



MUON PRODUCTION TARGETS

Francesco Collamati - INFN Rome
LEMMA working group

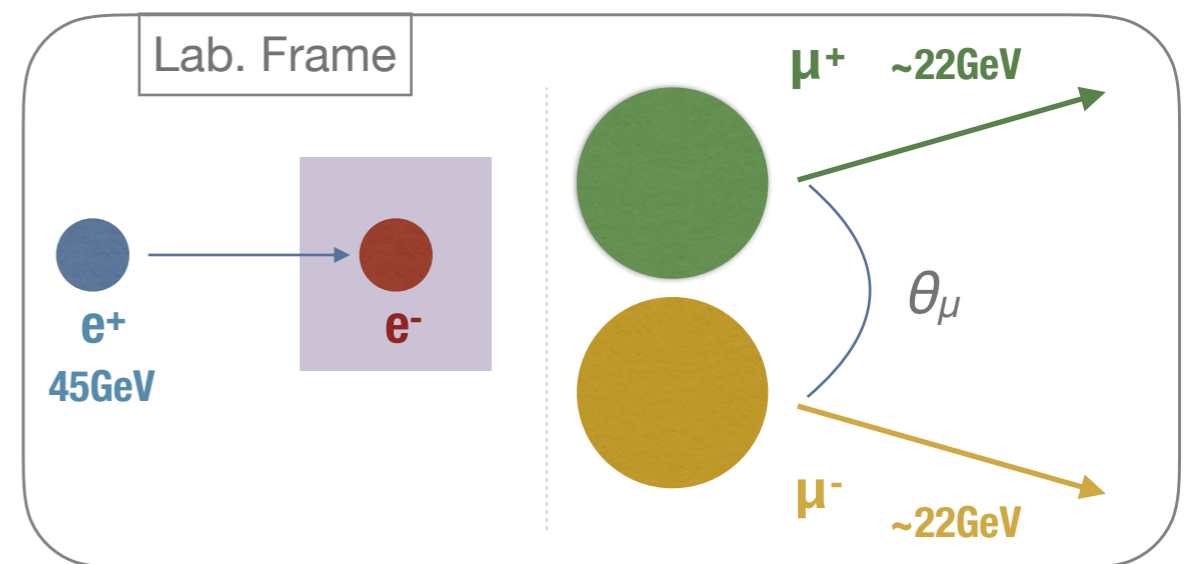
THE MUON PRODUCTION ISSUE

◆ **LEMMA** idea is to exploit direct muon production via
 $e^+e^- \rightarrow \mu^+\mu^-$

- ✓ Low emittance
- ✓ Small energy spread
- ✓ Low background
- ✓ Reduced losses from decay

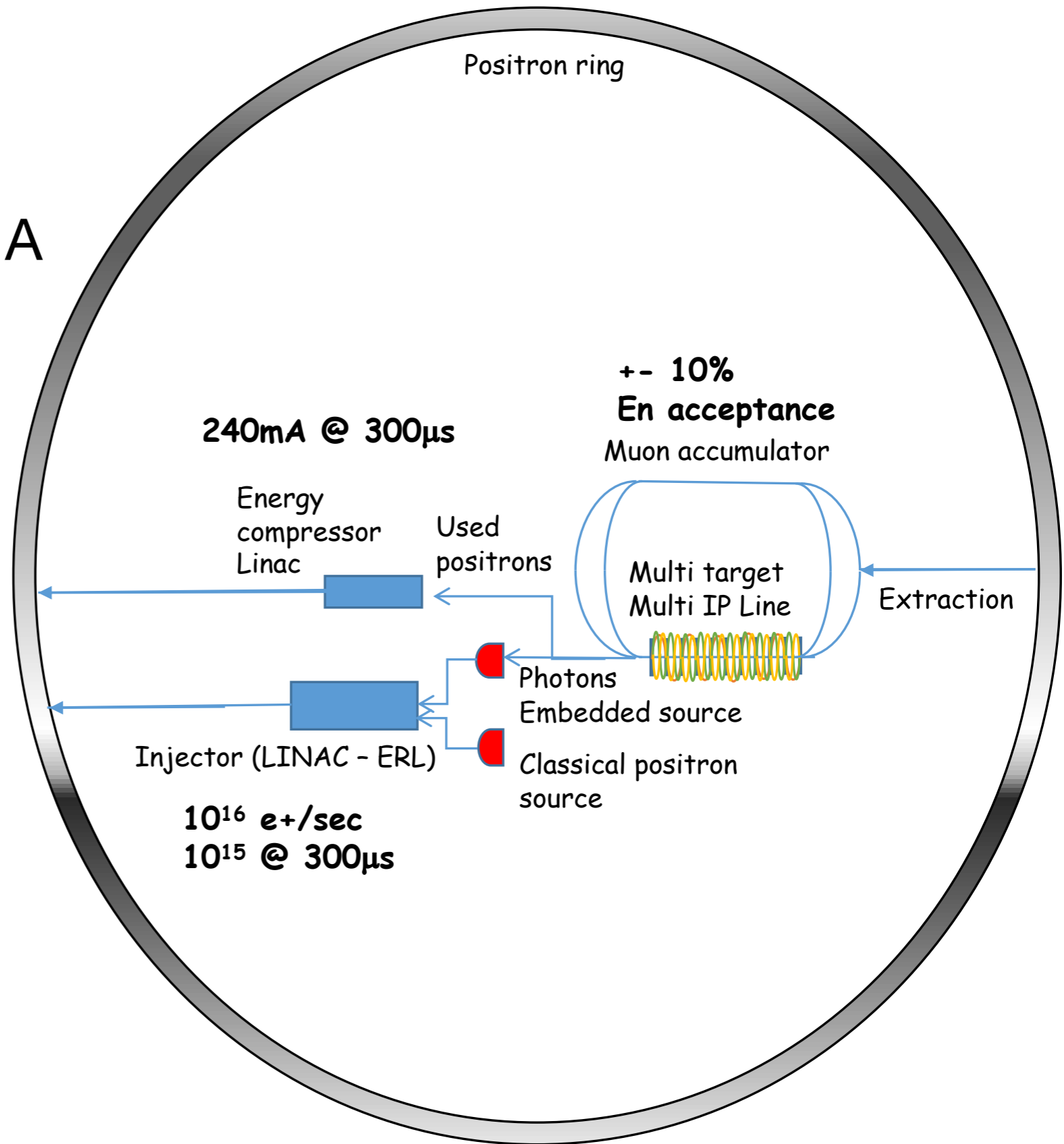
◆ Due to the very **small cross section** of the positron annihilation process, an elevated amount of positrons must be used

- ➔ Positron source intensity
- ➔ Power load on target



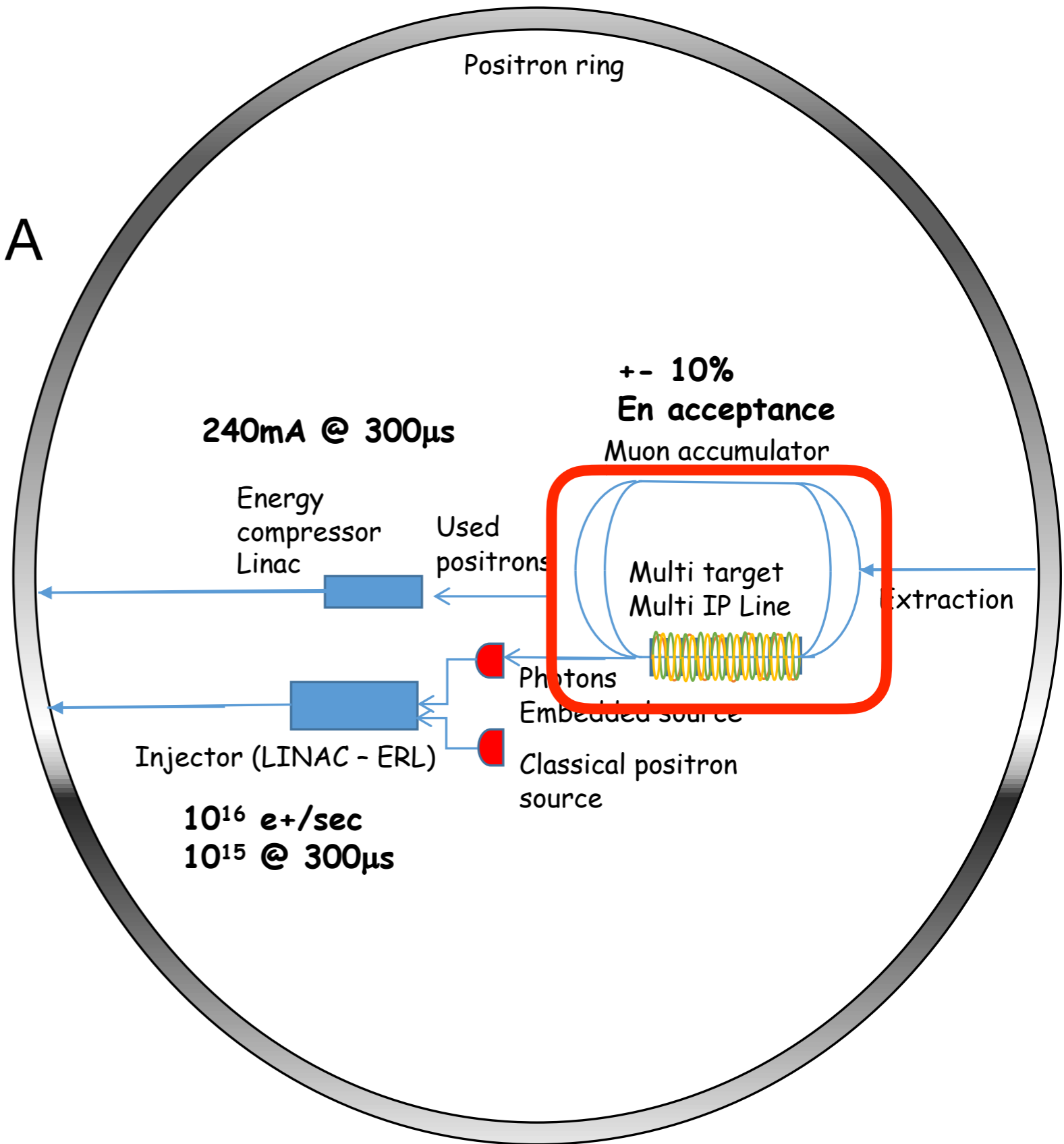


THE LEMMA SCHEME





THE LEMMA SCHEME



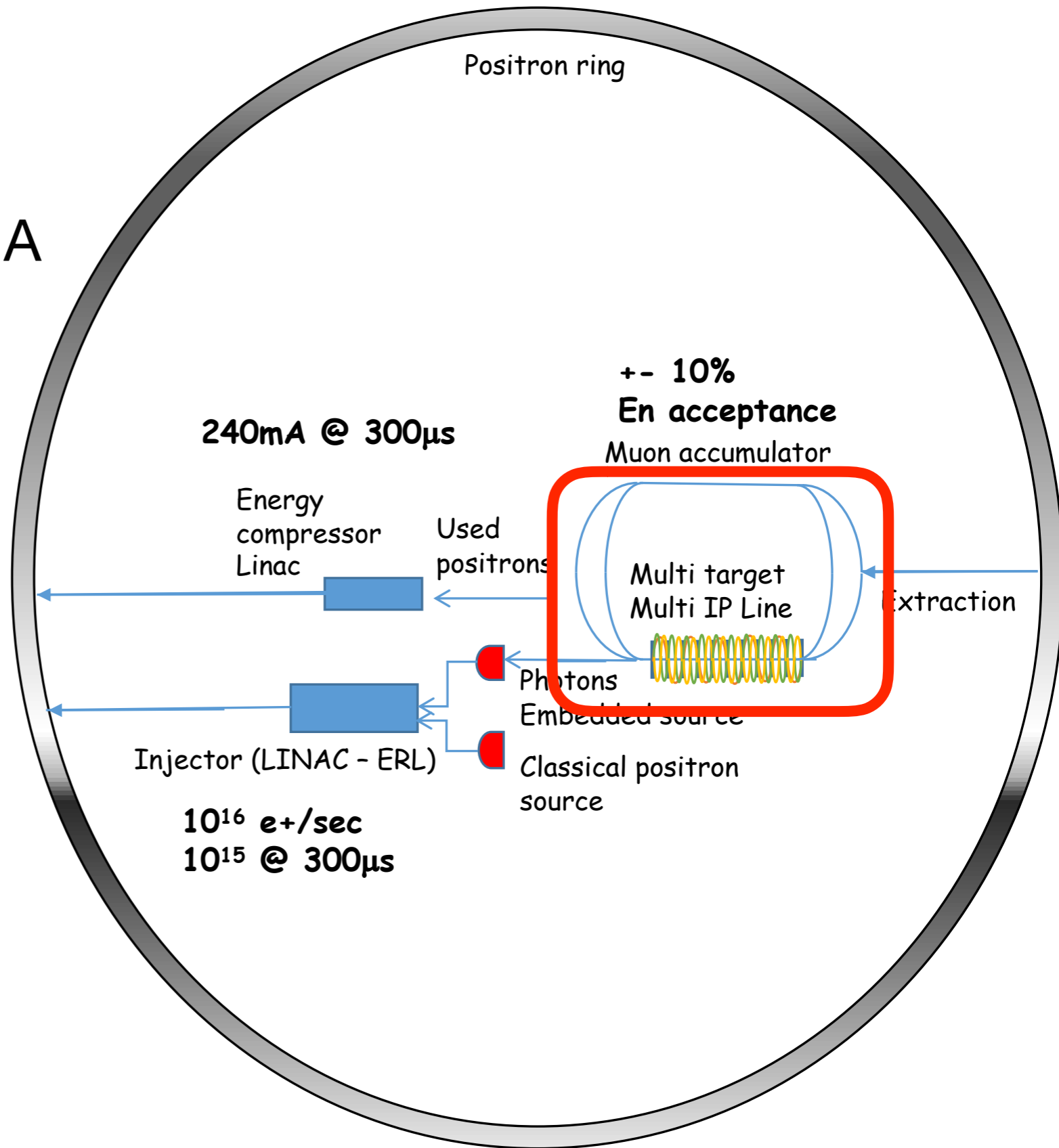


THE LEMMA SCHEME

A tool is needed to study/optimize muon production in a variety of possible configurations

number/size/position of targets,
beam energy/size.....

line optics





THE TOOL USED

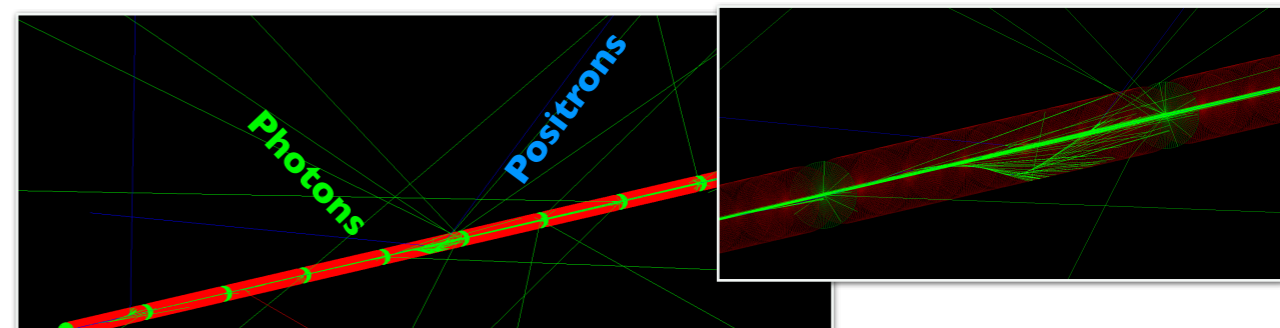
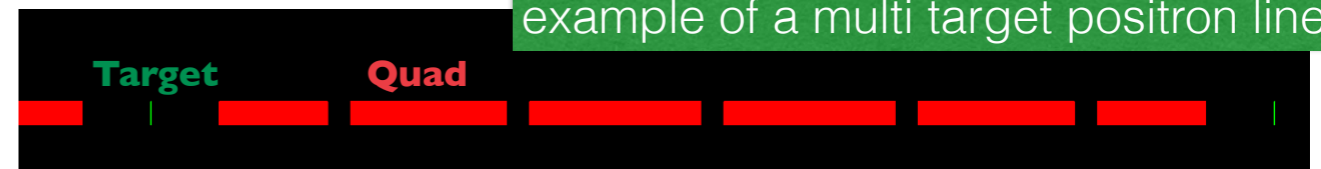


- ◆ The natural tool would seem Geant4, but to effectively use it with the possibility to vary all parameters some form of automatisisation (from machine optics to G4) is needed
- ◆ For this study, **MDISim** was used, which is a tool developed by H. Burkhardt @CERN for LHC/FCC studies, that enables to:
 - ✓ Read the machine optics
 - ✓ Import it (geometry + magnetic fields) in Geant4 (via gdml)

[REF](#)

example of a multi target positron line

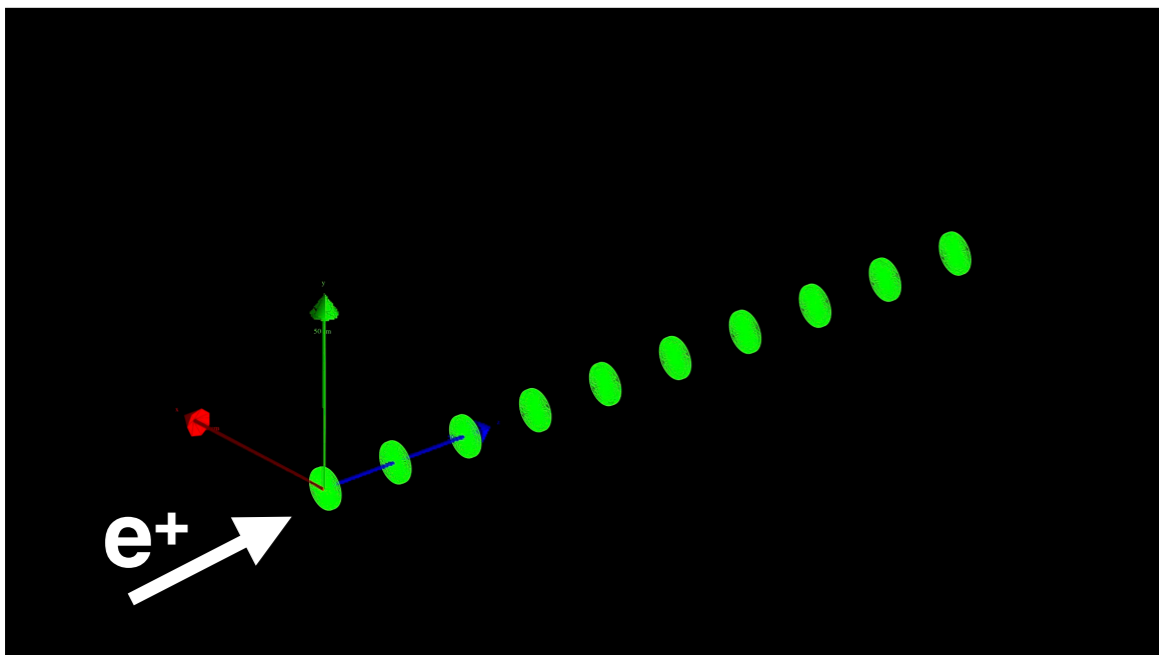
- ◆ Once in Geant4, a whole lot of studies can be performed!



THE MUON PRODUCTION ISSUE

◆ As a first approach, a “Single IP - Multi Target Line” was used

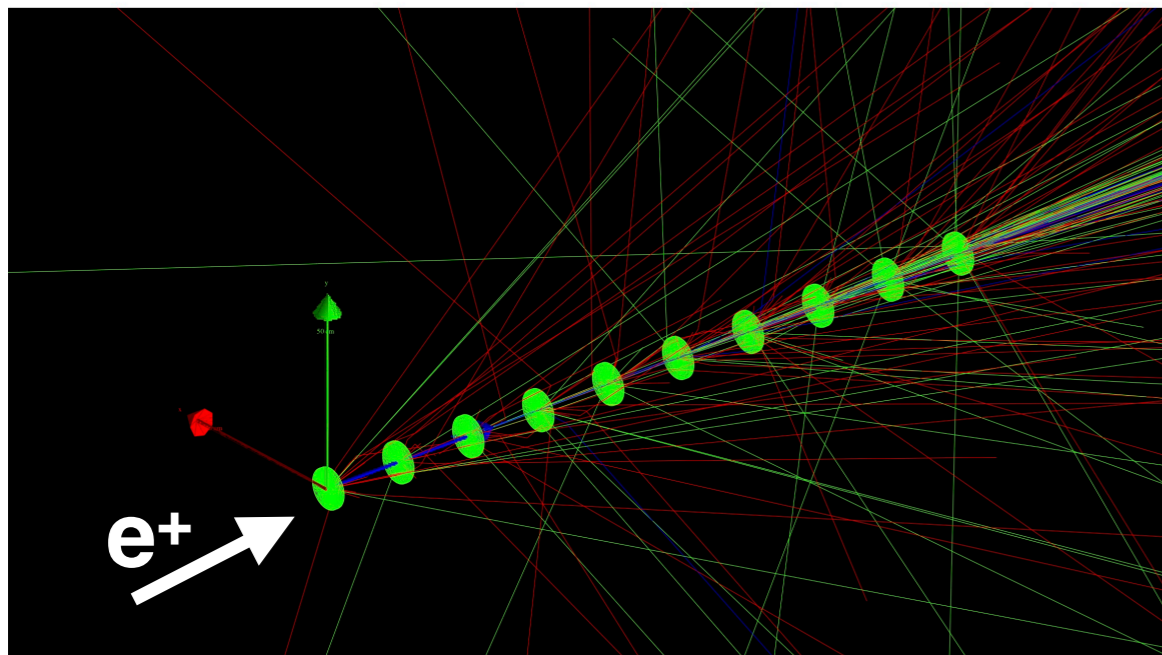
- ➔ 10 Berillium targets
- ➔ 1 cm thick each
- ➔ 2 m total z length



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- ◆ A primary beam of positrons is fired, $E=45\text{GeV}$ by default
- ◆ Particles are tracked along the line, taking into account all relevant processes
 - ✓ Bremsstrahlung
 - ✓ Ionisation
 - ✓ Multiple scattering
 - ✓ Secondaries creation
 - ✓ (...)

THE MUON PRODUCTION ISSUE

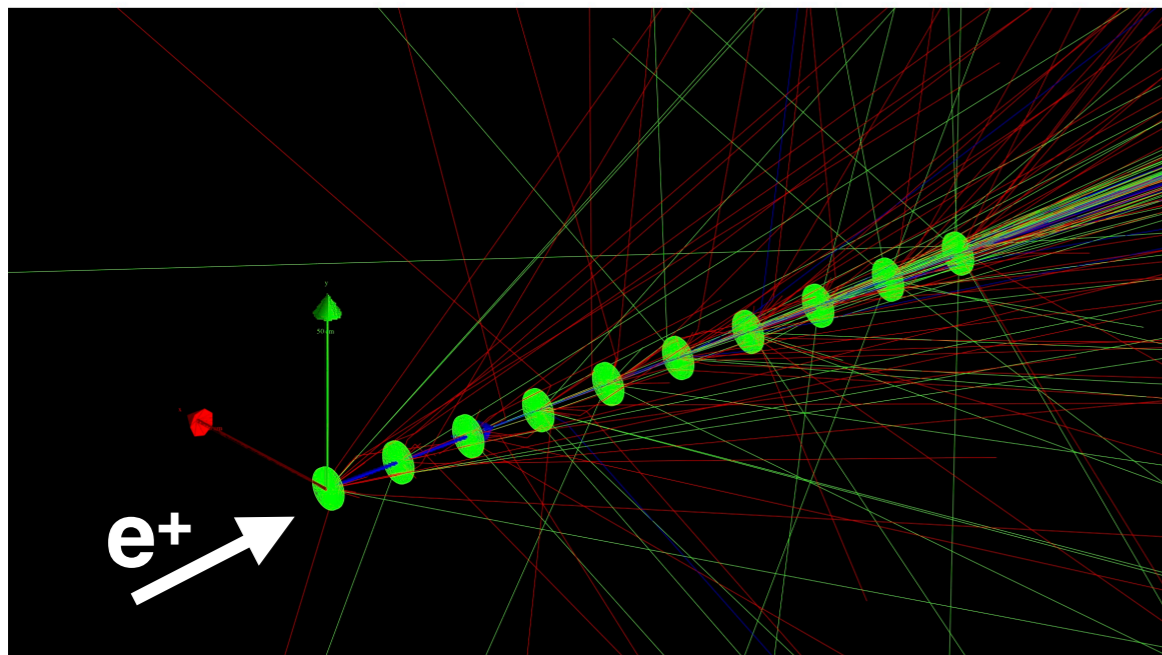
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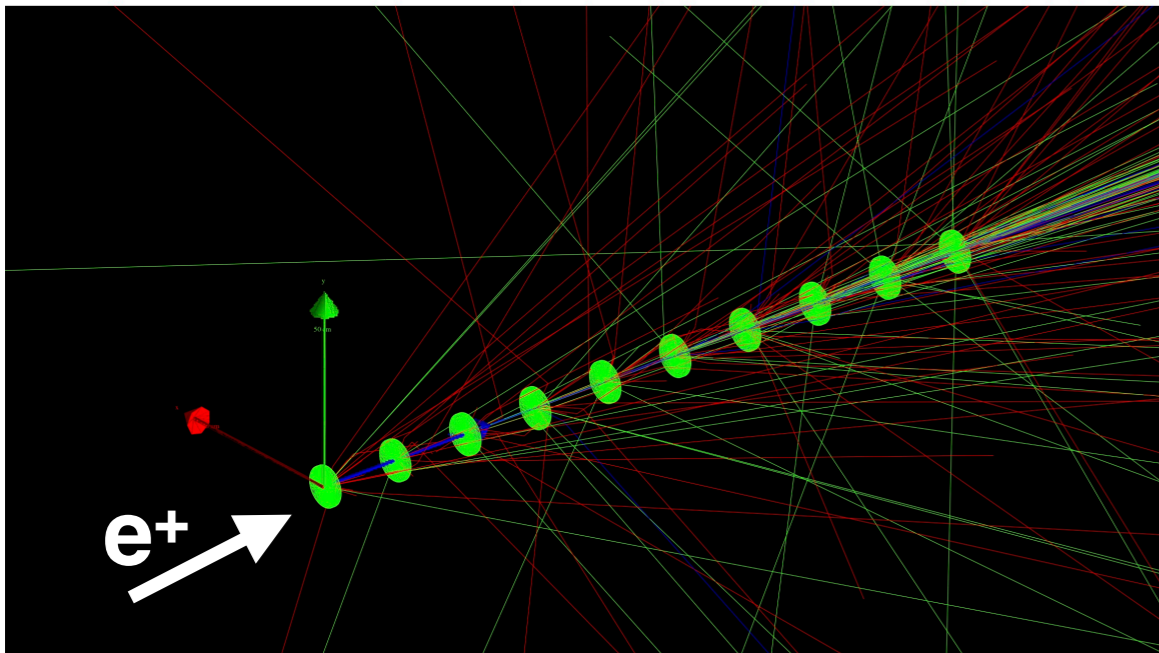


Aim of the study:

How **many muons** are produced?
Which **quality** of the beam?
How about the **positron degradation**?

▶ THE MUON PRODUCTION ISSUE

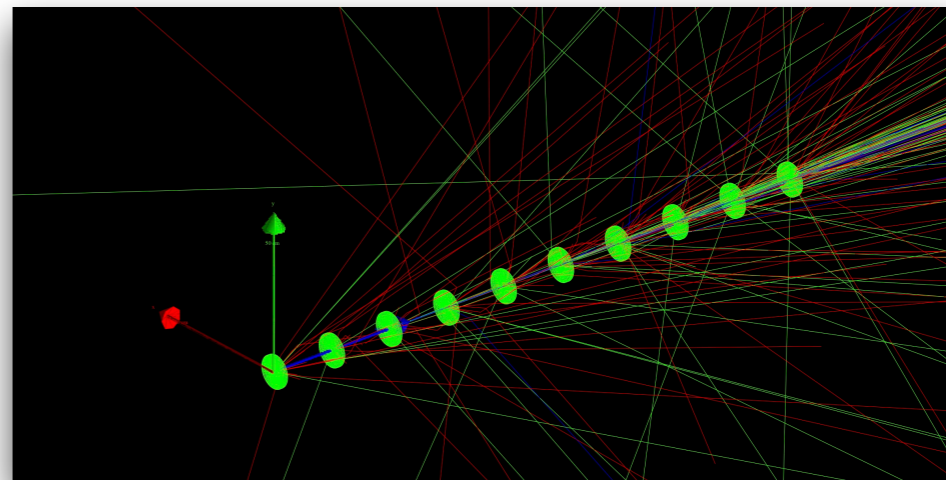
◆ **CAVEAT:** the muon production **cross section** has been artificially **biased**



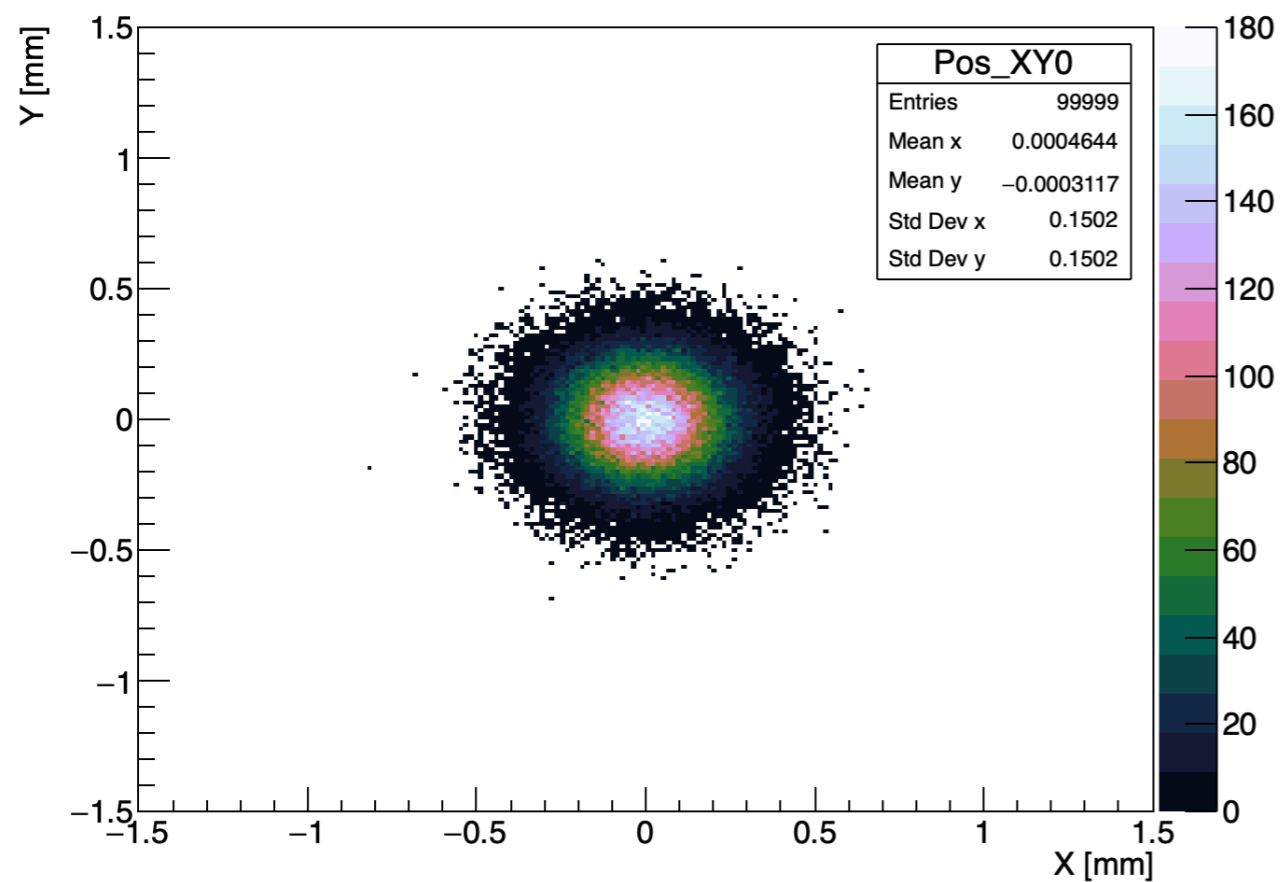
- ◆ To see enough muons in a reasonable amount of CPU time
- ◆ $\sim x10^3$ factor, then properly taken into account in following plots
- ◆ Small ($\sim\%$) effect on positrons survival



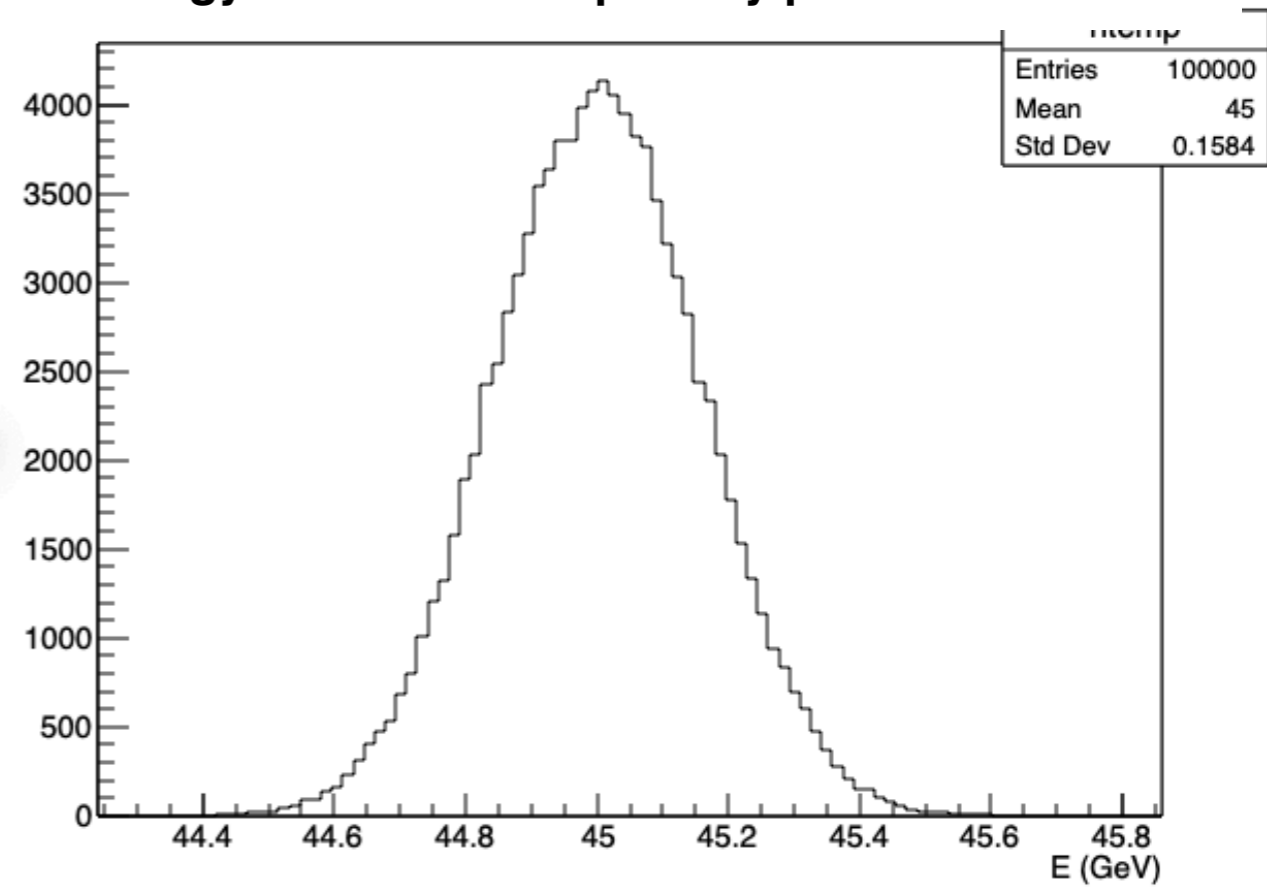
SIMULATION RESULTS



Spot size of primary positron beam

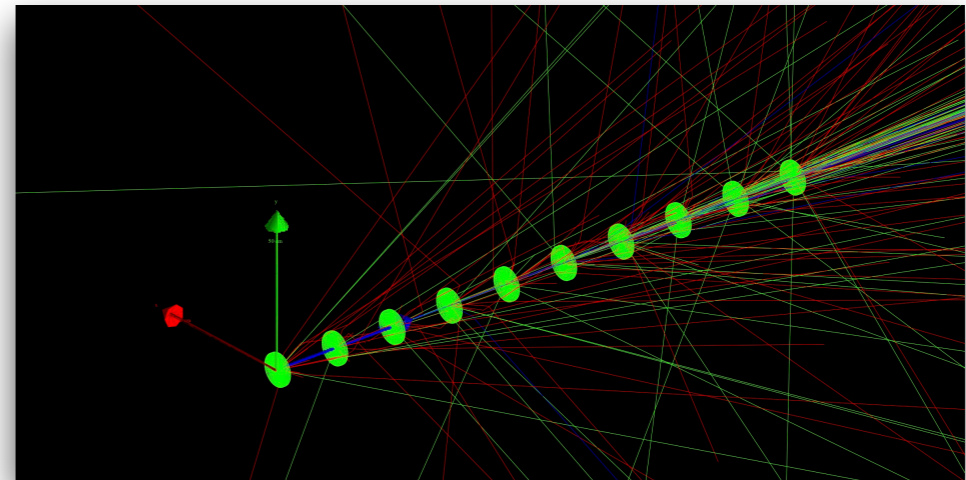


Energy distribution of primary positron beam



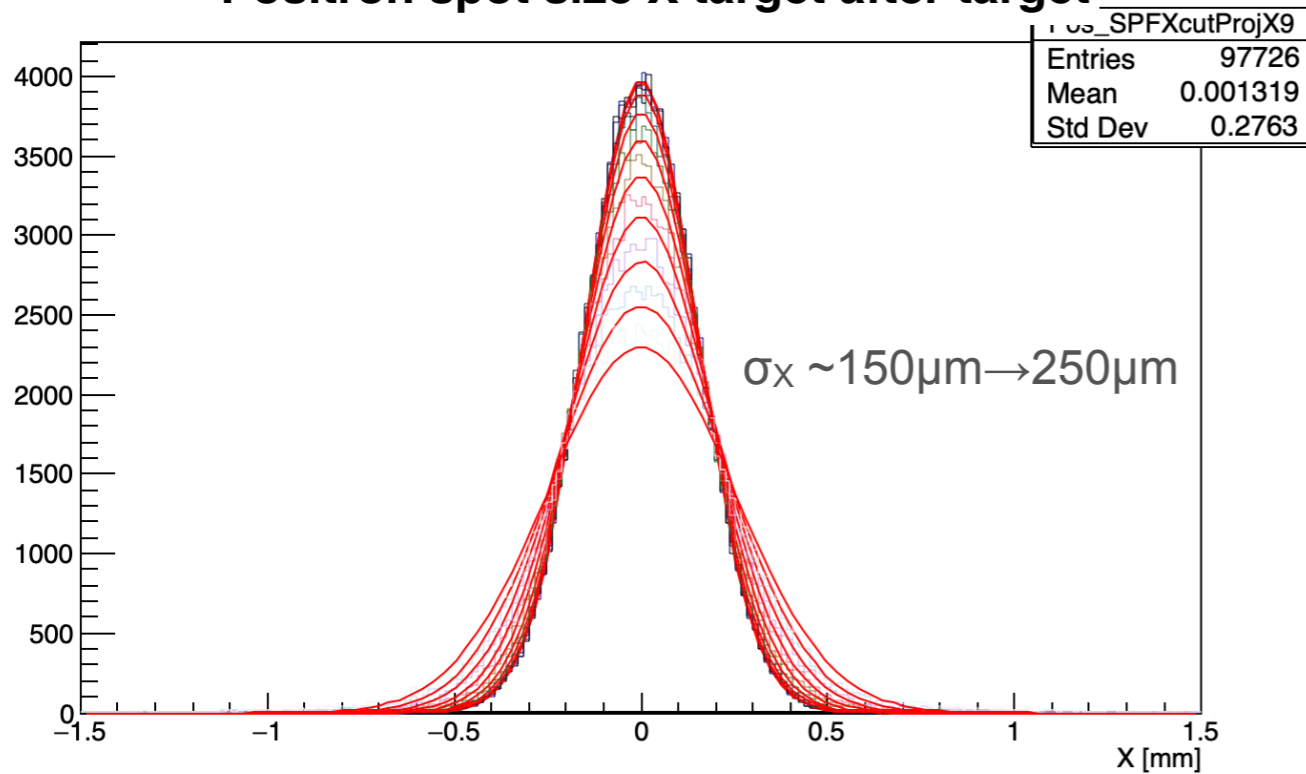


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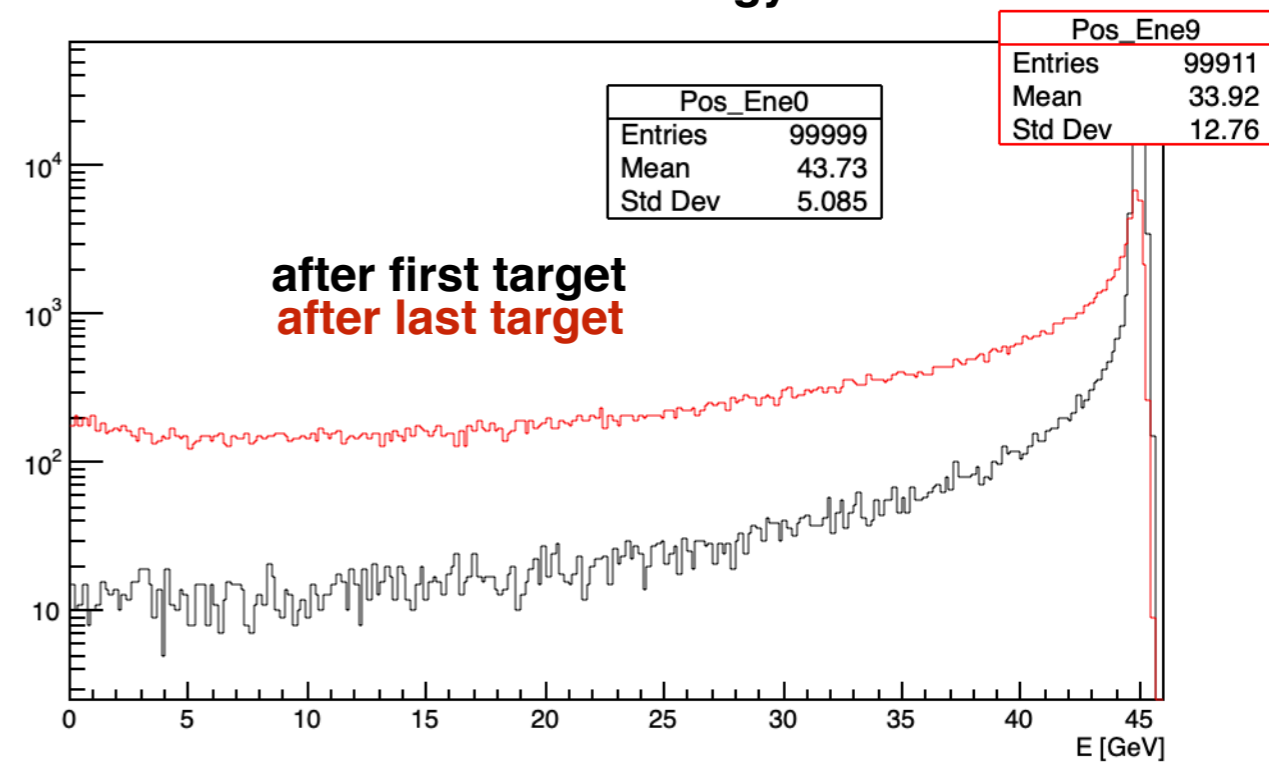


- ◆ 45 GeV positrons
- ◆ 10x1cm Be targets

Positron spot size X target after target

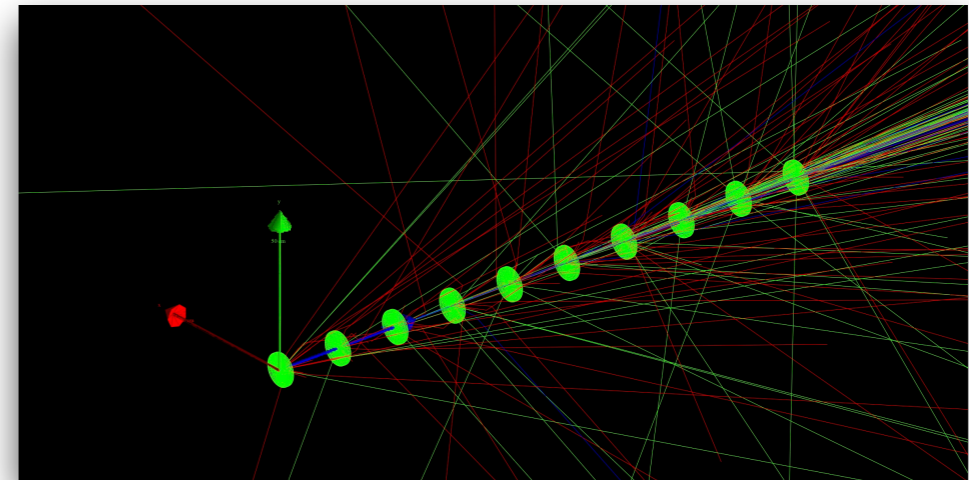


Positron energy



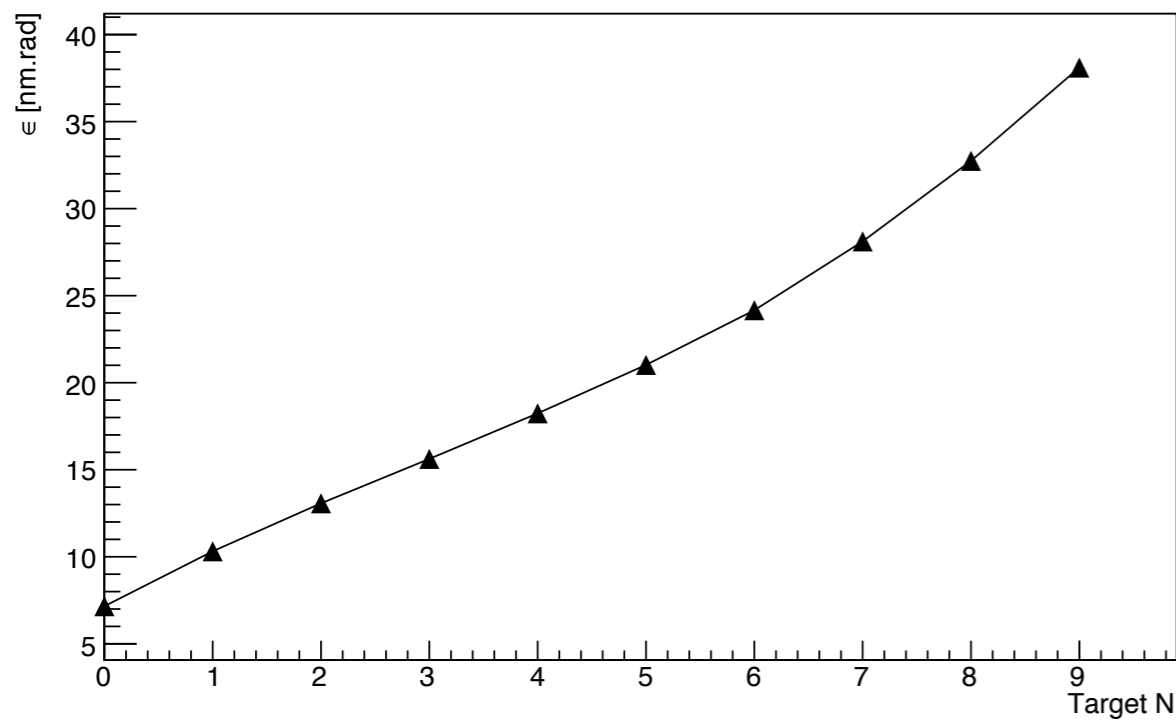


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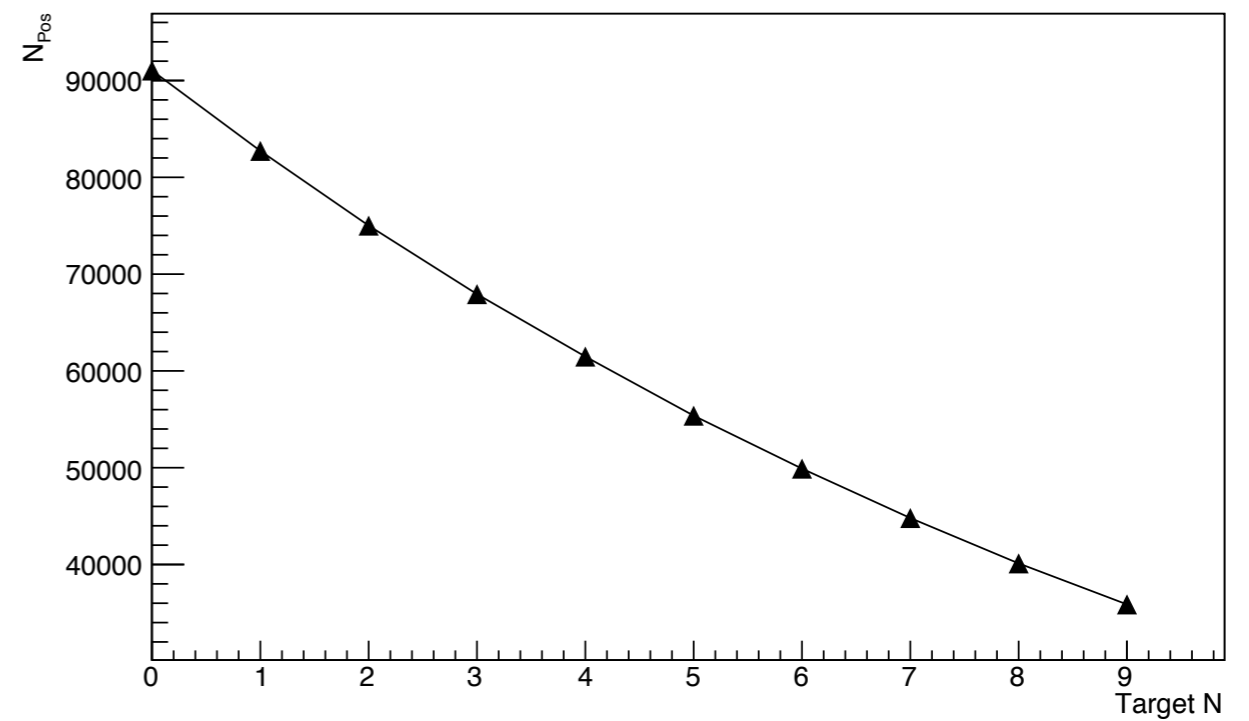


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Positron horizontal emittance



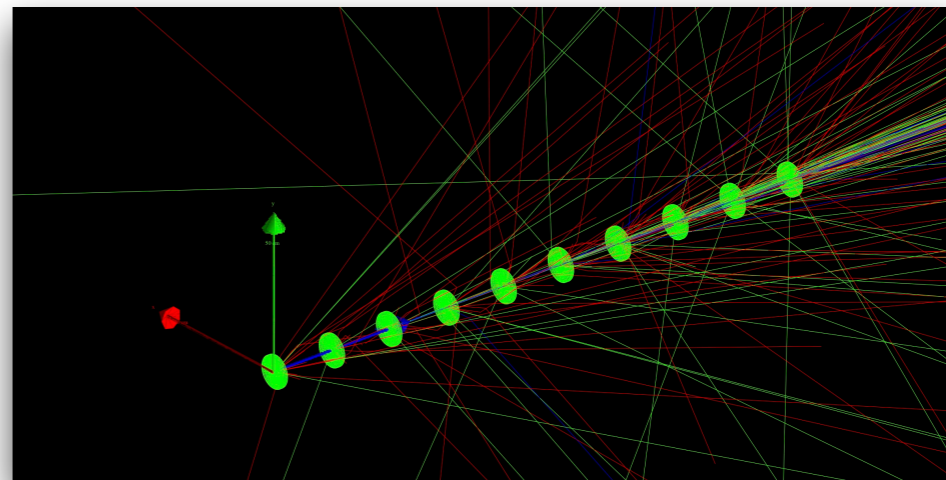
Positron survival (+-5% en. acc.)



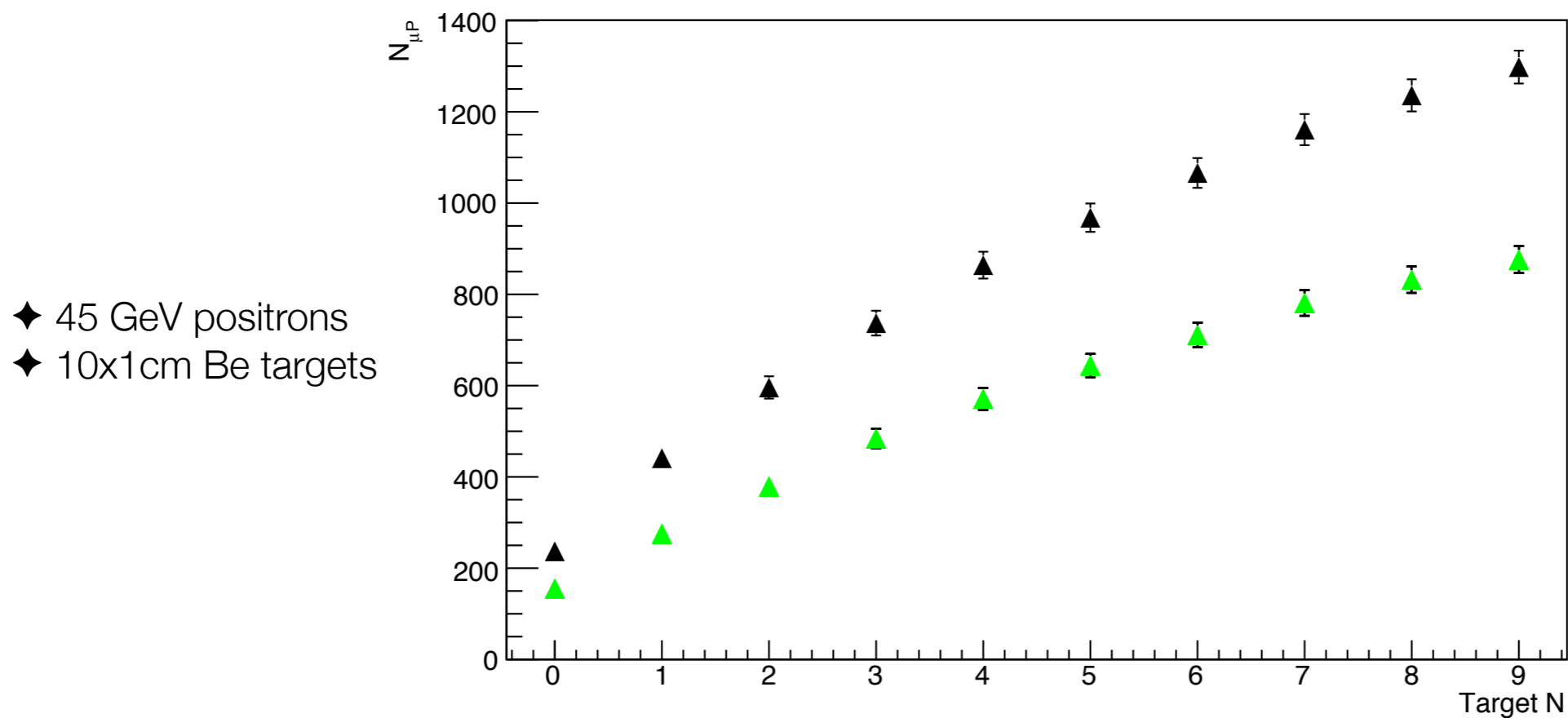
More than the 60% of the primary positron beam is lost after 10 targets



SIMULATION RESULTS



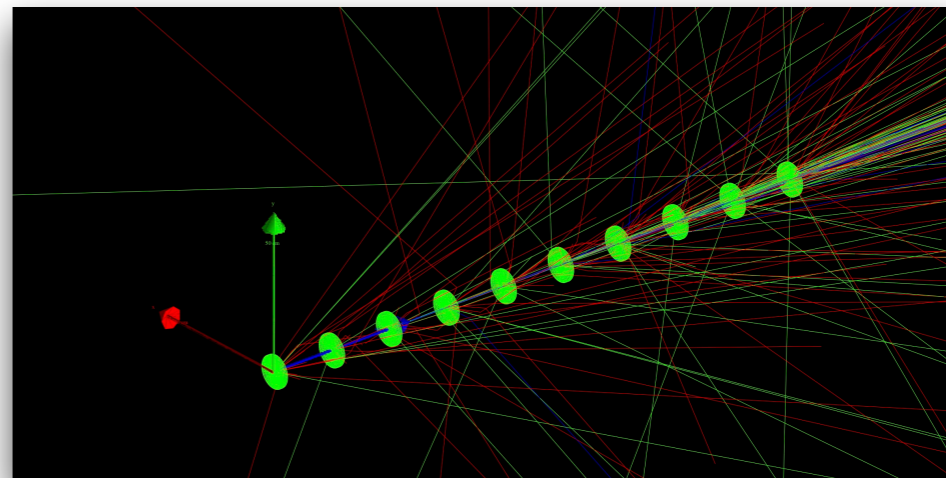
Final number of accumulated MuP vs target



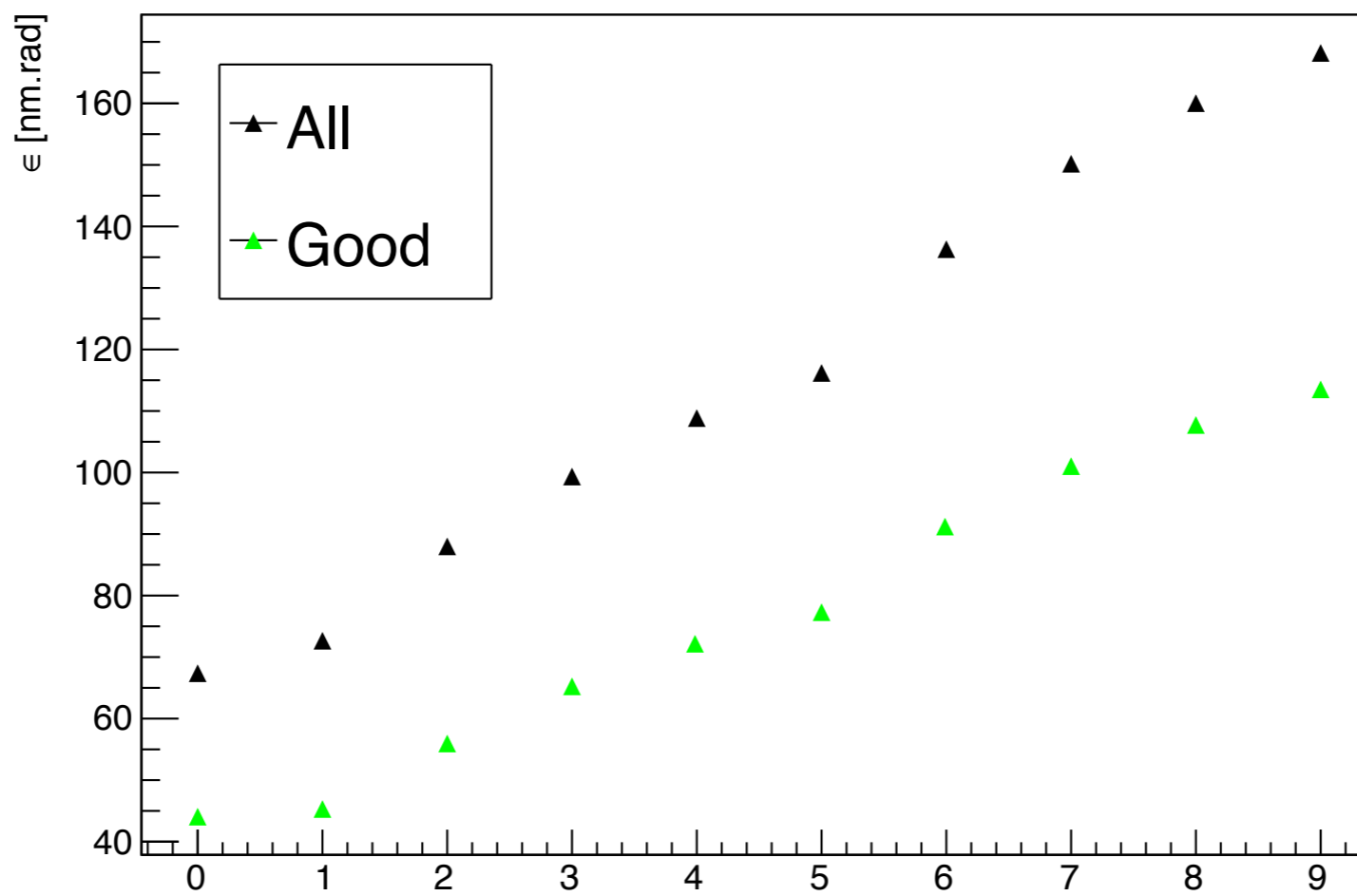
**Mu energy acceptance
+8-12%**
(see Blanco's talk)



SIMULATION RESULTS



Muon RMS Emittance



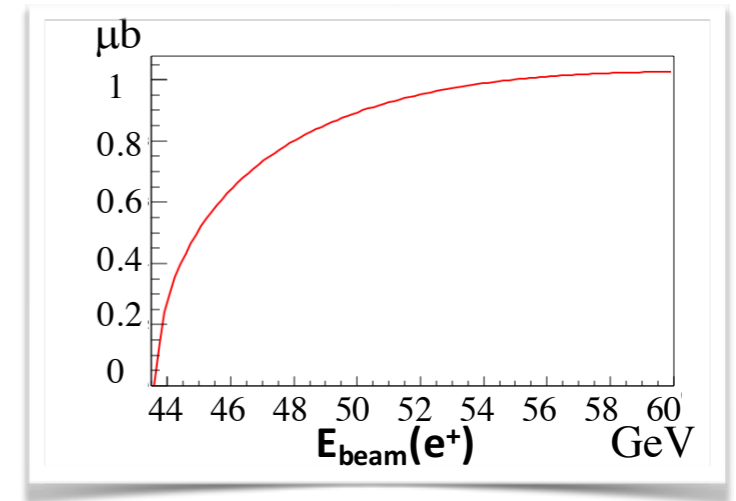
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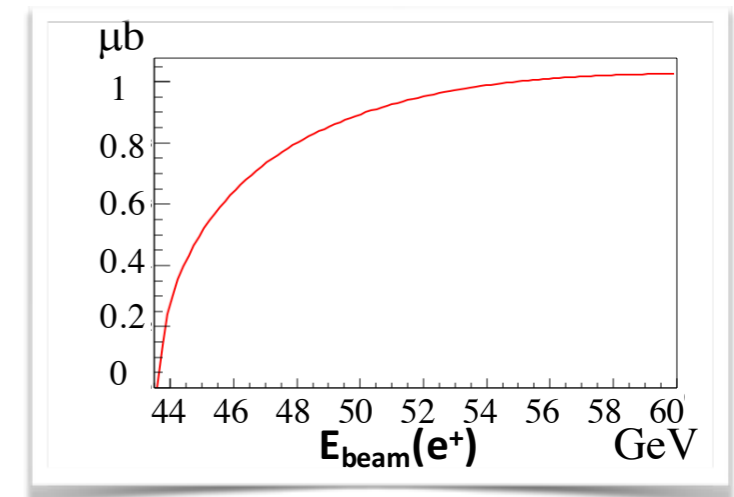
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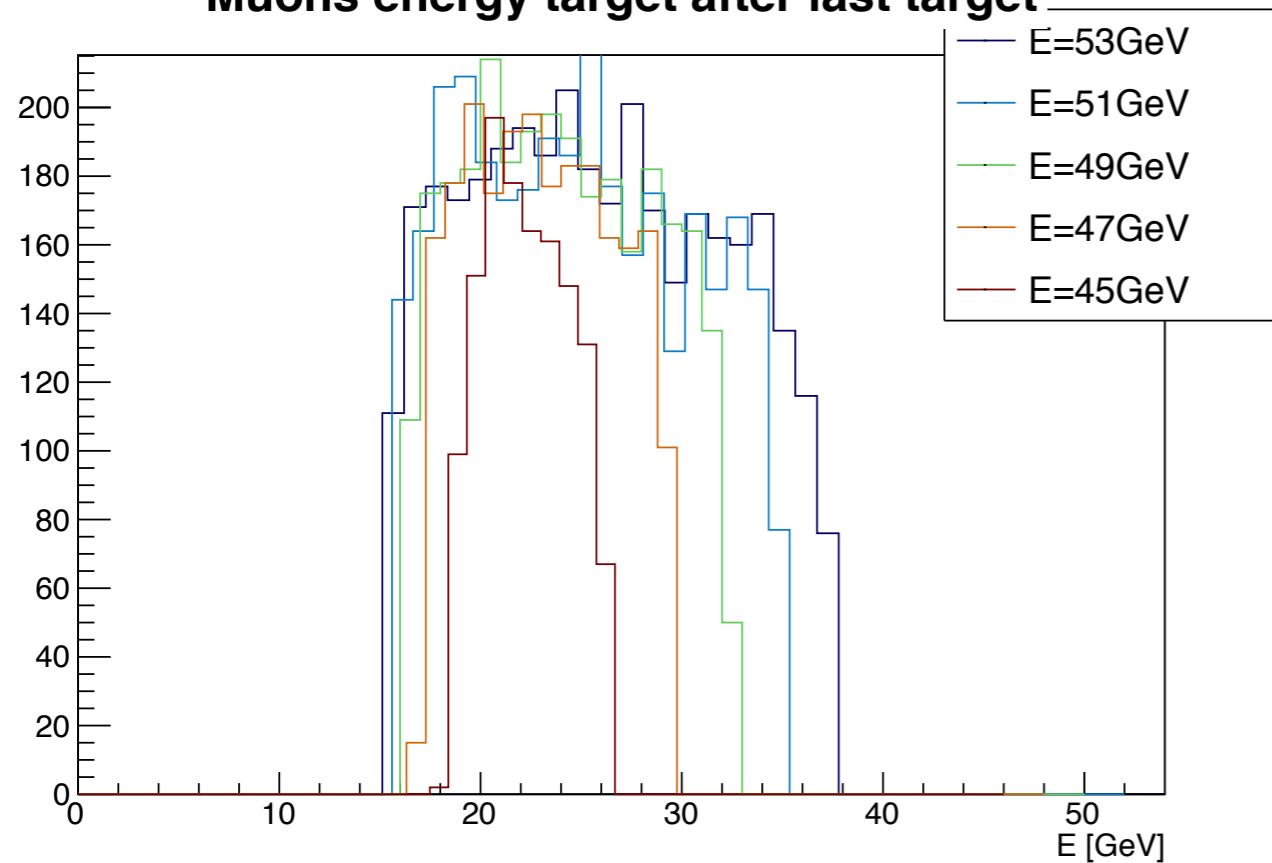


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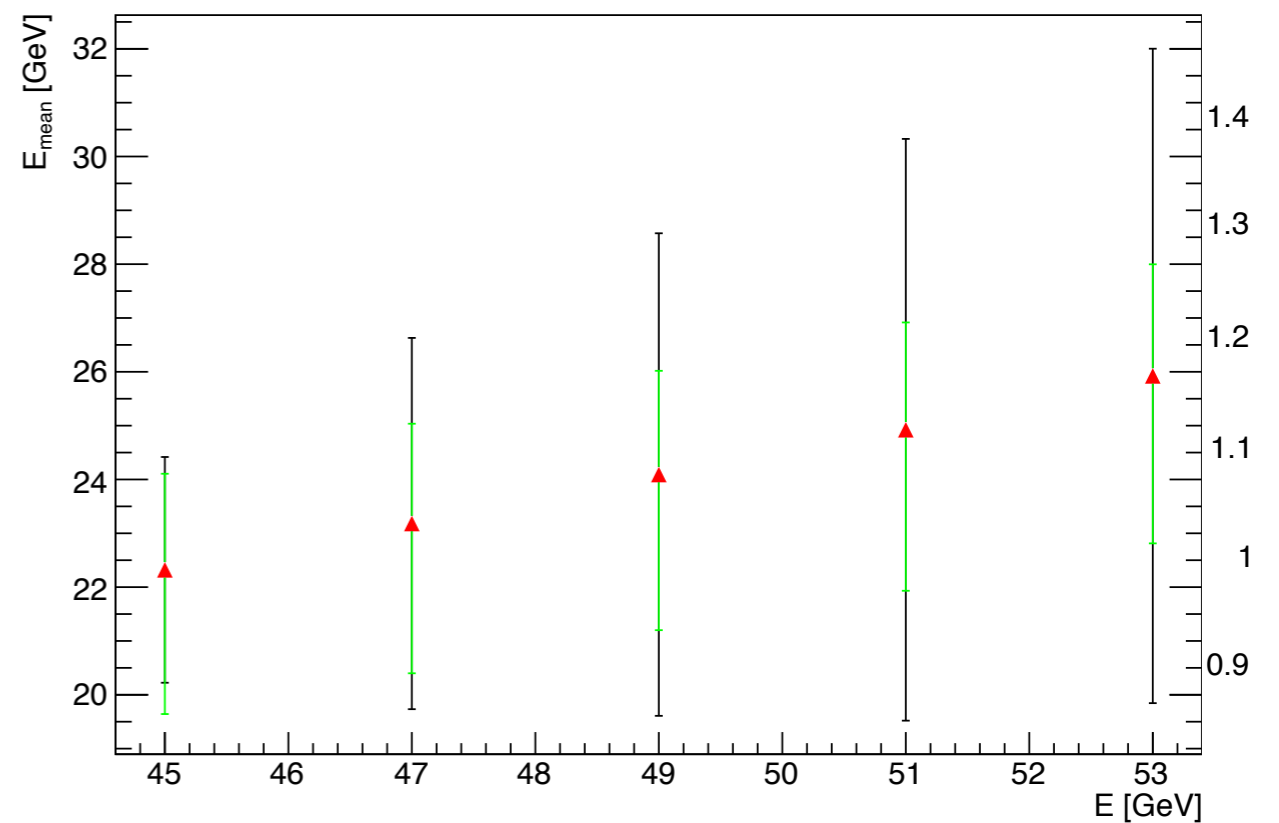
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Muons energy target after last target



Mean energy (+- RMS) of muons after last target

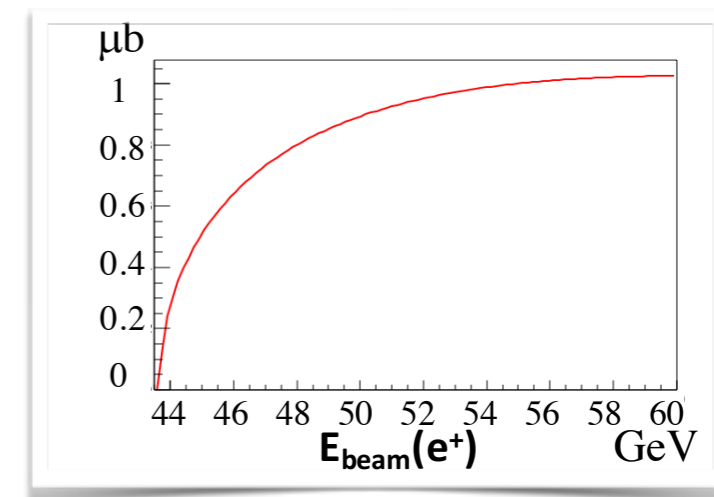


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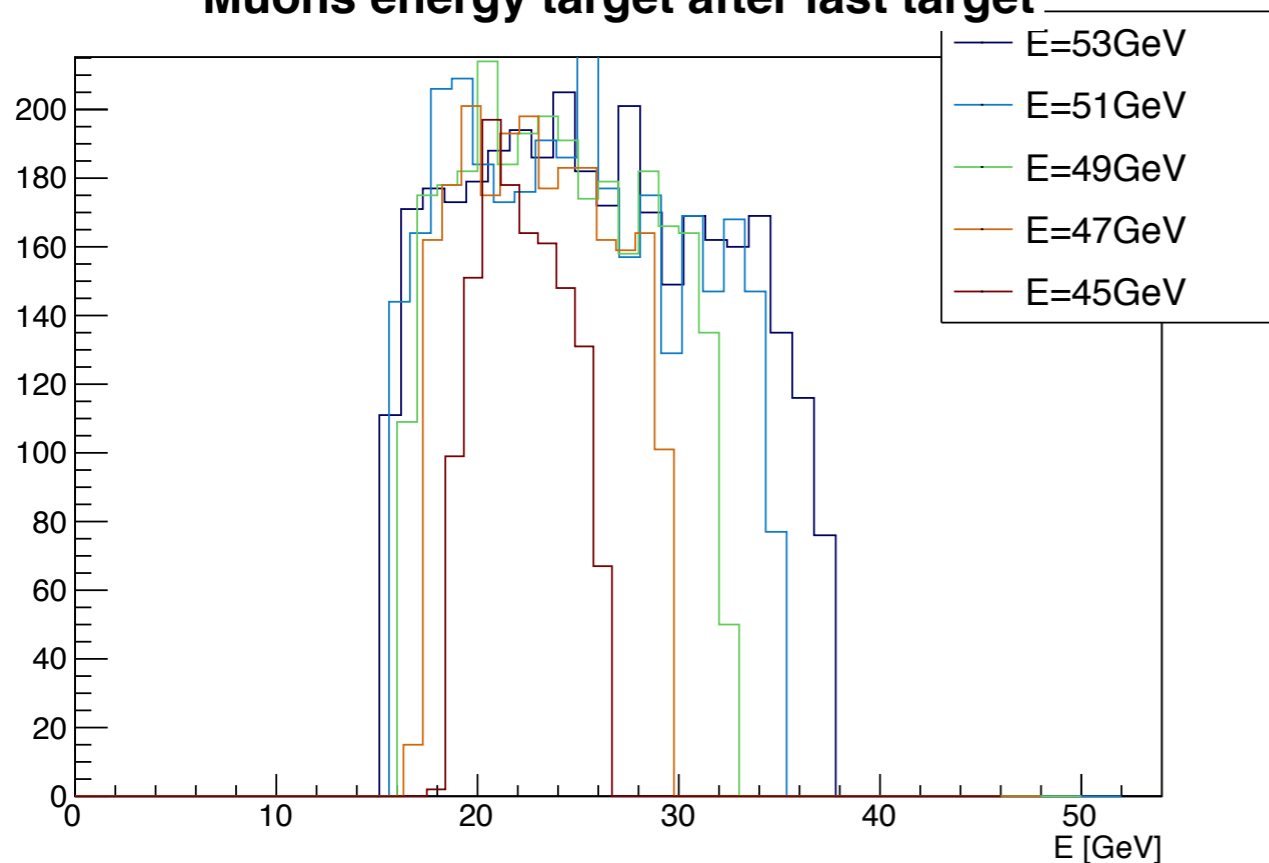


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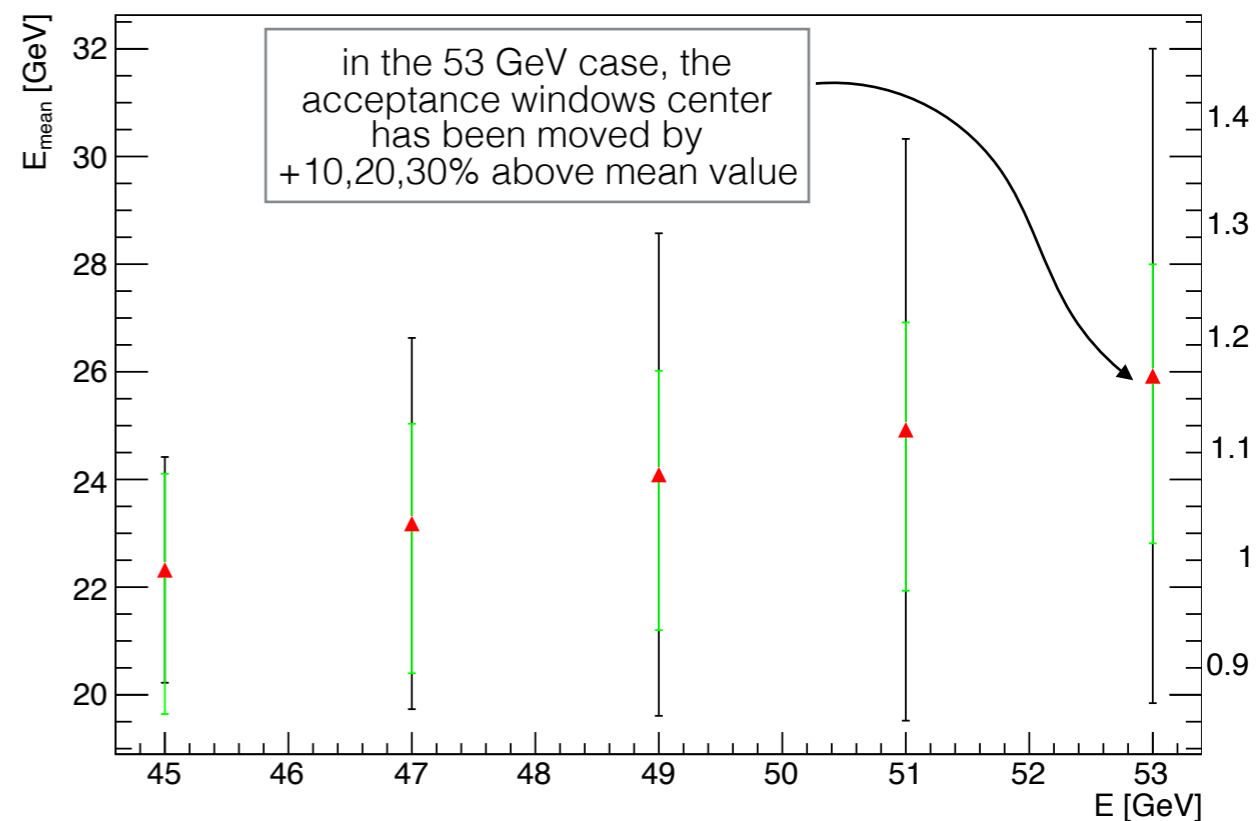
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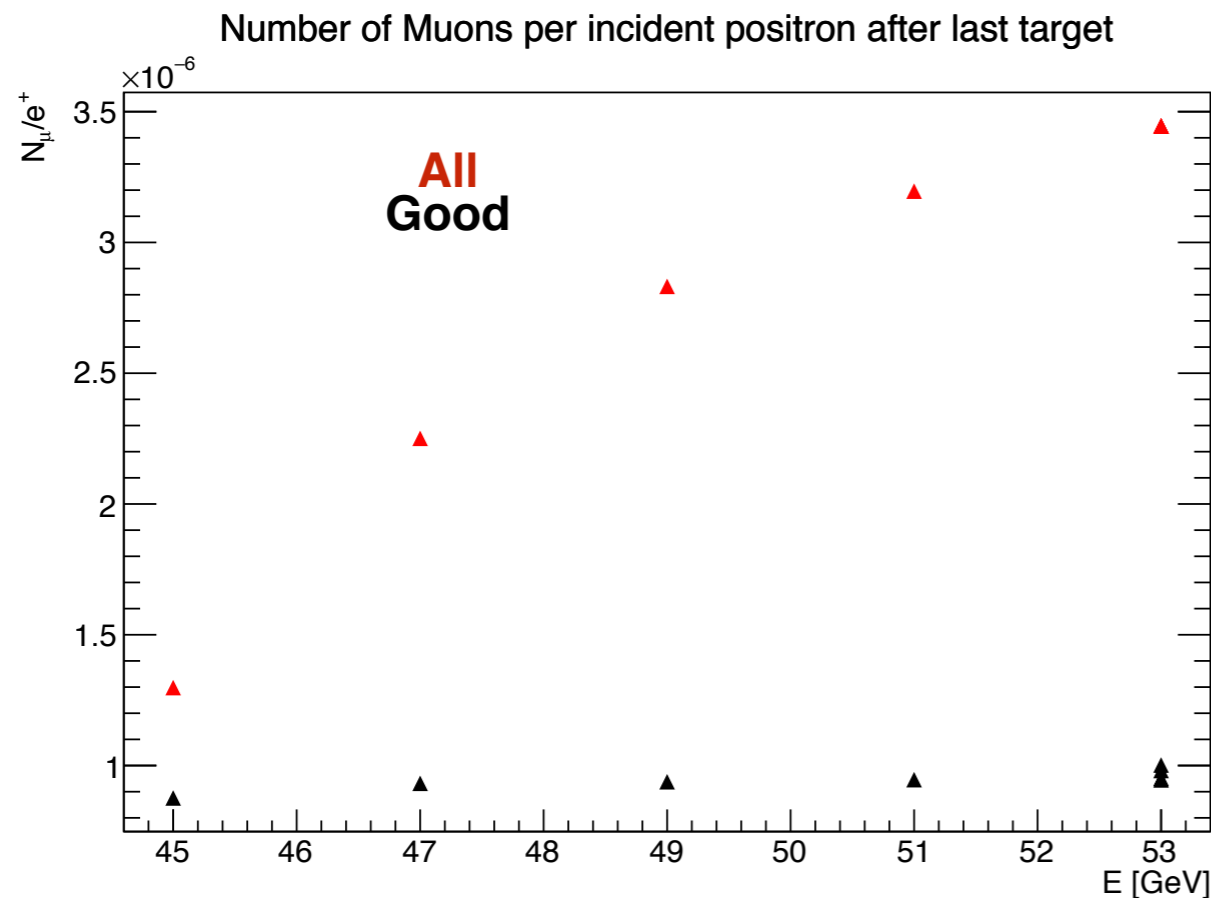
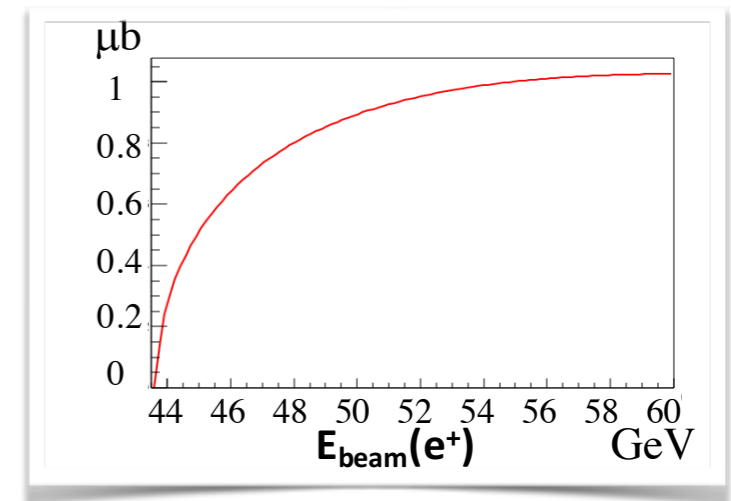


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SIMULATION RESULTS

What happens if we rise the beam energy?



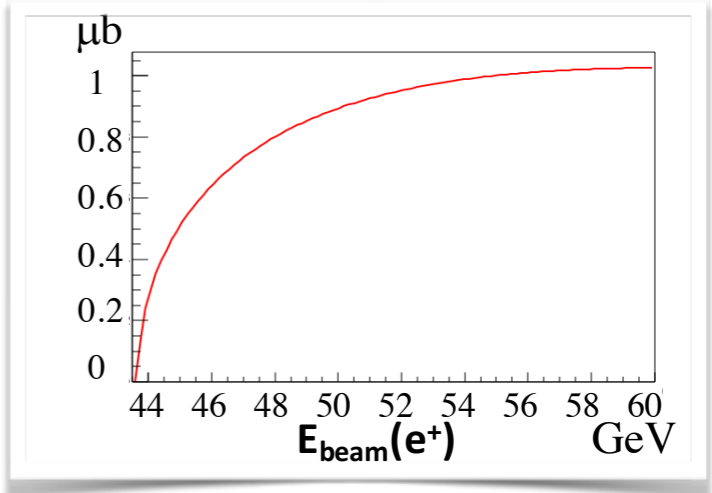
- ➔ Rising the energy, there is a significant **increase** in the total **number of produced muons**
- ➔ The increase is much less evident if we select “good” muons

- ◆ 45 GeV positrons
- ◆ 10x1cm Be targets

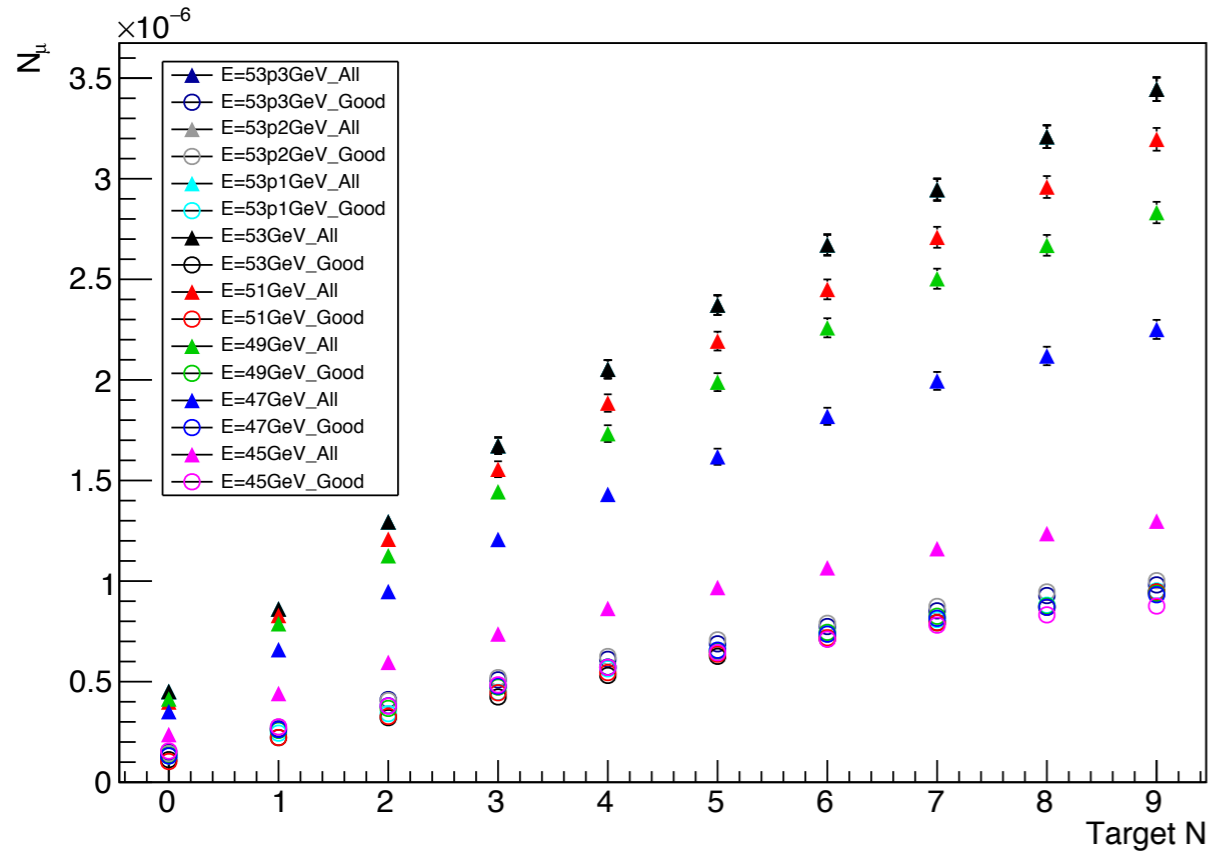


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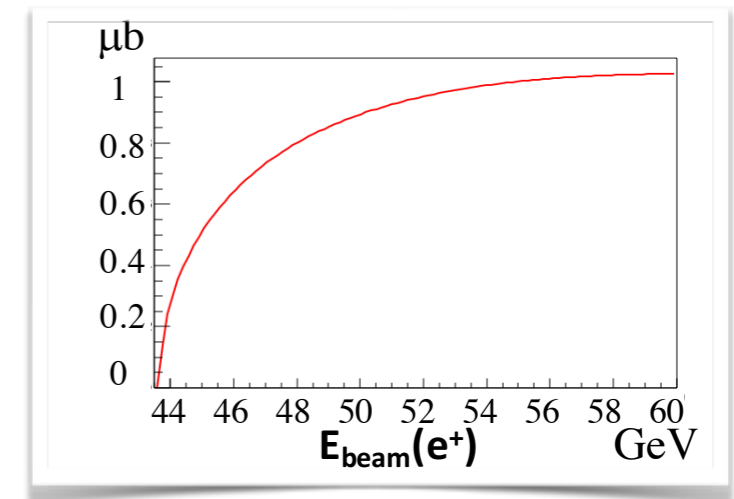
Total number of muons produced after each target per incident positron



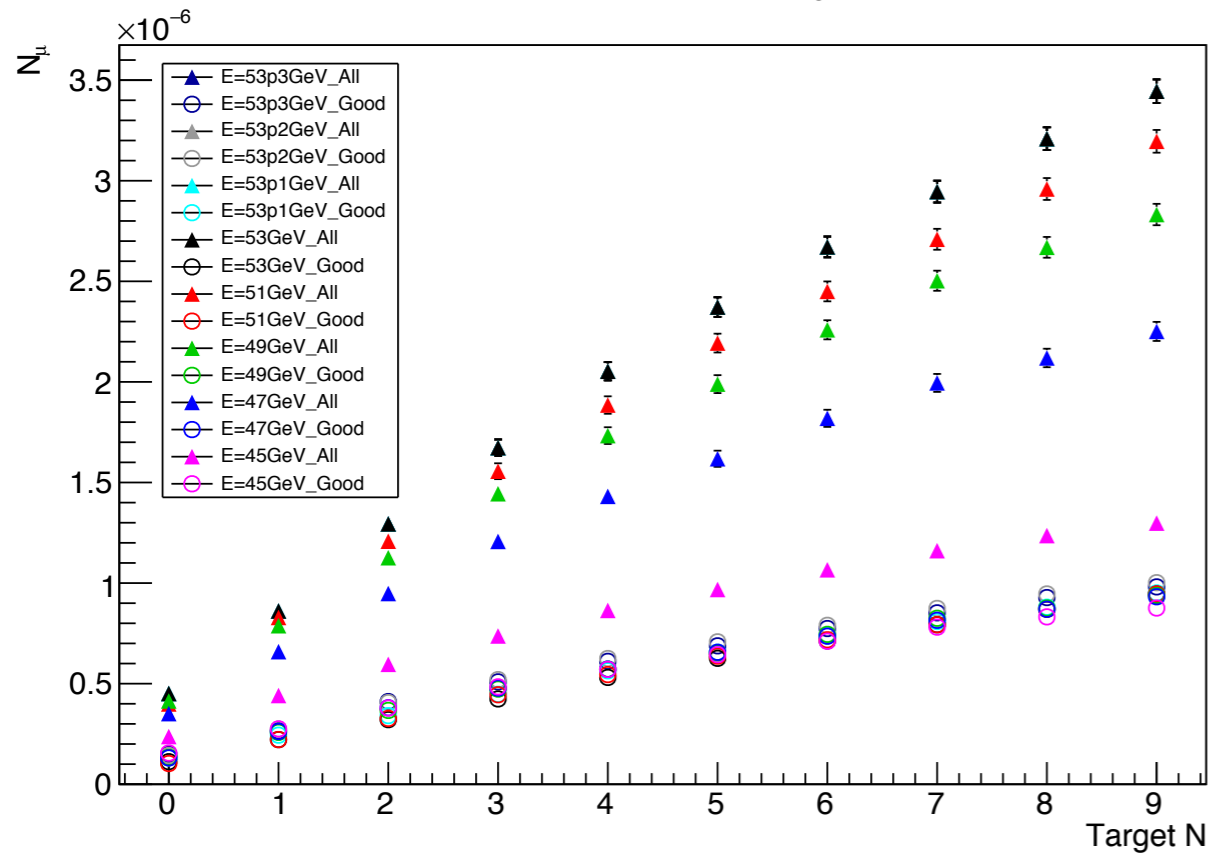


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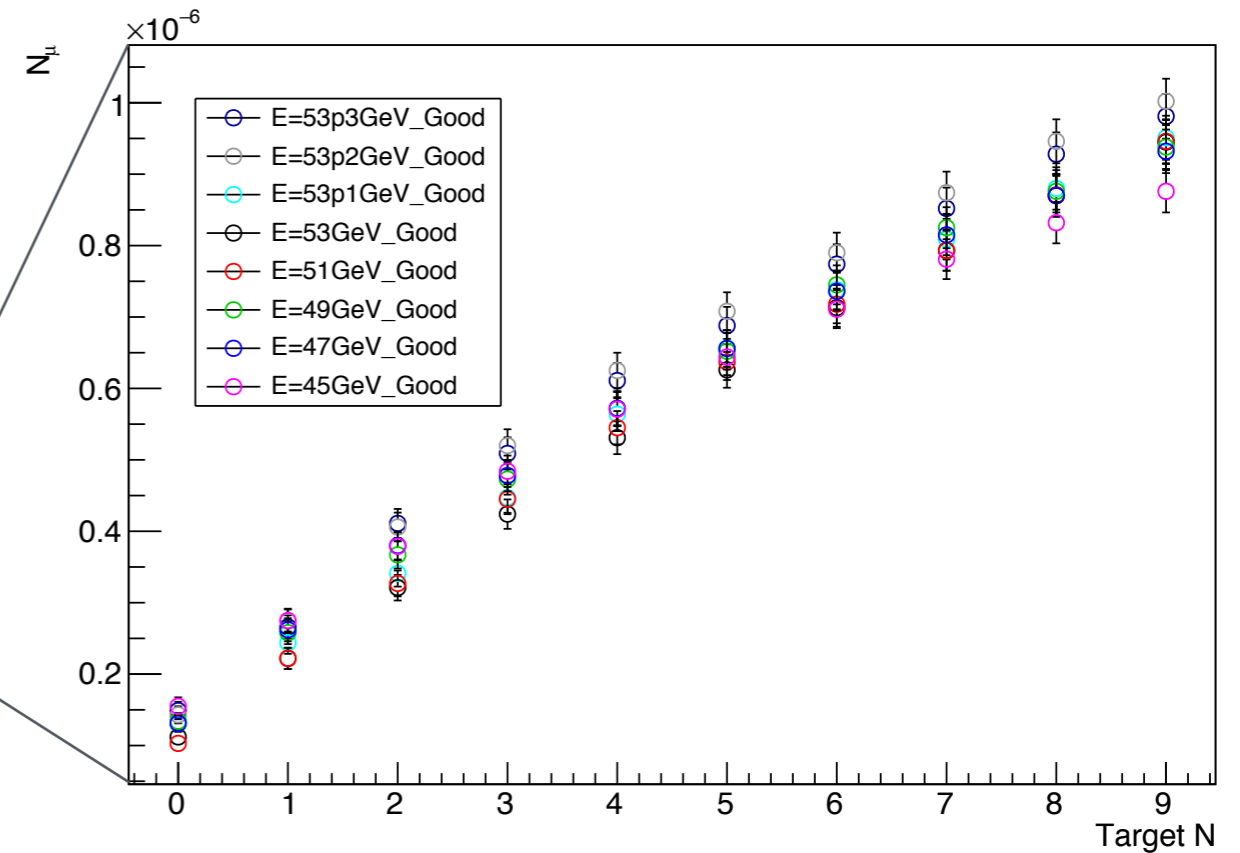
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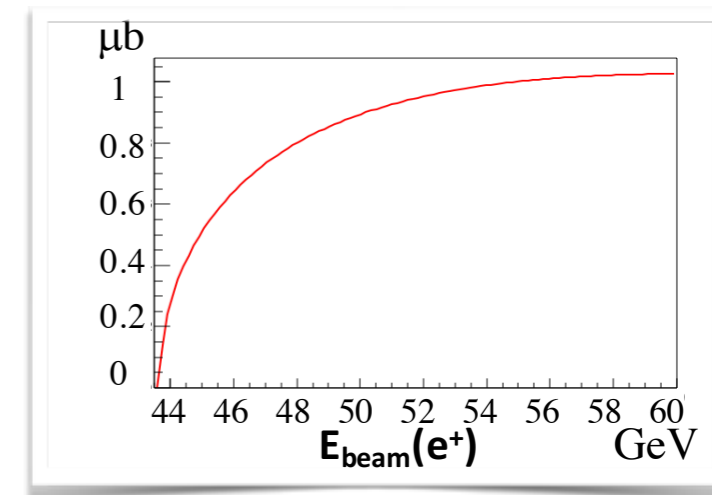
Number of good muons (within energy acceptance) produced after each target per incident positron



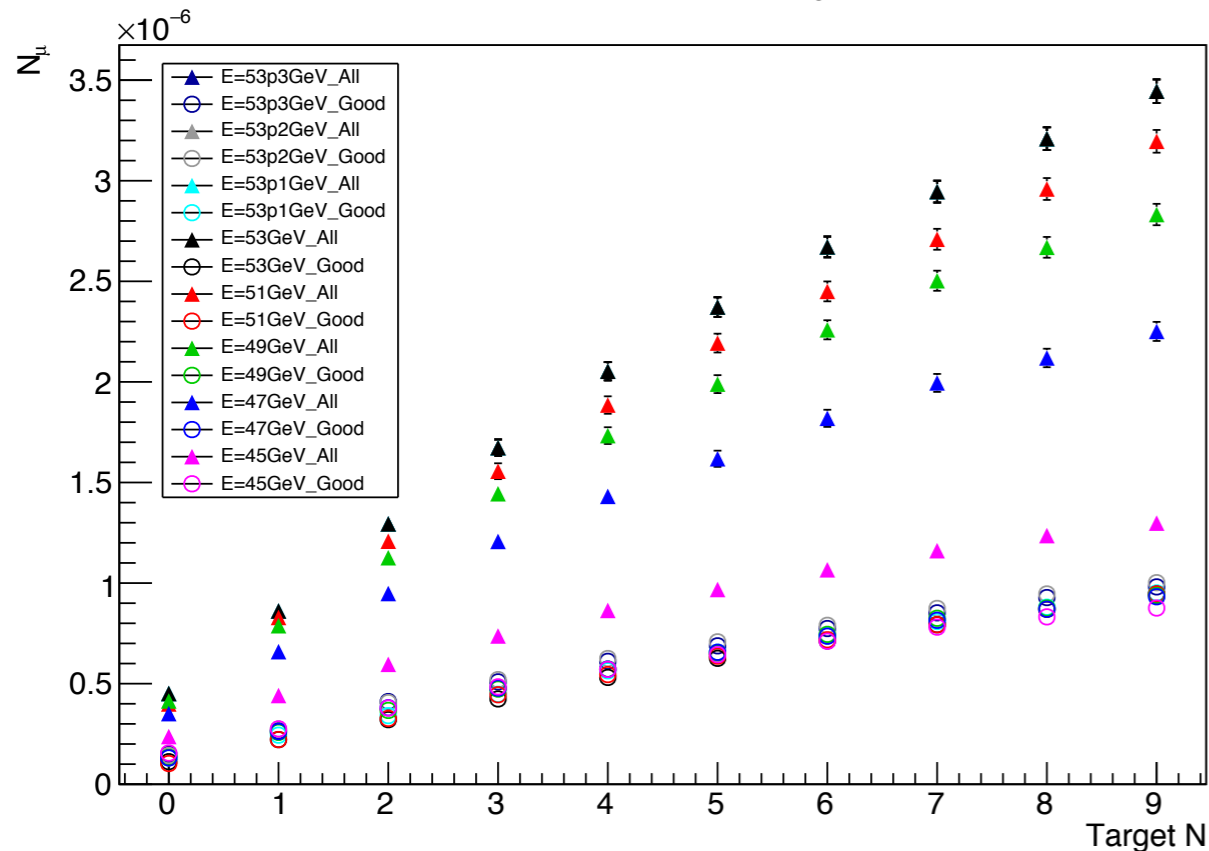


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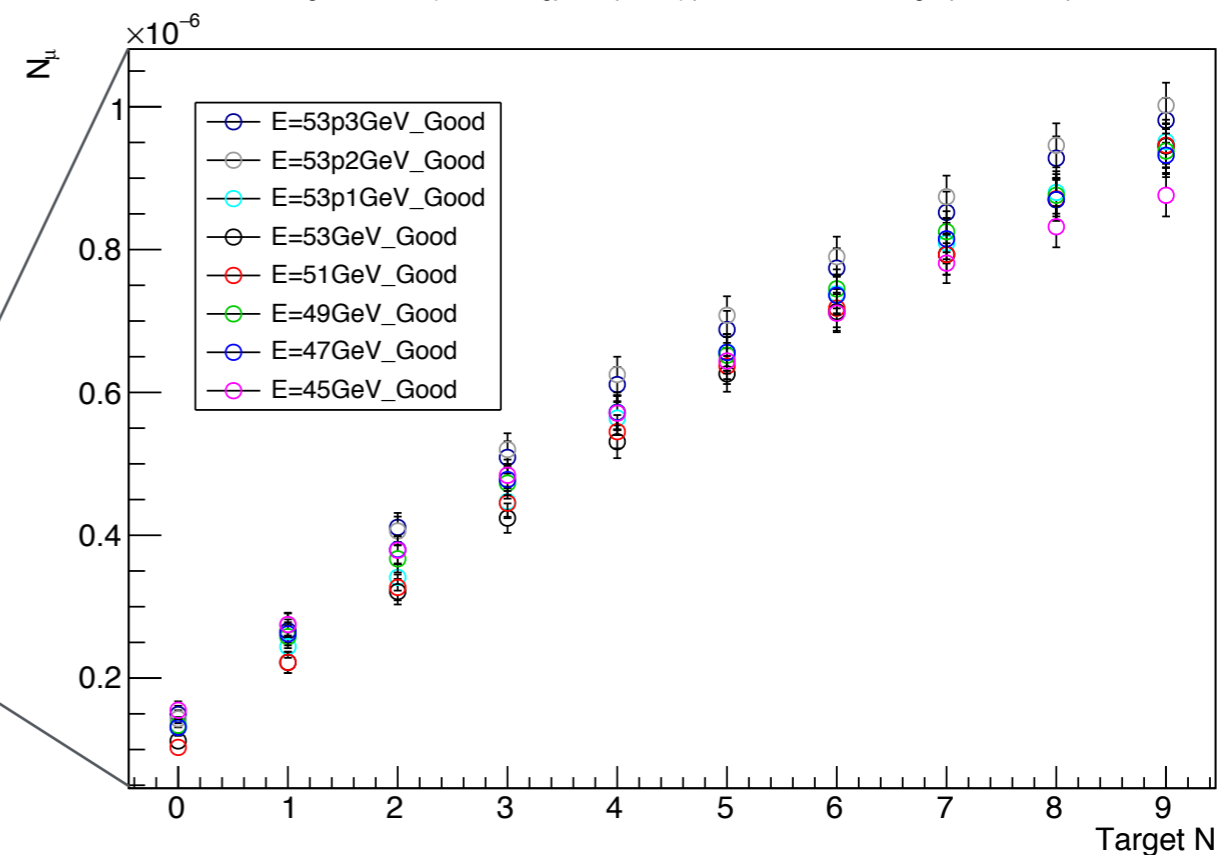
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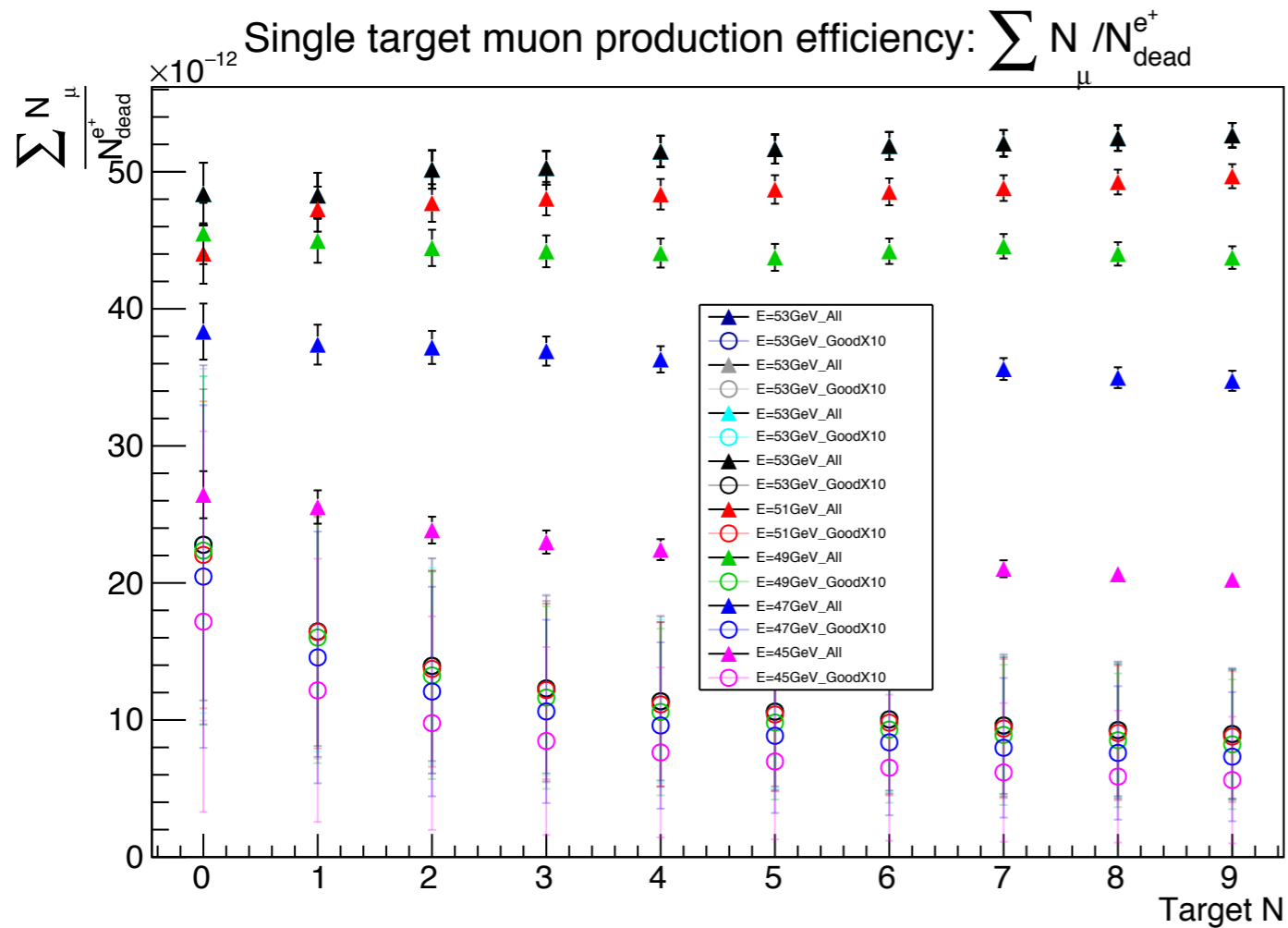
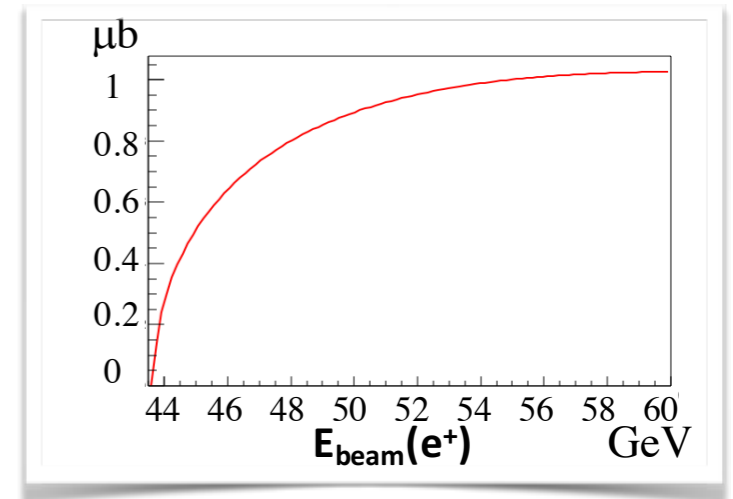


➔ Best configuration @last target:
- E=53GeV
- Collection window centred at 26.3 GeV (23.2-28.4)
➔ ~10% increase



SIMULATION RESULTS

What happens if we rise the beam energy?



Number of muons alive/good after the N-target vs number of positrons put outside energy acceptance by the N-target

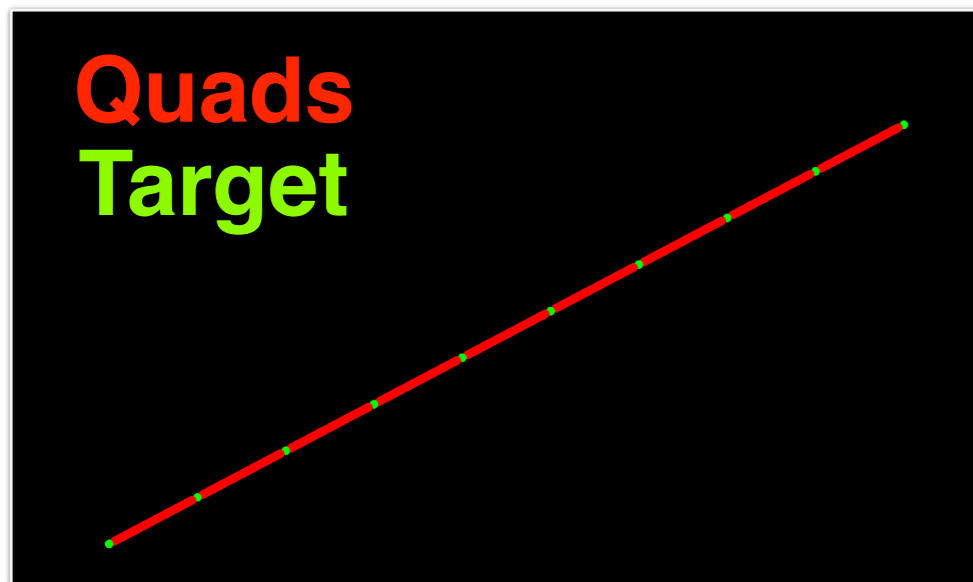
➔ **Tradeoff** between amount of muons produced and positron beam degradation



MULTI IP MULTI TARGET LINE

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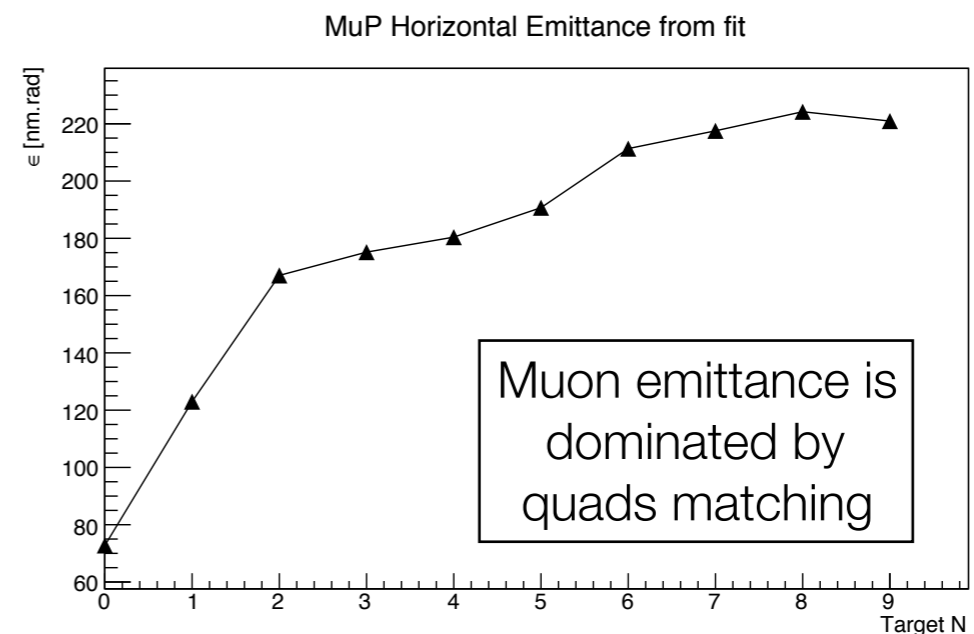
◆ The software tool allows to import any optics line in Geant4 to perform the same study



- ➔ 10 Beryllium targets
- ➔ 3 mm thick each
- ➔ 45 m total z length

◆ **Powerful.. but complicated!**

◆ The optics contribution becomes crucial





POWER LOAD CONSIDERATIONS

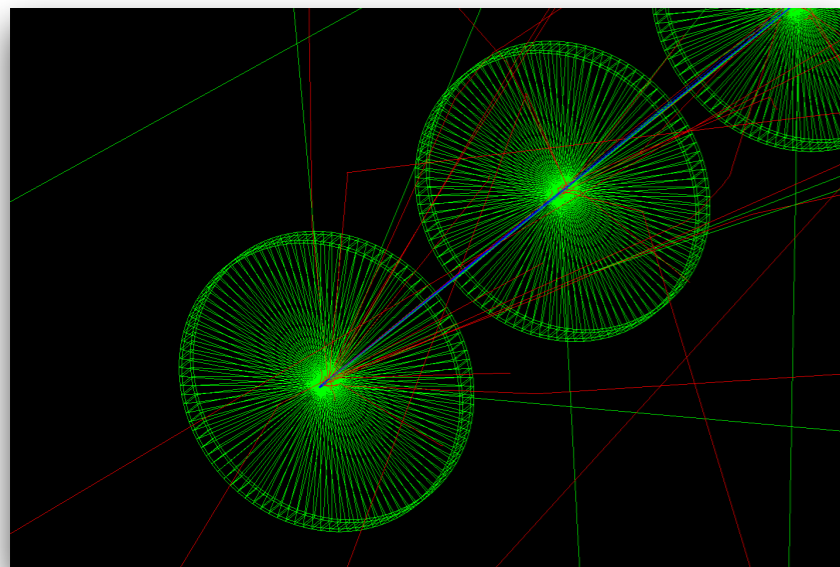




POWER LOAD CONSIDERATIONS

- ◆ To compensate for the low cross section, a huge amount of ~ 45 GeV positrons must collide with the target

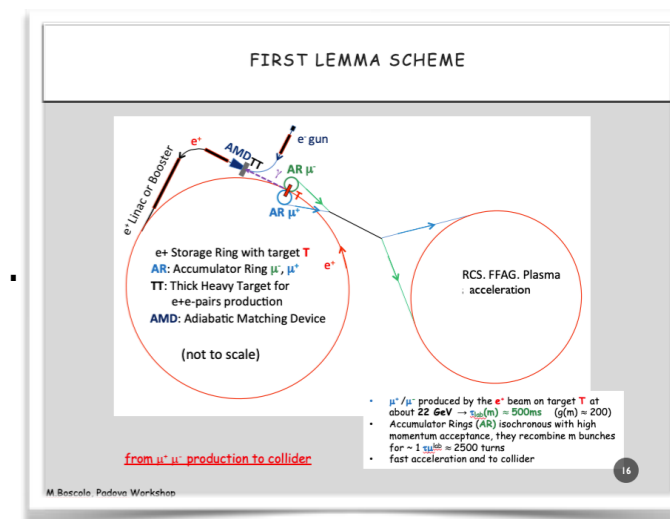
→ **power deposition** and **target temperature** must be kept under control



- ◆ The detailed study of power deposition had been developed in the “LEMMA-0 scheme”

- ◆ Energy deposition is simulated with FLUKA, and dedicated codes are used to simulate heat propagation, dissipation, steady state temperature...

Ref: “Theoretical modeling for the thermal stability of solid targets in LEMMA muon collider” - G. Cesarini, HiRadMat 2019

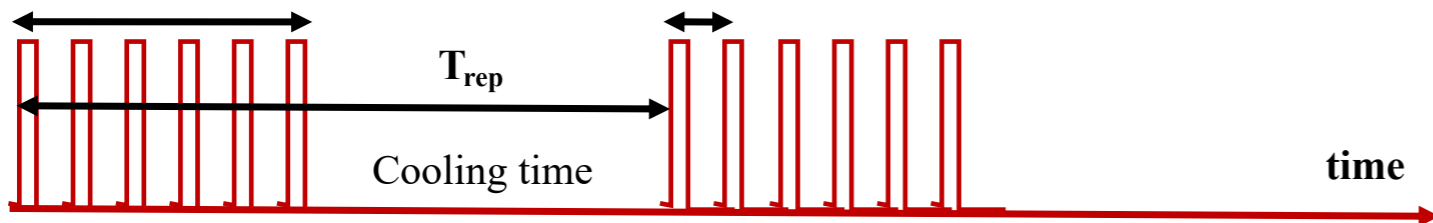
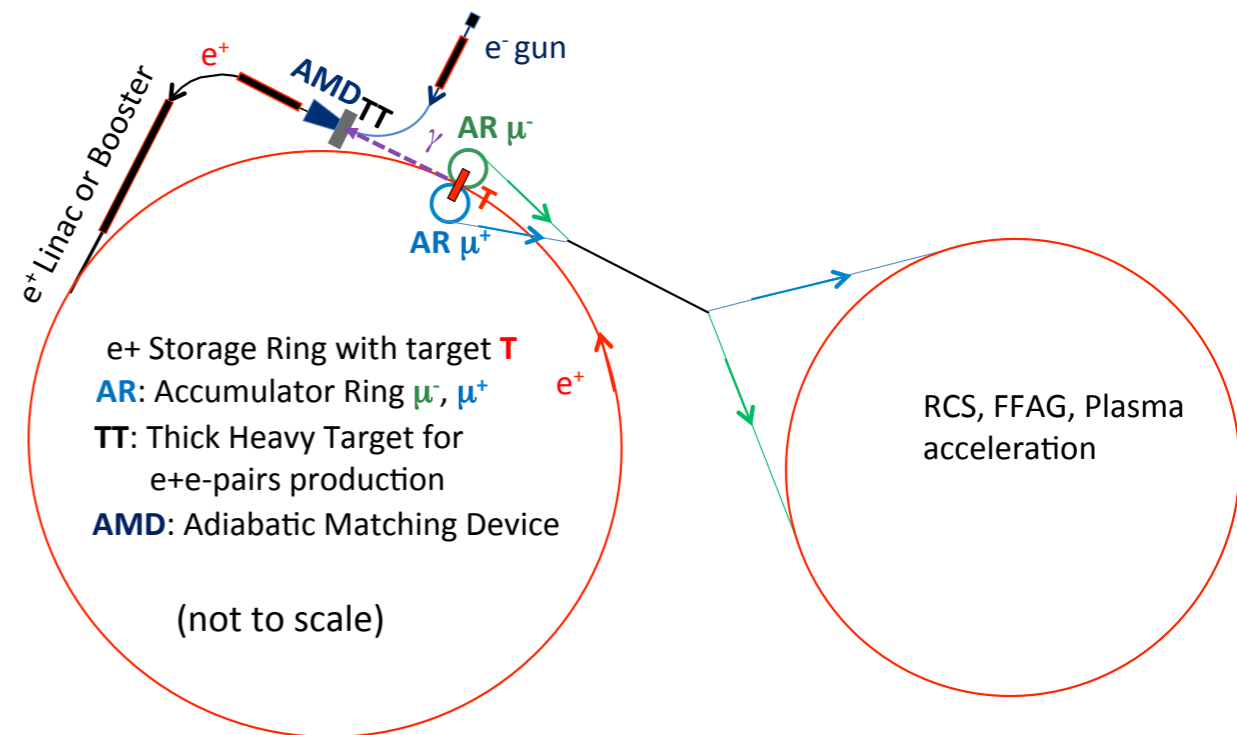




POWER LOAD CONSIDERATIONS

Symbol	Description	Reference Value
a	Gaussian beam spot size	300 μm
τ	bunch duration	10 ps
N_{part}	positron number	$3 \cdot 10^{11}$
N_{pulses}	number of consecutive bunches	100
T_{pulse}	time between two bunches	400 ns
$T_{heating}$	total time of N_{pulses}	40 μs
T_{rep}	repetition time of the N_{pulses} sequence	0.1 s

- ◆ “LEMMA0” Scheme
- ◆ 45 GeV positrons
- ◆ 1x3mm targets
- ◆ Beryllium/Carbon

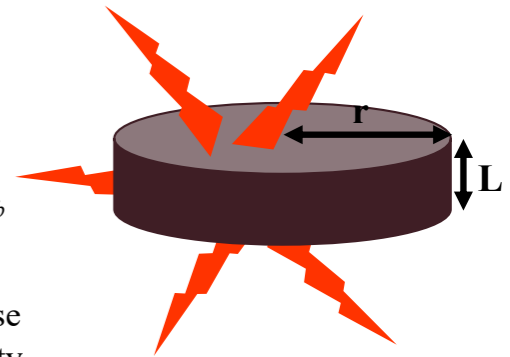




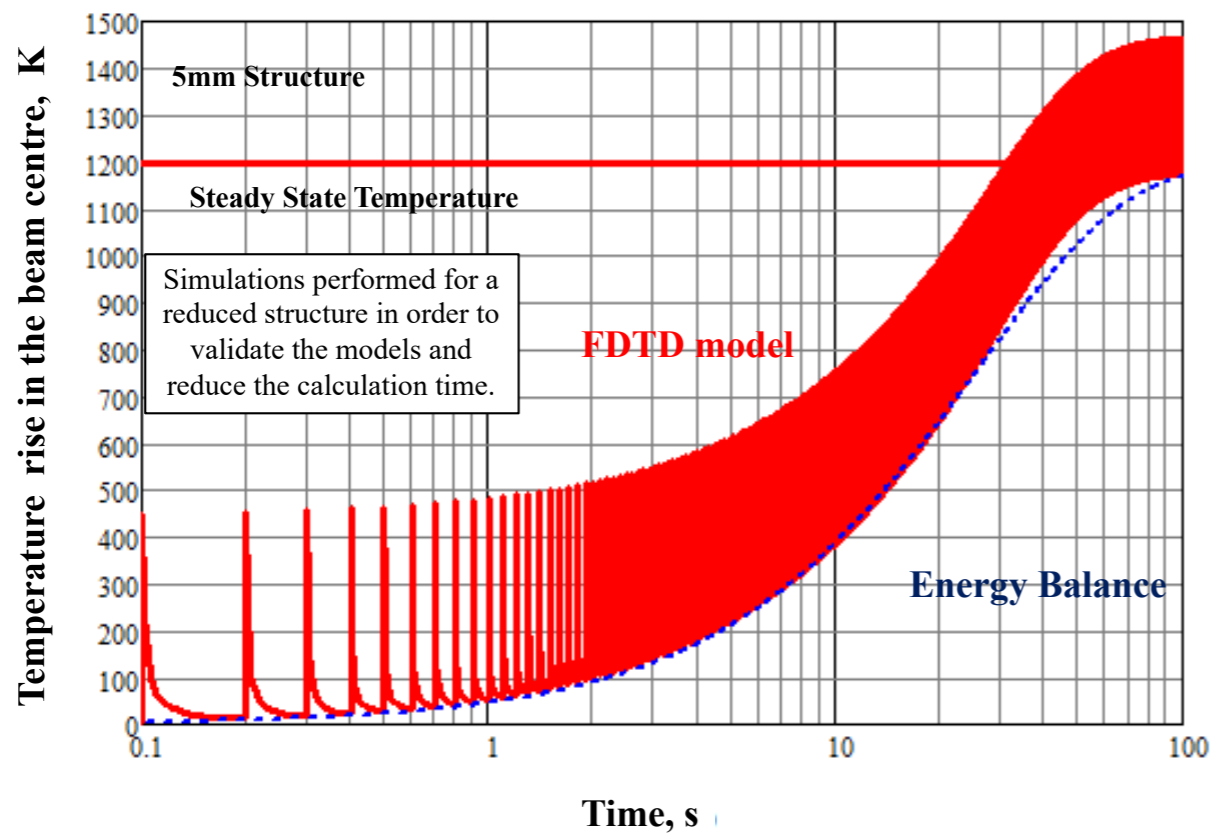
STEADY STATE TEMPERATURE

$$\Delta T = \sqrt{T_{amb}^4 + \left(\frac{a^2 \cdot L}{r^2 + r \cdot L} \right) \frac{C_{max,a} \cdot N_{part} \cdot N_{pulses}}{\epsilon \cdot \sigma_B \cdot T_{rep}}} - T_{amb}$$

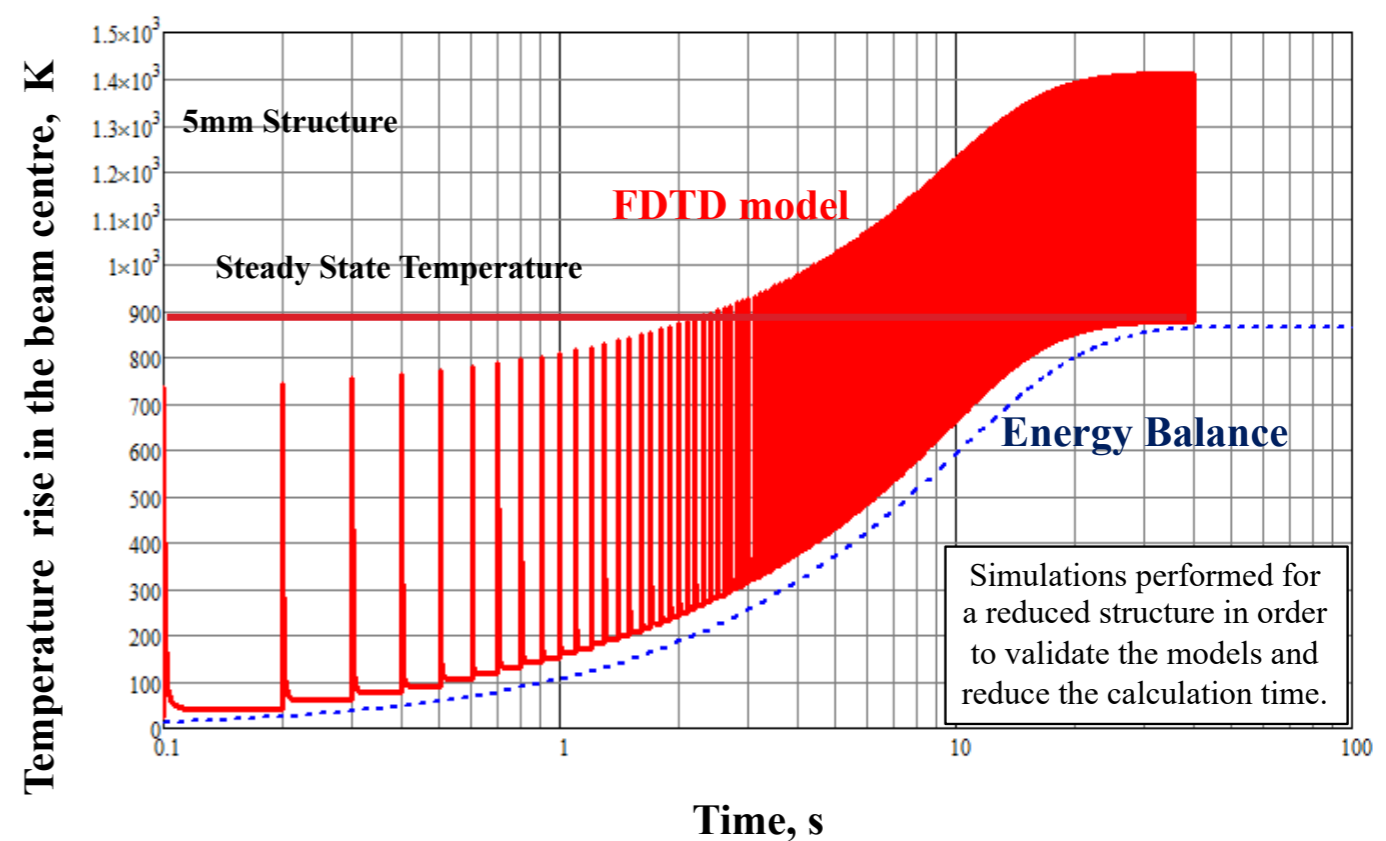
ϵ emissivity, σ_B Stefan-Boltzmann constant, T_{rep} pulse train repetition period, $C_{max,a}$ deposited energy density peak by the Fluka data



Beryllium



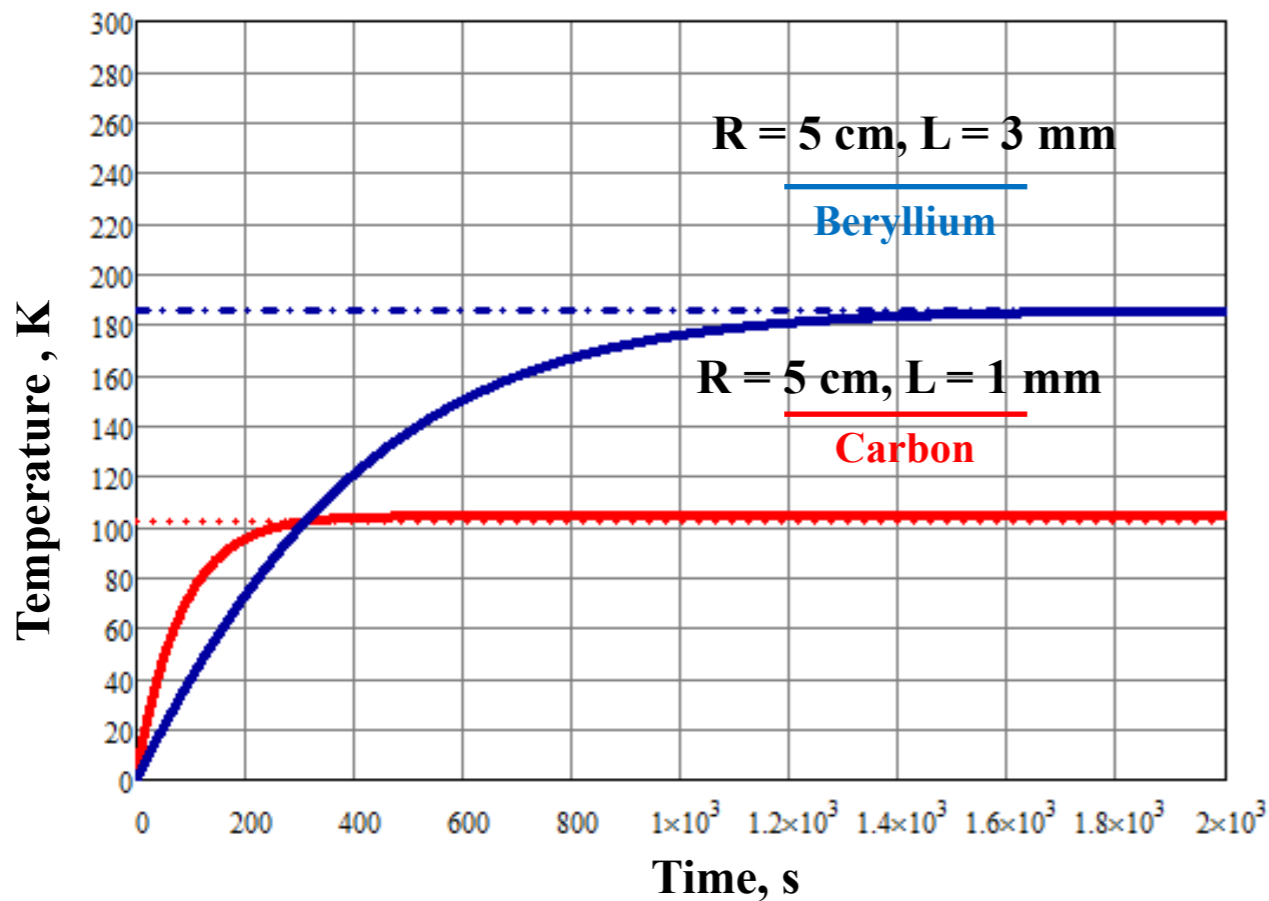
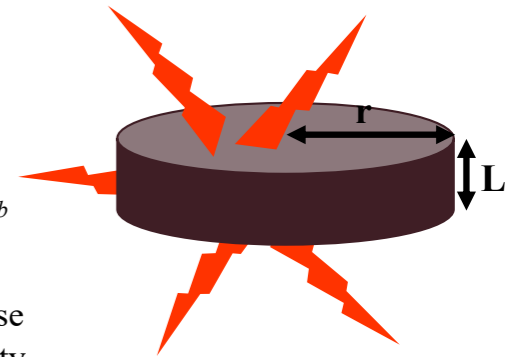
Carbon



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◆ Beryllium target

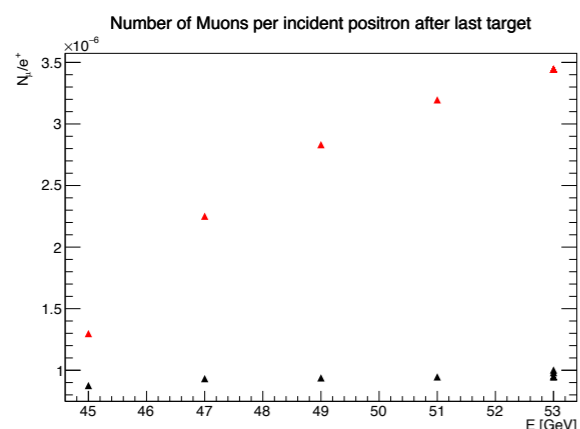
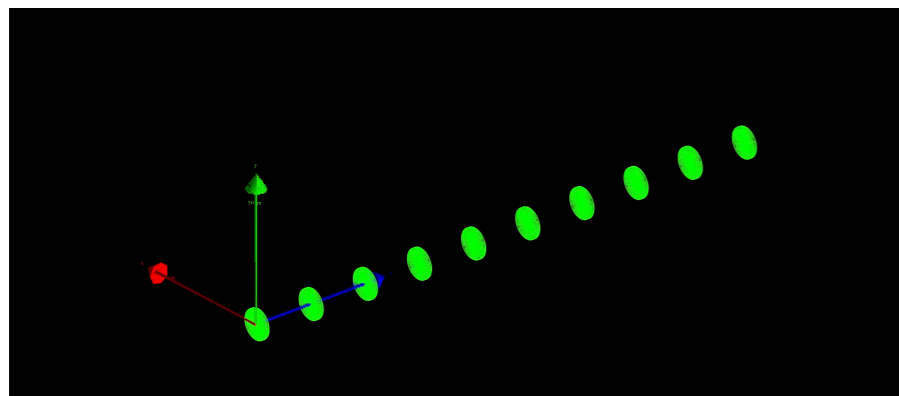
radius $r = 5$ cm, thickness $L = 3$ mm;
Steady state temperature increase: $\Delta T_{ss} = 185.5$ K
Melting point: 1551 K

◆ Carbon target

radius $r = 5$ cm, thickness $L = 1$ mm;
Steady state temperature increase: $\Delta T_{ss} = 102.5$ K
Melting point: 3923 K

MUON PRODUCTION TARGET: SUMMARY

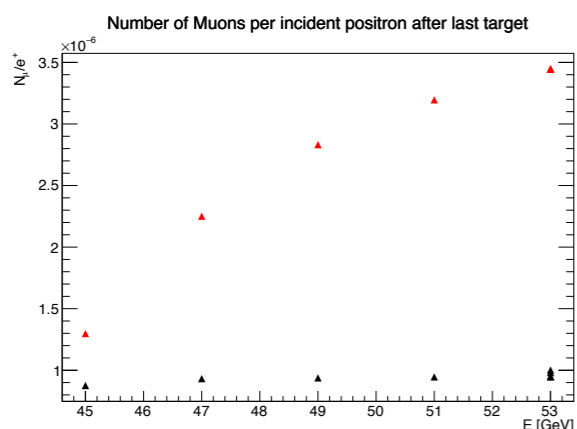
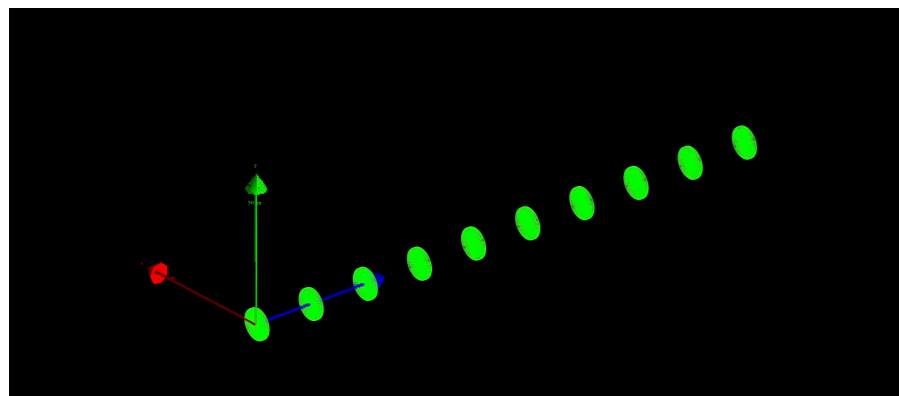
- ◆ A powerful Monte Carlo simulation has been developed
- ◆ As a first approach, a “Single IP - Multi Target Line” has been simulated



- ➔ 10 Berillium targets
- ➔ 1 cm thick each
- ➔ 2 m total z length
- ◆ **Rising** the positron beam **energy** leads to a greater number of muons (x3), but the **advantage** is strongly **reduced** (+10%) after muon collection **cuts**
- ◆ An **optimal working point** must be identified as the best **tradeoff** between muon production, positron degradation and power load on the target
- ◆ A software algorithm to analyse power deposition has been developed in the LEMMA0 scheme, and is going to be applied also in the actual LEMMA scheme
- ◆ + *new target options...*

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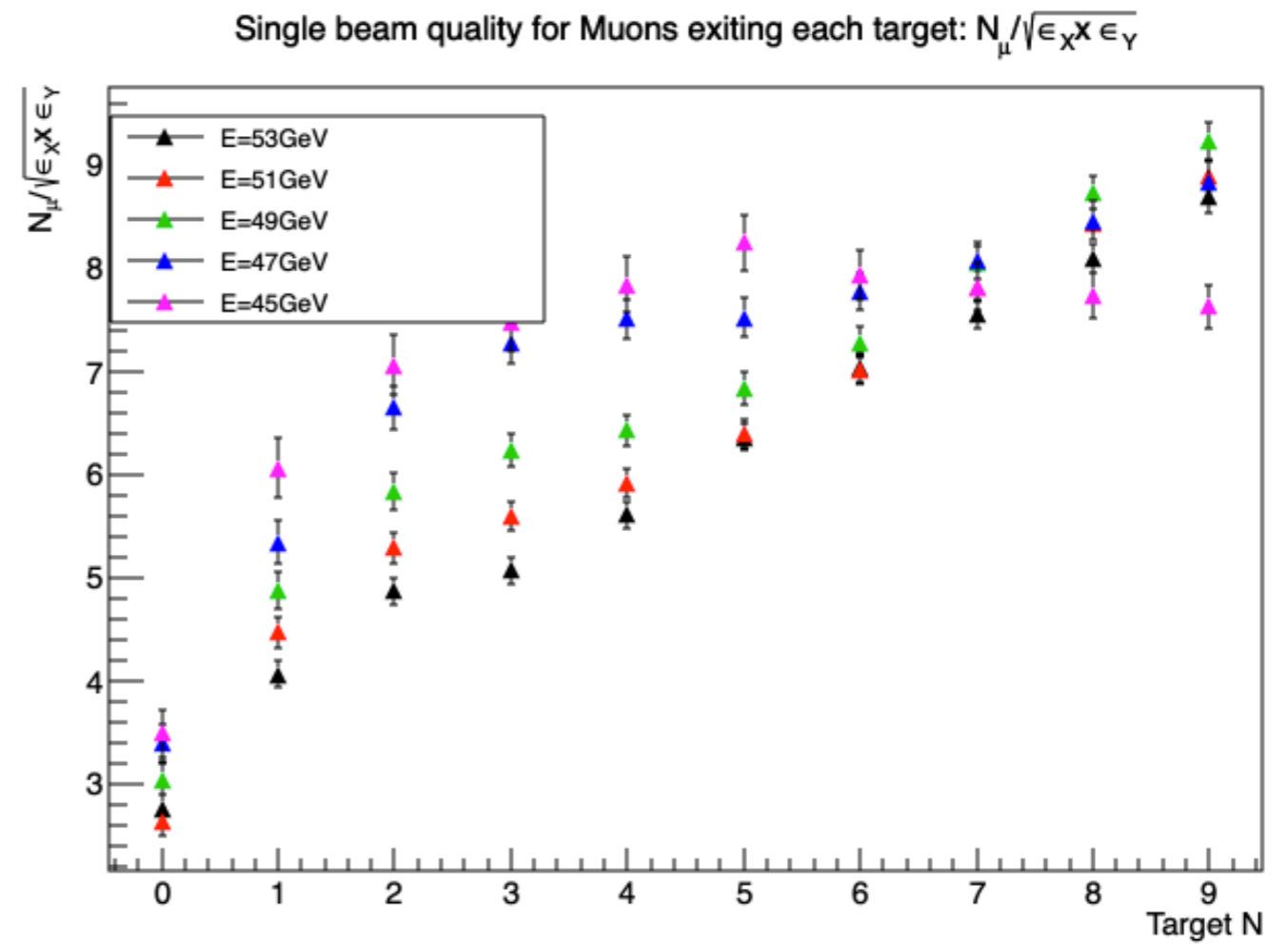
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BACKUP

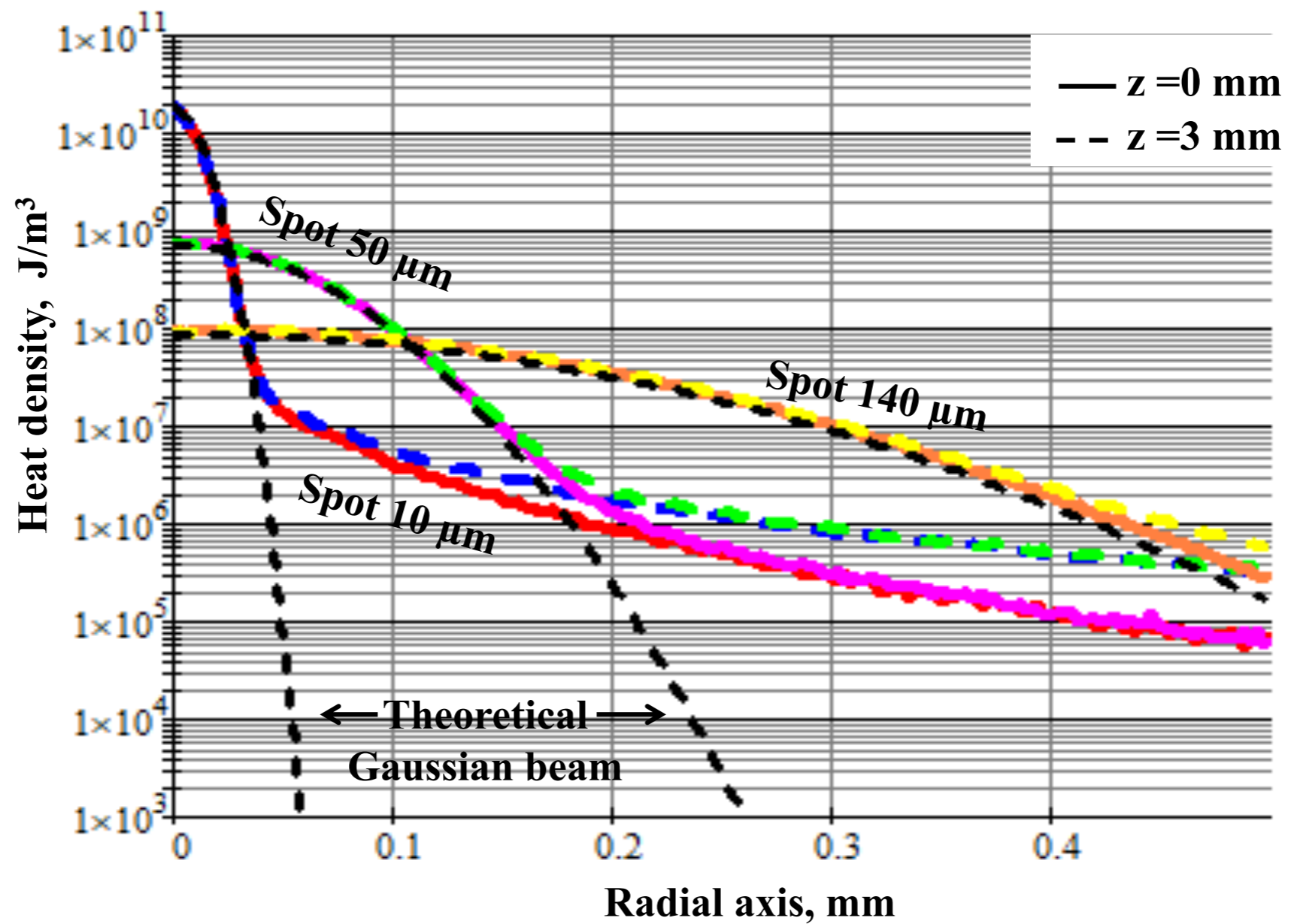


SIMULATION RESULTS





SIMULATION RESULTS

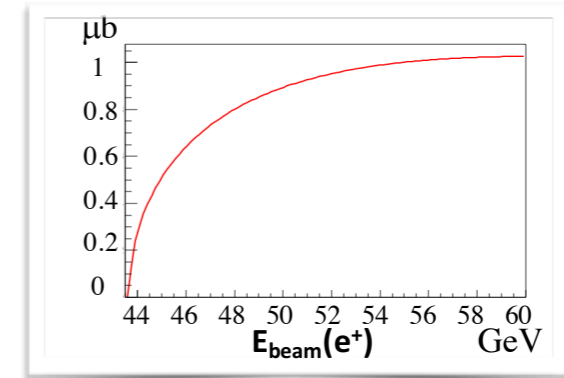


Muons energy target after target

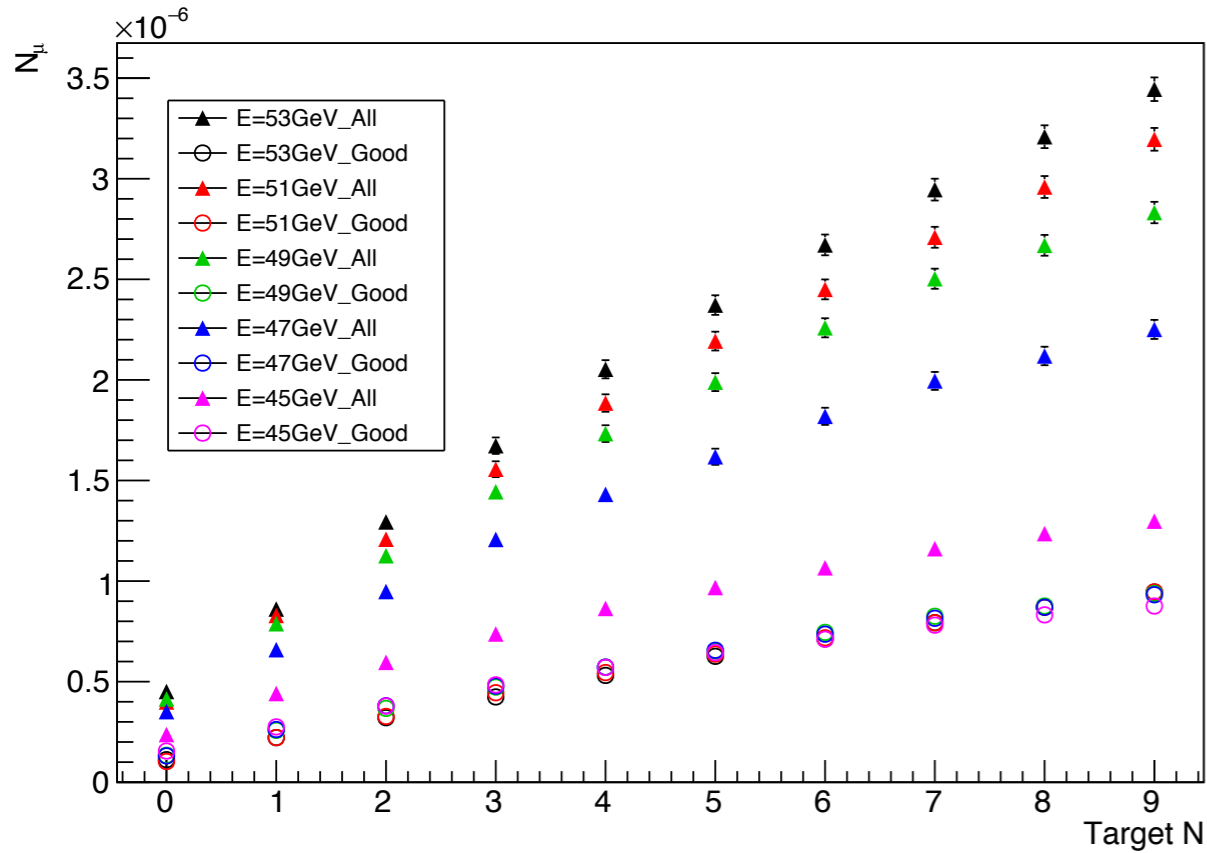


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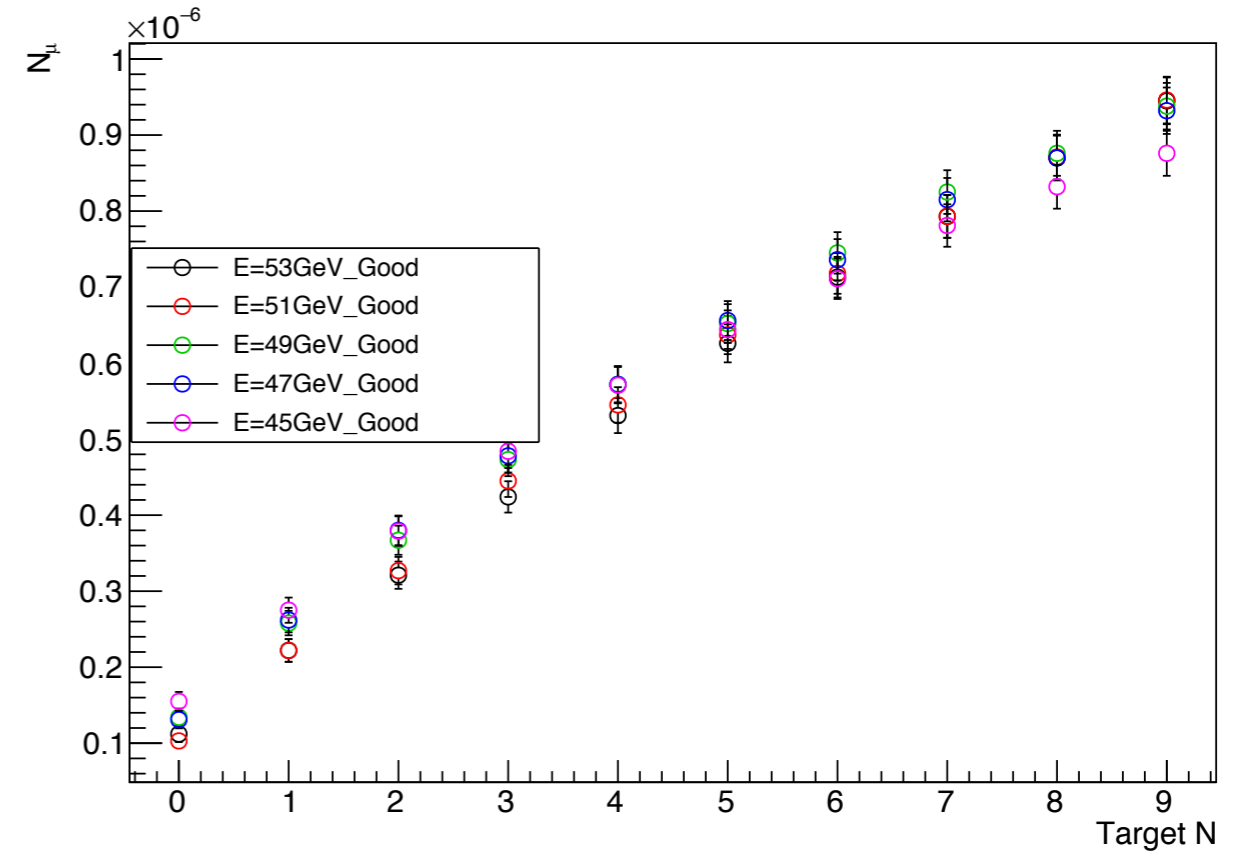
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Number of good muons (within energy acceptance) produced after each target per incident positron



THE MUON PRODUCTION ON ISSUE

◆ **CAVEAT:** the muon production **cross section** has been artificially **biased**

- ◆ To see enough muons in a reasonable amount of CPU time
- ◆ $\sim x10^3$ factor, then properly taken into account in following plots
- ◆ What effect on positrons' survival?

