

Precision predictions for $pp \rightarrow tt\gamma$

Malgorzata Worek

Plan

- * Motivation for $t\bar{t}\gamma$
- * Status of theoretical predictions for $t\bar{t}\gamma$
- * NWA vs. off-shell effects $\Rightarrow t\bar{t}$
- * Results for $t\bar{t}\gamma \Rightarrow$ di-lepton channel
- * Predictions for $t\bar{t}\gamma/t\bar{t} \Rightarrow$ di-lepton channel
- * Summary: $t\bar{t} \& t\bar{t}j \& t\bar{t}\gamma \& t\bar{t}Z \Rightarrow$ di-lepton ✓
- * Outlook: $t\bar{t} \& t\bar{t}j \& t\bar{t}V, V=\gamma, Z, H, W^+ \& W^- \Rightarrow$ di-lepton & lepton-jet ✗

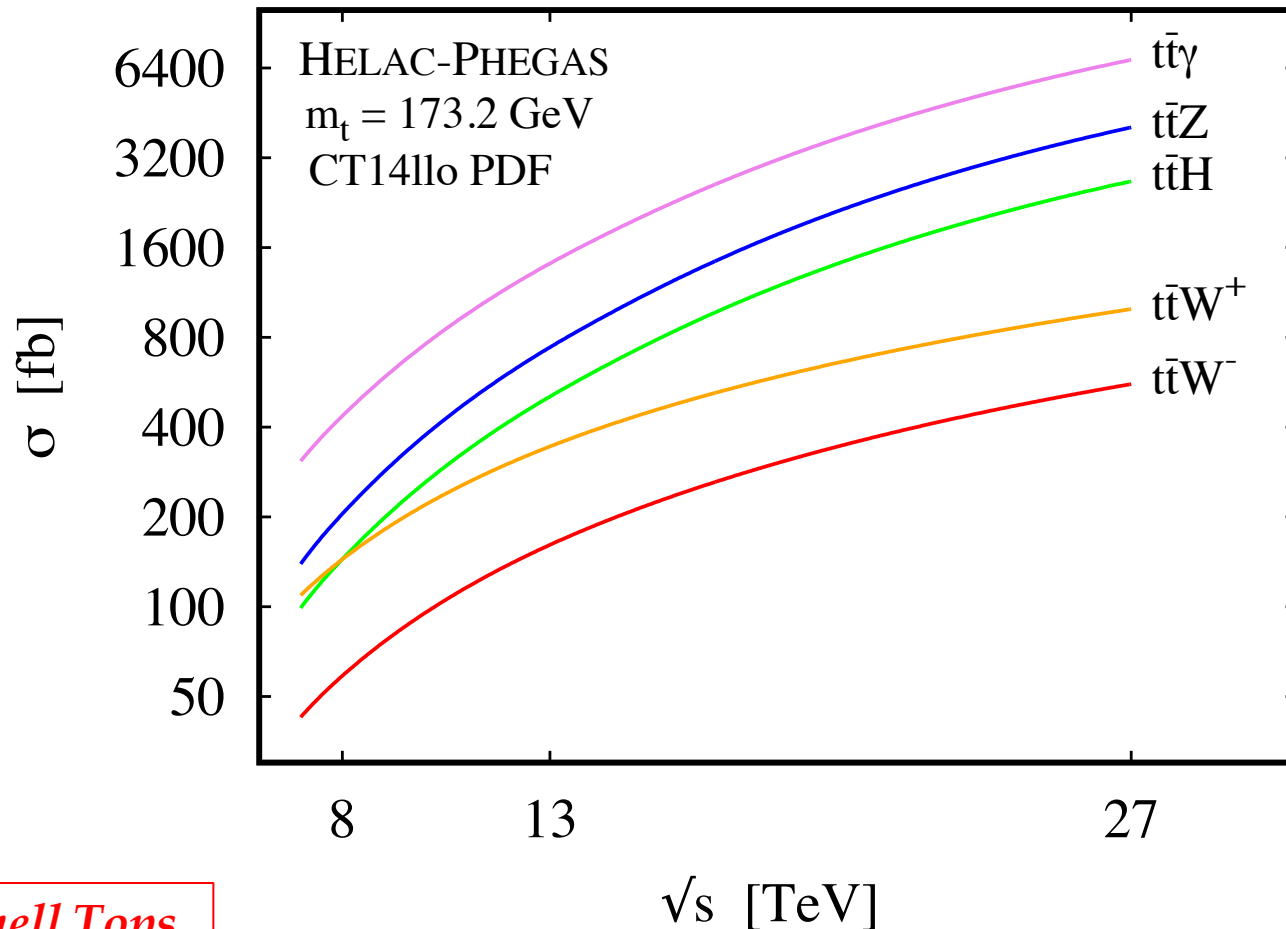
Collaborators:

- *G. Bevilacqua (University of Debrecen, Hungary)*
- *H. B. Hartanto (University of Durham, UK)*
- *M. Kraus (Florida State University, USA)*
- *T. Weber (RWTH Aachen University, Germany)*

Motivations For $t\bar{t}$

* Besides $t\bar{t}$ & $t\bar{t}j$ more exclusive final states can be accessed @ LHC

$t\bar{t}\gamma$, $t\bar{t}Z$, $t\bar{t}H$, $t\bar{t}W^+$ & $t\bar{t}W^-$ @ LHC

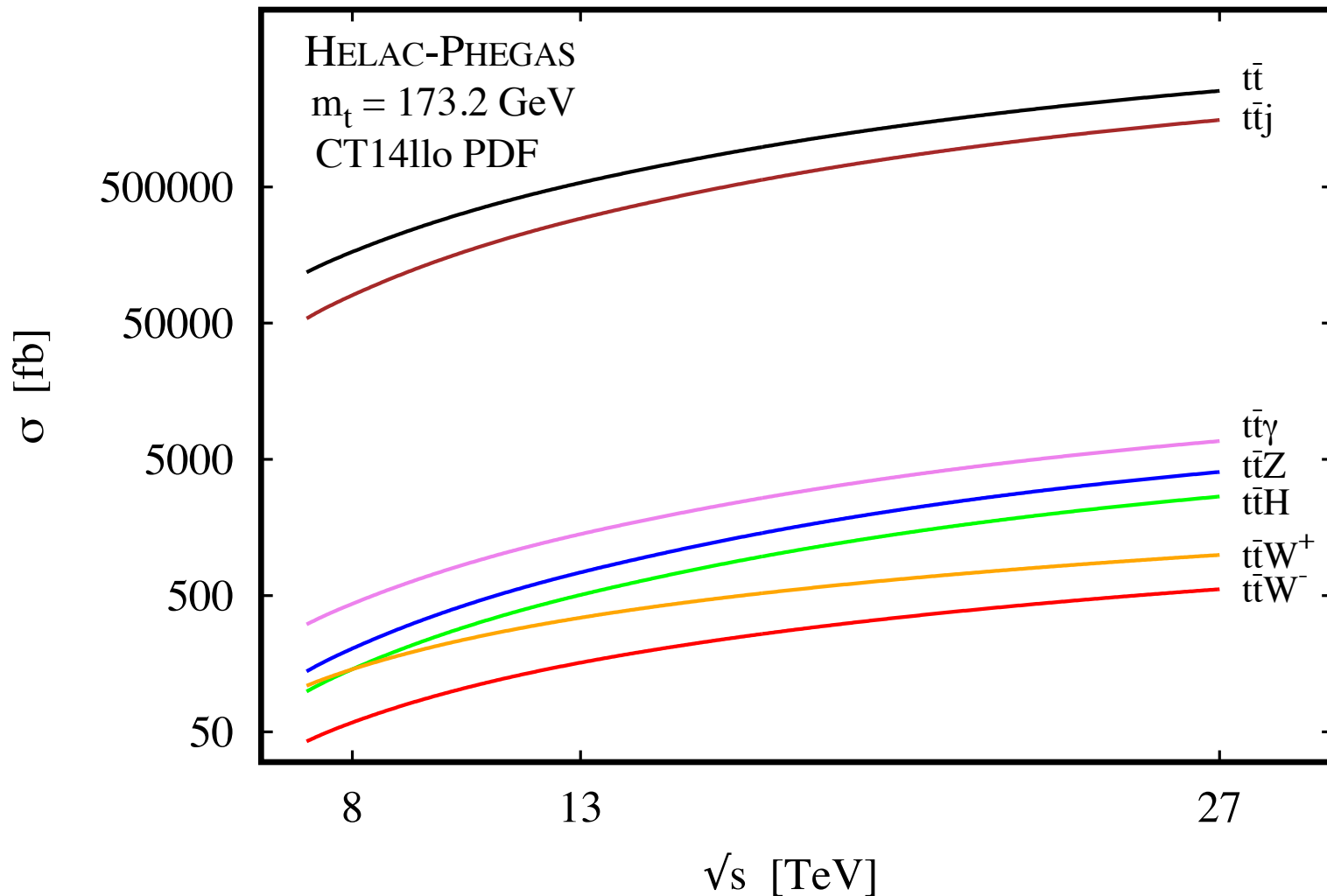


On-shell Tops

tt & $tt+X$ @ LHC

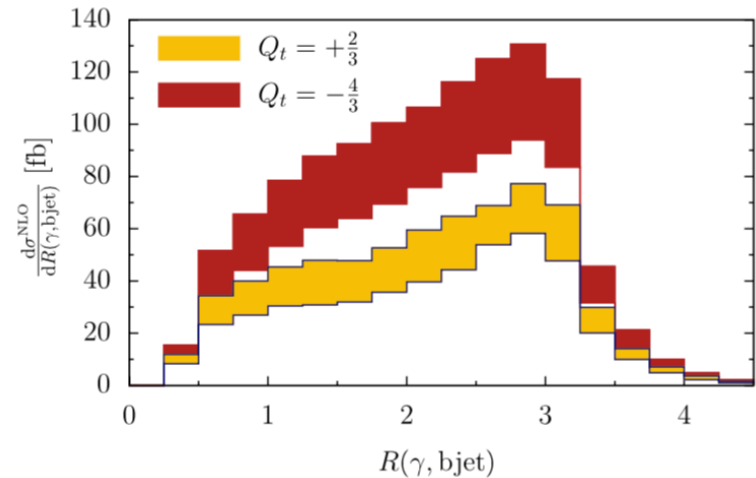
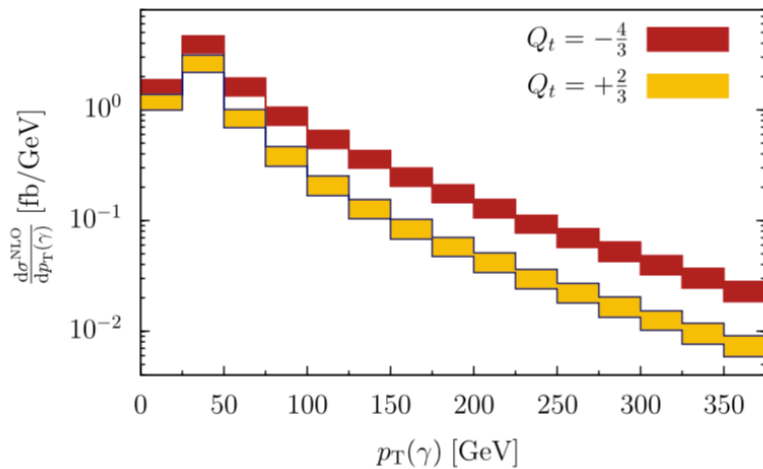
On-shell Tops

$tt, ttj, tt\gamma, ttZ, ttH, ttW^+$ & ttW^- @ LHC



Motivations For $t\bar{t}\gamma$

- * $t\bar{t}V$ cross sections much smaller than $t\bar{t}(j)$
- * Information on couplings $\Rightarrow \gamma \& Z \& H \& W^+ \& W^-$
- * $\sigma_{t\bar{t}\gamma}$ direct way to measure top quark charge @ LHC $\Rightarrow \sigma_{t\bar{t}\gamma} \sim Q_t^2$ @ LHC
- * $Q_t = +\frac{2}{3}$ with $CL \geq 5\sigma$ @ LHC \Rightarrow Indirectly from $Q_t = Q_W - Q_{b\text{-jet}}$ in $t\bar{t}$
- * Exotic physics scenarios \Rightarrow top-like quarks with $Q_t \neq +\frac{2}{3}$



Tops in NWA

$pp \rightarrow t\bar{t}\gamma \rightarrow \ell^+ \nu_e b\bar{b} j j \gamma$ @ 14 TeV LHC

Melnikov, Schulze, Scharf '11

Motivations For $t\bar{t}\gamma$

- * *Probe the strength and the structure of $t\bar{t}\gamma$ vertex* \Rightarrow SM + contributions from dimension-six effective operators \Rightarrow Constrains on anomalous couplings

$$\mathcal{L}_{t\bar{t}\gamma} = -eQ_t\bar{t}\gamma^\mu t A_\mu - e\bar{t}\frac{i\sigma^{\mu\nu}(p_t - p_{\bar{t}})_\nu}{m_t}(d_V^\gamma + id_A^\gamma\gamma_5)t A_\mu$$

- * Measure *cross section ratio* (also differential ratios)

*Aguilar-Saavedra '09
Schulze, Soreq '16*

$$\mathcal{R} = \frac{\sigma_{pp \rightarrow t\bar{t}\gamma}}{\sigma_{pp \rightarrow t\bar{t}}}$$

Bevilacqua, Hartanto, Kraus, Weber, Worek '19

- * More stable against radiative corrections
- * Reduced scale dependence \Rightarrow Various uncertainties cancel in ratio
- * Enhanced predictive power \Rightarrow Interesting to probe new physics @ LHC
- * Top quark and leptonic charge asymmetry
- * Differential asymmetries, ...

*Aguilar-Saavedra, Alvarez, Juste, Rubbo '14
Maltoni, Pagani, Tsinikos '16
Bergner, Schulze '19*

Theoretical Predictions For $t\bar{t}$

- * NLO corrections for on-shell top quarks \Rightarrow General idea about size of NLO corrections. Can not provide reliable description of top quark decay products and radiation pattern

- * *NLO QCD*

*Duan, Ma, Zhang, Han, Guo, Wang '09 '11
Maltoni, Pagani, Tsinikos '16*

- * *NLO electroweak*

Duan, Zhang, Wang, Song, Li '16

- * For more realistic studies decays are needed

- * *NLO QCD for on-shell top quarks + PS* \Rightarrow Top decays in parton shower approximation, omitting photon emission in PS evolution & omitting $t\bar{t}$ spin correlations

Kardos, Trocsanyi '14

- * *NLO QCD in NWA* \Rightarrow NLO QCD corrections to top production & decays, photon emission of top quark and of top quark decay product & $t\bar{t}$ spin correlations included

Melnikov, Schulze, Scharf '11

- * *NLO QCD complete off-shell effects of top quarks* \Rightarrow resonant & non-resonant diagrams, interferences and off-shell effects of the top quarks

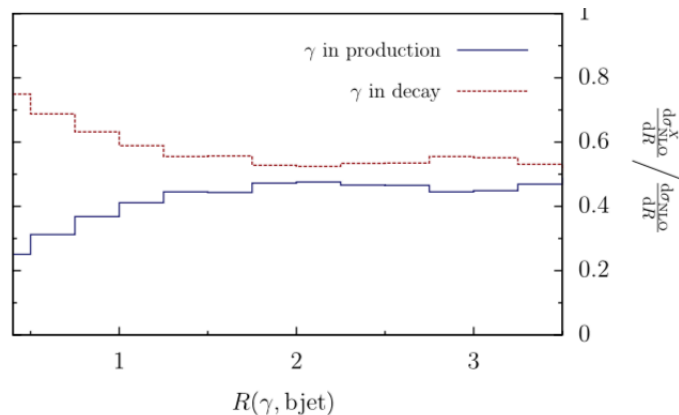
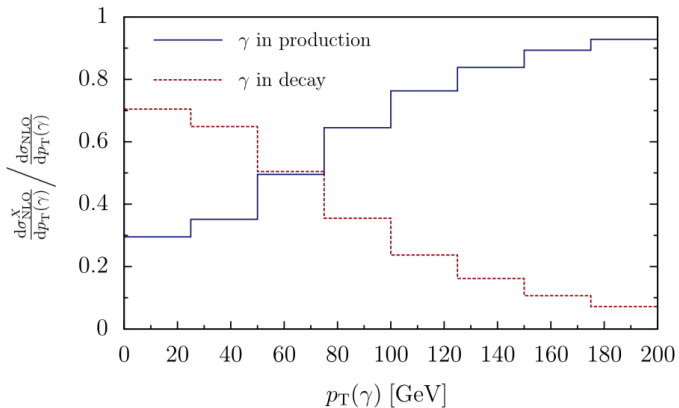
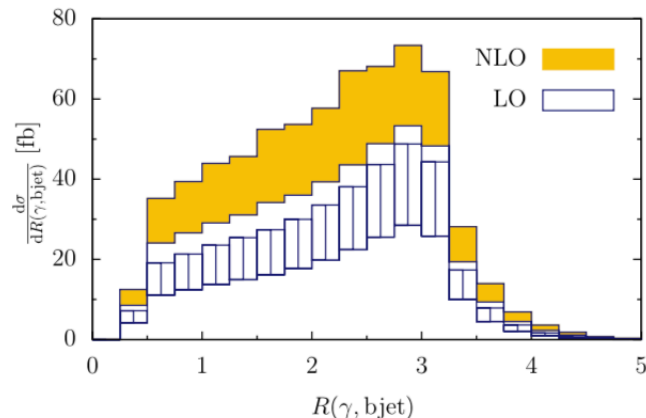
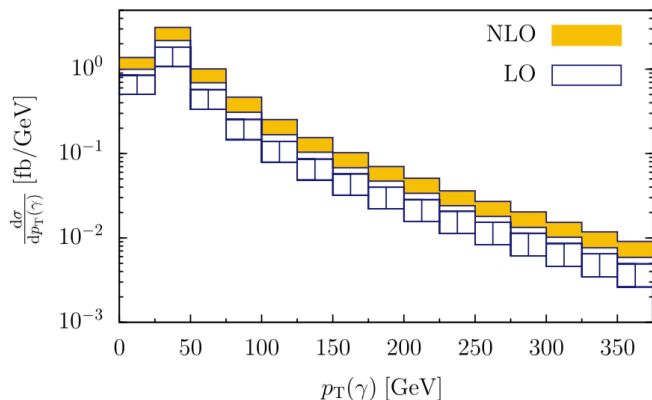
Bevilacqua, Hartanto, Kraus, Weber, Worek '18

$t\bar{t}\gamma$ in NWA @ LHC

Tops in NWA

Melnikov, Schulze, Scharf '11

$pp \rightarrow t\bar{t}\gamma \rightarrow \ell^+ \nu_\ell b\bar{b}j\gamma$ @ 14 TeV LHC



✿ Large fraction of isolated photons comes from radiative decay of tops

$$\sigma^{\text{NLO}} = 138 \text{ fb}$$

$$\sigma_{\gamma\text{-Prod.}}^{\text{NLO}} = 60.9 \text{ fb}$$

$$\sigma_{\gamma\text{-Dec.}}^{\text{NLO}} = 77.2 \text{ fb}$$

How Good Is NWA ?

* In NWA tops are restricted to on-shell states

Off-shell Tops

* Approximation is controlled by the ratio $\Rightarrow \Gamma_t/m_t \approx 0.8\%$

* Should be accurate for sufficiently inclusive observables

* *Off-shell effects for integrated σ_{tt} @ few % level @ NLO in QCD*

<i>tt (di-lepton)</i>	<i>Denner, Dittmaier, Kallweit, Pozzorini '11 '12 Bevilacqua, Czakon, van Hameren, Papadopoulos, Worek '11 Denner, Pellen '16 (EW) Jezo, Lindert, Nason, Oleari, Pozzorini '16 (PS)</i>	✓
<i>tt (semi-leptonic)</i>	<i>Denner, Pellen '18</i>	
<i>ttH (di-lepton)</i>	<i>Denner, Feger '15 Denner, Lang, Pellen, Uccirati '17 (EW+QCD)</i>	
<i>ttj (di-lepton)</i>	<i>Bevilacqua, Hartanto, Kraus, Worek '16 '18</i>	✓
<i>ttγ (di-lepton)</i>	<i>Bevilacqua, Hartanto, Kraus, Weber, Worek '18 '19</i>	✓
<i>ttZ (di-lepton)</i>	<i>Bevilacqua, Hartanto, Kraus, Weber, Worek '19</i>	✓

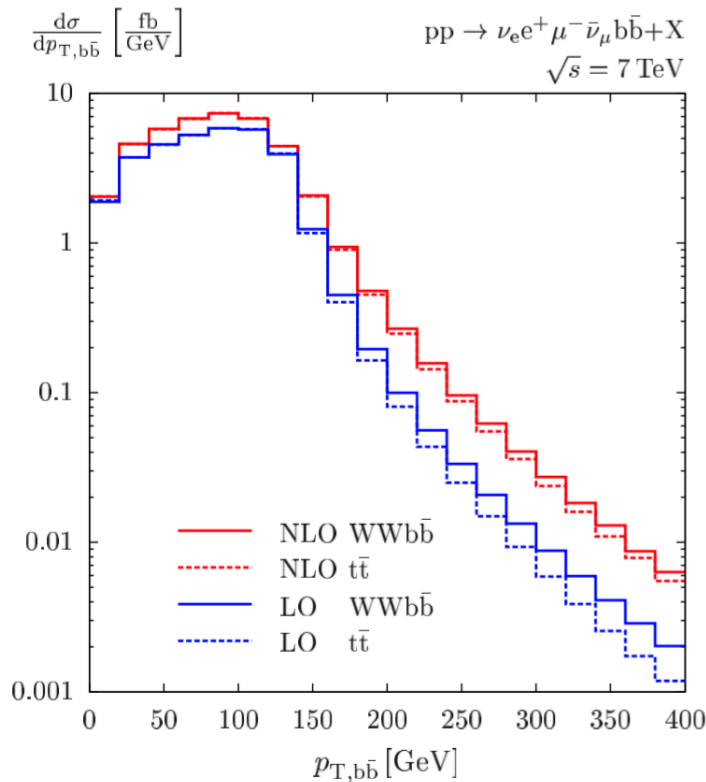
NWA & Off-Shell Effects

- ✿ Off-shell results vs. results with (spin-correlated) NWA

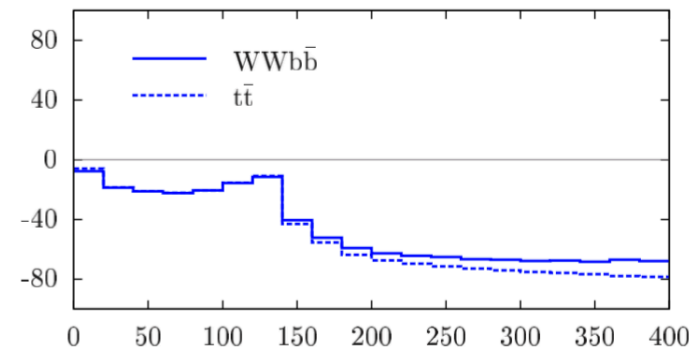
Off-shell Tops

- ✿ *Tens of per cent* in phase-space regions where $t\bar{t}$ suppressed as signal

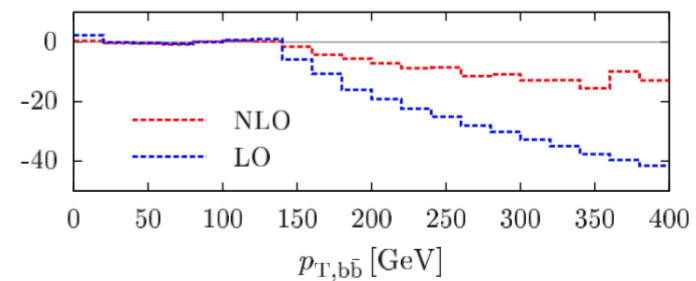
- ✿ Important as background to *Higgs & BSM searches*



LO/NLO - 1 [%]



$t\bar{t}/WWb\bar{b} - 1$ [%]

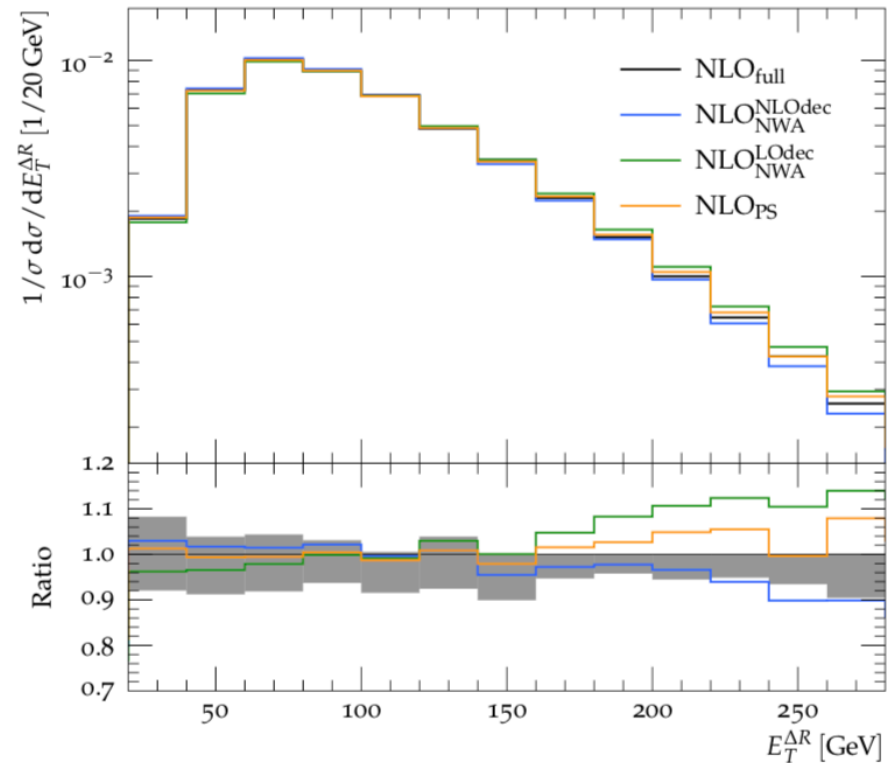
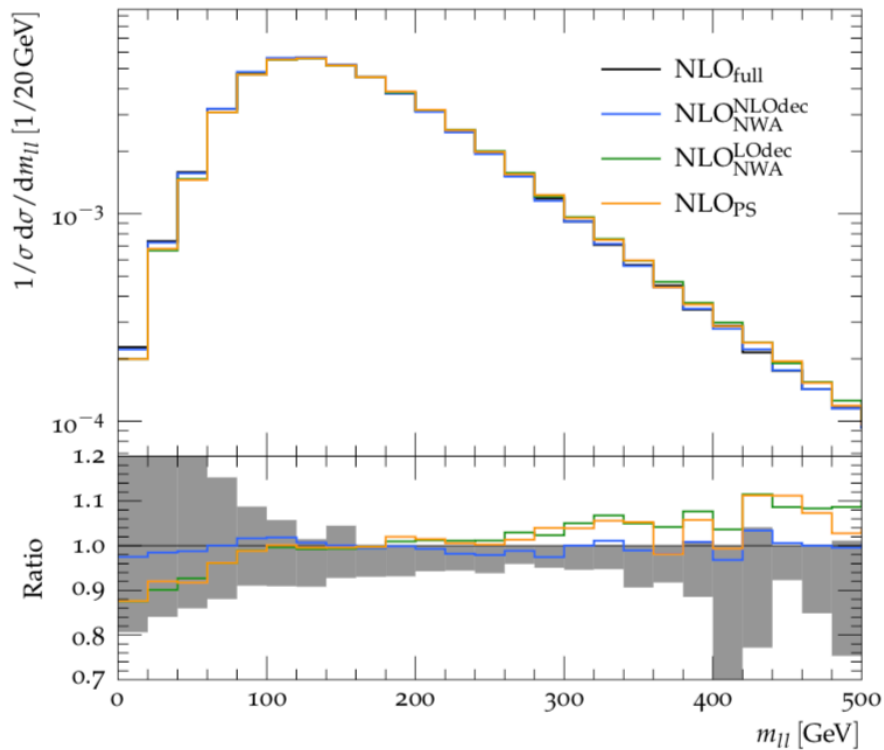


NWA & Off-Shell Effects

✦ Observables used for a recent top quark mass determination

Off-shell, NWA, PS

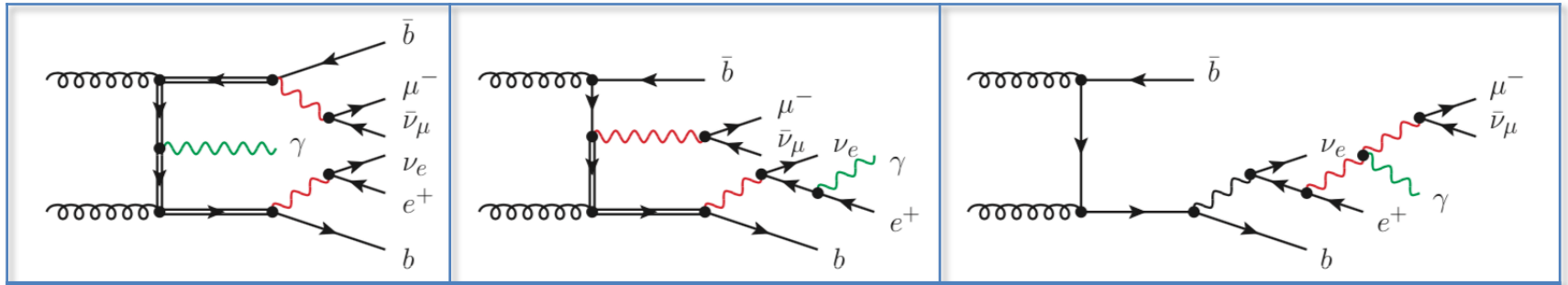
$$pp \rightarrow t\bar{t} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} \text{ @ LHC}_{13\text{TeV}}$$



NWA & Off-Shell Effects

* Feynman Diagrams \Rightarrow 628 @ LO for gg channel

$$t\bar{t}\gamma + X @ \mathcal{O}(\alpha_s^2\alpha^5)$$

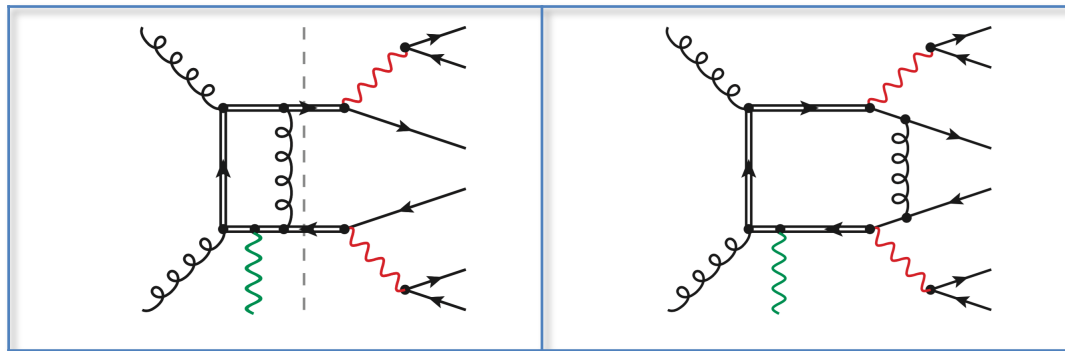


* NLO \Rightarrow 4348 real emission & 36032 @ 1-loop for gg channel

* Most complicated \Rightarrow 90 heptagons & 958 hexagons

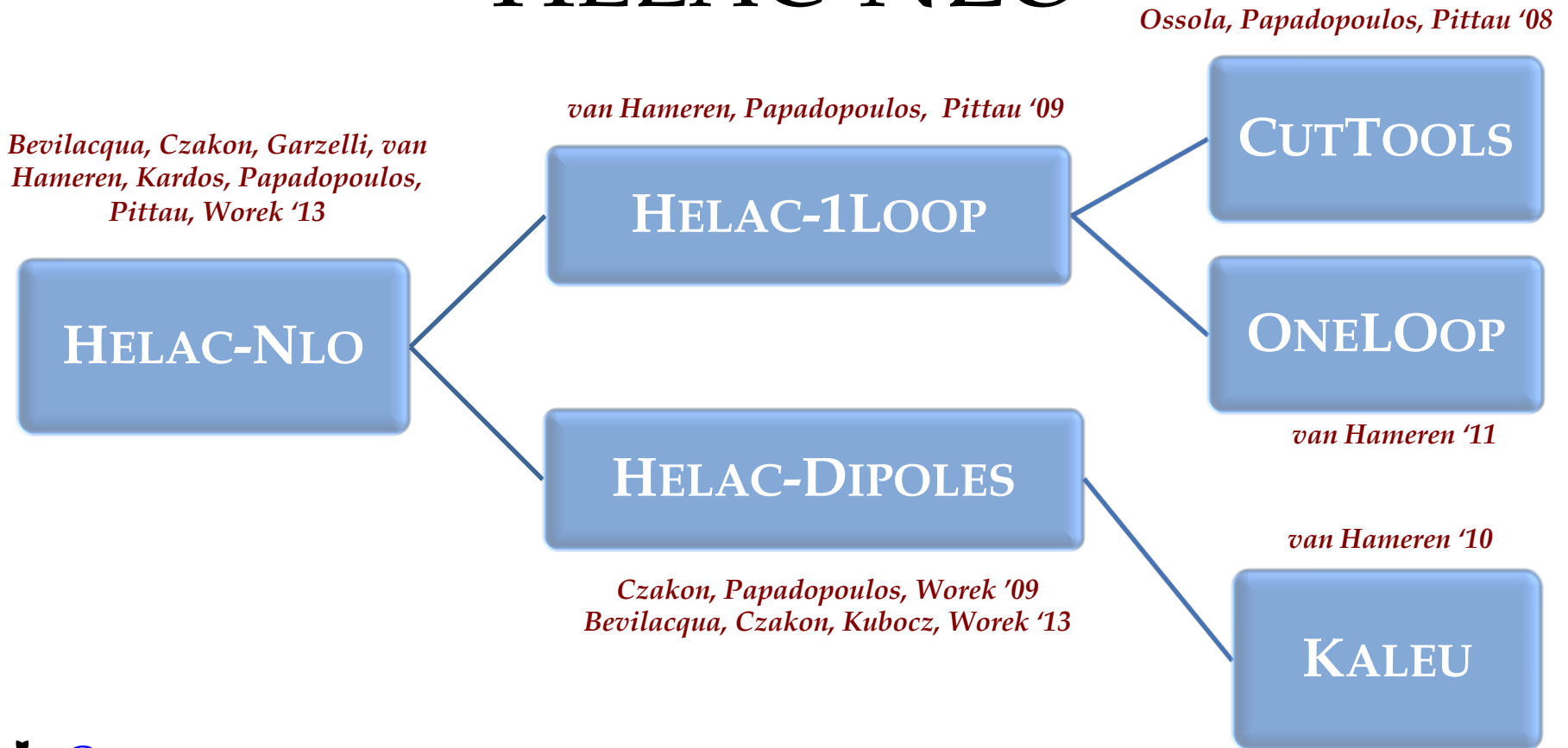
$$t\bar{t}\gamma + X @ \mathcal{O}(\alpha_s^3\alpha^5)$$

$t\bar{t}\gamma$ in NWA
up to pentagons



$t\bar{t}\gamma$ full
up to heptagons

HELAC-NLO



* *Output:*

- * Theoretical predictions stored in the form of the *Ntuples Event Files*
- * Modified *Les Houches & ROOT Event Files*
- * Kinematical cuts can be changed
- * New observables can be defined
- * Renormalization and/or factorization scales & PDFs can be changed

Setup for $t\bar{t}\gamma$

✱ Different lepton generations

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma @ \text{LHC}_{13\text{TeV}}$$

✱ Interference effects neglected \Rightarrow *Per-mille level @ LO*

✱ Contribution from b quarks in the initial state neglected \Rightarrow *Effect < 0.1% @ LO*

✱ *2 b-jets, one photon, two charged leptons & p_T^{miss}*

✱ Photon: $p_T(\gamma) > 25 \text{ GeV}, |y_\gamma| < 2.5$

✱ Isolation condition for photon \Rightarrow Reject event if $R \leq R_{\gamma j}$ with $R_{\gamma j} = 0.4$

Fraxione '98

$$\sum_i E_{T,i} \Theta(R - R_{\gamma i}) \leq E_{T,\gamma} \left(\frac{1 - \cos(R)}{1 - \cos(R_{\gamma j})} \right)$$

✱ For hard photon $\alpha = \alpha(0) = 1/137 \Rightarrow$ *Predictions decreased by 3%*

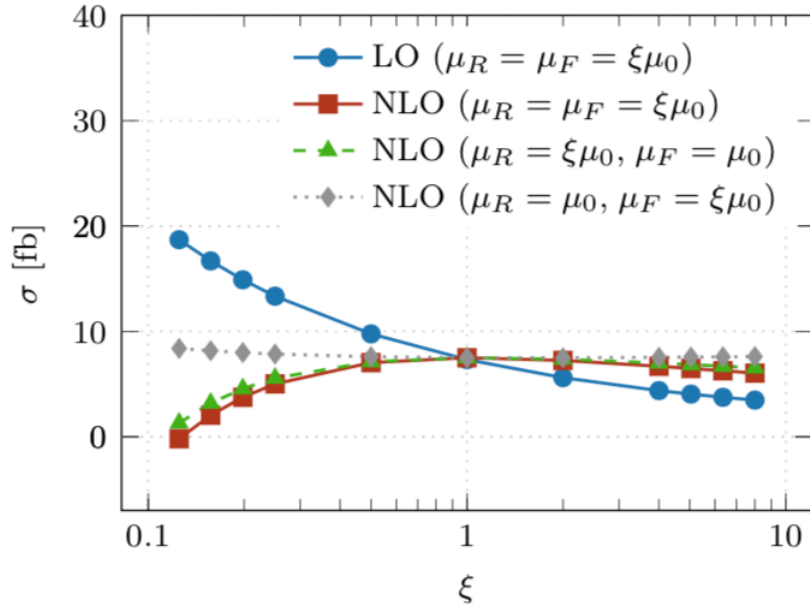
✱ Electroweak coupling in the G_μ scheme \Rightarrow account for some electroweak effects

✱ Kinematics-independent & kinematic-dependent scale: $\mu_0 = m_t/2, H_T/4$

tt̄γ with $\mu_0 = H_T/4$

Off-shell Tops

Bevilacqua, Hartanto, Kraus, Weber, Worek '18



$$\mu_R \neq \mu_F, \quad 0.5 < \mu_R/\mu_F < 2$$

$$\mu_0 = H_T/4, \text{ CT14}$$

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ @ LHC_{13TeV}

$$\sigma_{pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma}^{\text{LO}}(\text{CT14}, \mu_0 = H_T/4) = 7.32^{+2.44 (33\%)}_{-1.71 (23\%)} \text{ fb},$$

$$\sigma_{pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma}^{\text{NLO}}(\text{CT14}, \mu_0 = H_T/4) = 7.50^{+0.10 (1\%)}_{-0.46 (6\%)} \text{ fb}.$$

$$H_T = p_{T, e^+} + p_{T, \mu^-} + p_{T, j_b} + p_{T, j_{\bar{b}}} + p_T^{\text{miss}} + p_{T, \gamma}$$

✳ Positive & small *NLO corrections of 2.5%*

✳ Theoretical uncertainties

→ **33% @ LO & 6% @ NLO**

$$\sigma_{pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma}^{\text{NLO}}(\text{CT14}, \mu_0 = m_t/2) = 7.44^{+0.07 (1\%)}_{-1.03 (14\%)} [\text{scales}]^{+0.05 (1\%)}_{+0.28 (4\%)} [\text{PDF}] \text{ fb}.$$

$t\bar{t}\gamma$ with $\mu_0 = m_t/2$

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}\gamma$ @ LHC_{13TeV}

PDF	$p_{T,b}$	σ^{LO} [fb]	δ_{scale}	σ^{NLO} [fb]	δ_{scale}	δ_{PDF}	$\mathcal{K} = \frac{\text{NLO}}{\text{LO}}$
CT	25	11.78	+4.10 (35%) -2.84 (24%)	11.16	+0.11 (1%) -1.18 (11%)	+0.32 (3%) -0.35 (3%)	0.95
	30	10.63	+3.71 (35%) -2.56 (24%)	9.89	+0.09 (1%) -1.15 (12%)	+0.29 (3%) -0.31 (3%)	0.93
	35	9.44	+3.31 (35%) -2.28 (24%)	8.65	+0.07 (1%) -1.09 (13%)	+0.25 (3%) -0.27 (3%)	0.92
	40	8.27	+2.92 (35%) -2.01 (24%)	7.45	+0.06 (1%) -1.01 (14%)	+0.22 (3%) -0.24 (3%)	0.90
MMHT	25	12.81	+4.90 (38%) -3.28 (26%)	11.26	+0.09 (1%) -1.24 (11%)	+0.24 (2%) -0.21 (2%)	0.88
	30	11.55	+4.43 (38%) -2.96 (26%)	9.97	+0.07 (1%) -1.21 (12%)	+0.21 (2%) -0.19 (2%)	0.86
	35	10.24	+3.95 (39%) -2.64 (26%)	8.71	+0.07 (1%) -1.14 (13%)	+0.18 (2%) -0.17 (2%)	0.85
	40	8.96	+3.47 (39%) -2.31 (26%)	7.50	+0.07 (1%) -1.06 (14%)	+0.16 (2%) -0.14 (2%)	0.84
NNPDF	25	11.86	+4.40 (37%) -2.97 (25%)	11.58	+0.10 (1%) -1.26 (11%)	+0.16 (1%) -0.16 (1%)	0.98
	30	10.68	+3.97 (37%) -2.68 (25%)	10.27	+0.08 (1%) -1.23 (12%)	+0.14 (1%) -0.14 (1%)	0.96
	35	9.47	+3.53 (37%) -2.38 (25%)	8.97	+0.07 (1%) -1.16 (13%)	+0.12 (1%) -0.12 (1%)	0.95
	40	8.27	+3.10 (38%) -2.09 (25%)	7.73	+0.07 (1%) -1.08 (14%)	+0.11 (1%) -0.11 (1%)	0.93

Off-shell Tops

Stability w.r.t. $p_{T,b}$ cut

✿ NLO QCD corrections stable against $p_{T,b}$ cut

✿ CT14 PDF uncertainties similar/smaller than difference between various PDF sets

✿ Similar results for $p_{T,\gamma}$ cut

tty with $\mu_0 = H_T/4$

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ @ LHC_{13TeV}

PDF	$p_{T,b}$	σ^{LO} [fb]	δ_{scale}	σ^{NLO} [fb]	δ_{scale}	δ_{PDF}	$\mathcal{K} = \frac{\text{NLO}}{\text{LO}}$
CT	25	10.68	+3.54 (33%) -2.49 (23%)	11.19	+0.16 (1%) -0.54 (5%)	+0.32 (3%) -0.35 (3%)	1.05
	30	9.58	+3.18 (33%) -2.24 (23%)	9.93	+0.14 (1%) -0.54 (5%)	+0.28 (3%) -0.31 (3%)	1.04
	35	8.44	+2.80 (33%) -1.97 (23%)	8.69	+0.12 (1%) -0.50 (6%)	+0.25 (3%) -0.27 (3%)	1.03
	40	7.32	+2.45 (33%) -1.71 (23%)	7.50	+0.11 (1%) -0.45 (6%)	+0.22 (3%) -0.23 (3%)	1.02
MMHT	25	11.59	+4.22 (36%) -2.88 (25%)	11.29	+0.16 (1%) -0.57 (5%)	+0.24 (2%) -0.22 (2%)	0.97
	30	10.38	+3.78 (36%) -2.58 (25%)	10.02	+0.13 (1%) -0.58 (6%)	+0.22 (2%) -0.19 (2%)	0.97
	35	9.12	+3.33 (36%) -2.26 (25%)	8.77	+0.11 (1%) -0.54 (6%)	+0.19 (2%) -0.17 (2%)	0.96
	40	7.90	+2.89 (37%) -1.96 (25%)	7.57	+0.09 (1%) -0.48 (6%)	+0.16 (2%) -0.15 (2%)	0.96
NNPDF	25	10.78	+3.82 (35%) -2.62 (24%)	11.62	+0.17 (1%) -0.58 (5%)	+0.16 (1%) -0.16 (1%)	1.08
	30	9.65	+3.42 (35%) -2.34 (24%)	10.31	+0.14 (1%) -0.58 (6%)	+0.14 (1%) -0.14 (1%)	1.07
	35	8.48	+3.01 (35%) -2.05 (24%)	9.02	+0.12 (1%) -0.53 (6%)	+0.12 (1%) -0.12 (1%)	1.06
	40	7.34	+2.61 (36%) -1.78 (24%)	7.79	+0.10 (1%) -0.48 (6%)	+0.11 (1%) -0.11 (1%)	1.06

Off-shell Tops

Stability w.r.t. $p_{T,b}$ cut

✿ NLO QCD corrections stable against $p_{T,b}$ cut

✿ CT14 PDF uncertainties similar/smaller than difference between various PDF sets

✿ Similar results for $p_{T,\gamma}$ cut

$t\bar{t}\gamma$ with $\mu_0 = m_t/2$ & $\mu_0 = H_T/4$

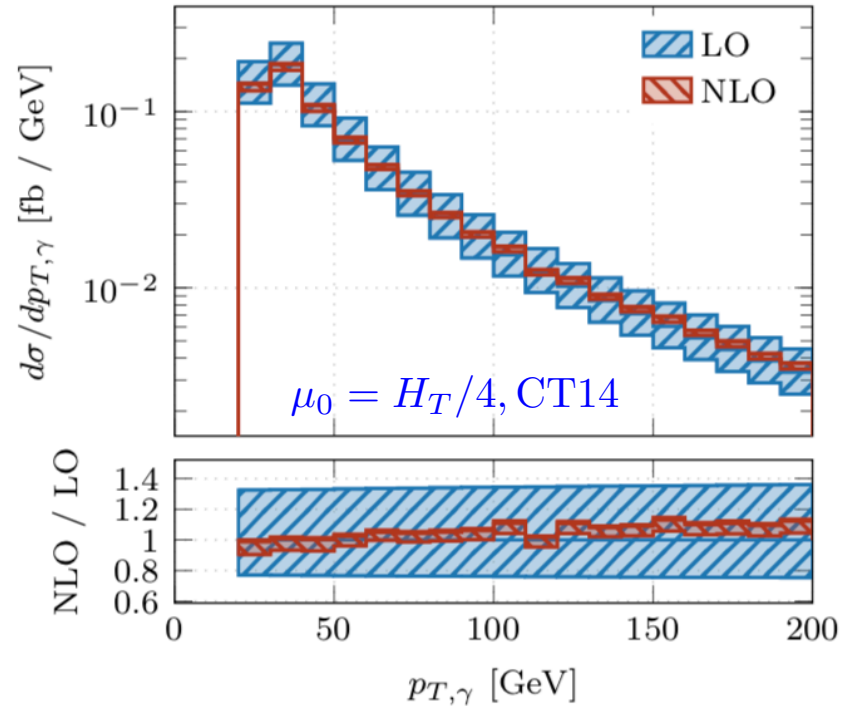
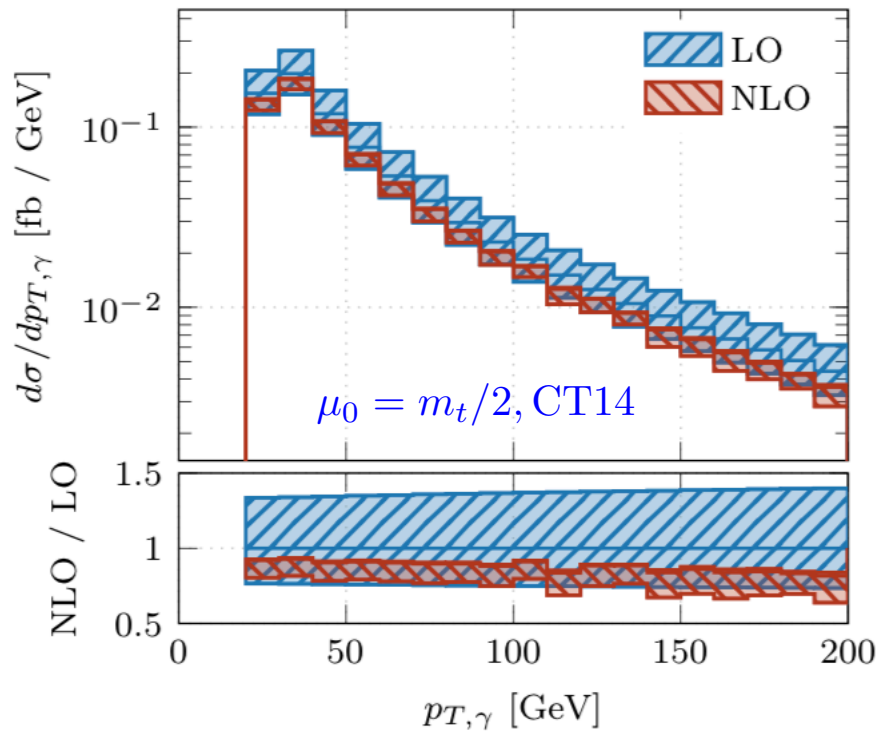
LHC_{13 TeV}

$p_T(\gamma)$

Off-shell Tops

Bevilacqua, Hartanto, Kraus, Weber, Worek '18

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}\gamma$ @ LHC_{13 TeV}



- ✱ Negative NLO corrections up to 18%
- ✱ Theoretical error up to $\pm 22\%$

- ✱ Positive NLO corrections up to 13%
- ✱ NLO error bands within LO
- ✱ Theoretical error up to $\pm 8\%$

$t\bar{t}\gamma$ with $\mu_0 = m_t/2$ & $\mu_0 = H_T/4$

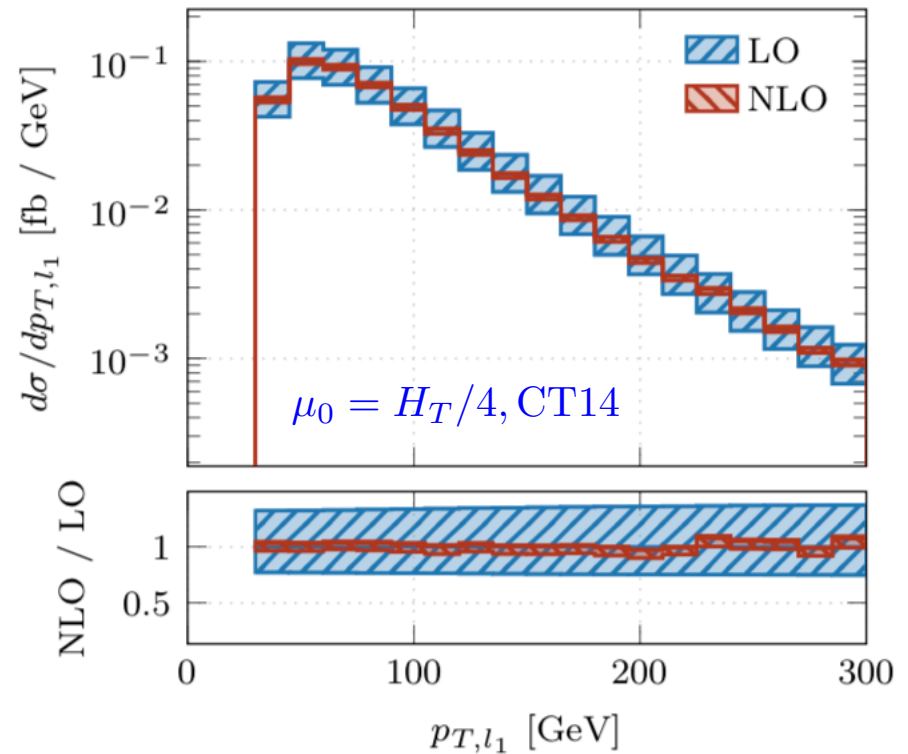
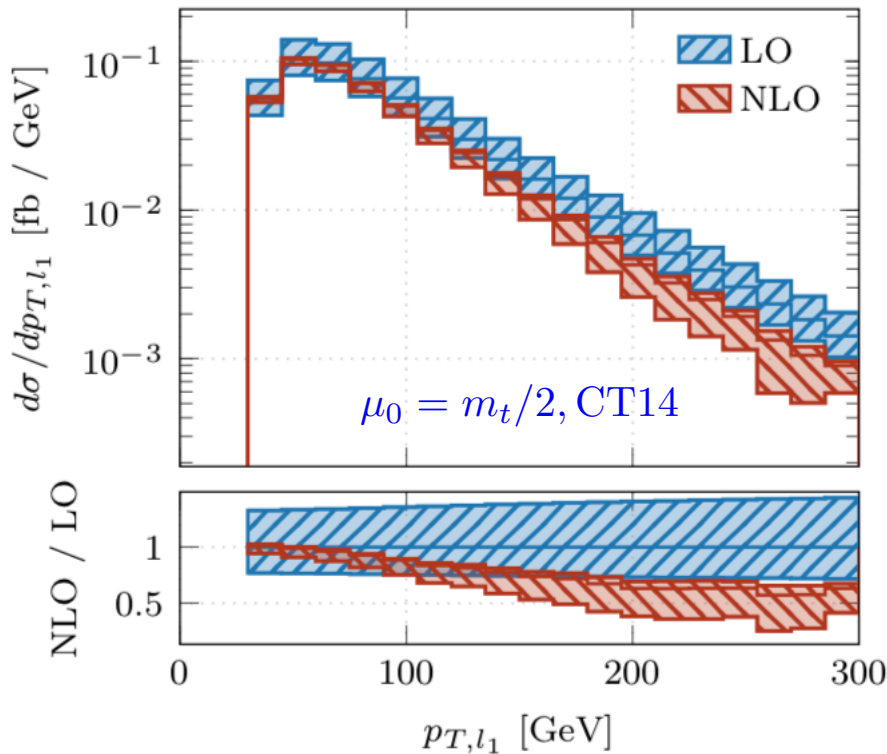
$p_T(l_1)$

Off-shell Tops

LHC_{13 TeV}

Bevilacqua, Hartanto, Kraus, Weber, Worek '18

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ @ LHC_{13 TeV}



- * NLO Corrections up to **- 43%**
- * Theoretical uncertainties up to **$\pm 56\%$**

- * NLO Corrections up to **+ 8%**
- * Error reduced down to **$\pm 7\%$**

*Dynamical scale very effective in stabilizing perturbative convergence !
Provides smaller theoretical error !*

$t\bar{t}\gamma/t\bar{t}$

Off-shell Tops

* Can we decrease theoretical error even further for $t\bar{t}\gamma$?

* For *fiducial cross section* with dynamical scale we have $\pm 6\%$

* For *differential distributions* we have $\pm (10\% - 30\%)$

$$\mathcal{R} = \frac{\sigma_{t\bar{t}\gamma}^{\text{NLO}}(\mu_1)}{\sigma_{t\bar{t}}^{\text{NLO}}(\mu_2)}$$

* **ANSWER IS YES** \Rightarrow with $t\bar{t}\gamma/t\bar{t}$ we have $\pm (1\% - 3\%)$
for *integrated cross section ratio*

* *Differential cross section ratios* $\pm (1\% - 6\%)$

$$\mathcal{R}_X = \left(\frac{d\sigma_{t\bar{t}\gamma}^{\text{NLO}}(\mu_1)}{dX} \right) \left(\frac{d\sigma_{t\bar{t}}^{\text{NLO}}(\mu_2)}{dX} \right)^{-1}$$

* High precision comparable to NNLO QCD results for top quark physics !

* *Processes need to be correlated* \Rightarrow top quark pair production excellent candidate

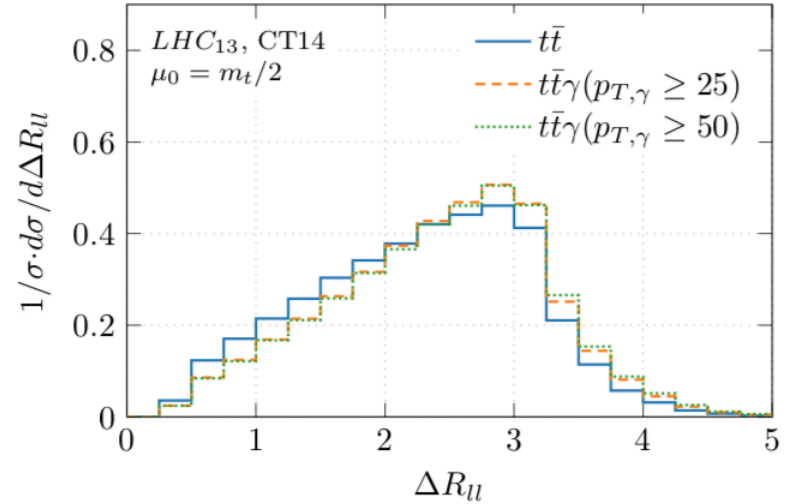
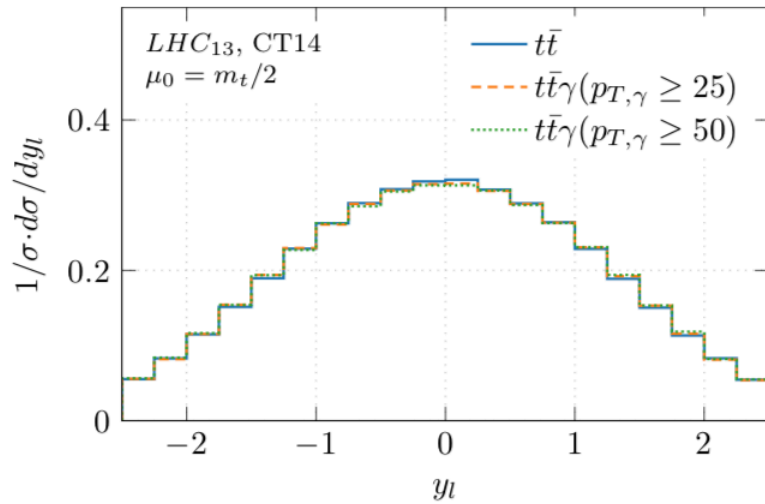
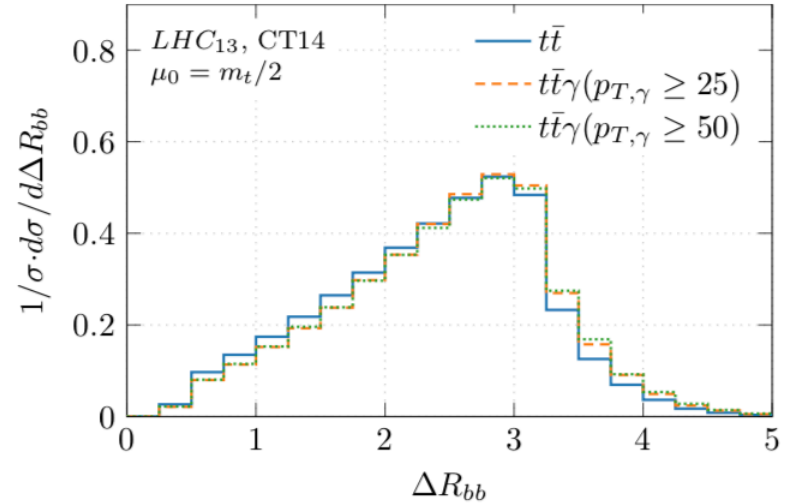
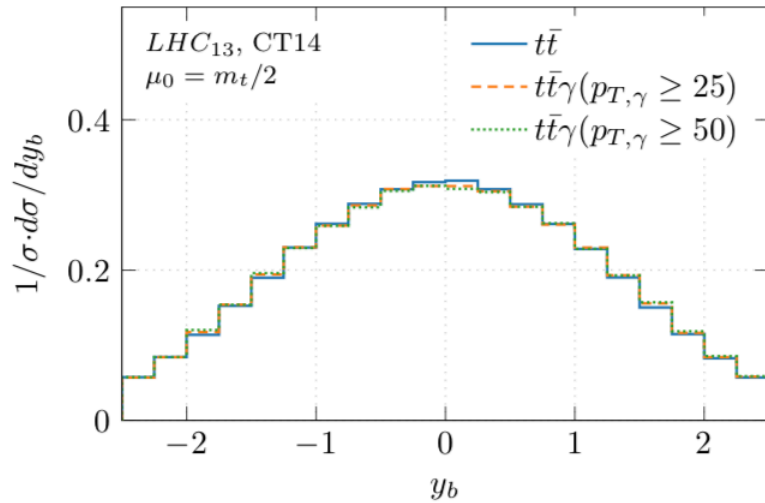
$$\left(\frac{\mu_1}{\mu_0}, \frac{\mu_2}{\mu_0} \right) = \{(2, 2), (0.5, 0.5)\}$$

* *Similar dynamical scale choice need to be implemented for μ_1 and μ_2 !*

$t\bar{t}\gamma$ & $t\bar{t}$

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}\gamma$ @ LHC₁₃TeV

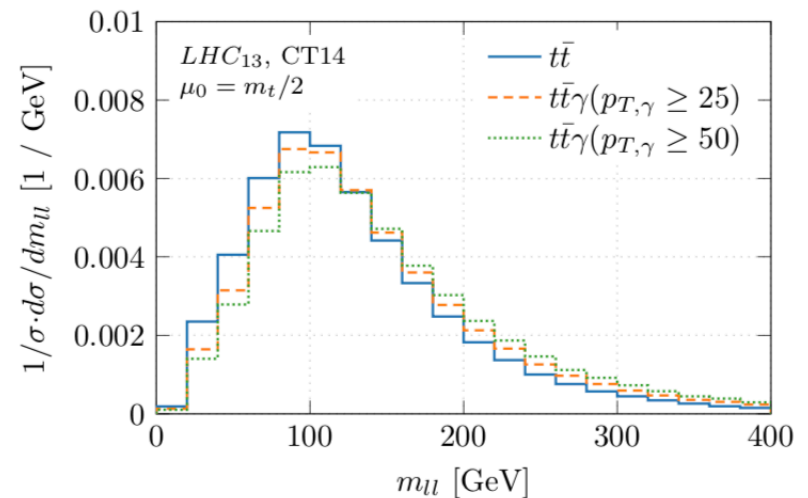
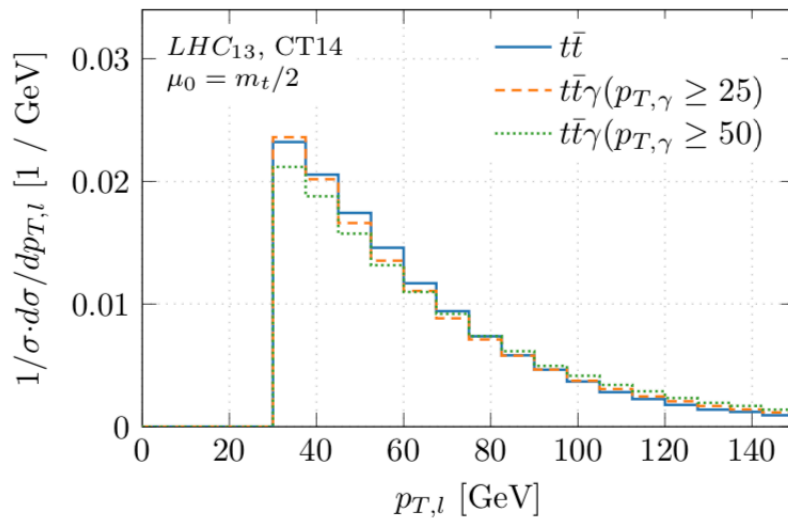
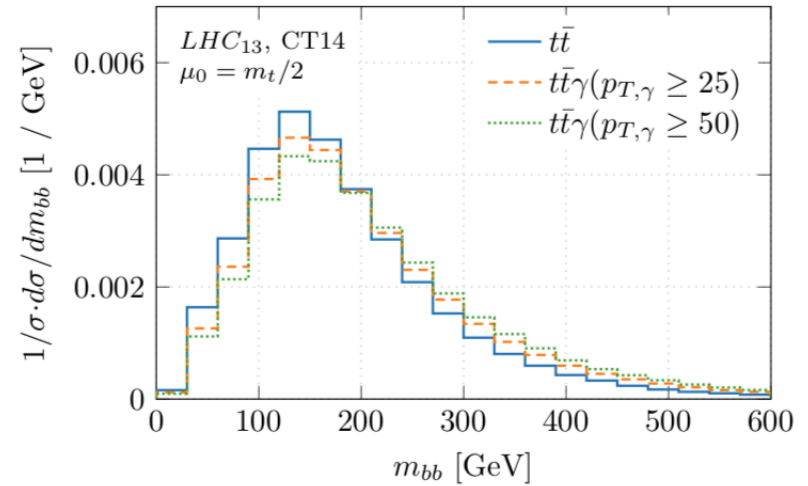
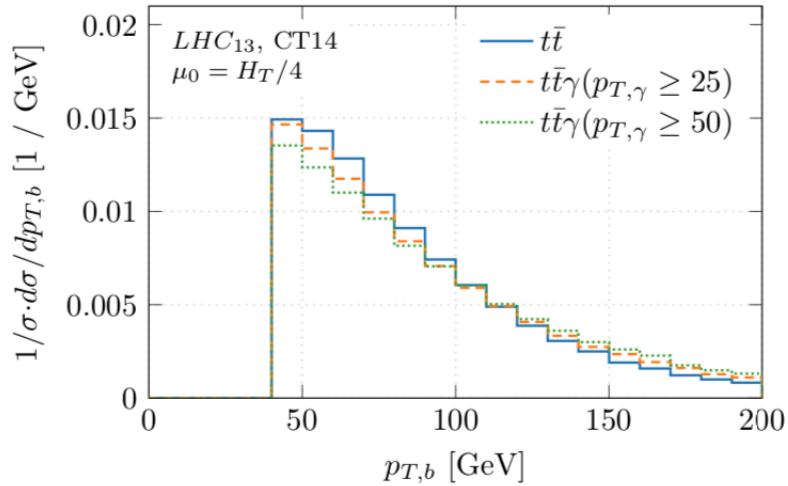
Off-shell Tops



$t\bar{t}\gamma$ & $t\bar{t}$

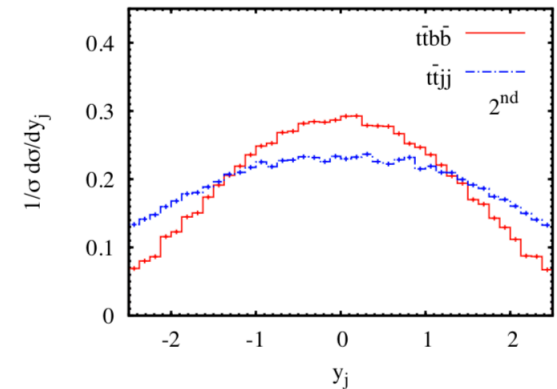
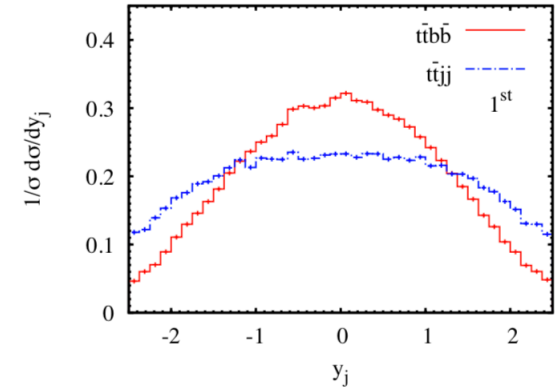
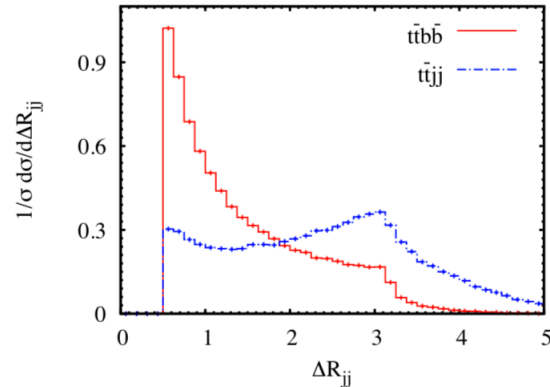
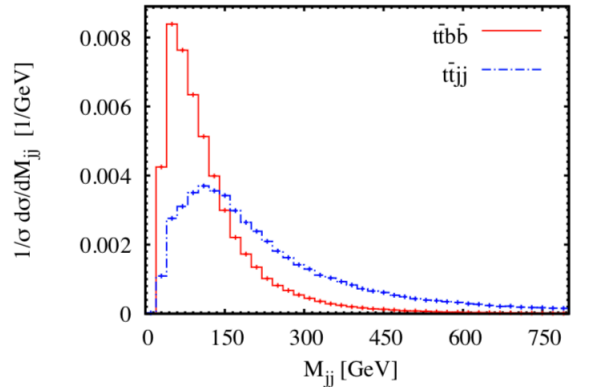
$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}\gamma$ @ LHC₁₃TeV

Off-shell Tops



ttbb & ttjj

$pp \rightarrow t\bar{t}b\bar{b} \text{ \& \ } t\bar{t}jj \text{ @ LHC}_{8\text{TeV}}$



- ✿ Different jet kinematics makes the ttbb and ttjj processes uncorrelated in several observables
- ✿ Scale uncertainty is not significantly reduced when taking ratio of cross sections

On-shell Tops

LHC_{8TeV}

$t\bar{t}\gamma/t\bar{t}$

Off-shell Tops

$$\mathcal{R} = \frac{\sigma_{t\bar{t}\gamma}^{\text{NLO}}(\mu_1)}{\sigma_{t\bar{t}}^{\text{NLO}}(\mu_2)}$$

$$\mathcal{R}(\mu_0 = m_t/2, \text{CT14}, p_{T,\gamma} > 25 \text{ GeV}) = (4.56 \pm 0.25) \cdot 10^{-3} (5\%),$$

$$\mathcal{R}(\mu_0 = H_T/4, \text{CT14}, p_{T,\gamma} > 25 \text{ GeV}) = (4.62 \pm 0.06) \cdot 10^{-3} (1\%),$$

$$\mathcal{R}(\mu_0 = m_t/2, \text{CT14}, p_{T,\gamma} > 50 \text{ GeV}) = (1.89 \pm 0.16) \cdot 10^{-3} (8\%),$$

$$\mathcal{R}(\mu_0 = H_T/4, \text{CT14}, p_{T,\gamma} > 50 \text{ GeV}) = (1.93 \pm 0.06) \cdot 10^{-3} (3\%).$$

✳ Our best NLO QCD predictions with dynamical scale choice:

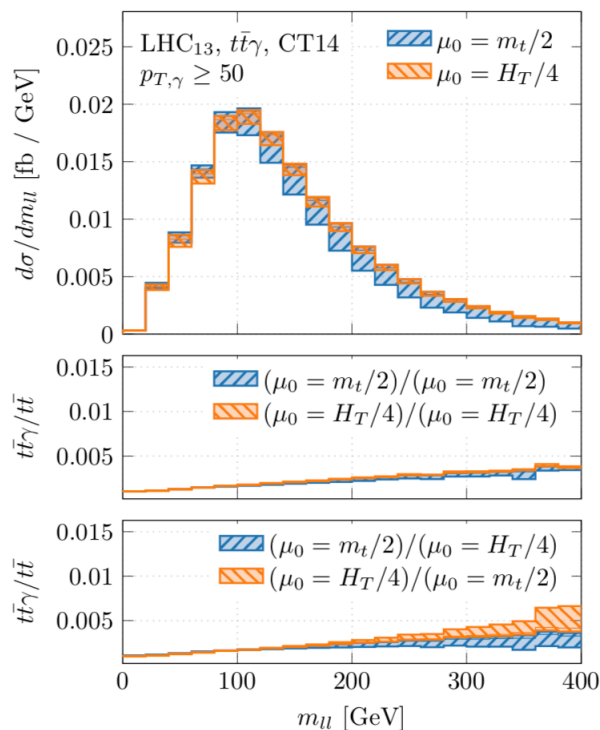
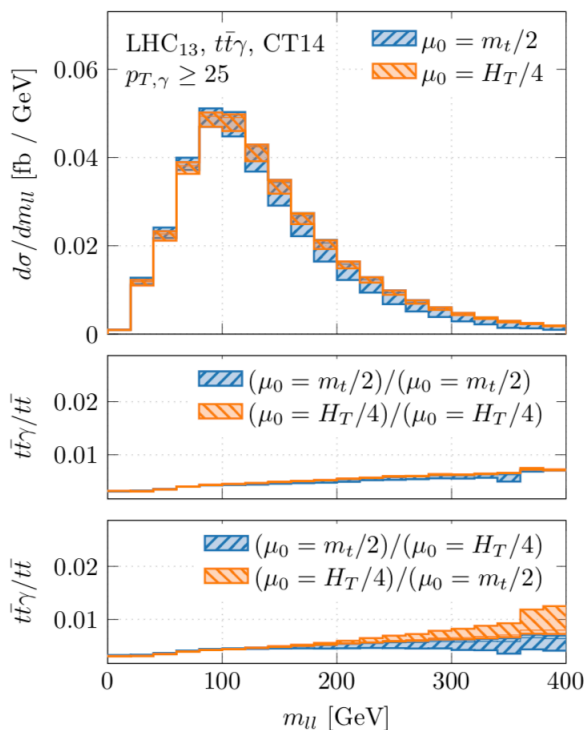
$$\mathcal{R}(\mu_0 = H_T/4, \text{CT14}, p_{T,\gamma} > 25 \text{ GeV}) = (4.62 \pm 0.06 [\text{scales}] \pm 0.02 [\text{PDFs}]) \cdot 10^{-3}$$

$$\mathcal{R}(\mu_0 = H_T/4, \text{CT14}, p_{T,\gamma} > 50 \text{ GeV}) = (1.93 \pm 0.06 [\text{scales}] \pm 0.02 [\text{PDFs}]) \cdot 10^{-3},$$

Differential Cross Section Ratio

Bevilacqua, Hartanto, Kraus, Weber, Worek '19

Off-shell Tops



$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ @ LHC₁₃TeV

Theoretical uncertainties:

$\pm (1\% - 4\%)$
dynamical scale

$\pm (20\% - 25\%)$
fixed scale

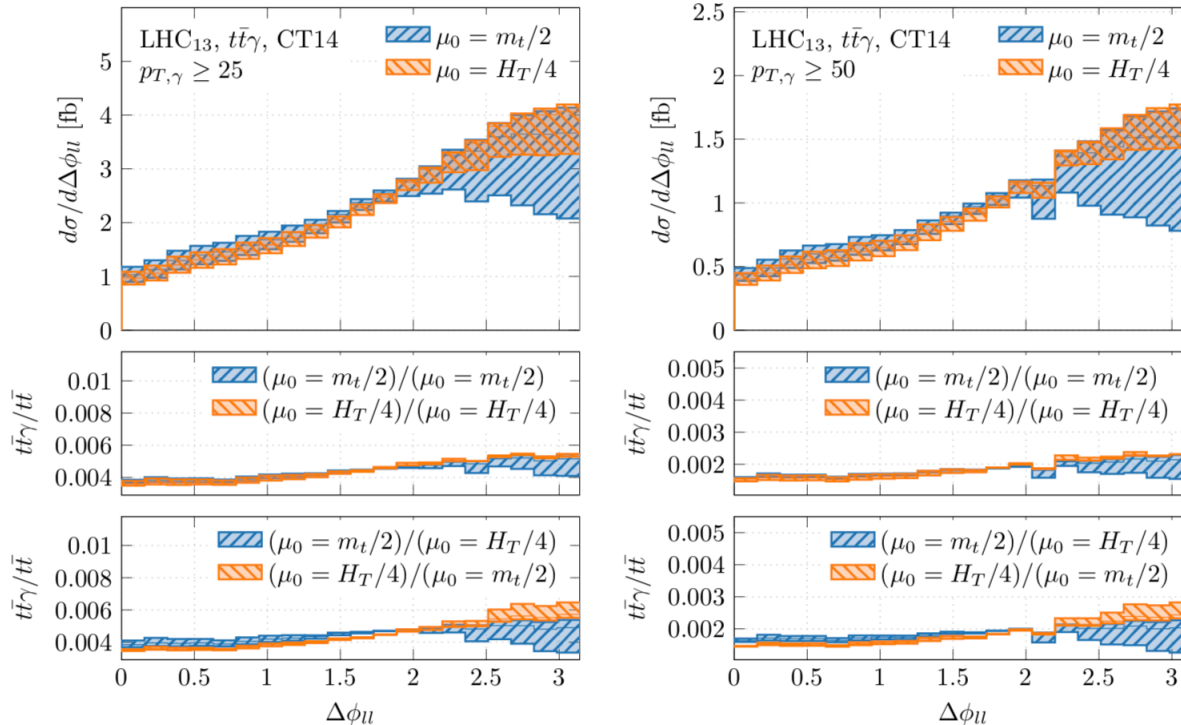
✿ Should be compared to uncertainties for absolute differential cross section
 ✿ *up to $\pm 10\%$ for $\mu_0 = H_T/4$ & up to $\pm 50\%$ for $\mu_0 = m_t/2$*

✿ When different scales are used in numerator and denominator *up to 60%*

Differential Cross Section Ratio

Bevilacqua, Hartanto, Kraus, Weber, Worek '19

Off-shell Tops



$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma @ \text{LHC}_{13\text{TeV}}$

Theoretical
uncertainties:

$\pm (2\% - 3\%)$
dynamical scale

$\pm (20\% - 30\%)$
fixed scale

✿ Should be compared to uncertainties for absolute differential cross section
 ✿ up to $\pm 20\%$ for $\mu_0 = H_T/4$ & up to $\pm 50\%$ for $\mu_0 = m_t/2$

✿ When different scales are used in numerator and denominator up to 60%

Summary

Off-shell Tops

- * The most precise NLO QCD theoretical predictions for $t\bar{t}\gamma$ in di-lepton channel
 - * Complete off-shell effects for top quarks
 - * *Corrections to production & decays & $t\bar{t}$ spin correlations*
 - * *Photon emission of top quark and of top quark decay product*
 - * *Possibility of using kinematic-dependent scales*
- * NLO QCD corrections stable against $p_{T,\gamma}$ & $p_{T,b}$ cut
- * CT14 PDF uncertainties similar/smaller than difference between various PDF sets
- * Uncertainties due to scale dependence dominant source of theoretical systematics
- * $t\bar{t}\gamma$ relevant for BSM searches and studies of top quark properties
- * Cross section ratio(s) increase precision without going to NNLO QCD !

Outlook

✱ Similar results in di-lepton channel for

Off-shell Tops

✱ $pp \rightarrow tt$

✱ $pp \rightarrow ttj$

✱ $pp \rightarrow ttZ (Z \rightarrow \nu \nu)$

✱ Backgrounds for new physics searches, e.g. $pp \rightarrow tt + p_T^{miss}$

✱ $pp \rightarrow tt$ & $pp \rightarrow ttZ (Z \rightarrow \nu \nu) \Rightarrow$ reducible & irreducible backgrounds

✱ (some letter)MSSM, Dark Matter Models, Simplified Models, ...

✱ Precise measurements of the top-quark fiducial cross sections

✱ Precise measurements of top-quark properties @ LHC $\Rightarrow m_t$ & α_s & PDFs & ...

✱ *Next steps:*

✱ *Comparisons:* NWA vs. off-shell effects dedicated studies for $tt\gamma$

✱ *New processes:* $pp \rightarrow ttW^+$ & $pp \rightarrow ttW^- \Rightarrow$ di-lepton

✱ *New processes:* $tt, ttj, ttV, V = \gamma, H, Z, W^+ \& W^- \Rightarrow$ lepton+jet

Backup

SM parameters & Cuts for $t\bar{t}$

$$m_W = 80.385 \text{ GeV},$$

$$m_Z = 91.1876 \text{ GeV},$$

$$\Gamma_t^{\text{LO}} = 1.47848 \text{ GeV},$$

$$m_t = 173.2 \text{ GeV},$$

$$\Gamma_W = 2.0988 \text{ GeV},$$

$$\Gamma_Z = 2.50782 \text{ GeV},$$

$$\Gamma_t^{\text{NLO}} = 1.35159 \text{ GeV},$$

$$G_\mu = 1.166378 \times 10^{-5} \text{ GeV}^{-2}.$$

$$p_{T,\ell} > 30 \text{ GeV},$$

$$p_{T,b} > 40 \text{ GeV},$$

$$p_T^{\text{miss}} > 20 \text{ GeV},$$

$$|y_\ell| < 2.5,$$

$$|y_b| < 2.5,$$

$$\Delta R_{\ell\gamma} > 0.4,$$

$$\Delta R_{\ell\ell} > 0.4,$$

$$\Delta R_{bb} > 0.4,$$

$$\Delta R_{\ell b} > 0.4,$$

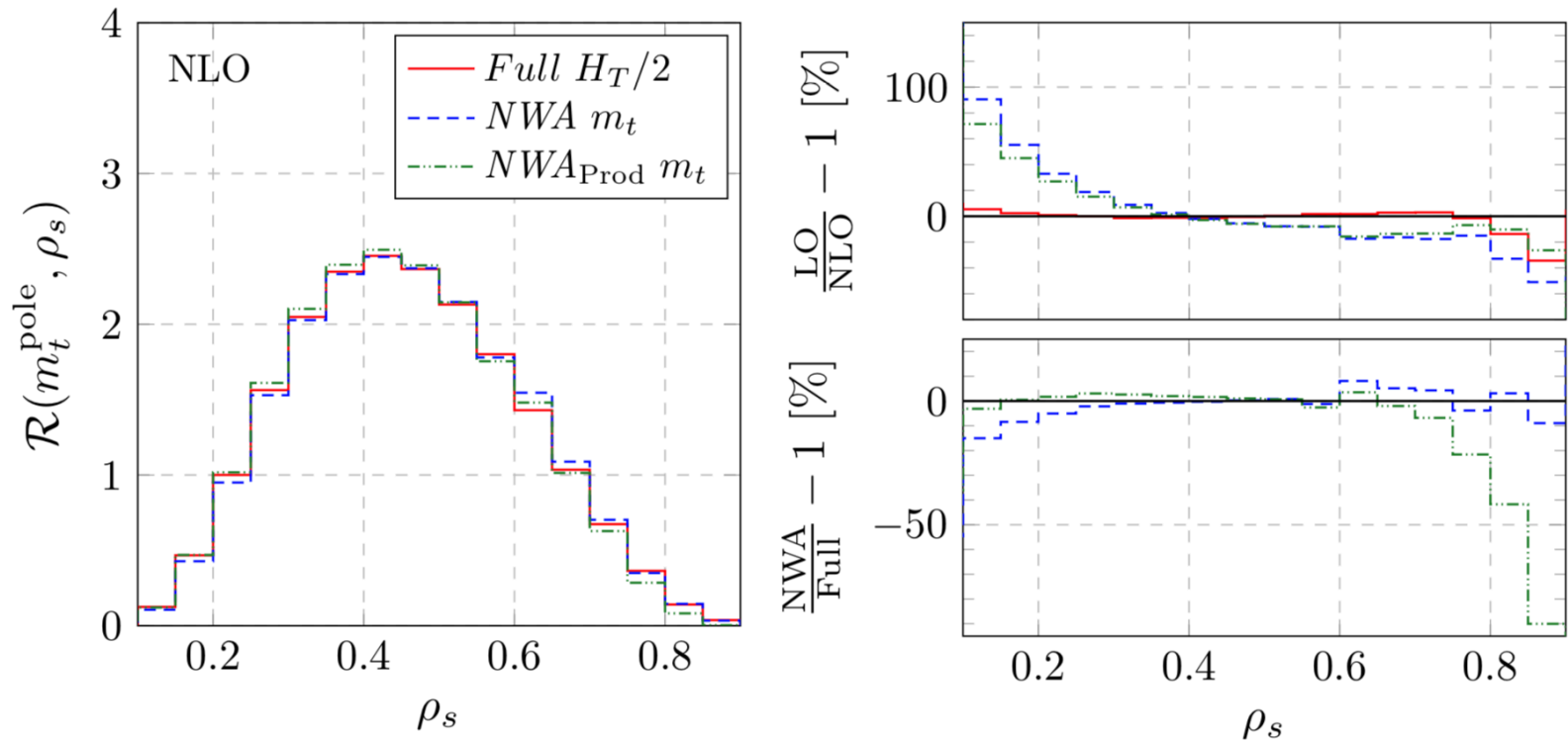
NWA & Off-Shell Effects

❖ Observable used for a recent *top quark mass determination*

Off-shell, NWA

$pp \rightarrow t\bar{t}j \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}j$ @ LHC_{13TeV}

Bevilacqua, Hartanto, Kraus, Schulze, Worek '18



$$\mathcal{R}(m_t^{\text{pole}}, \rho_s) = \frac{1}{\sigma_{t\bar{t}j}} \frac{d\sigma_{t\bar{t}j}}{d\rho_s}(m_t^{\text{pole}}, \rho_s)$$

$$\rho_s = \frac{2m_0}{M_{t\bar{t}j}}$$

NWA & Off-Shell Effects

25 fb⁻¹

$$pp \rightarrow t\bar{t}j \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}j @ \text{LHC}_{13\text{TeV}}$$

Theory, NLO QCD CT14 PDF	$m_t^{\text{out}} \pm \delta m_t^{\text{out}}$ [GeV]	Averaged $\chi^2/\text{d.o.f.}$	Probability <i>p-value</i>	$m_t^{\text{in}} - m_t^{\text{out}}$ [GeV]
<i>31 bins</i>				
<i>Full</i> , $\mu_0 = H_T/2$	173.09 ± 0.42	1.04	0.41 (0.8σ)	+0.11
<i>Full</i> , $\mu_0 = E_T/2$	172.45 ± 0.39	1.12	0.30 (1.0σ)	+0.75
<i>Full</i> , $\mu_0 = m_t$	173.76 ± 0.40	1.87	0.003 (3.0σ)	-0.56
<i>NWA</i> , $\mu_0 = m_t$	175.65 ± 0.31	2.99	$7 \cdot 10^{-8}$ (5.4σ)	-2.45
<i>NWA</i> _{Prod.} , $\mu_0 = m_t$	169.59 ± 0.30	3.10	$2 \cdot 10^{-8}$ (5.6σ)	+3.61
<i>5 bins</i>				
<i>Full</i> , $\mu_0 = H_T/2$	173.08 ± 0.40	0.94	0.44 (0.8σ)	+0.12
<i>Full</i> , $\mu_0 = E_T/2$	172.48 ± 0.38	1.58	0.18 (1.3σ)	+0.72
<i>Full</i> , $\mu_0 = m_t$	173.75 ± 0.40	6.76	$2 \cdot 10^{-5}$ (4.3σ)	-0.55
<i>NWA</i> , $\mu_0 = m_t$	175.49 ± 0.30	5.31	$2 \cdot 10^{-4}$ (3.7σ)	-2.29
<i>NWA</i> _{Prod.} , $\mu_0 = m_t$	169.39 ± 0.47	3.42	$8 \cdot 10^{-3}$ (2.6σ)	+3.81

tt γ & tt

Off-shell Tops

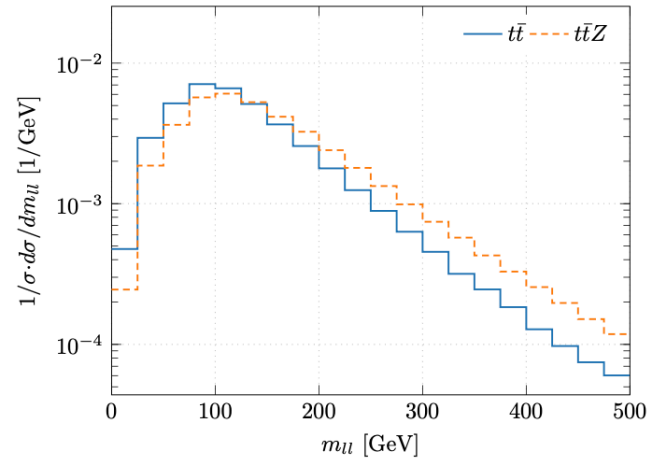
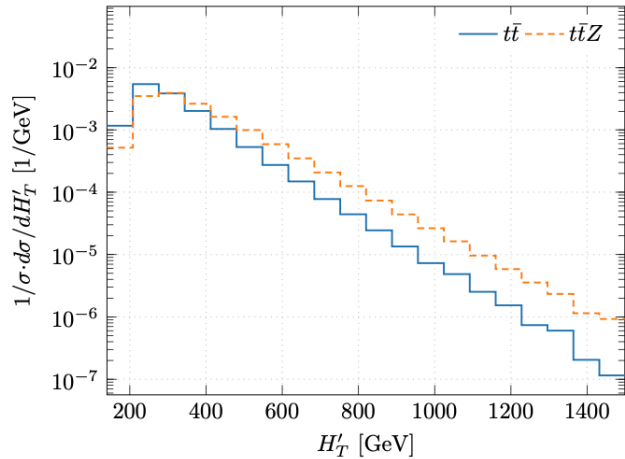
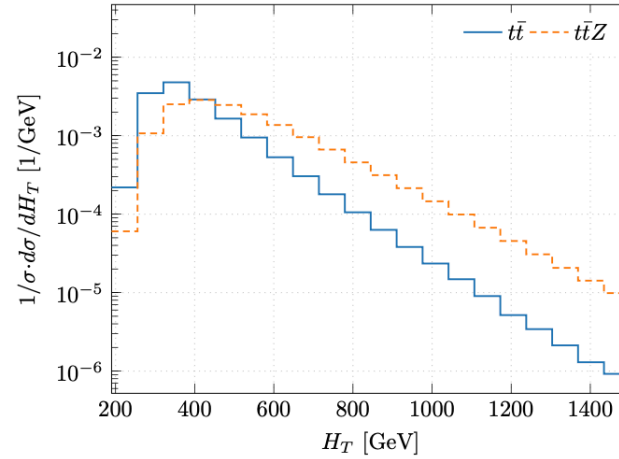
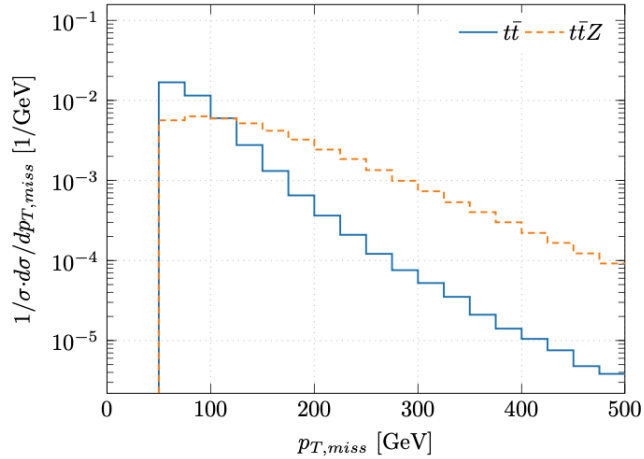
PDF set, $\mu_R = \mu_F = \mu_0$	$\sigma_{e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b}}^{\text{NLO}}$ [fb]	$\sigma_{e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b}\gamma}^{\text{NLO}}$ [fb] $p_{T,\gamma} > 25$ GeV	$\sigma_{e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b}\gamma}^{\text{NLO}}$ [fb] $p_{T,\gamma} > 50$ GeV
CT14, $\mu_0 = m_t/2$	1629.4 ^{+18.4 (1%)} _{-144.7 (9%)}	7.436 ^{+0.074 (1%)} _{-1.034 (14%)}	3.081 ^{+0.050 (2%)} _{-0.514 (17%)}
CT14, $\mu_0 = H_T/4$	1620.5 ^{+21.6 (1%)} _{-118.8 (7%)}	7.496 ^{+0.099 (1%)} _{-0.457 (6%)}	3.125 ^{+0.040 (1%)} _{-0.142 (4%)}
MMHT14, $\mu_0 = m_t/2$	1650.5 ^{+17.0 (1%)} _{-152.7 (9%)}	7.490 ^{+0.080 (1%)} _{-1.081 (14%)}	3.093 ^{+0.053 (2%)} _{-0.535 (17%)}
NNPDF3.0, $\mu_0 = m_t/2$	1695.0 ^{+18.4 (1%)} _{-153.3 (9%)}	7.718 ^{+0.078 (1%)} _{-1.102 (14%)}	3.195 ^{+0.054 (2%)} _{-0.550 (17%)}

Bevilacqua, Hartanto, Kraus, Weber, Worek '19

ttZ

✿ Normalized NLO differential cross sections

Off-shell Tops



ttZ

✿ Normalized NLO differential cross sections

Off-shell Tops

