

# OPTIMIZING THE SIGNAL OF ODDERON

T. Csörgő<sup>1,2</sup>, T. Novák<sup>2</sup>, R. Pasechnik<sup>3</sup>, A. Ster<sup>1</sup> and I. Szanyi<sup>1,4</sup>

<sup>1</sup> Wigner RCP, Budapest, Hungary

<sup>2</sup> MATE KRC, Gyöngyös, Hungary

<sup>3</sup> University of Lund, Lund, Sweden

<sup>4</sup> Eötvös University, Budapest, Hungary

## Statistically Significant Observations of Odderon

### Model independent results:

Significance  $\geq 6.26 \sigma$

### Model dependent results:

Significance  $\geq 7.08 \sigma$

### D0-TOTEM results:

Significance  $\geq t 5.2 \sigma$

**New: Model independently  
Optimal Significance  $\geq 6.36 \sigma$**

Domain of validity

Sliding window, closing doors

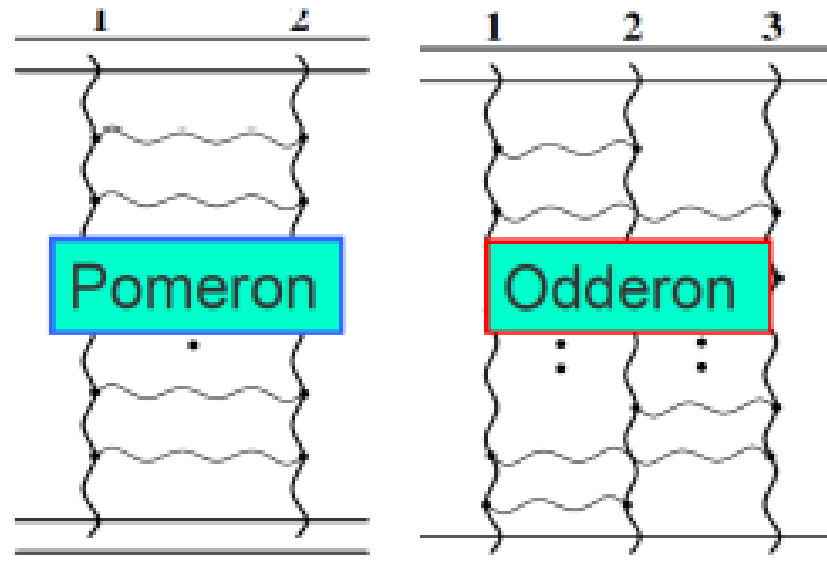
Summary



# Odderon: 48 years old scientific puzzle

Odderon: L. Lukaszuk, B. Nicolescu,  
Lett. Nuovo Cim. 8, 405 (1973)

At CERN LHC's TeV energy scale:  
Odderon is an odd component of  
elastic scattering:  
Changes sign for crossing



# Odderon: origin of its name

Odderon name coined in 1975:  
D. Joynson, E. Leader, B. Nicolescu, C. Lopez  
Nuovo Cim. 30A, 345 (1975)

IL NUOVO CIMENTO

VOL. 30 A, N. 3

1 Dicembre 1975

## **Non-Regge and Hyper-Regge Effects in Pion-Nucleon Charge Exchange Scattering at High Energies.**

D. JOYNSON (\*), E. LEADER (\*\*) and B. NICOLESCU

*Division de Physique Théorique (\*\*), Institut de Physique Nucléaire (\*,\*) - Paris  
Laboratoire de Physique Théorique des Particules Élémentaires - Paris (\*,\*)*

C. LOPEZ (\*,\*)

*Laboratoire de Physique Théorique et Hautes Energies - Paris (\*,\*)*

(ricevuto il 24 Giugno 1975)

# Odderon: well established in QCD

Odderon proposed in Regge phenomenology:

L. Lukaszuk, B. Nicolescu, Lett. Nuovo Cim. 8, 405 (1973)

Three Gluon Integral Equation and Odd c Singlet Regge  
Singularities in QCD

J. Kwiecinski, M. Praszalowicz, Phys.Lett.B 94 (1980) 413-416

A new Odderon intercept from QCD:

R. A. Janik, J. Wosiek, Phys. Rev. Lett. 82 (1999) 1092

Odderon in QCD:

J. Bartels, L.N. Lipatov, G. P. Vacca: Phys. Lett. B (2000) 178

Odderon in QCD with running coupling:

J. Bartels, C. Contreras, G. P. Vacca, *JHEP* 04 (2020) 183

For an excellent theory intro/review, see Yu. Kovchegov's  
CTEQ Webinar, April 28, 2021

<http://youtu.be/yHBO3zcB3V4>

# Odderon Search

## and symmetry violation in elastic collisions

$$T_{\text{el}}^O(s, t) = \frac{1}{2} \left( T_{\text{el}}^{p\bar{p}}(s, t) - T_{\text{el}}^{pp}(s, t) \right)$$

$$\sqrt{s} \geq 1 \text{ TeV},$$

**Two simple consequences:**

$$T_{\text{el}}^O(s, t) = 0 \implies \frac{d\sigma^{pp}}{dt} = \frac{d\sigma^{p\bar{p}}}{dt} \quad \text{for } \sqrt{s} \geq 1 \text{ TeV}$$

$$\frac{d\sigma^{pp}}{dt} \neq \frac{d\sigma^{p\bar{p}}}{dt} \quad \text{for } \sqrt{s} \geq 1 \text{ TeV} \implies T_{\text{el}}^O(s, t) \neq 0$$

# Observations of Odderon with $> 5 \sigma$




## Evidence of Odderon-exchange from scaling properties of elastic scattering at TeV energies #5


T. Csörgő (Wigner RCP, Budapest and CERN), [T. Novák](#) (Unlisted, HU), R. Pasechnik (Lund U., Dept. Theor. Phys.), [A. Ster](#) (Wigner RCP, Budapest), [I. Szanyi](#) (Wigner RCP, Budapest) (Dec 26, 2019)

Published in: *Eur.Phys.J.C* 81 (2021) 2, 180 • e-Print: 1912.11968 [hep-ph]

*Eur. Phys. J. C* (2021) **81**: 180

<https://doi.org/10.1140/epjc/s10052-021-08867-6>

 pdf  DOI  cite

 15 citations

## Observation of Odderon Effects at LHC energies -- A Real Extended Bialas-Bzdak Model Study #2

T. Csorgo (Wigner RCP, Budapest and Eötvös KRC, Gyongyos), I. Szanyi (Eötvös U. and Wigner RCP, Budapest) (May 28, 2020)

e-Print: 2005.14319 [hep-ph]

*Eur. Phys. J. C* (2021) **81**:611

<https://doi.org/10.1140/epjc/s10052-021-09381-5>

 pdf  cite

## Comparison of $pp$ and $p\bar{p}$ differential elastic cross sections and observation of the exchange of a colorless $C$ -odd gluonic compound #1

D0 and TOTEM Collaborations • V.M. Abazov (Dubna, JINR) et al. (Dec 7, 2020)

e-Print: 2012.03981 [hep-ex]

*Phys. Rev. Lett.* (2021) **in press**

Accepted for a publication




 pdf  links  cite

# Three Odderon Proceedings with $> 5 \sigma$

## Scaling of high-energy elastic scattering and the observation of Odderon #1

T. Csörgő (Wigner RCP, Budapest and Eszterhazy Karoly U., Eger), T. Nagy (Eötvös KRC, Gyongyos), R. Pasechnik (Lund U., Dept. Theor. Phys.), A. Ster (Wigner RCP, Budapest), I. Szanyi (Wigner RCP, Budapest and Eötvös U.) (Apr 15, 2020)

Published in: Gribov-90 Memorial Volume, pp. 69-80 (2021) (World Scientific, Singapore, ed. Yu. Dokshitzer, P. L'evai, V.A. Luk'acs and J. Nyiri) • e-Print: 2004.07318 [hep-ph]

 pdf  DOI  cite


Gribov'90 Memorial Volume, pp. 69-80 (2021)

[https://doi.org/10.1142/9789811238406\\_0012](https://doi.org/10.1142/9789811238406_0012)

## Proton Holography -- Discovering Odderon from Scaling Properties of Elastic Scattering #2

T. Csorgo (Wigner RCP, Budapest and Eszterhazy Karoly U., Eger), T. Nagy (Eötvös KRC, Gyongyos), R. Pasechnik (Lund U., Dept. Theor. Phys. Inst.), A. Ster (Wigner RCP, Budapest), I. Szanyi (Wigner RCP, Budapest and Eötvös U.) (Apr 15, 2020)

Published in: EPJ Web Conf. 235 (2020) 06002 • Contribution to: ISMD 2019 • e-Print: 2004.07095 [hep-ph]

 pdf  DOI  cite

EPJ Web Conf. 235 (2020) 06002, proc. ISMD 2019




<https://doi.org/10.1051/epjconf/202023506002>

 1 citation

## Comparison of differential elastic cross sections in $pp$ and $p\bar{p}$ collisions as evidence of the existence of the colourless $C$ -odd three-gluon state #1


D0 and Totem Collaborations • Christophe Royon (Kansas U.) for the

Published in: PoS ICHEP2020 (2021) 496 • Contribution to: ICHEP2020, 496 • e-Print: 2012.03150 [hep-ex]

 pdf  DOI  cite

PoS ICHEP 2020 (2021)

<https://doi.org/10.22323/1.390.0496>

 2 citations



# Three Oldest Hungarian Universities

UP Story - 650 years

Home » University » UP Story 650 years



## University of Pécs: 1367

The history of higher education in Pécs dates back to 1367, when Louis the Great initiated the establishment of a university in the episcopal city of Pécs. As a result of an integration process of several stages, the University of Pécs was founded, which has become one of the most famous, prestigious institutions having a leading role in regional education. It has ten faculties which cover the full spectrum of high-quality higher education.

1367

The University of Debrecen, the oldest institution of higher education in the country operated continuously in the same city, is one of the research universities of national excellence in Hungary offering the widest spectrum of educational programs in 14 faculties and 24 doctoral schools.

## University of Debrecen: 1538



Its history of higher education in the city reach all the way back to the 16<sup>th</sup> century and the foundation of the Reformed College of Debrecen in 1538. The College played a central role in Hungarian education and culture for centuries. This is the date featured on the symbol of the university as well, the *gerundium*, a tool originally used by the students of the Reformed College to put out fires, showing respect for ancestors and traditions.

(S,C) structure evident,

S: statement, valid if

C: condition is satisfied

See talk of [R. Dardashti](#) at ISMD21

Eötvös Loránd University: 1635

*The* predecessor of Eötvös Loránd University (ELTE) was founded in Nagyszombat in 1635 (sixteen thirty-five) by Archbishop of Esztergom, Péter Pázmány, and it is the oldest Hungarian university where the teaching has continued uninterrupted since its inception. More than sixty years



# Model independent results since ISMD'19

## Evidence of Odderon-exchange from scaling properties of elastic scattering at TeV energies

#5

T. Csörgő (Wigner RCP, Budapest and CERN), T. Novák (Unlisted, HU), R. Pasechnik (Lund U., Dept. Theor. Phys.), A. Ster (Wigner RCP, Budapest), J. Szanyi (Wigner RCP, Budapest) (Dec 26, 2019)

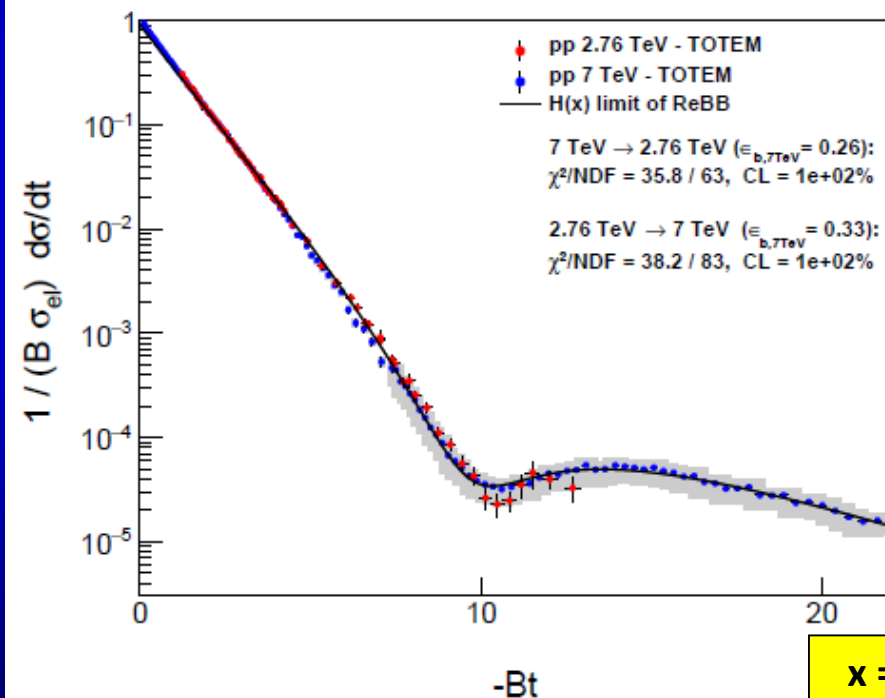
Published in: *Eur.Phys.J.C* 81 (2021) 2, 180 • e-Print: 1912.11968 [hep

Eur. Phys. J. C (2021) **81**: 180

<https://doi.org/10.1140/epjc/s10052-021-08867-6>

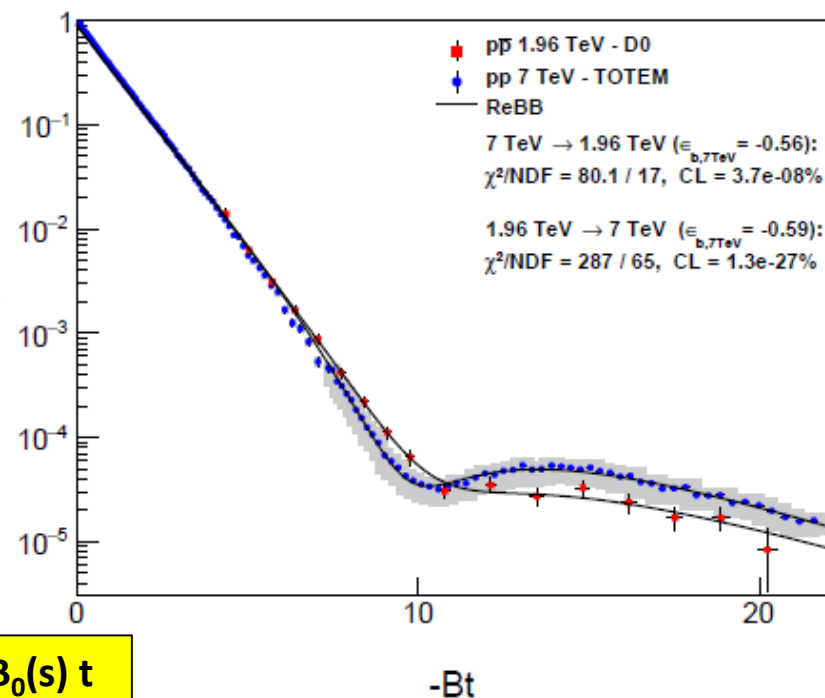
pdf DOI cite

15 citations



$$H(x) = 1/(B \sigma_{el}) d\sigma/dt \text{ vs } x = -Bt$$

$$x = -Bt = -B_0(s)t$$



**S: Model independent Odderon significance  $\geq 6.26 \sigma$**

**C1: All D0 and TOTEM published data at 1.96, 2.76 and 7.0 TeV**

**C2: domain of validity is still determined model dependently.**

# Model independent results since ISMD'19

## Scaling of high-energy elastic scattering and the observation of Odderon

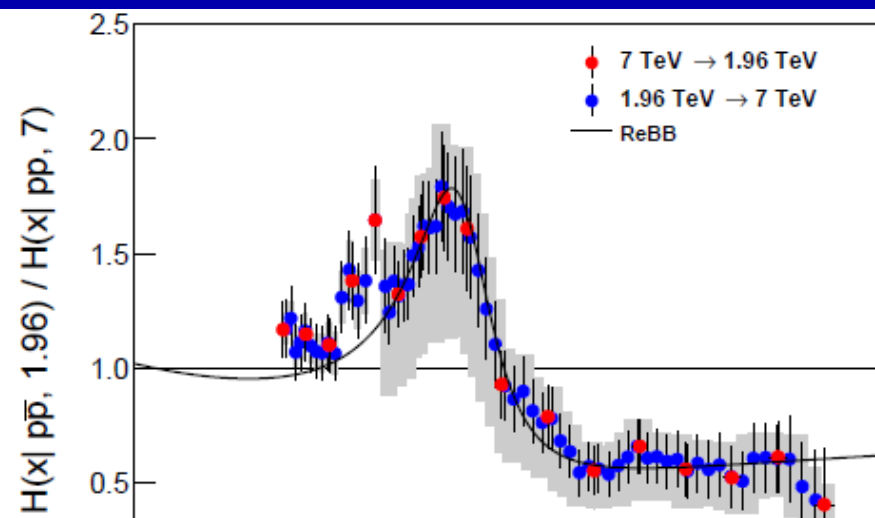
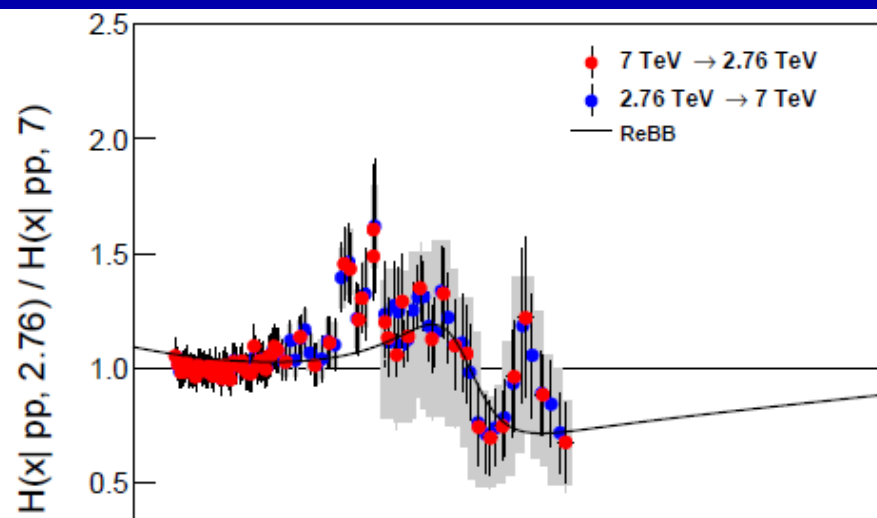
#1

T. Csörgő (Wigner RCP, Budapest and Eszterhazy Karoly U., Eger), T. Novák (Eötvös KRC, Gyongyos), R. Pasechnik (Lund U., Dept. Theor. Phys.), A. Ster (Wigner RCP, Budapest), L. Szany (Wigner RCP, Budapest and Eötvös U.) (Apr 15, 2020)

Published in: Gribov-90 Memorial Volume, pp. 69-80 (2021) (World Scientific) and J. Nyiri • e-Print: 2004.07318 [hep-ph]

Gribov'90 Memorial Volume, pp. 69-80 (2021)

[https://doi.org/10.1142/9789811238406\\_0012](https://doi.org/10.1142/9789811238406_0012)



**S: Model independent Odderon significance  $\geq 6.26 \sigma$**

**C1: All D0 and TOTEM published data at 1.96, 2.76 and 7.0 TeV**

**C2: domain of validity is still determined model dependently.**

$H(x, s_1)/H(x, s_2)$  nearly 1 for pp with small violations. Peak for pbarp over pp.

Model independent Odderon significance  $6.26 \sigma$

Small violations under theoretical control (next slide).

New result presented in this talk: domain of validity model independently

# Model dependent evidence for Odderon

Observation of Odderon Effects at LHC energies -- A Real Extended Bialas-Bzdak Model Study

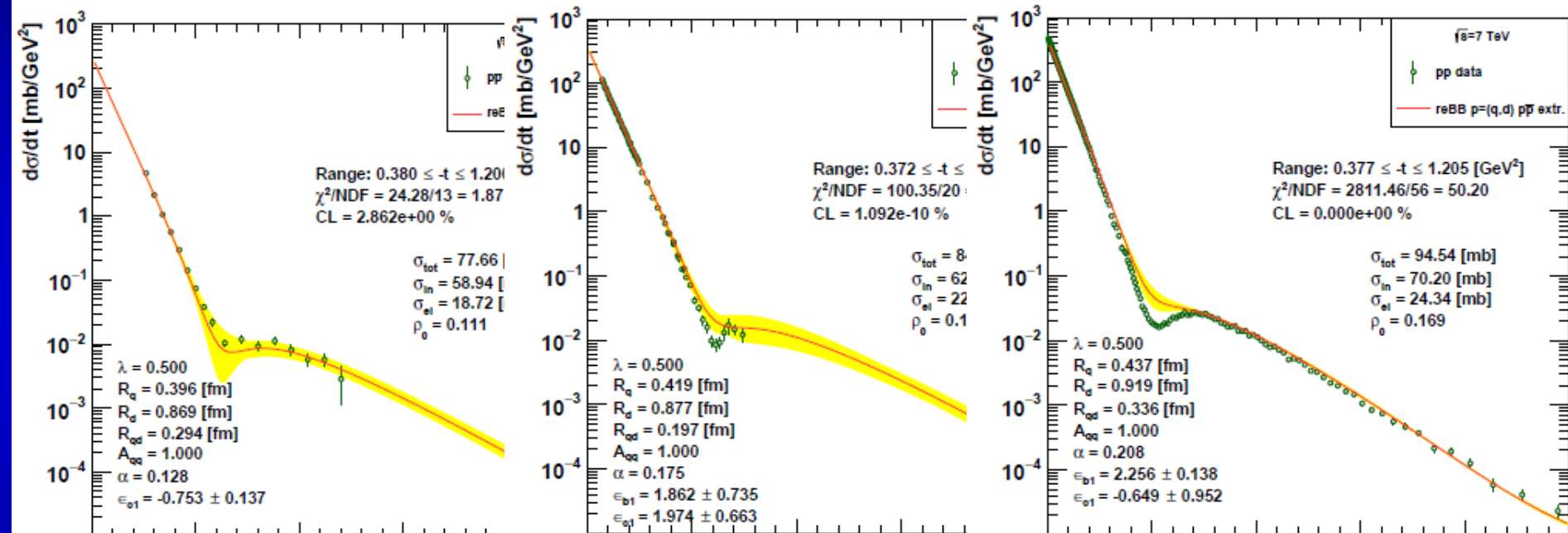
#2

T. Csorgo (Wigner RCP, Budapest and Eötvös KRC, Gyöngyös), I. Szanyi (Eötvös KRC, Budapest)

e-Print: 2005.14319 [hep-ph]

Eur. Phys. J. C (2021) 81:611

<https://doi.org/10.1140/epjc/s10052-021-09381-5>



**S: Model independent Odderon significance  $\geq 7.08 \sigma$**

**C1: All D0 and TOTEM published data at 1.96, 2.76 and 7.0 TeV,**

**C2: domain of validity extended to both pp and pbarp**

But limited to  $0.372 \leq -t \leq 1.2$  GeV<sup>2</sup> and  $0.546 \leq \sqrt{s} \leq 7$  (8) TeV

**Model dependent, Real Extended Bialas-Bzdak theory results, Odderon significance  $\geq 7.08 \sigma$ , a Glauber model for  $p = (q, d)$**

# Evidence for Odderon, new D0-TOTEM

Comparison of  $pp$  and  $p\bar{p}$  differential elastic cross sections and observation of the exchange of a colorless  $C$ -odd gluonic compound

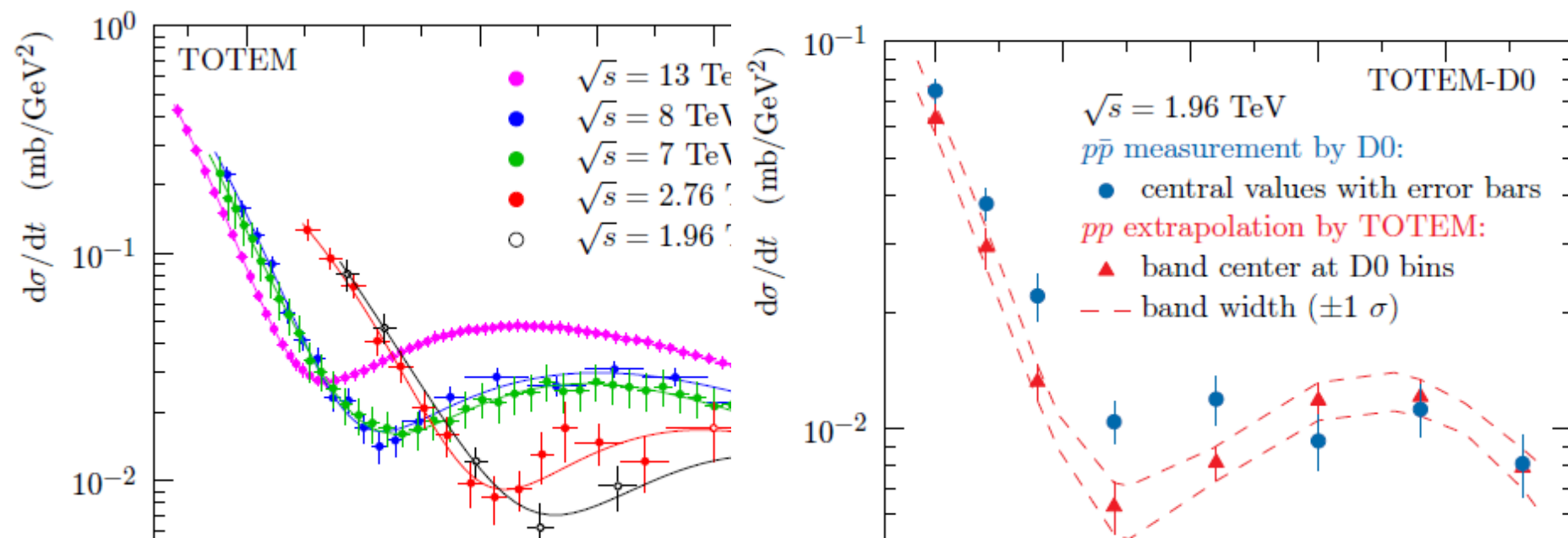
#1

D0 and TOTEM Collaborations • V.M. Abazov (Dubna, JINR) et al. (Dec 7, 2020)

e-Print: 2012.03981 [hep-ex]

[pdf](#) [links](#) [cite](#)

Phys. Rev. Lett. (2021) in press  
Accepted for a publication



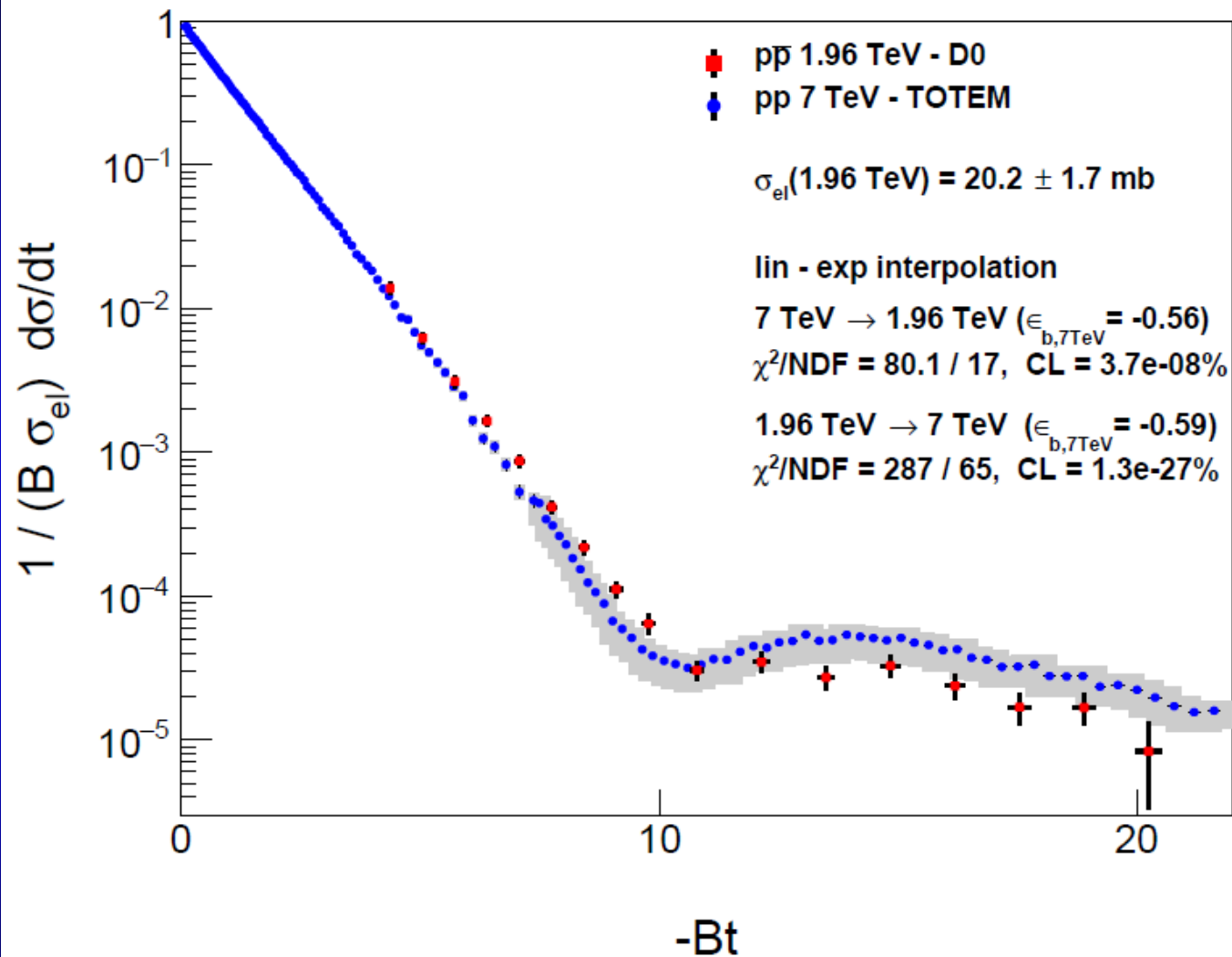
**S: Odderon significance  $\geq 5.2 \sigma$ ,**

C1: if combined with 13 TeV  $\sigma_{\text{tot}}$  and  $\rho_0$

C2: if **new pp data** at 13, 8 TeV and 1 new point at 2.76 TeV is added,

C3: if **only 8 out of the 17 D0 points** is used

# Model independent result



$H(x|pp)$   
 s-independent:  
 2.76 – 7(8) TeV

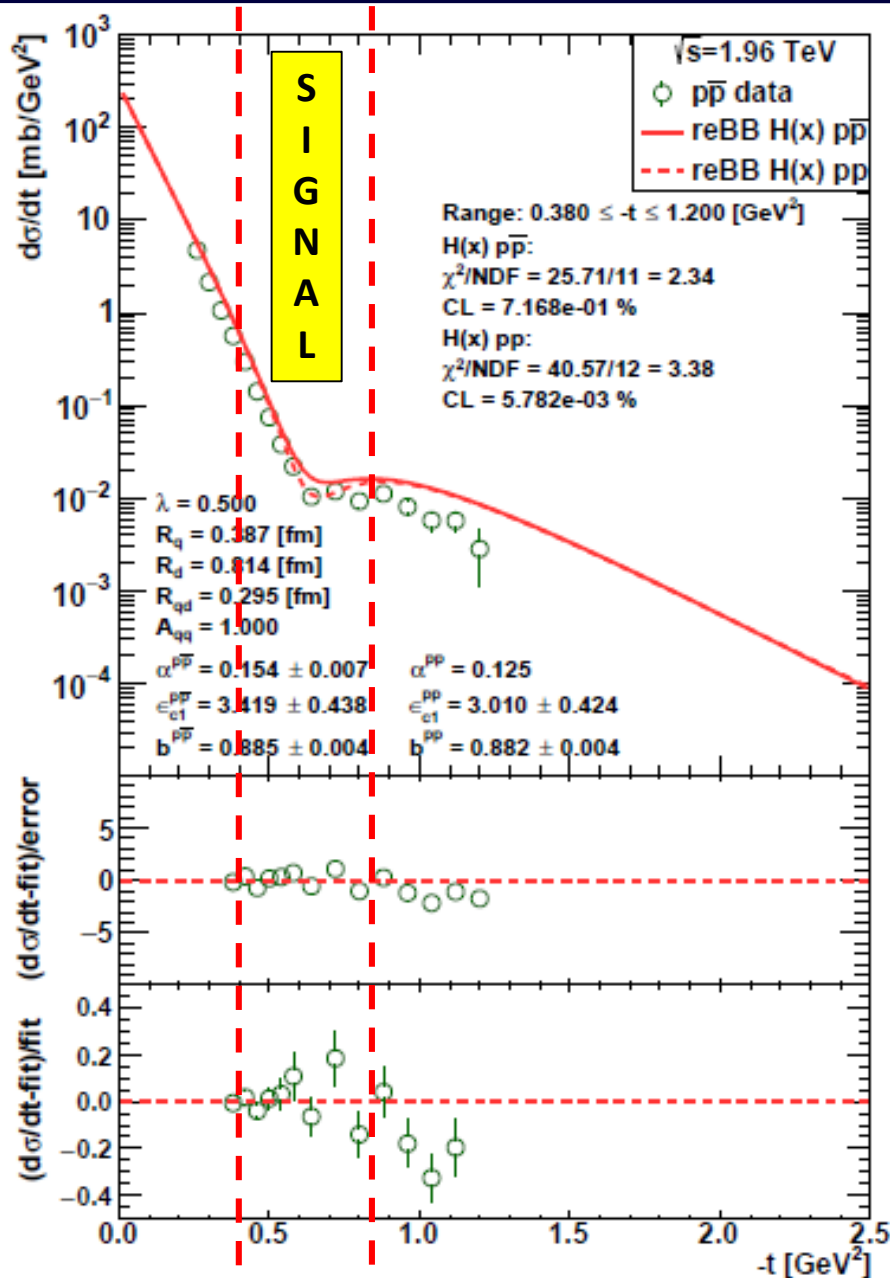
$H(x|pp, 7 \text{ TeV})$   
 $\neq$   
 $H(x|pantip, 1.96 \text{ TeV})$

Odderon,  
 IF scaling holds  
 in pp down to  
 1.96 TeV

**6.26  $\sigma$**   
**Odderon effect**

Energy range: tested both model independently and with modelling.  
 Modelling is useful, but model independent tests more important!

# Is $H(x,s) = H(x)$ at 1.96 TeV?



**MODEL DEPENDENTLY:** Yes  
1.96 TeV

Highest energy where p+antip data are available

$H(x)$  scaling limit:  
in the Bialas-Bzdak model

Fits pbarp data up to largest  $-t$   
(red line, dashed line:  $pp$ )

Pull plots:  
(data-fit)/error  
(data-fit)/fit

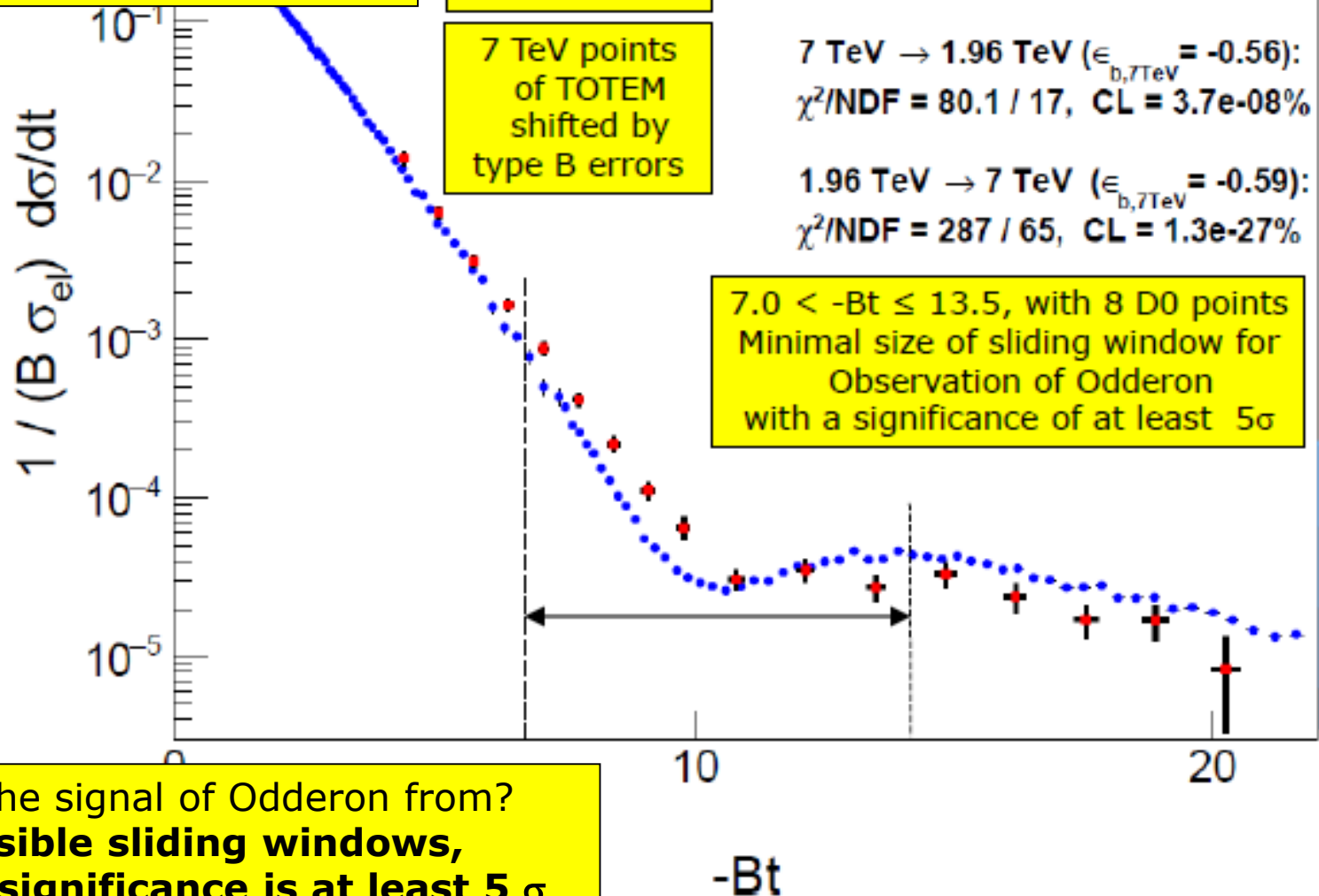
$t_{\text{max}}(1.96 \text{ TeV}, pp) > 1.2 \text{ GeV}^2$

$\rightarrow x_{\text{max}}(1.96 \text{ TeV}, pp) > 20$



# SLIDING WINDOW for $5\sigma$

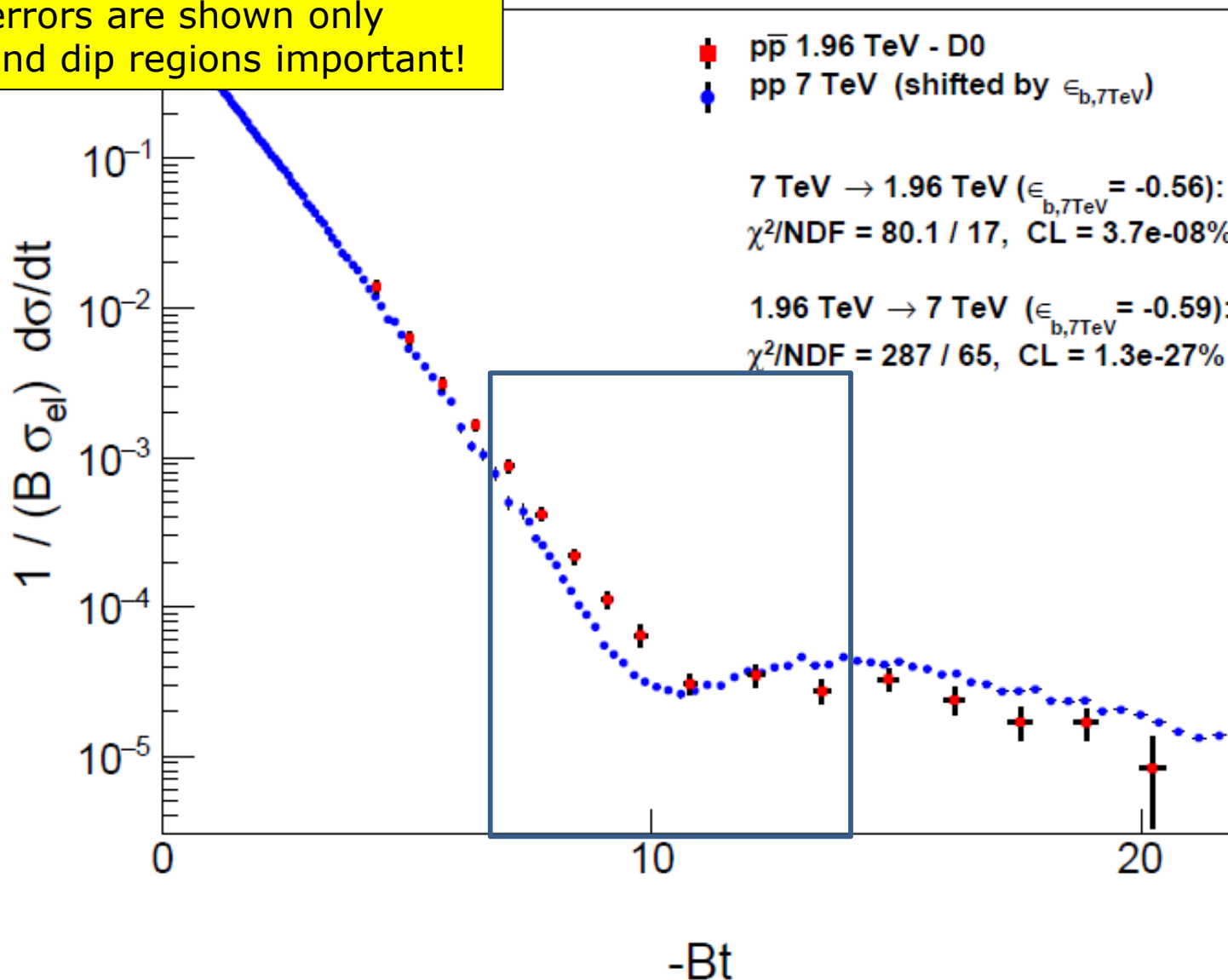
**Model independent results:  
only datapoints,  
without s-dependent  
extrapolations !**



Where is the signal of Odderon from?  
**All possible sliding windows,  
where the significance is at least  $5\sigma$**

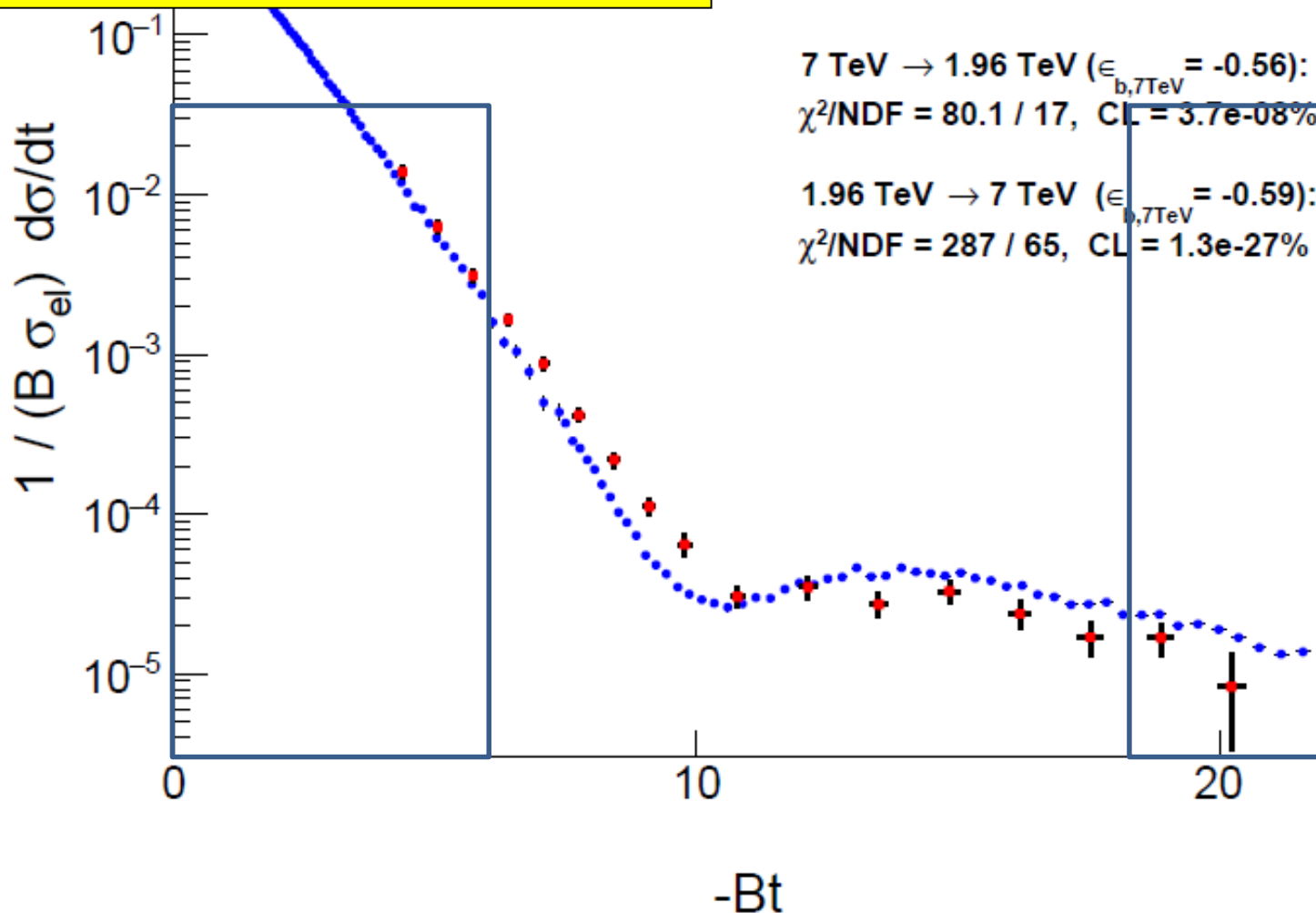
# SLIDING WINDOWS

7 TeV data shifted  
by  $\epsilon_{B7, \text{TeV}}$  to minimize  $\chi^2$   
Type A errors are shown only  
Both swing and dip regions important!



# CLOSING DOORS/GATES

7 TeV data shifted  
by  $\epsilon_{B7, \text{TeV}}$  to minimize  $\chi^2$   
Type A errors are shown only  
Both swing and dip regions important!



# RESULTS FOR CLOSING GATES

**Two sliding gates of size n and size m:**  
(n,m): Leaving out the first n and last m D0 point

Sliding door technique with two wings (n,m)

Left door excludes the first n, right door excludes the last m D0 points

n	m	Odderon signal	Background
2	2	6.27 $\sigma$	1.68 $\sigma$
3	2	6.33 $\sigma$	1.70 $\sigma$
4	2	6.21 $\sigma$	2.37 $\sigma$

**New MODEL INDEPENDENT RESULT:**  
**Optimized Odderon signal is 6.33  $\sigma$**

**New MODEL INDEPENDENT RESULT 2:**  
**Best window: leaving out first 3 and last 2 D0 point**

**New MODEL INDEPENDENT RESULT 3:**  
**Best background: pp and pbarp agree within 1.7  $\sigma$**

# SUMMARY: AT LEAST 6.36 $\sigma$ ODDERON

**An at least 6.36  $\sigma$  Odderon effect**

**Odderon first discovered in three papers  
2 published  
1 accepted for publication, but  
under three different conditions**

(S,C) structure evident,  
S: statement, valid if  
C: condition is satisfied

See talk of [R. Dardashti](#) at ISMD21

# **OBSERVATION OF ODDERON**

**2020 → 2020**

**THANK YOU FOR YOUR  
ATTENTION**



# ODE TO ODDERON → OBERON

## Ode to Odderon

Let's be truly happy,  
for what we've come upon:  
We have just discovered  
the elusive odderon!

For forty-eight years,  
forging a ring of colors white:  
Odd number of gluons  
has been hiding in plain sight!

*"Discovery consists of seeing what everybody has seen,  
and thinking what nobody has thought."*

*Albert Szent-Györgyi*

## OBERON POETRY MAGAZINE

So happy together,  
with love for science and research:  
Happiness and pleasure  
must not slow down the search!

Let's live in harmony,  
and in equanimity:  
Let's make light of the fight,  
gloom is our true enemy!

© by Tamás Csörgő

Gyöngyös, Hungary, March 11 – April 11, 2021

# BACKUP SLIDES

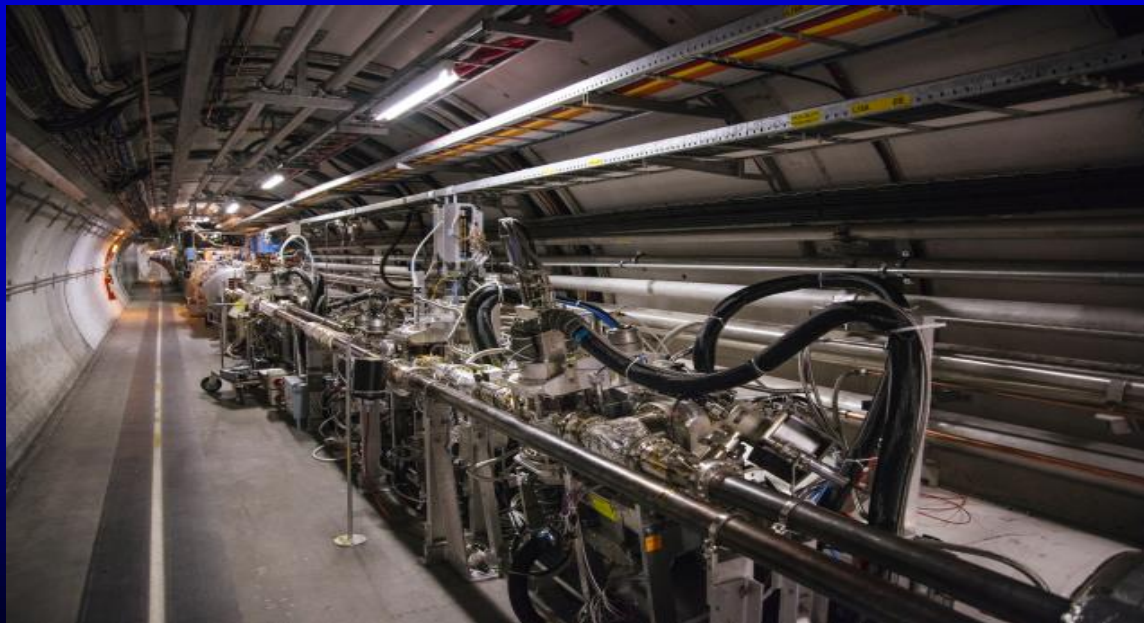


$$O = (g_1, g_2, g_3)$$

$$g_1 = B\bar{R} + R\bar{B}$$

$$g_2 = R\bar{G} + G\bar{R}$$

$$g_3 = G\bar{B} + B\bar{G}$$



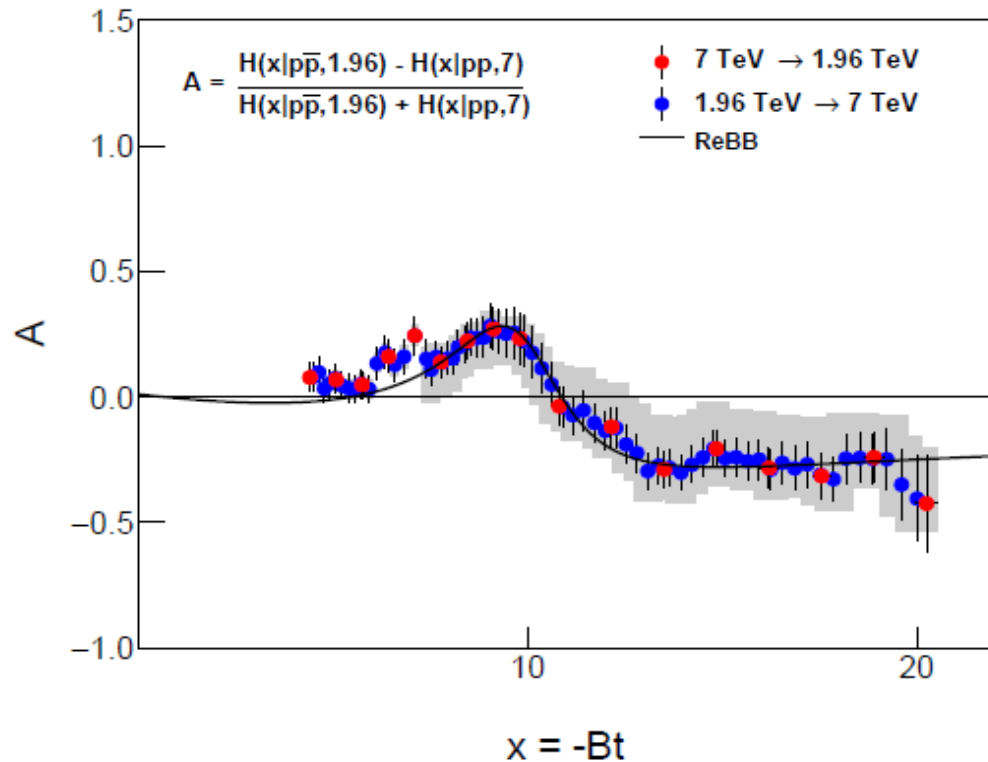
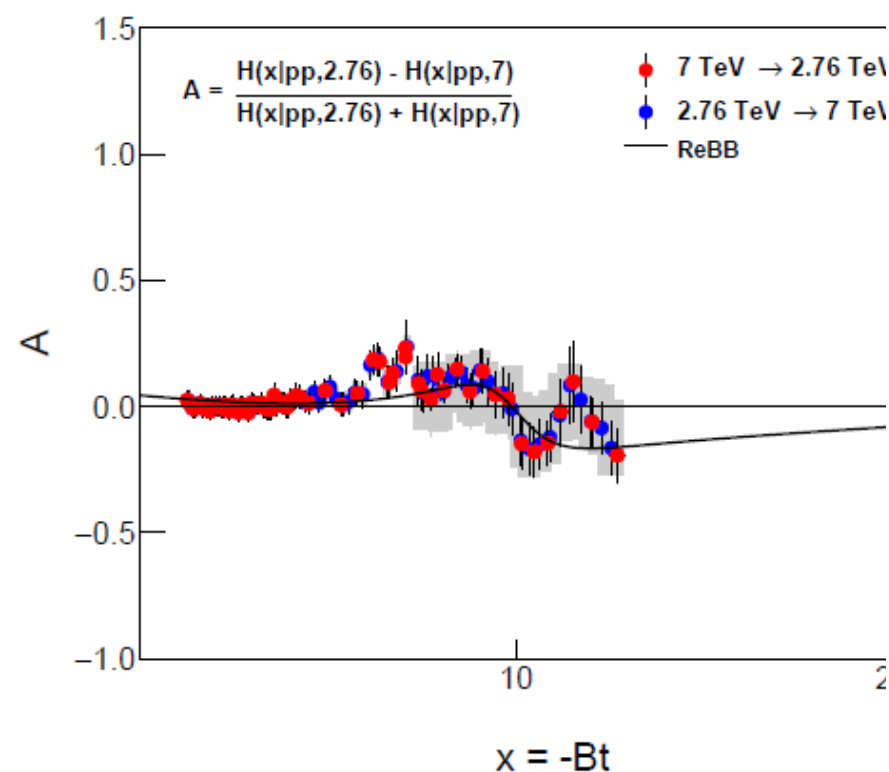
# Asymmetry parameter for C-violation

$$A(x|p\bar{p},s_1|pp,s_2) = \frac{H(x|p\bar{p},s_1) - H(x|pp,s_2)}{H(x|p\bar{p},s_1) + H(x|pp,s_2)},$$
$$A(x|pp,s_1|pp,s_2) = \frac{H(x|pp,s_1) - H(x|pp,s_2)}{H(x|pp,s_1) + H(x|pp,s_2)}.$$

$A(x|p\bar{p},s_1|pp,s_2)$   
does NOT vanish  
for a C-symmetry violation AND

$A(x|pp,s_1|pp,s_2)$   
vanishes if  
H(x) scaling valid

# Main result of A



$A(x|pp,s_1|pp,s_2) \sim 0$   
vanishes if  
 $H(x)$  scaling valid

$A(x|p\bar{p},s_1|pp,s_2) \neq 0$   
does NOT vanish  
if Odderon term is present

Scaling violations: under theoretical control:  
Model calculations by solid line, see e-Print: [2005.14319](https://arxiv.org/abs/2005.14319) [hep-ph]

# Essentially, Odderon

$$p+p \rightarrow p+p$$

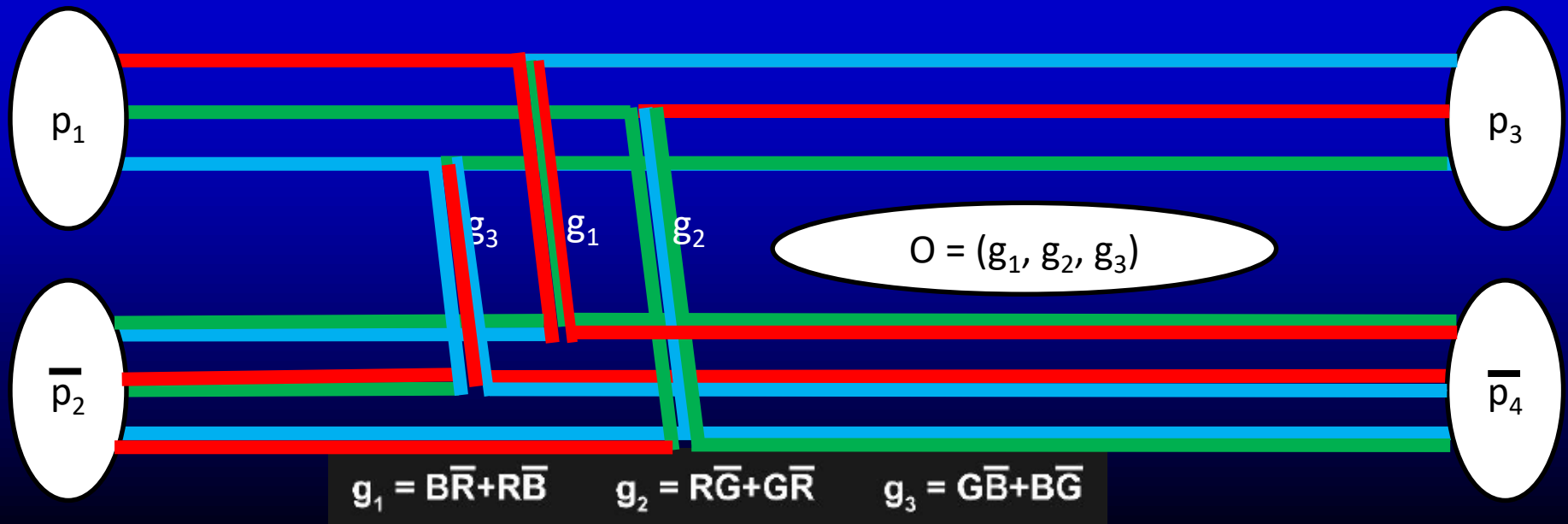
$$(RGB) + (RGB) \rightarrow (GBR) + (GBR)$$

-

$$p+\bar{p} \rightarrow p+\bar{p}$$

$$(RGB) + (\bar{R}\bar{B}\bar{G}) \rightarrow (BRG) + (\bar{B}\bar{G}\bar{R})$$

25



# Formalism: elastic scattering

$$\sigma_{el}(s) = \int_0^\infty d|t| \frac{d\sigma(s)}{dt}$$

$$\frac{d\sigma(s)}{dt} = \frac{1}{4\pi} |T_{el}(s, \Delta)|^2, \quad \Delta = \sqrt{|t|}.$$

$$\sigma_{tot}(s) \equiv 2 \operatorname{Im} T_{el}(\Delta = 0, s)$$

$$B(s, t) = \frac{d}{dt} \ln \frac{d\sigma(s)}{dt}$$

$$B(s) \equiv B_0(s) = \lim_{t \rightarrow 0} B(s, t),$$

$$\rho(s, t) \equiv \frac{\operatorname{Re} T_{el}(s, \Delta)}{\operatorname{Im} T_{el}(s, \Delta)}$$

$$\rho(s) \equiv \rho_0(s) = \lim_{t \rightarrow 0} \rho(s, t)$$

Basic problem:  $d\sigma/dt$  measures an amplitude, *modulus squared*.  
How to achieve amplitude level reconstruction? Phase info lost...



# Formalism in b space

$$\frac{d\sigma(s)}{dt} = \frac{1}{4\pi} |T_{el}(s, \Delta)|^2, \quad \Delta = \sqrt{|t|}.$$

$$\begin{aligned} t_{el}(s, b) &= \int \frac{d^2\Delta}{(2\pi)^2} e^{-i\Delta \mathbf{b}} T_{el}(s, \Delta) = \\ &= \frac{1}{2\pi} \int J_0(\Delta b) T_{el}(s, \Delta) \Delta d\Delta, \\ \Delta &\equiv |\boldsymbol{\Delta}|, \quad b \equiv |\mathbf{b}|. \end{aligned}$$

$$t_{el}(s, b) = i \left[ 1 - e^{-\Omega(s, b)} \right]$$

$$P(s, b) = 1 - \left| e^{-\Omega(s, b)} \right|^2$$

Impact parameter or b space:

*elastic scattering interferes with propagation w/o collisions*: Genuine quantum physics.

Complex opacity function  $\Omega(s, b)$  (eikonal, from unitarity)

$0 \leq P(s, b) \leq 1$  : *inelastic* scattering has a probabilistic interpretation

# Odderon search: a possible strategy

Known trivial s-dependences in  
 $\sigma_{\text{tot}}(s), \sigma_{\text{el}}(s), B(s), \rho(s)$

Try to scale this out  
Data collapsing (scaling)

Look for scaling violations

In the TeV energy range:  
Odderon is equivalent with  
a crossing-odd component  
Look for violations of C-symmetry

# Looking for Crossing-Odd(eron) effects

$$\begin{aligned}T_{\text{el}}^{pp}(s,t) &= T_{\text{el}}^{+}(s,t) - T_{\text{el}}^{-}(s,t), \\T_{\text{el}}^{p\bar{p}}(s,t) &= T_{\text{el}}^{+}(s,t) + T_{\text{el}}^{-}(s,t), \\T_{\text{el}}^{+}(s,t) &= T_{\text{el}}^P(s,t) + T_{\text{el}}^f(s,t), \\T_{\text{el}}^{-}(s,t) &= T_{\text{el}}^O(s,t) + T_{\text{el}}^{\omega}(s,t).\end{aligned}$$

$$\begin{aligned}T_{\text{el}}^P(s,t) &= \frac{1}{2} \left( T_{\text{el}}^{pp}(s,t) + T_{\text{el}}^{p\bar{p}}(s,t) \right) \\T_{\text{el}}^O(s,t) &= \frac{1}{2} \left( T_{\text{el}}^{p\bar{p}}(s,t) - T_{\text{el}}^{pp}(s,t) \right)\end{aligned}$$

for  $\sqrt{s} \geq 1 \text{ TeV}$ ,

## Three simple consequences:

$$T_{\text{el}}^O(s,t) = 0 \implies \frac{d\sigma^{pp}}{dt} = \frac{d\sigma^{p\bar{p}}}{dt} \quad \text{for } \sqrt{s} \geq 1 \text{ TeV}$$

$$\frac{d\sigma^{pp}}{dt} = \frac{d\sigma^{p\bar{p}}}{dt} \quad \text{for } \sqrt{s} \geq 1 \text{ TeV} \not\Rightarrow T_{\text{el}}^O(s,t) = 0.$$

$$\frac{d\sigma^{pp}}{dt} \neq \frac{d\sigma^{p\bar{p}}}{dt} \quad \text{for } \sqrt{s} \geq 1 \text{ TeV} \implies T_{\text{el}}^O(s,t) \neq 0$$

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# Scaling in the diffractive cone region

$$\frac{d\sigma}{dt} = A(s) \exp [B(s)t]$$

$$A(s) = B(s) \sigma_{\text{el}}(s) = \frac{1 + \rho_0^2(s)}{16 \pi} \sigma_{\text{tot}}^2(s),$$

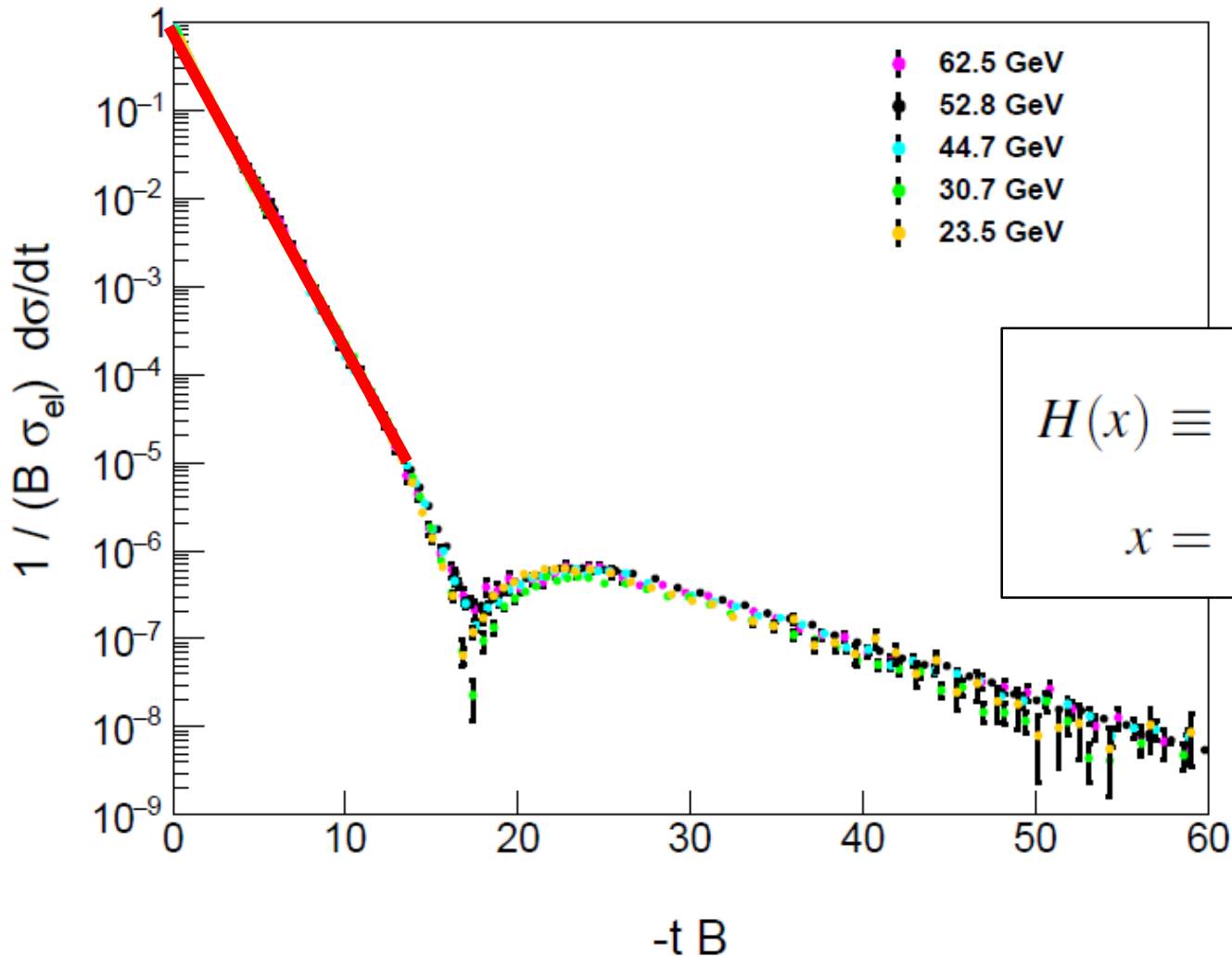
$$\frac{1}{B(s) \sigma_{\text{el}}(s)} \frac{d\sigma}{dt} = \exp [tB(s)]$$

$$H(x) \equiv \frac{1}{B(s) \sigma_{\text{el}}(s)} \frac{d\sigma}{dt},$$
$$x = -tB(s).$$

Advantages:

- 1)  $H(x) = \exp(-x)$  in the cone
- 2) Start from a place that you know
- 3) Measurable both for pp and pbarp

# Test of the $H(x)$ scaling at ISR



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$H(x) = \exp(-x)$  in the cone  
Works better than expected, even in the bump/tail region!

# Derivation of $H(x)$ scaling for all $x$

$$t_{el}(s, b) = (i + \rho_0) r(s) E(\tilde{x}).$$

$$\text{Re exp} [-\Omega(s, b)] = 1 - r(s) E(\tilde{x}),$$

$$\text{Im exp} [-\Omega(s, b)] = \rho_0 r(s) E(\tilde{x}),$$

$$\tilde{x} = b/R(s),$$

$$R(s) = \sqrt{B(s)},$$

$$\frac{d\sigma}{dt} = \frac{1}{4\pi} |T_{el}(\Delta)|^2 = \frac{1 + \rho_0^2}{4\pi} r^2(s) R^2(s) |\tilde{E}(R(s)\Delta)|^2$$

$$A = \left. \frac{d\sigma}{dt} \right|_{t=0} = \frac{1 + \rho_0^2}{4\pi} r^2(s) R^2(s) |\tilde{E}(0)|^2,$$

$$\frac{1}{A} \frac{d\sigma}{dt} = \frac{|\tilde{E}(\sqrt{x})|^2}{|\tilde{E}(x=0)|^2} = H(x),$$

Advantages:

$H(x) \neq \exp(-x)$  arbitrary positive def. in the dip-bump region  
Measurable both for pp and p-antip. Normalized as  $H(0) = 1$ .