

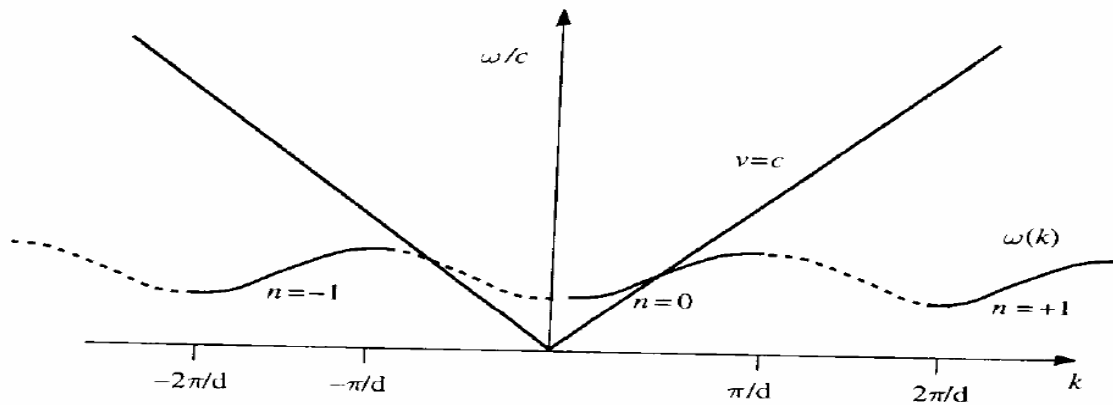
Accelerator Physics Exercises No. 4

- Answers to be handed in on 26 November 2019

Question 4.1

Using the dispersion diagramme below and assuming a four-cell cavity:

- Plot the points on the first, $n = 0$, arm of the diagramme which correspond to the appropriate k -value.
- Estimate the phase and group velocities for these points by inspection.



Question 4.2

A new 50 GeV (kinetic energy) proton synchrotron, the PS2 accelerator, has been proposed to replace the CERN PS. The new accelerator will sit in a new ring tunnel which has a mean radius of 215 m. and will receive an injected beam at 4 GeV (kinetic energy) from a new linear accelerator - the Superconducting Proton Linac (SPL). The 1.8 T magnetic field of the bending magnets is excited by a sine wave which oscillates between injection and top energy at a frequency of 0.3 Hz. Given that the mass of the proton is 0.9383 GeV:

- What is the revolution frequency at 4 GeV, 20 GeV and 50 GeV?
- Assuming the revolution frequency at 20 GeV, calculate the voltage per turn necessary to match the maximum rate of the rise of the field.
- If $\sin \phi_s = \sin 60^\circ$, what is the peak voltage necessary in the cavity? Note that $\phi_s=0$ corresponds to the zero crossing of the accelerating voltage and the particle is not accelerated.
- If the harmonic number is 32, what are the RF frequencies at 4 GeV and 50 GeV for $\phi_s=0$?

Question 4.3

Design a pill-box cavity 50 cm. long for a representative 10 MHz frequency for the PS2 accelerator. What is the resonant frequency for the next highest mode (TM_{011}) in the cavity?

Question 4.4

What is the transit-time factor for protons of 4 GeV (kinetic energy)?

Question 4.5

How strong must the electric field intensity of a travelling plane wave be to accelerate electrons with an energy gradient of 10 MeV/m? (Hint: Use the Poynting vector).

Question 4.6

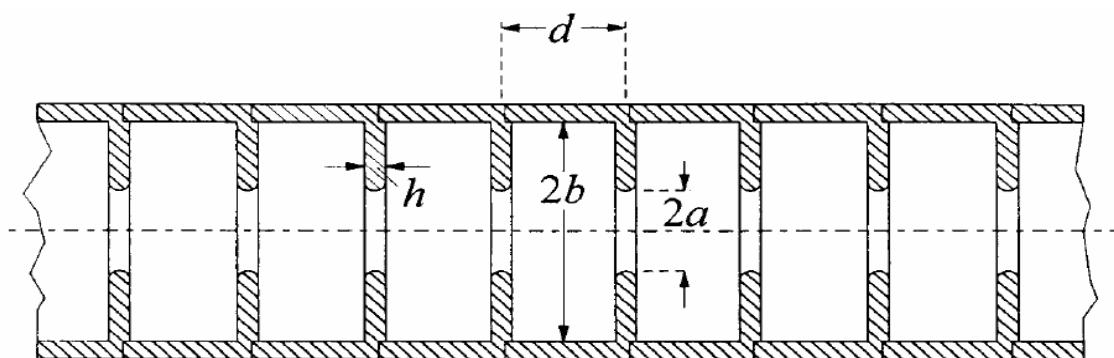
The SLAC accelerating linac structure has the design shown in the figure below with the following dimensions:

$$2b = 82.474 \text{ mm.}$$

$$2a = 22.606 \text{ mm.}$$

$$h = 5.842 \text{ mm.}$$

$$d = 35.001 \text{ mm.}$$



Assuming that the cavities are operated in the $2\pi/3$ mode with a phase velocity $\beta_z = 1$ and a supplied power of 35 MW, what is the total accelerating voltage and energy gain per metre for a SLAC structure of length $l = 3$ m.?