

Focussing Lattices of Compton Gamma Rings

CERN, KEK, LAL, DESY, KIPT, ...

Required intensities

$$N_{e^+} \sim 10^{14} / \text{s} \rightarrow N_{\gamma} \sim 10^{16} / \text{s} \rightarrow n_{\gamma} \sim 0.3 - 0.4 / (e^- \text{ turn})$$

Large energy spread

$$\delta_{tot} = \sqrt{\frac{\Delta E_{SR}}{\Delta E_{tot}} \delta_{SR}^2 + \frac{\Delta E_{CS}}{\Delta E_{tot}} \delta_{CS}^2} \approx \delta_{CS} \sqrt{\frac{\Delta E_{CS}}{\Delta E_{tot}}} \approx \begin{cases} 3.0\% \text{ for } CO_2 \text{ ring} \\ 6.2\% \text{ for } YAG \text{ ring} \end{cases}$$

$$\Delta E_{tot} = \Delta E_{SR} + \Delta E_{CS}; \quad \delta_{SR}, \delta_{CS} - \text{partial energy spreads}$$

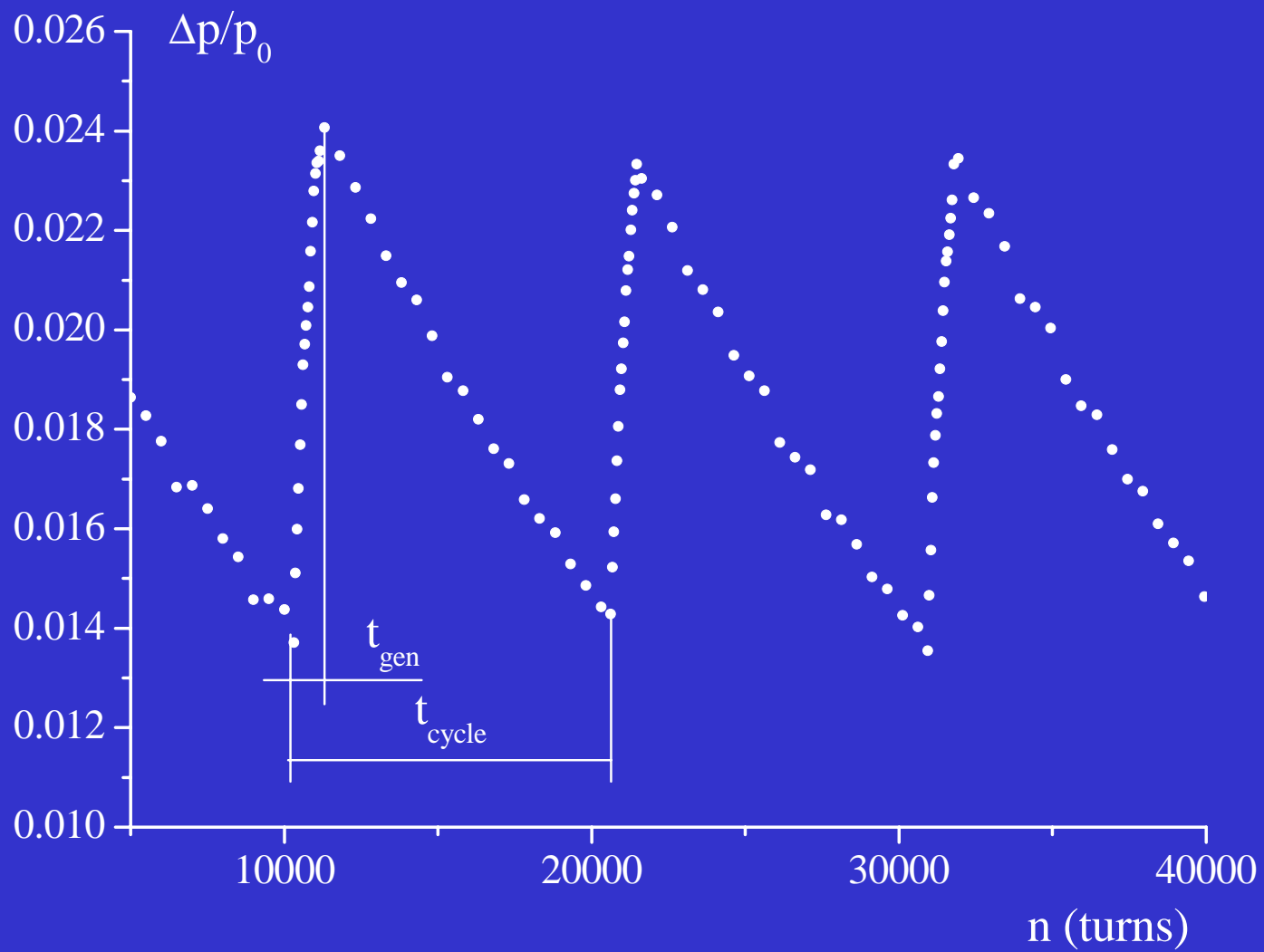
Large energy acceptance $\sigma_{RF} > 4 \div 5 \delta_{tot}$

Correction of high order chromaticity

$$\Delta Q = \frac{\partial Q}{\partial \delta} \delta + \frac{\partial^2 Q}{\partial \delta^2} \delta^2 + \frac{\partial^3 Q}{\partial \delta^3} \delta^3 + \dots$$

Suppression of high order dispersion functions at IP's

$$\Delta x = \eta_1 \delta + \eta_2 \delta^2 + \eta_3 \delta^3 + \dots$$



Energy spread during several cycles

Photon number per electron and per turn

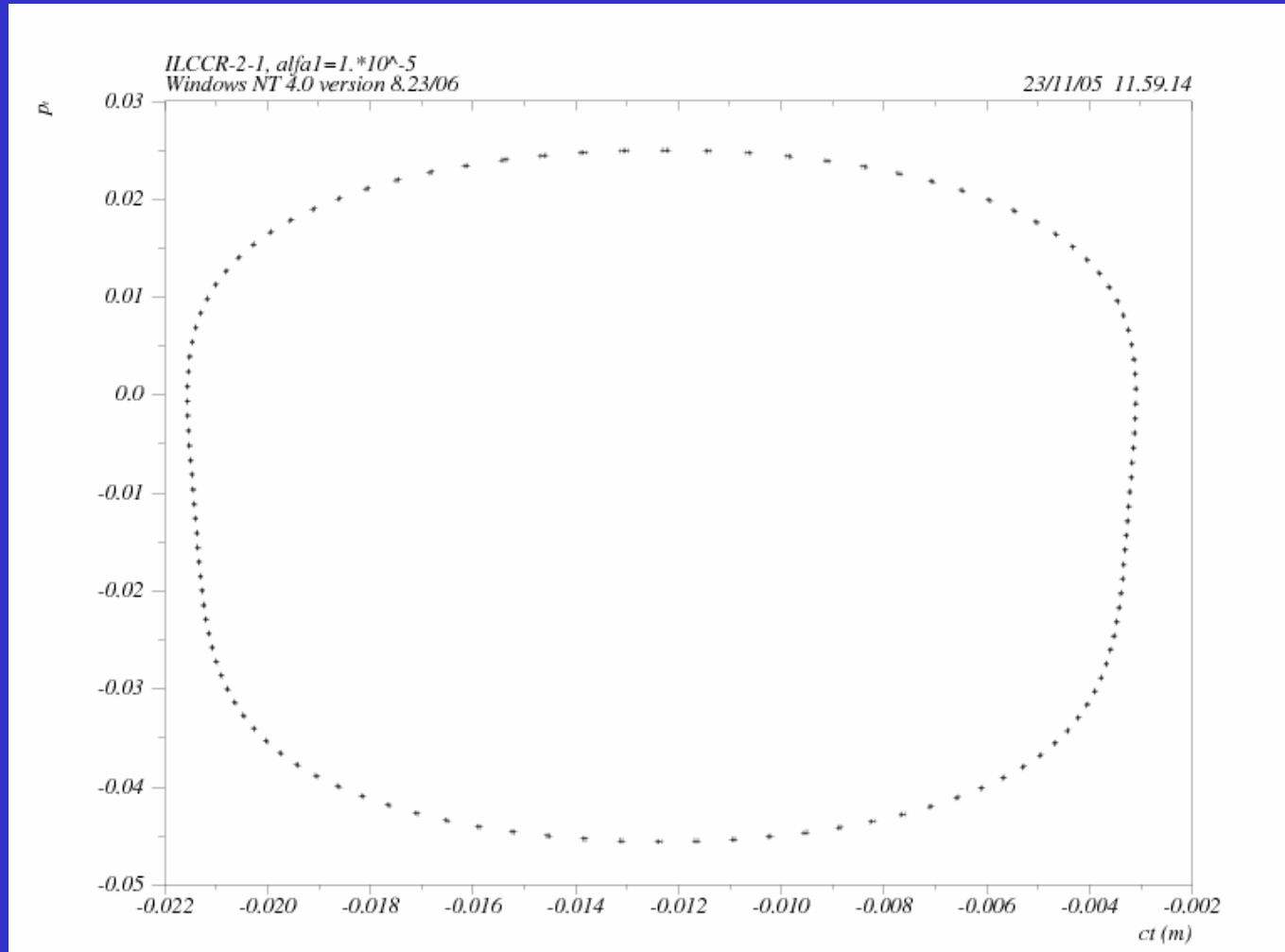
$$n_\gamma \approx \frac{n_{ph} \sigma_C}{\sqrt{z_e^2 + z_{ph}^2} \sqrt{x_e^2 + x_{ph}^2 + (s_e^2 + s_{ph}^2) \phi_{col}^2 / 4}}$$

Longitudinal size of electron beam $s_e = (\alpha_1 c / \Omega_s) \delta$

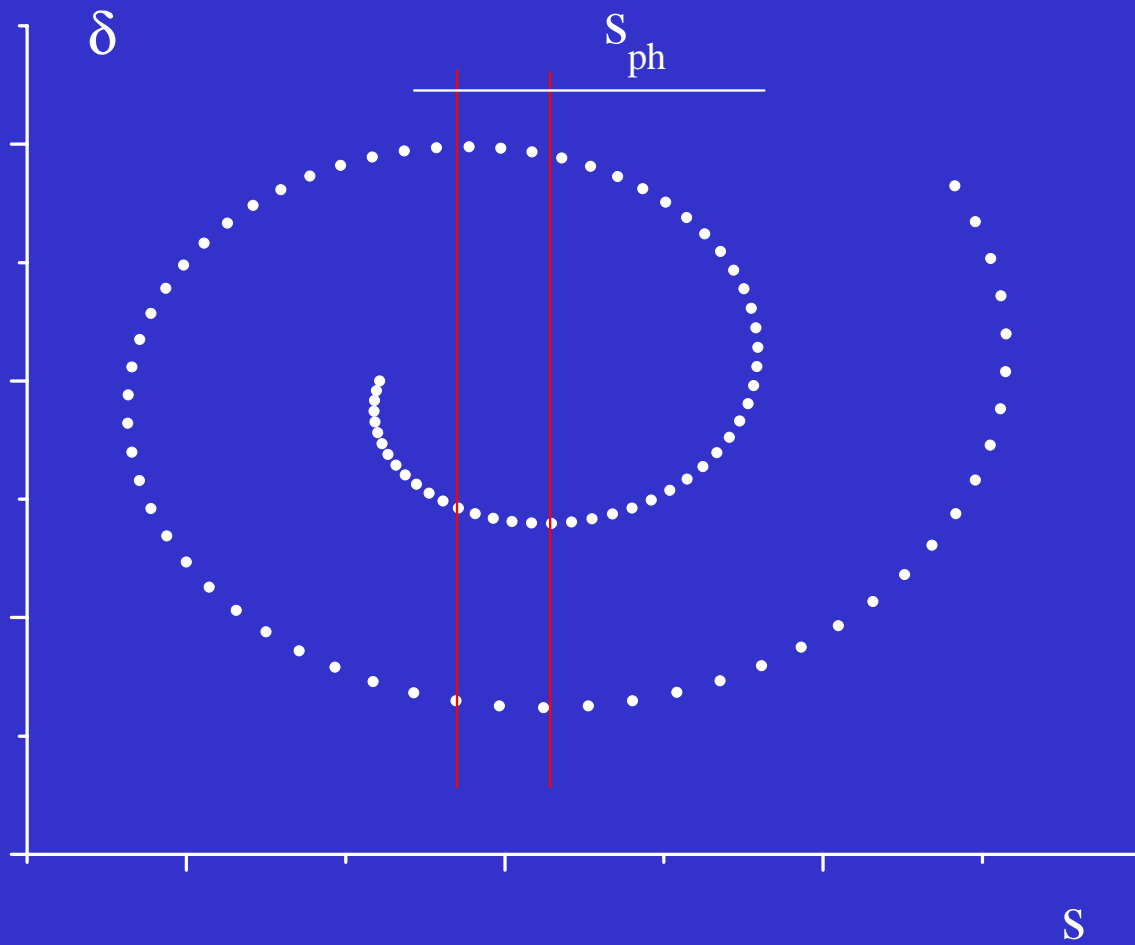
$s_e < 1$ mm in storage ring with $\Omega_s = 5$ kHz ($Q_s = 0.01$ for storage ring with circumference $C = 600$ m)

$\alpha_1 < 1.66 * 10^{-6}$ at energy spread equal to 1 %.

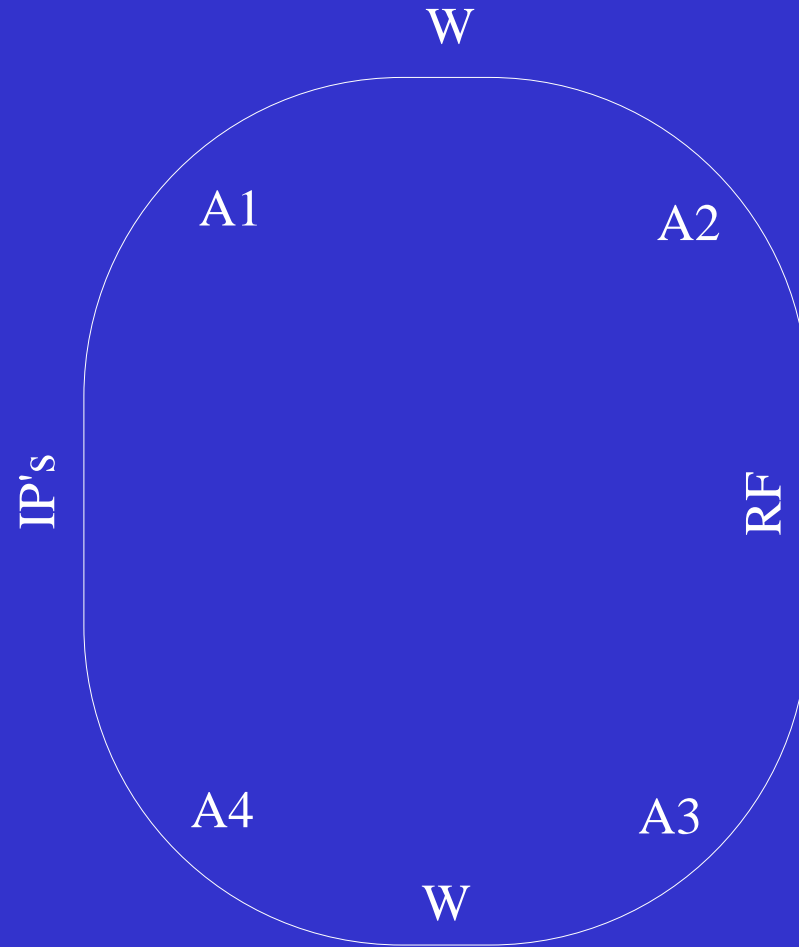
Orbit lengthening $\frac{\Delta C}{C_0} = \alpha_1 \delta + \alpha_2 \delta^2 + \alpha_3 \delta^3 + \dots$



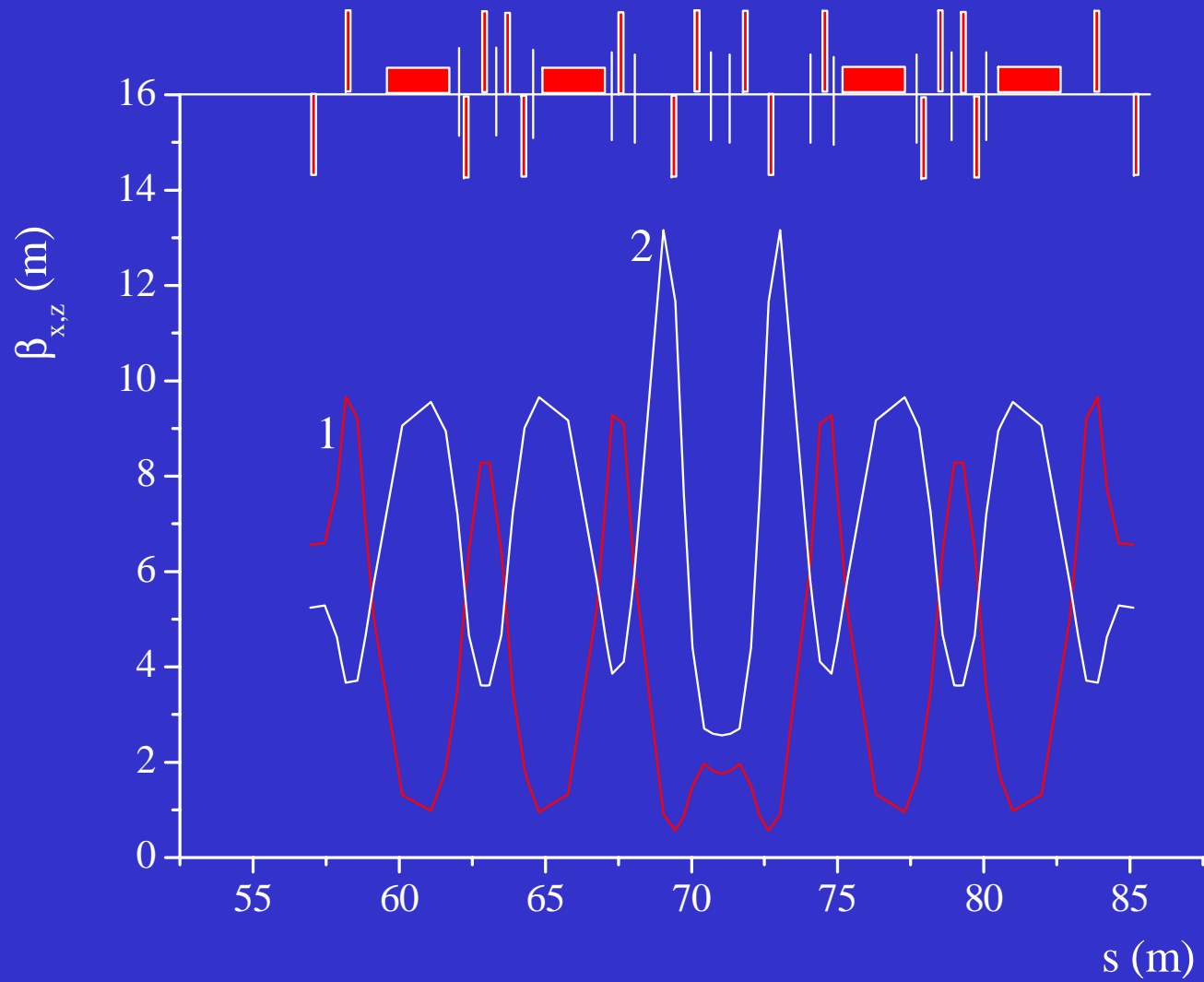
Phase trajectory of synchrotron motion. $E_0 = 4.1$ GeV,
 $\alpha_1 = 1*10^{-5}$ (MAD simulation)



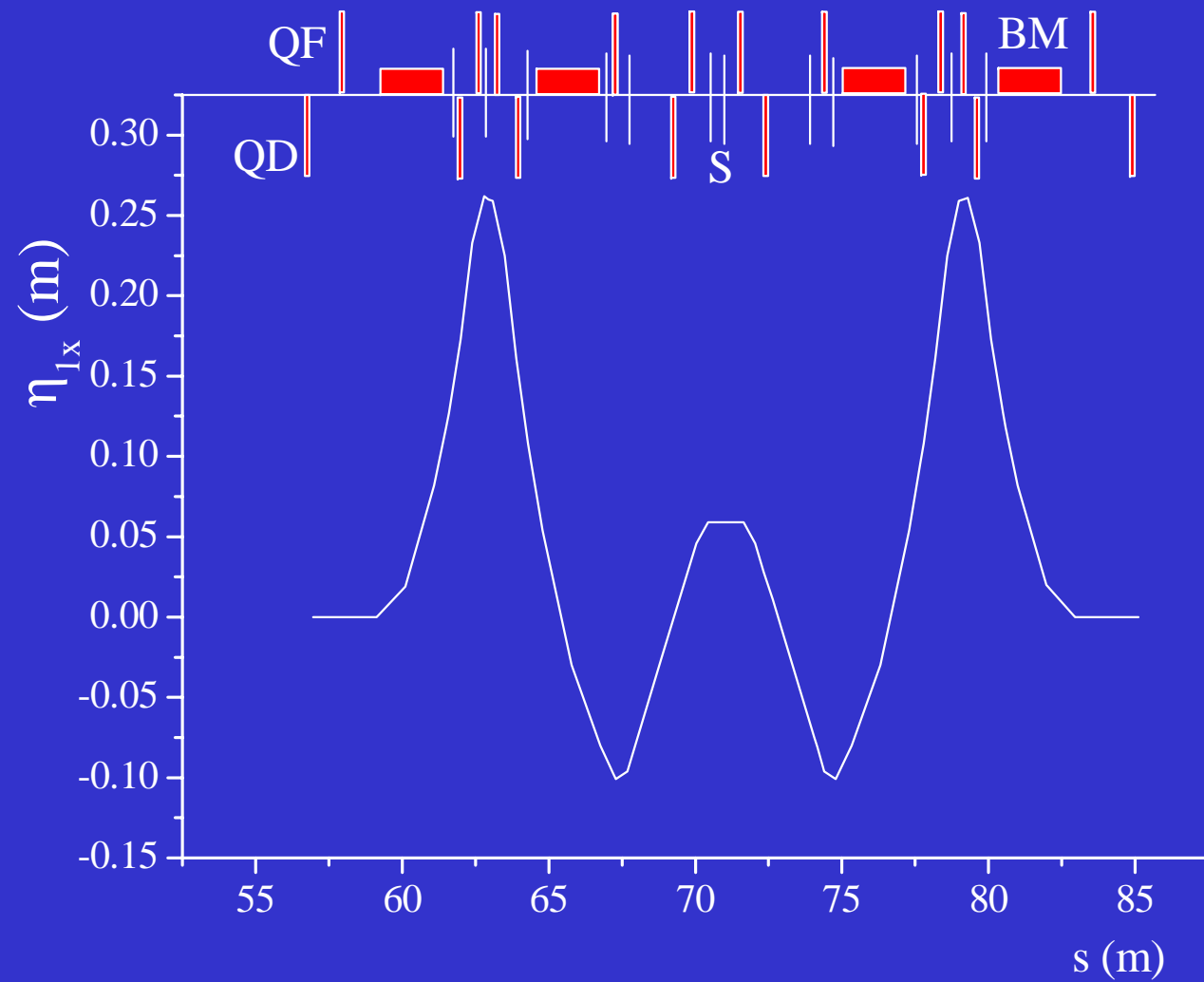
“Averaged” synchrotron motion at intense Compton scattering



Layout of Compton ring. A1-A4 – ring arcs; IP's, RF, W – long straight sections of interaction points, RF and wigglers



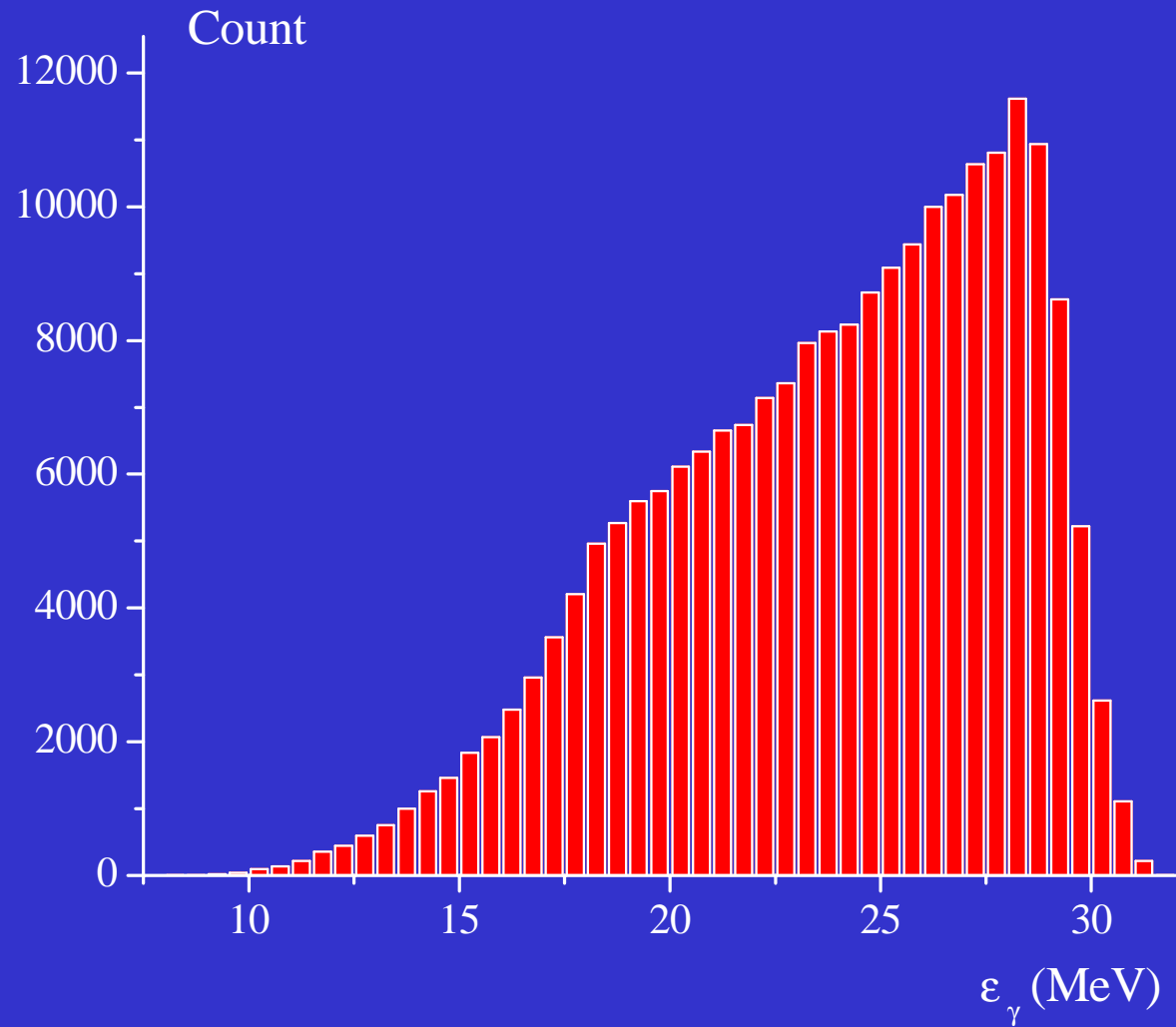
Horizontal (1) and vertical (2) amplitude functions
of four – bending section



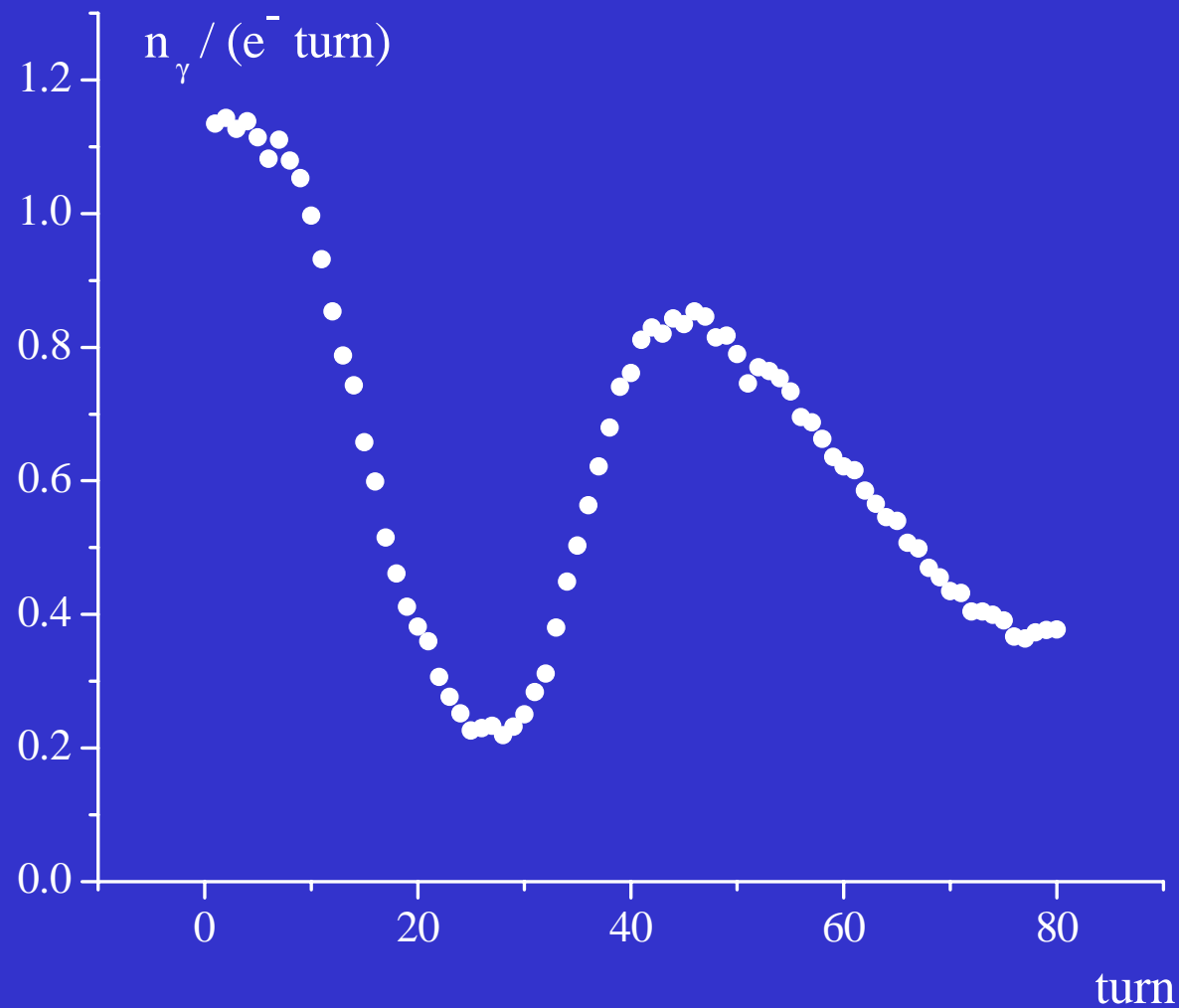
First order dispersion function of four – bending section.
 BM are bending magnets, QF,QD - quadrupoles, S - sextupoles

Main parameters of CO₂ Compton ring:

- Electron energy up to $E_0 = 5$ GeV;
- circumference $C = 719.5$ m;
- number of IP's $N_{IP} = 30$;
- harmonics number $h = 1560$;
- RF frequency $f_{RF} = 650$ MHz;
- number of bending magnets $N_{BM} = 80$;
- horizontal betatron number $Q_X = 53.17$;
- vertical betatron number $Q_Z = 22.24$;
- chromaticity $\chi_X = -73.9$, $\chi_Z = -49.4$;
- natural emittance at the maximal electron energy $\epsilon_X = 2.8 \cdot 10^{-9}$;
- RF – voltage $V_{RF} = 60$ MV;
- linear momentum compaction factor $0 \ll \alpha_1 \ll 2 \cdot 10^{-4}$.



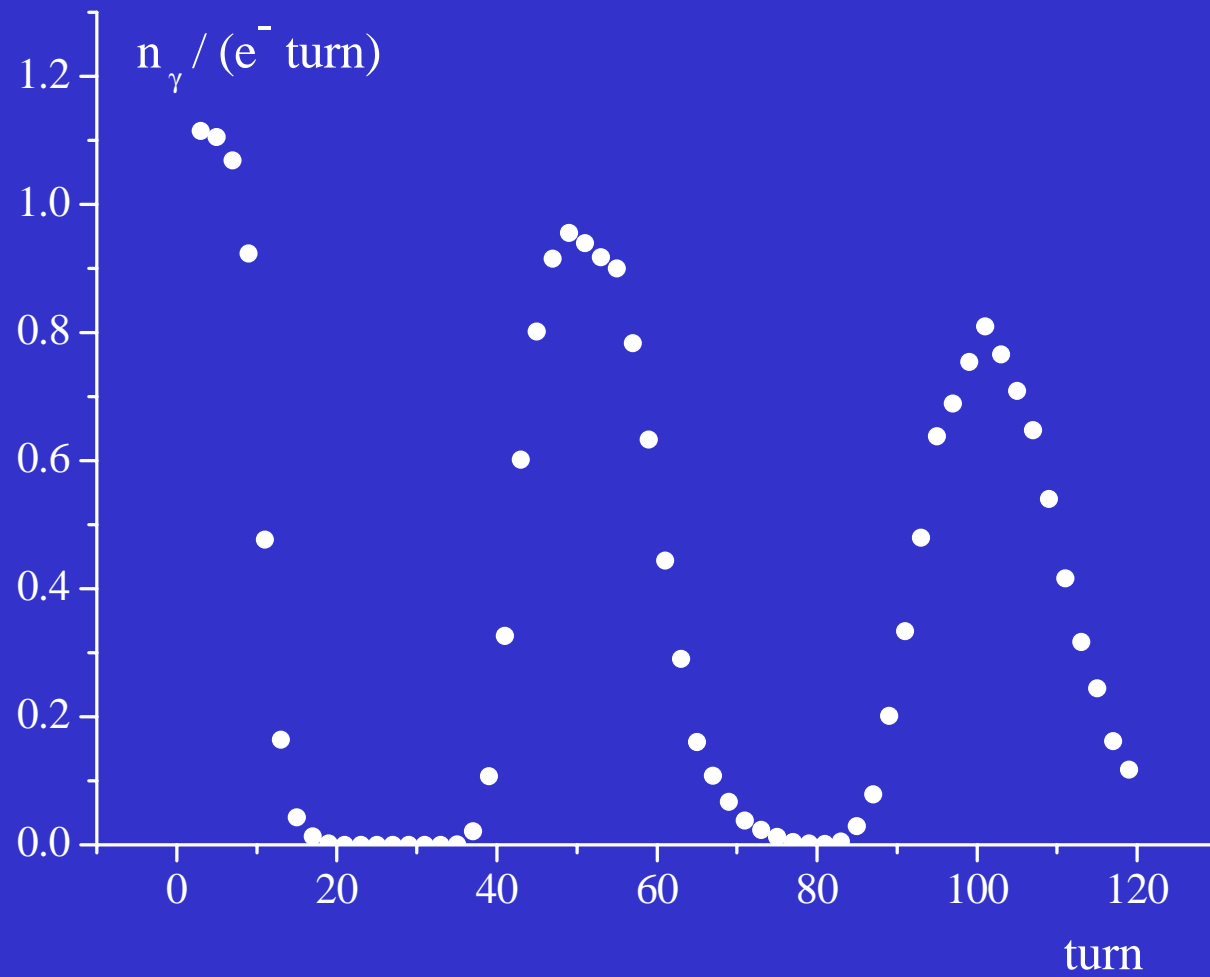
Collimated spectrum within collimation angle 0.1 mrad.
Electron energy is 4.1 GeV, number of electrons 10000.



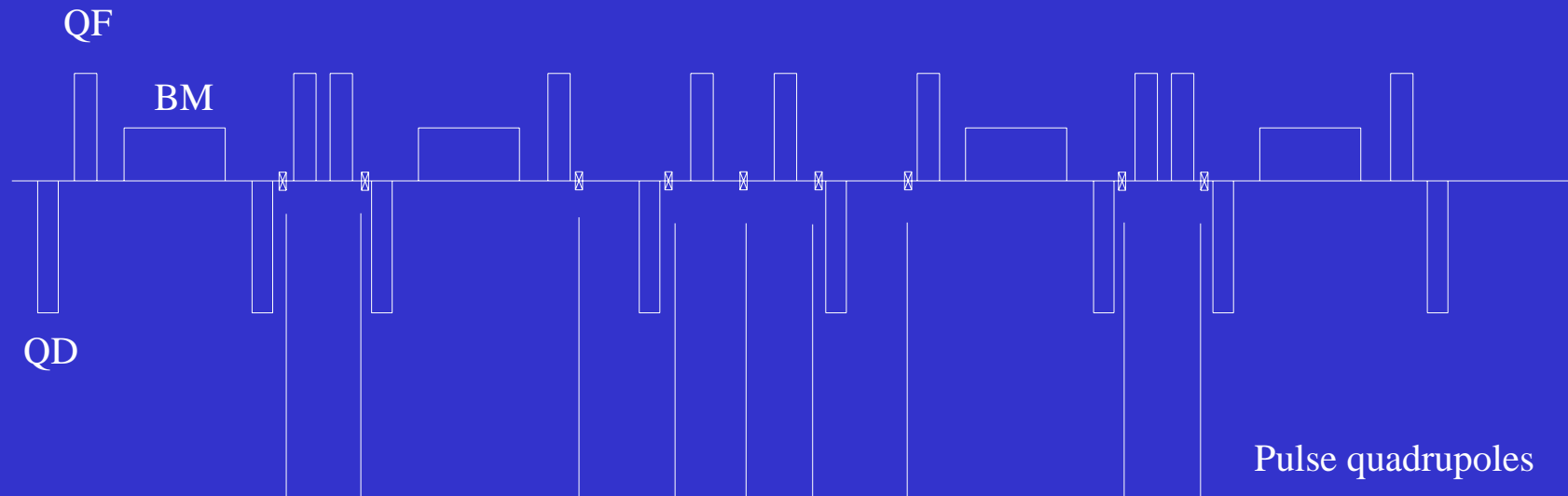
Gamma beam intensity in train vs. turn number at RF phase manipulation.

RF frequency $f_{\text{RF}} = 650$ MHz, initial electron beam coordinates

$s = 0.012$ m (10 degrees), $\delta = 0$



Gamma beam intensity in train vs. turn number at $f_{\text{RF}} = 1950$ MHz.
Initial electron beam coordinates $s = 0.$, $\delta = 0.$



Distribution of pulse quadrupoles over arc cell

Preliminary evaluated parameters of CLIC Compton ring:

- electron beam energy $E_0 = 1.3 \text{ GeV}$;
- circumference $C = 191.8 \text{ m}$ ($h = 1200$ at RF frequency 1875 MHz);
- number of interaction points $N_{\text{IP}} = 2\text{-}3$;
- RF voltage $V_{\text{RF}} = 10 \text{ MV}$;
- momentum compaction factor at low α_1 mode $\sim 1\text{-}5 \cdot 10^{-5}$;
- number of four – bending arc cells $N_{\text{C}} = 8$;
- required RF acceptance $\sigma_{\text{RF}} \sim 10 \%$;
- natural emittance $\varepsilon_{\text{X}} \approx 3\text{-}5 \cdot 10^{-9} \dots$

What are priority measures for further design?

- analytical treatment and simulation of electron beam instabilities in quasi-stationary operation mode;
- developing of the code for minimization of the second order momentum compaction factor (it would be most preferable to develop the HARMON module in MAD code);
- extension of the circle of participants in lattice design.