



Measurement of the CKM matrix elements $|V_{tb}|$, $|V_{ts}|$,
and $|V_{td}|$ in single top events in proton-proton collisions
at $\sqrt{s} = 13$ TeV
CMS Highlight: LHCTopWG talk

LHCTopWG Open Meeting

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INFN e Università di Napoli

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Overview

- 1 Introduction
- 2 Analysis setup
 - Baseline selection
- 3 Signal extraction
 - Regions definition
 - QCD extraction
- 4 Fit procedure
- 5 Summary

Single top cross section: previous approach

In production

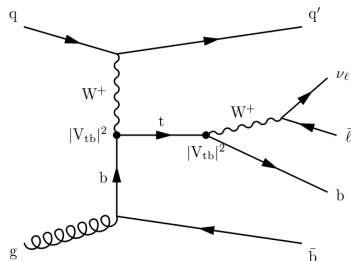
$$\sigma_{t\text{-ch.}} = \sigma_{t\text{-ch.,b}} = \alpha |V_{tb}|^2$$

- Only the contributions to $|V_{tb}|^2$ in the production vertex cross section is considered.

In decay

$$R = \frac{|V_{tb}|^2}{|V_{tb}|^2 + |V_{td}|^2 + |V_{ts}|^2} \sim 1$$

- The decay is fixed to the SM prediction.



Any V-A possible enhancement to $|V_{tb}|$, $|V_{td}|$, and $|V_{ts}|$ might be altering production and decay contributions to t -channel production

Single top cross section: TOP-17-012 approach

In production...

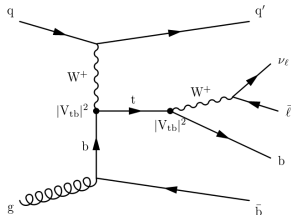
$$\begin{aligned}\sigma_{t\text{-ch.}} &= \sigma_{t\text{-ch.,b}} + \sigma_{t\text{-ch.,d}} + \sigma_{t\text{-ch.,s}} = \\ &= \alpha|V_{tb}|^2 + \beta|V_{td}|^2 + \gamma|V_{ts}|^2\end{aligned}$$

...by adding the decay

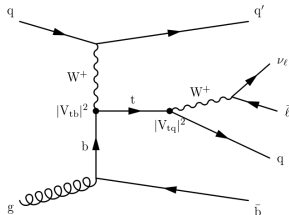
$$\begin{aligned}\sigma_{t\text{-ch.}} \times \text{BR}(t \rightarrow Wq) &\approx \alpha|V_{tb}|^2|V_{tb}|^2 + \alpha|V_{tb}|^2(|V_{td}|^2 + |V_{ts}|^2) \\ &+ \beta|V_{td}|^2|V_{tb}|^2 + \gamma|V_{ts}|^2|V_{tb}|^2\end{aligned}$$

Three signals:

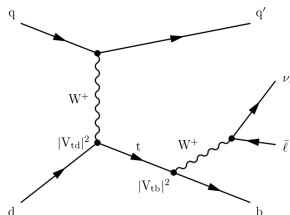
#1 $ST_{(b,b)}$ signal



#2 $ST_{(b,q)}$ signal

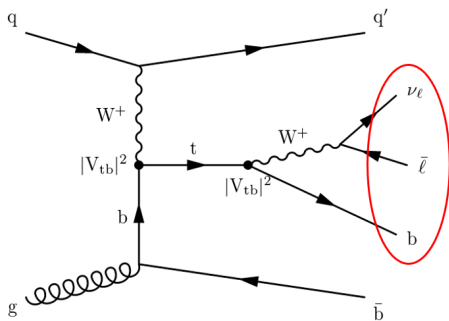


#3 $ST_{(q,b)}$ signal



$ST_{(b,b)}$ features

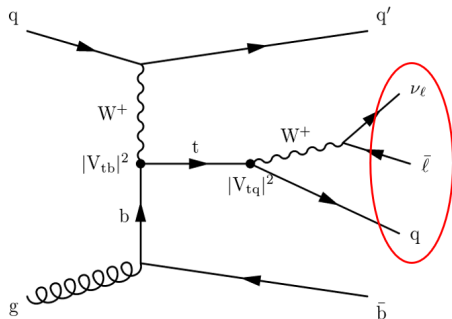
$ST_{(b,b)}$ signal: standard



- b-jet from top quark:
 - $l\nu b$ correct top quark candidate association
- Second b from gluon splitting:
 - if selected $\rightarrow 3j2t$ pure $|V_{tb}|^4$
 - if lost $\rightarrow 2j1t$ pure $|V_{tb}|^4$
 - if not tagged $\rightarrow 3j1t$ background to other signals

$ST_{(b,q)}$ features

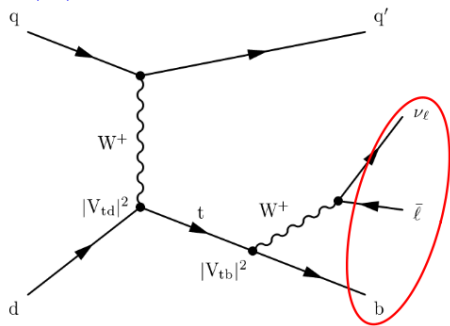
$ST_{(b,q)}$ signal: NEW



- b-jet from gluon splitting
 - $l\nu b$: wrong top quark candidate.
- light jet from top quark:
 - $l\nu q$: correct top quark candidate.
- Reconstructing the top quark with non-btagged jet gives the right kinematic variables
- Main signal region: 1 b-jet, 1 fwd jet, 1 non-b jet.

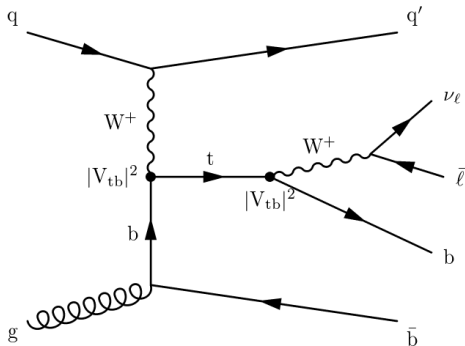
$ST_{(q,b)}$ features

$ST_{(q,b)}$ signal: NEW



- b-jet from top quark:
 - $l\nu b$: correct top quark candidate association.
- Main difference: PDF in the initial state.
- Main signal region: 1 b-jet, 1 fwd jet.

Baseline selection



Light jet from top-quark recoiling (j')

Lepton (e or μ) coming from W-boson decay

Neutrino (ν_e or ν_μ) coming from W-boson decay

Jet coming from top-quark decay

Jet coming from gluon splitting

Required objects

1	Tight muon	$p_T > 26 \text{ GeV}/c$	$ \eta < 2.4$	$I_{rel}^\mu < 0.06$	
0	Loose muon	$p_T > 10 \text{ GeV}/c$	$ \eta < 2.4$	$I_{rel}^\mu < 0.2$	
1	Tight electron	$E_T > 35 \text{ GeV}$	$ \eta < 2.1$	$I_{rel}^e < 0.0588$ (B)	$I_{rel}^e < 0.0571$ (E)
0	Veto electron	$E_T > 15 \text{ GeV}$	$ \eta < 2.5$	$I_{rel}^e < 0.2$	
2(3)	Jet	$E_T > 40 \text{ GeV}$	$ \eta < 4.7$		
1(2)	b-Jet	$E_T > 40 \text{ GeV}$	$ \eta < 2.4$	CMVA ≥ 0.9432	

Top quark reconstruction

Top quark mass reconstructed with

- jet momentum
- lepton momentum
- missing transverse momentum (neutrino)

To obtain $p_{z,\nu}$ one uses:

$$m_W^2 = \left(E_\ell + \sqrt{\cancel{E}_T^2 + p_{z,\nu}^2} \right)^2 - \left(\vec{p}_{T,\ell} + \vec{\cancel{E}}_T \right)^2 - \left(p_{z,\ell}^2 + p_{z,\nu}^2 \right)^2$$

So:

$$p_{z,\nu} = \frac{\Lambda \cdot p_{z,\ell}}{p_{T,\ell}^2} \pm \sqrt{\frac{\Lambda^2 \cdot p_{z,\ell}^2}{p_{T,\ell}^4} - \frac{E_\ell^2 \cdot \cancel{E}_T^2 - \Lambda^2}{p_{T,\ell}^2}} \quad \text{where:} \quad \Lambda = \frac{m_W^2}{2} + \vec{p}_{T,\ell} \cdot \vec{\cancel{E}}_T$$

2 real solutions (in $\sim 65\%$ of signal events)

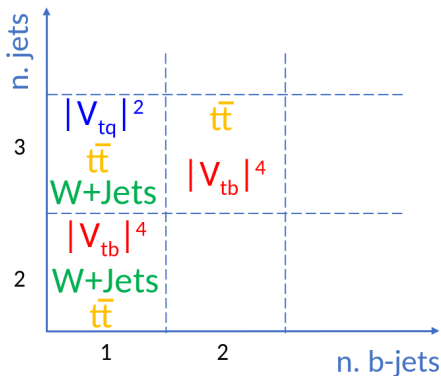
- take smaller $|p_{z,\nu}'|$ solution

complex solutions

- $|p_{x,y}'|$ pair which minimizes ΔR to the original \cancel{E}_T

Regions categorization

- 2-jets–1-tag rich in t -channel $|V_{tb}|^4$
- 3-jets–1-tag rich in t -channel $|V_{tq}|^2$
- 3-jets–2-tags rich in $t\bar{t}$ and pure in $|V_{tb}|^4$



- The three regions are rich with different signal components
- All the samples taken into account in each region for both muon and electron channels.
- Simultaneous fit to extract the CKM matrix elements AND constrain the backgrounds.

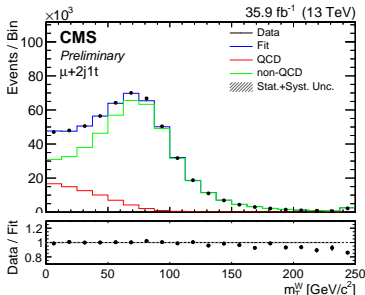
QCD estimation

Large cross-section, low selection efficiency \rightarrow QCD MC with large uncertainty
Extraction from the data

- Approach for 2-jets-1-tag and 3-jets-1-tag:
 - Identification of a sideband rich in QCD events
 - Yield obtained by fitting the m_T^W shape in the isolated region
 \rightarrow ML fit with two components: QCD and non-QCD
 - For the 3j1t the additional scale factor for the $|\eta_{j'}| > 2.5$ region derived from data anti-iso

$$SF = \frac{N_{Data_{SB}}^{\eta_{j'} > 2.5}}{N_{Data_{SB}}}$$

- Approach for 3-jets-2-tags:
 - Contribution from QCD negligible! No extra selection required.



Signal extraction overview

2-jets-1-tag

- j' defined as the non b-tagged jet
- QCD sample depleted with $m_T^W > 50$ GeV requirement
- BDT training: single top t -channel ($ST_{(b,b)}$) vs $t\bar{t}$ and $W + \text{jets}$

3-jets-1-tag

- j' defined as the most forward non b-tagged jet
- signal region $m_T^W > 50$ GeV & $|\eta_{j'}| > 2.5$
- BDT training: single top t -channel with $|V_{tq}|^2$ vertex in decay ($ST_{(b,q)}$) vs single top t -channel ($ST_{(b,b)}$), standard $t\bar{t}$ and $W + \text{jets}$

3-jets-2-tags

- j' defined as the non b-tagged jet
- BDT training: single top t -channel ($ST_{(b,b)}$) vs $t\bar{t}$

Fit strategy and Systematics

- Three different theoretical models used to account BSM models too
- The systematic uncertainties used are:
 - Profiled:
 - The b tagging and mis-identification efficiencies
 - Lepton trigger and reconstruction
 - The uncertainty in the average expected number of pileup interactions
 - $t\bar{t}$ modelling $\rightarrow Q^2$ scale, UE event, ME-PS matching (hdamp), ISR, FSR
 - Renormalisation and factorisation scale uncertainty (μ_R/μ_F) for minor backgrounds
 - The uncertainty due to the choice of PDFs
 - MC limited size samples \rightarrow Barlow-Beeston lite method
 - nonprofiled:
 - Jet energy scale (JES)
 - Jet energy resolution for the signal samples
 - The integrated luminosity is known with a relative uncertainty of $35.89 \text{ cm}^{-2}\text{s}^{-1} \pm 2.6\%$.
 - t -channel modelling $\rightarrow Q^2$ scale, PSQ^2 scale, ME-PS matching (hdamp), PDF choice

Master formulas

The following signal strengths can be defined:

$$\mu_b = \frac{\sigma_{t\text{-ch.,b}}^{\text{obs}} \mathcal{B}(t \rightarrow Wb)^{\text{obs}}}{\sigma_{t\text{-ch.,b}}(\mathcal{B}(t \rightarrow Wb))}$$
$$\mu_{sd} = \frac{\sigma_{t\text{-ch.,b}}^{\text{obs}} \mathcal{B}(t \rightarrow Wd,s)^{\text{obs}} + \sigma_{t\text{-ch.,s,d}}^{\text{obs}} \mathcal{B}(t \rightarrow Wb)^{\text{obs}}}{\sigma_{t\text{-ch.,b}} \mathcal{B}(t \rightarrow Wd,s) + \sigma_{t\text{-ch.,s,d}} \mathcal{B}(t \rightarrow Wb)}$$

In the general case $\mathcal{B}(t \rightarrow Wq) = \Gamma_q / \Gamma_{\text{top}}$

$$\mu_b = \frac{|V_{tb}|_{\text{obs}}^4 \Gamma_q^{\text{obs}} \Gamma_{\text{top}}}{|V_{tb}|^4 \Gamma_q \cdot \Gamma_{\text{top}}^{\text{obs}}}$$
$$\mu_{sd} = \frac{|V_{tb}|_{\text{obs}}^2 (|V_{ts}|^2 + |V_{td}|^2)^{\text{obs}} \Gamma_q^{\text{obs}} \Gamma_{\text{top}}}{|V_{tb}|^2 (|V_{ts}|^2 + |V_{td}|^2) \Gamma_q \Gamma_{\text{top}}^{\text{obs}}}$$

Unconstrained case

- Within the SM the following relations hold:

$$\Gamma_{\text{top}} \sim \Gamma_b \quad \rightarrow \quad \mathcal{B}(t \rightarrow Wq) = R_q = \frac{|V_{tq}|^2}{|V_{tb}|^2 + |V_{ts}|^2 + |V_{td}|^2}$$

- No unitarity relation imposed! Unconstrained case.
- In this assumption, two fits are performed

μ_b (Max Likelihood)

μ_{sd} (Asymptotic).

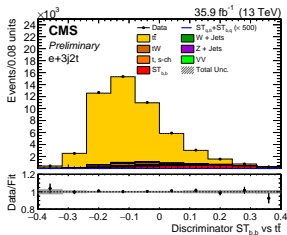
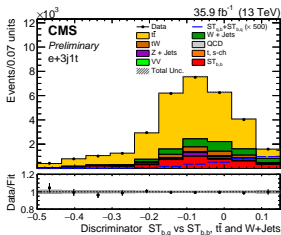
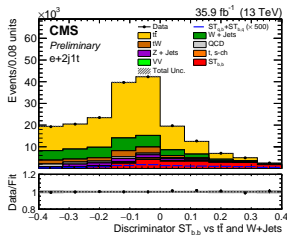
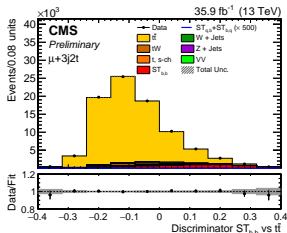
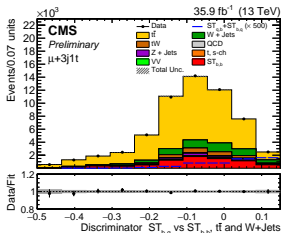
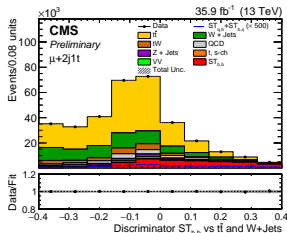
The results obtained are:

$$\mu_b = 0.99 \pm 0.03(\text{profiled}) \pm 0.12(\text{nonprofiled})$$

$$\mu_{sd} < 86 \text{ at } 95\% \text{ C.L.}$$

Unconstrained case: Post fit plots

Muon



Unconstrained case: Interpretation

The fit result for the standard t -channel, events with $|V_{tb}|^4$ vertexes, is converted in terms of $|V_{tb}|^2$ by exploiting the following relation:

$$\frac{\sigma_{t\text{-ch.,b}}^{\text{obs}} \mathcal{B}(t \rightarrow Wb)^{\text{obs}}}{\sigma_{t\text{-ch.,b}} \mathcal{B}(t \rightarrow Wb)} = \frac{(|V_{tb}|^4)^{\text{obs}}}{|V_{tb}|^4}$$
$$|V_{tb}|^2 = 0.99 \pm 0.02 \pm 0.06$$
$$|V_{tb}| = 1.00 \pm 0.01 \pm 0.03$$

The fit result for the non-standard t -channel decays, events with a $|V_{td}|^2$ or $|V_{ts}|^2$ vertex, is:

$$\frac{\sigma_{t\text{-ch.,b}}^{\text{obs}} \mathcal{B}(t \rightarrow Wd,s)^{\text{obs}}}{\sigma_{t\text{-ch.,b}} \mathcal{B}(t \rightarrow Wd,s)} + \frac{\sigma_{t\text{-ch.,s,d}}^{\text{obs}} \mathcal{B}(t \rightarrow Wb)^{\text{obs}}}{\sigma_{t\text{-ch.,s,d}} \mathcal{B}(t \rightarrow Wb)} = \frac{(|V_{td}|^2 + |V_{ts}|^2)^{\text{obs}} (|V_{tb}|^2)^{\text{obs}}}{|V_{td}|^2 + |V_{ts}|^2 |V_{tb}|^2}$$
$$|V_{td}|^2 + |V_{ts}|^2 < 0.17 \text{ at } 95\% \text{ C.L.}$$

Constrained SM case

By assuming the SM the unitarity relation holds.

SM constraint

$$|V_{tb}|^2 + |V_{ts}|^2 + |V_{td}|^2 = 1$$

Master formulas

$$\mu_b = \frac{|V_{tb}|^{4 \text{ obs}}}{|V_{tb}|^4}$$
$$\mu_{sd} = \frac{|V_{tb}|^{2 \text{ obs}} \cdot (1 - |V_{tb}|^{2 \text{ obs}})}{|V_{tb}|^2 \cdot (1 - |V_{tb}|^2)}$$

In this case $|V_{tb}|$ directly fitted.

Results:

$$|V_{tb}| = 0.980_{-0.011}^{+0.014}(\text{stat.} + \text{syst.}) \pm 0.031(\text{nonprofiled})$$

$$|V_{td}|^2 + |V_{ts}|^2 = 0.040_{-0.028}^{+0.023}(\text{stat.} + \text{syst.}) \pm 0.059(\text{nonprofiled})$$

BSM scenario 1

New physics effects:

- enhancement of $|V_{tb}|^2$, $|V_{ts}|^2$, or $|V_{td}|^2$ in production, in decay, or in both.
- existence of new particles $\rightarrow |V_{tb}|^2 + |V_{ts}|^2 + |V_{td}|^2 \neq 1$
- modification of the total top decay width

First case: $|V_{tb}|^2 + |V_{ts}|^2 + |V_{td}|^2 \neq 1$

$$\mu_b = \frac{|V_{tb}|_{\text{obs}}^4}{|V_{tb}|^4 (|V_{tb}|_{\text{obs}}^2 + |V_{ts}|_{\text{obs}}^2 + |V_{td}|_{\text{obs}}^2)}$$
$$\mu_{sq} = \frac{|V_{tb}|_{\text{obs}}^2 (|V_{ts}|_{\text{obs}}^2 + |V_{td}|_{\text{obs}}^2)}{(|V_{ts}|^2 + |V_{td}|^2) (|V_{tb}|_{\text{obs}}^2 + |V_{ts}|_{\text{obs}}^2 + |V_{td}|_{\text{obs}}^2)}$$

Free parameters: $|V_{tb}|$ and $|V_{td}|^2 + |V_{ts}|^2$

Results:

$$|V_{tb}| = 0.988 \pm 0.027(\text{stat} + \text{syst}) \pm 0.043(\text{nonprofiled})$$

$$|V_{td}|^2 + |V_{ts}|^2 = 0.06 \pm 0.05(\text{stat} + \text{syst})_{-0.03}^{+0.04}(\text{nonprofiled}).$$

BSM scenario 2

Second case: $\Gamma_{\text{top}}^{\text{obs}} \neq \Gamma_{\text{top}}$

$$\mu_b = \frac{|V_{\text{tb}}|_{\text{obs}}^4 \Gamma_{\text{top}}}{|V_{\text{tb}}|_{\text{obs}}^4 \Gamma_{\text{top}}^{\text{obs}}}$$

$$\mu_{sd} = \frac{|V_{\text{tb}}|_{\text{obs}}^2 (|V_{\text{ts}}|_{\text{obs}}^2 + |V_{\text{td}}|_{\text{obs}}^2) |V_{\text{tb}}|_{\text{obs}}^4 \Gamma_{\text{top}}}{(|V_{\text{ts}}|^2 + |V_{\text{td}}|^2) \Gamma_{\text{top}}^{\text{obs}}}.$$

Free parameters: $|V_{\text{tb}}|^2$, $|V_{\text{td}}|^2 + |V_{\text{ts}}|^2$, and $\Gamma_{\text{top}}^{\text{obs}}/\Gamma_{\text{top}}$

Results:

$$|V_{\text{tb}}| = 0.988 \pm 0.011(\text{stat} + \text{syst}) \pm 0.021(\text{nonprofiled})$$

$$|V_{\text{td}}|^2 + |V_{\text{ts}}|^2 = 0.06 \pm 0.05(\text{stat} + \text{syst}) \pm 0.04(\text{nonprofiled})$$

$$\frac{\Gamma_{\text{top}}^{\text{obs}}}{\Gamma_{\text{top}}} = 0.99 \pm 0.42(\text{stat} + \text{syst}) \pm 0.03(\text{nonprofiled}).$$

Summary

- First direct measurements of CKM matrix elements
- single top events \rightarrow 1 lepton + 2/3 jets (1/2 b-tagged)
- QCD multijets template from sideband by inverting the lepton selection criteria
- Three regions defined and three BDTs, one for region:
 - single top t -channel vs $t\bar{t}$ and $W +$ jets in 2j1t
 - single top t -channel with $|V_{tq}|^2$ vertex in decay vs single top t -channel, standard $t\bar{t}$ and $W +$ jets in 3j1t
 - single top t -channel vs $t\bar{t}$ in 3j2t

The results obtained are:

Unconstrained case

$$|V_{tb}| = 1.00 \pm 0.01 \pm 0.03$$

$$|V_{tb}|^2 = 0.99 \pm 0.02 \pm 0.06$$

$$|V_{td}|^2 + |V_{ts}|^2 \leq 0.17 \text{ at } 95\% \text{ C.L.}$$

Constrained case

$$|V_{tb}| = 0.980_{-0.011}^{+0.014} \pm 0.031$$

$$|V_{td}|^2 + |V_{ts}|^2 = 0.040_{-0.028}^{+0.023} \pm 0.059$$

BACKUP

MC samples

Monte Carlo samples used:

- Standard single top:
 - NLO precision in POWHEG 2.0 4FS
- Non standard production and decay for single top: $[|V_{td}|, |V_{ts}|]$
 - NLO precision in POWHEG 2.0 5FS
- Associate production tW :
 - NLO precision in POWHEG 1.0 5FS
- $t\bar{t}$:
 - NLO precision in POWHEG 2.0 5FS
- W + jets, single top s -channel and dibosons events:
 - NLO precision in aMC@NLO
- Multi-jet QCD:
 - Derived from data by reverting the isolation cuts on the lepton
 - Cross check with MADGRAPH

All standard MC used reported in back up slides.

Standard objects selection

- Data:
 - 2016 Dataset Run-BCDEFG
- Triggers
 - μ : HLT_IsoMu24v* or HLT_IsoTkMu24v*
 - e: HLT_Ele32_eta2p1_WPTight_Gsfv*
- 1 Lepton (Tight):
 - μ : $p_T > 10$ GeV, $|\eta| < 2.4$ and $I_{rel}^{\delta\beta\text{-corr.}} < 0.06$
 - e: $p_T > 35$ GeV, $|\eta| < 2.1$, $I_{rel}^{\rho\text{-corr.}} > 0.2$
 - Trigger, ID, Isolation SF for electron and muon **derived privately and validated** by MUON and EGamma POGs
- No additional Lepton (Loose):
 - μ : $p_T > 10$ GeV, $|\eta| < 2.4$ and $I_{rel}^{\delta\beta\text{-corr.}} > 0.2$
 - e: With Veto ID, $p_T > 15$ GeV, $|\eta| < 2.5$
- Jets:
 - CHS anti- k_T jets with Loose PF ID, $p_T > 40$ GeV, $|\eta| < 4.7$
 - Lepton-jet disambiguation by $\Delta R(\text{Lep}, \text{jet}) > 0.4$
 - b-tagged with CMVAT tight working point, $|\eta| < 2.4$
- Corrections and scale factors: b-tagging reshaping; pileup reweighting ($\sigma_{pp} = 69$ mb); Summer16_23Sep2016V4 JEC; Summer16_25nsV1 JER, pre-firing.

QCD depletion

QCD normalized to fit results.

Other processes normalized to the expected cross sections.

