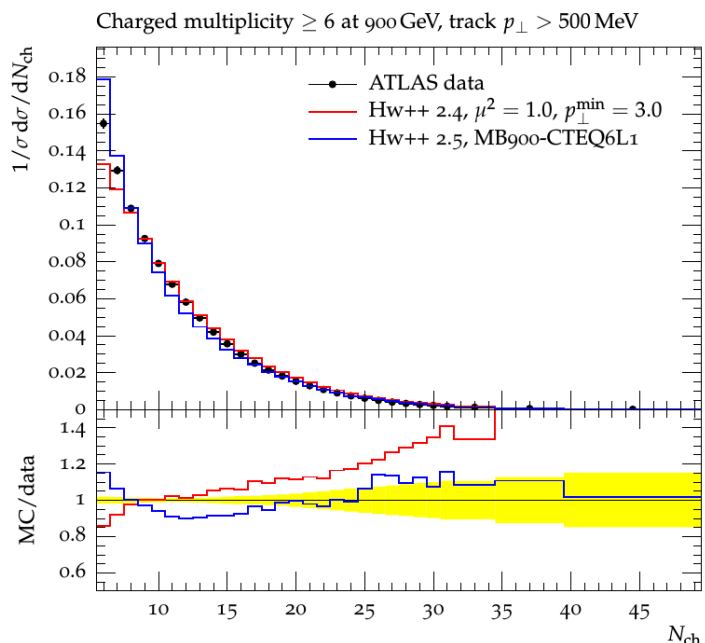
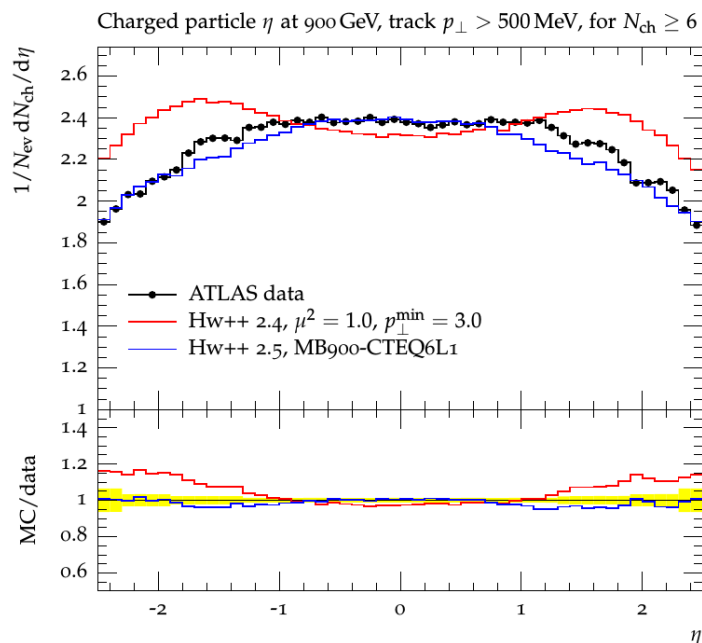
Cluster hadronization [Webber, Nucl. Phys. B238 (1984) 492]



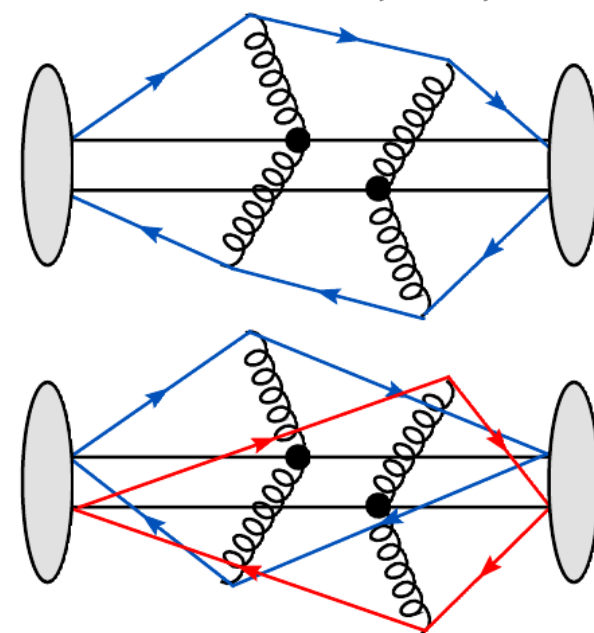
- ▶ perturbative QCD provides *preconfinement* [Amati, Veneziano, Phys. Lett. B83 (1979) 87]
- ▶ colour-singlet pairs end up close in phase space and form highly excited hadronic states, the *clusters*
- ▶ improved description of soft events/UE at hadron colliders: manually **reduce cluster masses**
- ▶ if $M_C + M_D < M_A + M_B$ accept alternative clustering with probability p_{reco} (model parameter)

[Gieseke, Rohr, AS, EPJC 72, 2012]

Colour Reconnection fitting to LHC data



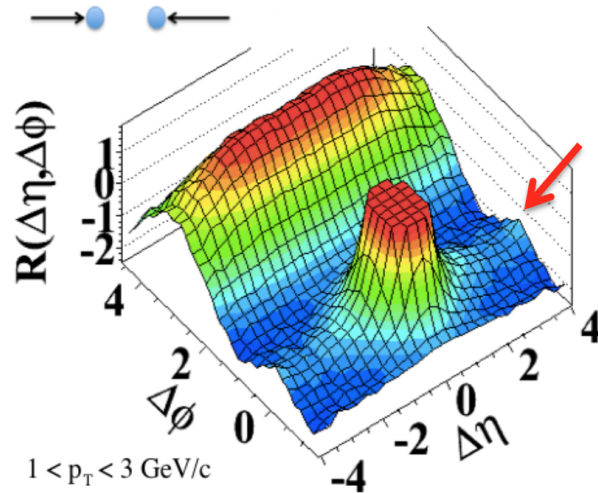
Colour structure (p_{reco} , p_{CD})



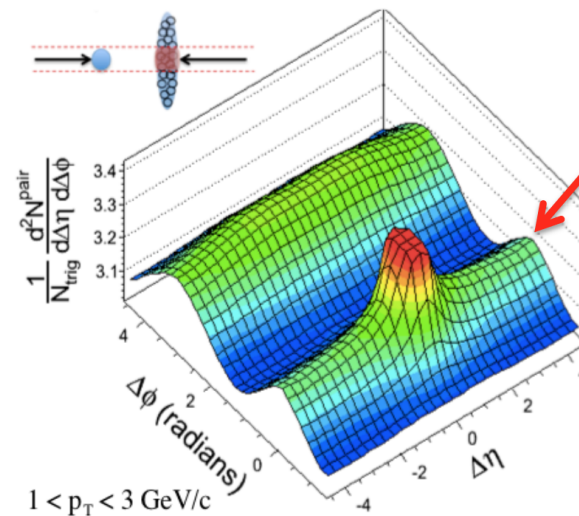
Still many open questions

- Hadronization of very dense systems shows unexpected correlations

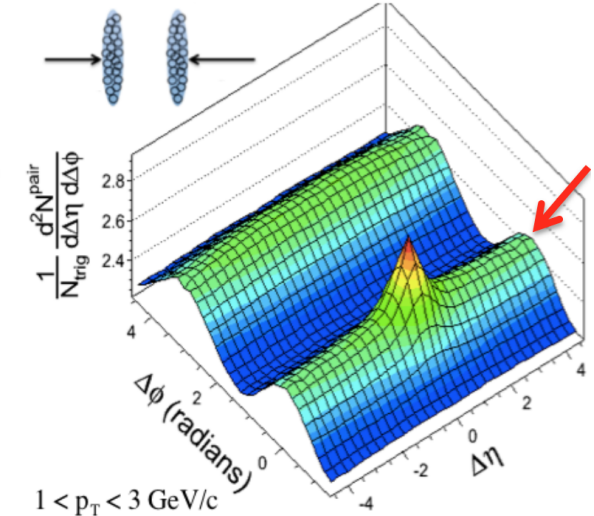
(a) pp $\sqrt{s} = 7$ TeV, $N_{\text{trk}}^{\text{offline}} \geq 110$



(b) pPb $\sqrt{s_{\text{NN}}} = 5.02$ TeV, $220 < N_{\text{trk}}^{\text{offline}} \leq 260$



(c) PbPb $\sqrt{s_{\text{NN}}} = 2.76$ TeV, $220 < N_{\text{trk}}^{\text{offline}} \leq 260$

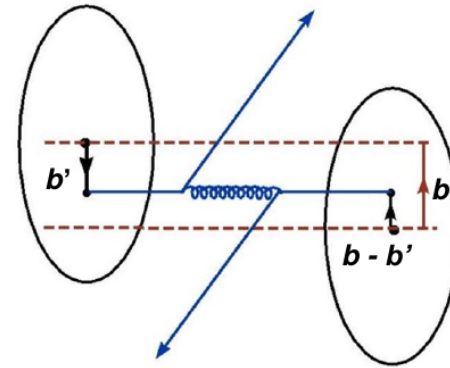


- Can we improve the colour reconnection in Herwig by including space-time information?

Space-time Coordinate of MPI - the impact parameter b

The average number of interactions

$$\bar{n}(b, s) = A(b)\sigma^{inc}(s; p_t^{\min}) = 2\chi(b, s)$$



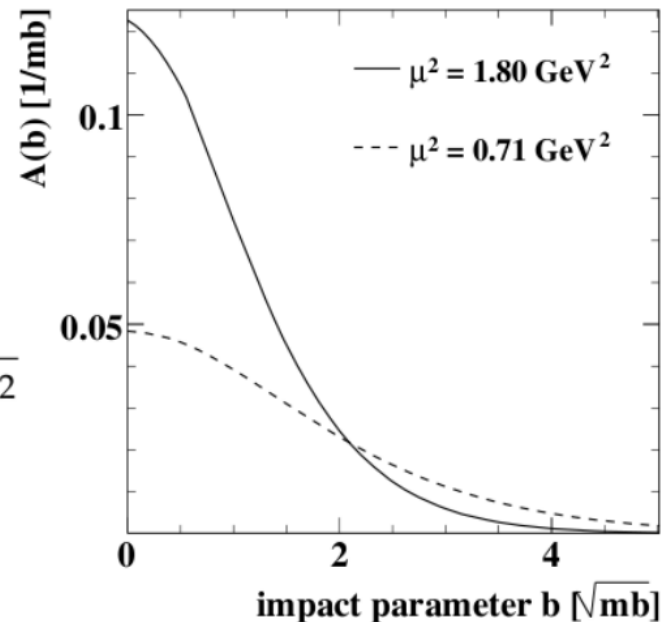
$A(b)$ is the partonic overlap function of the colliding hadrons

$$A(b) = \int d^2\vec{b}' G_A(|\vec{b}'|) G_B(|\vec{b} - \vec{b}'|)$$

$G(\vec{b})$ from electromagnetic FF:

$$G_p(\vec{b}) = G_{\bar{p}}(\vec{b}) = \int \frac{d^2\vec{k}}{(2\pi)^2} \frac{e^{i\vec{k}\cdot\vec{b}}}{(1 + \vec{k}^2/\mu^2)^2}$$

But μ^2 *not fixed* to the
electromagnetic 0.71 GeV^2 .
Free for colour charges.



Extension to soft MPI:

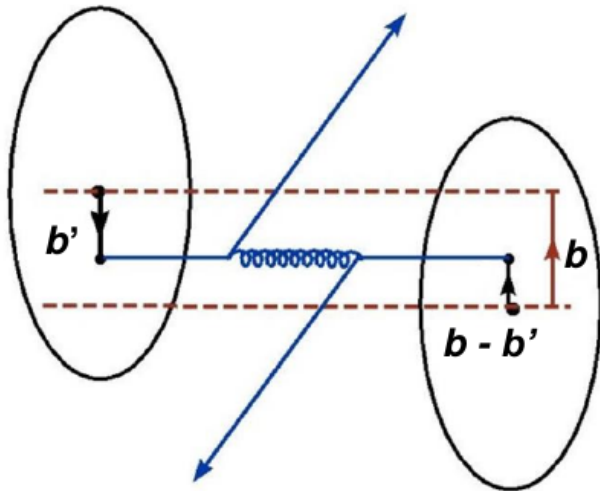
$$\chi_{\text{tot}}(\vec{b}, s) = \frac{1}{2} \left(A(\vec{b}; \mu_{\text{hard}}) \sigma^{\text{inc}}(s; p_t^{\min}) + A(\vec{b}; \mu_{\text{soft}}) \sigma_{\text{soft}}^{\text{inc}} \right) = \chi_h + \chi_k$$

Space-time Coordinate of MPI

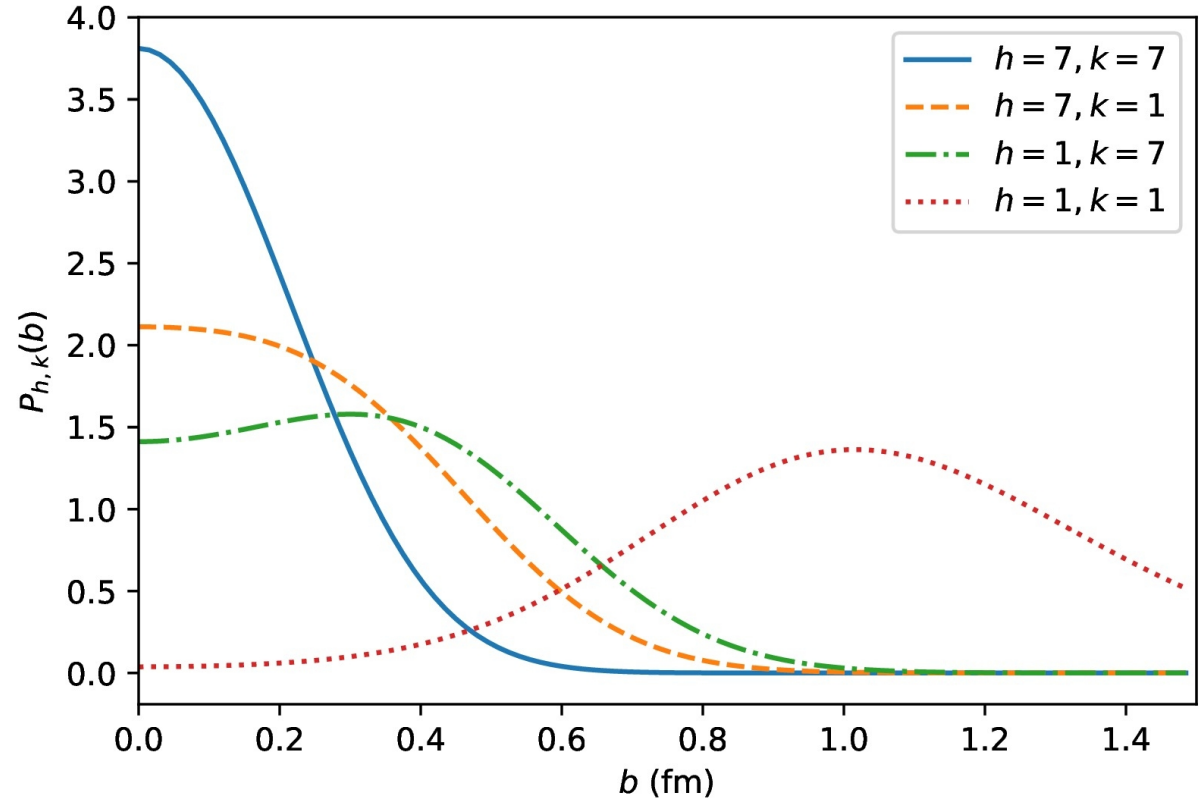
Main assumptions of eikonal MPI model:

- Independent scatter at fix \mathbf{b}

$$\mathcal{P}_{h,k}(b) = \frac{(2\chi_h)^h}{h!} \frac{(2\chi_k)^k}{k!} e^{-2(\chi_h + \chi_k)}$$



Poissonian distribution of MPI as a function of b



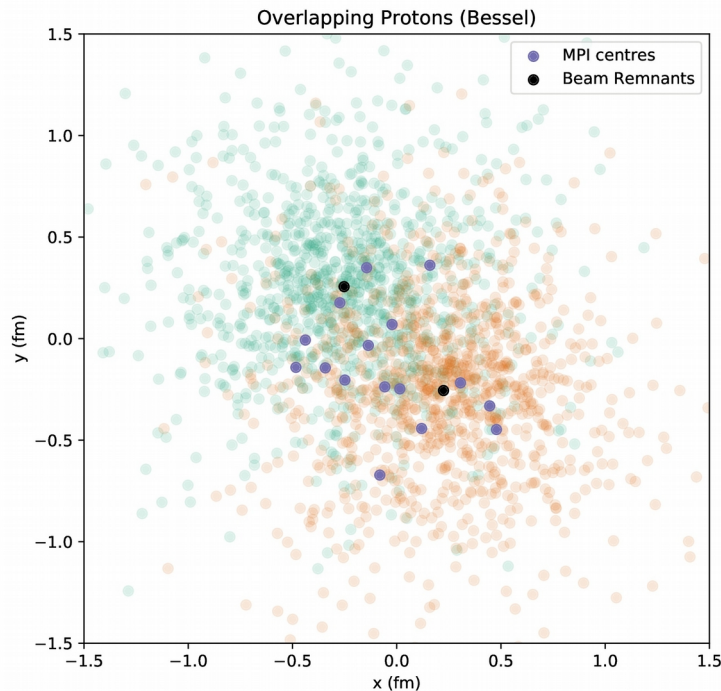
- The more interactions that occur, the more likely the collision is to be central.
- Keeping the number of interactions fixed (h) but having more soft interactions (k) makes the distribution have a broader tail.

Space-time Coordinate of MPI centres

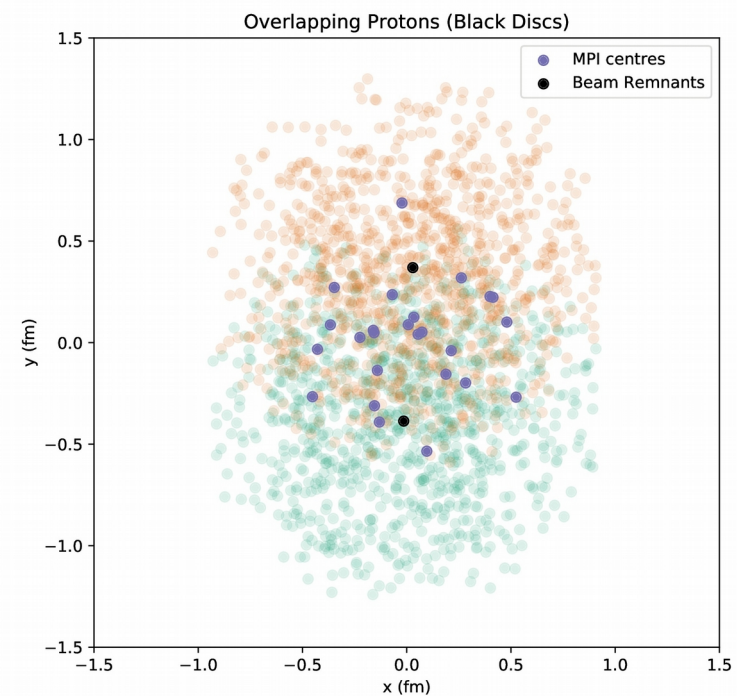
- After b is determined the overlap function governs the density of MPI scattering centres in the transverse plane.

$$A(b) = \int d^2b' G(b') G(b - b')$$

Electromagnetic Form Factor



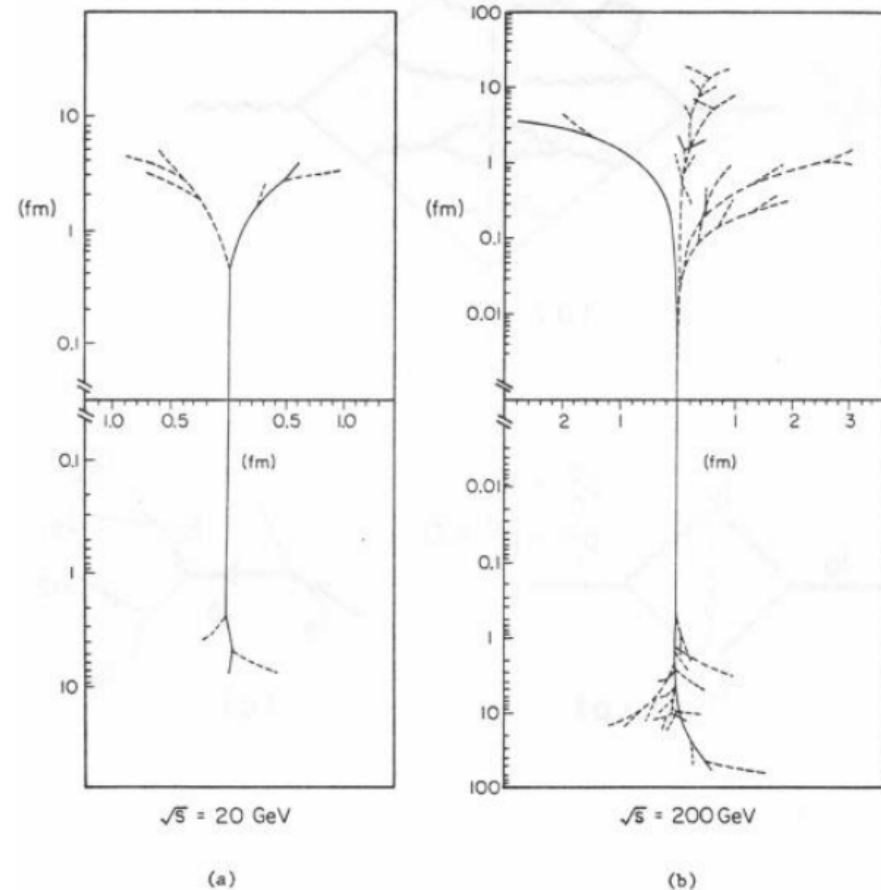
Black Disk



- Soft and hard interactions have different $A(b)$ hard scatters are slightly more concentrated in the centre, while soft scatters have a longer tail.
- The beam remnants receive the proton positions.
- Once these points have been generated, all coordinates get the same random global rotation in the transverse plane.

Space-time Coordinate of Parton Shower in Herwig 7

SPACETIME DEVELOPMENT OF TYPICAL PARTON SHOWERS $\sqrt{s_c} = 1 \text{ GeV}$



G. C. Fox, S. Wolfram,
A Model for Parton Showers in QCD
Nucl. Phys. B168 (1980) 285

Herwig 7

- FortranHerwig-like algorithm
[G. Corcella et al., JHEP 0101 \(2001\) 010, chapter 3.8](#)
- The mean lifetime τ of a parton in its own rest frame (similar as for particles decays)

$$\tau(q^2) = \frac{\hbar\sqrt{q^2}}{\sqrt{(q^2 - M^2)^2 + \left(\frac{\Gamma q^2}{M}\right)^2}},$$

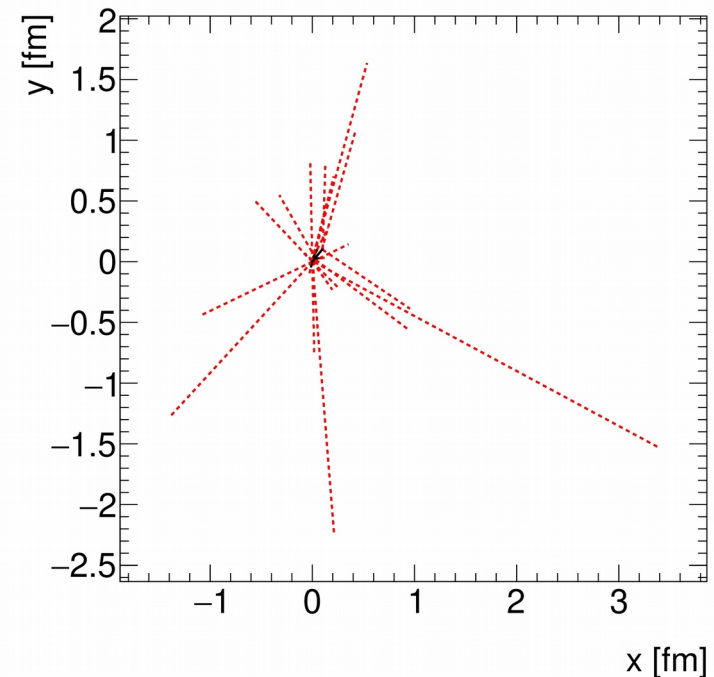
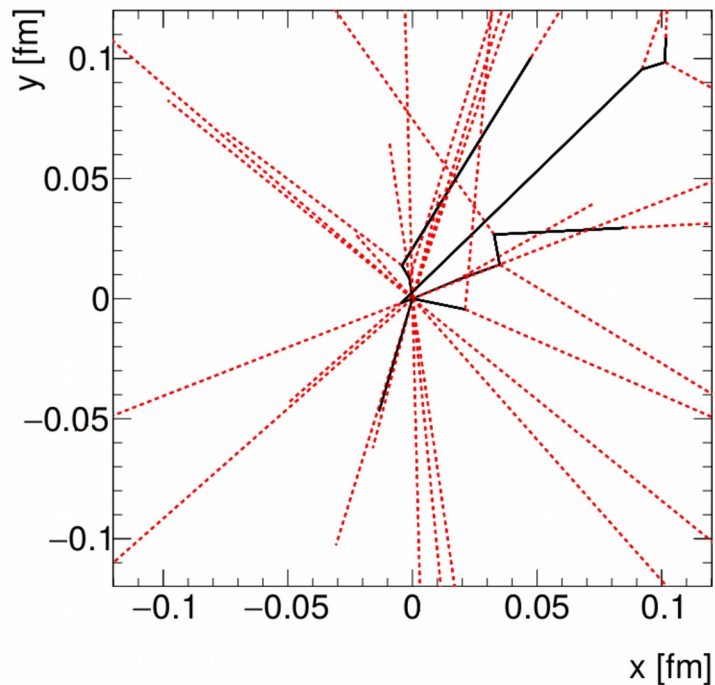
- rest-frame decay time t^*

$$P_{\text{decay}} = 1 - \exp\left(-\frac{t^*}{\tau}\right).$$

- Distance travelled in the lab-frame

$$t = \gamma t^*, \vec{d} = \vec{\beta} \gamma t^*$$

Space-time Coordinate of Parton Shower



- Fermi-scale parton shower effects
- Most distance traveled by the last step of the parton shower evolution (red lines)
- We will only give coordinates to the partons that remain at the end of the shower
- To avoid unphysically large distances traveled by partons with very small virtualities we introduce a minimum virtuality ν^2 (free parameter of the model), so the mean lifetime:

$$\tau_{0,p} = \frac{\hbar m_p}{\nu^2}.$$

- We do not consider z, t directions

Spacetime Colour Reconnection

- With the transverse coordinates in place, we use this information to perform and inform CR
- We introduce a boost-invariant distance measure:

$$R_{ij}^2 = \frac{\Delta r_{ij}^2}{d_0^2} + \Delta y_{ij}^2, \text{ where } \Delta r_{ij}^2 = (\vec{x}_{\perp,i} - \vec{x}_{\perp,j})^2$$

d_0 is the characteristic length scale for CR, a tunable parameter

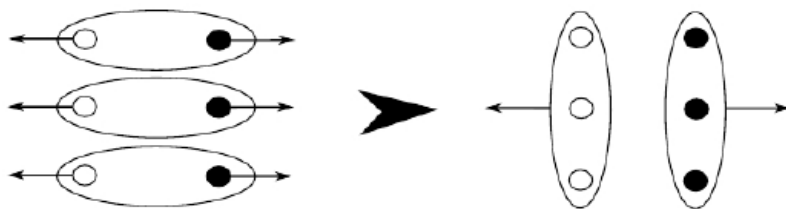
- This is inspired by conventional jet algorithms, where we replace the azimuthal separation with transverse separation.
- We use similar strategy as in the simple plain CR base on the cluster mass measure.
- If the sum of the cluster separations is smaller after a possible reconnection:

$$R_{q'} + R_{q''} < R_q + R_{q''}$$

then we accept the reconnection with a probability p_{reco}

- Baryonic spacetime colour reconnection uses the algorithm from

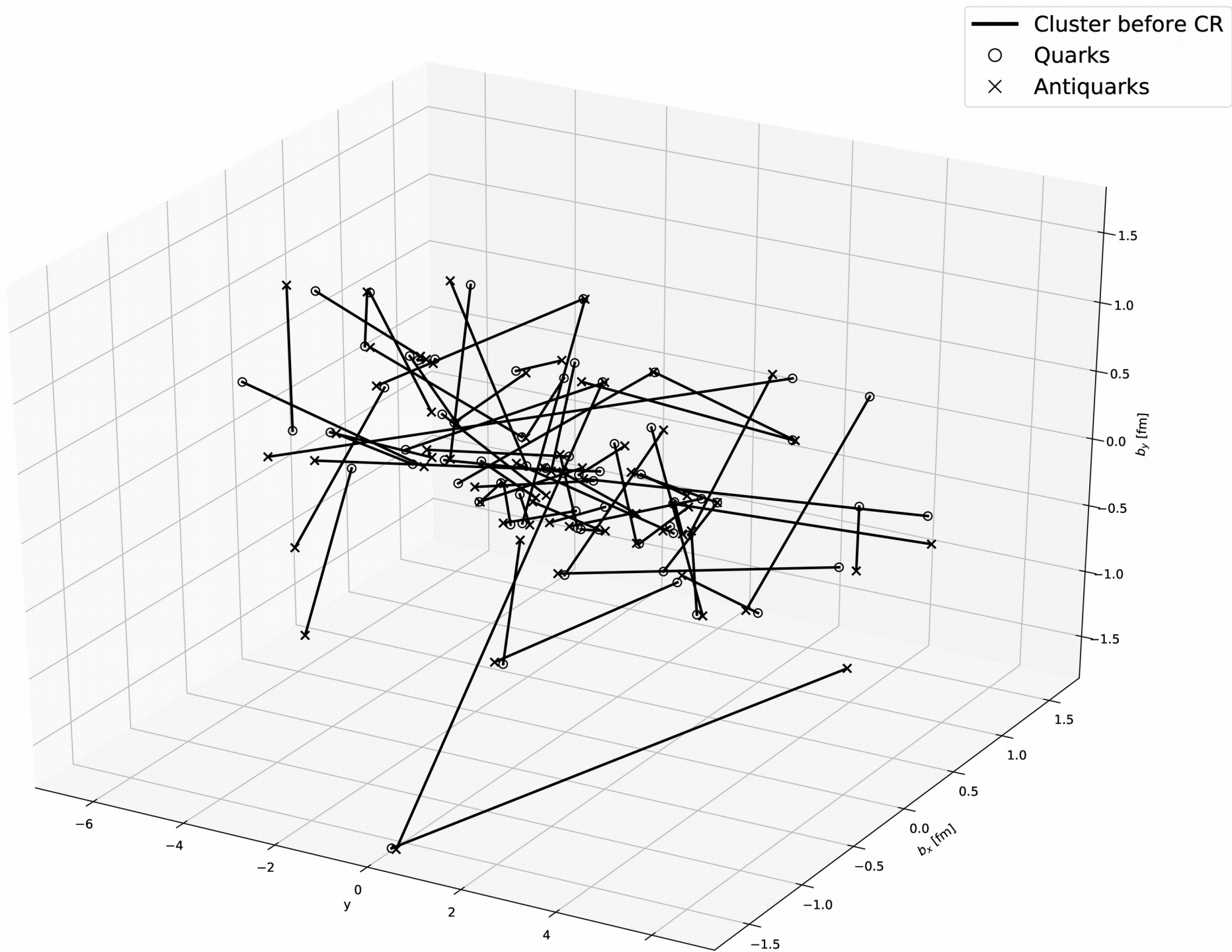
[S. Gieseke, P. Kirchga e er, S. Pl atzer Eur.Phys.J. C78 (2018)]



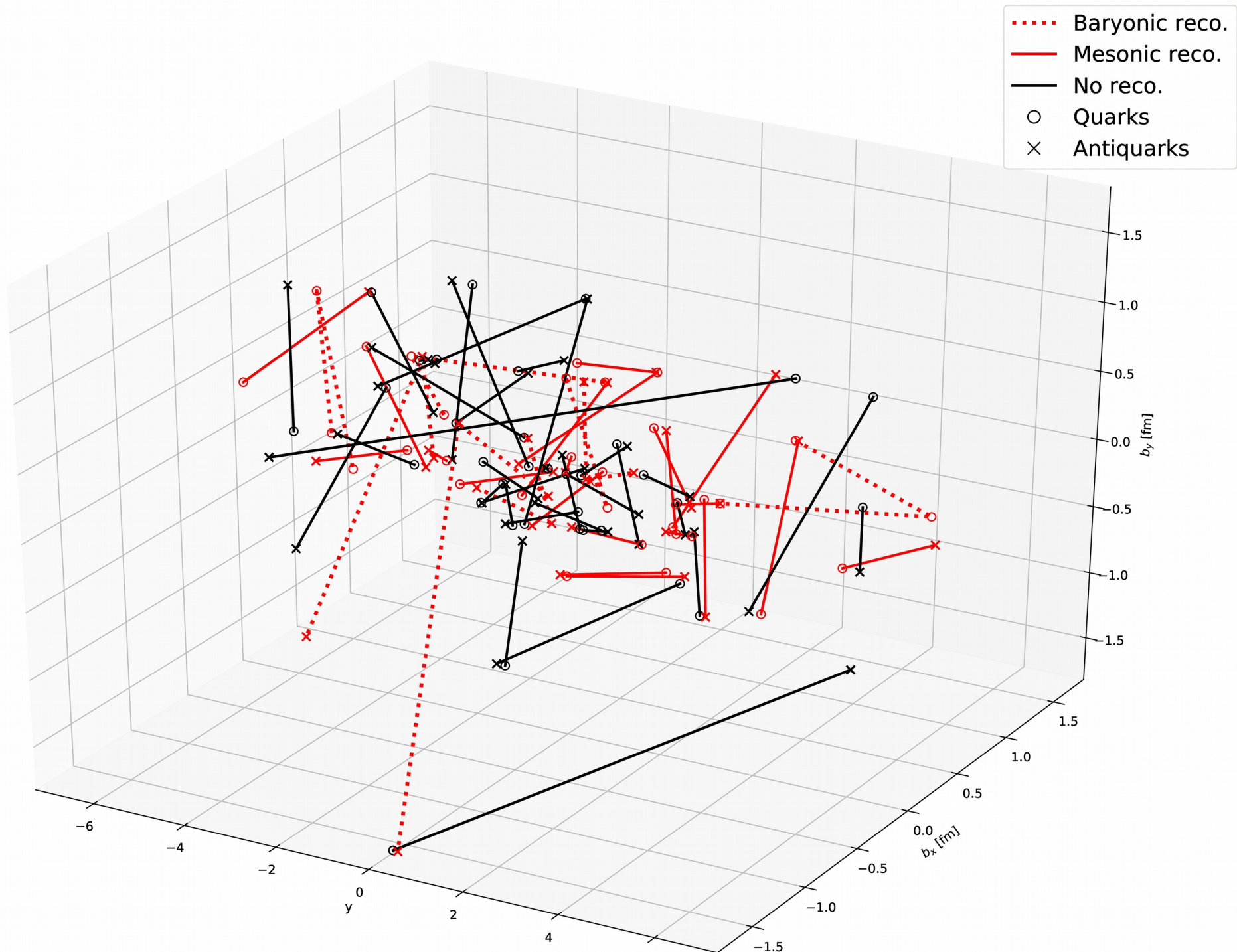
$$R_{q,qq} + R_{\bar{q},\bar{q}\bar{q}} < R_{q,\bar{q}} + R_{qq,\bar{q}\bar{q}}$$

[See Stefan's talk for more models and details]

Spacetime Colour Reconnection – Numerical results



Spacetime Colour Reconnection – Numerical results



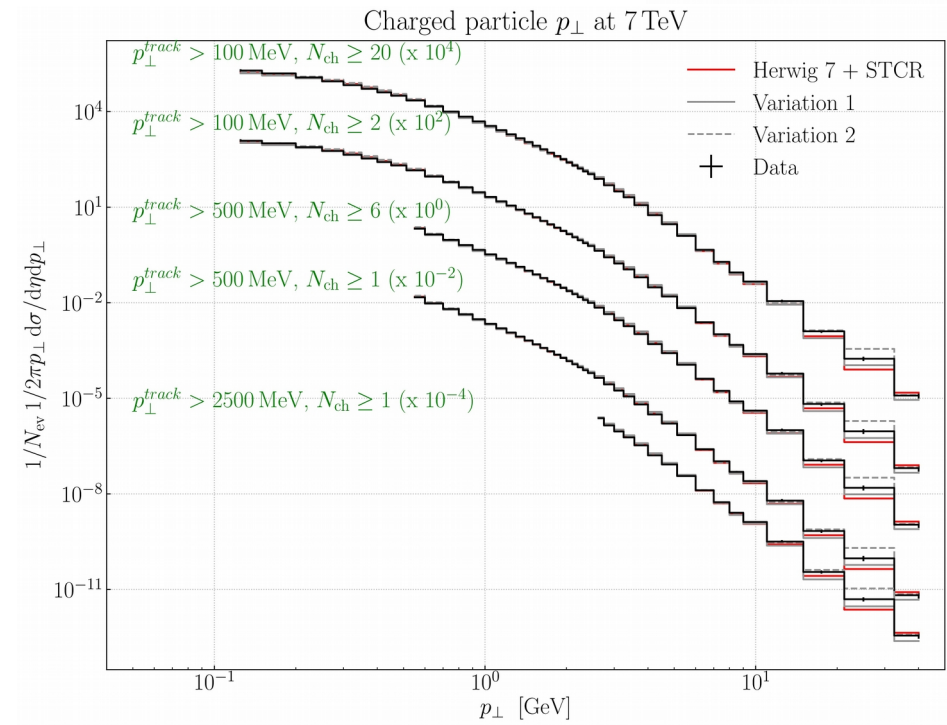
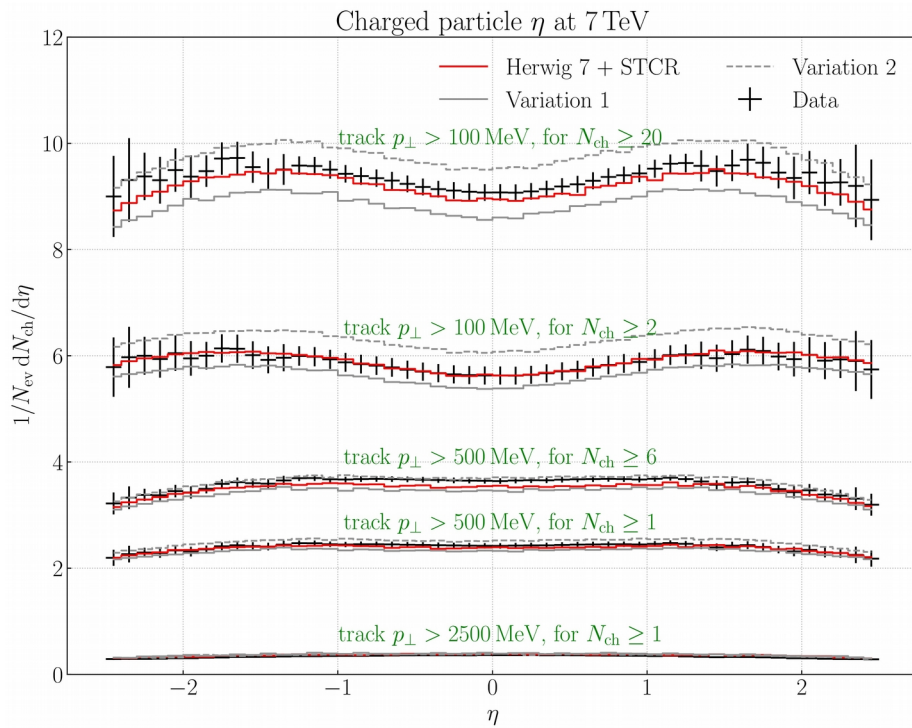
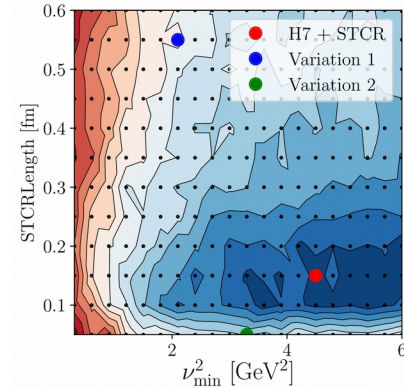
Good agreement with Minimum Bias data

Tuning using autotunes [J. Bellm and L. Gellersen arXiv:1908.10811]

Best tune: $\nu^2 = 4.5 \text{ GeV}^2$, $d_0 = 0.15 \text{ fm}$

Variation 1: $\nu^2 = 3.3 \text{ GeV}^2$, $d_0 = 0.05 \text{ fm}$

Variation 2: $\nu^2 = 2.1 \text{ GeV}^2$, $d_0 = 0.55 \text{ fm}$



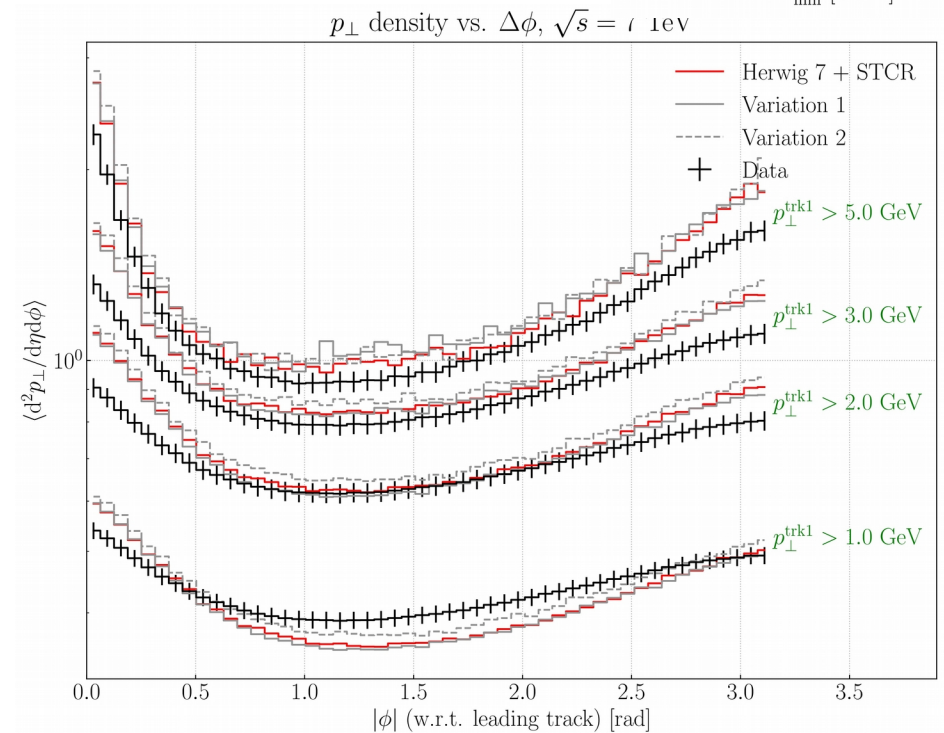
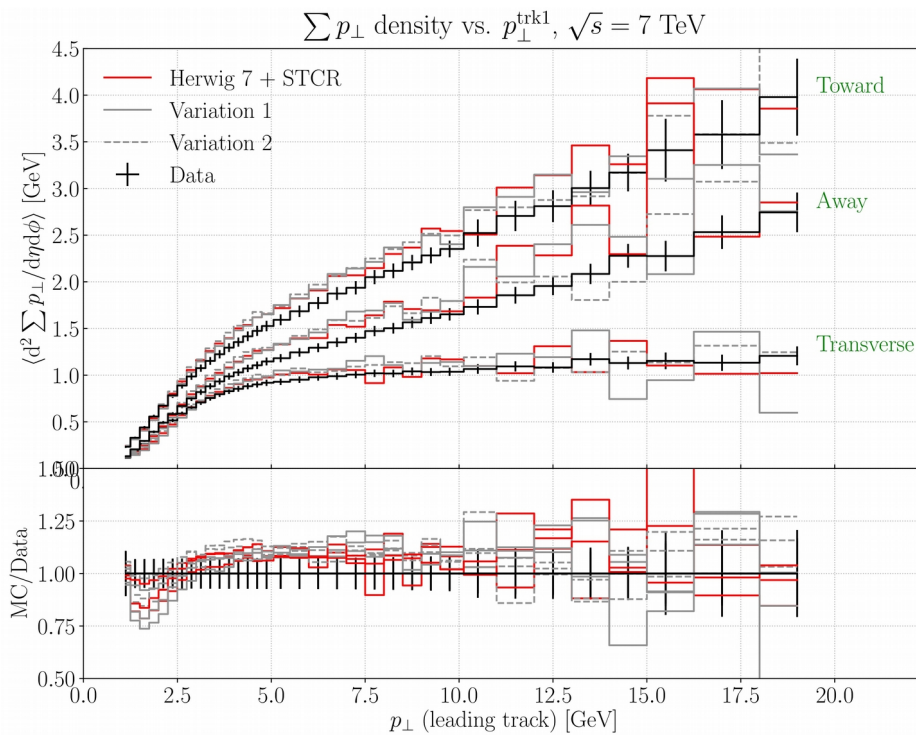
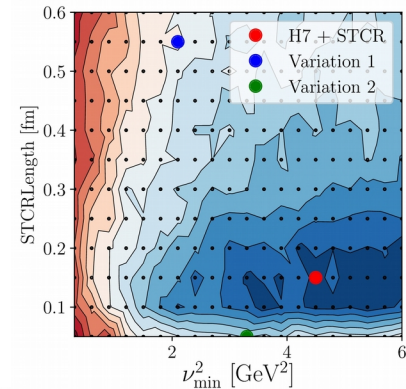
Good agreement with Underlying Event data

Tuning using autotunes [J. Bellm and L. Gellersen arXiv:1908.10811]

Best tune: $\nu^2 = 4.5 \text{ GeV}^2$, $d_0 = 0.15 \text{ fm}$

Variation 1: $\nu^2 = 3.3 \text{ GeV}^2$, $d_0 = 0.05 \text{ fm}$

Variation 2: $\nu^2 = 2.1 \text{ GeV}^2$, $d_0 = 0.55 \text{ fm}$








Summary and Outlook

- We present a model for generating spacetime coordinates in the Monte Carlo Herwig 7
- Then we introduced a colour reconnection model by minimizing a boost-invariant distance measure of the system.
- We compare the model to a series of soft physics observables. We find reasonable agreement with the data.
- This suggests that pp-collider colour reconnection may be able to be applied in larger systems.

More information about Monte Carlo Event Generators

**2020 CTEQ - MCnet Summer School
on QCD Phenomenology and Monte Carlo Event Generators**

organizers sponsors

    European Commission |  Horizon 2020
European Union Funding
for Research & Innovation 

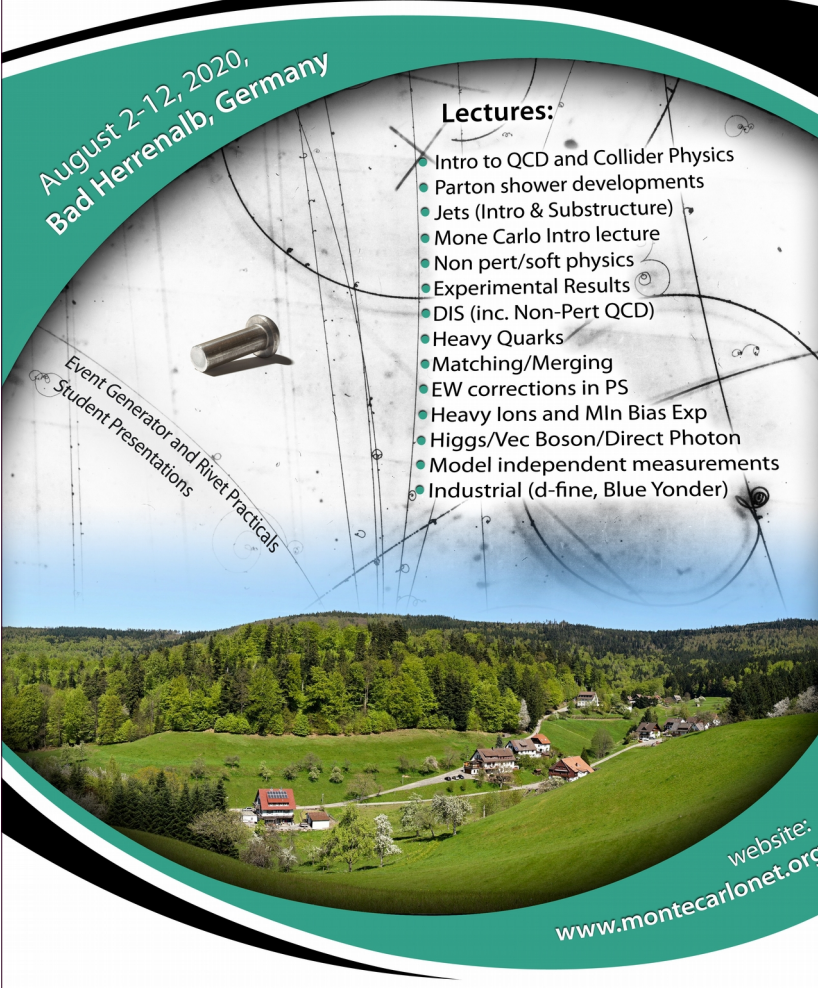
August 2-12, 2020,
Bad Herrenalb, Germany

Lectures:

- Intro to QCD and Collider Physics
- Parton shower developments
- Jets (Intro & Substructure)
- Monte Carlo Intro lecture
- Non pert/soft physics
- Experimental Results
- DIS (inc. Non-Pert QCD)
- Heavy Quarks
- Matching/Merging
- EW corrections in PS
- Heavy Ions and MIn Bias Exp
- Higgs/Vec Boson/Direct Photon
- Model independent measurements
- Industrial (d-fine, Blue Yonder)

Event Generator and Rivet Practicals
Student Presentations

website:
www.montecarlonet.org



Next school will be organized by KIT

Monte Carlo

training studentships



3-6 month fully funded studentships for current PhD students at one of the MCnet nodes. An excellent opportunity to really understand and improve the Monte Carlos you use!

Application rounds every 3 months.

MCnet projects
Pythia+Vincia
Herwig
Sherpa
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“Plugin” – Ariadne+HEJ
CEDAR – Rivet+Professor
+Contur+hepforge+...



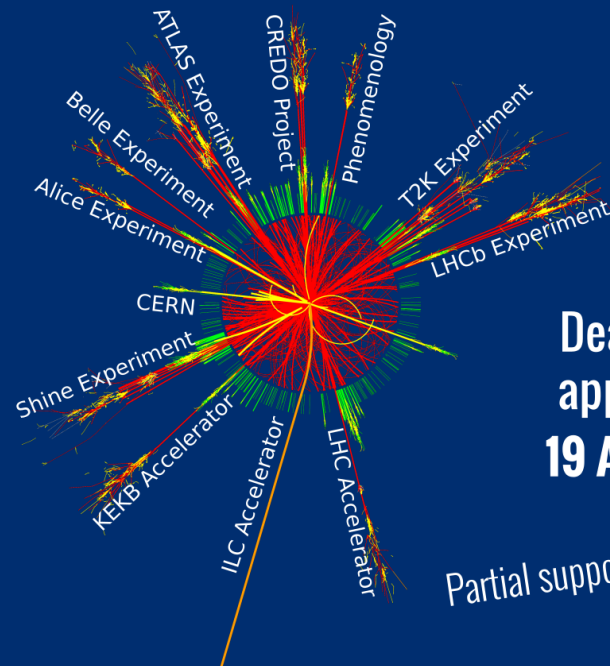
for details go to:
www.montecarlonet.org

Institute of Nuclear Physics Polish Academy of Sciences



particle physics summer student programme

6 – 31 July 2020
Cracow, Poland



**Deadline for
applications
19 April 2020**

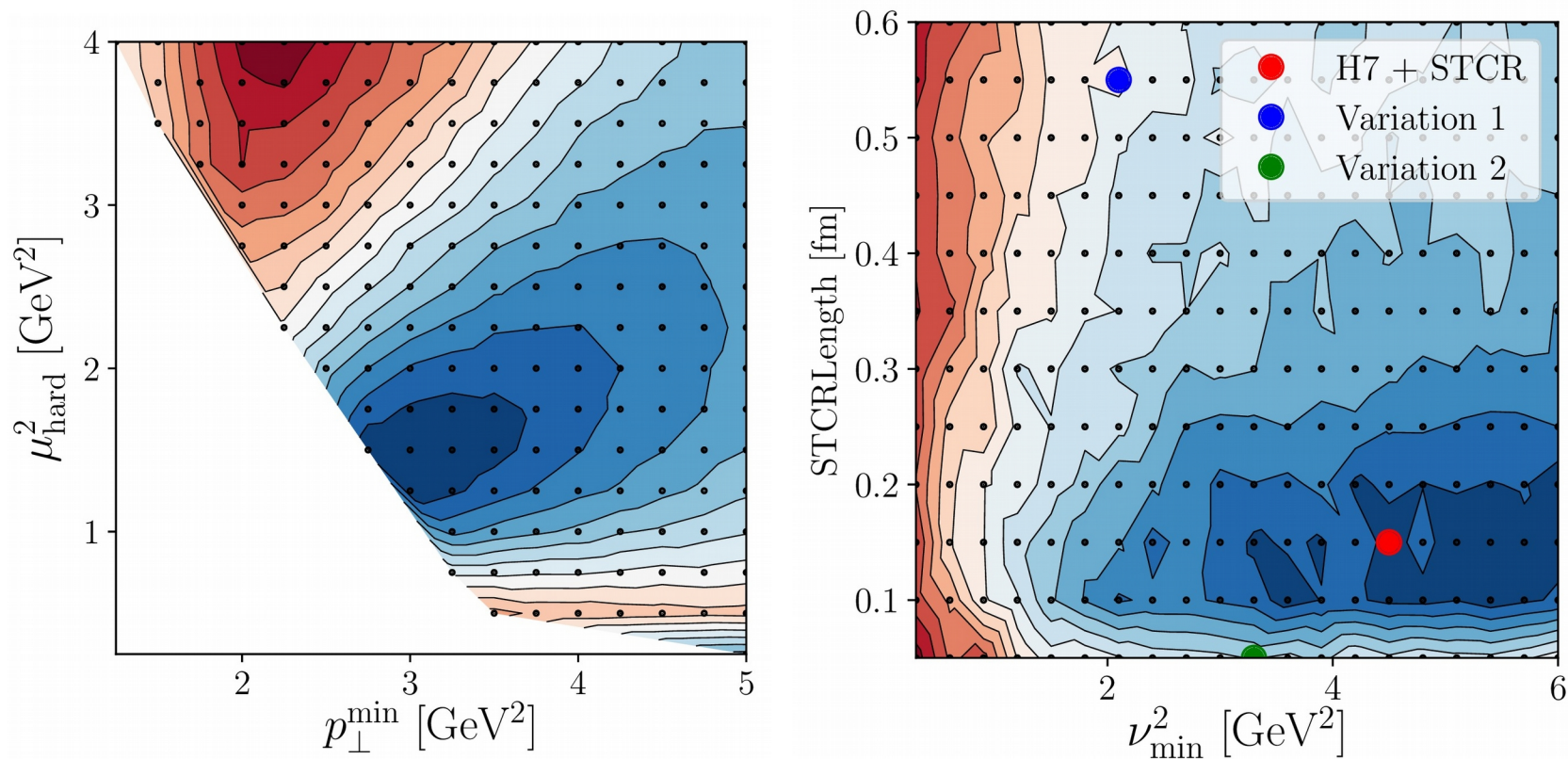
Partial support for best applicants!

Find us on 



More information and application form at
ppss.ifj.edu.pl

Thank you for your attention!



σ_{tot} [mb]	R_{Diff}	p_{\perp}^{min} [GeV]	μ_{hard}^2 [GeV ²]
96.0	0.2	3.0	1.5
ν^2 [GeV ²]	d_0 [fm]	w_b	$(\mu_{\text{soft}}^2 [\text{GeV}^2])$
4.5	0.15	0.98	0.254