

Inclusive jet cross sections at LHeC and prospects for an α_s determination

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Inclusive jet cross sections

Inclusive jet cross sections

- Measured in Breit frame
- LO proportional to $O(\alpha_s)$
- Jets are defined as kT jets, $R=1.0$
→ low hadron. uncertainty

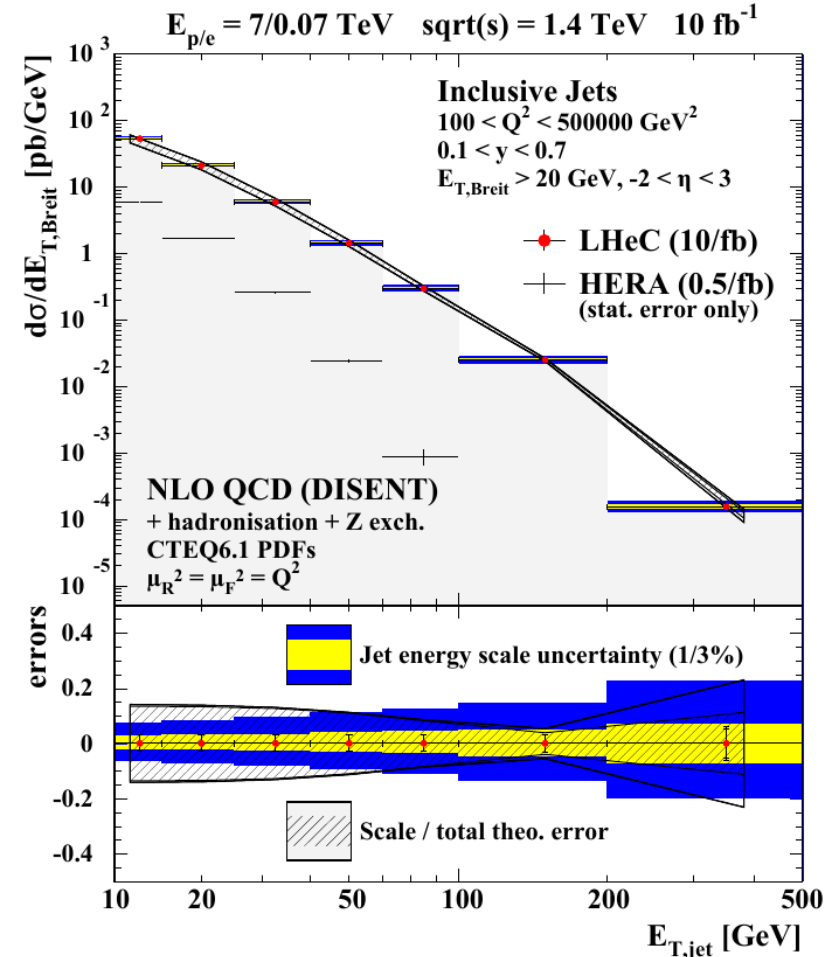
Large cross section

Large kinematic reach

In comparison to HERA

- HERA: $5 < p_T < \sim 60$ GeV
LHeC: $4 < p_T < \sim 600$ GeV
- HERA: $5.5 < Q^2 < \sim 15000$ GeV²
LHeC: $4 < Q^2 < \sim 600000$ GeV²

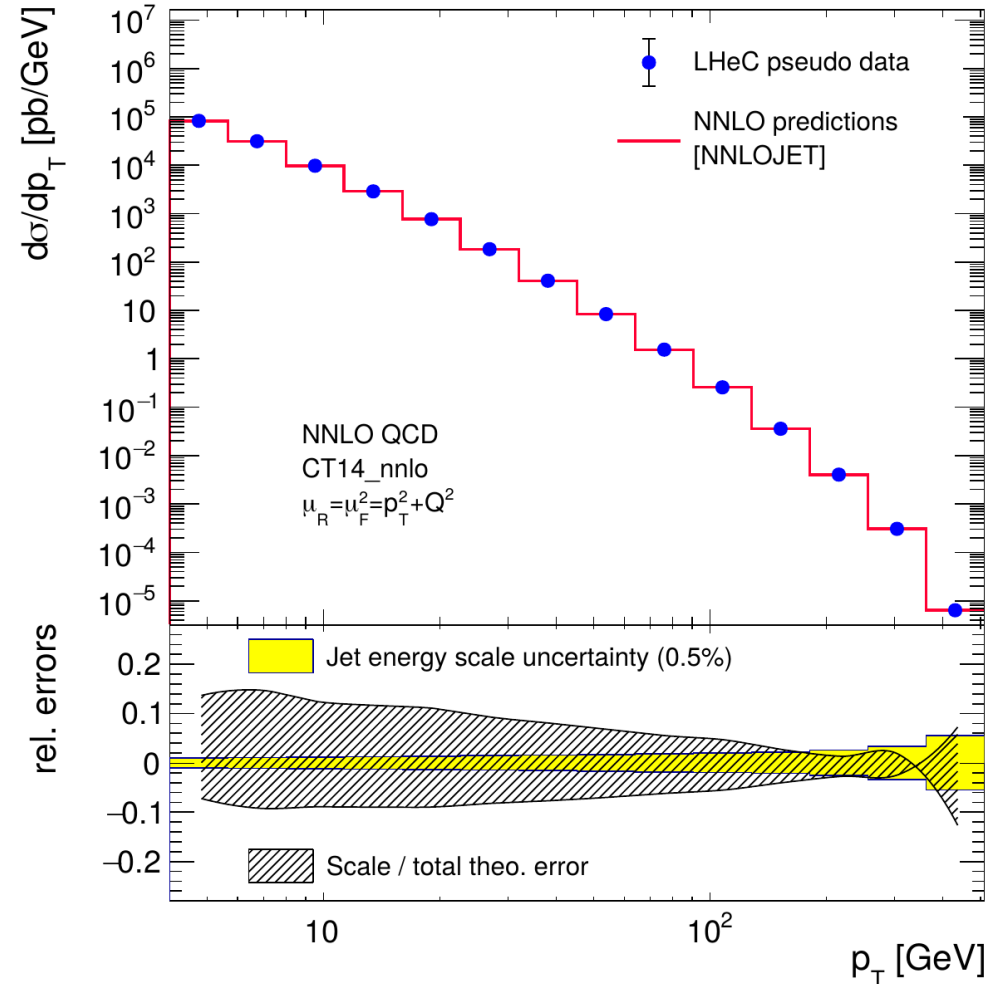
'Old' CDR



New NNLO predictions

NNLOJET + fastNLO

- NNLOJET predictions (Gehrmann et al.)
- NNPDF31 as PDF
- $X_{\min} \sim 0.5 * 10^{-5}$
- Scale: $\mu_R^2 = \mu_F^2 = Q^2 + p_{T,\text{jet}}^2$
- $4 < Q^2 < 524288 \text{ GeV}^2$
- $0.001 < y < 0.95$
- $-5 < \eta_{\text{lab}} < 5$
- $p_{T,\text{jet}} > 4 \text{ GeV}$
- electron method for reconstruction of Q^2 (and x for boost)
- NNLO scale uncertainty: vary scales by 0.5 and 2



Pseudo-data & error summary

Pseudo-data obtained from NNLO predictions

- It was validated, that when using data==prediction, no bias on the error estimate is observed
- [*] stat: at highest- p_T , assume that 2 jets are recorded per event (back-to-back)

Uncertainty	Shift	Size on cross section
Statistics [*]	min 0.15%	>0.15%, < 5%
Electron energy	0.1 %	0.02 – 0.62%
Polar angle	2mrad	0.02 – 0.48%
Calorimeter noise	+/- 20 MeV (per jet)	0.01 – 0.74%
JES	0.5 % (lab-frame)	0.2 – 4.4%
Uncorrelated		0.6%
Normalisation		1.0%

- Any further uncertainty (eff., model, unfold, rad.-corr., etc.) has an unknown p_T and Q^2 shape
→ further uncertainty are represented through **uncorrelated** or **normalisation**

Jet energy scale uncertainty

Jet energy scale uncertainty

- Achieved precision at HERA (H1): 1%

LHeC

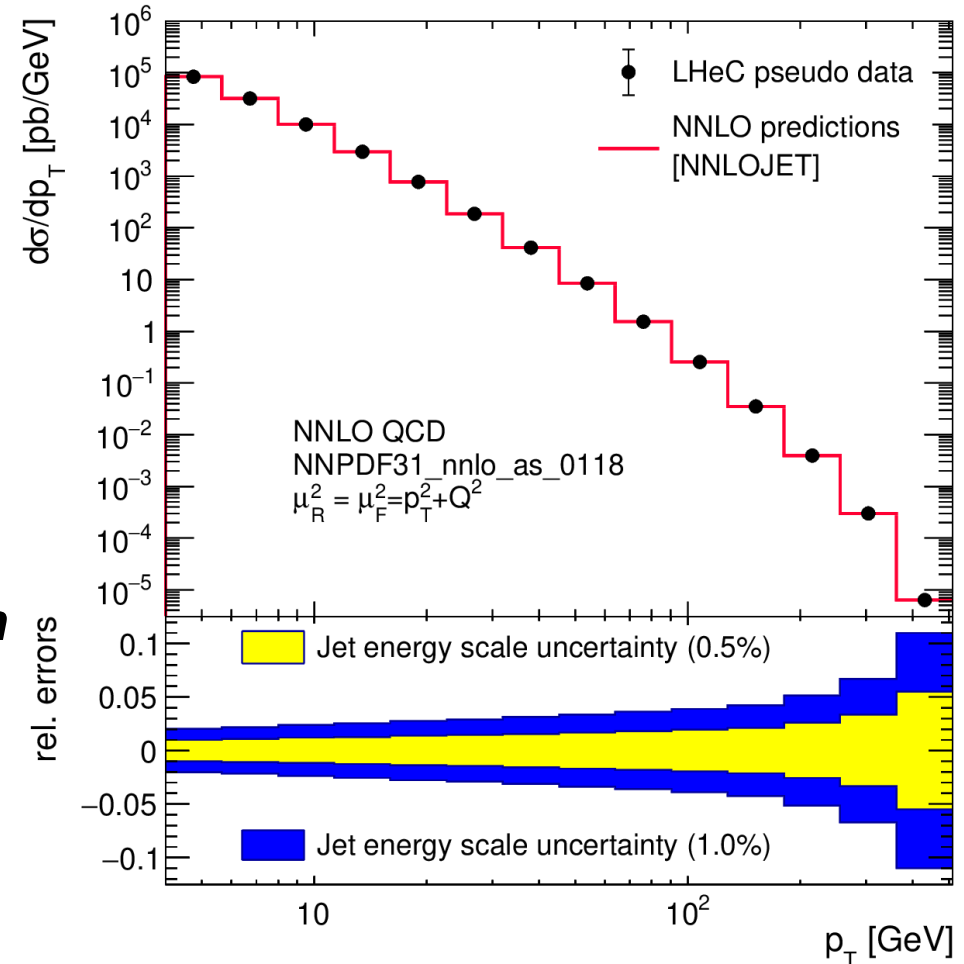
- Likely achieve: $\delta_{\text{JES}} \sim 0.5\%$

Propagation to cross sections

- JES is defined in lab-frame
- Dedicated simulation performed to

Size of JES uncertainty on cross section

- Similar to values reported by H1
- Very similar with CDR2012



Fit methodology

Fit methodology

- similar to EPJ C77 (2017) 791 & EPJ C79 (2019) 68 & arXiv:1906.05303
- NNLO predictions: account for α_s in ME & DGLAP ($\mu_0 \sim 30\text{GeV}$)

ME (NNLOJET), P (QCDNUM)

$$\sigma = f_{\mu_0} \otimes P_{\mu_0 \rightarrow \mu_F}(\alpha_s(M_Z)) \otimes \hat{\sigma}(\alpha_s(M_Z), \mu)$$

Only f_{μ_0} is taken
from NNPDF31

- α_s dependence in P is almost negligible

Minimisation with Minuit

- Consider all uncertainties as 'relative' in χ^2
 - No 'error-rescaling' needed.
 - No dependence on actual size of cross section in fit

$$\chi^2 = \sum_{ij} \log \frac{S_i}{\tilde{\sigma}_i} V_{ij}^{-1} \log \frac{S_j}{\tilde{\sigma}_j}$$

Consider 2D pseudo-data

- use 509 data points (H1 had 78 in HERA-II)
- pT binning gauged with CMS and H1 binning
- Q2 binning gauged with HERA (H1) NC DIS binning

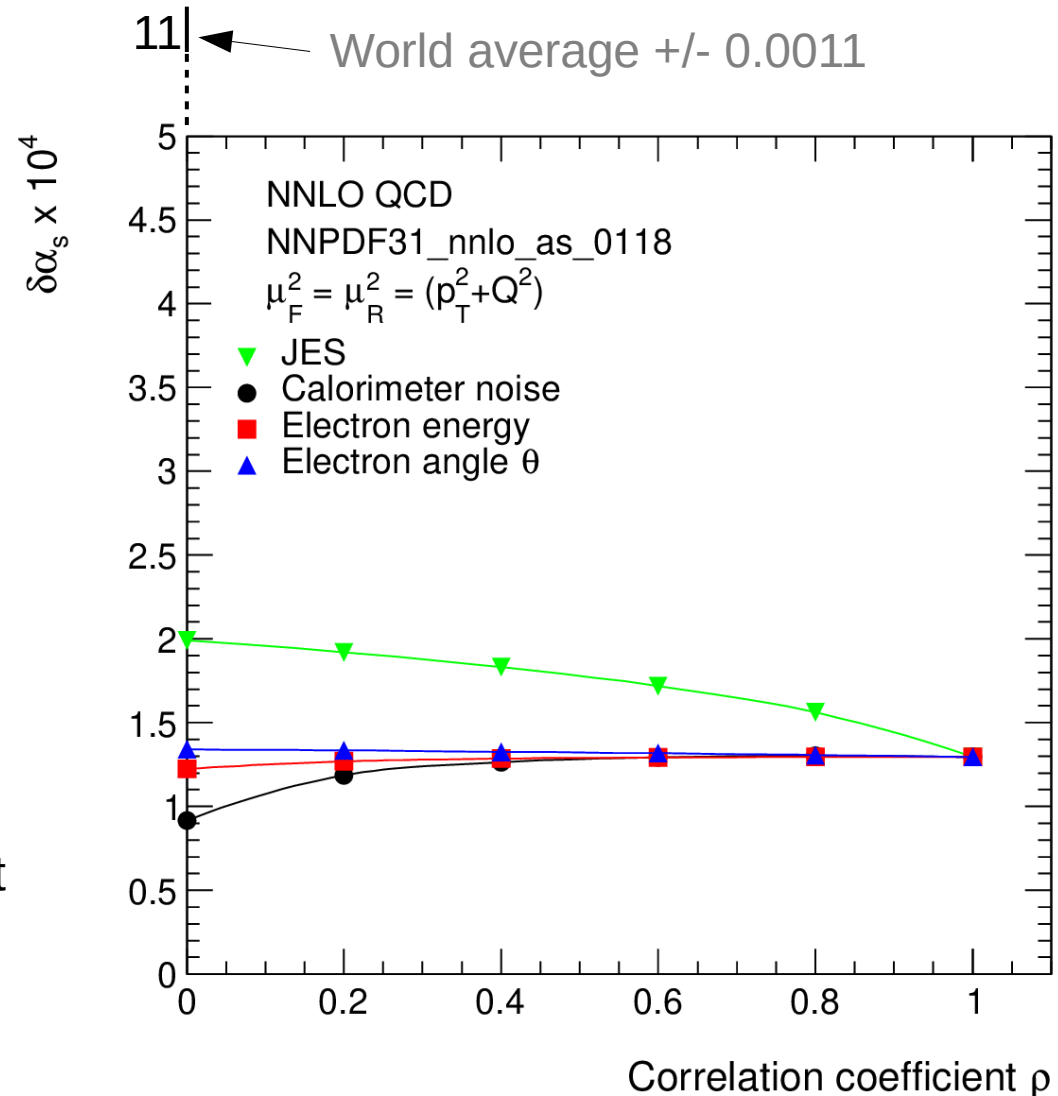
α_s uncertainty vs. 'correlation model'

Systematic uncertainties are considered as 'fully' correlated

- This may not be overoptimistic
- A full calibration could come with many smaller (correlated) error sources

Vary the correlation of a single syst. uncertainty

- Electron uncertainties are altogether fairly negligible
- Calorimeter noise decreases $\delta\alpha_s$ when considered uncorrelated
- JES increases $\delta\alpha_s$ when 'decorrelating' it



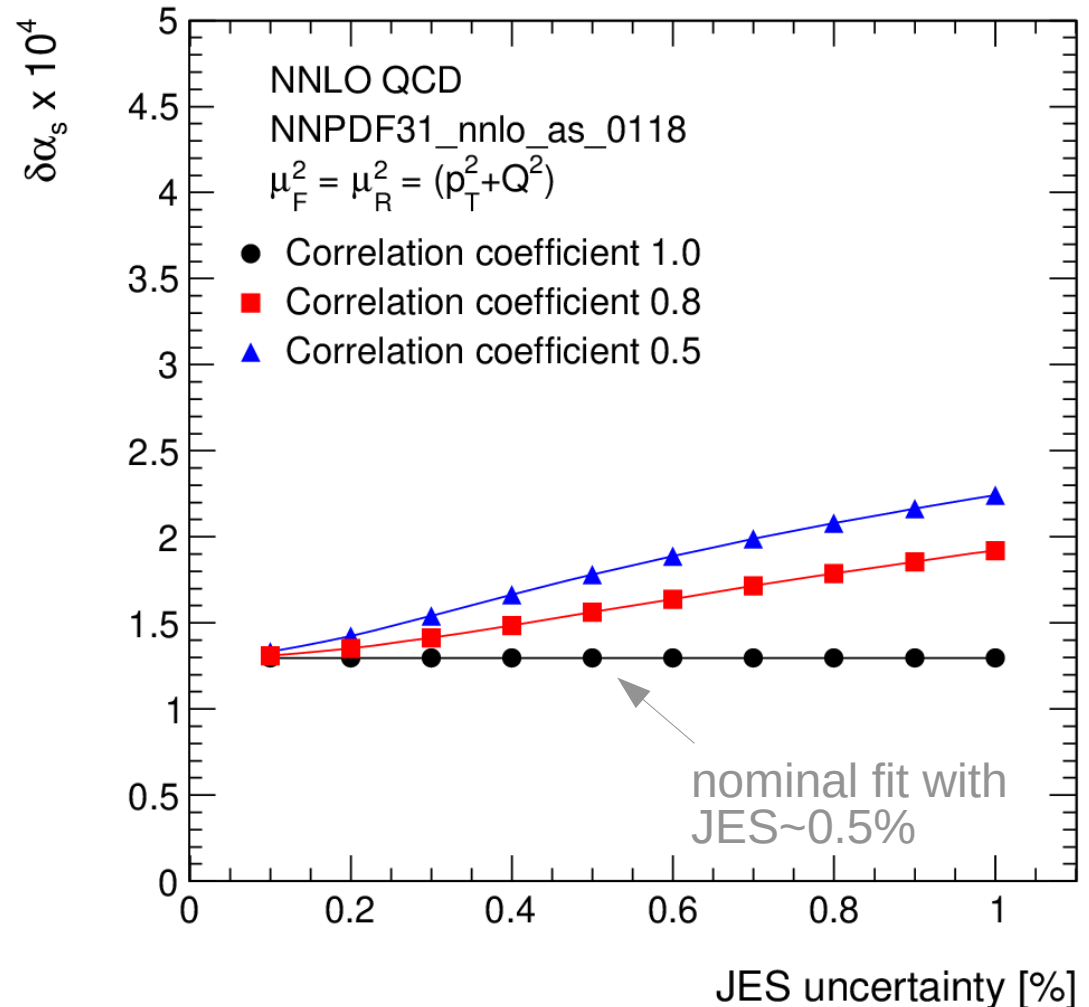
Size of jet-energy scale (JES)

Jet energy scale (JES)

- JES is expected to be 0.5% at detector-level
- H1 achieved 1%
- ATLAS/CMS ~1% (but pile-up, and difficult in-situ calibration!)
- Maybe even 0.3% is achievable ?!

Increase JES

- 0.1% up to 1.0%
- For fully correlated JES, size of JES irrelevant (but shape matters)
- moderate de-correlation:
→ moderate increase of $\delta\alpha_s$



Size of normalisation and uncorr. uncert.

Study size of

- normalisation uncertainty
- uncorrelated uncertainty

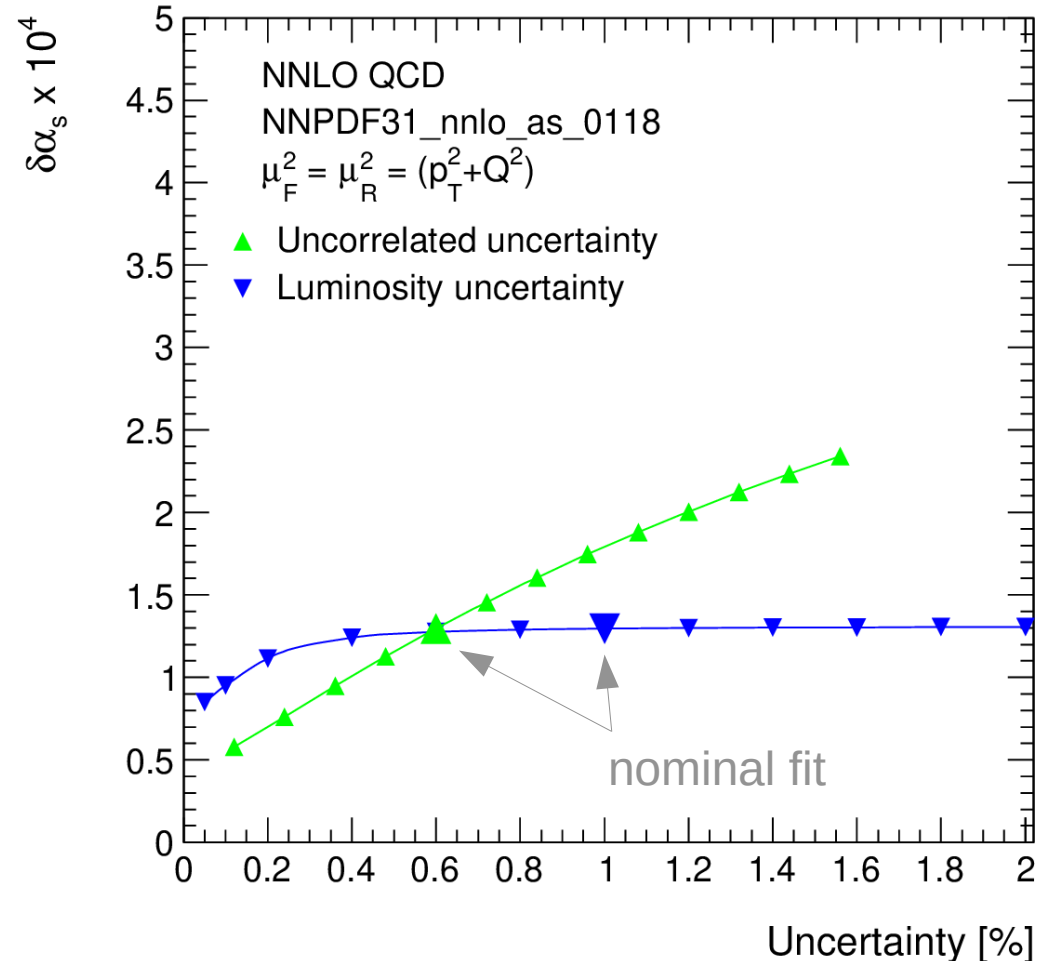
These two errors collect all sources with unknown p_T and Q^2 dependence

Normalisation uncertainty

- Fit uncertainty largely independent on size of normalisation uncertainty

Uncorrelated uncertainty

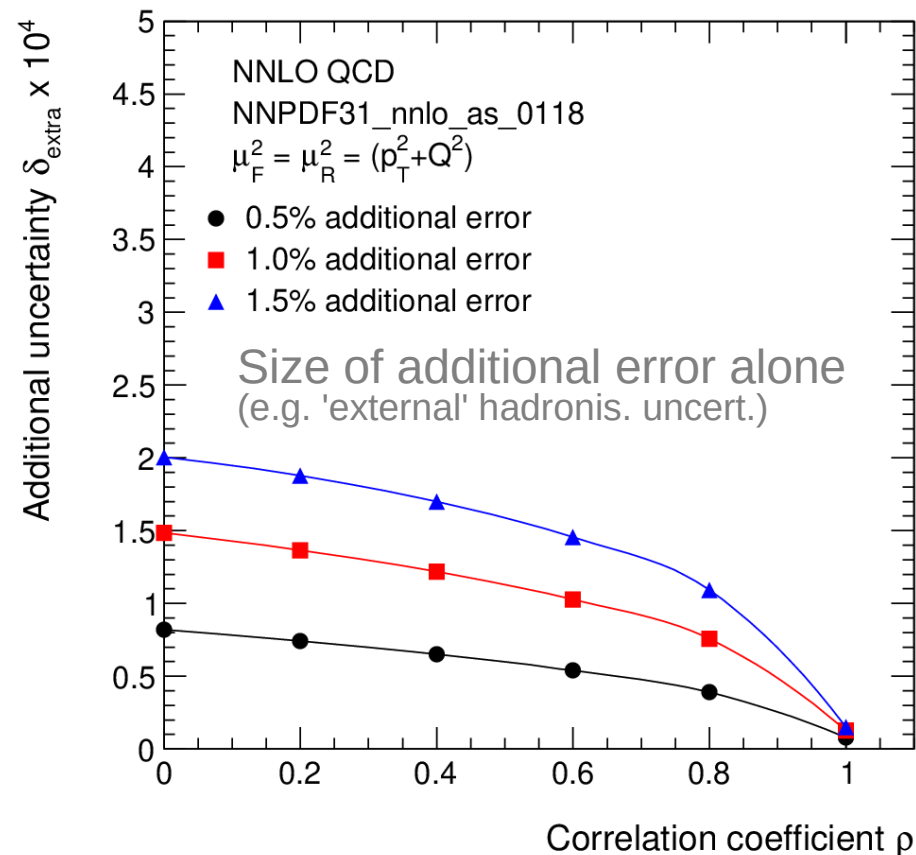
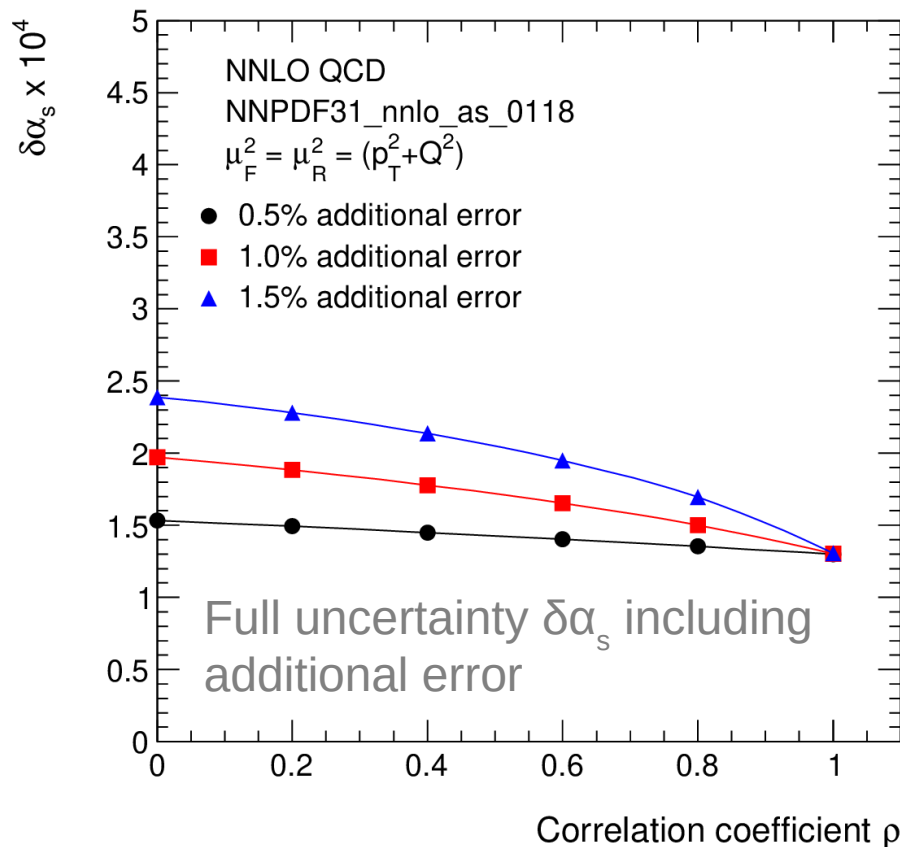
- Fit uncertainty largely dependent on size of uncorr. uncertainty
- Dominant uncertainty
- Difficult to estimate & correlates with number of data points



Consider an additional error

One additional error of same size for all points

- Study different sizes (0.5, 1.0, 1.5%) vs. its correlation
- Moderate increase in uncertainty



Error budget

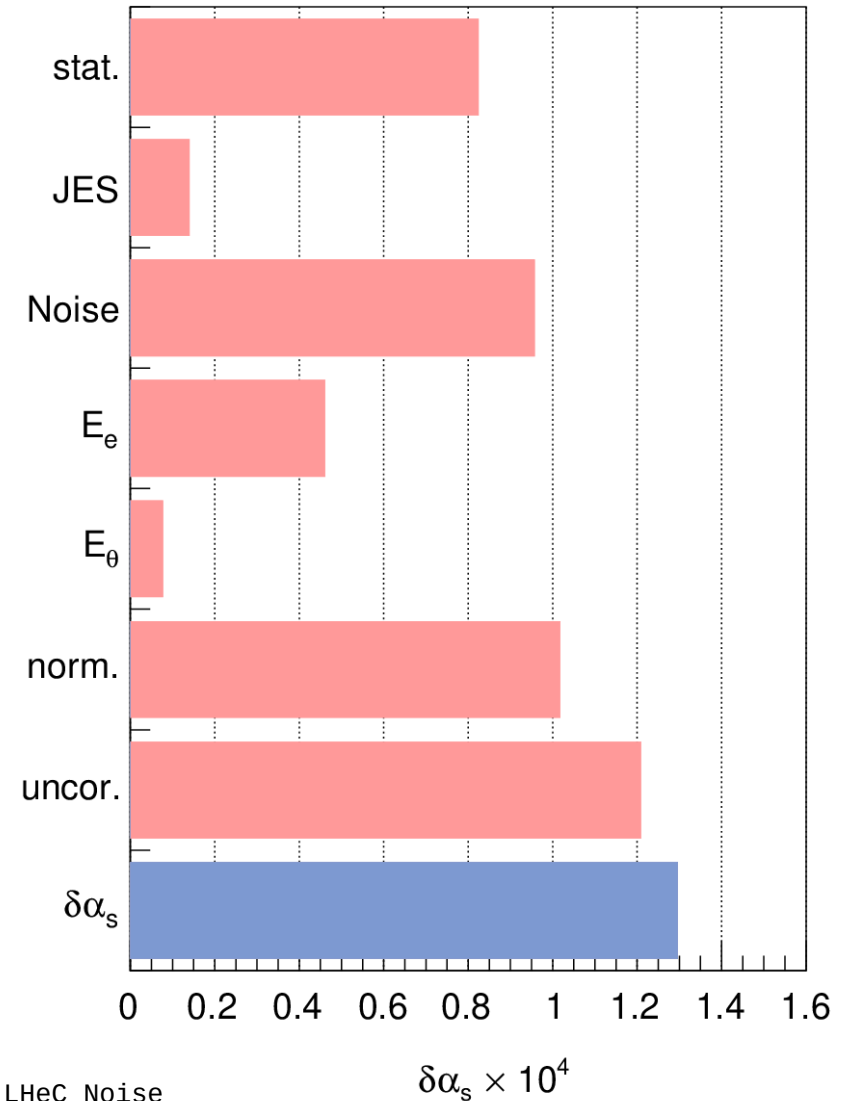
Estimate size of individual uncertainty

- Repeat fit with a single source excluded
 - Calculate quadratic 'difference' to nominal fit uncertainty
- (only) an approximate estimate
(quadratic sum of all sources overestimates total uncertainty)

Reasonable estimate

- Uncor. dominant
- stat. not negligible (min 0.15%)
- Calo-Noise more important than JES
 - shape more similar to α_s dependence
 - more important at lower p_T
- Electron uncertainties negligible
- Normalisation uncertainty important albeit it is finally constraint by fit
- PDF uncert (NNPDF31) ~ 0.0002 [not shown]

LHeC α_s error budget (approx.)



Correlations
AlphasMz

AlphasMz
1

LHeC_E1En
0.25549

LHeC_E1Th
0.15361

LHeC_JES5
-0.30176

LHeC_Lumi
-0.82283

LHeC_Noise
-0.86228

$\delta\alpha_s \times 10^4$

NNLO scale uncertainty

Scale uncertainty

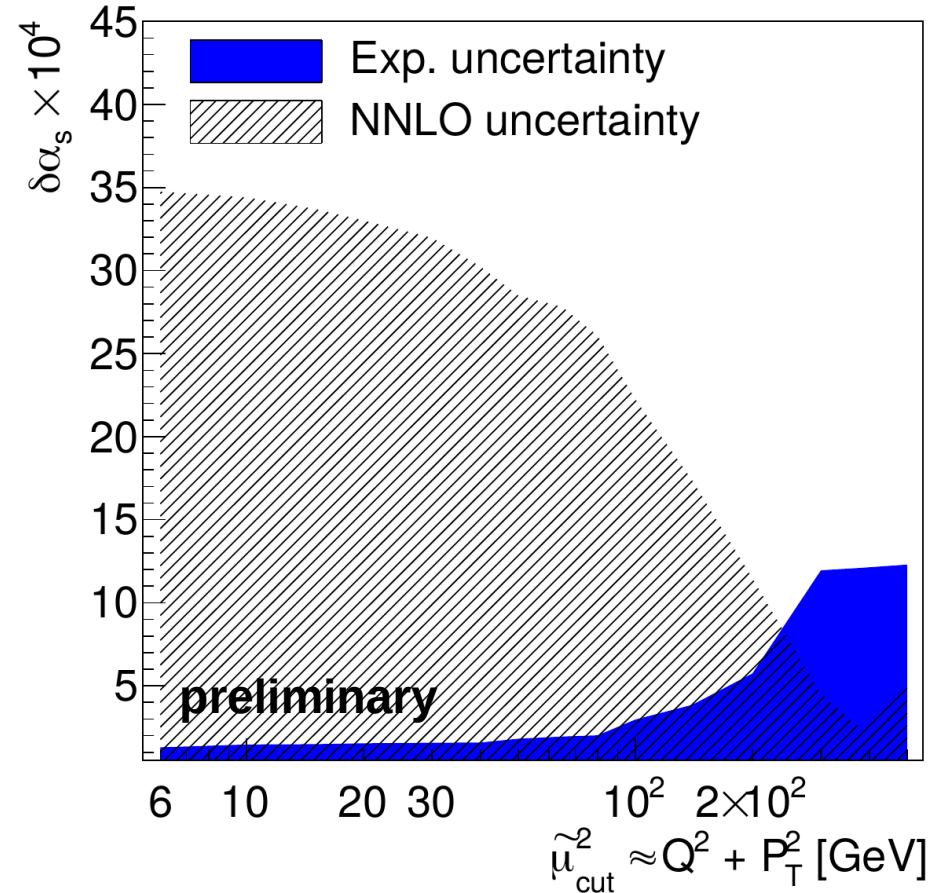
- Vary scale(s) by 0.5 and 2
- Or alternatively:
 - Estimate derivative w.r.t. μ_R , μ_F and get scale uncertainty as linear error propagation

Scale uncertainty full fit

- about: +/- 0.0035
- fairly large

Restrict data to higher scales

- define a lower cut: $\mu^2 \sim Q^2 + p_T^2$
- Cut lower scales: expect reduction of scale uncertainty



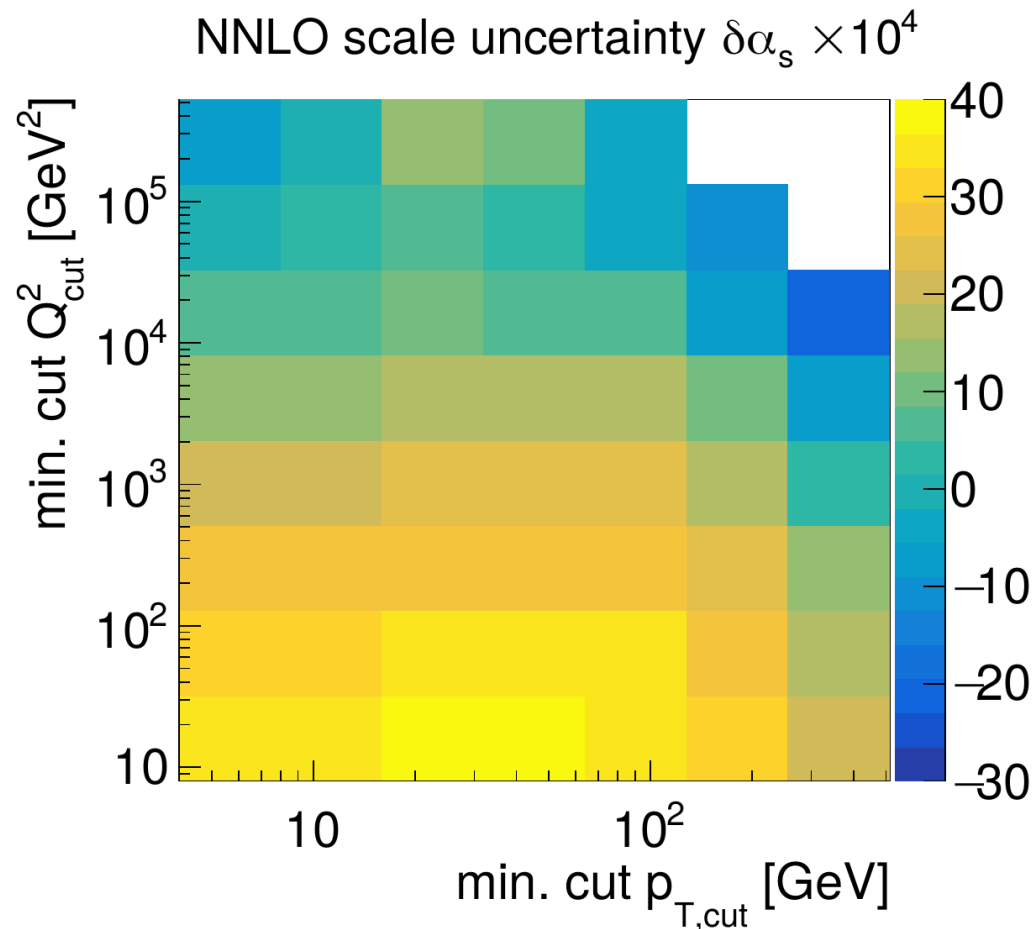
NNLO scale uncertainty

Evaluate NNLO scale uncertainty

- Cut lower values p_T and Q^2

NNLO scale uncertainty

- Exclusion of low- p_T bins does not reduce scale uncertainty
- Exclusion of low- Q^2 bins reduces scale uncertainty
- For $Q^2 > 2000 \text{ GeV}^2$
 $\delta\alpha_s^{\text{scale}} \sim 0.0015$
- For $Q^2 > 8000 \text{ GeV}^2$
 $\delta\alpha_s^{\text{scale}} \sim 0.001$



α_s determination at different μ_R intervals

α_s determination at different μ_r intervals

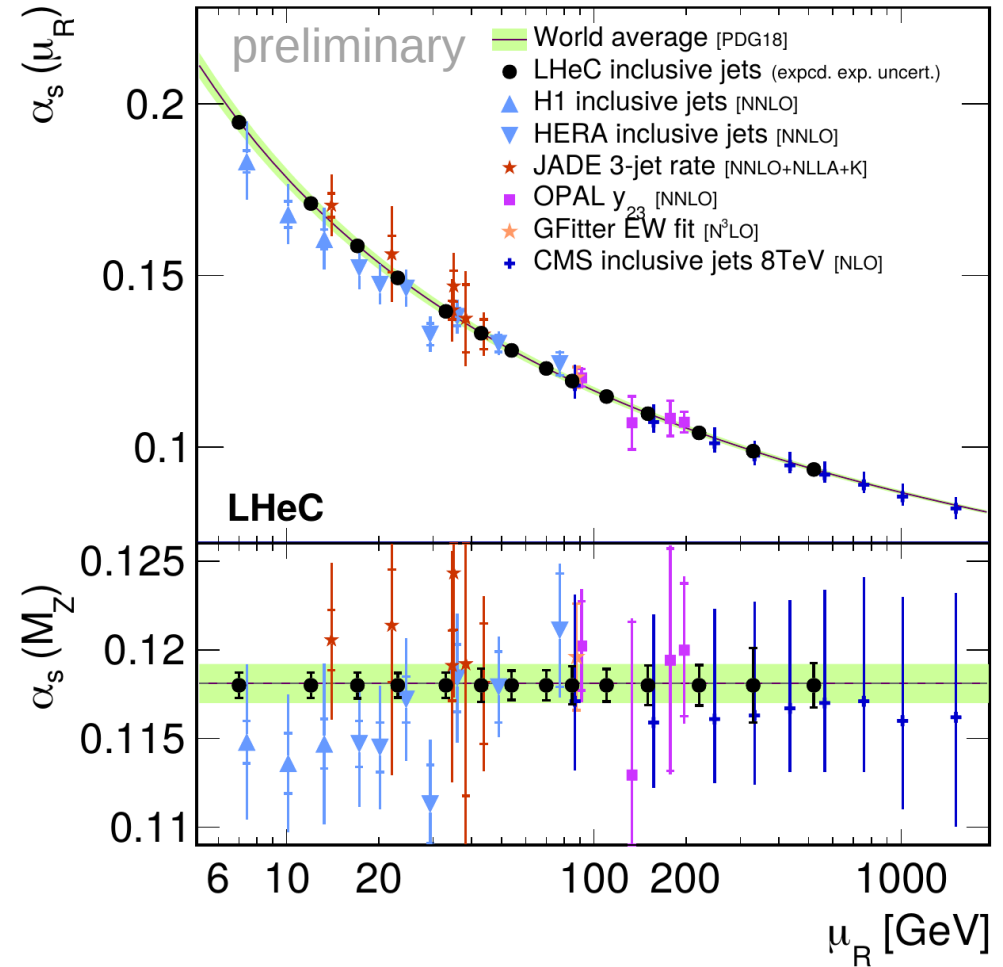
→ 'running'

$$\text{Use: } \mu_R^2 = Q^2 + p_T^2$$

High exp. sensitivity over large kinematic range

- $6 < \mu_R < 600 \text{ GeV}$
- Exp. uncertainty typically $\delta\alpha_s \sim 0.0007\text{--}0.0011$ for all studied intervals

Great improvement over other (jet-based) measurements



α_s from inclusive NC/CC DIS cross sections

Perform α_s -fit together with PDFs

- 'standard' HERA-like parameterisation
- Validate that different gluon param. do not alter the α_s uncertainty significantly

NC+CC DIS @ 60 x 7000 GeV

- $\delta\alpha_s \sim 0.00029$

NC+CC DIS @ 50 x 7000 GeV

- $\delta\alpha_s \sim 0.00038$
- $Q^2 > 20 \text{ GeV}^2$: $\delta\alpha_s \sim 0.00044$

+ inclusive jets

- NC/CC + incl. jets: fit does not yield reliable uncertainties (yet)

Snowmass 2013

case	cut [Q^2 in GeV^2]	relative precision in %
HERA only (14p)	$Q^2 > 3.5$	1.94
HERA+jets (14p)	$Q^2 > 3.5$	0.82
LHeC only (14p)	$Q^2 > 3.5$	0.15
LHeC only (10p)	$Q^2 > 3.5$	0.17
LHeC only (14p)	$Q^2 > 20.$	0.25
LHeC+HERA (10p)	$Q^2 > 3.5$	0.11
LHeC+HERA (10p)	$Q^2 > 7.0$	0.20
LHeC+HERA (10p)	$Q^2 > 10.$	0.26

DATA	exp. error on α_s
NC e ⁺ only	0.48%
NC	0.41%
NC & CC	0.23% :=⁽¹⁾
⁽¹⁾ $\gamma_h > 5^\circ$	0.36% := ⁽²⁾
⁽¹⁾ +BCDMS	0.22%
⁽²⁾ +BCDMS	0.22%
⁽¹⁾ stat. *= 2	0.35%

(prel.) conclusion
 In such a 'combined' PDF+ α_s fit I do not see much impact of the inclusive jet pseudo-data

Summary and conclusions

Inclusive jets @ LHeC

- new NNLO calculations performed
- pseudo-data estimated

α_s estimate

- α_s uncertainty estimated from inclusive jet pseudo-data
- Exp. uncertainty: $\delta\alpha_s \sim \mathbf{0.00013}$
 - Improvement w.r.t. current world average by factor ~ 8
- NNLO scale uncertainty remains
 - Reduction feasible with restricted kinematic range (remove parts with large $\log(pT/Q)$)
 - Reduction possible with improved predictions (resumm.)
 - Other processes with possibly less scale dependence (e.g. di-jets)
- α_s from inclusive DIS
 - $E_e = 60$ GeV: $\delta\alpha_s \sim 0.0003$
 - $E_e = 50$ GeV: $\delta\alpha_s \sim 0.0004$