

Pomeron Calculus: X-sections, Diffraction & MC

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Outline

- ▶ Optical theorem, unitarity & AGK cuts
- ▶ Enhanced Pomeron graphs: resummation
- ▶ Phenomenological approach - 2 Pomeron poles:
 - total, elastic & diffractive x-sections
- ▶ 'Semihard Pomeron'
- ▶ MC approach (QGSJET II)

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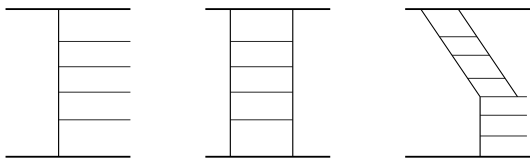
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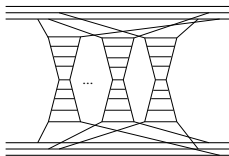
'Elementary' processes:

non-diffr. production virtual rescattering diffraction

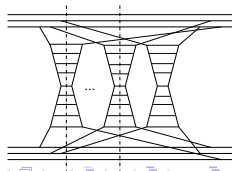


- ▶ elastic scattering - coherence of the parton cascade preserved by the scattering process
- ▶ 'elementary' inel. process - coherence broken \Rightarrow hadronization
- ▶ general interaction - multiple scattering:

$$\sigma_{\text{tot}} = \text{Im}$$



$$= \Sigma$$



Optical theorem + AGK rules

⇒ relation between elastic amplitude & inelastic final states

$$\left| \begin{array}{cccc} \text{Diagram 1} & + & \text{Diagram 2} & + & \text{Diagram 3} & + & \text{Diagram 4} \end{array} \right|^2$$

$$= \begin{array}{cccc} \text{Diagram 1} & + & \text{Diagram 2} & + & \text{Diagram 3} & + & \text{Diagram 4} \end{array}$$

The diagrams consist of horizontal lines representing particle trajectories. The top row shows four diagrams representing different topologies of scattering. The first diagram has a single vertical line. The second has two vertical lines. The third has two vertical lines with a gap between them. The fourth has two vertical lines with a gap between them and a vertical line in the middle. The bottom row shows the same four diagrams, but each has a vertical dashed line passing through it, representing an AGK-cut.

- ▶ AGK rules: no interference between different topologies of final states
- ▶ ⇒ all possible final states - obtained via AGK-cuts of elastic scattering diagrams
- ▶ partial cross sections - expressed via amplitudes for 'elementary' scattering

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The diagram shows the square of the sum of four elastic scattering diagrams. The top row shows the sum of four diagrams, each enclosed in a vertical bar. The diagrams are: 1) a single vertical line with four horizontal rungs; 2) a vertical line with four horizontal rungs and a vertical line on the right; 3) a vertical line with four horizontal rungs, a vertical line in the middle, and a vertical line on the right; 4) a vertical line with four horizontal rungs and a vertical line on the right. The bottom row shows the expansion of the square, resulting in the sum of all possible topologies formed by cutting the diagrams with vertical dashed lines. The dashed lines are placed at the positions of the vertical lines in the original diagrams.

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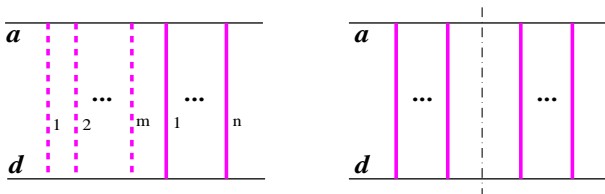
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The diagrams are schematic representations of scattering amplitudes. The top row shows four diagrams representing the square of the sum of four terms. The bottom row shows four diagrams representing the sum of the squares of each term, with vertical dashed lines indicating cuts in the diagrams.

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- ▶ ⇒ all possible final states - obtained via AGK-cuts of elastic scattering diagrams
- ▶ partial cross sections - expressed via amplitudes for 'elementary' scattering

Schematic (elementary parton cascades \equiv Pomerons):



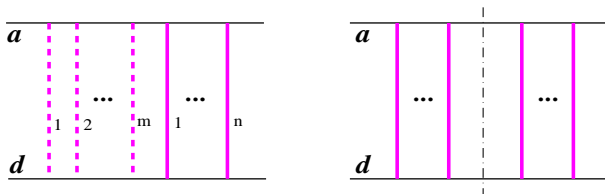
- ▶ Pomeron amplitudes - various approaches possible (purely phenomenological, BFKL, ...)

Intermediate states between Pomeron exchanges include inelastic excitations: $\sum_i |X_i\rangle\langle X_i| = |\rho\rangle\langle\rho| + \sum_{i \neq \rho} |X_i\rangle\langle X_i|$

- ▶ Good-Walker-like scheme - use elastic scattering eigenstates:

$$|X_i\rangle \rightarrow \sum_j \sqrt{C_{j/X_i}} |j\rangle$$

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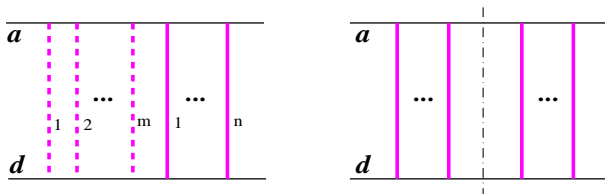
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E.g., using eikonal vertices for Pomeron emission:

$$f_{pp}(s, b) = i \sum_{j,k} C_{j/p} C_{k/p} \left[1 - e^{-\chi_{jk}^{\mathbb{P}}(s, b)} \right]$$

$\chi_{jk}^{\mathbb{P}} = \Im m f_{jk}^{\mathbb{P}}$ - eikonal for Pomeron exchange between $|j\rangle$ and $|k\rangle$

▶ \Rightarrow allows to calculate X-sections for various final states:

$$\sigma_{ad}^{(n)}(s) = \sum_{j,k} C_{j/p} C_{k/p} \int d^2 b \frac{[2\chi_{jk}^{\mathbb{P}}(s, b)]^n}{n!} e^{-2\chi_{jk}^{\mathbb{P}}(s, b)}$$

$$\begin{aligned} \sigma_{ad}^{\text{diffr-proj}}(s) &= \sum_{j,k,l,m} (C_{j/p} \delta_{jl} - C_{j/p} C_{l/p}) C_{k/p} C_{m/p} \\ &\times \int d^2 b \left[1 - e^{-\chi_{jk}^{\mathbb{P}}(s, b)} \right] \left[1 - e^{-\chi_{lm}^{\mathbb{P}}(s, b)} \right] \end{aligned}$$

▶ partial x-sections are obtained after **resummation of all virtual (elastic) rescatterings**

▶ if the decomposition in eigenstates is energy-independent:

low mass diffraction ($M_X^2 \ll s$) only

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Higher diffraction = more asymmetric eigenstates

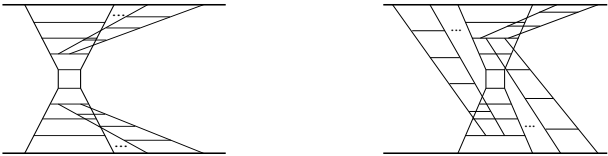
smaller σ_{tot} (σ_{inel}) - inelastic screening

bigger fluctuations of multiplicity / of N_{part} in pA (AA)

Non-linear effects

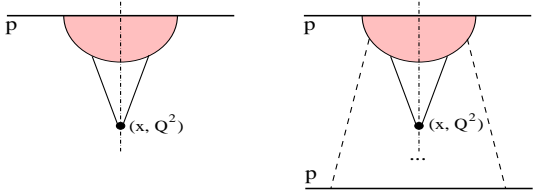
Pomeron-Pomeron interactions \Rightarrow rich physics

- ▶ e.g. final states with jets:

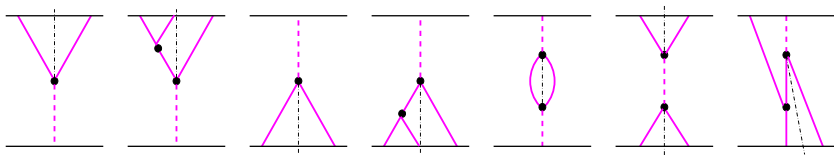


'fan' diagrams - low-x PDFs as 'seen' in DIS & inclusive cross sections

'net fans' - 'reaction-dependent PDFs' (depend on rescattering on the partner hadron)



High mass diffraction from enhanced diagrams:

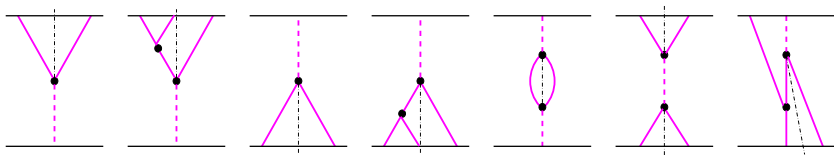


- ▶ sign-indefinite contributions
- ▶ higher orders - increasingly important with energy
- ▶ \Rightarrow all order resummation needed
- ▶ same applies to other final states

General solution to the problem (e.g. MC implementation) requires:

- ▶ knowledge of the Pomeron amplitude
- ▶ knowledge of multi-Pomeron vertices
- ▶ complete resummation of enhanced diagrams:
for elastic scattering amplitude & for particular final states

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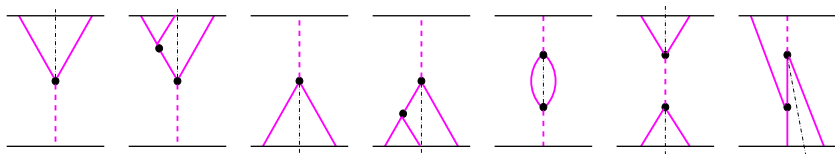


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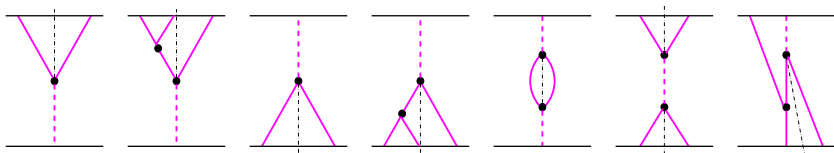


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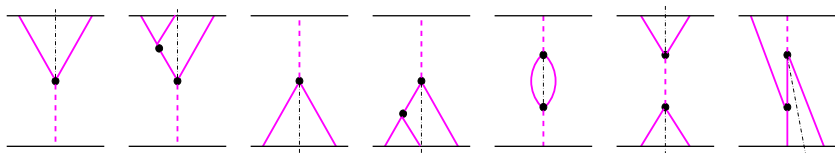


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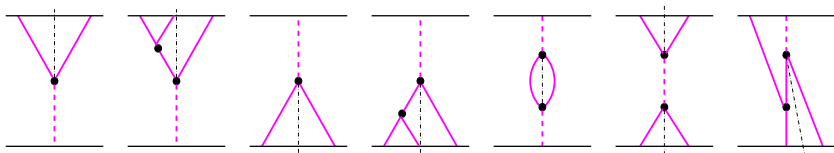


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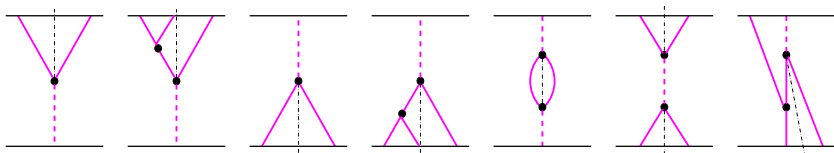


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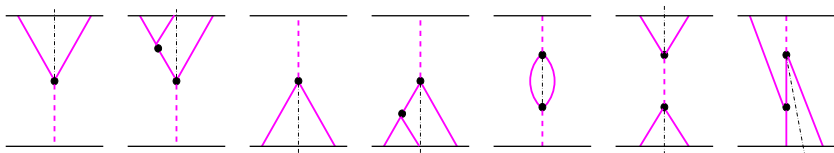


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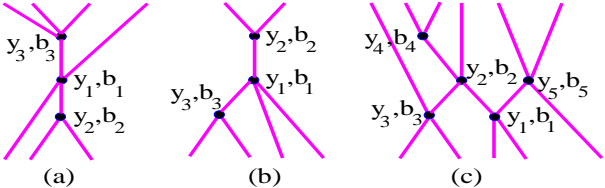
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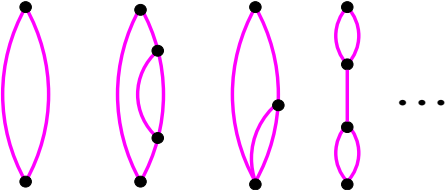
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Diagrammatic resummation

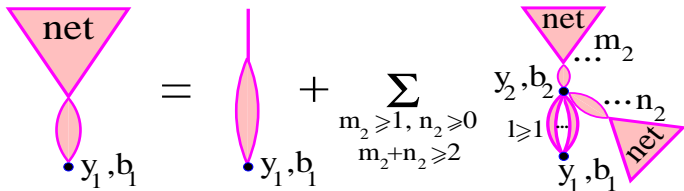
Without Pomeron 'loops' one would have 'net'-like graphs:



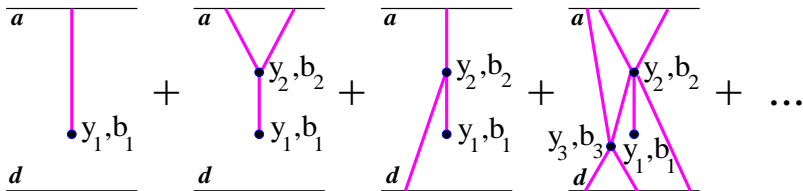
In reality, any 'intermediate' Pomeron may be replaced by 'loops':



Introduce 'net fan' contributions via Schwinger-Dyson equation:

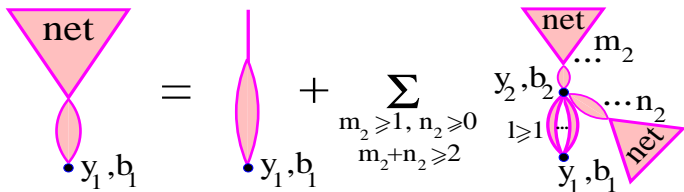


- ▶ correspond to arbitrary Pomeron 'nets' coupled to given vertex (for simplicity, loops not shown)

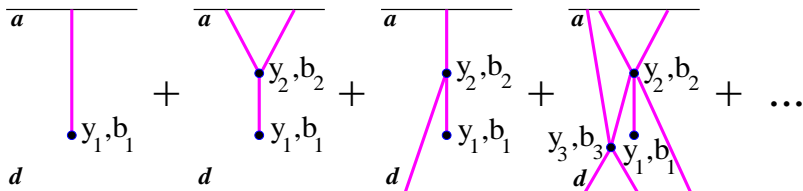


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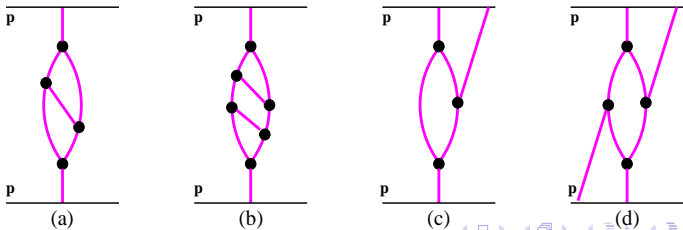


- ▶ have the meaning of 'reaction-dependent PDFs'

Sum of (almost) all irreducible contributions to elastic amplitude
 $(\Omega_{pp(jk)}(s, b))$:

$$\sum_{\substack{m_1, n_1 \geq 1 \\ m_1 + n_1 \geq 3}} \text{net} - \sum_{\substack{m_1, n_2 \geq 1 \\ m_2, n_1 \geq 0 \\ m_1 + n_1 \geq 2}} \text{net} + \text{net} - \text{net}$$

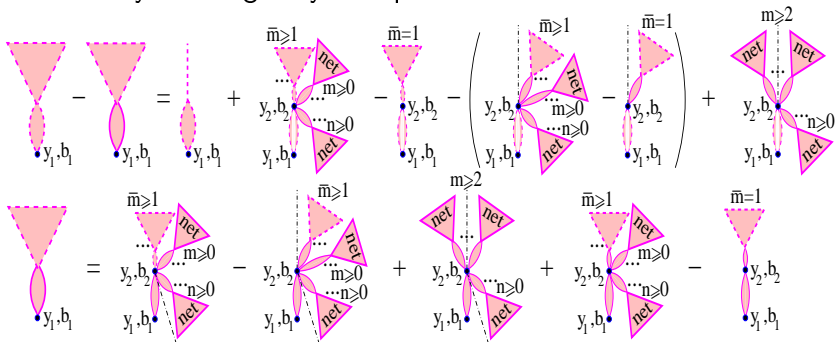
examples of graphs which are not included in this scheme:



Knowing the amplitude one can calculate σ_{tot} , $d\sigma_{\text{el}}/dt$, etc.

However, to describe the structure of final states one needs the complete set of **partial cross sections**

- ▶ one assumes the validity of **AGK cutting rules**
- ▶ one starts from 'building blocks': AGK-cuts of 'net fans' - defined by Schwinger-Dyson equations



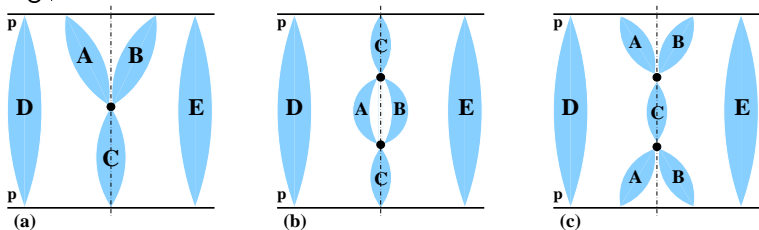
One obtains the complete system of cuts:

$$\begin{aligned}
 & \left[\begin{array}{ccc} \bar{m} \geq 2 & \bar{m} \geq 2 & \bar{m} \geq 2 \\ m > 0 & m > 0 & m > 0 \\ y_1, b_1 & y_1, b_1 & y_1, b_1 \\ \dots & \dots & \dots \\ \dots & \dots & \dots \\ \bar{n} \geq 2 & \bar{n} \geq 2 & \bar{n} \geq 2 \end{array} \right] + \left[\begin{array}{cc} m \geq 2 & m \geq 2 \\ \text{net} & \text{net} \\ y_1, b_1 & y_1, b_1 \\ \dots & \dots \\ \dots & \dots \\ \bar{n} \geq 2 & \bar{n} \geq 2 \end{array} \right] + \left[\begin{array}{cc} \bar{m} \geq 2 & \bar{m} \geq 2 \\ m \geq 0 & m \geq 0 \\ y_1, b_1 & y_1, b_1 \\ \dots & \dots \\ \dots & \dots \\ \bar{n} \geq 2 & \bar{n} \geq 2 \end{array} \right] \\
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 (4) & \quad (5) \quad (6) \quad (7) \\
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 \end{aligned}$$

Obtained contributions satisfy s -channel unitarity (completeness):

$$\sum_{i=1}^{11} \bar{\Omega}_{pp(jk)}^{(i)}(s, b) = \Omega_{pp(jk)}(s, b)$$

- ▶ allow to derive x-sections for various topologies of final states
- ▶ e.g., diffractive cuts:

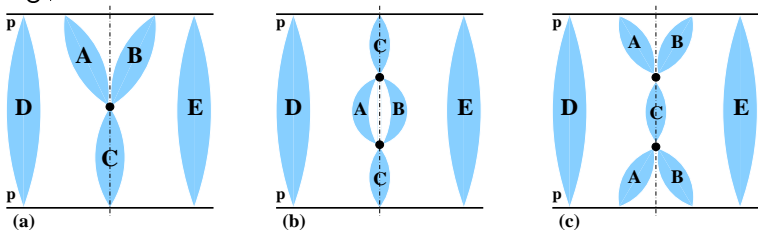


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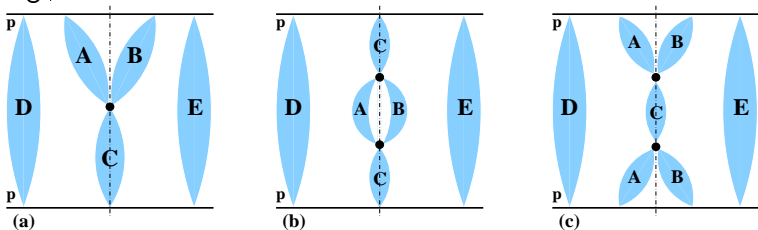


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Particular (simple) model

Let us assume eikonal multi- \mathbb{P} vertices: $G^{(m,n)} = r_{3\mathbb{P}} \gamma_{\mathbb{P}}^{m+n-3}$

- ▶ 2-component ('soft' + 'hard') Pomeron:

$$D^{\mathbb{P}}(s, t) = 8\pi i \left[s^{\alpha_{\mathbb{P}(s)}} e^{\alpha'_{\mathbb{P}(s)} \ln s t} + r_{h/s} s^{\alpha_{\mathbb{P}(h)}} e^{\alpha'_{\mathbb{P}(h)} \ln s t} \right]$$

- ▶ dipole form factor for proton elastic eigenstates $|j\rangle$:

$$F_j^{\mathbb{P}}(t) = \frac{\gamma_j}{(1 - \Lambda_j t)^2}; \quad \gamma_j = \gamma(1 \pm \kappa), \quad j = 1, 2$$

- ▶ Pomeron eikonal:

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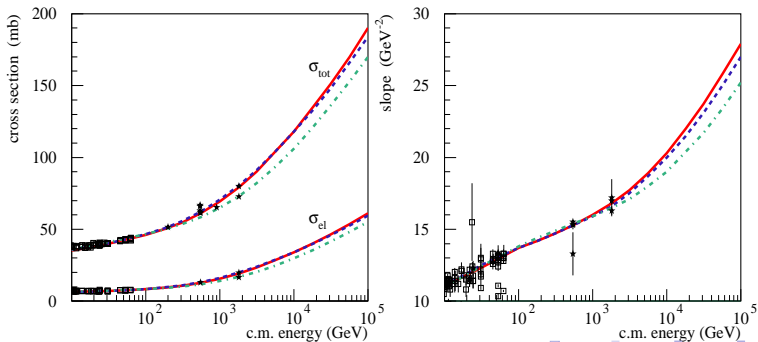
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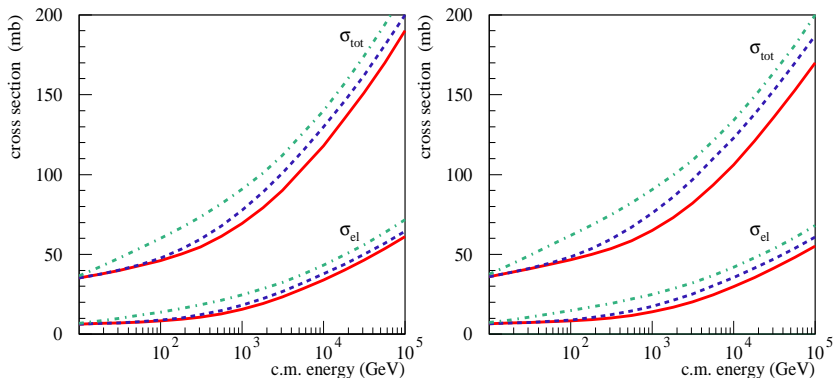
Few parameter sets differ by the fit to CDF/E710 at $\sqrt{s}=1800$ GeV and by the \mathbb{P} mass cutoff ($\xi = \ln M_{\min}^2$): $\xi = 2$ - A, C; $\xi = 1.5$ - B

	$\alpha_{\mathbb{P}(s)}$	$\alpha_{\mathbb{P}(h)}$	$\alpha'_{\mathbb{P}(s)}$, GeV ⁻²	$\alpha'_{\mathbb{P}(h)}$, GeV ⁻²	γ , GeV ⁻¹	η	$r_{h/s}$	Λ_1 , GeV ⁻²	Λ_2 , GeV ⁻²	$r_{3\mathbb{P}}$, GeV ⁻¹	$\gamma_{\mathbb{P}}$, GeV ⁻¹
(A)	1.145	1.35	0.13	0.075	1.65	0.6	0.06	1.06	0.3	0.14	0.5
(B)	1.15	1.35	0.165	0.08	1.75	0.6	0.065	1.03	0.3	0.15	0.5
(C)	1.14	1.31	0.14	0.085	1.6	0.5	0.09	1.1	0.4	0.14	0.5

► total / elastic cross sections and elastic slope

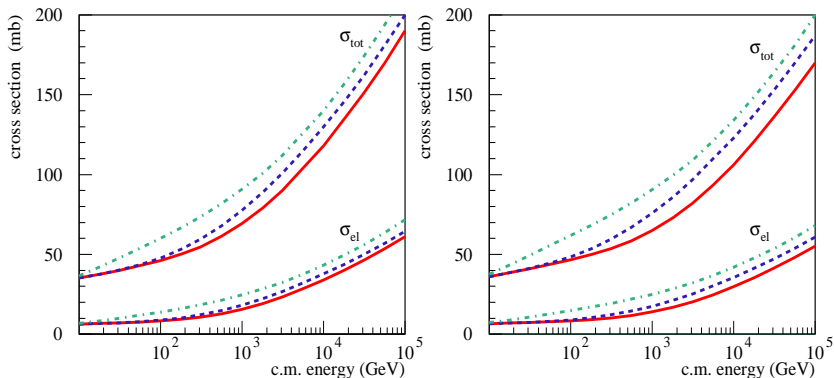


Using only 'net'-like (blue) / 'loop'-like (green) enhanced graphs:



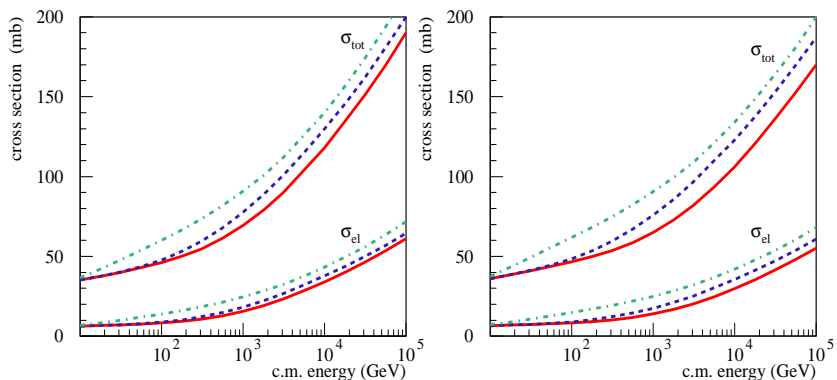
- ▶ \Rightarrow none of the two classes can be neglected
- ▶ \mathbb{P} -loops only - far insufficient for cross section calculations
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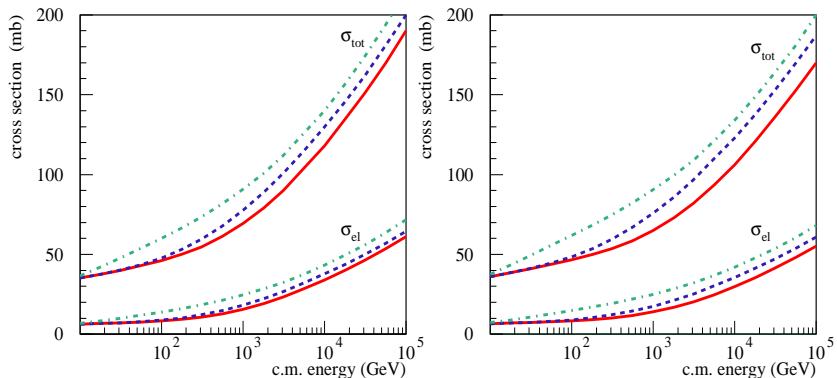
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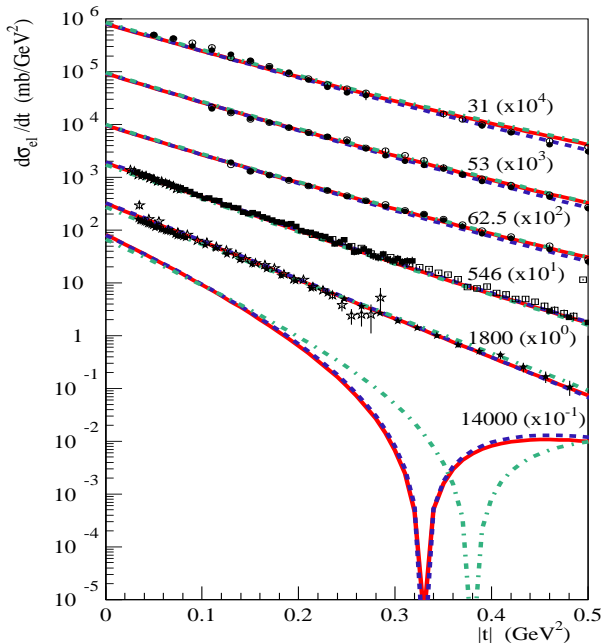
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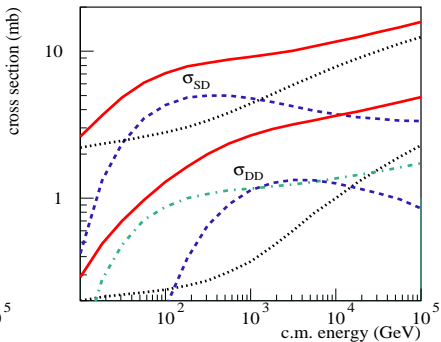
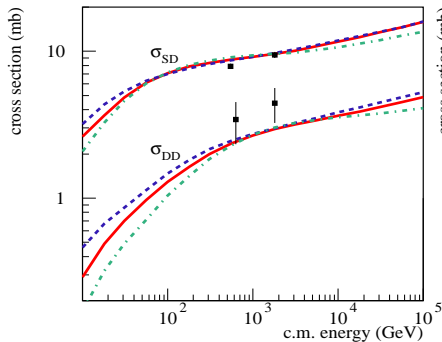
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Differential elastic cross section



Diffractive cross sections

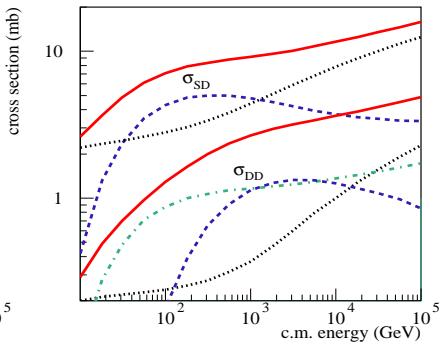
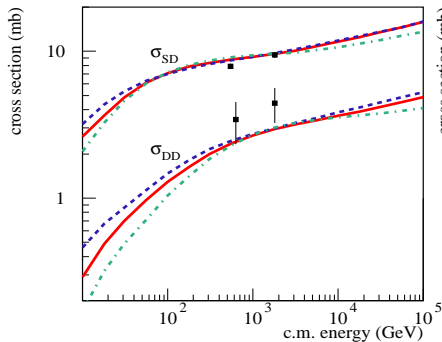
Single ($M_X^2/s < 0.15$) and double ($y_{\text{gap}}^{(0)} \geq 3$) diffraction x-sections



- ▶ high mass diffraction - decreases with energy
- ▶ suppression of diffraction - by eikonal RGS factors and by absorptive corrections from higher order cut enhanced graphs

Diffractive cross sections

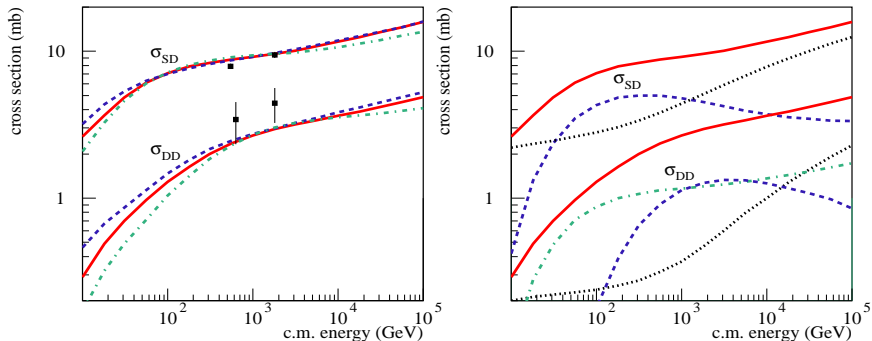
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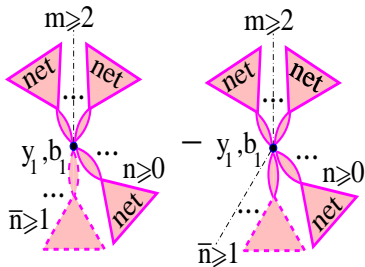
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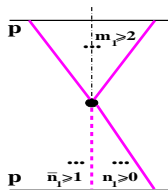


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Examples - partial resummations of higher order graphs



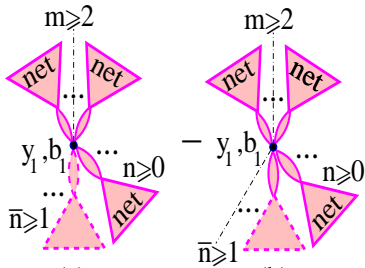
- ▶ dominant contributions to σ_{SD} :



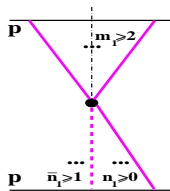
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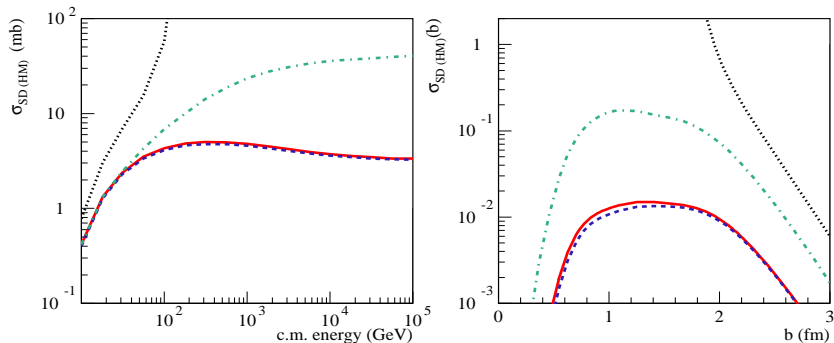


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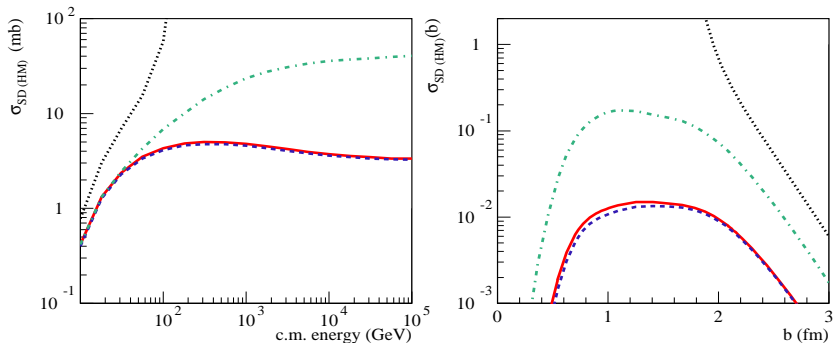
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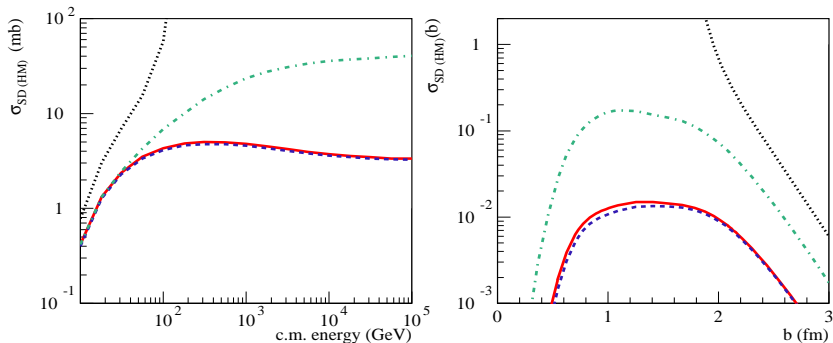
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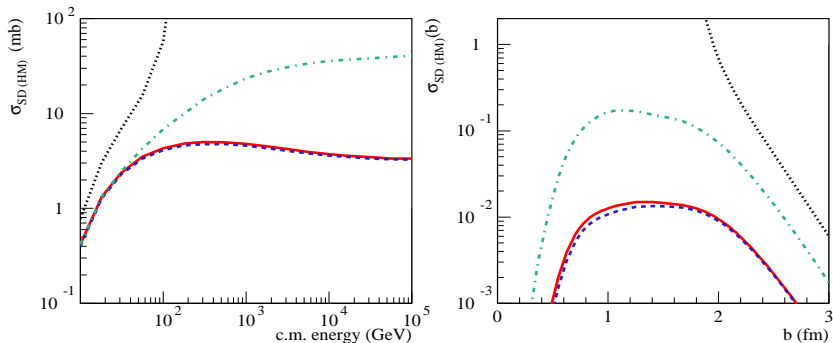
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From the Tevatron to the LHC

1.8 TeV	σ^{tot}	σ^{el}	σ^{SD}	σ^{DD}	$\sigma_{\text{HM}}^{\text{SD}}$	$\sigma_{\text{HM}}^{\text{DD}}$	$\sigma_{\text{LHM}}^{\text{DD}}$	σ^{DPE}
Set (A)	79.3	19.3	9.62	3.62	4.52	1.95	1.20 (1.17)	0.19
Set (B)	80.5	19.9	9.84	4.06	4.78	2.37	1.24 (1.20)	0.23
Set (C)	72.8	16.4	10.5	3.84	5.74	2.01	1.42 (1.36)	0.28
KMR	73.7	16.4	13.8		9.7			
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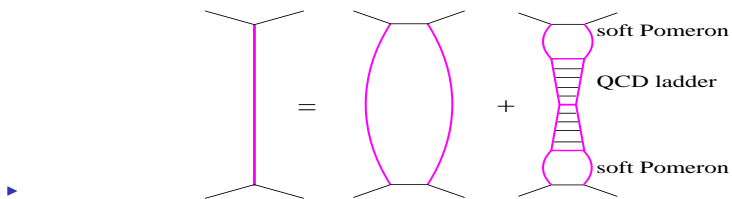
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'Semihard Pomeron'

Parton cascades **start at low virtualities** \Rightarrow

- ▶ Q_0^2 - cutoff between 'soft' and perturbative physics
- ▶ 'Soft' interactions (all $|q^2|$ - small $\Rightarrow \alpha_s(q^2) > 1$):
 - pQCD is inapplicable \Rightarrow 'soft' Pomeron amplitude
- ▶ 'Semihard' processes ($|q^2| > Q_0^2 \Rightarrow \alpha_s(q^2) \ll 1$)
 - 'soft' Pomeron for $|p_t^2| < Q_0^2$
 - DGLAP ladder for $|p_t^2| > Q_0^2$
- ▶ general interaction \Rightarrow 'general Pomeron':



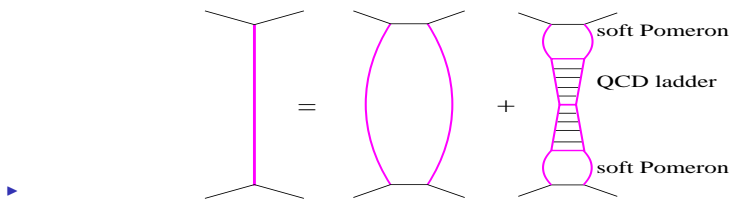
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Monte Carlo approach (QGSJET-II)

MC procedure:

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- ▶ Pomeron loops included (only net-like graphs in II-03)
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- ▶ $\mathbb{P}\mathbb{P}$ -coupling fixed by H1 LPS diffractive data
(in II-03 - by $F_2^{D(3)}$ from ZEUS rap-gap data)
- ▶ parameter fit included data on $d\sigma_{pp}^{\text{el}}/dt$, $d\sigma_{\pi p}^{\text{el}}/dt$, $d\sigma_{Kp}^{\text{el}}/dt$
- ▶ higher soft/hard cutoff: $Q_0^2 = 3 \text{ GeV}^2$ ($Q_0^2 = 2.5 \text{ GeV}^2$ in II-03)

corresponds to $p_{\perp, \text{hard}}^{\text{min}} = 2Q_0 \simeq 3.4$ GeV for the chosen
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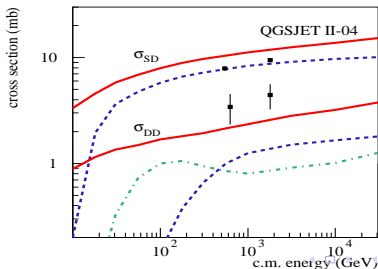
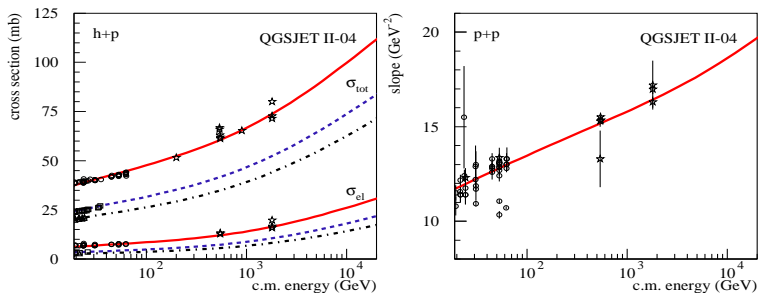
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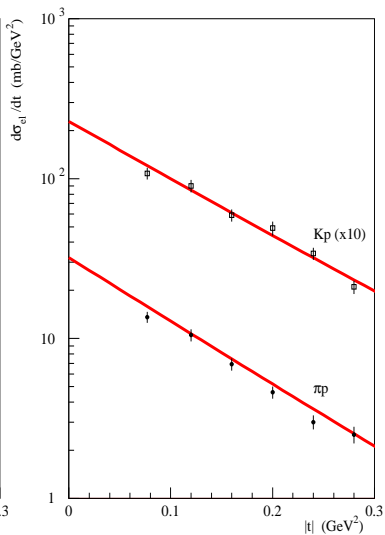
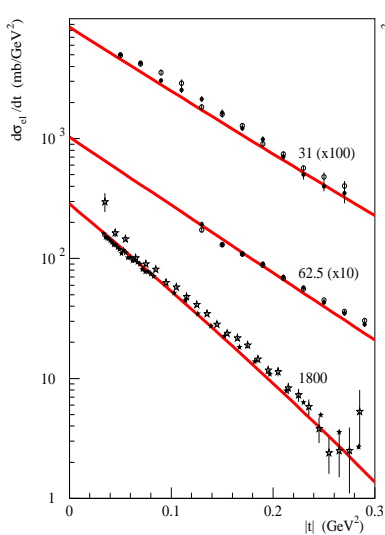
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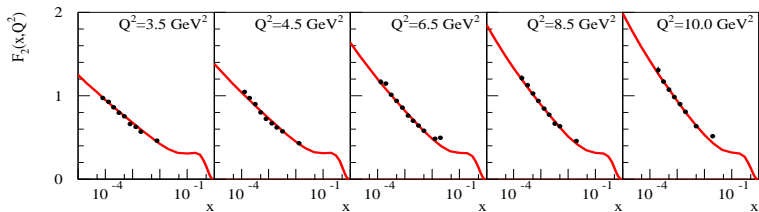
Total, elastic & diffractive X-sections / slope



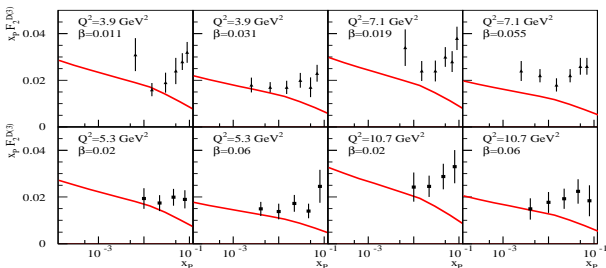
$d\sigma_{hp}^{el}/dt$ - only for small $|t|$ (Gaussian form-factor used)



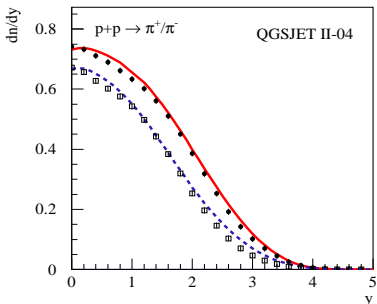
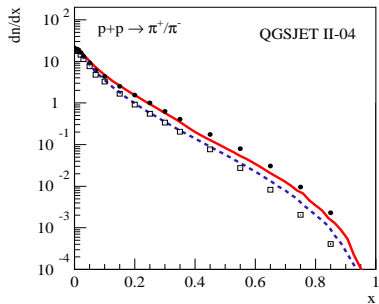
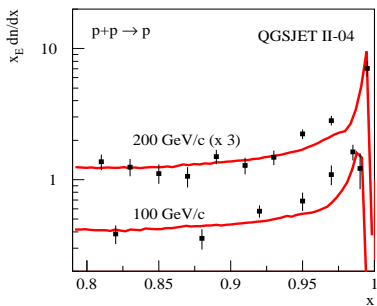
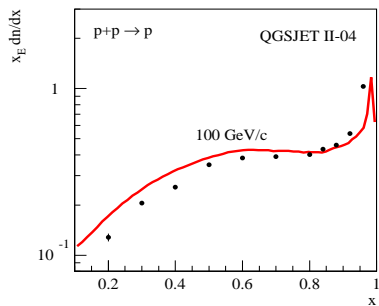
$$F_2, F_2^{D(3)}$$



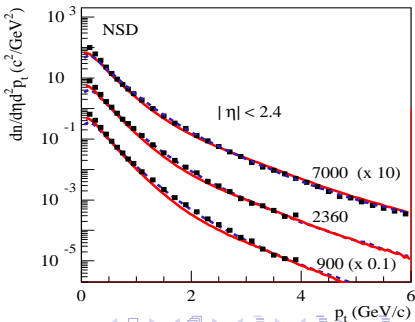
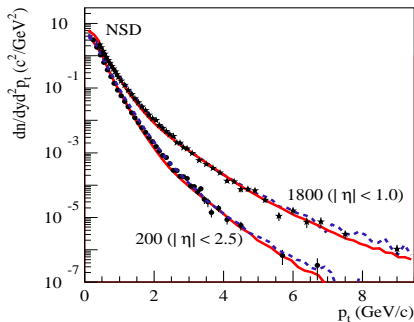
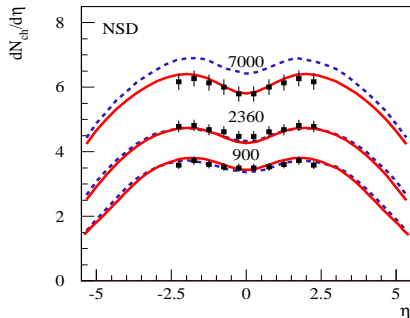
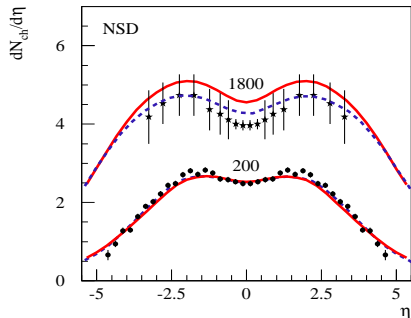
$F_2^{D(3)}$ - upper limit on r_{3P} (RRP & $\bar{q}q$ contributions neglected)



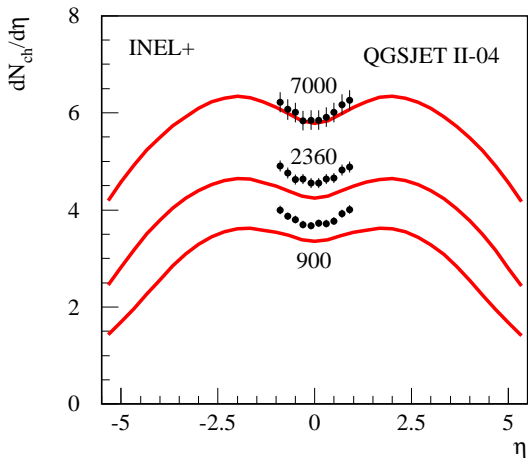
Some results at fixed target energies



Versions II-04 (solid) / II-03 (dashed) at $\sqrt{s} = 0.2 \div 7$ TeV



But: the influence of detector effects unclear in CMS results
E.g., contradiction with ALICE 'inel>0' selection:



Outlook

QGSJET-II is based on

- ▶ optical theorem & **s-channel unitarity**
- ▶ all-order resummation of enhanced Pomeron graphs
- ▶ complete set of partial x-sections (for all possible final states)
- ▶ self-consistent MC implementation
- ▶ 'semihard Pomeron' scheme for hard processes
- ▶ phenomenological soft Pomeron (\Rightarrow strings) for soft processes
- ▶ phenomenological vertices for Pomeron-Pomeron interactions

Main drawbacks:

- ▶ neglects energy-momentum correlations (at amplitude level) in multiple scattering
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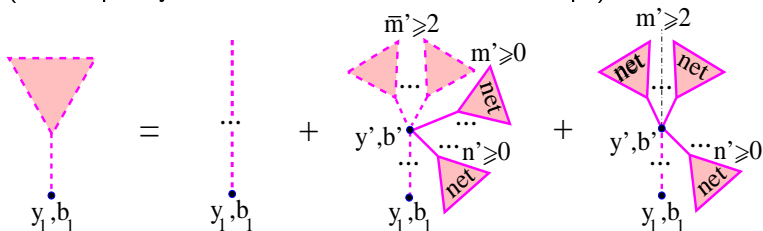
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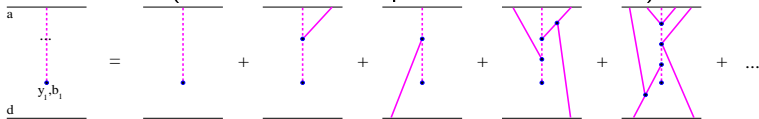
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Procedure for a 'cut net-fan' reconstruction
(for simplicity, illustrated without Pomeron loops)



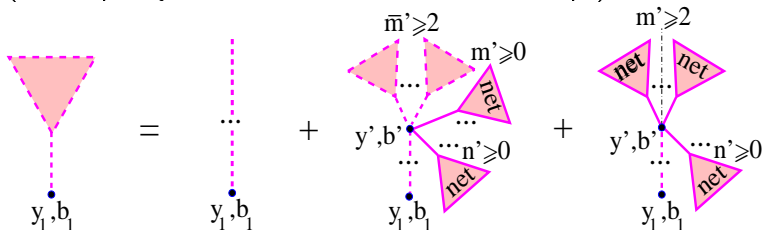
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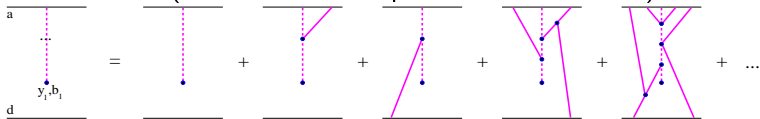
- ▶ or a diffractive cut (last graph in the rhs)
- ▶ or a splitting into 2 or more cut net-fans (2nd graph in the rhs)

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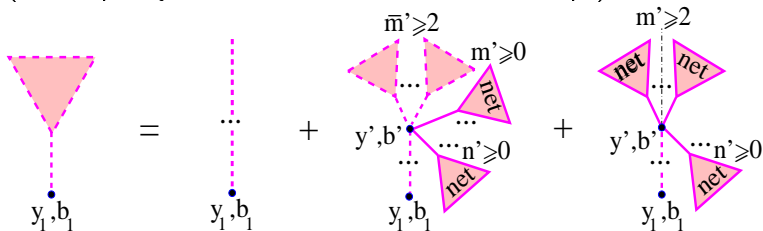
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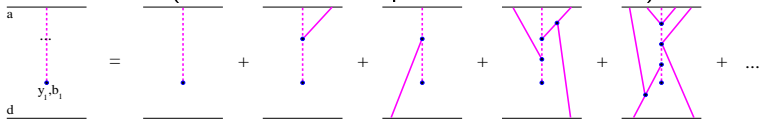
- ▶ or a diffractive cut (last graph in the rhs)
- ▶ or a splitting into 2 or more cut net-fans (2nd graph in the rhs)

Backup

Procedure for a 'cut net-fan' reconstruction
(for simplicity, illustrated without Pomeron loops)

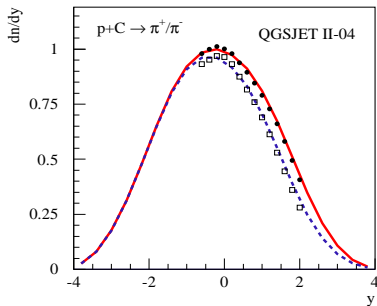
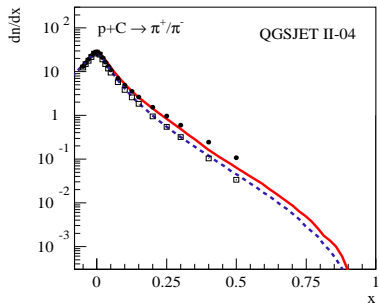


- ▶ at each step, one checks if the remaining piece is just a single cut Pomeron (with all the absorptive effects included):



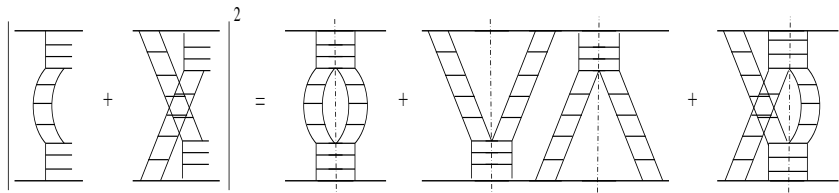
- ▶ or a diffractive cut (last graph in the rhs)
- ▶ or a splitting into 2 or more cut net-fans (2nd graph in the rhs)

Fixed target pC-collision



Interferention between double diffraction and double single diffraction

Example: double high mass diffraction at the lowest order



Comparison with heavy ions (QGSJET-II-03 - previous version)

