

# Treatment of Fiducial Acceptance Cuts in $q_T$ Resummation.

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# Recap of inclusive Drell-Yan.

Consider  $p(P_a^\mu)p(P_b^\mu) \rightarrow Z/\gamma^*(q^\mu) \rightarrow \ell^-(k_1^\mu)\ell^+(k_1^\mu)$ :

- Cross section factorizes into leptonic/hadronic tensor,  $q^\mu L_{\mu\nu} = q^\mu W_{\mu\nu} = 0$

$$\frac{d\sigma}{d^4q} = L^{\mu\nu}(q^\mu)W_{\mu\nu}(q^\mu, P_a^\mu, P_b^\mu)$$

- Leptonic tensor is simple, by convention includes line-shape (here: photon case)

$$L^{\mu\nu}(q^\mu) \equiv L(q^2)(q^2 g^{\mu\nu} - q^\mu q^\nu), \quad L(q^2) \sim \frac{\alpha_{\text{em}}^2}{q^4}$$

▶  $d\sigma/d^4q = L(q^2)W(q^\mu, P_a^\mu, P_b^\mu)$  proportional to trace  $W \equiv g_{\mu\nu}W^{\mu\nu}$

- $W$  is scalar, so only depends on  $q^2 \equiv Q^2$  and  $P_{a,b} \cdot q = E_{\text{cm}}\sqrt{Q^2 + q_T^2} e^{\pm Y}$

▶ Resummation limit  $q_T \rightarrow 0$  of  $W$  receives only quadratic power corrections:

$$W = \left\{ \delta(q_T^2) + \alpha_s \left[ \frac{\ln q_T^2/Q^2}{q_T^2} + \frac{1}{q_T^2} + \delta(q_T^2) \right] + \dots \right\} \left[ 1 + \mathcal{O}\left(\frac{q_T^2}{Q^2}\right) \right]$$

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# Leptonic observables & tensor decomposition.

Consider  $p(P_a^\mu)p(P_b^\mu) \rightarrow Z/\gamma^*(q^\mu) \rightarrow \ell^-(k_1^\mu)\ell^+(k_2^\mu)$  and measure  $k_{1,2}^\mu$ :

- Parametrize decay phase space by two rest-frame angles  $\cos \theta, \varphi$ :

$$\frac{d\sigma}{d^4q d\cos\theta d\varphi} = L^{\mu\nu}(q^\mu, \cos\theta, \varphi)W_{\mu\nu}(q^\mu, P_a^\mu, P_b^\mu)$$

- **Leptonic** tensor carries dependence on lepton momenta (shown:  $P$ -even case)

$$L^{\mu\nu}(q^\mu, \cos\theta, \varphi) \sim \frac{\alpha_{\text{em}}^2}{q^4} (k_1^\mu k_2^\nu + k_2^\mu k_1^\nu - g^{\mu\nu} k_1 \cdot k_2)$$

- Decompose  $W^{\mu\nu}$  into nine allowed orthogonal tensor structures  $K_i^{\mu\nu}$ :

$$\frac{d\sigma}{d^4q d\cos\theta d\varphi} = \sum_{i=-1}^7 (L \cdot K_i)(K_i \cdot W) \equiv \sum_{i=-1}^7 L_i W_i$$

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- Decompose  $W^{\mu\nu}$  into nine allowed orthogonal tensor structures  $K_i^{\mu\nu}$ :

$$\begin{aligned} \frac{d\sigma}{d^4q d\cos \theta d\varphi} &= \sum_{i=-1}^7 (L \cdot K_i)(K_i \cdot W) \equiv \sum_{i=-1}^7 L_i W_i \\ &= \frac{d\sigma}{d^4q} \left[ 1 + \cos^2 \theta + \sum_{i=0}^7 A_i f_i(\cos \theta, \varphi) \right] \end{aligned}$$

- ▶  $K_i$  map onto spherical harmonics  $f_i(\cos \theta, \varphi)$  with **angular coefficients**  $A_i$

# Resummation in the strict $q_T \rightarrow 0$ limit.

What are the leading singular terms as  $q_T \rightarrow 0$  that **must** be resummed?

- Expand hadronic structure functions as  $W_i \rightarrow W_i^{\text{res}}$
- ▶ All\* vanish except for  $W_{-1}^{\text{res}} \leftrightarrow d\sigma^{\text{res}}/dq_T$  and  $W_4^{\text{res}} \leftrightarrow dA_{\text{FB}}^{\text{res}}/dq_T$

\*Up to intrinsically nonperturbative effects

- Expand leptonic tensor as  $L_i(q_T, \cos \theta, \varphi) \rightarrow L_i(q_T = 0, \cos \theta, \varphi)$ 
  - ▶ Leptons are exactly back to back,  $p_T^{\ell^-} = p_T^{\ell^+}$
  - ▶ No distinguished transverse direction anymore, so  $L_i(\varphi)$

▶ 
$$\frac{d\sigma}{d^4q d\cos \theta d\varphi} \sim \frac{1}{2\pi} \left[ (1 + \cos^2 \theta) W_{-1}^{\text{res}} + \cos \theta W_4^{\text{res}} \right] \quad \text{as } q_T \rightarrow 0$$

- Underappreciated fact:  $W_{-1}^{\text{res}} \neq W_4^{\text{res}}$ , easy to see from FO expansion:

$$W_i^{\text{res}} = \delta(q_T) \sum_q Q_q^{\text{EW}}(i) f_q f_{\bar{q}} + \mathcal{O}(\alpha_s)$$

- ▶ Calculating  $A_4^{\text{FO}} \times d\sigma^{\text{res}}/dq_T$  does not recover  $A_{\text{FB}}^{\text{res}}/dq_T$  at small  $q_T$

# Resumming fiducial power corrections.

What are the power corrections to  $\sum_i L_i(q_T = 0) W_i^{\text{res}}$ ?

- Hadronic structure functions are scalar, so  $W_i = W_i^{\text{res}} [1 + \mathcal{O}(q_T^2/Q^2)]$
- $L_i$  are also scalar, but  $L_i(q_T) = L_i(0) [1 + \mathcal{O}(q_T/Q)]$  in the presence of practically any measurements on the decay products

**WHY?** Boosting back into lab frame from rest frame (say: Collins-Soper frame), we have

$$p_{\ell-}^\mu = \frac{Q}{2} \left( \gamma + \frac{q_T}{Q} s_\theta c_\varphi, \gamma s_\theta c_\varphi + \frac{q_T}{Q}, s_\theta s_\varphi, c_\theta \right), \quad \gamma = \frac{\sqrt{Q^2 + q_T^2}}{Q}$$

- ▶ Measuring  $p_T^\ell$  and/or  $\eta_\ell$  results in a linear dependence on  $q_T$
- We can fix this – we can even exploit it!

By restoring the exact  $q_T$  dependence of the  $L_i$ ,  
we resum all linear power corrections to all orders in  $\alpha_s$ :

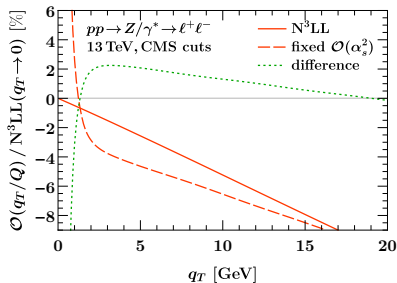
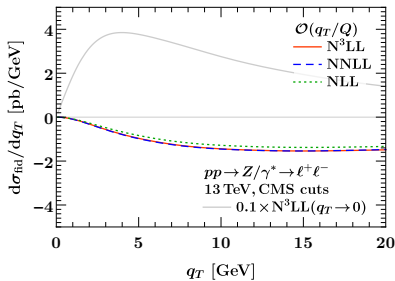
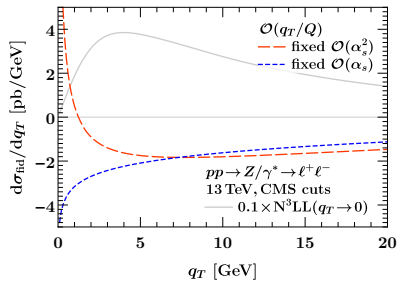
$$\frac{d\sigma}{d^4q d\cos\theta d\varphi} = \left[ L_{-1}(q_T) W_{-1}^{\text{res}} + L_4(q_T) W_4^{\text{res}} \right] \left[ 1 + \mathcal{O}(q_T^2/Q^2) \right]$$

# Relation to literature.

- Keeping  $L_i(q_T)$  exact allows for nonzero recoil in the resummation  
... see numerics on the next slides for examples of this
- Equivalent to evaluating tree-level matrix element in a (sensibly) boosted frame, as done e.g. in RESBOS or DYRES
- One-parameter ambiguity in how to distribute  $p_T$  between annihilating partons [Catani, Ferrera, de Florian, Grazzini '15]
  - ▶ Corresponds to slightly rotated basis choice for the  $K_i^{\mu\nu}$
- Can show using  $K_i^{\mu\nu}$  that the difference is strictly  $\mathcal{O}(q_T^2/Q^2)$ 
  - Change of basis for  $P$ -even structure functions is known [Boer, Vogelsang '06]
- ▶ Linear power corrections to fiducial  $q_T$  spectrum are **unique**



# Numerical impact: $d\sigma_{\text{fid}}/dq_T$

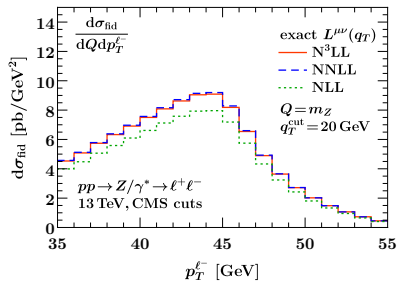
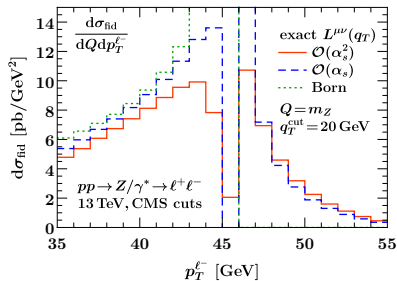
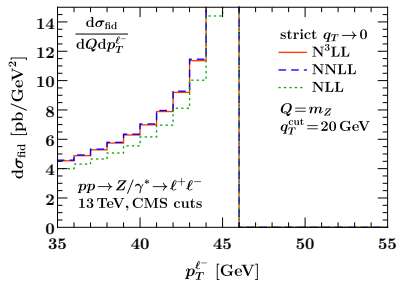
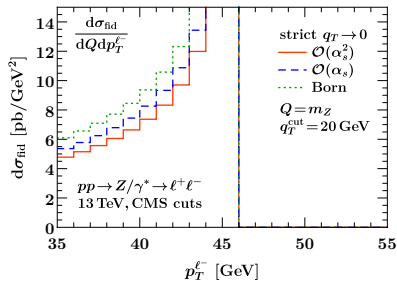


Shorthand for fiducial power corrections:

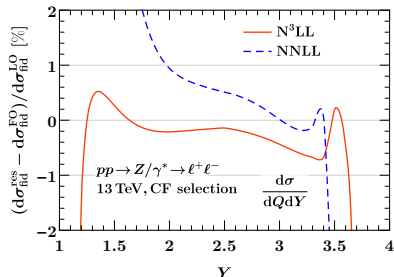
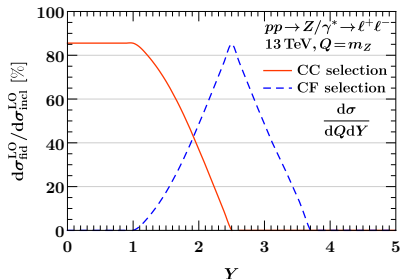
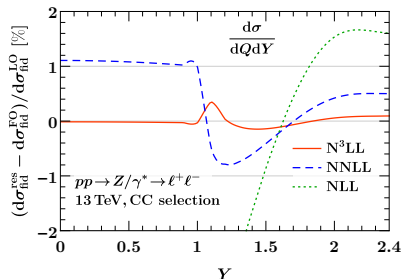
$$\mathcal{O}(q_T/Q) \equiv \sum_i \left[ L_i(q_T) - L_i(0) \right] W_i^{\text{res}}$$

CMS cuts:  $p_T^{\text{min}} = 25 \text{ GeV}, |\eta_\ell| < 2.4$

# Numerical impact: $d\sigma_{\text{fid}}/dp_T^{\ell^-}$



# Application: Resummation effects in $d\sigma_{\text{fid}}/dY$



Question: Is the fiducial rapidity spectrum sensitive to resummation effects?

[see also talk by M. Boonekamp in Durham]

Note: Requires care to ensure

$$\int dq_T [\sigma_{\text{res}}^{\text{incl}} - \sigma_{\text{sing}}^{\text{incl}}] = 0$$

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- Demonstrated that linear power corrections in the fiducial  $q_T$  spectrum arise (only) from the cuts on leptonic phase space
- Enables their resummation at N<sup>3</sup>LL, including the physical effect of recoil
- Showed first results for the lepton  $p_T$  spectrum at N<sup>3</sup>LL
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Thank you for your attention!