

# Fermion dark matter in models with $U(1)$ symmetry



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Paper in preparation

# Higgs portal DM

Kanemura, Matsumoto, Nabeshima, Okada, 1005.5651 (PRD),  
Djouadi, Lebedev, Mambrini, Quevillon, 1112.3299 (PLB), ...

- Minimal models (renormalizable and gauge invariant)
  - Real scalar
    - **Scalar DM:** Real scalar with a  $Z_2$  symmetry  
J. M. Cline, K. Kainulainen, P. Scott and C. Weniger, 1306.4710 (PRD)], ...
    - **Fermion DM:** Real scalar + Singlet fermion  
Y. G. Kim, K. Y. Lee and S. Shin, 0803.2932 (JHEP),  
S. Baek, P. Ko and W. I. Park, 1112.1847 (JHEP), ...
  - Complex scalar
    - **Goldstone DM:** Complex scalar with a softly broken global  $U(1)$  symmetry  
C. Gross, O. Lebedev, T. Toma, 1708.02253 (PRL)], ...
    - **Vector DM:** Complex scalar with a local  $U(1)_X$  symmetry
      - The  $U(1)_X$  gauge boson gets mass after SSB (Dark Higgs mechanism)
      - The  $U(1)_X$  kinetic mixing term  $B_{\mu\nu} F^{\mu\nu}$  should be forbidden by a  $Z_2$  symmetry  
S. Baek, P. Ko, W. I. Park and E. Senaha, 1212.2131 (JHEP),  
M. Duch, B. Grzadkowski and M. McGarrie, 1506.08805 (JHEP), ...
- **We discuss models with  $U(1)_X$  without ad hoc discrete symmetry.**

# DM with $U(1)$ symmetry

- Particle contents

- Complex scalar field  $S$  (Dark Higgs) w/  $U(1)_X$  charge  $Q_S = 1$
- $U(1)_X$  gauge field  $X_\mu$  (Dark Photon)  $D_\mu S = (\partial_\mu + ig_X Q_S X_\mu) S$
- $\Psi$  [= Scalar, Fermion] (Dark Matter) w/  $U(1)_X$  charge  $Q_\Psi = 1/N$

- **The stability of DM [ $\Psi$ ] is guaranteed by residual  $Z_N$  symmetry<sup>\*</sup>, after spontaneous symmetry breaking of  $U(1)$  by  $\langle S \rangle \neq 0$ .**

<sup>\*</sup> **Local (gauged)  $U(1)$  symmetry protects DM stability even with higher dimensional terms.**

- $N = 2$  case ( $\Psi^2 S^\dagger \rightarrow Z_2$  symmetry)

- $\Psi =$  Scalar [S. Baek, P. Ko, W.I. Park, 1407.6588 (PLB)]
- $\Psi =$  Fermion

A. Ahmed, M. Duch, B. Grzadkowski, M. Iglicki, 1710.01853 (EPJC): Multi-comp. DM ( $\epsilon=0$ )

L. Darmé, S. Rao, L. Roszkowski, 1710.08430 (JHEP):  $m_{\text{DM}} < m_{Z'}$

M. Pospelov, et al., 0711.4866 (PLB),...:  $m_{\text{DM}} \gtrsim m_{Z'}$  (secluded regime) w/o Dark Higgs mechanism

S. Baek, P. Ko, TM, W. I. Park (**this work**): We focus on the role of dark Higgs for DM indirect searches.

P. Ko, TM, Y. L. Tang, 1910.04311 : DM bound state formation (**see Yi-Lei Tang's talk on Tuesday**)

- $N = 3$  case ( $\Psi^3 S^\dagger \rightarrow Z_3$  symmetry)

- $\Psi =$  Scalar [P. Ko, Y. Tang, 1402.6449 (JCAP)]

# Global $U(1)$ vs. Local $U(1)$ in fermion DM

- Scalar sector:  $V_0(\Phi, \mathbb{S}) = -m_\Phi^2 |\Phi|^2 - m_S^2 |\mathbb{S}|^2 + \lambda_\Phi |\Phi|^4 + \lambda_S |\mathbb{S}|^4 + \lambda_{\Phi S} |\Phi|^2 |\mathbb{S}|^2$

$$\Phi^{\text{SM}}, \mathbb{S} = \frac{1}{\sqrt{2}} (v_S + s + ix^0) \rightarrow (h, H) \text{ w/ mixing angle } \theta$$

- Fermion sector:  $\mathcal{L}_\psi = -m_\psi \bar{\psi} \psi - \frac{y_\psi}{\sqrt{2}} \bar{\psi}^c \psi \mathbb{S}^\dagger + h.c.$       $\psi_+ = \frac{\psi + \psi^c}{\sqrt{2}}$       $\psi_- = \frac{\psi - \psi^c}{\sqrt{2}i}$

- **Global model**  $\mathcal{L} = \mathcal{L}_{\text{SM}} + |\partial_\mu \mathbb{S}|^2 - V_0(\Phi, \mathbb{S}) + i\bar{\psi} \partial \psi + \mathcal{L}_\psi$

The NG boson  $x$  plays the role of a dark radiation. [S. Weinberg, 1305.1971 (PRL)]

$T_{\text{dec}} \sim m_\mu$  [ $\Delta N_{\text{eff}} = 0.39$ ] could satisfy the constraint of  $N_{\text{eff}}$ .

- **Local model**  $\mathcal{L} = \mathcal{L}_{\text{SM}} - \frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{1}{2} \sin \epsilon X_{\mu\nu} B^{\mu\nu} + |D_\mu \mathbb{S}|^2 - V_0(\Phi, \mathbb{S}) + i\bar{\psi} D \psi + \mathcal{L}_\psi$

The NG boson  $x$  is absorbed by the gauge boson  $Z'$ .

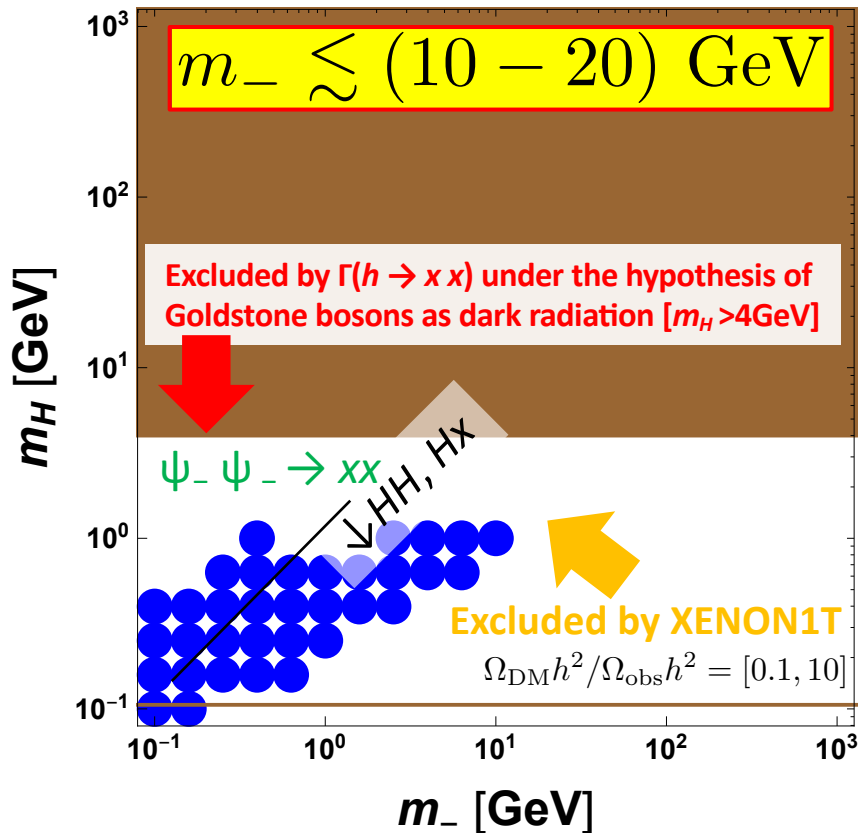
SSB gives the origin of the  $Z'$  mass (Dark Higgs mechanism).

We compare the local  $U(1)$  model and the global  $U(1)$  model.

# Comparing two models with the DM direct search exclusion

The **global** U(1) model

$$(m_+/m_- - 1, s_\theta, \lambda_S) = (10^{-3}, 10^{-4}, 1)$$

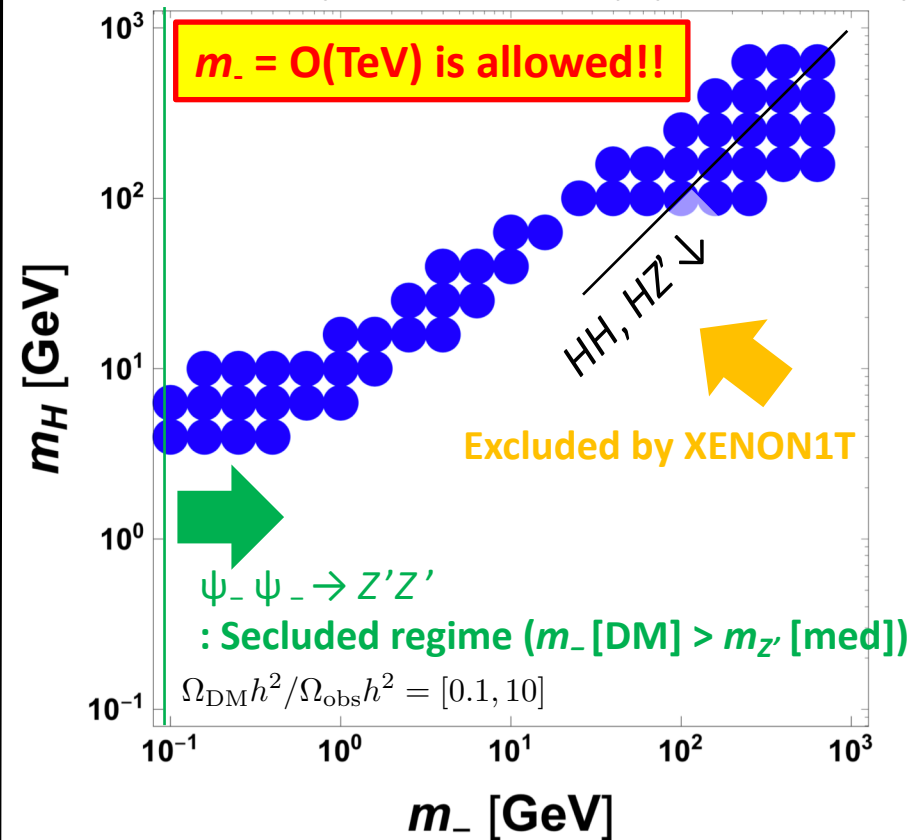


Consistent with [C. G. -Cely, A. Ibarra, E. Molinaro, 1310.6256 (JCAP)]

The global model limit for  $m_{Z'}$  or  $g_X \rightarrow 0$  in the local model

The **local** U(1) model

$$m_{Z'} = 0.1 \text{ GeV}, (m_+/m_- - 1, s_\epsilon, s_\theta, \lambda_S) = (0.5, 10^{-1}, 10^{-6}, 1)$$

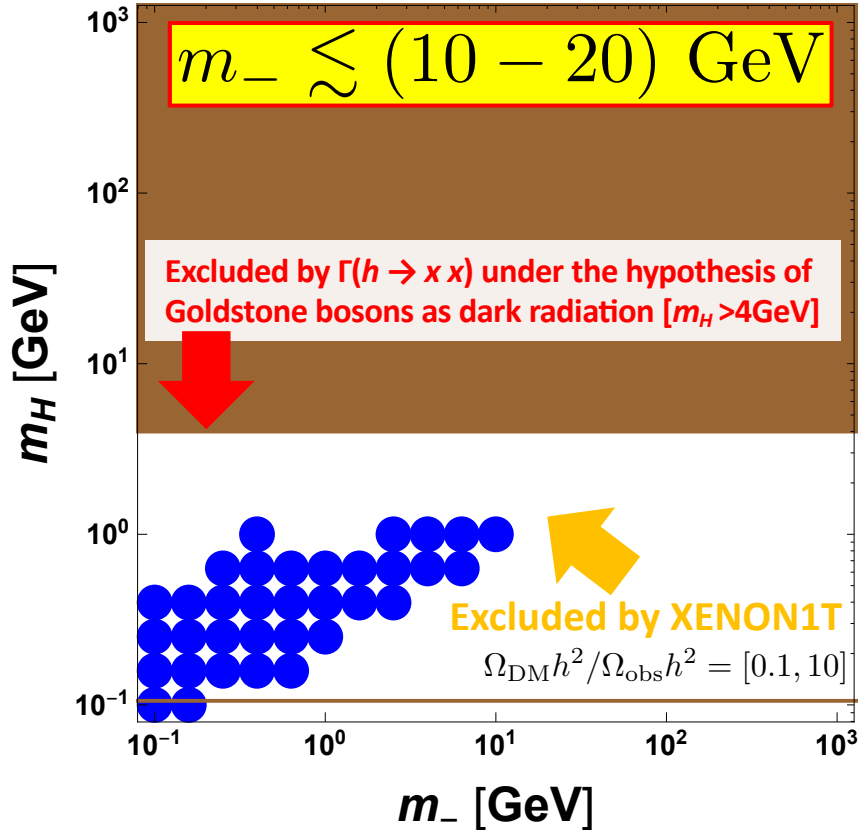


If  $y_\psi$  is large,  $\psi_- \psi_- \rightarrow HH$  is possible at  $m_H < m_-$ .  
 $\rightarrow$  Large  $m_-$  is allowed for the local U(1) model.

# Comparing two models with the DM direct search exclusion

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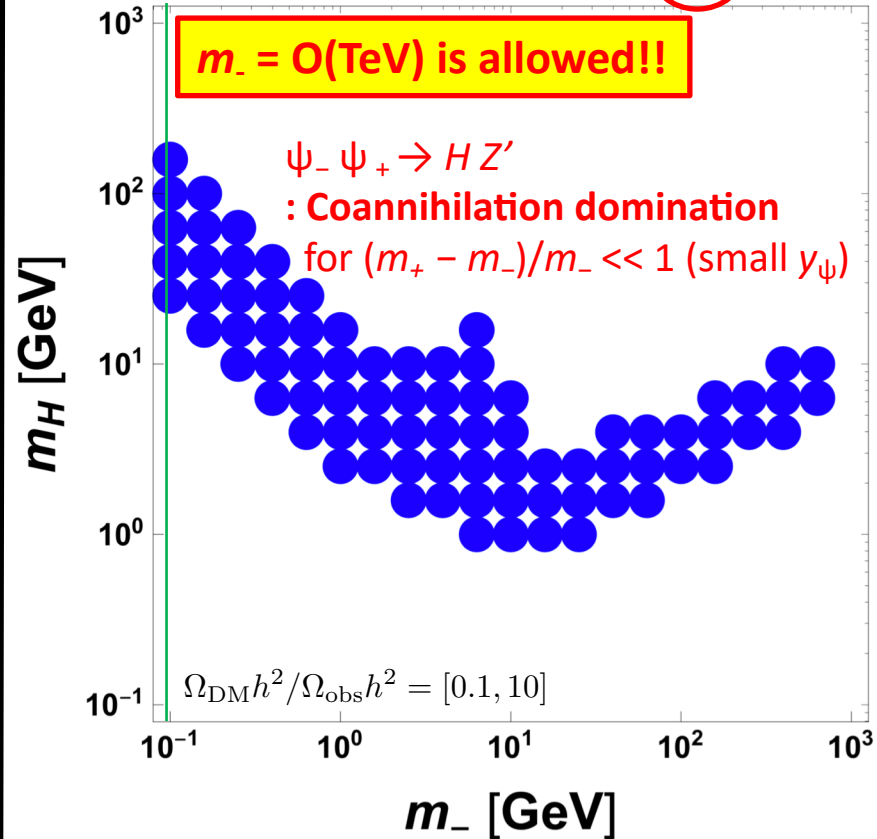


Consistent with [C. G. -Cely, A. Ibarra, E. Molinaro, 1310.6256 (JCAP)]

The global model limit for  $m_{Z'}$  or  $g_X \rightarrow 0$  in the local model

The **local** U(1) model

$$m_{Z'} = 0.1 \text{ GeV}, (m_+/m_- - 1, s_\epsilon, s_\theta, \lambda_S) = (10^{-2}, 10^{-1}, 10^{-6}, 1)$$

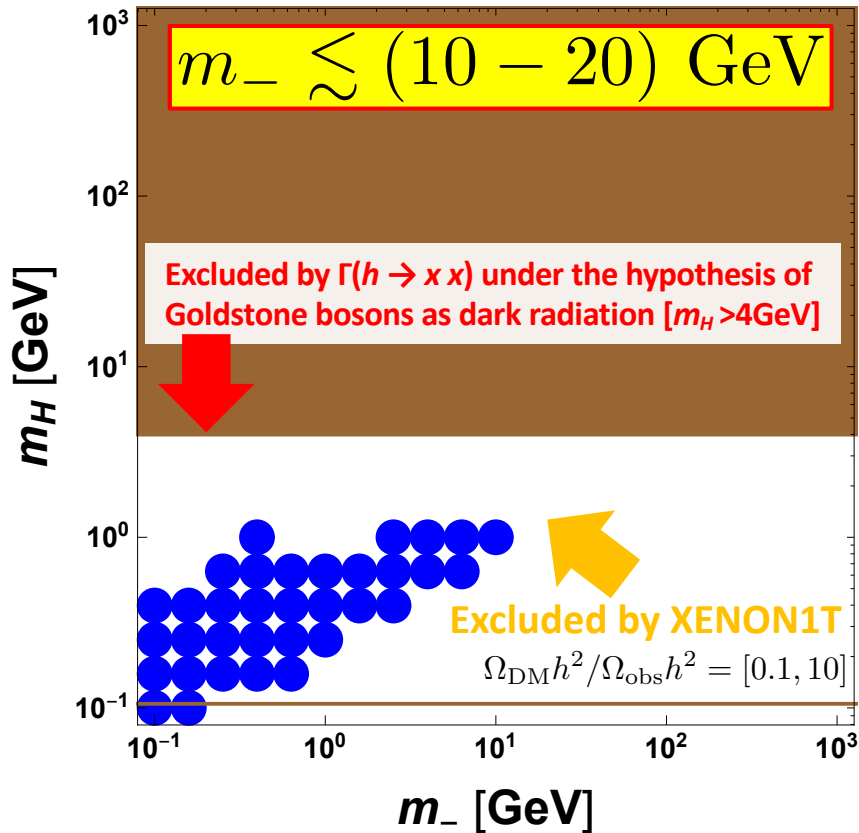


Coannihilation process gives significant deviation with large  $g_X$  for the local model.

# Comparing two models with the DM direct search exclusion

The **global** U(1) model

$$(m_+/m_- - 1, s_\theta, \lambda_S) = (10^{-3}, 10^{-4}, 1)$$

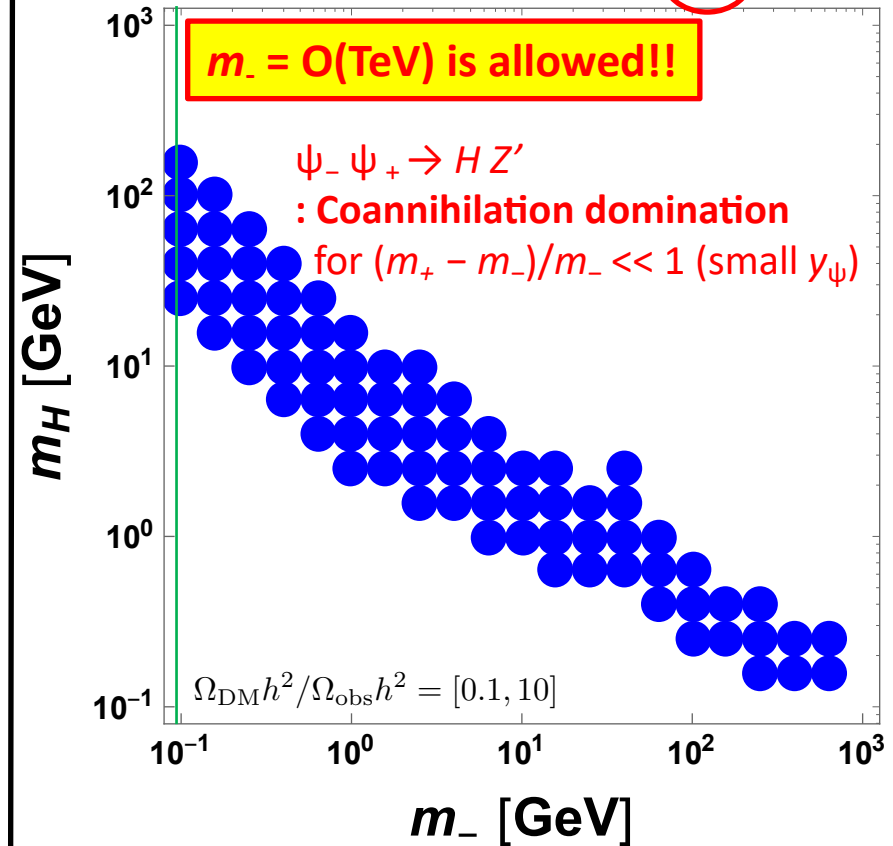


Consistent with [C. G. -Cely, A. Ibarra, E. Molinaro, 1310.6256 (JCAP)]

The global model limit for  $m_{Z'}$  or  $g_X \rightarrow 0$  in the local model

The **local** U(1) model

$$m_{Z'} = 0.1 \text{ GeV}, (m_+/m_- - 1, s_\theta, \lambda_S) = (10^{-5}, 10^{-1}, 10^{-6}, 1)$$



Coannihilation process gives significant deviation with large  $g_X$  for the local model.

# DM indirect searches for local model

- Secluded regime is difficult to detect at colliders or direct searches, but indirect signatures will be important prove.

M. Pospelov, A. Ritz a, M. Voloshin, 0711.4866 (PLB)

- A unified model which explains PAMELA/Fermi, WMAP, INTEGRAL and DAMA simultaneously was proposed.

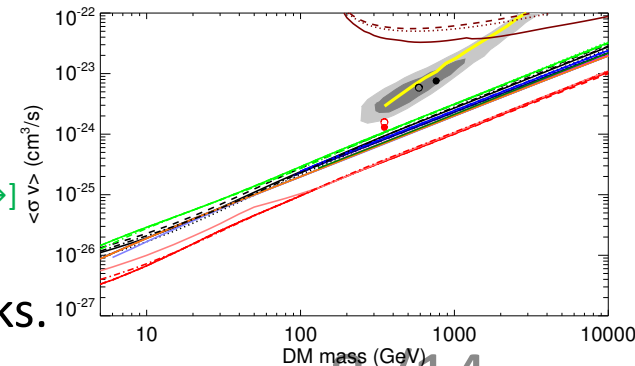
N. Arkani-Hamed, D. P. Finkbeiner, T. R. Slatyer and N. Weiner, 0810.0713 (PRD)

- Cosmic ray spectra require a WIMP with

- $m_{\text{DM}} \sim 0.5\text{-}1 \text{ TeV}$  N. Arkani-Hamed, D. P. Finkbeiner, T. R. Slatyer and N. Weiner, 0810.0713 (PRD)
- $\langle\sigma v\rangle \sim O(10^{-23}) \text{ cm}^3 \text{ s}^{-1}$  A. Lopez, C. Savage, D. Spolyar and D. Q. Adams, arXiv:1501.01618 (JCAP)

- However,

- CMB bound on s-wave annihilation excludes  $\langle\sigma v\rangle \gtrsim O(10^{-24}) \text{ cm}^3 \text{ s}^{-1}$  T. R. Slatyer, 1506.03811 (PRD) [Fig →]
- Dark Higgs mechanism (the origin of  $m_{Z'}$  or  $m_{\text{DM}}$ ) was not considered in the previous works.



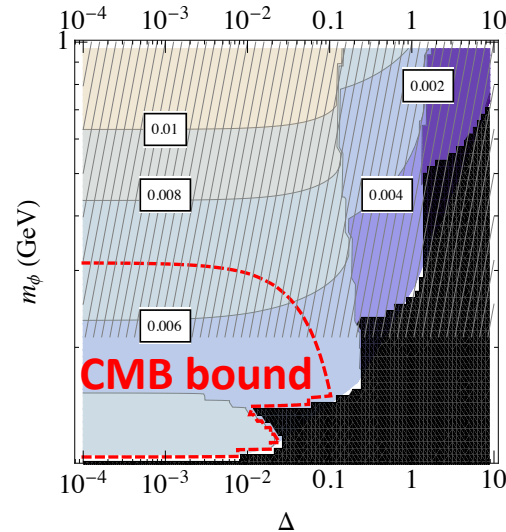


# DM indirect searches for local model

- In order to avoid the CMB constraint, we consider presence of local substructure with Sommerfeld enhancement.

$$S_{\text{eff}} \simeq S_{v(r)} + S_{v \rightarrow 0} \Delta(r) \quad \text{T. R. Slatyer, N. Toro and N. Weiner, 1107.3546 (PRD)}$$

- $S_v$  is the Sommerfeld enhancement factor at velocity  $v$
- $1 + \Delta(r) \equiv \frac{\langle \rho^2(r) \rangle}{\langle \rho(r) \rangle^2}$  is substructure boost factor where  $r =$  Galactocentric radius
- In the substructure-dominated case, the CMB bound allows for  $\Delta \gtrsim O(0.1)$

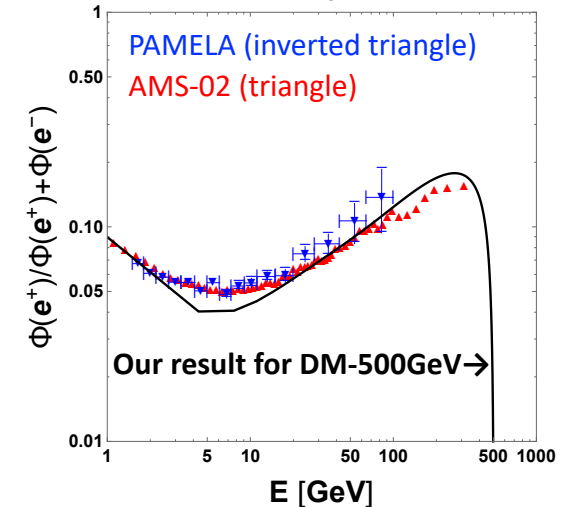
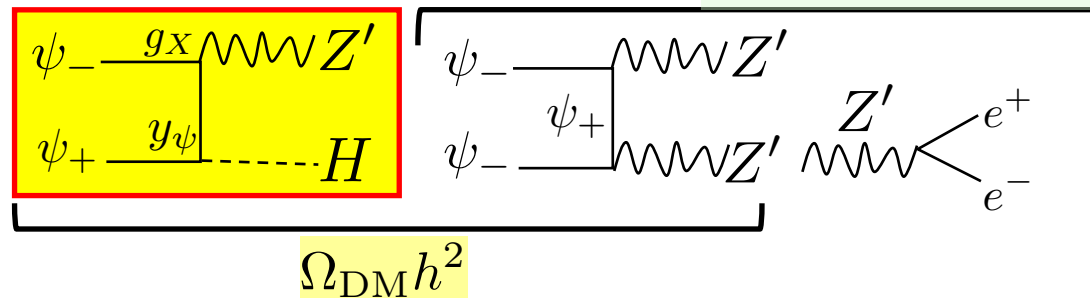


A case for 1000GeV DM  
with  $7 \times 10^{-4}$  GeV mass splitting

$$\frac{1}{2} \frac{y_\psi}{\Lambda} (\bar{\psi}^C \psi S^* S^* + h.c)$$

# Positron excess (PAMELA, Fermi, AMS-02, ...)

- Annihilation process:



- Benchmark point in our model:

BM	$m_-$	$\delta \equiv m_+ - m_-$	$g_X$	$m_{Z'}$	$\sin \epsilon$	$m_H$	$\sin \theta$
DM(500GeV)	500 GeV	0.005 GeV	0.79	100 MeV	$10^{-4}$	200 MeV	$10^{-6}$

PAMELA  $\uparrow$

co-annihilation  $\uparrow$

$\Omega_{DM} h^2$

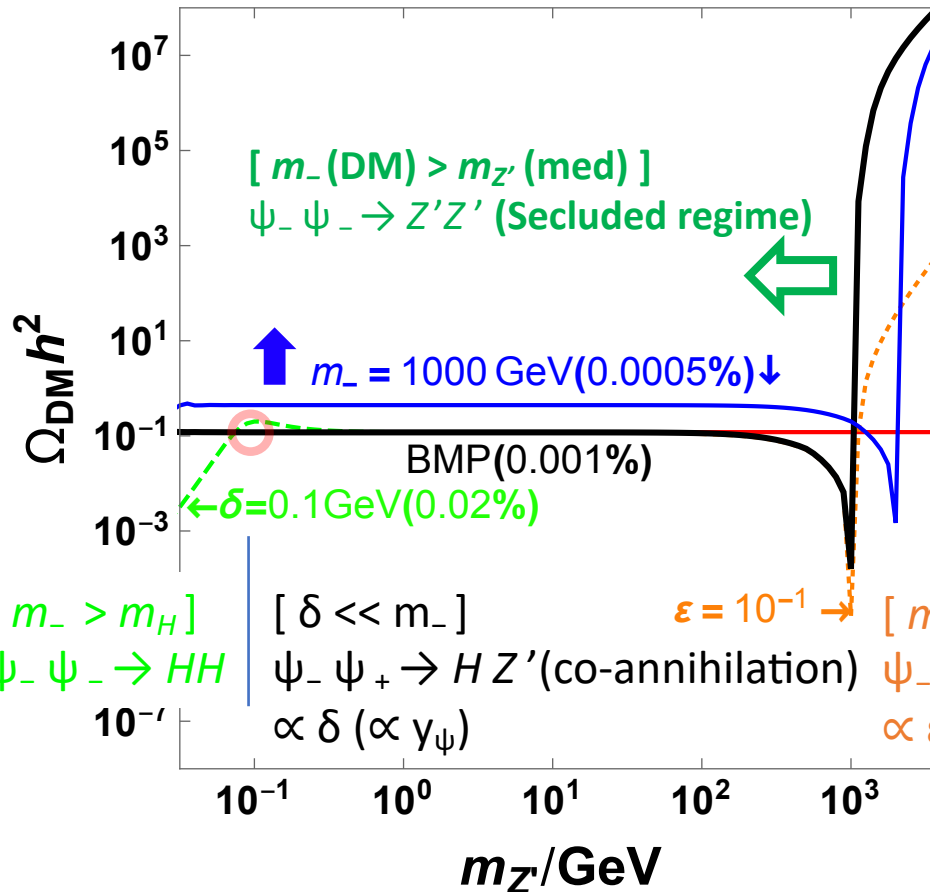
Constrained  
by dark photon  
searches

DM direct searches  
& perturbativity  
give upper bound

If  $m_{Z'} > 2m_\mu$ , the relic density does not change, but the final state may become more complicated.

- We find the contribution of dark Higgs is important!

# DM relic density (Parameter dependence)

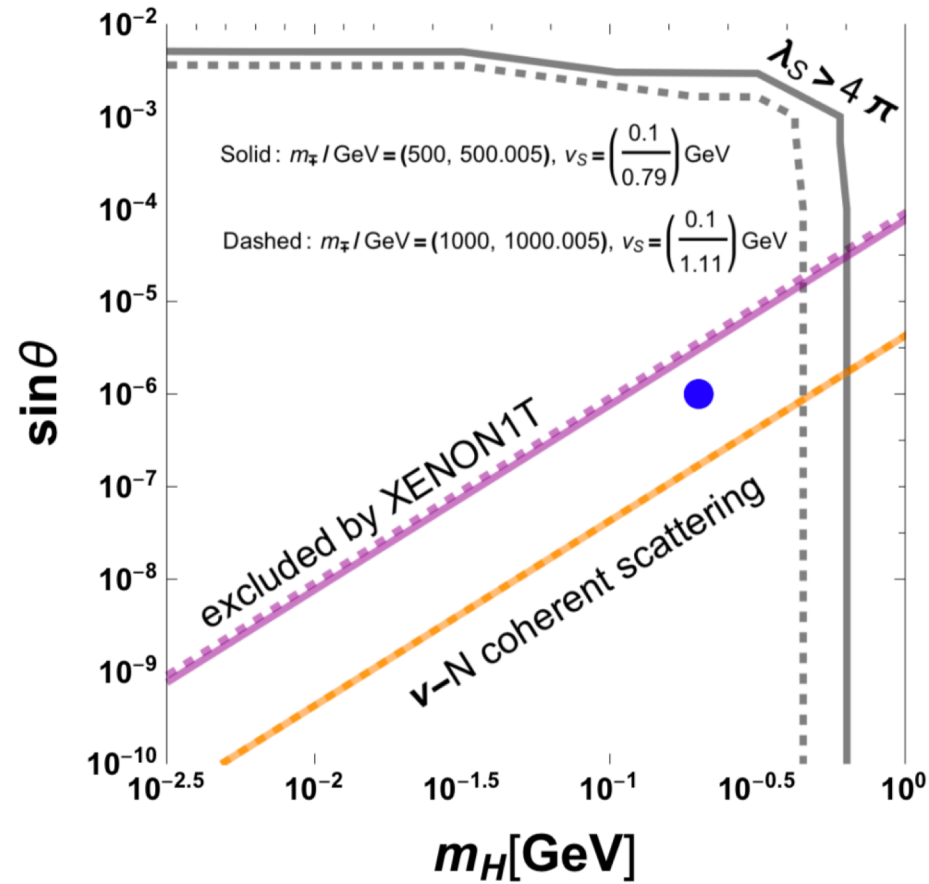
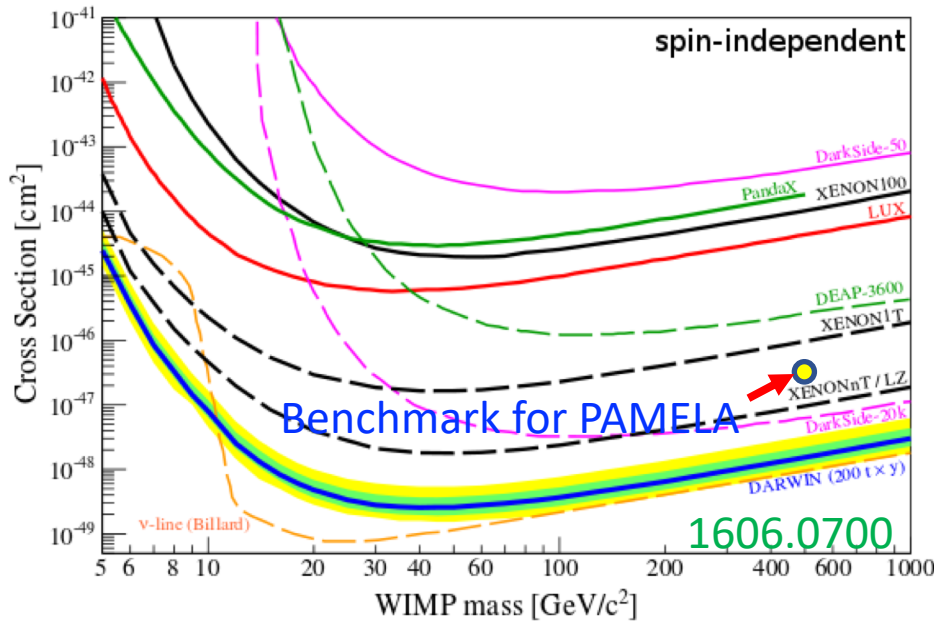


Dominant processes:

$[m_- > m_H]$   $\psi_- \psi_- \rightarrow HH$   
 $[m_- > m_{Z'}]$   $\psi_- \psi_- \rightarrow Z' Z'$  (Secluded regime)  
 $[m_- > m_H]$   $\psi_- \psi_+ \rightarrow H Z'$  (co-annihilation)  
 $[m_{Z'} > m_- + m_+]$   $\psi_- \psi_+ \rightarrow Z' \times Z \rightarrow SM SM$   
 $\propto \delta$  ( $\propto \gamma_\psi$ )  $\propto \epsilon$

BM	$m_-$	$\delta \equiv m_+ - m_-$	$g_X$	$m_{Z'}$	$\sin \epsilon$	$m_H$	$\sin \theta$
DM(500GeV)	500 GeV	0.005 GeV	0.79	100 MeV	$10^{-4}$	200 MeV	$10^{-6}$

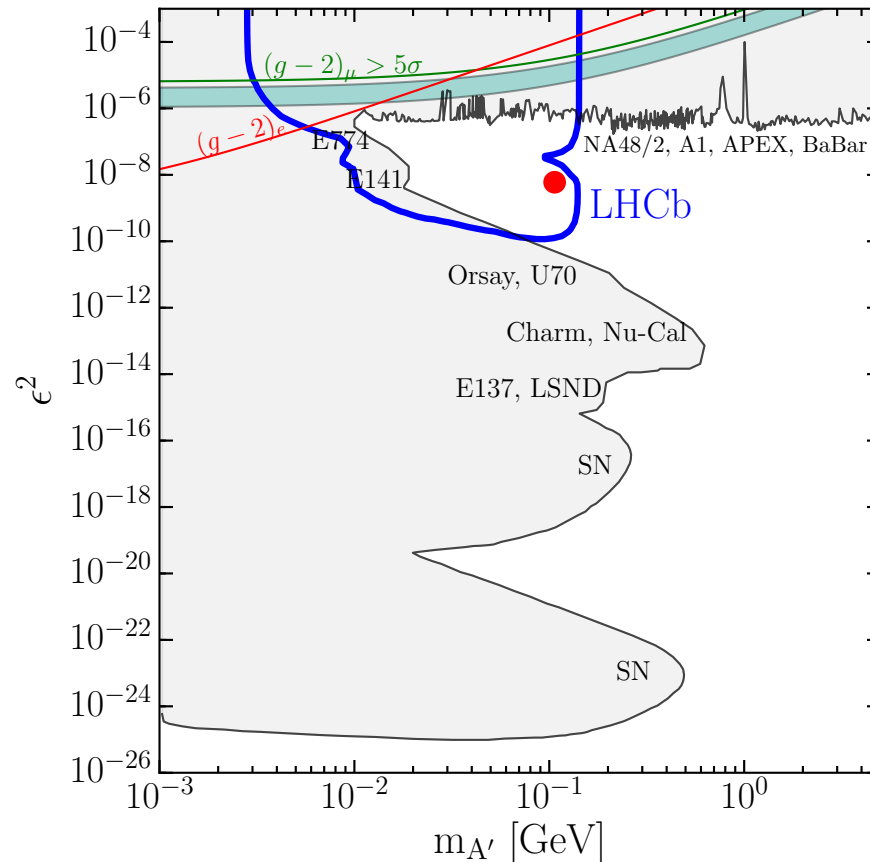
# DM direct searches



Perturbativity:  $\lambda_S = \frac{g_X^2}{2m_{Z'}^2} (m_h^2 \sin^2 \theta + m_H^2 \cos^2 \theta) < 4\pi$

# Dark photon searches

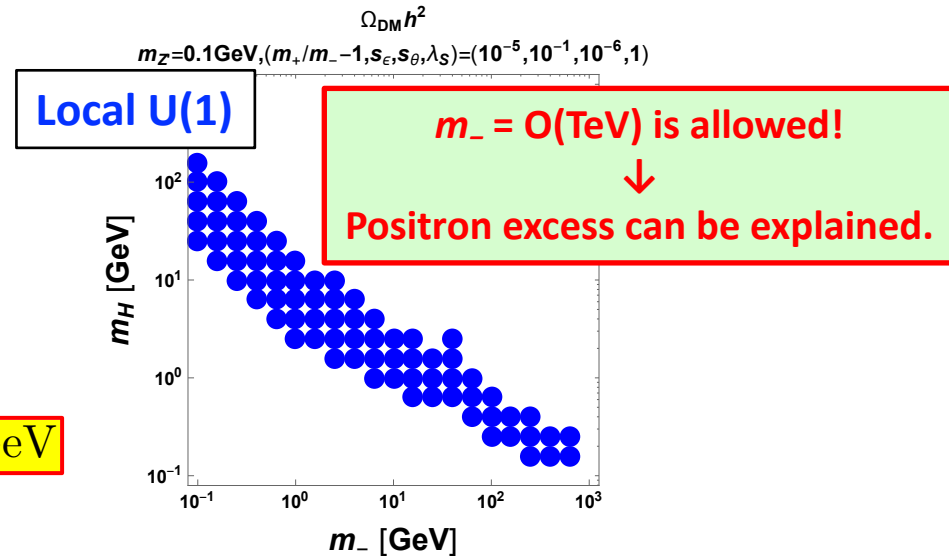
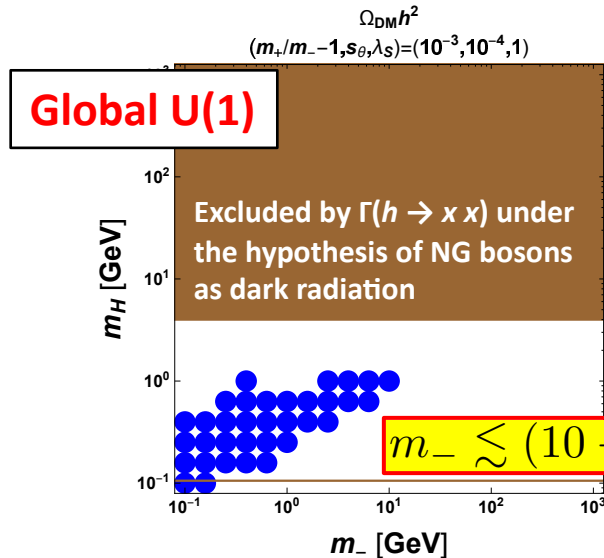
P. Ilten, J. Thaler, M. Williams and W. Xue, arXiv:1509.06765 (PRD)



**Our BMP will be explored by APEX/Belle-II/HPS/LHCb/SeaQuest/SHiP.**

# Conclusions

- “SSB of  $U(1)_X$ ”  $\rightarrow$  DM is stabilized by a residual discrete symmetry.
- We have focused on a case for **the fermion DM**.
- We have shown that the deviation from the global  $U(1)_X$  case is significant by the coannihilation  $HZ'$  for the secluded regime ( $m_{Z'} \ll m_-$ ) in the local  $U(1)_X$  case.



- Considering DM local substructure, the local  $U(1)_X$  can explain positron excess of DM indirect searches and will be explored by direct searches for DM ( $\psi_-$ ) & DP ( $Z'$ ).
- **We have shown that the contribution of the dark Higgs is important.**

# Back Up

# Benchmark points

BM	$m_-$	$\delta \equiv m_+ - m_-$	$g_X$	$m_{Z'}$	$\sin \epsilon$	$m_H$	$\sin \theta$
DM(500GeV)	500 GeV	0.005 GeV	0.79	100 MeV	$10^{-4}$	200 MeV	$10^{-6}$
$\Omega h^2$	$\langle \sigma v \rangle$ [ $\text{cm}^3 \text{sec}^{-1}$ ]	$\tau_{Z'}$ [sec]	$\tau_{\psi_+}$ [sec]	$\tau_H$ [sec]	$\sigma^{\text{SI}}$ [ $\text{cm}^2$ ]		
0.1187	$2.3 \times 10^{-26}$	$1.2 \times 10^{-13}$	$3.9 \times 10^{-4}$	$7.3 \times 10^{-3}$	$3.4 \times 10^{-47}$		
$\psi_- \psi_+ \xrightarrow{48\%} Z' H$	$\psi_- \psi_- \xrightarrow{100\%} Z' Z'$	$Z' \xrightarrow{50\%} \bar{u} u$	$\psi_+ \xrightarrow{99\%} \psi_- e^- e^+$ $\psi_+ \xrightarrow{1\%} \psi_- \bar{u} u$	$H \xrightarrow{88\%} \bar{s} s$			
$\psi_- \psi_- \xrightarrow{26\%} Z' Z'$		$Z' \xrightarrow{38\%} e^- e^+$		$H \xrightarrow{10\%} \bar{d} d$			
$\psi_+ \psi_+ \xrightarrow{26\%} Z' Z'$		$Z' \xrightarrow{12\%} \bar{d} d$		$H \xrightarrow{2\%} \bar{u} u$			



The **global** model

# Goldstone boson as dark radiation

[S. Weinberg, 1305.1971 (PRL)]

- Radiation = relativistic particle
- Effective number of neutrino species ( $N_{\text{eff}}$ )
  - SM @  $T < m_e$  ( $\gamma, \nu_{i=1,2,3}$ ):  $N_{\text{eff}}^{\text{SM}} (\equiv g_\nu/g_\gamma) = 3.046$

[Mangano, Miele, Pastor, Pinto, Pisanti, Serpico, 0506164 (NPB)]

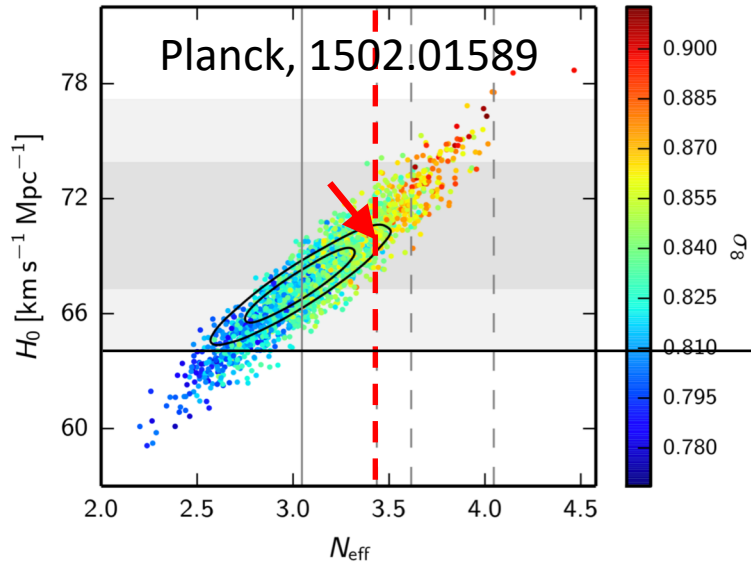
$$\rho_{\text{rad}} = \rho_\gamma + \rho_\nu = \left( 1 + \frac{g_\nu}{g_\gamma} \left( \frac{7}{8} \right) \left( \frac{T_\nu}{T_\gamma} \right)^4 \right) \rho_\gamma \quad \frac{(T_\nu)_{\text{after}}}{(T_\gamma)_{\text{before}}} = \left( \frac{2}{11/2} \right)^{1/3}$$

- Existence of dark radiation:  $\Delta N_{\text{eff}} \equiv N_{\text{eff}} - N_{\text{eff}}^{\text{SM}}$ 
  - Goldstone decoupling @  $T_{\text{dec}} < m_\mu$  ( $\gamma, \nu_{i=1,2,3}, e$ ):  $\Delta N_{\text{eff}} = 0.39$

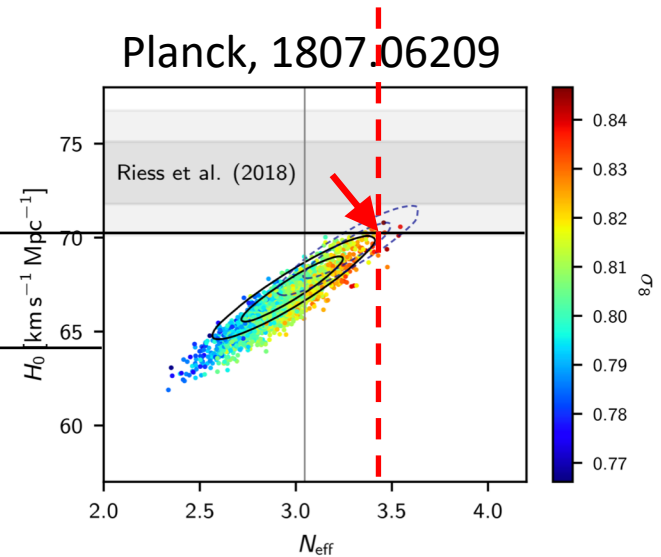
Assumption

$$\rho_x = \frac{1}{2} \left( \frac{T_x}{T_\gamma} \right)^4 \rho_\gamma = \left( \frac{1}{2} \frac{8}{7} \left( \frac{T_x}{T_\nu} \right)^4 \right) \left( \frac{7}{8} \right) \left( \frac{T_\nu}{T_\gamma} \right)^4 \rho_\gamma \quad \frac{(T_x)_{\text{before}}}{(T_\nu)_{\text{after}}} = \left( \frac{57/4}{43/4} \right)^{1/3}$$

# The global model: Constraint of $N_{\text{eff}}$



**Fig. 31.** Samples from *Planck* TT+lowP chains in the  $N_{\text{eff}}-H_0$  plane, colour-coded by  $\sigma_8$ . The grey bands show the constraint  $H_0 = (70.6 \pm 3.3) \text{ km s}^{-1} \text{ Mpc}^{-1}$  of Eq. (30). Notice that higher  $N_{\text{eff}}$  brings  $H_0$  into better consistency with direct measurements, but increases  $\sigma_8$ . Solid black contours show the constraints from *Planck* TT,TE,EE+lowP+BAO. Models with  $N_{\text{eff}} < 3.046$  (left of the solid vertical line) require photon heating after neutrino decoupling or incomplete thermalization. Dashed vertical lines correspond to specific fully-thermalized particle models, for example one additional massless boson that decoupled around the same time as the neutrinos ( $\Delta N_{\text{eff}} \approx 0.57$ ), or before muon annihilation ( $\Delta N_{\text{eff}} \approx 0.39$ ), or an additional sterile neutrino that decoupled around the same time as the active neutrinos ( $\Delta N_{\text{eff}} \approx 1$ ).



**Fig. 35.** Samples from *Planck* TT,TE,EE+lowE chains in the  $N_{\text{eff}}-H_0$  plane, colour-coded by  $\sigma_8$ . The grey bands show the local Hubble parameter measurement  $H_0 = (73.45 \pm 1.66) \text{ km s}^{-1} \text{ Mpc}^{-1}$  from [Riess et al. \(2018a\)](#). Solid black contours show the constraints from *Planck* TT,TE,EE+lowE+lensing+BAO, while dashed lines the joint constraint also including [Riess et al. \(2018a\)](#). Models with  $N_{\text{eff}} < 3.046$  (left of the solid vertical line) require photon heating after neutrino decoupling or incomplete thermalization.

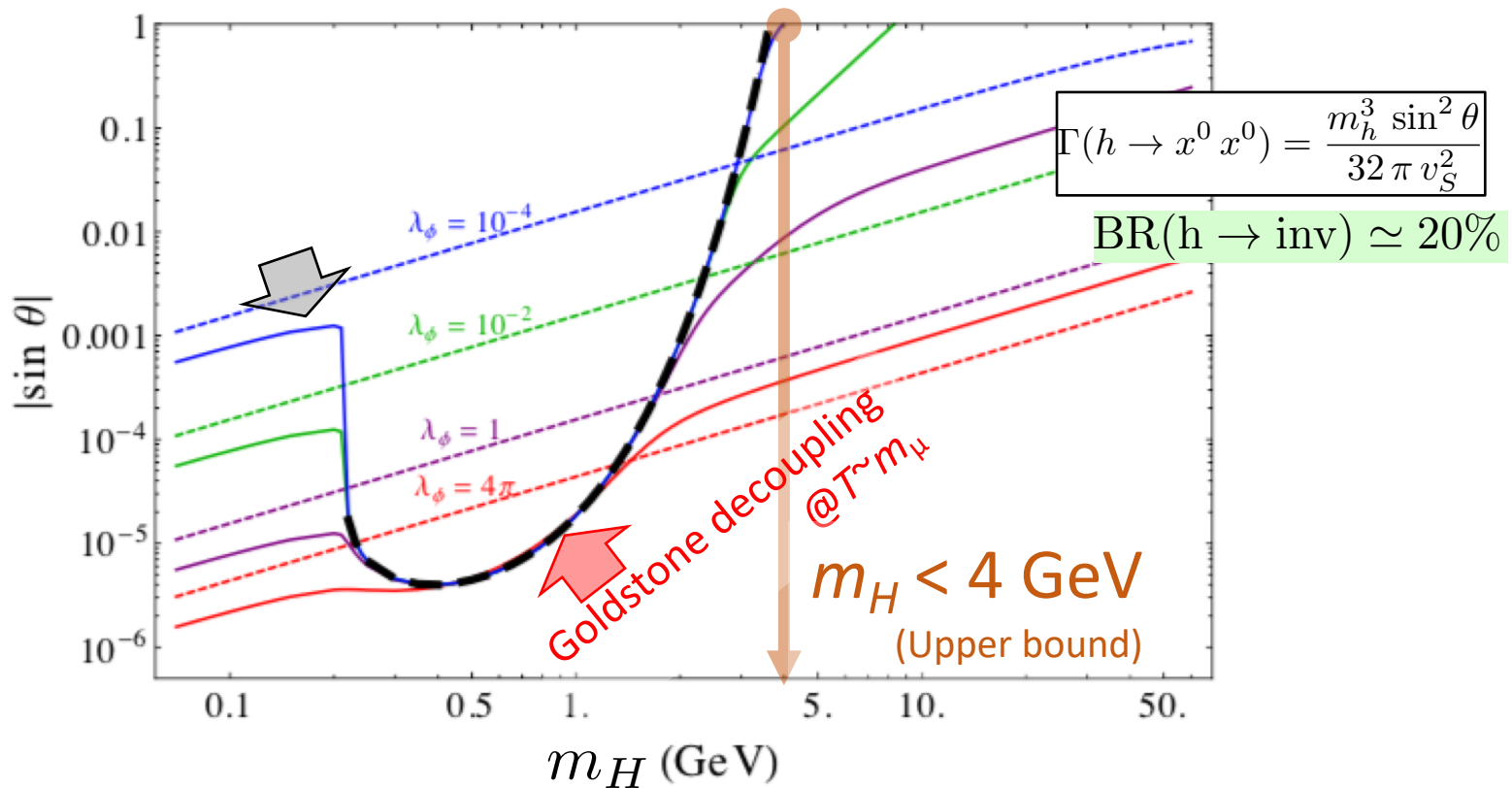
## Tension between $N_{\text{eff}}$ and $H_0$

→ The global model w/ $T_{\text{dec}} < m_\mu$  is allowed for the joint constraint ( $1\sigma$ ).

# The global model Constraints

[C. G. -Cely, A. Ibarra, E. Molinaro, 1310.6256 (JCAP)]

- Lower bound of  $\sin\theta$  ← Goldstone boson can play the role of a dark radiation
- Upper bound of  $\sin\theta$  ← Decay rate:  $\Gamma(h \rightarrow xx)$



# The global model Constraints

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- Lower bound of  $\sin\theta$  ← Goldstone boson can play the role of a dark radiation
- Upper bound of  $\sin\theta$  ← Decay rate:  $\Gamma(h \rightarrow xx)$  and DM direct detection

