

The 1st Asian-European-Institutes (AEI) Workshop for BSM and the 9th  
KIAS Workshop on Particle Physics and Cosmology

# Continuum Naturalness

- particle without particle

Seung J. Lee

Nov. 6, 2019

With C. Csaki, S. Lombardo, G. Lee, O. Telem; JHEP 2019(03)

With C. Csaki, G. Lee, O. Telem work in progress

With C. Csaki, W. Xue; work in progress



# Naturalness Paradigm Under Pressure

◆ **Naturalness** “typically” **implies new colored top partners**

~TeV scale to cut off the top contribution to the Higgs potential

not too many theoretical frameworks;

two major ones

**AdS/CFT**  
warped extra dimension  
(RS setup)

Supersymmetry:  
stop

Composite Higgs:  
Fermionic top partners  
(partial compositeness)

Higgs is a fundamental scalar,  
just like many other  
SUSY partners

Higgs is a composite resonance,  
just like many composite  
resonances in the theory of  
strong dynamics

# Naturalness Paradigm Under Pressure

## ◆ Naturalness “typically” implies new colored top partners

~TeV scale to cut off the top contribution to the Higgs potential

\*Neutral Naturalness is not discussed in this talk

not too many theoretical frameworks;

two major ones



**AdS/CFT**  
warped extra dimension  
(RS setup)

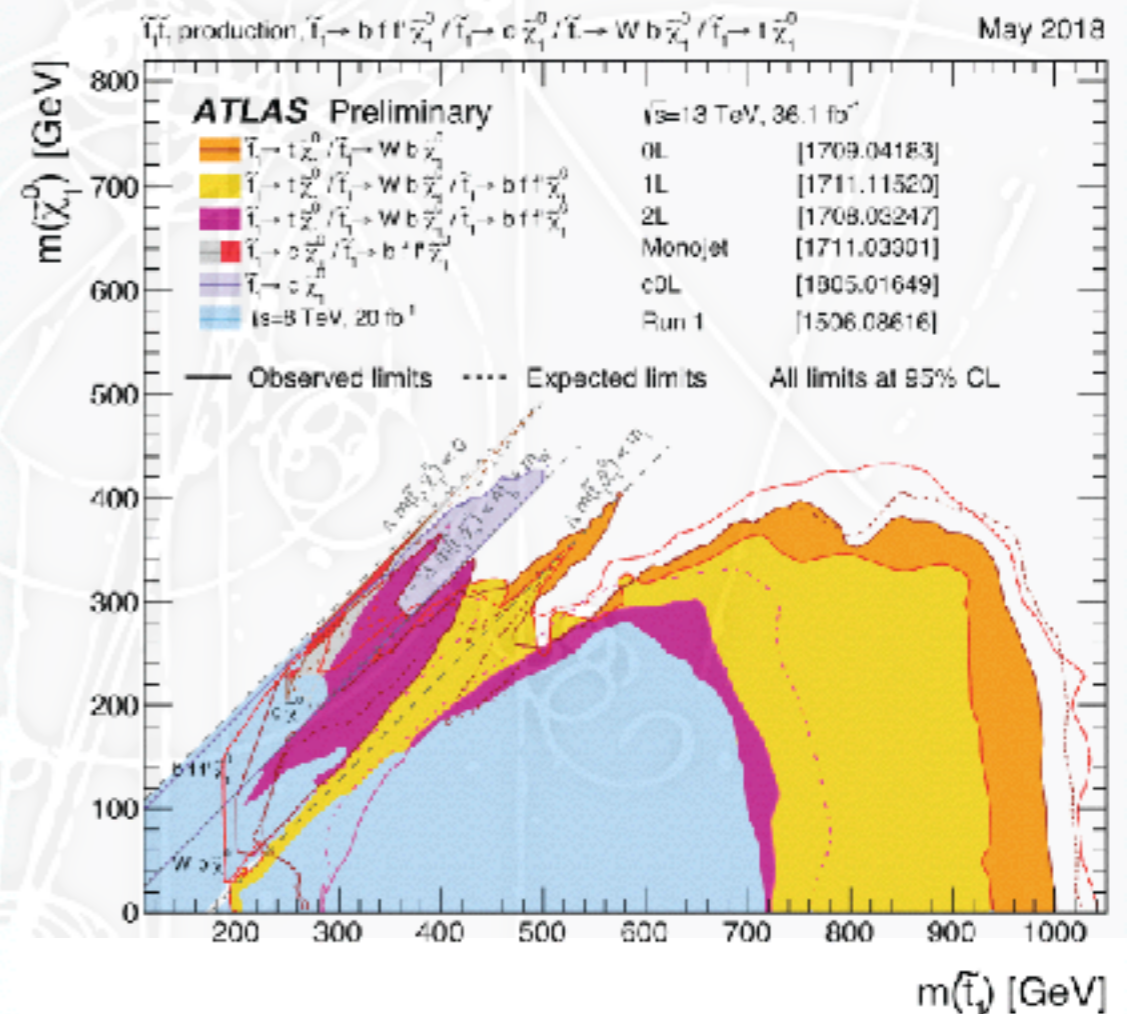
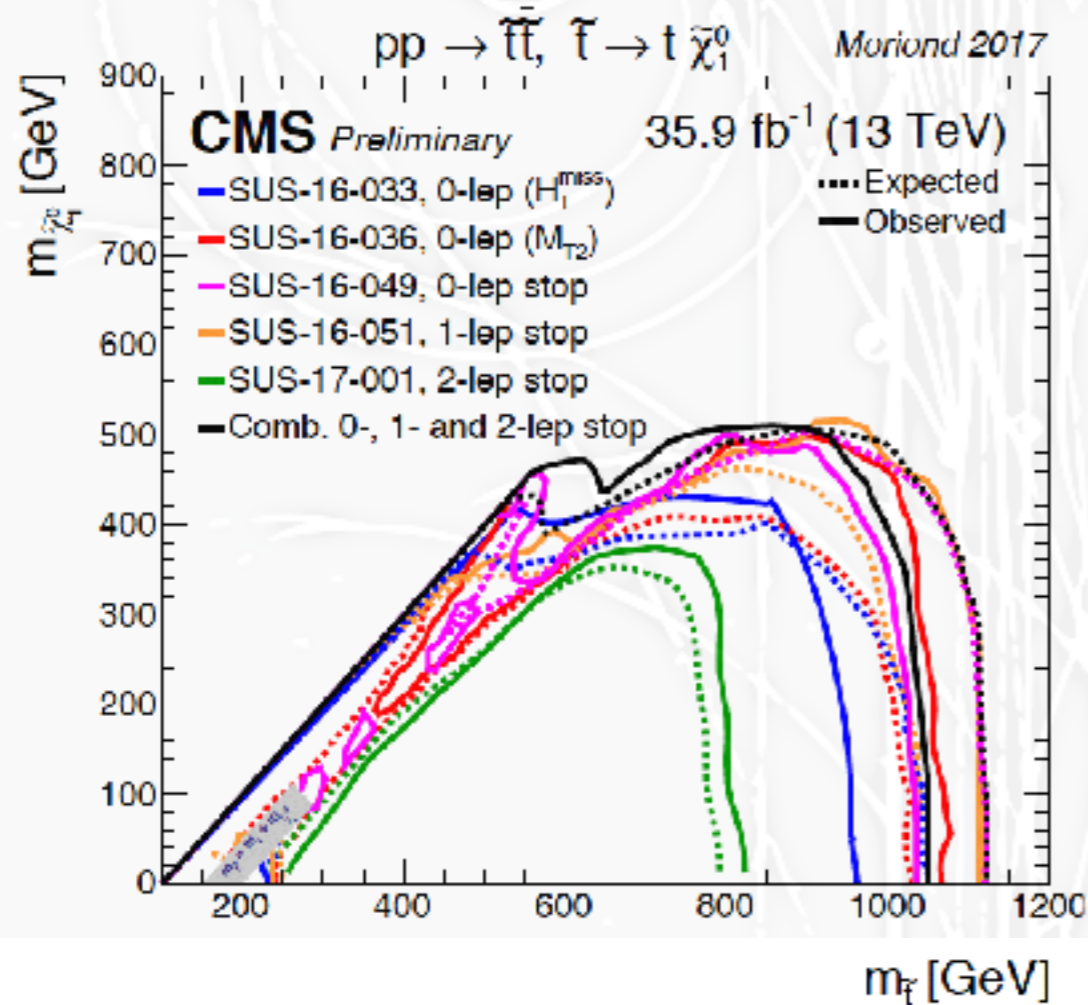
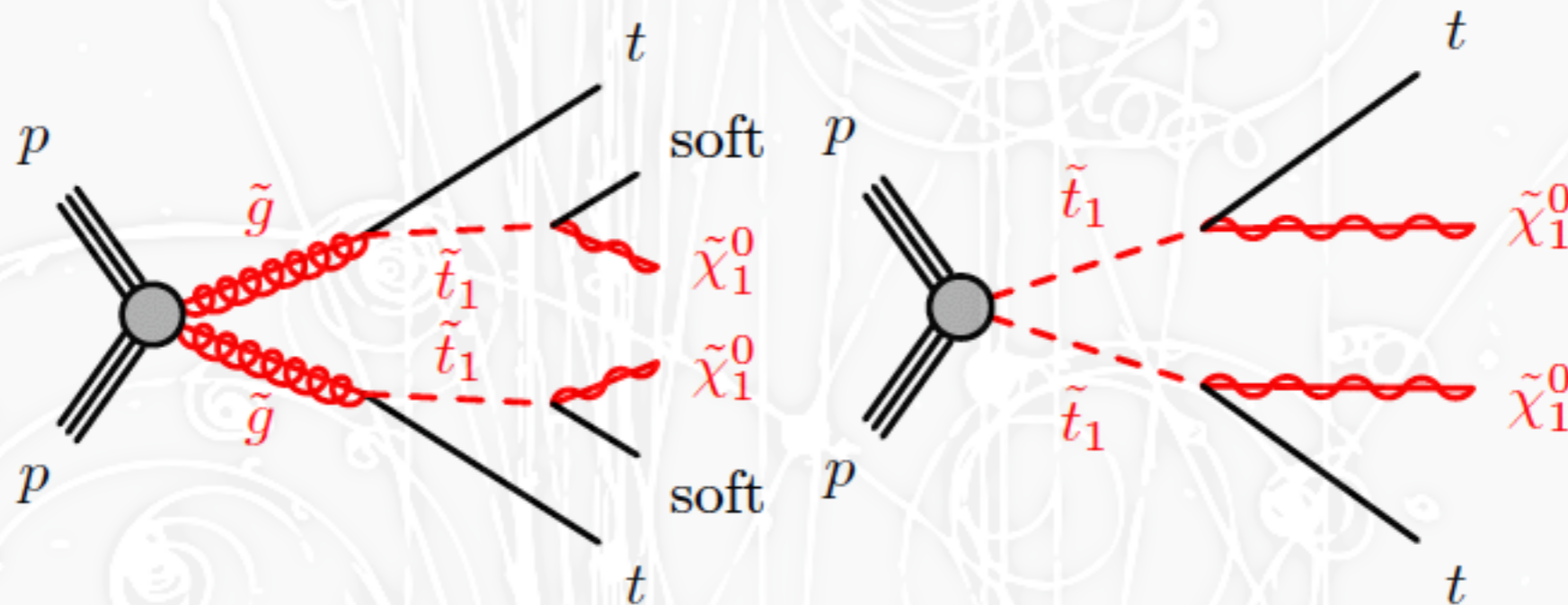
Supersymmetry:  
stop

Composite Higgs:  
Fermionic top partners  
(partial compositeness)

Higgs is a fundamental scalar,  
just like many other  
SUSY partners

Higgs is a composite resonance,  
just like many composite  
resonances in the theory of  
strong dynamics

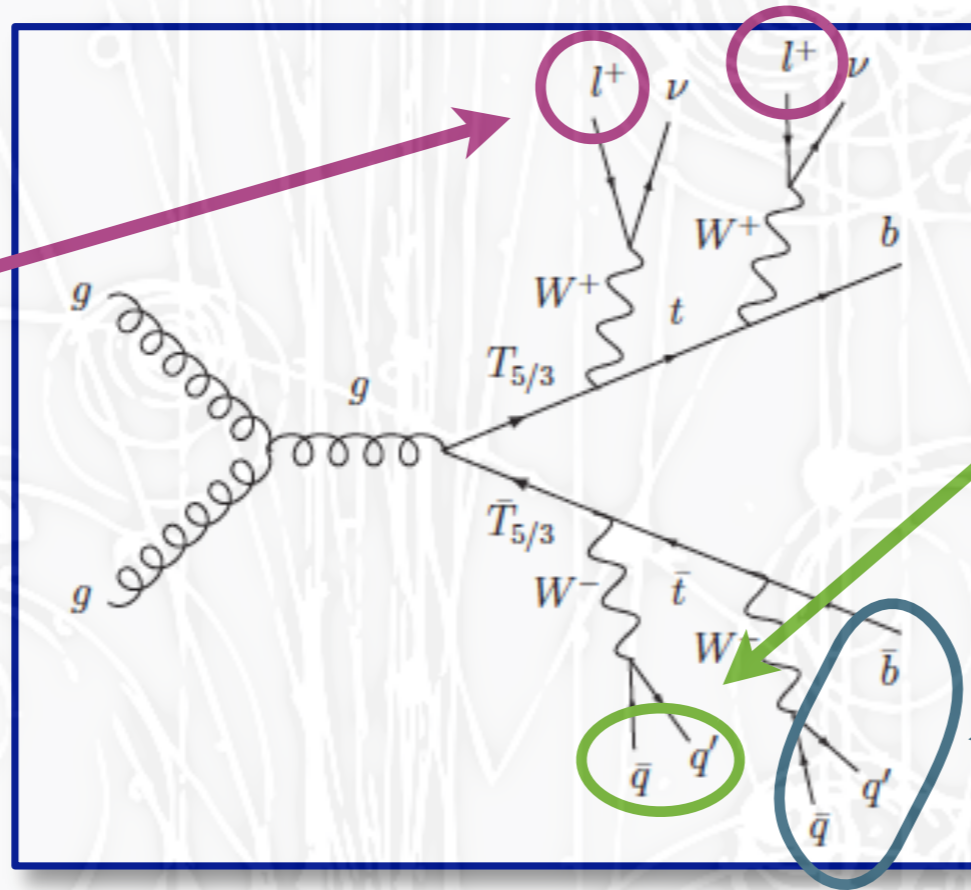
# SUSY top partner searches



# Composite Top Partner Searches

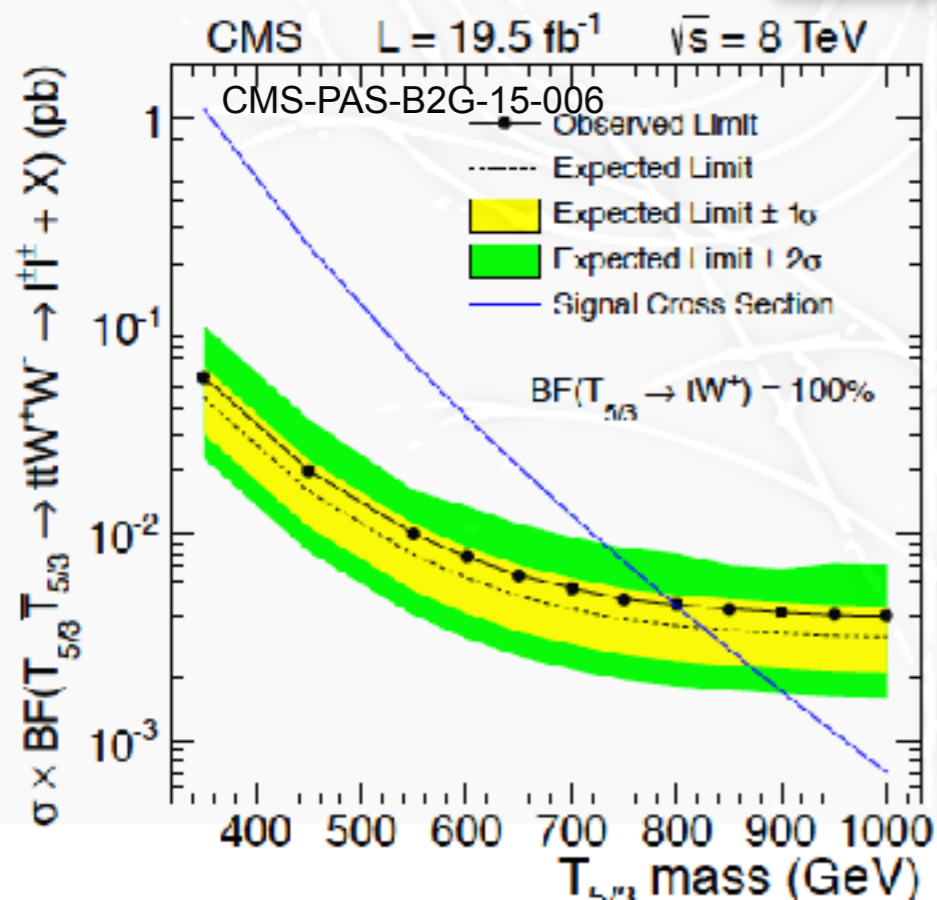
Simone, Matsedonski, Rattazzi, Wulzer '12  
 Azatov, Son, Spannowsky '13  
 Matsedonski, Panico, Wulzer '14

same-sign  
 dileptons



W tag:  
 2 subjects,  
 $M_j[60, 130]$

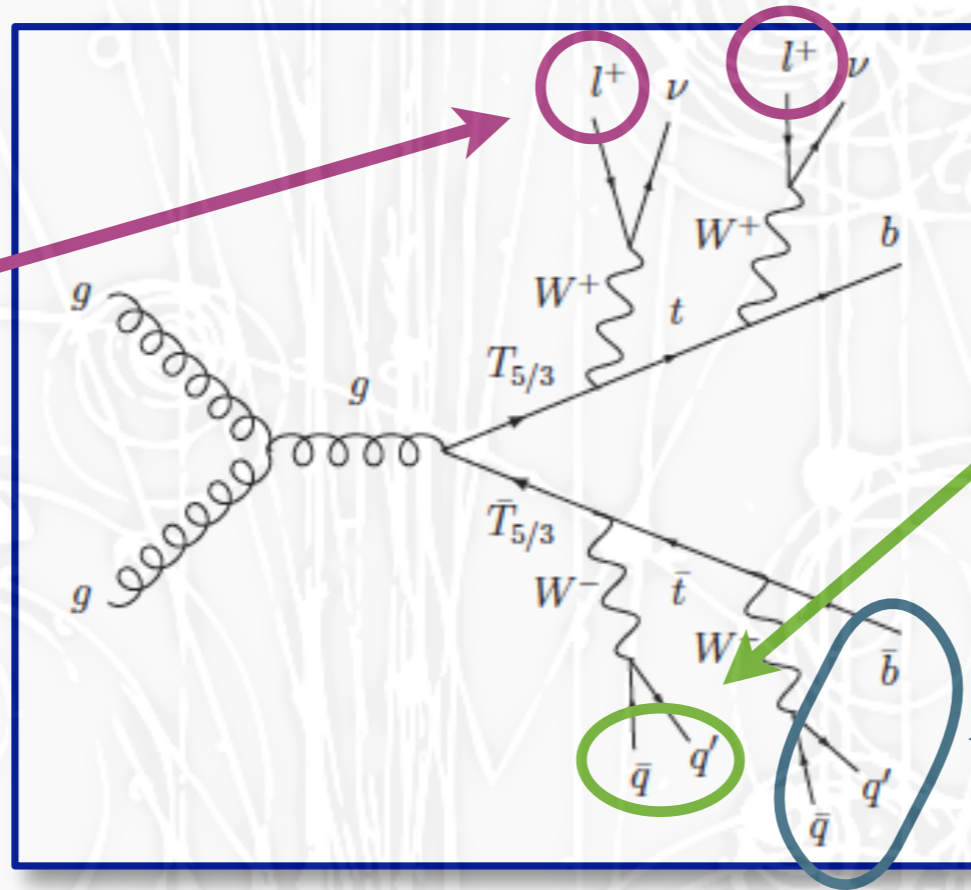
CMS top tag



# Composite Top Partner Searches

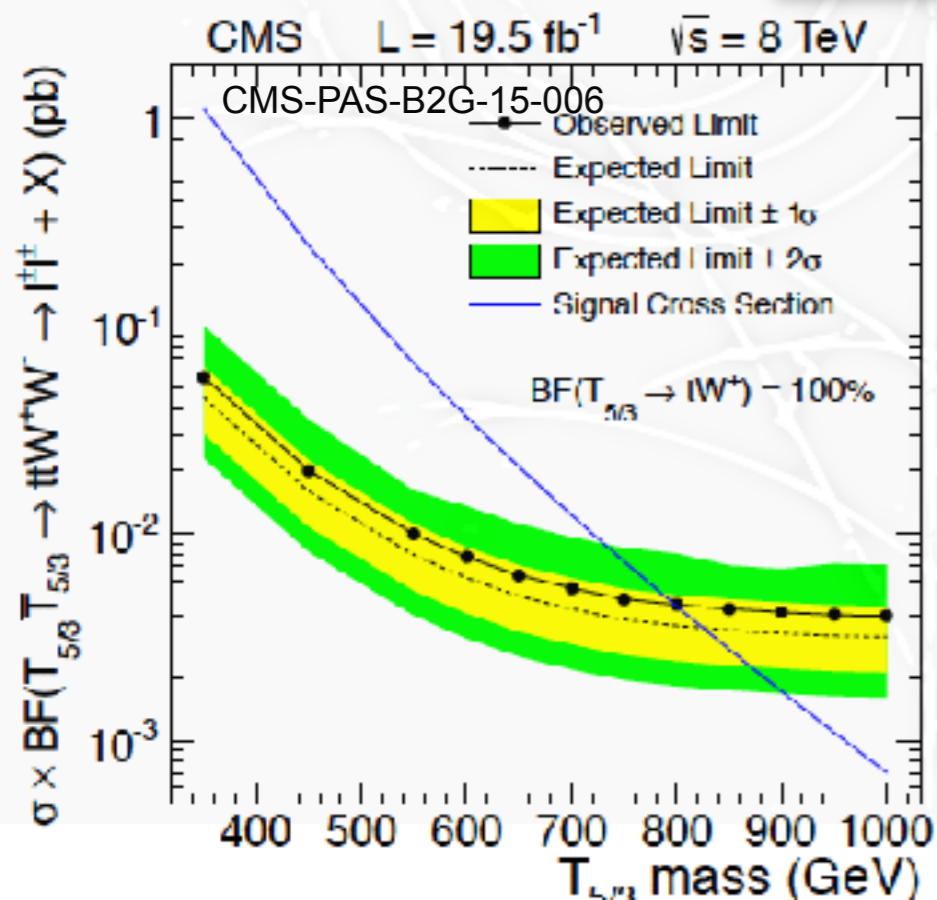
Simone, Matsedonski, Rattazzi, Wulzer `12  
 Azatov, Son, Spannowsky `13  
 Matsedonski, Panico, Wulzer `14

same-sign  
 dileptons



W tag:  
 2 subjects,  
 $M_j[60, 130]$

CMS top tag



Oblique parameter fits of LEP  
 & Tevatron data gave  
 $f \gtrsim 800 \text{ GeV}$

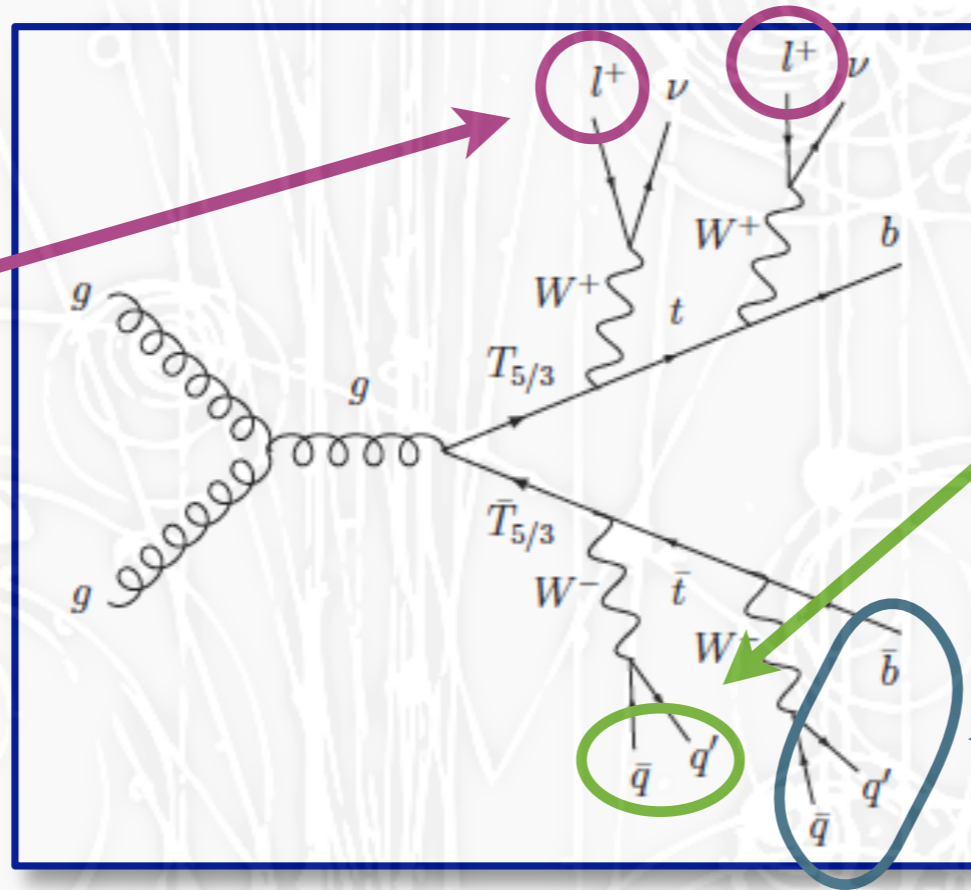
Grojean, Matsedonskyi, Panico `13

Ciuchini, Franco, Mishima,  
 Silvestrini `13

# Composite Top Partner Searches

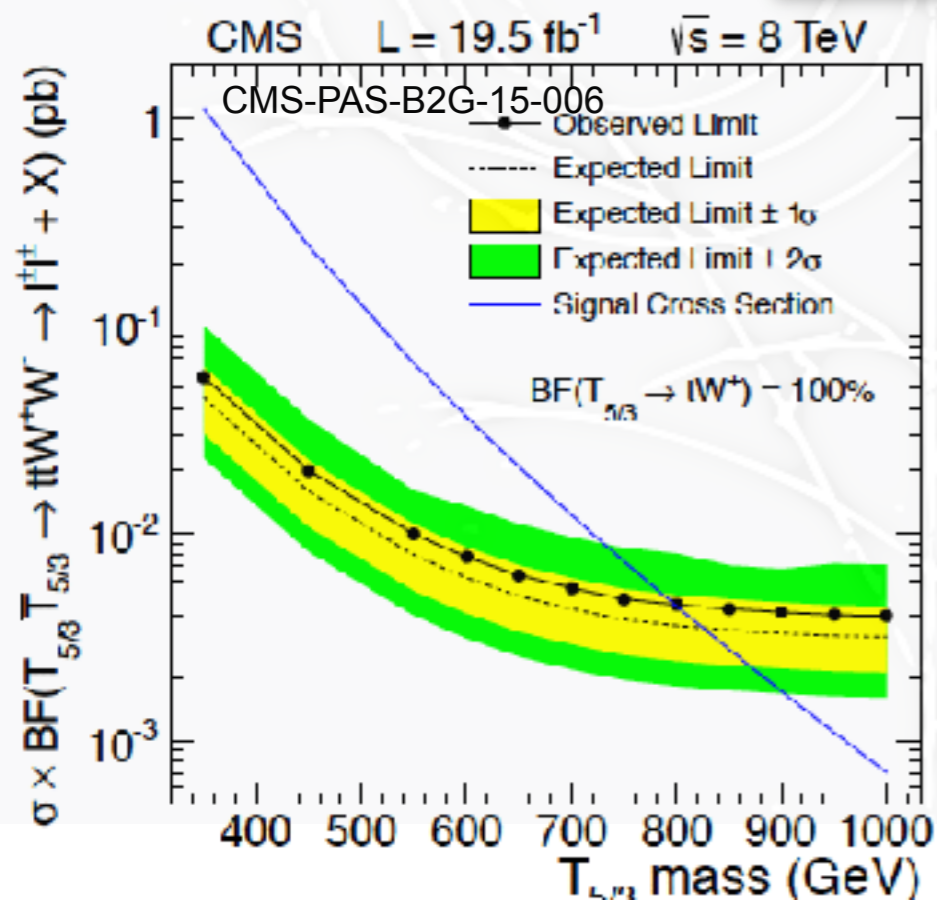
Simone, Matsedonski, Rattazzi, Wulzer '12  
 Azatov, Son, Spannowsky '13  
 Matsedonski, Panico, Wulzer '14

same-sign  
 dileptons



W tag:  
 2 subjects,  
 $M_j[60, 130]$

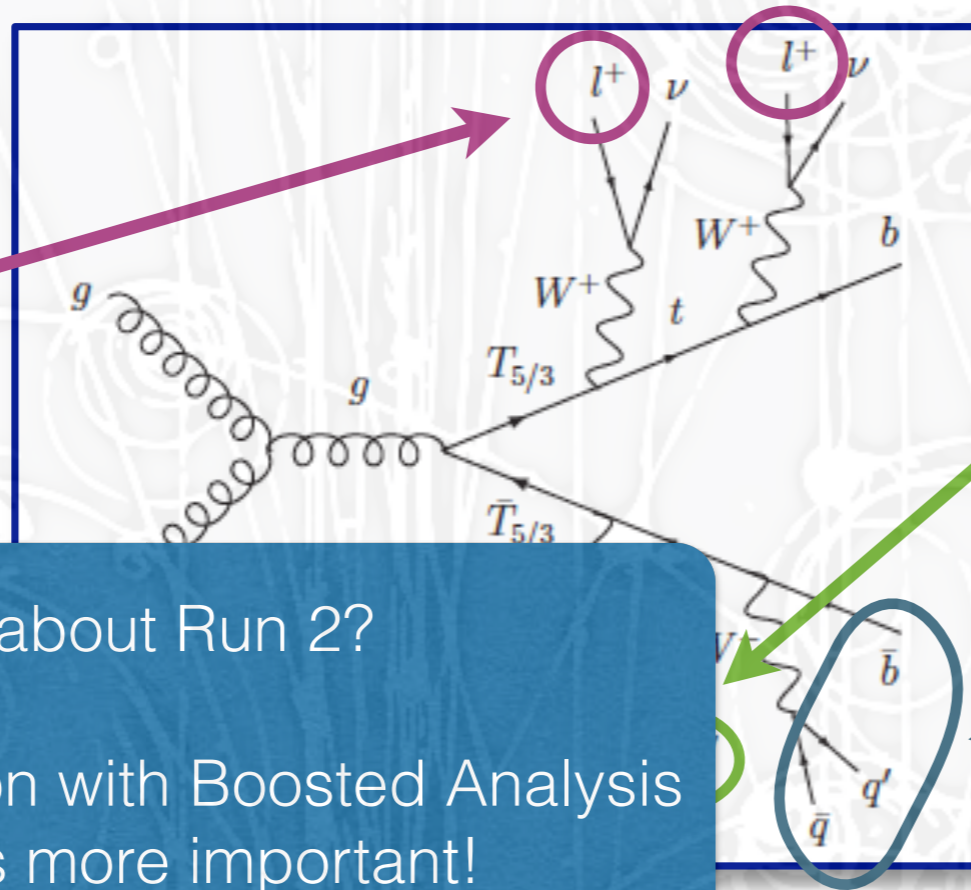
CMS top tag



# Composite Top Partner Searches

Simone, Matsedonski, Rattazzi, Wulzer `12  
 Azatov, Son, Spannowsky `13  
 Matsedonski, Panico, Wulzer `14

same-sign  
dileptons



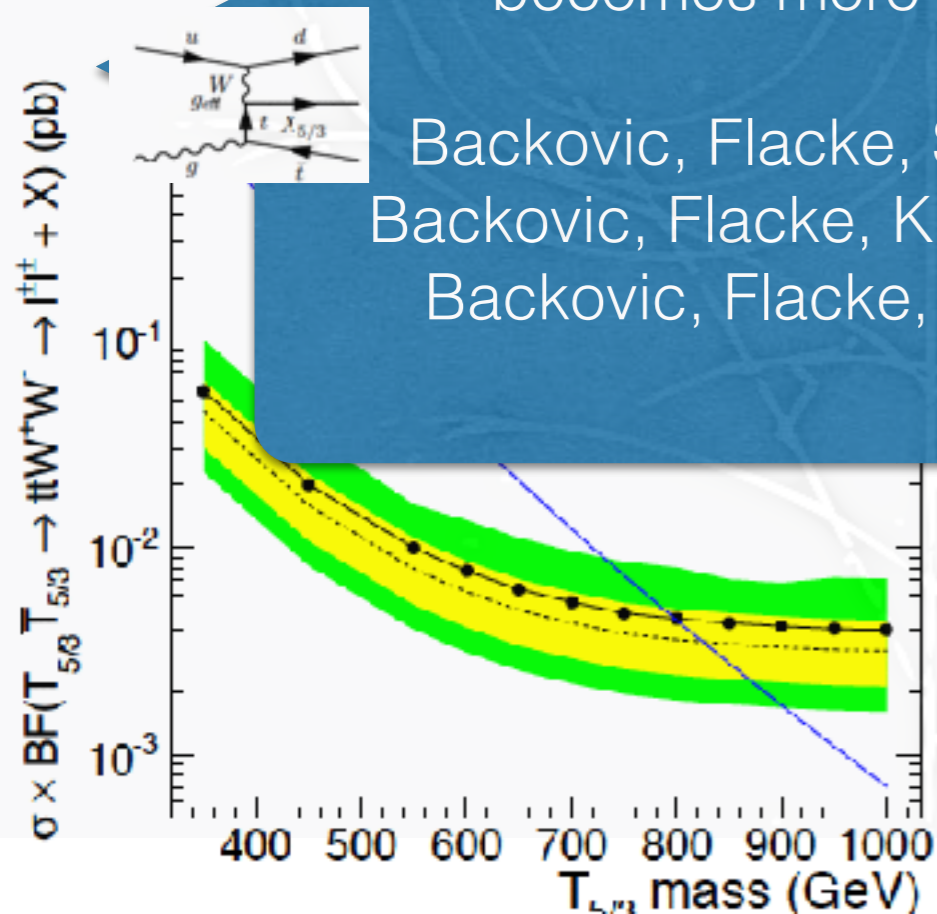
W tag:  
2 subjects,  
 $M_j[60, 130]$

CMS top tag

How about Run 2?

Single production with Boosted Analysis becomes more important!

Backovic, Flacke, SL, Perez `14  
 Backovic, Flacke, Kim, SL (x2), `15  
 Backovic, Flacke, Kim, SL, `16

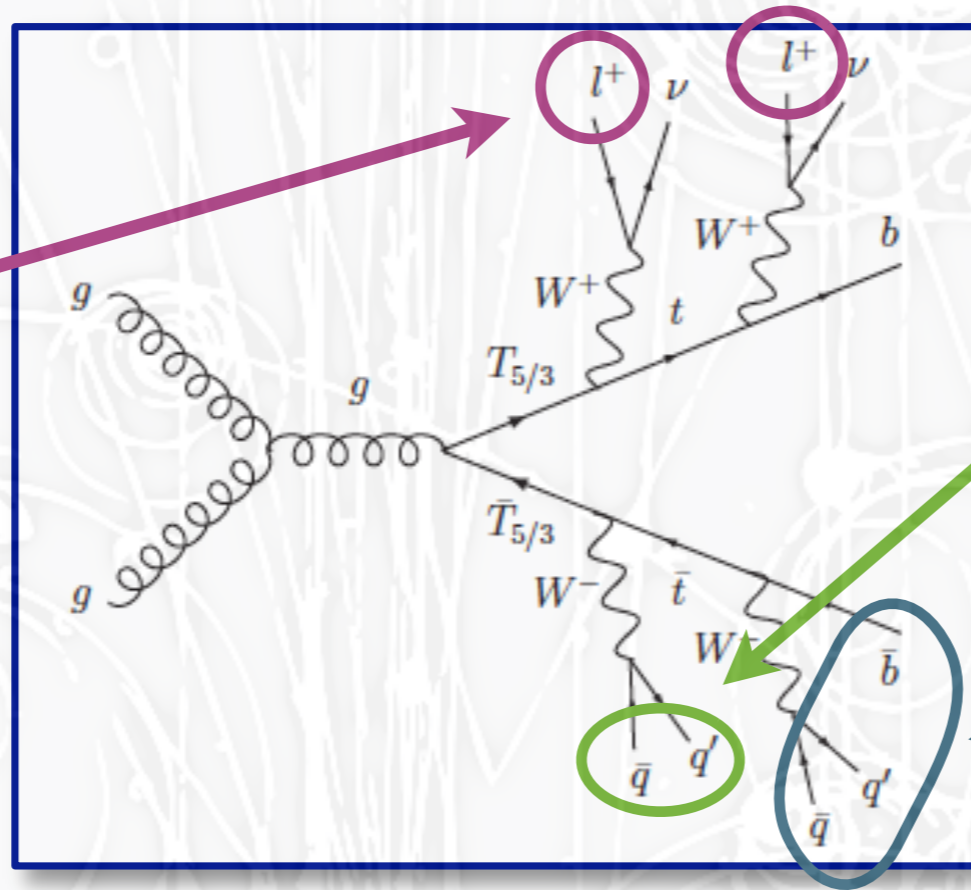




# Composite Top Partner Searches

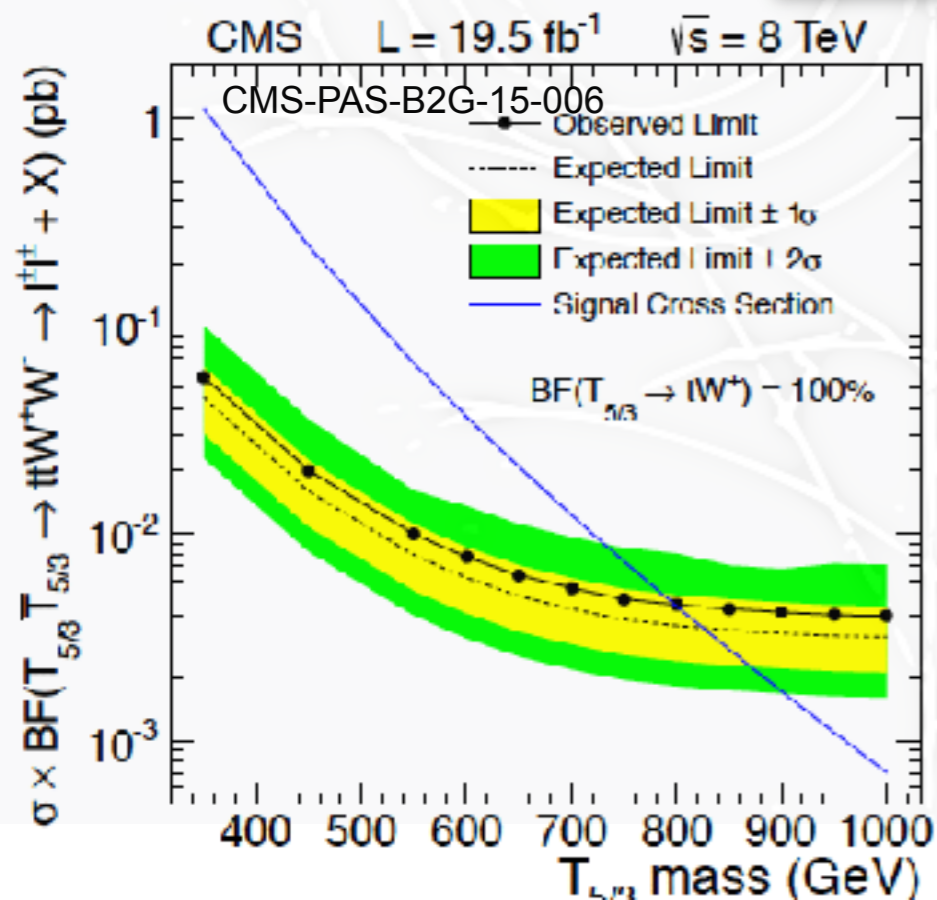
Simone, Matsedonski, Rattazzi, Wulzer `12  
 Azatov, Son, Spannowsky `13  
 Matsedonski, Panico, Wulzer `14

same-sign  
 dileptons



W tag:  
 2 subjects,  
 $M_j[60, 130]$

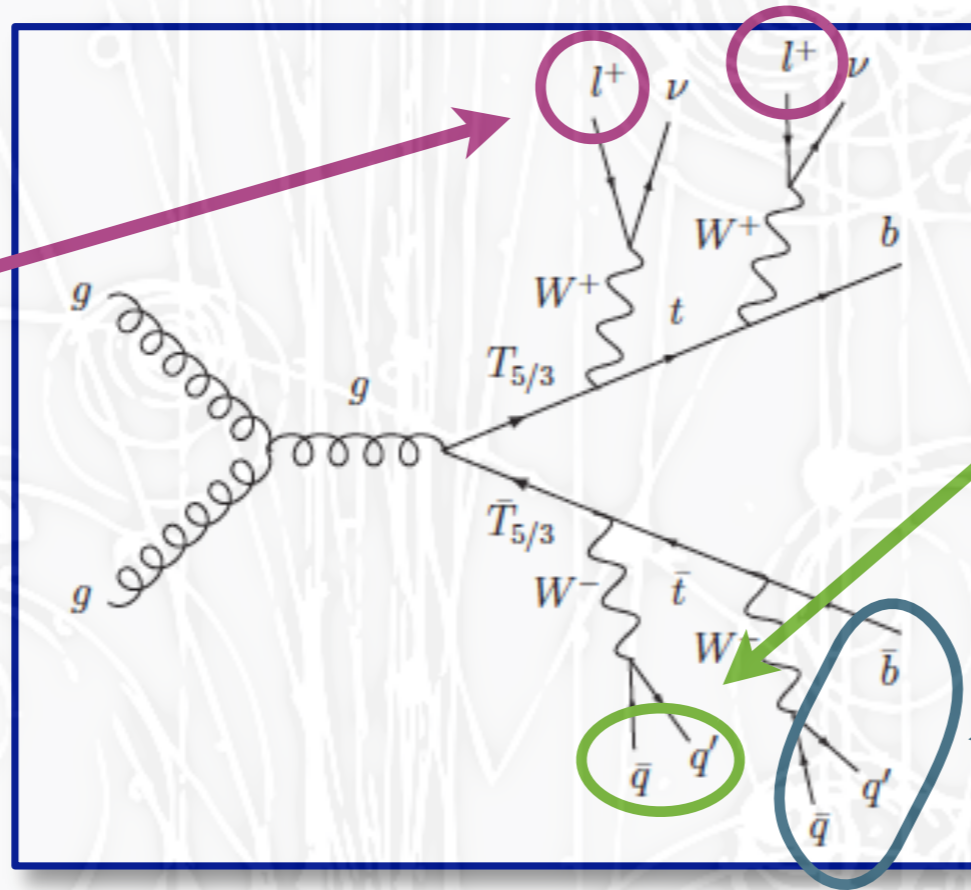
CMS top tag



# Composite Top Partner Searches

Simone, Matsedonski, Rattazzi, Wulzer '12  
 Azatov, Son, Spannowsky '13  
 Matsedonski, Panico, Wulzer '14

same-sign dileptons



W tag:  
 2 subjects,  
 $M_j[60, 130]$

CMS top tag

CMS  $\sqrt{s} = 13 \text{ TeV}$   $\mathcal{L} = 36.1 \text{ fb}^{-1}$

$TT \rightarrow bW+X$

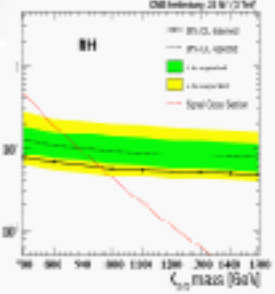
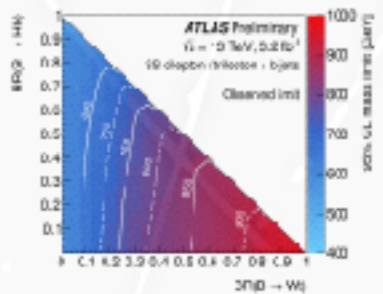
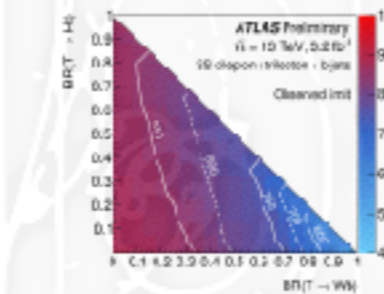
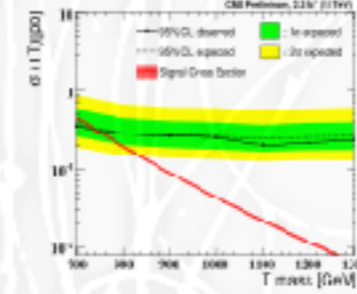
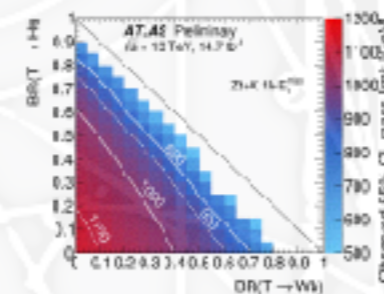
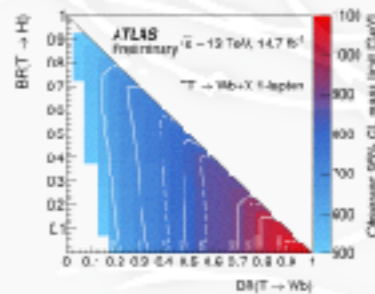
$TT \rightarrow tZ+X$

$TT (T \rightarrow tW, bZ, bH)$

$TT \rightarrow tH+X$

$BB \rightarrow tH+X$

$XX \rightarrow tWtW$



pair VLQ

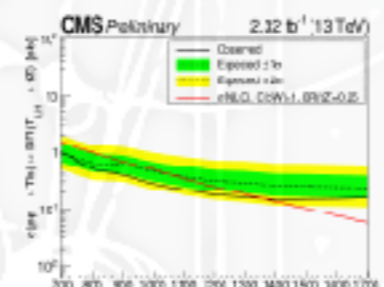
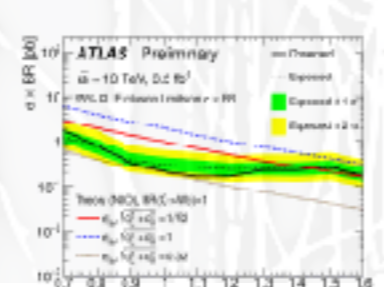
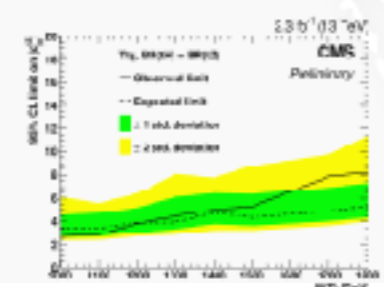
$T \rightarrow tH$

$T/Y \rightarrow bW$

$T \rightarrow tZ, B \rightarrow bZ$

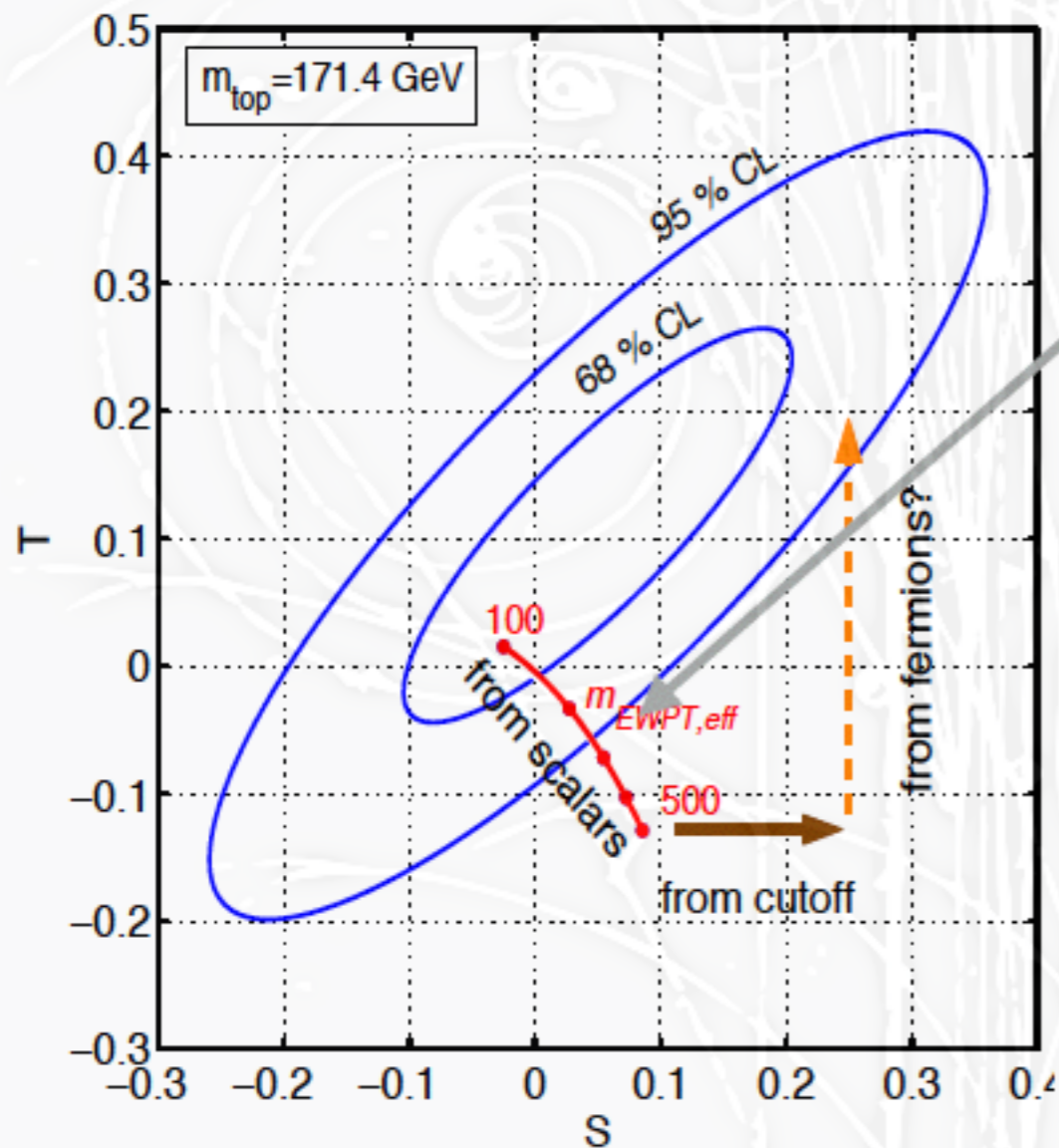
VLQ masses excluded up to:  
 - 1.4 TeV (100% BR  $T \rightarrow tH$ )  
 - 1.3 TeV (doublet)  
 $M(T_{5/3}) > 1.2 \text{ TeV}$  (95% CL)

single VLQ



$T_{5/3}$  mass (GeV)

# EWPT and Top Partners

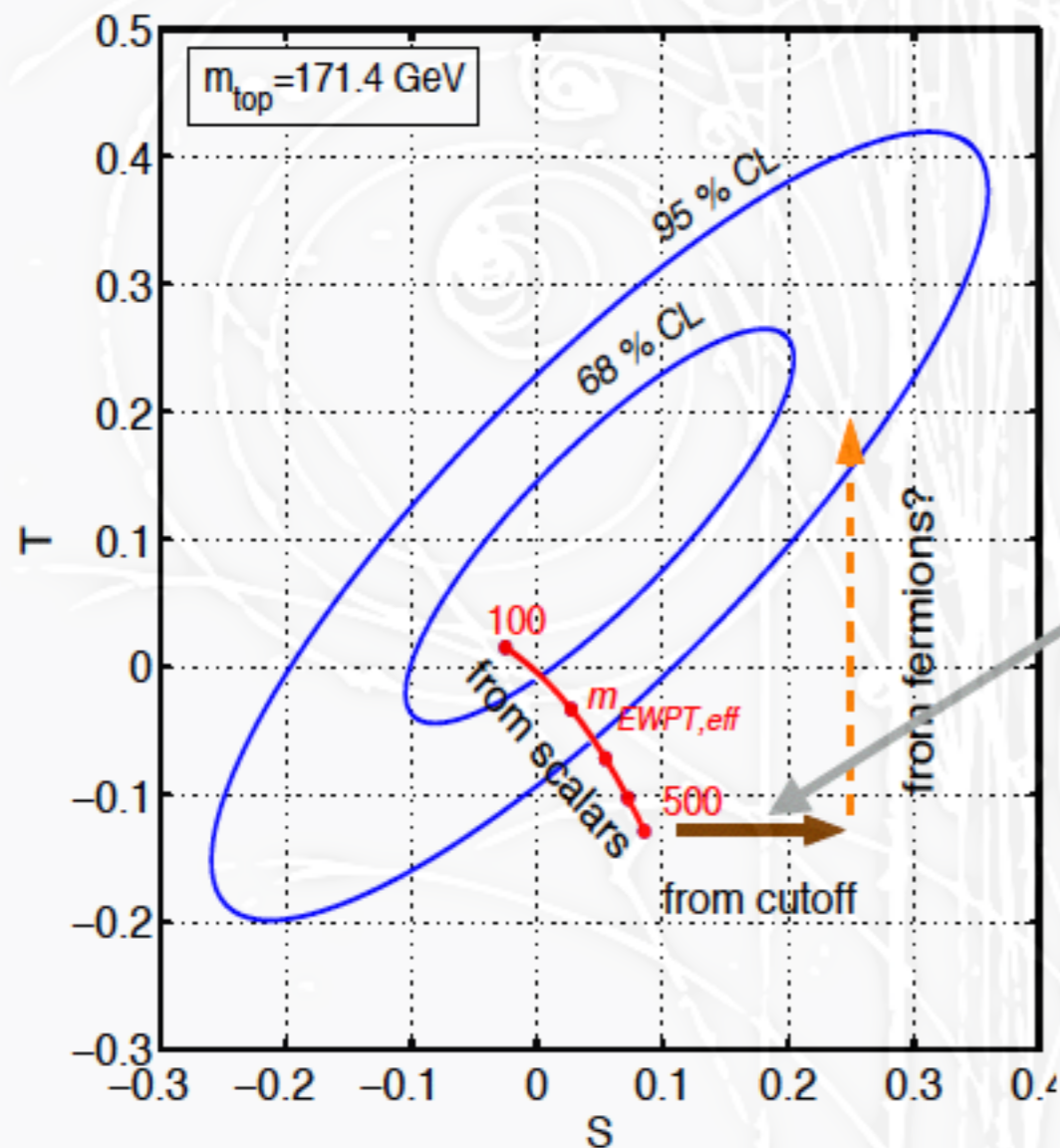


$$\Delta \hat{S} = \frac{g^2}{96\pi^2} \xi \log \left( \frac{8\pi m_W}{g m_h \sqrt{\xi}} \right)$$

$$\Delta \hat{T} = -\frac{3g'^2}{32\pi^2} \xi \log \left( \frac{8\pi m_W}{g m_h \sqrt{\xi}} \right)$$

Modified Higgs couplings go in bad direction.

# EWPT and Top Partners

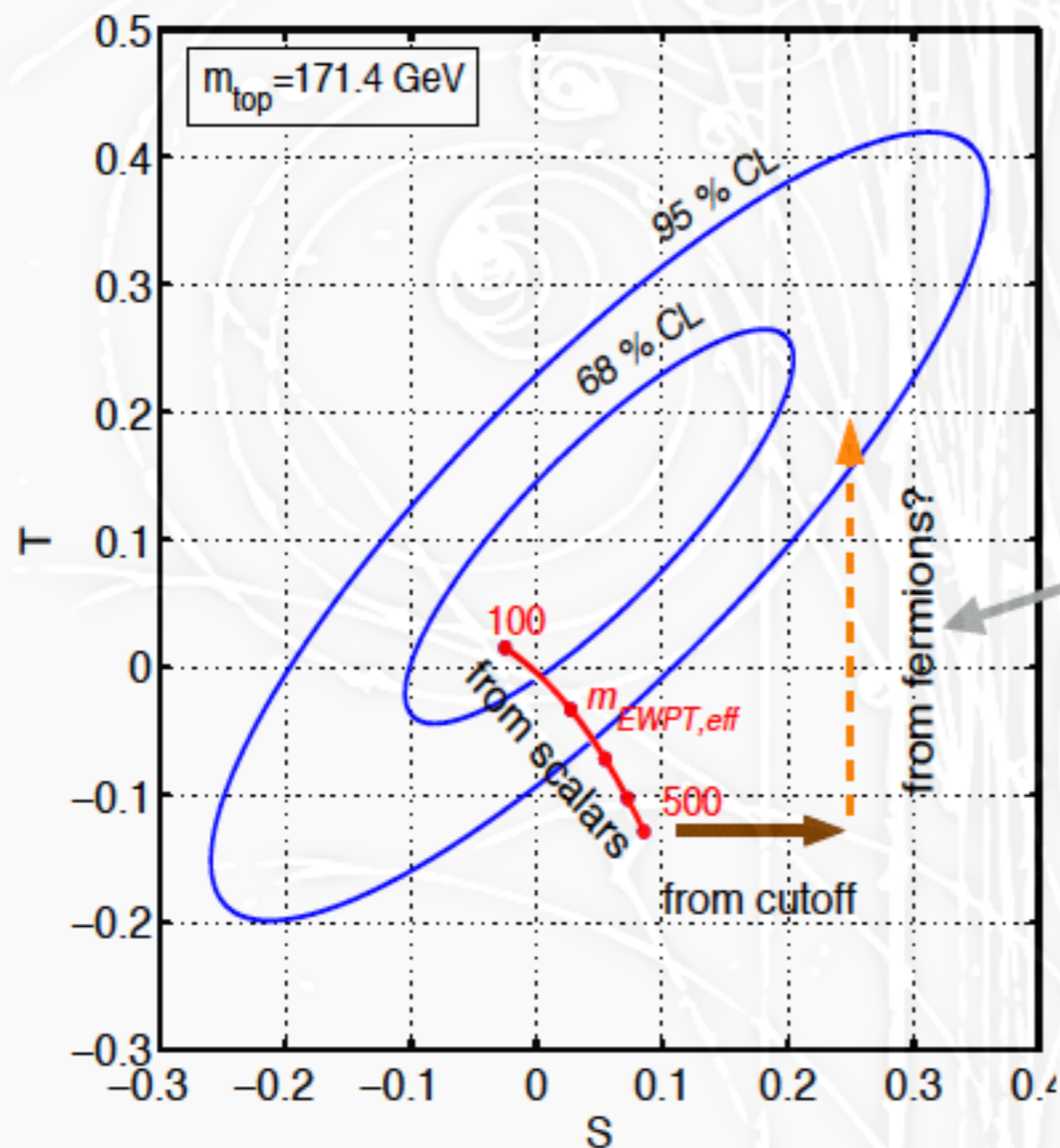


$$\Delta \hat{S} = \frac{g^2}{96\pi^2} \xi \log \left( \frac{8\pi m_W}{g m_h \sqrt{\xi}} \right) + \frac{m_W^2}{m_\rho^2}$$

$$\Delta \hat{T} = -\frac{3g'^2}{32\pi^2} \xi \log \left( \frac{8\pi m_W}{g m_h \sqrt{\xi}} \right)$$

Modified Higgs couplings go in bad direction.  
Resonance exchange as well

# EWPT and Top Partners



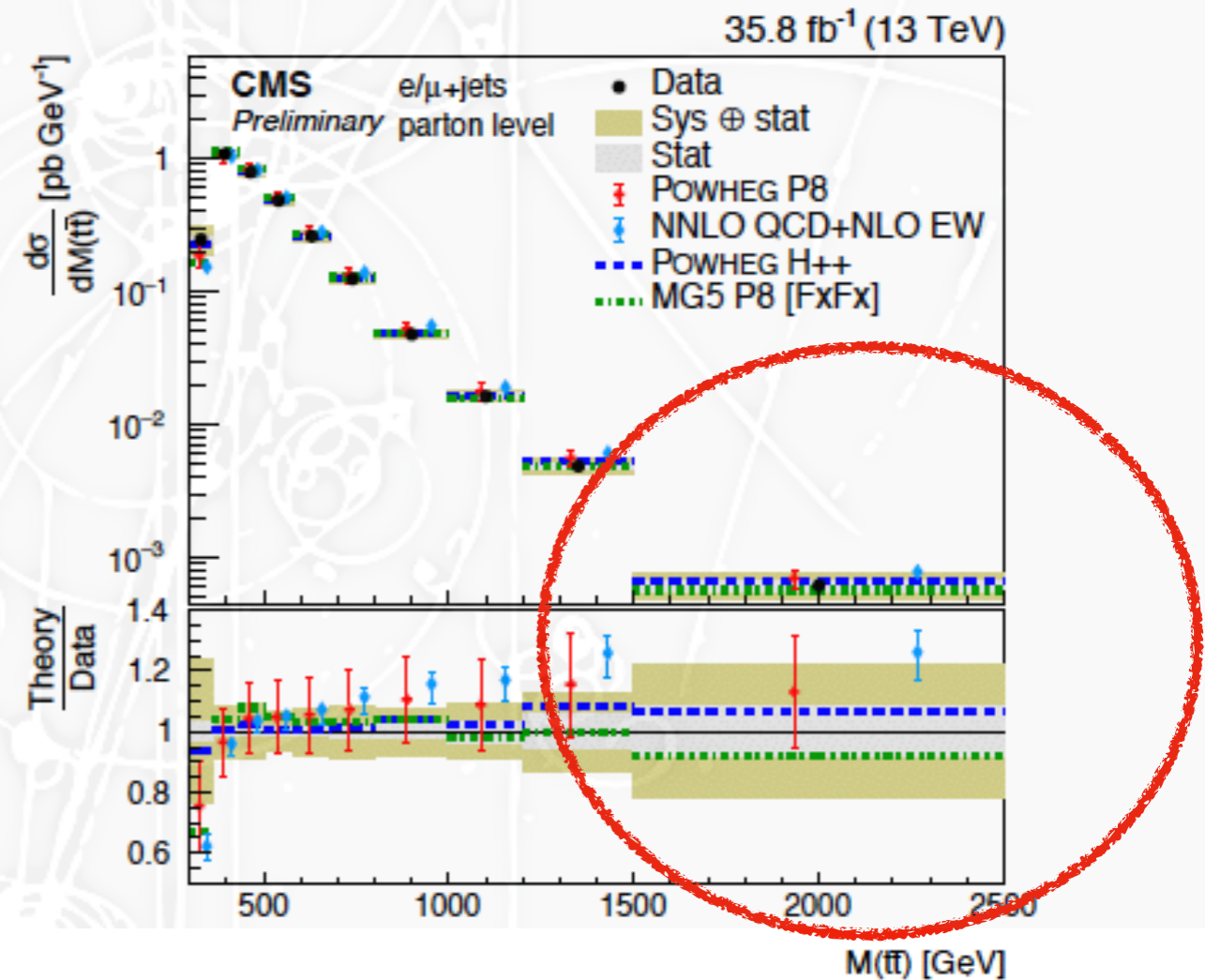
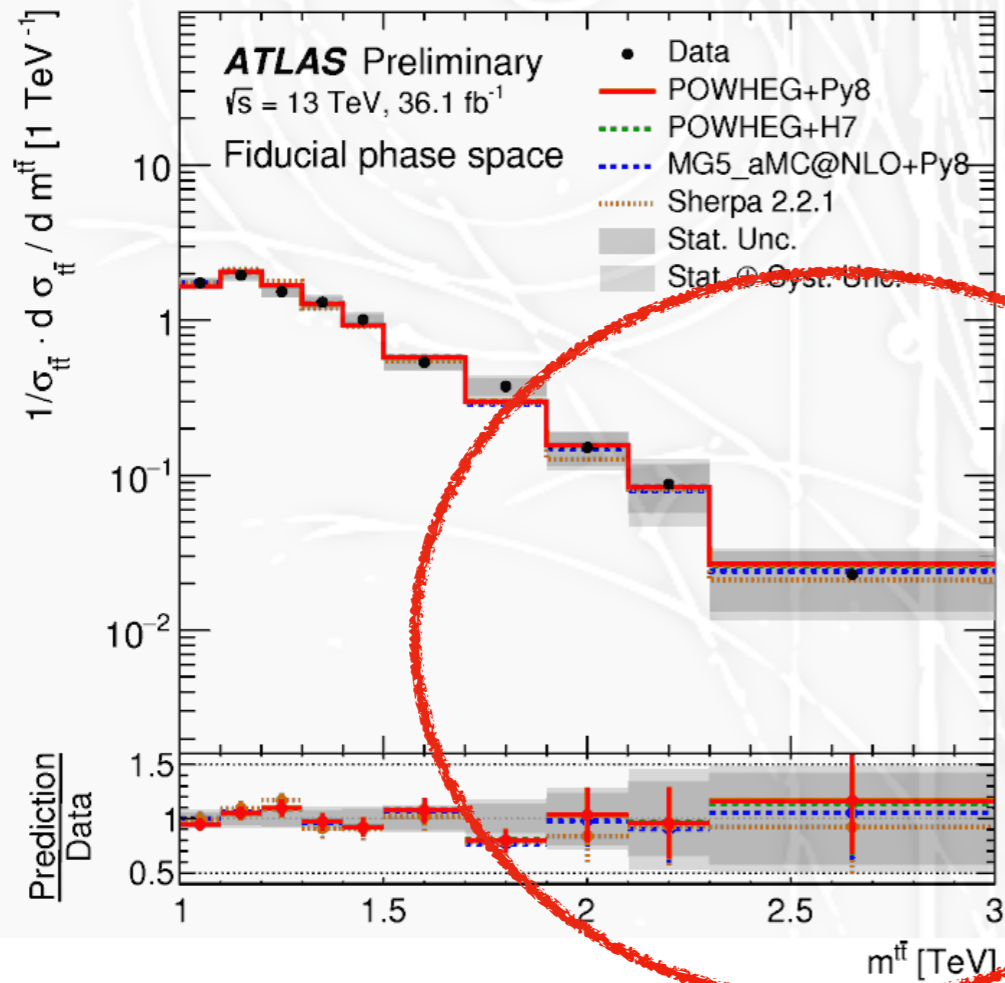
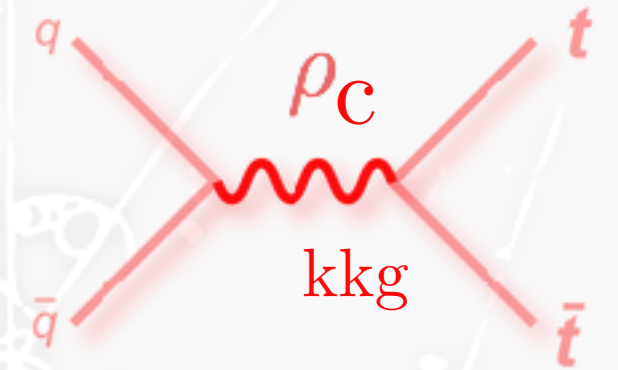
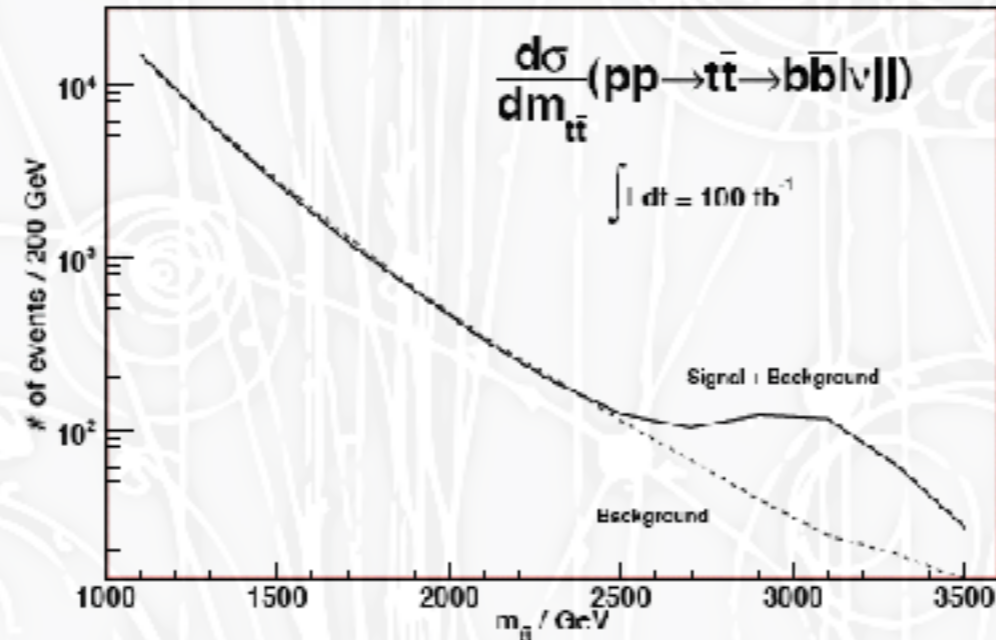
$$\Delta\hat{S} = \frac{g^2}{96\pi^2}\xi \log\left(\frac{8\pi m_W}{gm_h\sqrt{\xi}}\right) + \frac{m_W^2}{m_\rho^2} + \alpha\frac{g^2}{16\pi^2}\xi,$$

$$\Delta\hat{T} = -\frac{3g'^2}{32\pi^2}\xi \log\left(\frac{8\pi m_W}{gm_h\sqrt{\xi}}\right) + \beta\frac{3y_t}{16\pi^2}\xi,$$

Modified Higgs couplings go in bad direction.  
 Resonance exchange as well  
 Light Top Partners come to rescue.

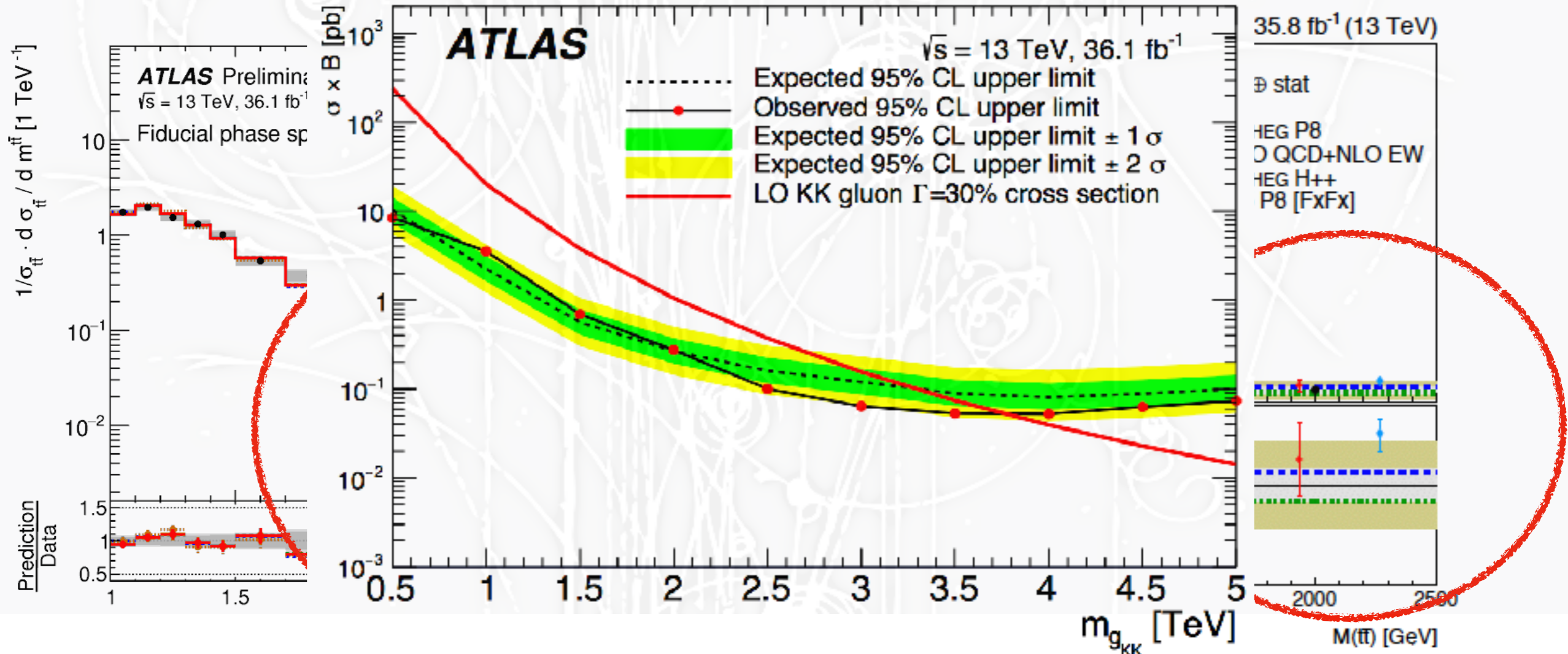
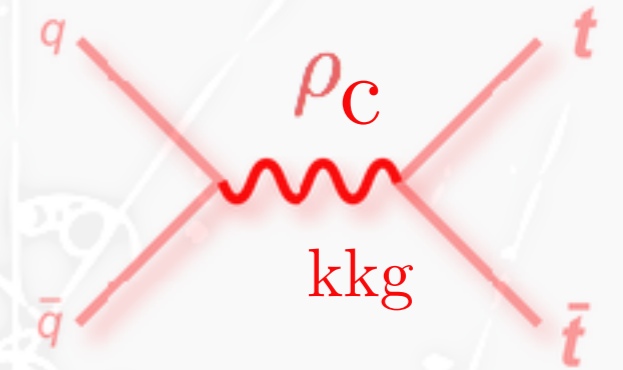
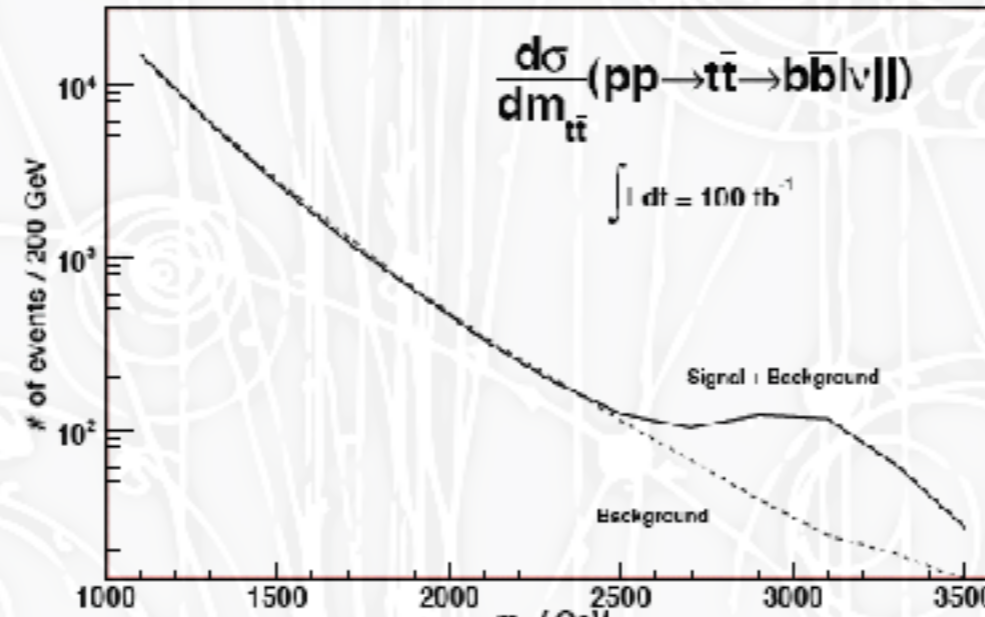
# No Resonance, No New Physics? Naturalness?

$$M_{KKG} = 3 \text{ TeV}$$

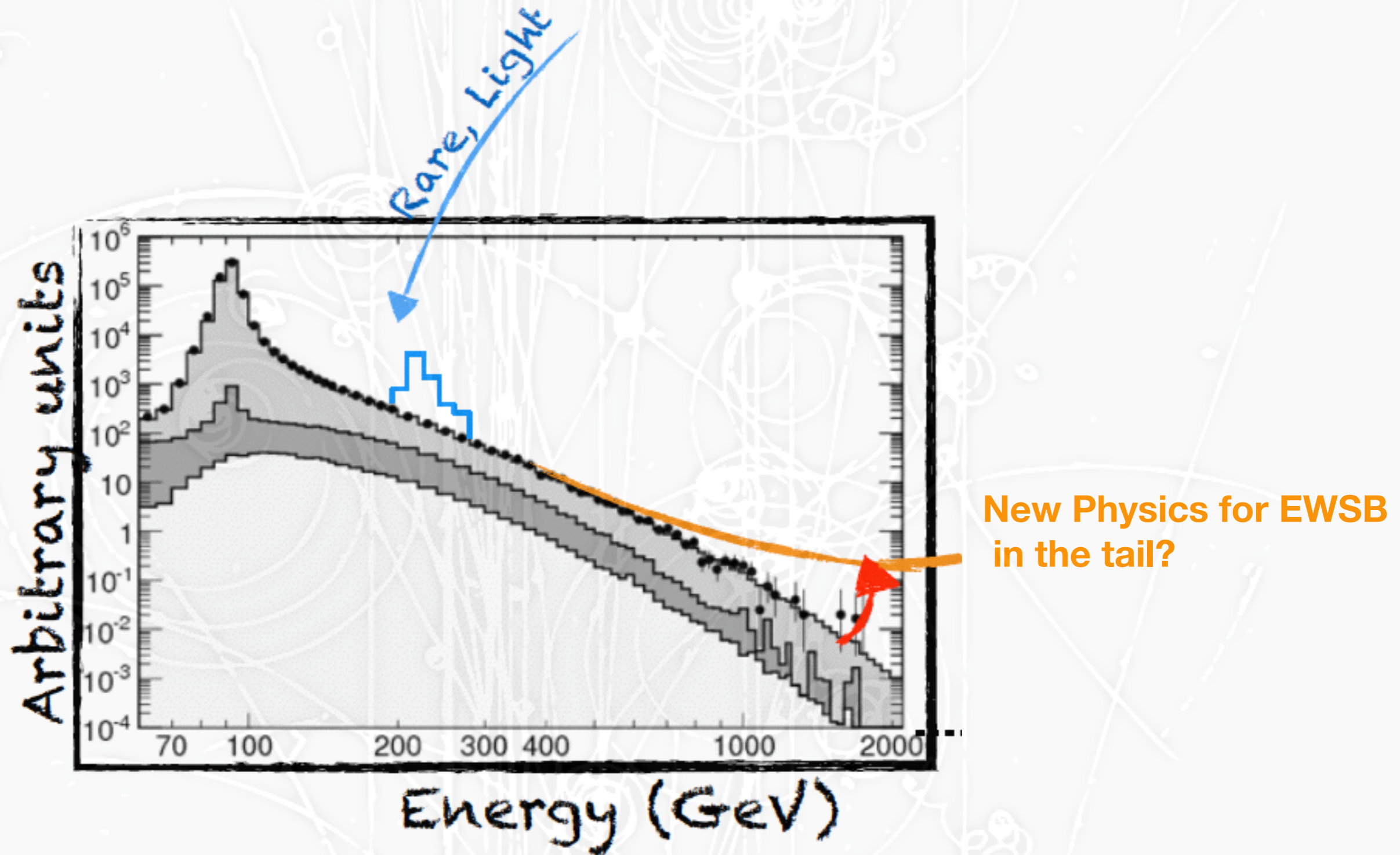


# No Resonance, No New Physics? Naturalness?

$$M_{KKG} = 3 \text{ TeV}$$



# No Resonance, No New Physics? Naturalness?



*picture adapted from Francesco Riva*



# No Resonance, No New Physics? Naturalness?

---

- ◆ **New Physics may appear solely as a continuum**
  - approximately conformal sector (i.e. CFT broken by IR cutoff)
  - multi-particle states with strong dynamics (branch cut at  $4m_\pi^2$  in  $\pi\pi \rightarrow \pi\pi$  scattering)

# No Resonance, No New Physics? Naturalness?

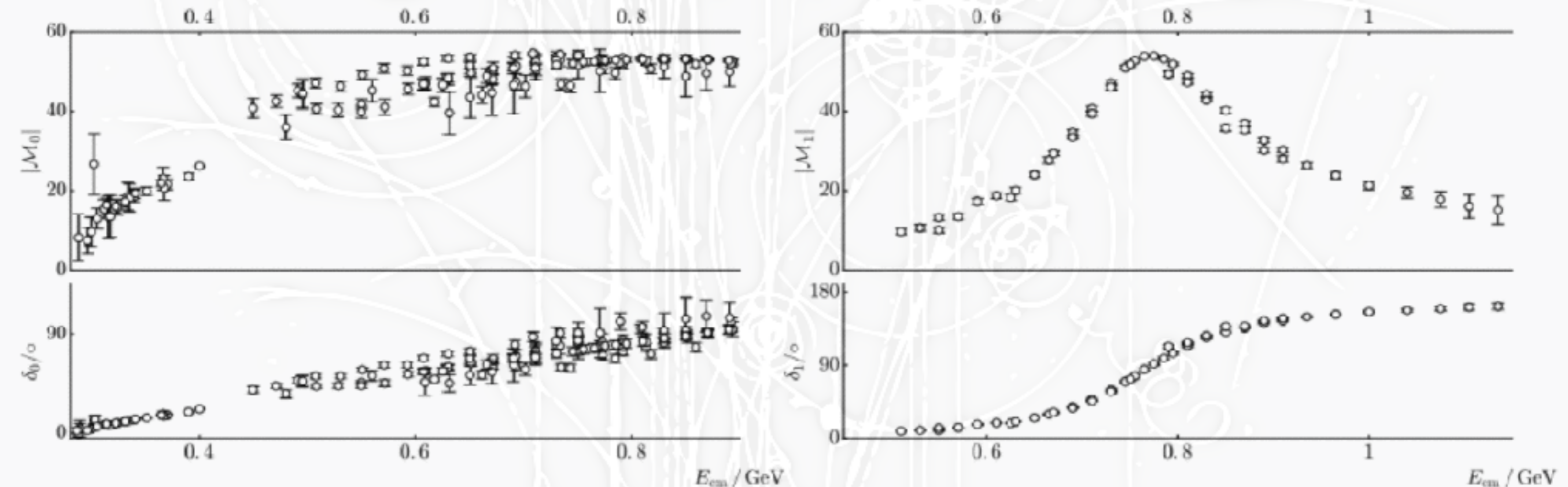
## ◆ New Physics may appear solely as a continuum

- approximately conformal sector (i.e. CFT broken by IR cutoff)
- multi-particle states with strong dynamics (branch cut at  $4m_\pi^2$  in  $\pi\pi \rightarrow \pi\pi$  scattering)

QCD

$\sigma / f_0(500)$

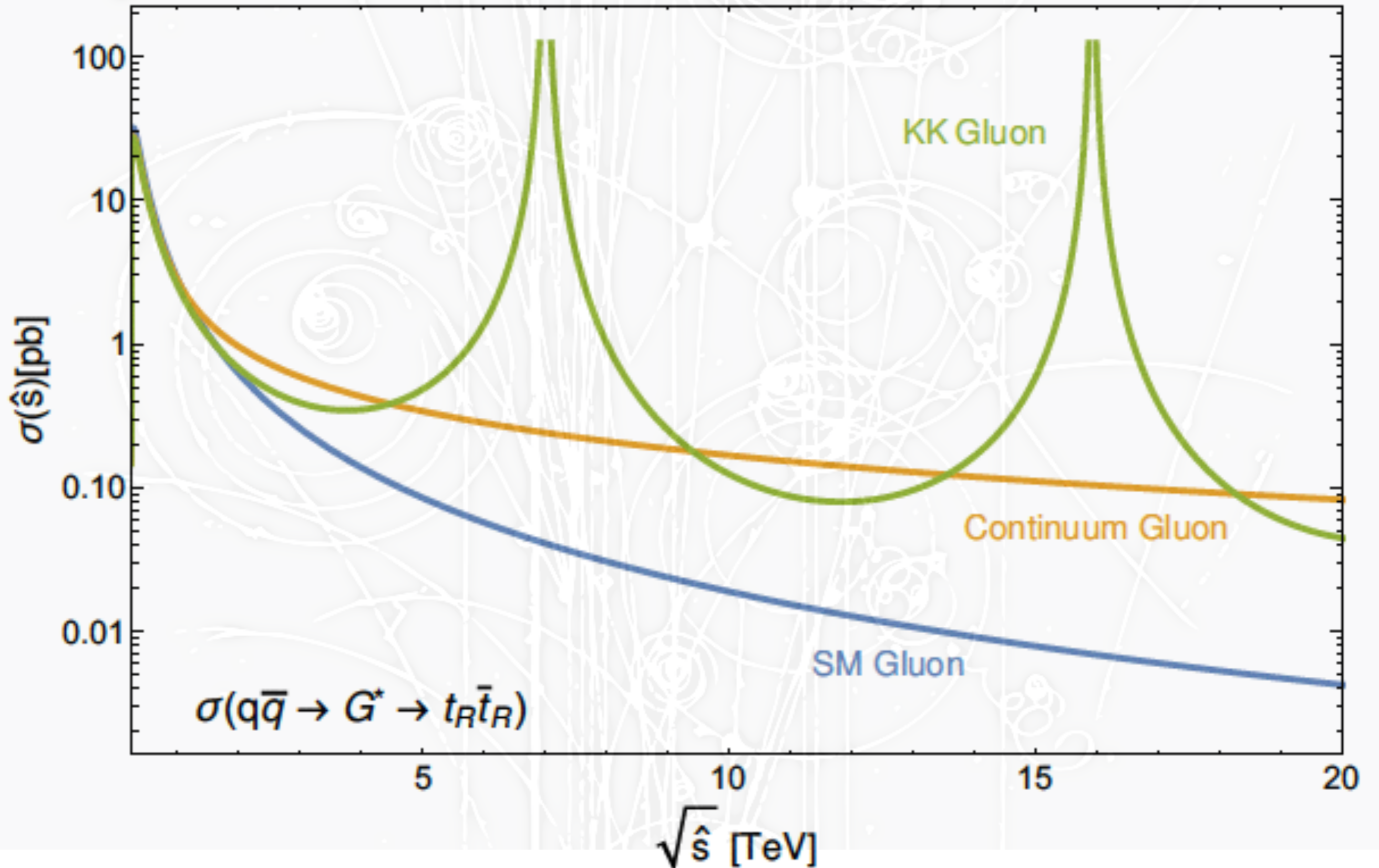
$\rho$



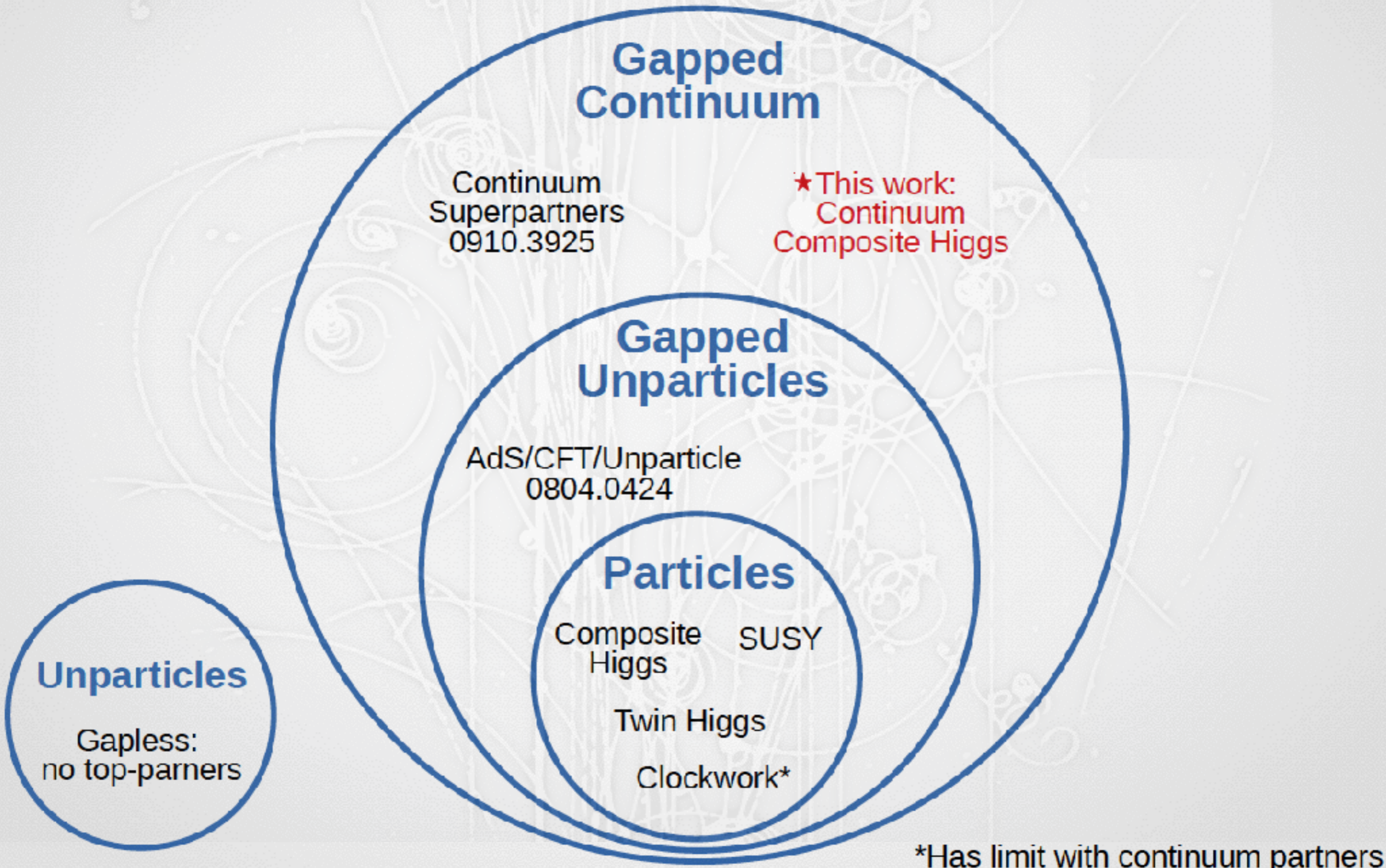
$M_\sigma = 450$  MeV  $\Gamma_\sigma = 550$  MeV

$M_\rho = 770$  MeV  $\Gamma_\rho = 145$  MeV

# No Resonance, No New Physics? Naturalness?



# Short Outline



# Continuum Top Partners

Csaki, Lombardo, Lee, SL, Telem

◆ MCHM (Agashe, Contino, Pomarol)  $\Rightarrow$  continuum version

- elementary fields which mix with the composite operators and the

form factors:  $\mathcal{L}_{\text{top}} = \bar{t}_L \not{p} \Pi_L(p) t_L + \bar{t}_R \not{p} \Pi_R(p) t_R + \bar{t}_L M(p) t_R + h.c.$

- 2-point function  $\langle tt \rangle$  is given by

$$-i\Pi_t(p) = \frac{1}{\not{p} - \frac{M(p)}{\sqrt{\Pi_L(p)\Pi_R(p)}}} \stackrel{\text{Källén-Lehmann}}{=} \int dm^2 \frac{\not{p} + m}{p^2 - m^2} \rho_t(m^2)$$

# Continuum Top Partners

Csaki, Lombardo, Lee, SL, Telem

◆ MCHM (Agashe, Contino, Pomarol)  $\Rightarrow$  continuum version

- elementary fields which mix with the composite operators and the

form factors:  $\mathcal{L}_{\text{top}} = \bar{t}_L \not{p} \Pi_L(p) t_L + \bar{t}_R \not{p} \Pi_R(p) t_R + \bar{t}_L M(p) t_R + h.c.$

- 2-point function  $\langle tt \rangle$  is given by

$$-i\Pi_t(p) = \frac{1}{\not{p} - \frac{M(p)}{\sqrt{\Pi_L(p)\Pi_R(p)}}} \stackrel{\text{Källén-Lehmann}}{=} \int dm^2 \frac{\not{p} + m}{p^2 - m^2} \rho_t(m^2)$$

- non-local effective action:

$$S_{\text{eff}} = \int d^4x d^4y \bar{\psi}(x) (i\not{\partial}_y - m) \Sigma(x - y) \psi(y)$$

# Continuum Top Partners

Csaki, Lombardo, Lee, SL, Telem

◆ MCHM (Agashe, Contino, Pomarol)  $\Rightarrow$  continuum version

- elementary fields which mix with the composite operators and the

form factors:  $\mathcal{L}_{\text{top}} = \bar{t}_L \not{p} \Pi_L(p) t_L + \bar{t}_R \not{p} \Pi_R(p) t_R + \bar{t}_L M(p) t_R + h.c.$

- 2-point function  $\langle tt \rangle$  is given by

$$-i\Pi_t(p) = \frac{1}{\not{p} - \frac{M(p)}{\sqrt{\Pi_L(p)\Pi_R(p)}}} \stackrel{\text{Källén-Lehmann}}{=} \int dm^2 \frac{\not{p} + m}{p^2 - m^2} \rho_t(m^2)$$

- non-local effective action:

$$S_{\text{eff}} = \int d^4x d^4y \bar{\psi}(x) (i\not{\partial}_y - m) \Sigma(x - y) \psi(y)$$

- gauge invariant way:

$$S_{\text{eff}} = \int \frac{d^4p d^4k}{(2\pi)^8} \bar{\psi}(k) (\not{p} - m) \Sigma(p^2) F(k - p, p)$$

$$\rho_h = \frac{1}{\pi} \text{Im} \Sigma^{-1}$$

$$F(x, y) = \mathcal{P} \exp \left( -igT^a \int_x^y A^a \cdot dw \right) \psi(y)$$

# Particle Without Particle

---

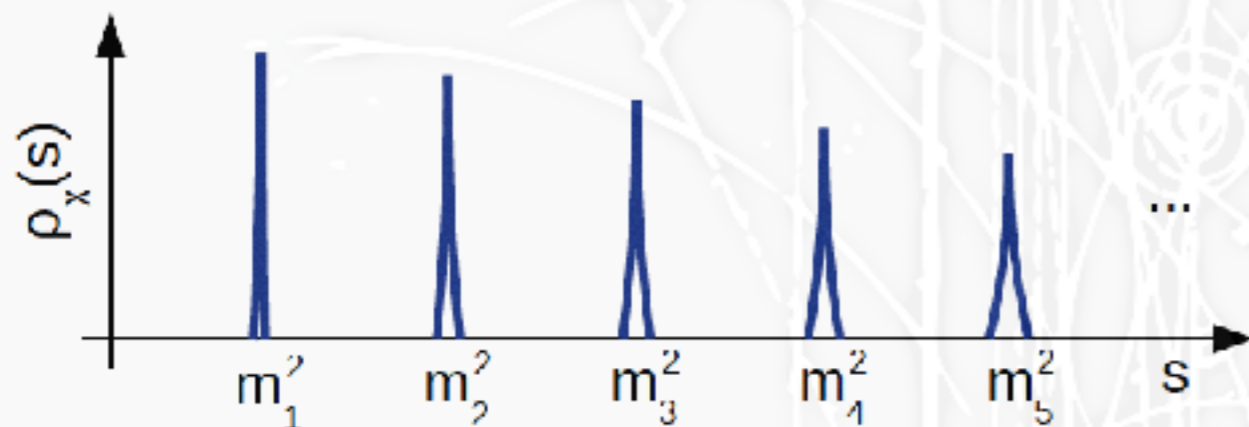
- ◆ **New Physics may appear solely as a continuum**
  - If the new strong dynamics responsible for furnishing a composite Higgs is near a **quantum critical point**, the composite spectrum may effectively consist of a continuum with a mass gap.
  - Idea: they may not be ordinary particles but form a continuum with a mass gap (similar to gapless unparticles like Terning et al. - also used gapped for SUSY)



# Particle Without Particle

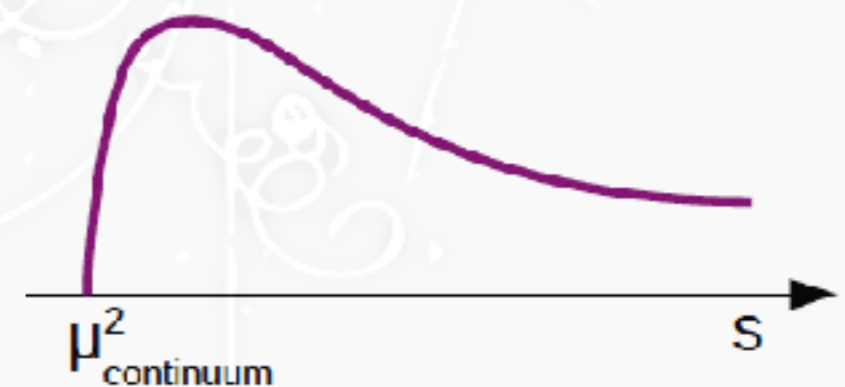
## ◆ New Physics may appear solely as a continuum

- If the new strong dynamics responsible for furnishing a composite Higgs is near a **quantum critical point**, the composite spectrum may effectively consist of a continuum with a mass gap.
- Idea: they may not be ordinary particles but form a continuum with a mass gap (similar to gapless unparticles like Terning et al. - also used gapped for SUSY)



Ordinary composites

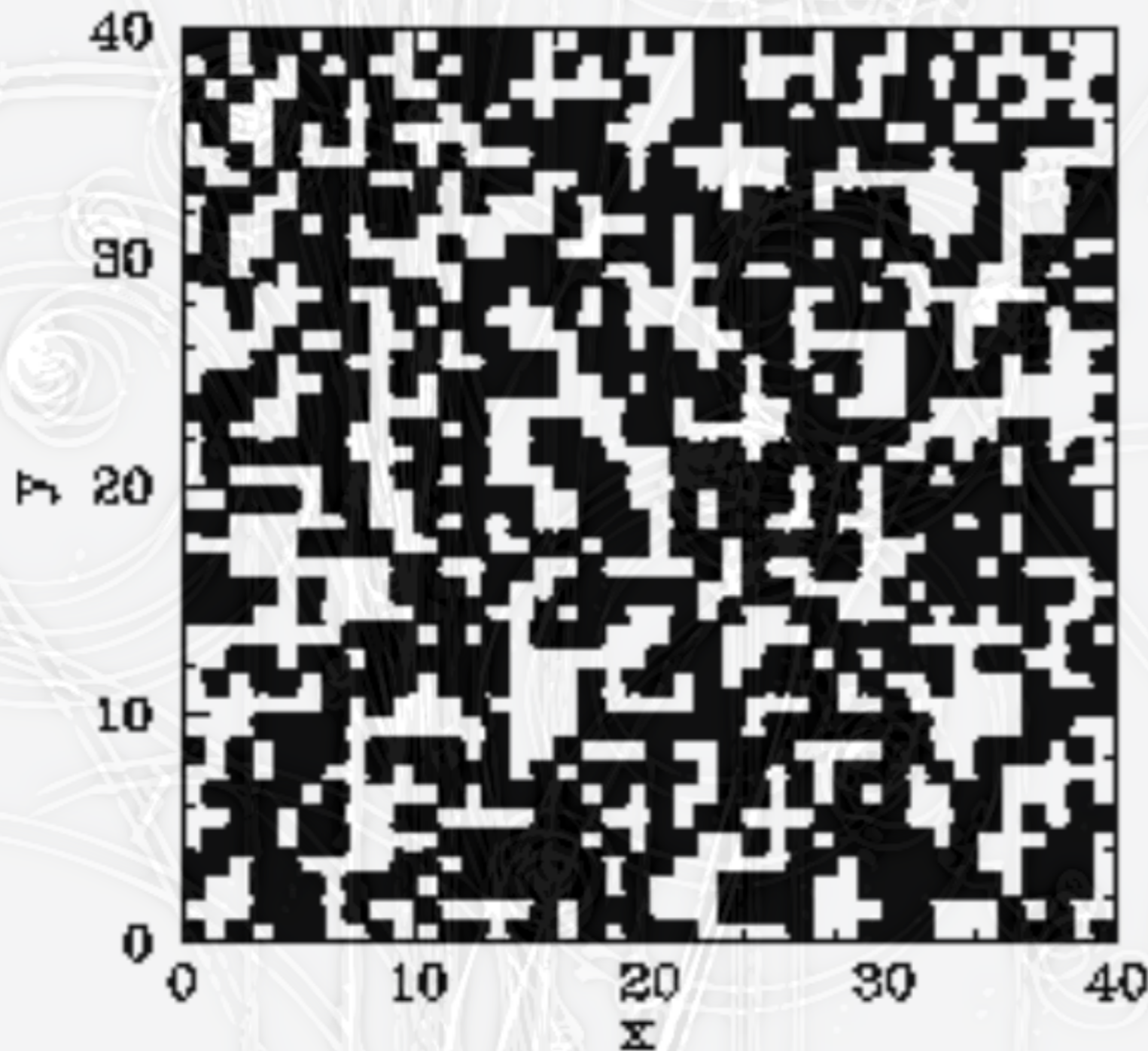
vs



Continuum partners

# Ising Model

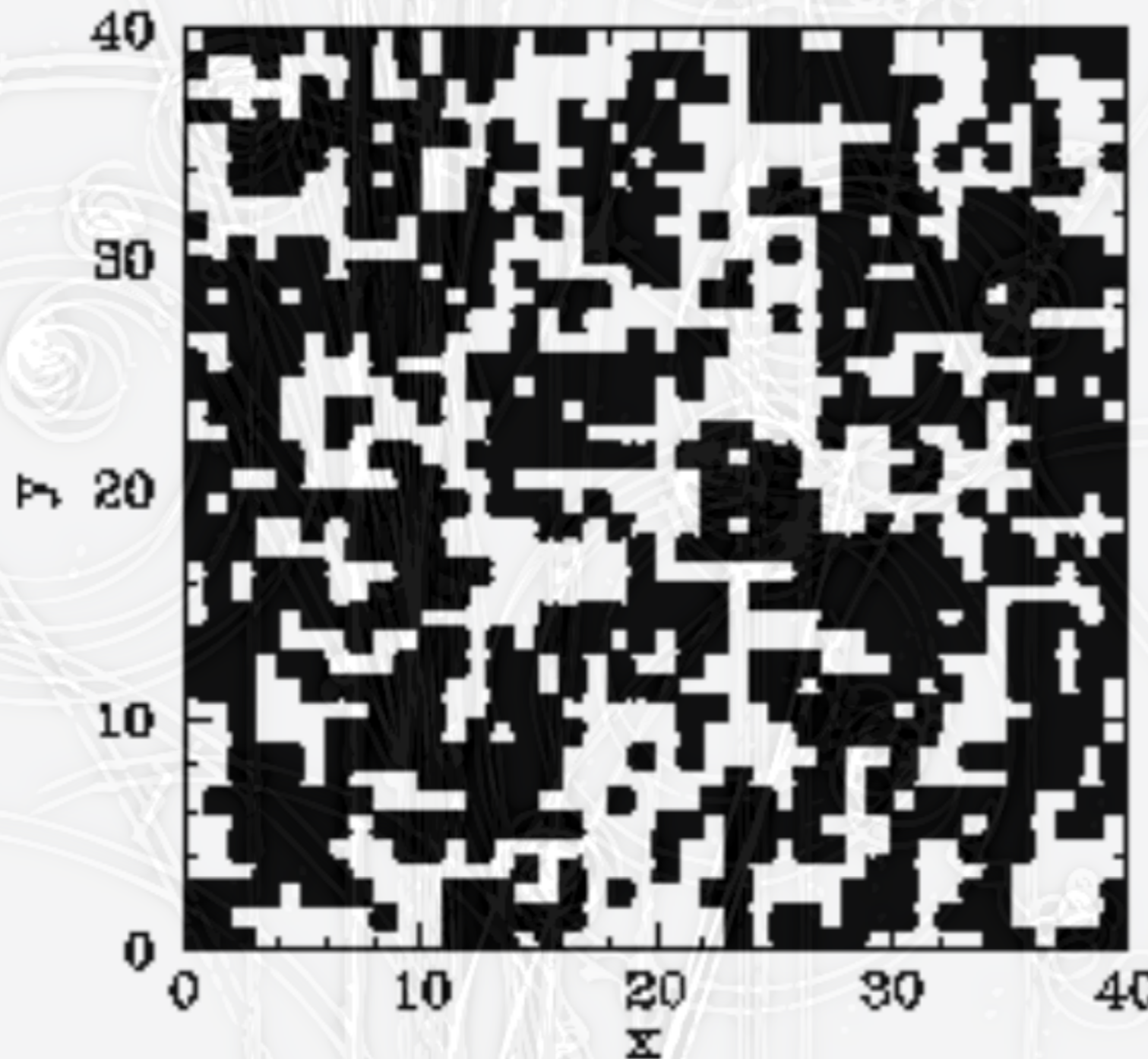
$$H = -J \sum s(x)s(x+n) - \mu\mathcal{H} \sum s(x)$$



$$s(x) = \pm 1$$

# Ising Model

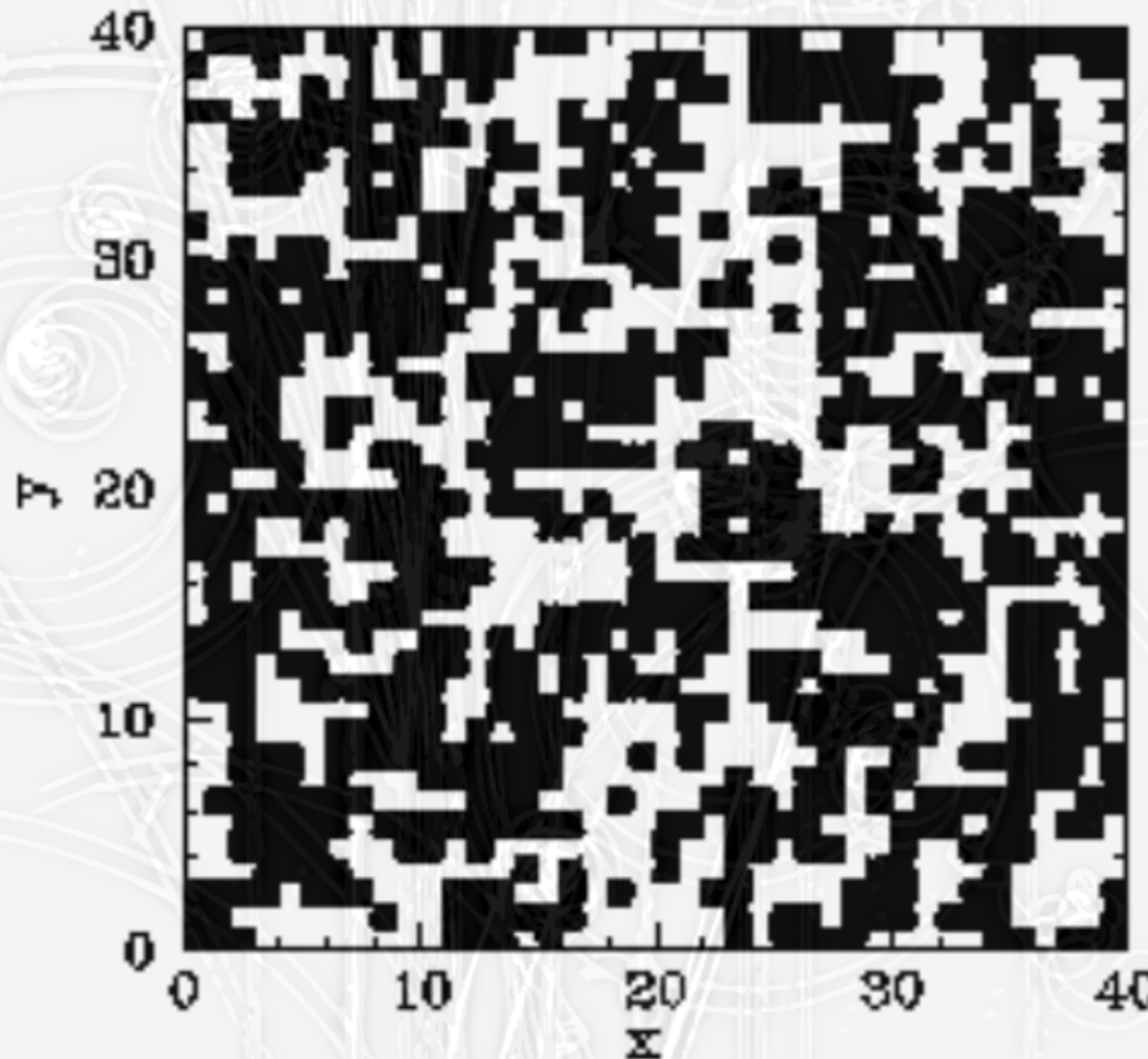
$$H = -J \sum s(x)s(x+n) - \mu\mathcal{H} \sum s(x)$$



$$s(x) = \pm 1$$

# Ising Model

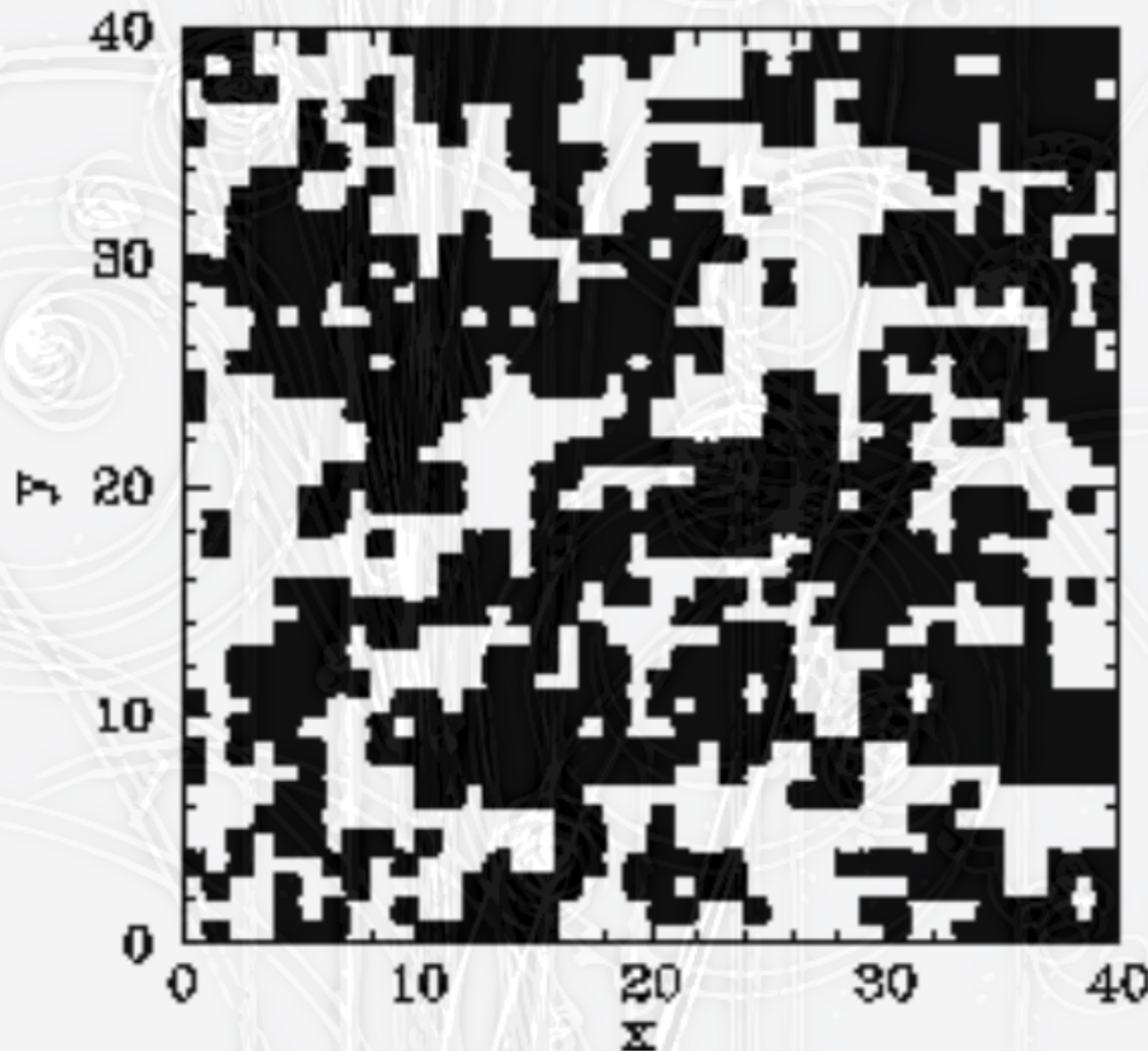
$$H = -J \sum s(x)s(x+n) - \mu\mathcal{H} \sum s(x)$$



$$s(x) = \pm 1$$

# Ising Model

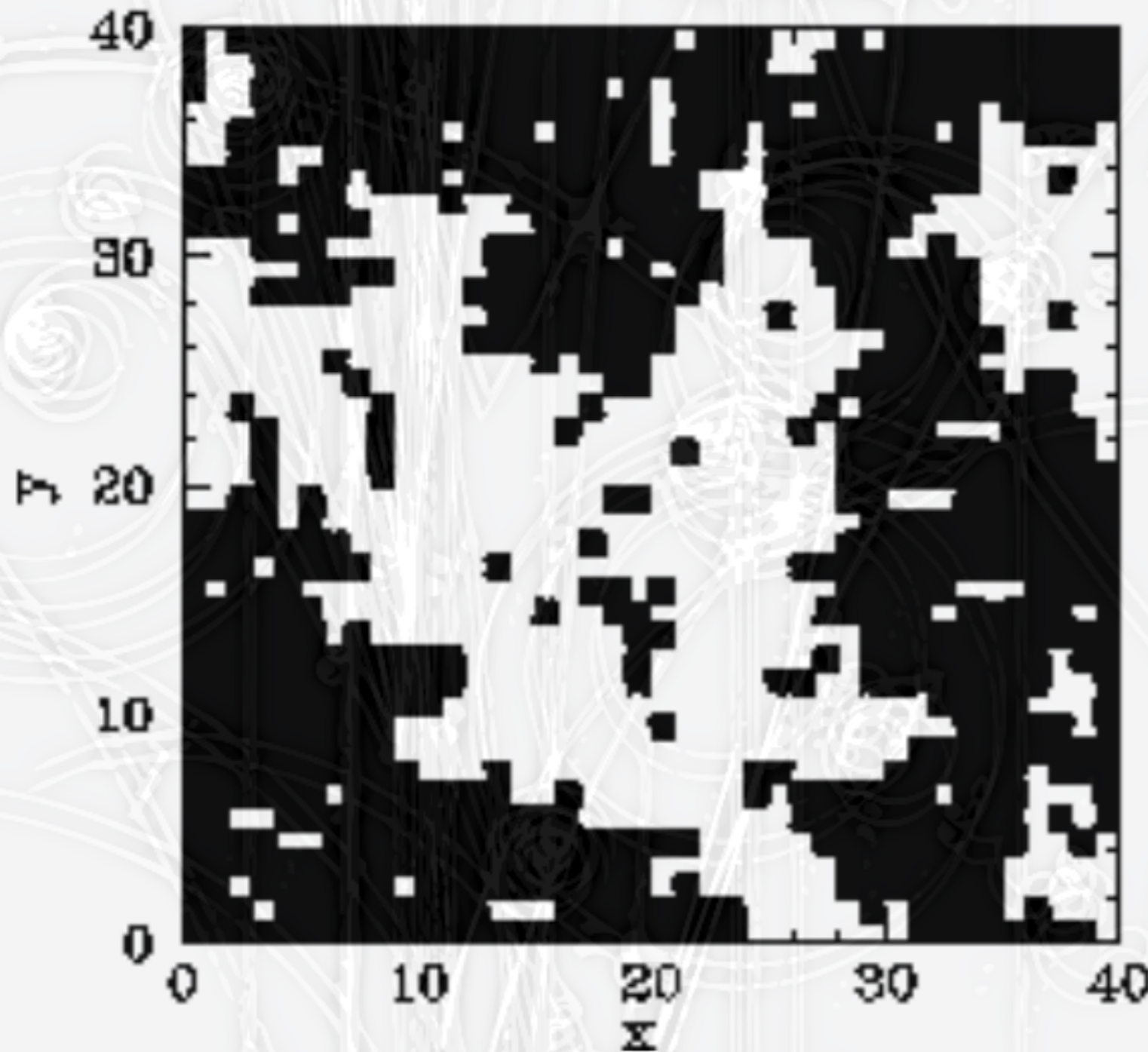
$$H = -J \sum s(x)s(x+n) - \mu\mathcal{H} \sum s(x)$$



$$s(x) = \pm 1$$

# Ising Model

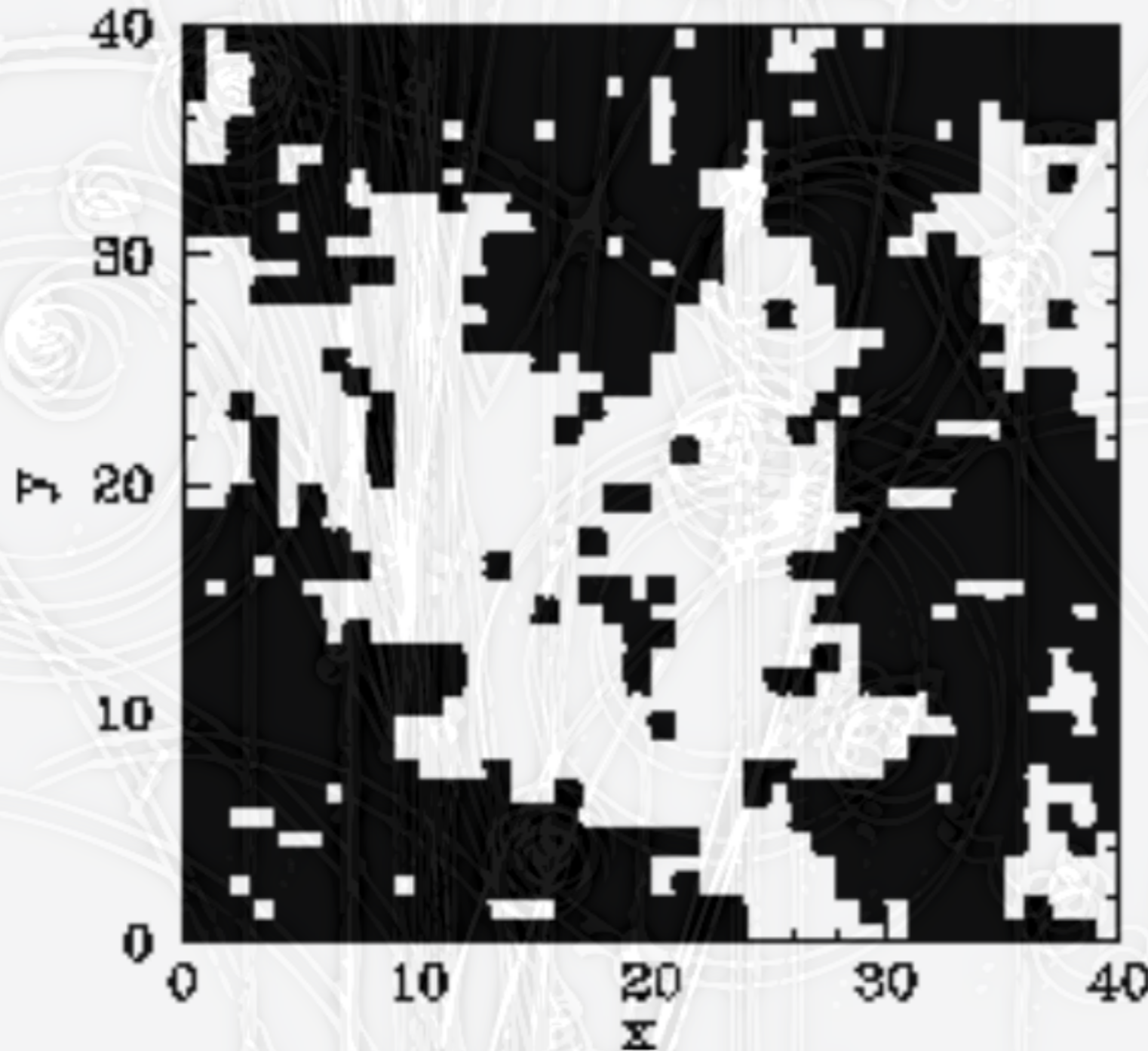
$$H = -J \sum s(x)s(x+n) - \mu\mathcal{H} \sum s(x)$$



$$s(x) = \pm 1$$

# Ising Model

$$H = -J \sum s(x)s(x+n) - \mu\mathcal{H} \sum s(x)$$



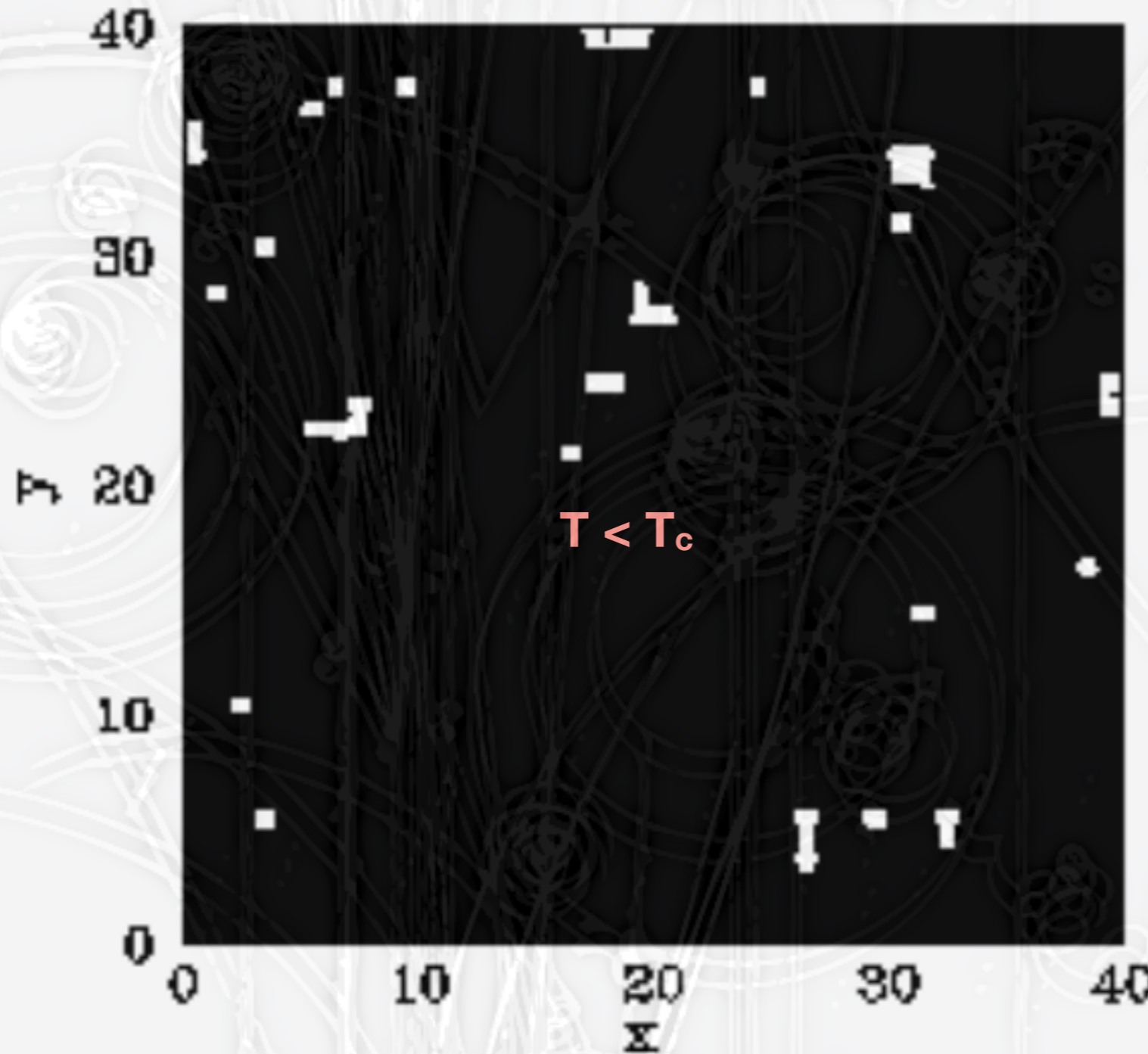
$$s(x) = \pm 1$$

$$\sim e^{-|x|/\xi}$$

$$\lim_{T \rightarrow T_c} \xi = \infty$$

# Ising Model

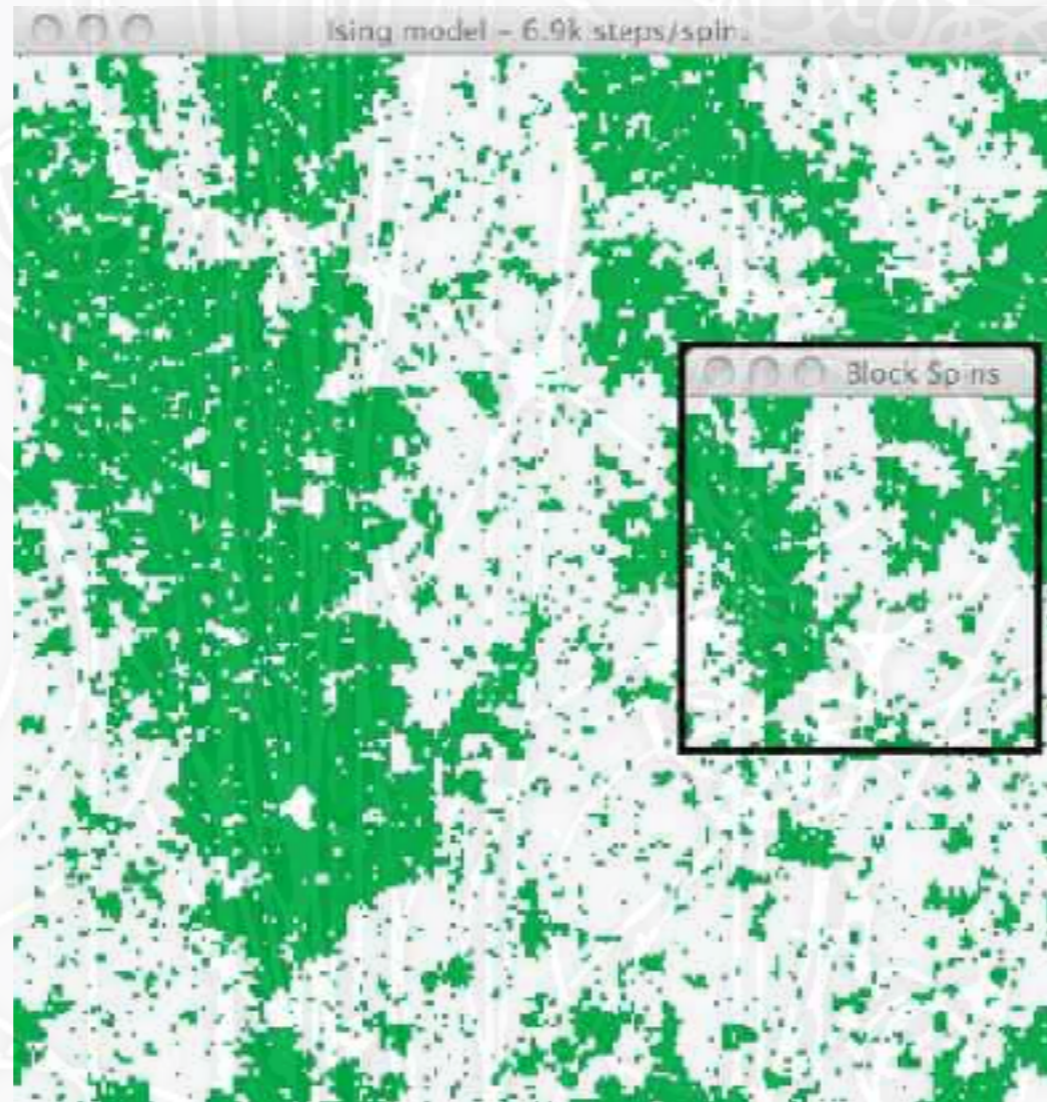
$$H = -J \sum s(x)s(x+n) - \mu\mathcal{H} \sum s(x)$$



$$s(x) = \pm 1$$

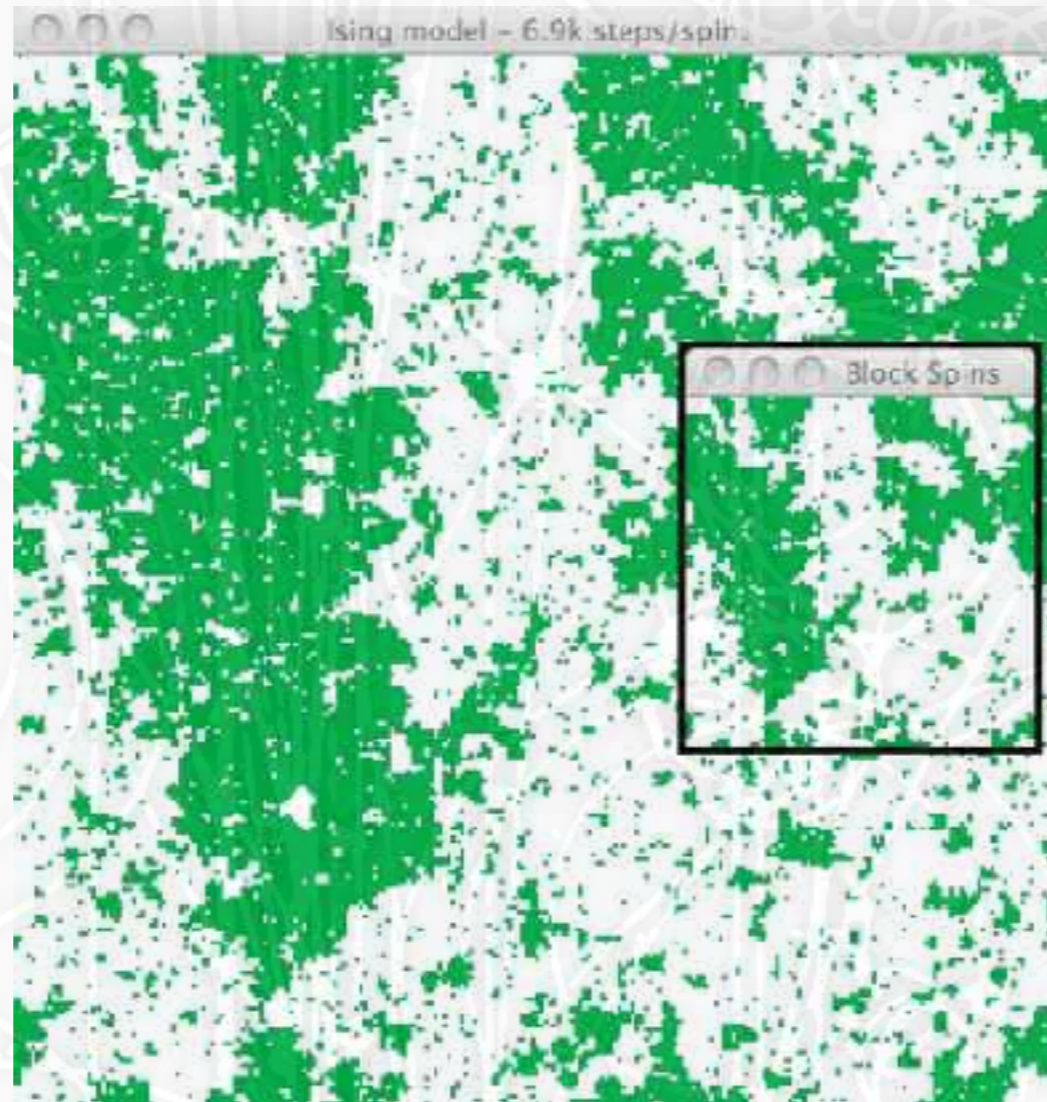


# Critical Ising Model is Scale Invariant



$$\text{at } T=T_c \quad \langle s(0)s(x) \rangle \propto \frac{1}{|x|^{2\Delta-1}}$$

# Critical Ising Model is Scale Invariant

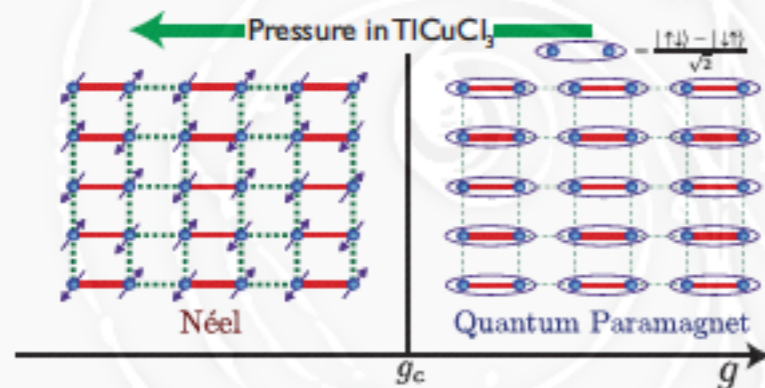
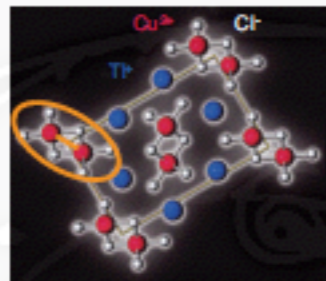


$$\text{at } T=T_c \quad \langle s(0)s(x) \rangle \propto \frac{1}{|x|^{2\Delta-1}} = \int d^3p \frac{e^{ip \cdot x}}{|p|^{4-2\Delta}}$$

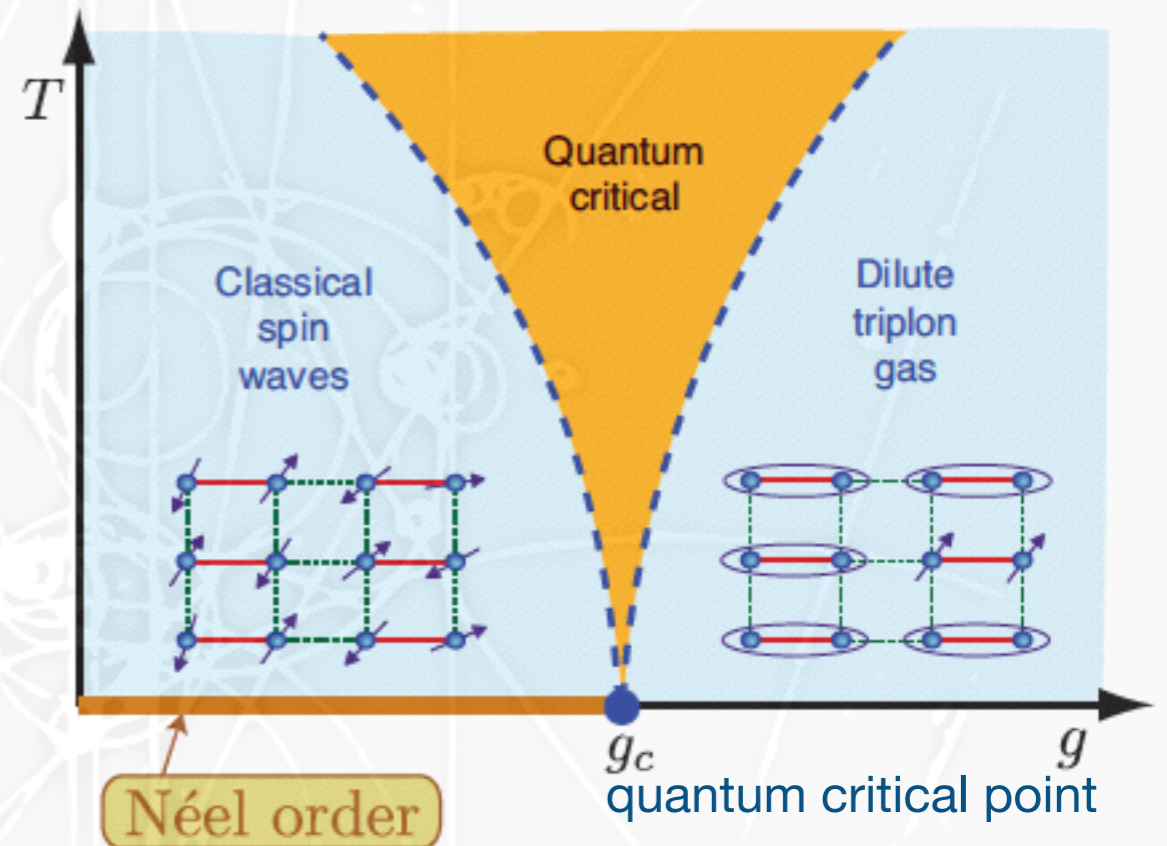
↑  
critical exponent

# Higgs & Quantum Phase Transition

Condensed matter systems can produce a light scalar by tuning the parameters close to a critical value where a continuous phase transition occurs.



Sachdev, arXiv:1102.4268



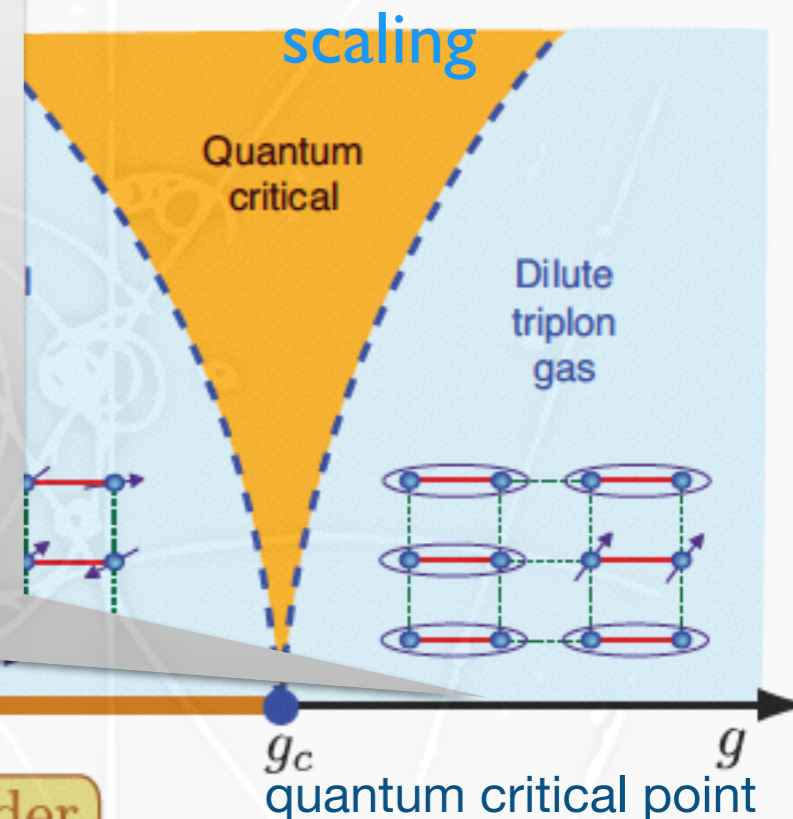
# Higgs & Quantum Phase Transition

Condensed matter systems can produce a light scalar by tuning the parameters close

**@2nd order QPT, @ critical point**, all masses vanish & the theory is scale invariant, characterized by the **dimensions** of the field,

and at low energies we will see the universal behavior of some fixed point that constitutes the low-energy EFT.

rs.



Sachdev, arXiv:1102.4268

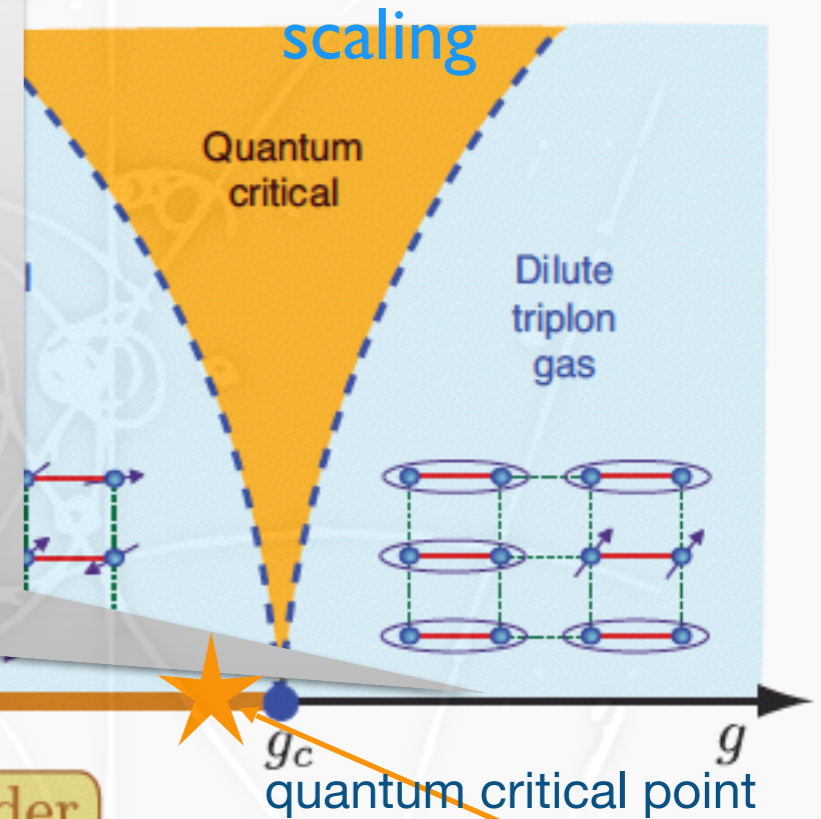
# Higgs & Quantum Phase Transition

Condensed matter systems can produce a light scalar by tuning the parameters close

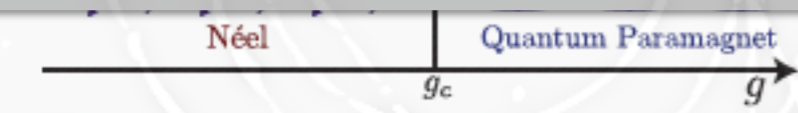
**@2nd order QPT, @ critical point**, all masses vanish & the theory is scale invariant, characterized by the **dimensions** of the field,

and at low energies we will see the universal behavior of some fixed point that constitutes the low-energy EFT.

rs.



We are here



Sachdev, arXiv:1102.4268

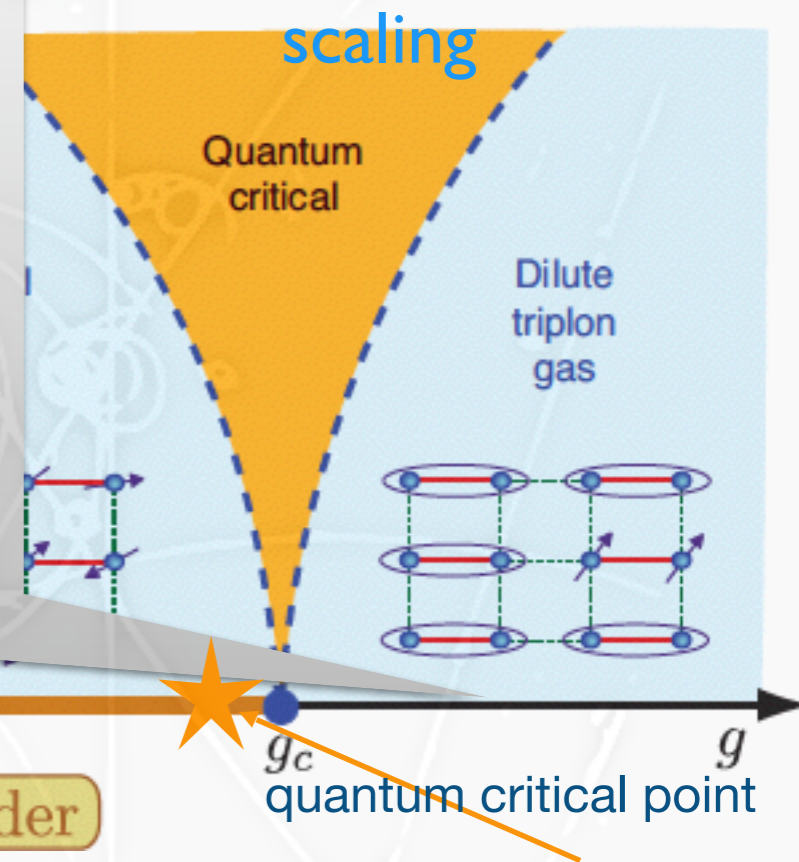
# Higgs & Quantum Phase Transition

Condensed matter systems can produce a light scalar by tuning the parameters close

**@2nd order QPT, @ critical point**, all masses vanish & the theory is scale invariant, characterized by the **dimensions** of the field,

and at low energies we will see the universal behavior of some fixed point that constitutes the low-energy EFT.

rs.



Sachdev, arXiv:1102.4268

We are here

**What is the nature of electroweak phase transition?**

**Does the underlying theory also have a QPT?**

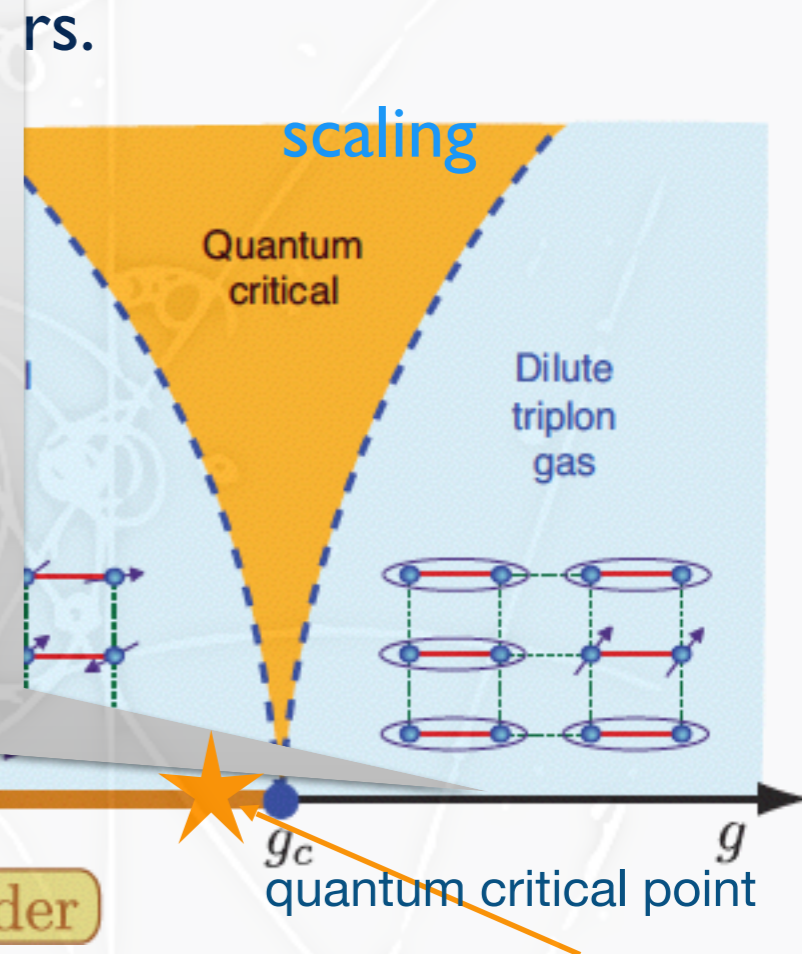
**If so, is it more interesting than mean-field theory?**

# Higgs & Quantum Phase Transition

Condensed matter systems can produce a light scalar by tuning the parameters close

**@2nd order QPT, @ critical point**, all masses vanish & the theory is scale invariant, characterized by the **dimensions** of the field,

and at low energies we will see the universal behavior of some fixed point that constitutes the low-energy EFT.



Sachdev, arXiv:1102.4268

We are here

**What is the nature of electroweak phase transition?**

**Does the underlying theory also have a QPT?**

**If so, is it more interesting than mean-field theory?**

$$G(p) \sim \frac{i}{p^2} \quad \text{vs.} \quad G(p) \sim \frac{i}{(p^2)^{2-\Delta}} \quad \text{or} \quad G(p) \sim \frac{i}{(p^2 - \mu^2)^{2-\Delta}}$$

# AdS/CFT

---

$$\left\langle e^{\int d^4x \phi_0(x) \mathcal{O}(x)} \right\rangle_{\text{CFT}} \approx \underline{e}^{S_{5\text{Dgravity}}[\phi(x,z)|_{z=0}=\phi_0(x)]}$$

$$ds^2 = \frac{R^2}{z^2} (dx_\mu^2 - dz^2)$$

$\mathcal{O} \subset \text{CFT} \leftrightarrow \phi$  AdS<sub>5</sub> field



# AdS/CFT

---

$$ds^2 = \frac{R^2}{z^2} (dx_\mu^2 - dz^2)$$
$$z > \epsilon$$

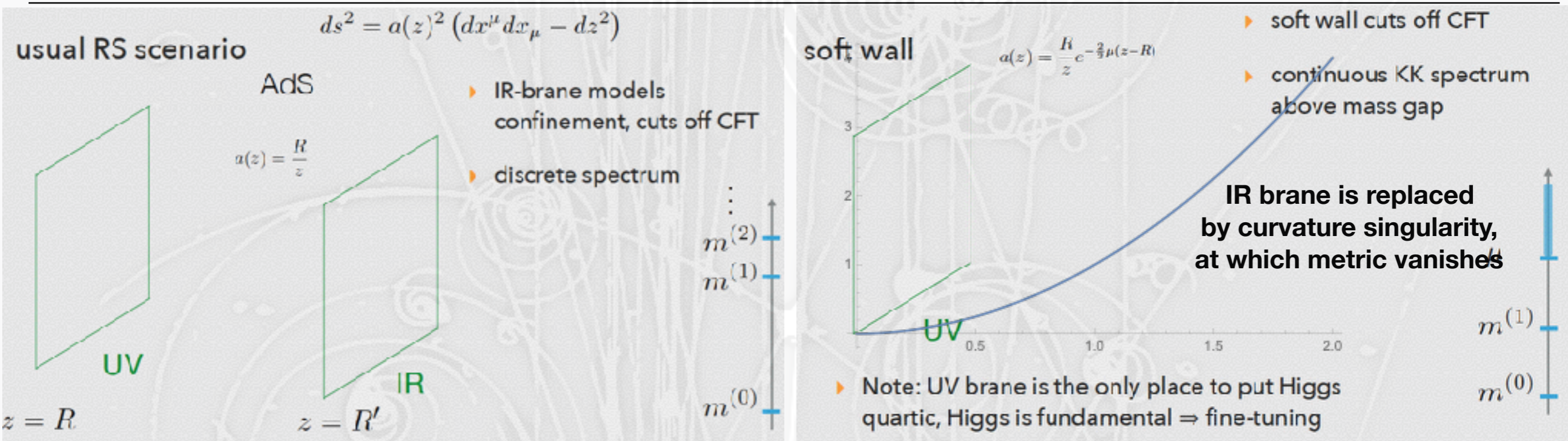
$$S_{bulk} = \frac{1}{2} \int d^4x dz \sqrt{g} (g^{\alpha\beta} \partial_\alpha \phi \partial_\beta \phi + m^2 \phi^2)$$

$$\phi(p, z) = az^2 J_\nu(pz) + bz^2 J_{-\nu}(pz)$$

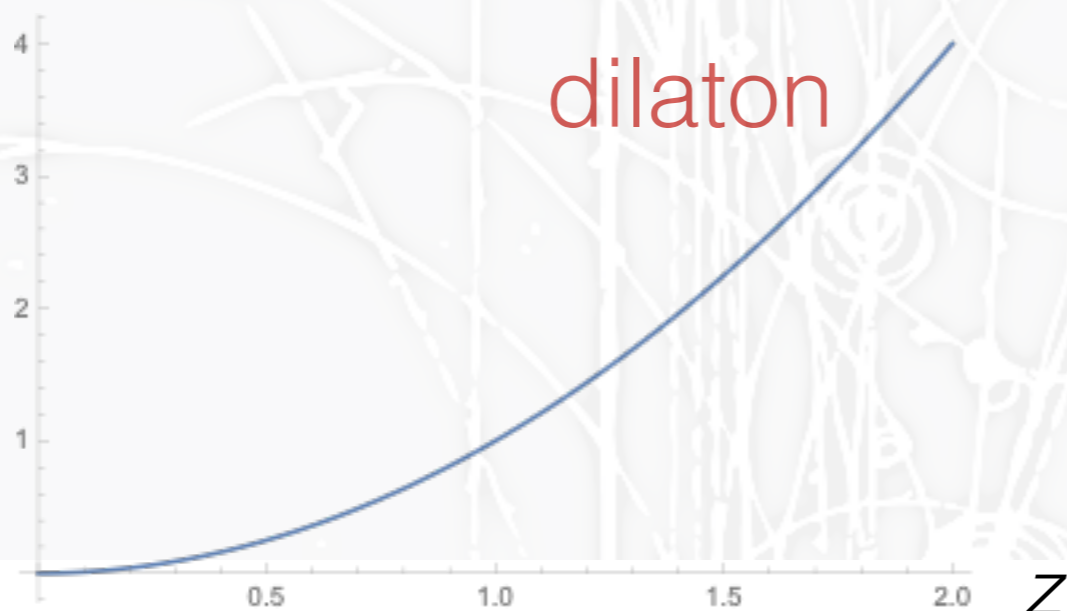
$$\Delta[\mathcal{O}] = 2 \pm \nu = 2 \pm \sqrt{4 + m^2 R^2}$$

$$\langle \mathcal{O}(p) \mathcal{O}(p) \rangle \propto \frac{\delta^{(4)}(p+p')}{(2\pi)^2} (p^2)^{\Delta-2}$$

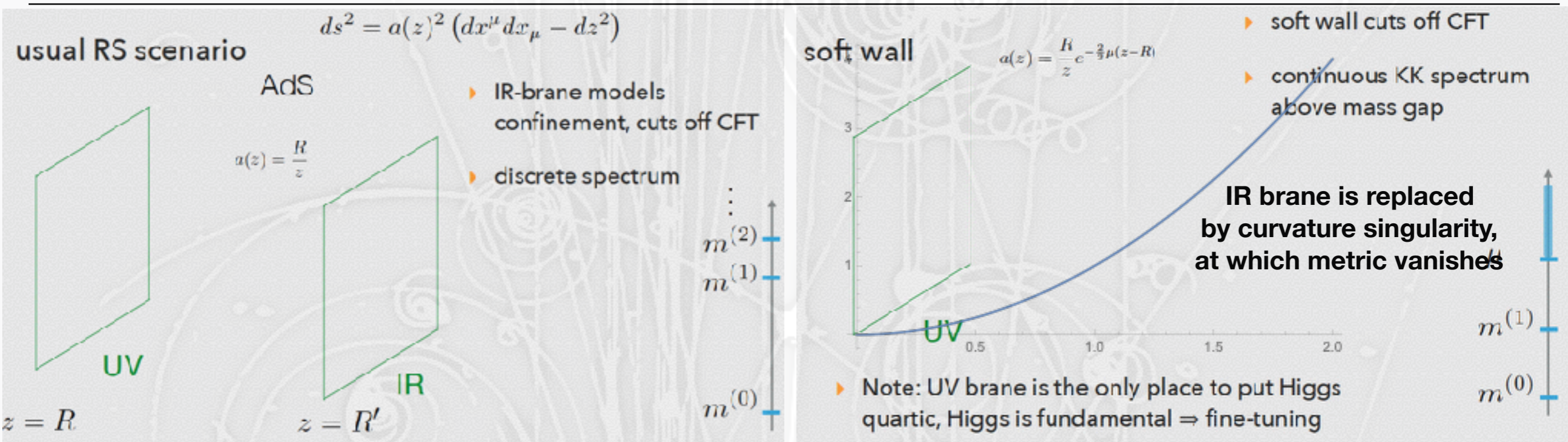
# broken CFT



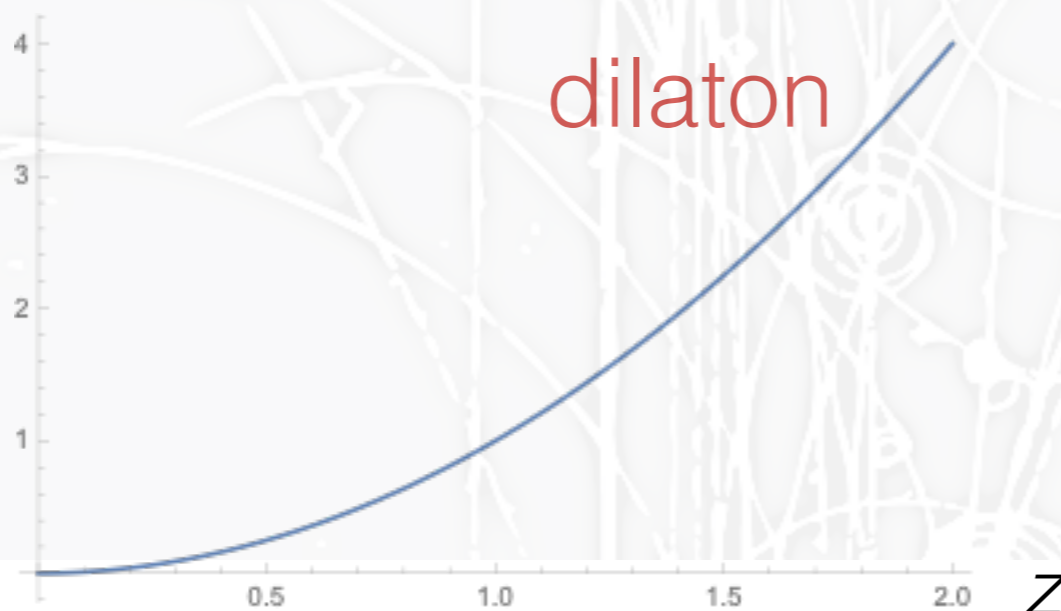
- ❖ Randall Sundrum 2 (only UV brane and bulk): cuts from 0 (CFT)
- ❖ RS1: putting IR cutoff at TeV
- ❖ New type of IR cutoff (soft wall) gives rise to a different phenomenology



# broken CFT

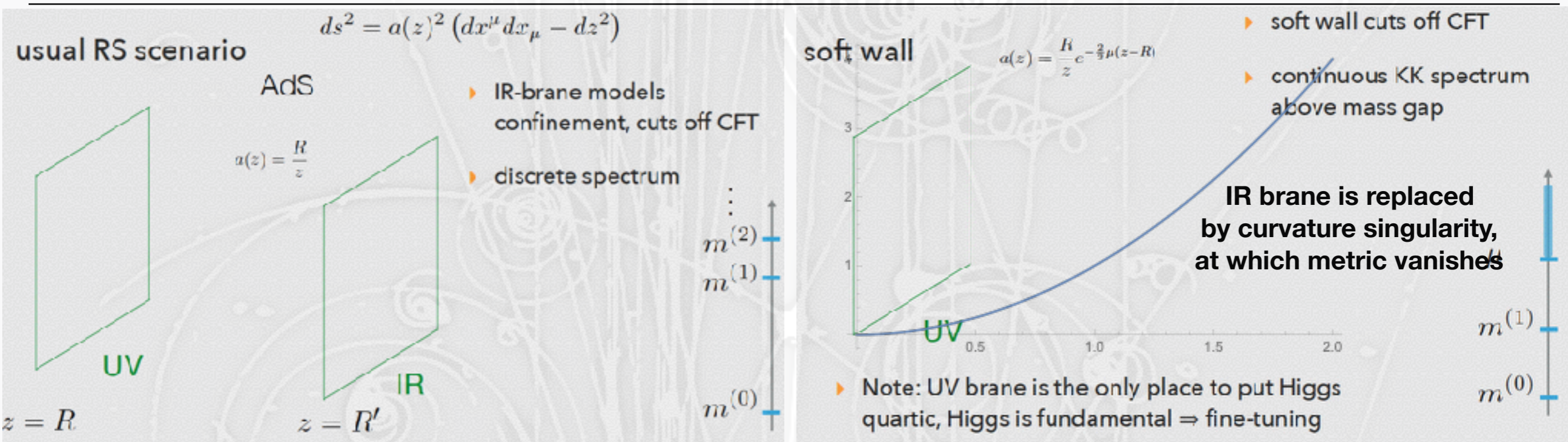


- ❖ Randall Sundrum 2 (only UV brane and bulk): cuts from 0 (CFT)
- ❖ RS1: putting IR cutoff at TeV
- ❖ New type of IR cutoff (soft wall) gives rise to a different phenomenology

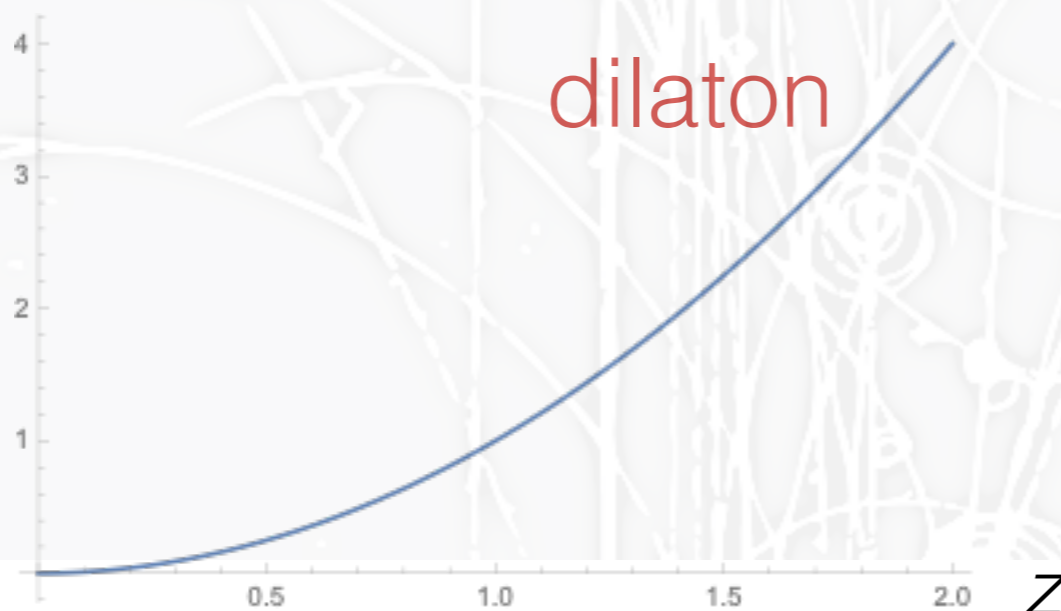


scalar getting VEV  $\Rightarrow$  marginal deformation of CFT

# broken CFT



- ❖ Randall Sundrum 2 (only UV brane and bulk): cuts from 0 (CFT)
- ❖ RS1: putting IR cutoff at TeV
- ❖ New type of IR cutoff (soft wall) gives rise to a different phenomenology



# broken CFT by IR cutoff

---

$$S_{\text{int}} = \frac{1}{2} \int d^4x dz \sqrt{g} \phi \mathcal{H}^\dagger \mathcal{H}$$

$$\phi = \left( \frac{\mu z}{R} \right)$$

$$z^5 \partial_z \left( \frac{1}{z^3} \partial_z \mathcal{H} \right) - z^2 (p^2 - \mu^2) \mathcal{H} - m^2 R^2 \mathcal{H} = 0$$

$$\langle \mathcal{O}(p) \mathcal{O}(p) \rangle \propto \frac{\delta^{(4)}(p+p')}{(2\pi)^2} (p^2 - \mu^2)^{\Delta-2}$$

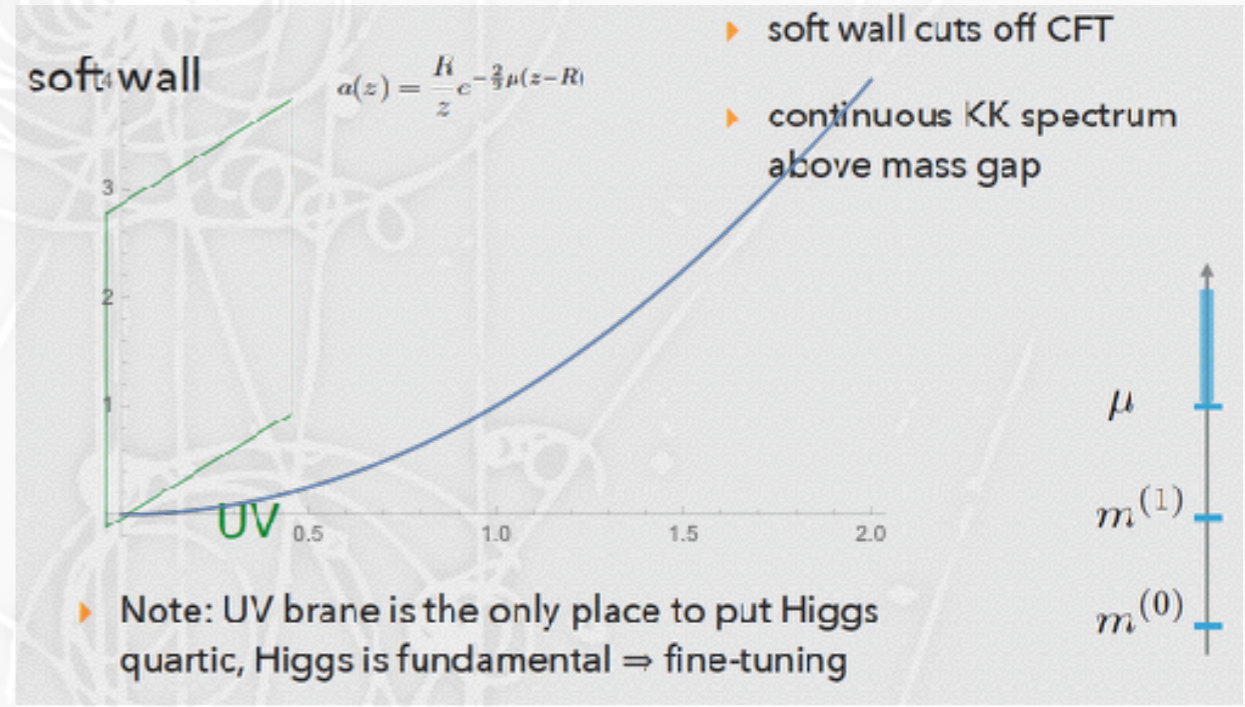
$$[\partial^2 - \mu^2]^{2-\Delta} \delta(x-y)$$

# soft wall (AdS/QCD)

$$ds^2 = a(z) (dx^\mu dx_\mu - dz^2)$$

$$a(z) = \frac{R}{z} e^{-\frac{2}{3}\mu(z-R)^\nu}$$

$$S_{\text{gauge}} = \int d^5x -\frac{1}{4} a(z) F_{MN}^2$$

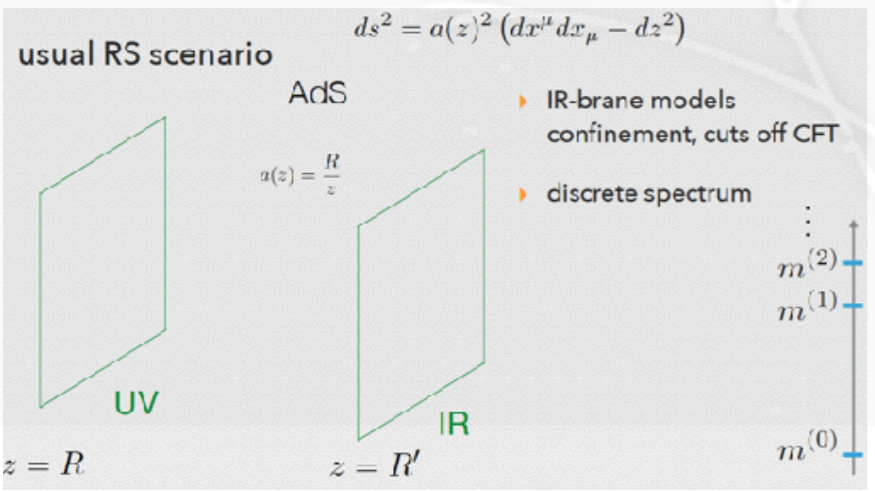


EOM:  $(a^{-1} \partial_z (a \partial_z) + p^2) f = 0$        $f = a^{-\frac{1}{2}} \Psi$

“Schrödinger Eqn”.:  $(-\partial_z^2 + V(z)) \Psi = p^2 \Psi$ ,       $V(z) = \frac{a''}{2a} - \frac{a'^2}{4a^2}$

$$V(z) \Big|_{z \rightarrow \infty} \rightarrow \left(\frac{\mu}{3}\right)^2 \Rightarrow \text{continuum begins at: } p^2 = (\mu/3)^2$$

$$\rightarrow \infty \text{ (infinite well)} \Rightarrow \text{KK towers}$$

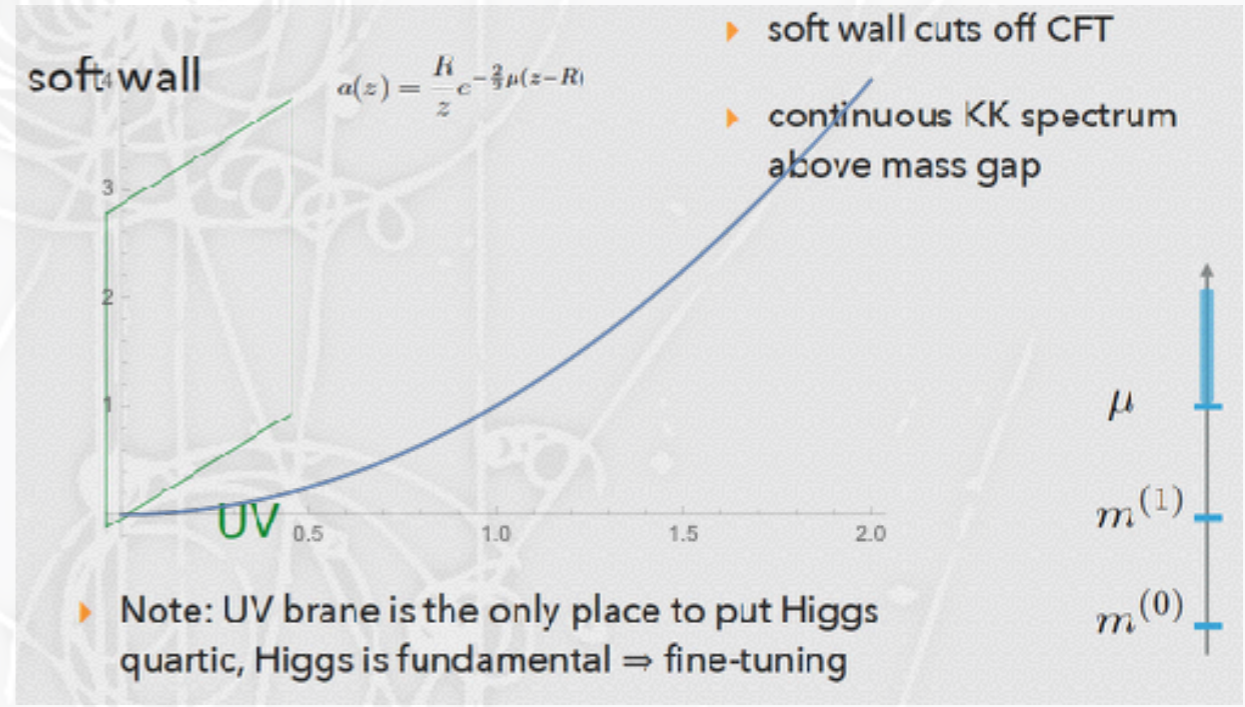


# soft wall (AdS/QCD)

$$ds^2 = a(z) (dx^\mu dx_\mu - dz^2)$$

$$a(z) = \frac{R}{z} e^{-\frac{2}{3}\mu(z-R)}$$

$$S_{\text{gauge}} = \int d^5x -\frac{1}{4} a(z) F_{MN}^2$$

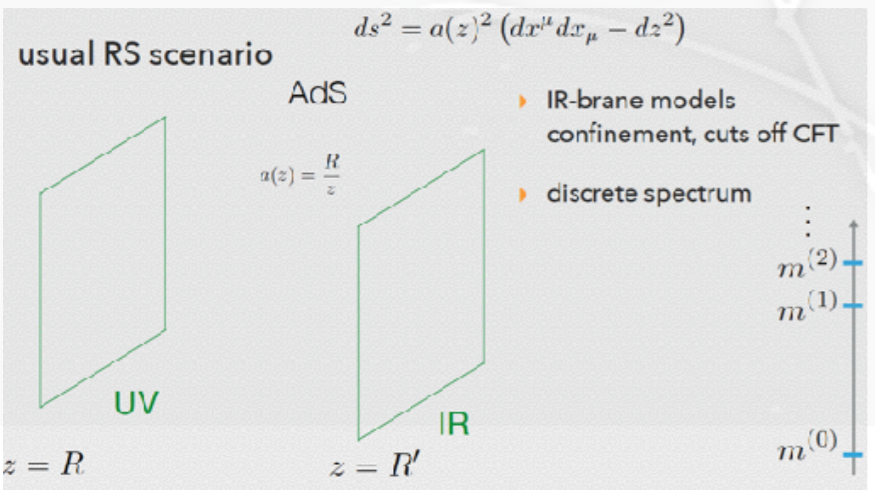


EOM:  $(a^{-1}\partial_z(a\partial_z) + p^2) f = 0$        $f = a^{-\frac{1}{2}} \Psi$

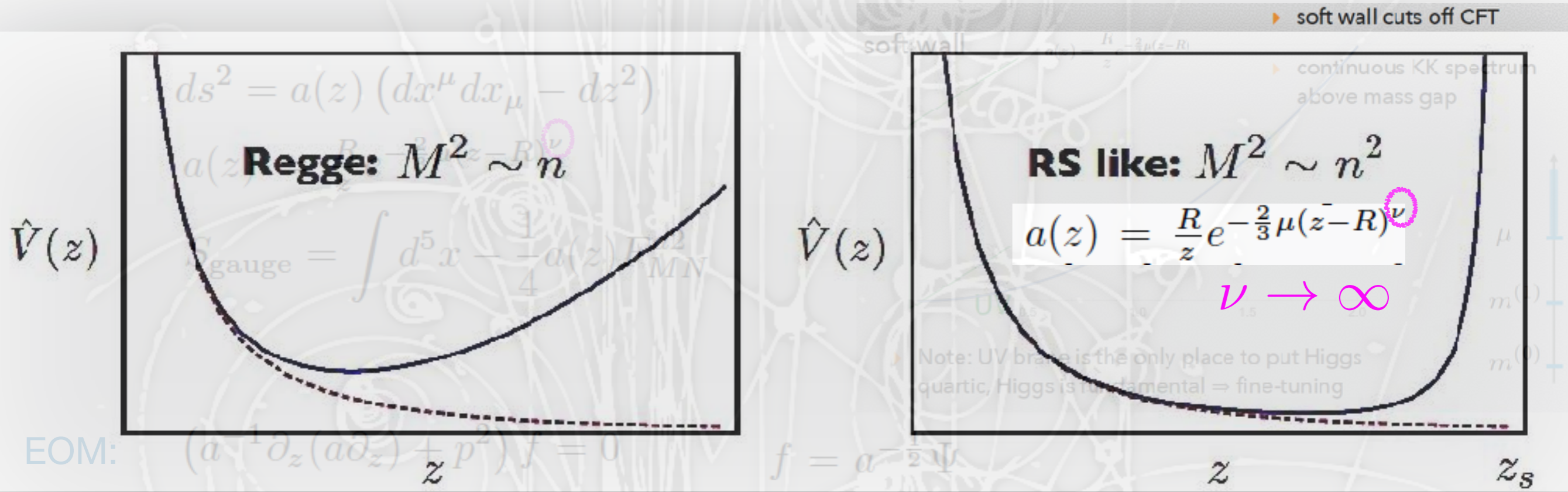
“Schrödinger Eqn”.:  $(-\partial_z^2 + V(z)) \Psi = p^2 \Psi$ ,       $V(z) = \frac{a''}{2a} - \frac{a'^2}{4a^2}$

$V(z)|_{z \rightarrow \infty} \rightarrow \left(\frac{\mu}{3}\right)^2 \Rightarrow$  continuum begins at:  $p^2 = (\mu/3)^2$

$\rightarrow \infty$  (infinite well)  $\Rightarrow$  KK towers



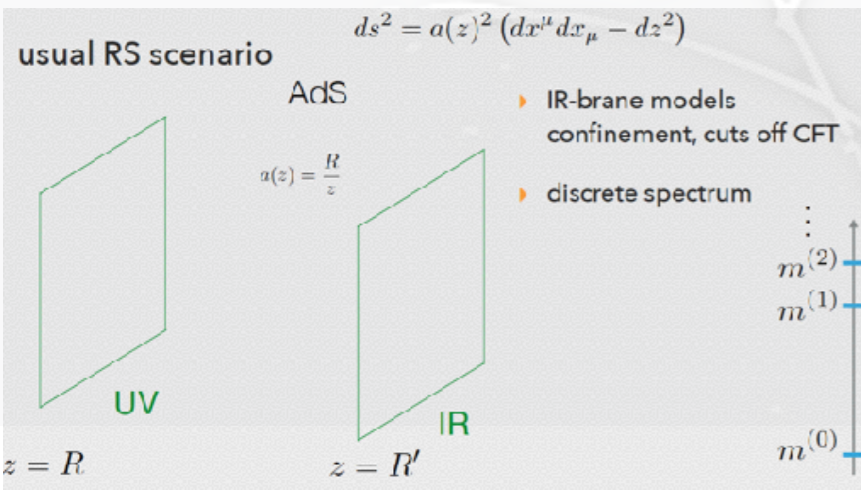
# soft wall (AdS/QCD)



“Schrödinger Eqn”.:  $(-\partial_z^2 + V(z)) \Psi = p^2 \Psi, \quad V(z) = \frac{a''}{2a} - \frac{a'^2}{4a^2}$

$V(z) \Big|_{z \rightarrow \infty} \rightarrow \left(\frac{\mu}{3}\right)^2 \Rightarrow$  continuum begins at:  $p^2 = (\mu/3)^2$

$\rightarrow \infty$  (infinite well)  $\Rightarrow$  KK towers





# soft wall (AdS/QCD)

$\hat{V}(z)$

$ds^2 = a(z) (dx^\mu dx_\mu - dz^2)$

**Regge:**  $M^2 \sim n^\nu$

$S_{\text{gauge}} = \int d^5x \frac{1}{4} a(z) F_{MN}^2$

EOM:  $(a^{-1} \partial_z (a \partial_z) + p^2) f = 0$

$a(z) = \frac{R}{z} e^{-\frac{2}{3} \mu(z-R)^\nu} \quad \nu \rightarrow 1$

**continuum with mass gap**

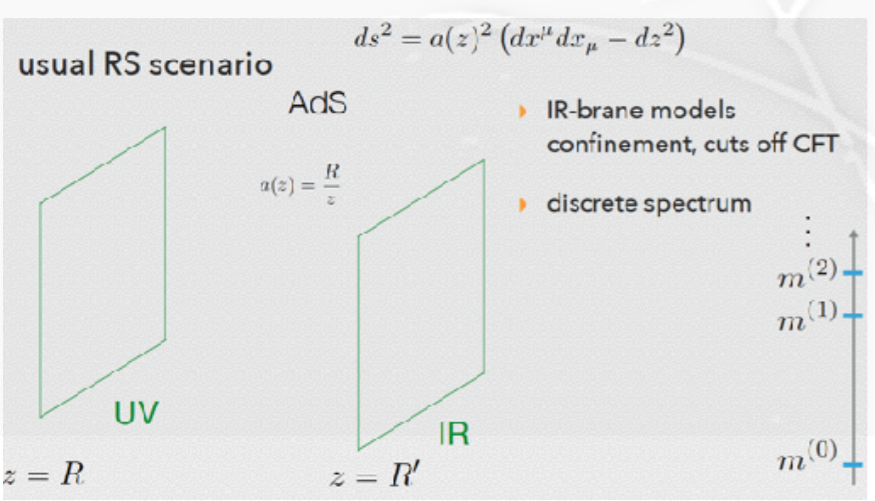
$\hat{V}(z)$

$z$

“Schrödinger Eqn”.:  $(-\partial_z^2 + V(z)) \Psi = p^2 \Psi, \quad V(z) = \frac{a''}{2a} - \frac{a'^2}{4a^2}$

$V(z) \Big|_{z \rightarrow \infty} \rightarrow \left(\frac{\mu}{3}\right)^2 \Rightarrow$  **continuum** begins at:  $p^2 = (\mu/3)^2$

$\rightarrow \infty$  (infinite well)  $\Rightarrow$  **KK towers**



# soft wall (AdS/QCD)

$\hat{V}(z)$

$ds^2 = a(z) (dx^\mu dx_\mu - dz^2)$

**Regge:**  $M^2 \sim R^\nu n$

$S_{\text{gauge}} = \int d^5x \frac{1}{4} a(z) F_{MN}^2$

EOM:  $(a^{-1} \partial_z (a \partial_z) + \frac{p^2}{z}) f = 0$

$a(z) = \frac{R}{z} e^{-\frac{2}{3} \mu (z-R)^\nu} \nu \rightarrow 1$

**continuum with mass gap**

$\hat{V}(z)$

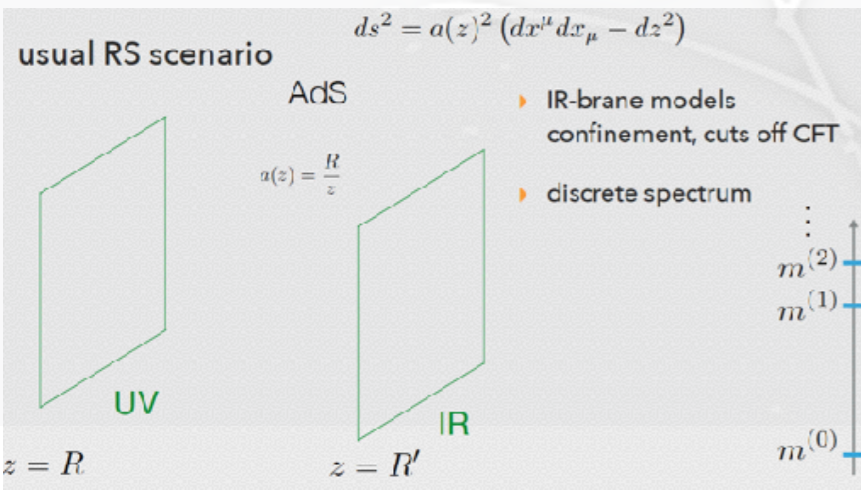
$z$

“Schrödinger Eqn”.:  $(-\partial_z^2 + V(z)) \Psi = p^2 \Psi, \quad V(z) \rightarrow \infty$

$V(z) \Big|_{z \rightarrow \infty} \rightarrow \left(\frac{\mu}{3}\right)^2 \Rightarrow \text{continuum}$

Stabilization of this setting:  
 Batell, Gherghetta, Sword '08  
 Cabrer, Gersdorff, Quiros '09

$\rightarrow \infty$  (infinite well)  $\Rightarrow$  KK towers



# soft wall (AdS/QCD)

$\hat{V}(z)$

$ds^2 = a(z) (dx^\mu dx_\mu - dz^2)$

**Regge:**  $M^2 \sim n^\nu$

$S_{\text{gauge}} = \int d^5x \frac{1}{4} a(z) F_{MN}^2$

EOM:  $(a^{-1} \partial_z (a \partial_z) + p^2) f = 0$

$a(z) = \frac{R}{z} e^{-\frac{2}{3}\mu(z-R)^\nu} \quad \nu \rightarrow 1$

**continuum with mass gap**

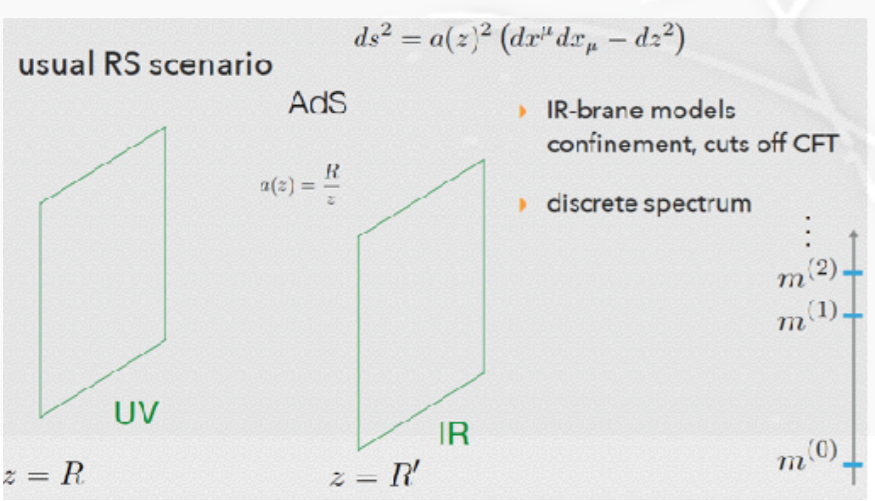
$\hat{V}(z)$

$z$

“Schrödinger Eqn”.:  $(-\partial_z^2 + V(z)) \Psi = p^2 \Psi, \quad V(z) = \frac{a''}{2a} - \frac{a'^2}{4a^2}$

$V(z) \Big|_{z \rightarrow \infty} \rightarrow \left(\frac{\mu}{3}\right)^2 \Rightarrow$  **continuum** begins at:  $p^2 = (\mu/3)^2$

$\rightarrow \infty$  (infinite well)  $\Rightarrow$  **KK towers**



# soft wall (AdS/QCD)

$\hat{V}(z)$ 

$$ds^2 = a(z) (dx^\mu dx_\mu - dz^2)$$

$$a(z) \text{ Regge: } M^2 z \sim R^\nu n$$

$$S_{\text{gauge}} = \int d^5x \frac{1}{4} a(z) F_{MN}^2$$

$\hat{V}(z)$ 

$$a(z) = \frac{R}{z} e^{-\frac{2}{3}\mu(z-R)^\nu} \quad \nu \rightarrow 1$$
**continuum with mass gap**

UV

IR

**linear dilaton:**

around UV, vanishing,  
only effect on IR and below

$$\Phi(z) = \mu(z - R)$$

$$z = R$$

$$z = R'$$

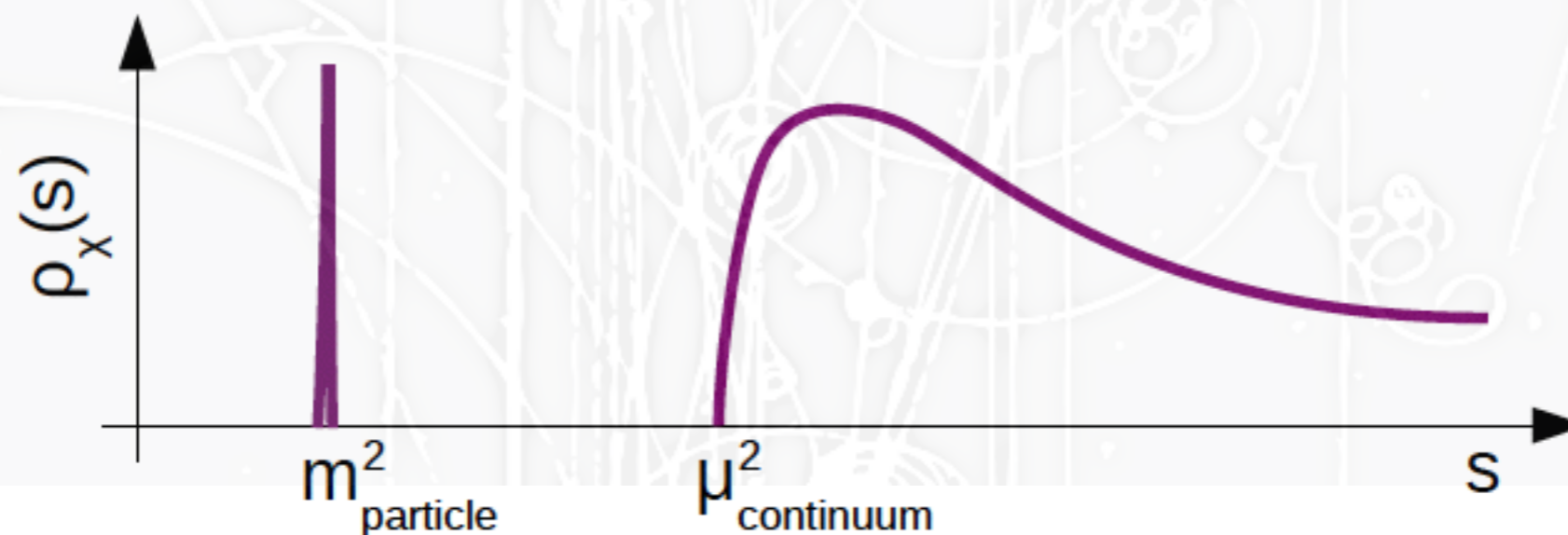
$$a_S(z) = \frac{R}{z}$$

z

# The Quantum Critical higgs

- ❖ At a QPT the approximate scale invariant theory is characterized by [the scaling dimension  \$\Delta\$](#)  of the gauge invariant operators. SM:  $\Delta = 1 + \mathcal{O}(\alpha/4\pi)$ .
- ❖ We want to present a general class of theories describing a higgs field near a non-mean-field QPT.
- ❖ In such theories, in addition to the pole (Higgs), there can also be a higgs continuum, representing additional states associated with the dynamics underlying the QPT

$$G_h(p^2) = \frac{i}{p^2 - m_h^2} + \int_{\mu^2}^{\infty} dM^2 \frac{\rho(M^2)}{p^2 - M^2}$$



# Modeling the QCH: generalized free fields

## Generalized Free Fields Polyakov, early '70s- skeleton expansions

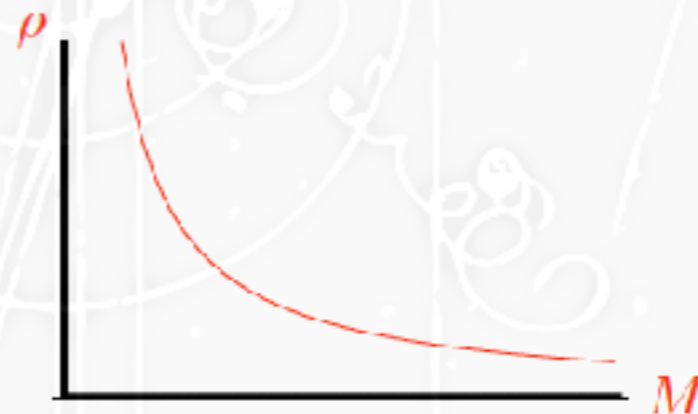
CFT completely specified by 2-point function - rest vanish

**Scaling - 2-point function:** 
$$G(p^2) = -\frac{i}{(-p^2 + i\epsilon)^{2-\Delta}}$$

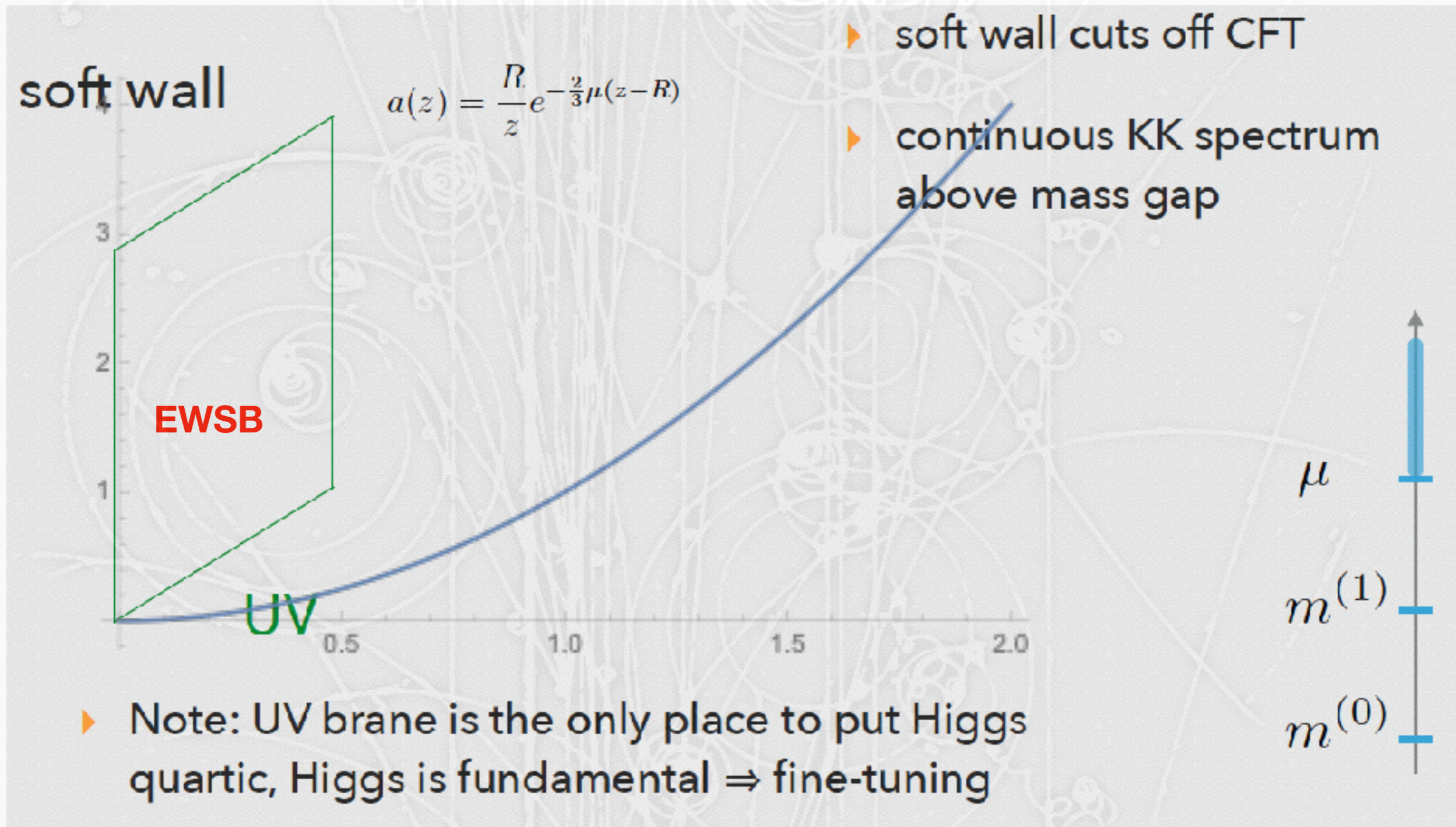
**Can be generated from:** 
$$\mathcal{L}_{\text{GFF}} = -\bar{h}^\dagger (\partial^2)^{2-\Delta} h$$
 Georgi  
hep-ph/0703260

Branch cut starting at origin - spectral density purely a continuum:

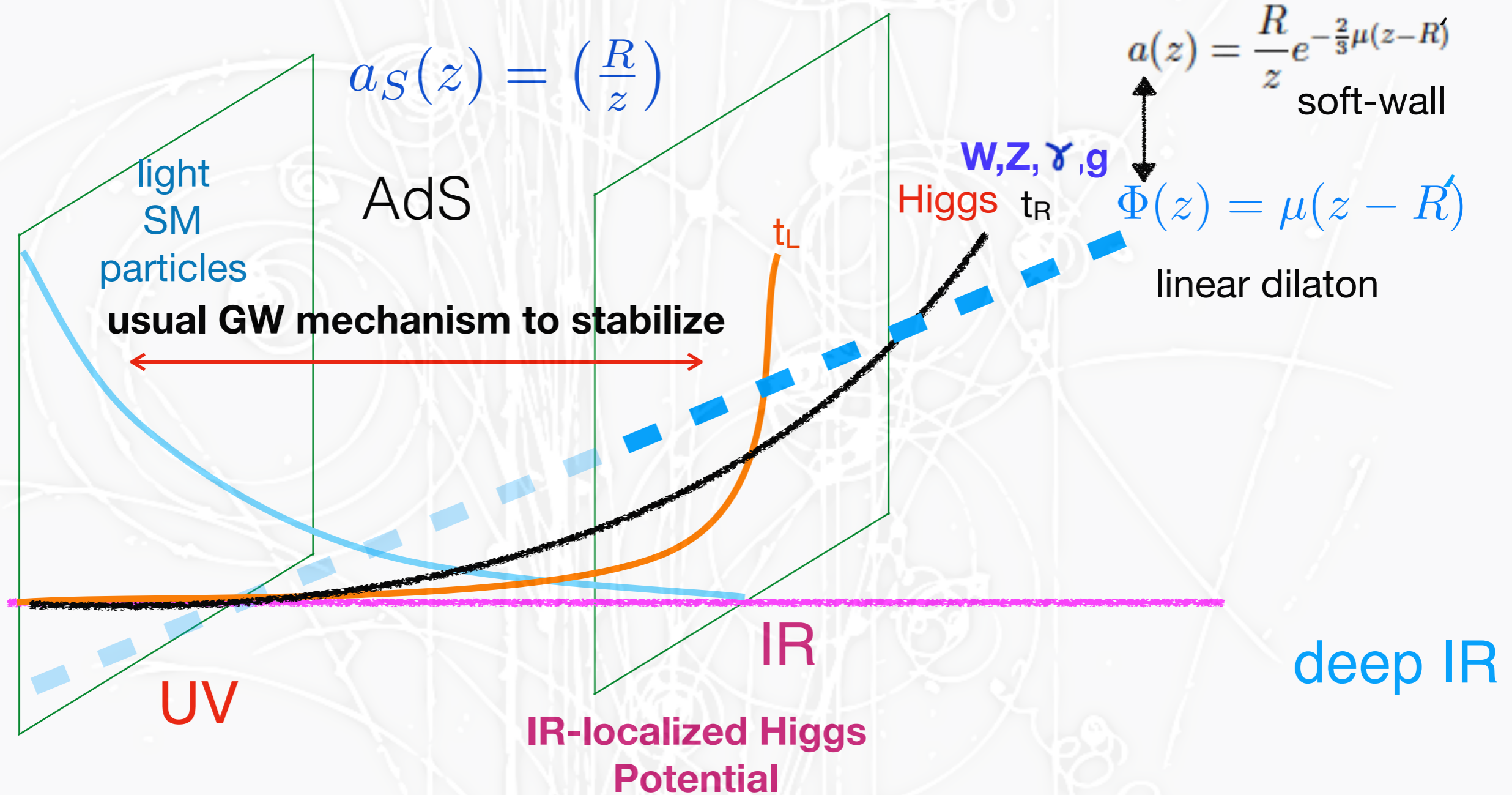
$$G(p) \sim \int_{\mu^2}^{\infty} dM^2 \frac{\rho(M^2)}{p^2 - M^2}$$



# Quantum Critical Higgs



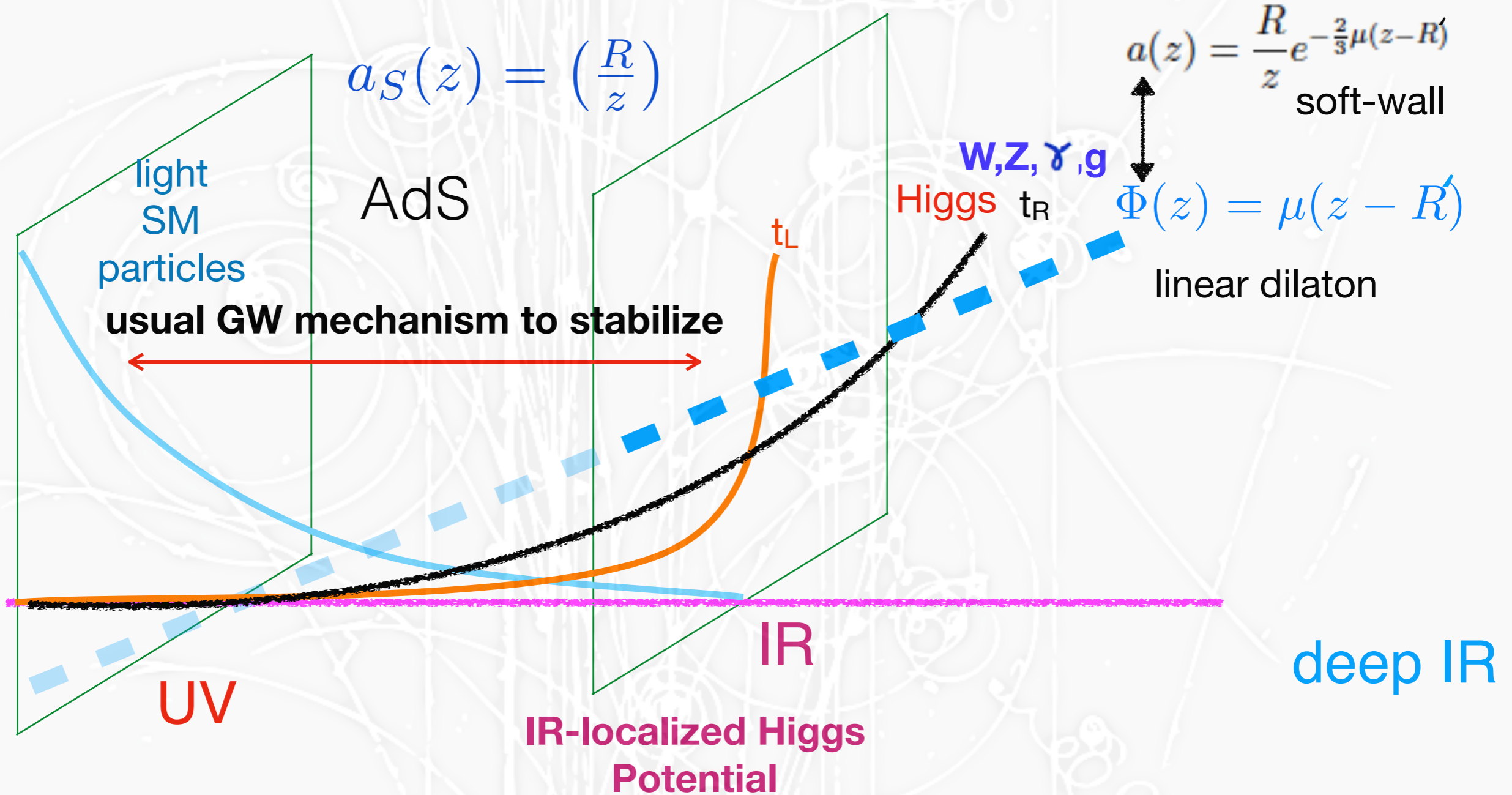
# A Natural Quantum Critical Higgs: 5D linear dilaton





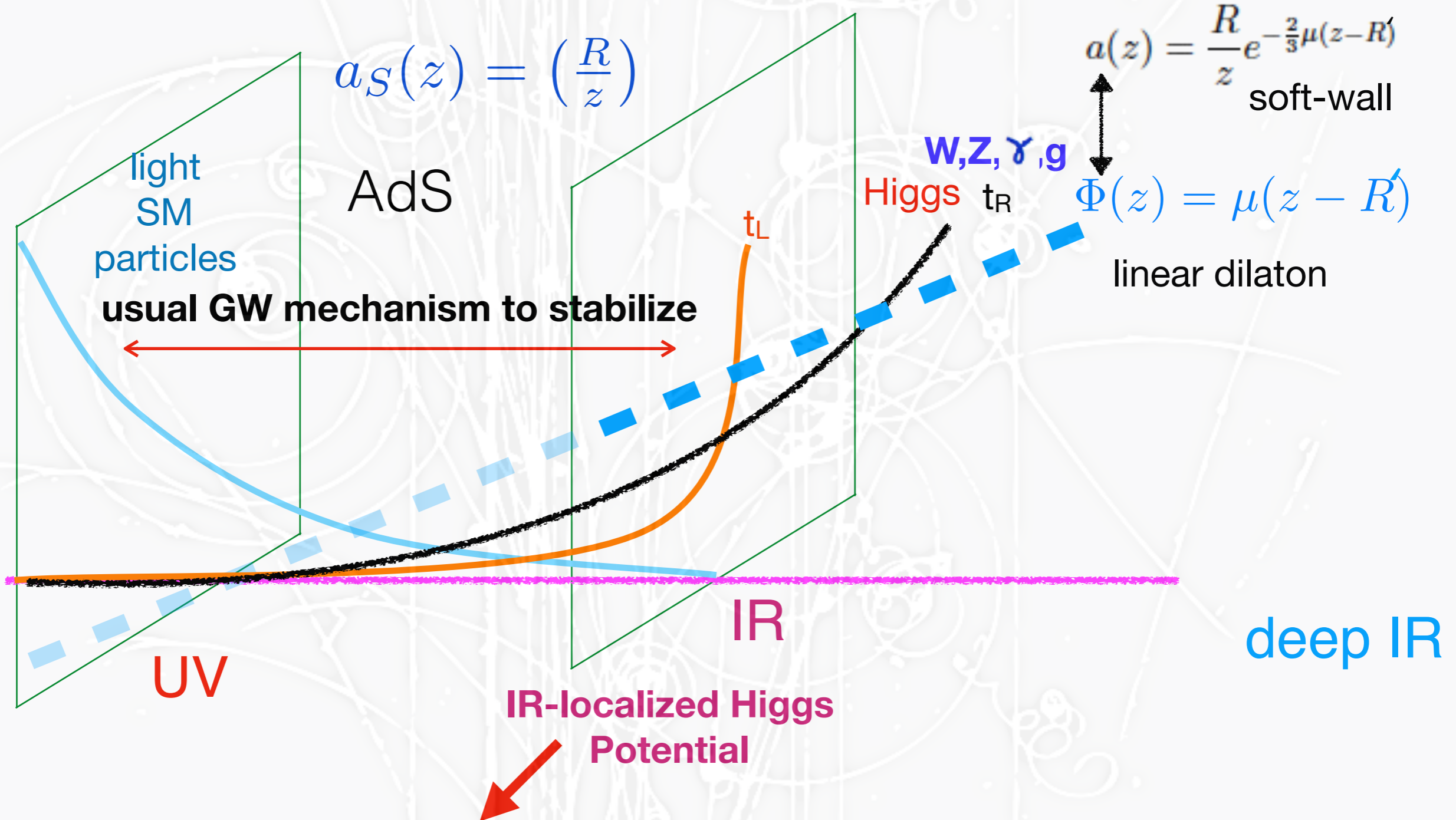
# A Natural Quantum Critical Higgs: 5D linear dilaton

Higgs arises from CFT with a domain wall (IR brane)



# A Natural Quantum Critical Higgs: 5D linear dilaton

Higgs arises from CFT with a domain wall (IR brane)



taking a pole (physical Higgs) out of CFT  
 => arises as a composite bound state of CFT

# A “more” Natural model: Linear Dilaton

$$i g_5 \int_R^{R'} A_5 dz$$

**bulk gauge symmetry  
broken down to**

$$SU(3)_c \times SO(4) \times U(1)_x$$

$$a(z) = \frac{R}{z} e^{-\frac{2}{3}\mu(z-R)}$$

soft-wall

**linear dilaton:**  
 $\Phi(z) = \mu(z - R)$

$$a_S(z) = \left(\frac{R}{z}\right)$$

$$SU(2) \times U(1)_Y$$

$$SO(5) \times U(1)_x$$

$$SO(4) \times U(1)_x$$

*W, Z,  $\gamma, g$*

*3rd generation,  
top partners*

light  
SM  
particles

PNGB Higgs

$A_5^a$

UV

IR

deep IR

theory gets closed to a fixed point, but then gets a mass gap

# A “more” Natural model: Linear Dilaton

PNGB Higgs: Wilson line with  $A_5$  (BC on IR brane)

$$ig_5 \int_R^{R'} A_5 dz$$

**bulk gauge symmetry  
broken down to**

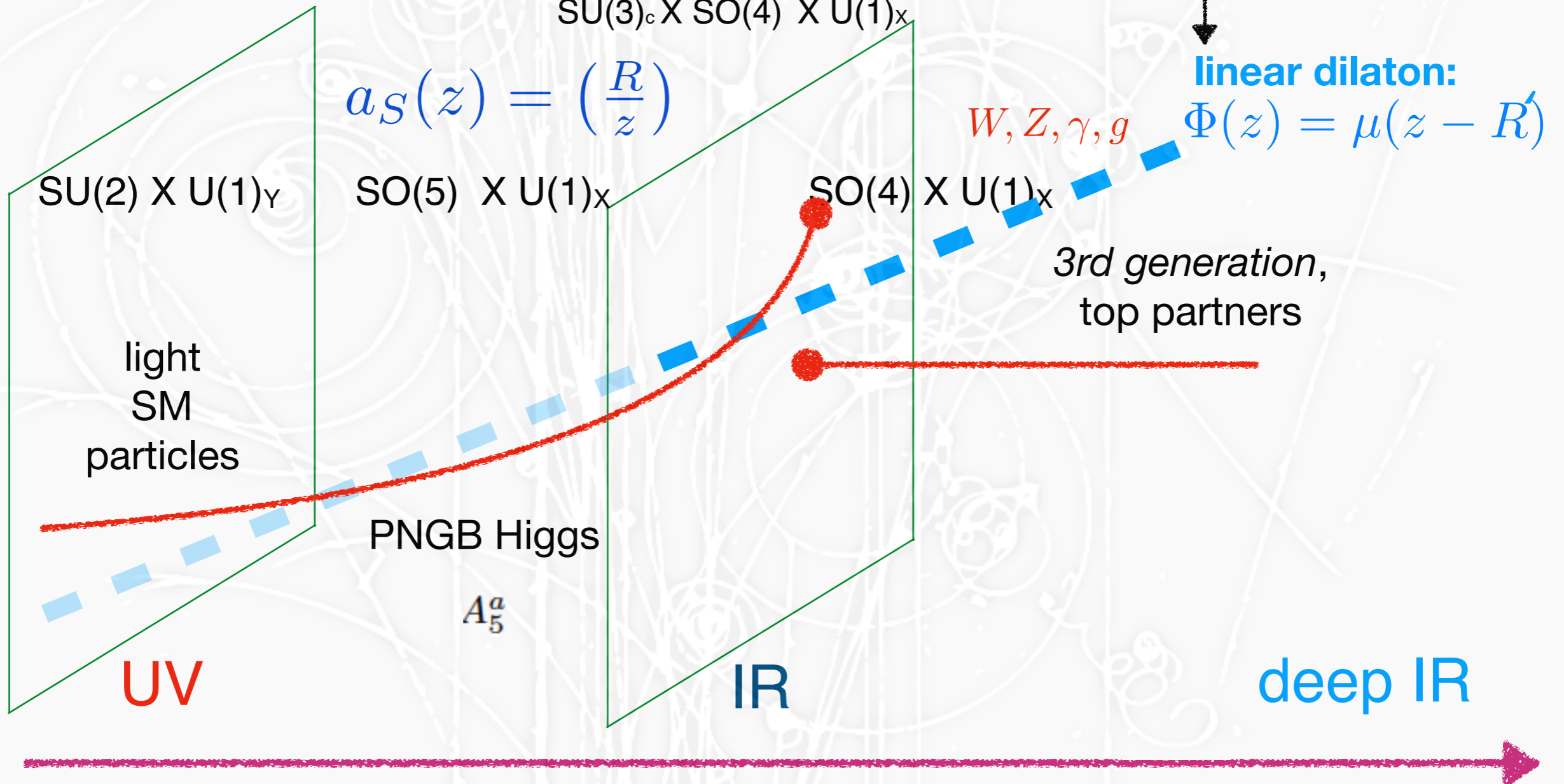
$$SU(3)_c \times SO(4) \times U(1)_x$$

$$a(z) = \frac{R}{z} e^{-\frac{2}{3}\mu(z-R)}$$

soft-wall

**linear dilaton:**  
 $\Phi(z) = \mu(z - R')$

$$a_S(z) = \left(\frac{R}{z}\right)$$



theory gets closed to a fixed point, but then gets a mass gap

# Continuum States

Csaki, Lombardo, Lee, SL, Telem

- ◆ To describe the continuum (for example Weyl fermions)

$$\mathcal{L}_\chi = -i\bar{\chi}\bar{\sigma}^\mu p_\mu \chi \quad \longrightarrow \quad \mathcal{L}_\chi^{\text{cont.}} = -i\bar{\chi} \frac{\bar{\sigma}^\mu p_\mu}{p^2 G(p^2)} \chi$$

- ◆  $G$  proportional to the 2-point function

$$\langle \bar{\chi} \chi \rangle^{\text{cont}} = i\sigma^\mu p_\mu G(p^2)$$

- ◆ Poles correspond to particles, branch cuts to continuum.

Characterized information written in terms of spectral density

$$G(p^2) = \int_0^\infty \frac{\rho(s)}{s - p^2 + i\epsilon} ds, \quad \rho(s) = \frac{1}{\pi} \text{Im}G(s)$$

# Unparticle Spectral densities (5D model)

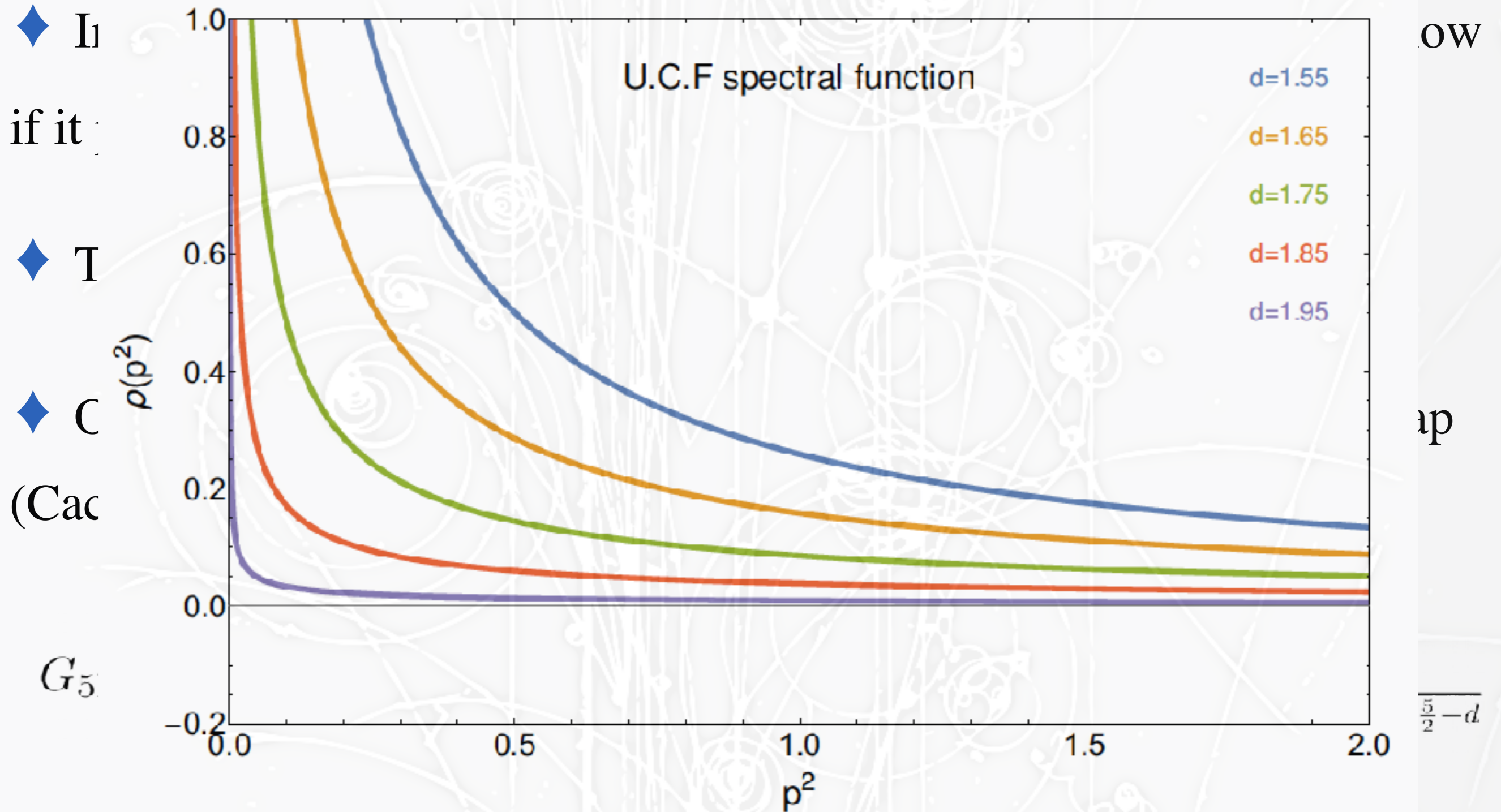
- ◆ In principle could just input the  $\rho(s)$  spectral density, but don't know if it provides unitary, causal QFT
- ◆ To make sure we don't use inconsistent  $\rho$ 's get them from 5D
- ◆ Old story: RS2 gives a model of continuum fermions without a gap (Cacciapaglia, Marandella, Terning)

$$G_{5D}(p^2) \propto \frac{\Gamma\left(\frac{1}{2} - c\right)}{4^c \Gamma\left(\frac{1}{2} + c\right)} \frac{1}{(-p^2)^{\frac{1}{2} - c}}$$

$$G_{4D}(p^2) \propto \frac{\Gamma\left(\frac{5}{2} - d\right)}{4^{d-2} \Gamma\left(d - \frac{3}{2}\right)} \frac{1}{(-p^2)^{\frac{5}{2} - d}}$$

- ◆ Boundary RS2 Green's fn = 4D ungapped continuum fermion (“unparticle”)

# Unparticle Spectral densities (5D model)



◆  $I_1$

if it

◆  $T$

◆  $C$

(Cac

$G_5$

OW

ap

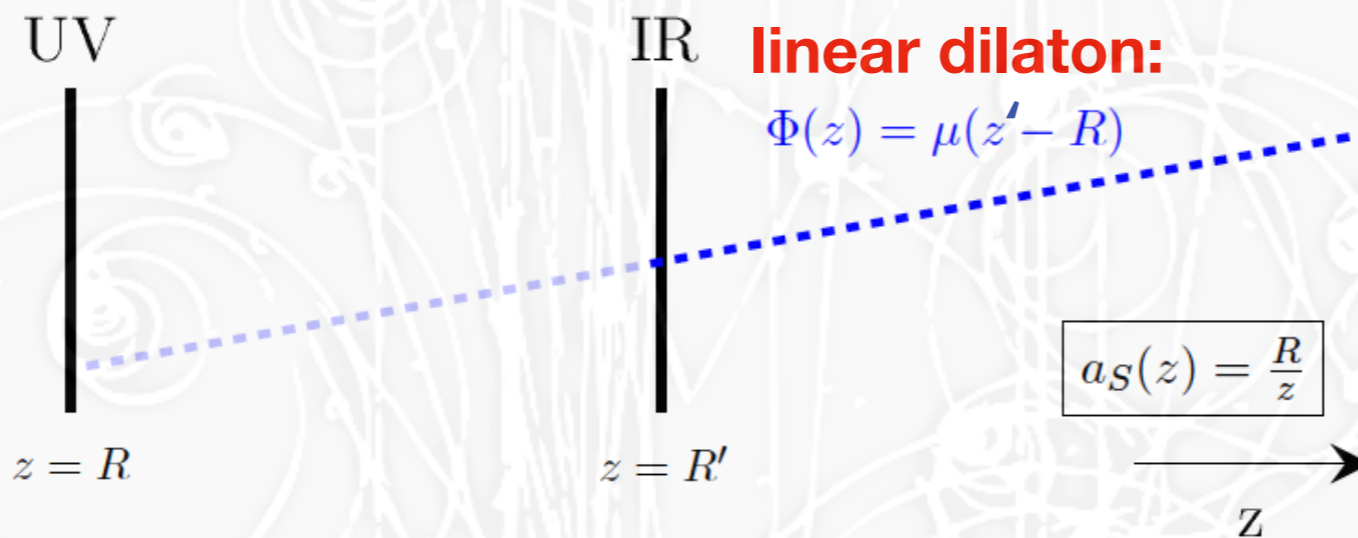
$\frac{1}{2} - d$

◆ Boundary RS2 Green's fn = 4D ungapped continuum fermion ("unparticle")

# Gapped Continuum

Csaki, Lombardo, Lee, SL, Telem

- ◆ To introduce mass gap, we need to modify the 5D background
- ◆ Introduce linear dilaton into AdS



- ◆  $\Phi(z)$  linear dilaton - around the UV brane vanishing

➡ won't have effect until IR ( $z \sim 1/\mu$ )

- ◆ Linear dilaton models the details of the IR dynamics (e.g. theory modified by dynamics of some **composite mesons** below IR scale, leading into **gapped continuum**)



# Gapped Continuum

Csaki, Lombardo, Lee, SL, Telem

- ◆ Fermion EOM's in this background can be solved exactly

- ◆ Fermion Lagrangian in “string frame”  $a_S(z) = \frac{R}{z}$

$$\mathcal{L}_S = e^{-2\Phi(z)} a_S^5(z) \left[ a_S^{-1}(z) \mathcal{L}_{\text{kin}} + \frac{1}{R} (c + y\Phi(z)) (\psi\chi + \bar{\chi}\bar{\psi}) \right]$$



bulk Yukawa coupling between the dilaton and the bulk fermion

- ◆ Kinetic term conventional

$$\mathcal{L}_{\text{kin}} = -i\bar{\chi}\bar{\sigma}^\mu p_\mu\chi - i\psi\sigma^\mu p_\mu\bar{\psi} + \frac{1}{2} \left( \psi \overleftrightarrow{\partial}_5 \chi - \bar{\chi} \overleftrightarrow{\partial}_5 \bar{\psi} \right)$$

- ◆ Go to Einstein frame to see physics best  $a(z) = a_S(z) e^{-\frac{2}{3}\Phi(z)}$

$$\mathcal{L}_E = a^4(z) \mathcal{L}_{\text{kin}} + a^5(z) \frac{\hat{c}(z)}{R} (\psi\chi + \bar{\chi}\bar{\psi})$$

- ◆ Effective mass parameter  $\hat{c}(z) \equiv (c + y\Phi(z)) e^{\frac{2}{3}\Phi(z)}$

# Solutions to the bulk equations

Csaki, Lombardo, Lee, SL, Telem

- ◆ Schrödinger form for the EOM

$$-\hat{\chi}''(z) + V_{\text{eff}}(z) \hat{\chi}(z) = p^2 \hat{\chi}(z), \quad \hat{\chi}(z) = \left(\frac{R}{z}\right)^2 \chi(z)$$

- ◆ Effective potential

$$V_{\text{eff}}(z) = \frac{c(c+1) + y\Phi(z)(2c + y\Phi(z) + 1) - yz\Phi'(z)}{z^2}$$

- ◆ Gapped continuum if  $V_{\text{eff}}(z \rightarrow \infty) = \text{const} > 0$

- ◆ To achieve that, need a linear dilaton

$$\Phi(z) = \mu(z - R) \text{ with } \mu \sim 1 \text{ TeV}$$

- ◆ will give:  $V_{\text{eff}}(z \rightarrow \infty) = y^2 \mu^2$

 gap will show at  $y\mu$

# Gapped Continuum

Csaki, Lombardo, Lee, SL, Telem

## ◆ 5D holographic model with a linear dilaton

$$S_f = \int d^5x a(z)^4 \bar{\Psi} \left( i\gamma^M \partial_M + 2i \frac{a'(z)}{a(z)} \gamma^5 - \frac{a(z)c(z)}{R} \right)$$

$$c(z) = (c + \mu(z - R)) e^{\frac{2}{3}\mu(z-R)}$$

$$-i\bar{\sigma}^\mu \partial_\mu \chi - \partial_5 \bar{\psi} - 2 \frac{a'}{a} \bar{\psi} + \frac{ac}{R} \bar{\psi} = 0$$

$$-i\sigma^\mu \partial_\mu \bar{\psi} + \partial_5 \chi + 2 \frac{a'}{a} \chi + \frac{ac}{R} \chi = 0.$$

$$\chi = g(z) \chi(z)$$

$$\bar{\psi}(z) = f(z) \bar{\psi}(x)$$

$$\chi(z) = A a^{-2}(z) W \left( -\frac{c\mu y}{\Delta}, c + \frac{1}{2}, 2\Delta z \right),$$

$$\psi(z) = A a^{-2}(z) W \left( -\frac{c\mu y}{\Delta}, c - \frac{1}{2}, 2\Delta z \right) \frac{\mu y - \Delta}{p},$$

# Gapped Continuum

Csaki, Lombardo, Lee, SL, Telem

## ◆ 5D holographic model with a linear dilaton

$$S_f = \int d^5x a(z)^4 \bar{\Psi} \left( i\gamma^M \partial_M + 2i \frac{a'(z)}{a(z)} \gamma^5 - \frac{a(z)c(z)}{R} \right)$$

$$c(z) = (c + \mu(z - R)) e^{\frac{2}{3}\mu(z-R)}$$

$$-i\bar{\sigma}^\mu \partial_\mu \chi - \partial_5 \bar{\psi} - 2 \frac{a'}{a} \bar{\psi} + \frac{ac}{R} \bar{\psi} = 0$$

$$-i\sigma^\mu \partial_\mu \bar{\psi} + \partial_5 \chi + 2 \frac{a'}{a} \chi + \frac{ac}{R} \chi = 0.$$

$$\chi = g(z) \chi(z)$$

$$\bar{\psi}(z) = f(z) \bar{\psi}(x)$$

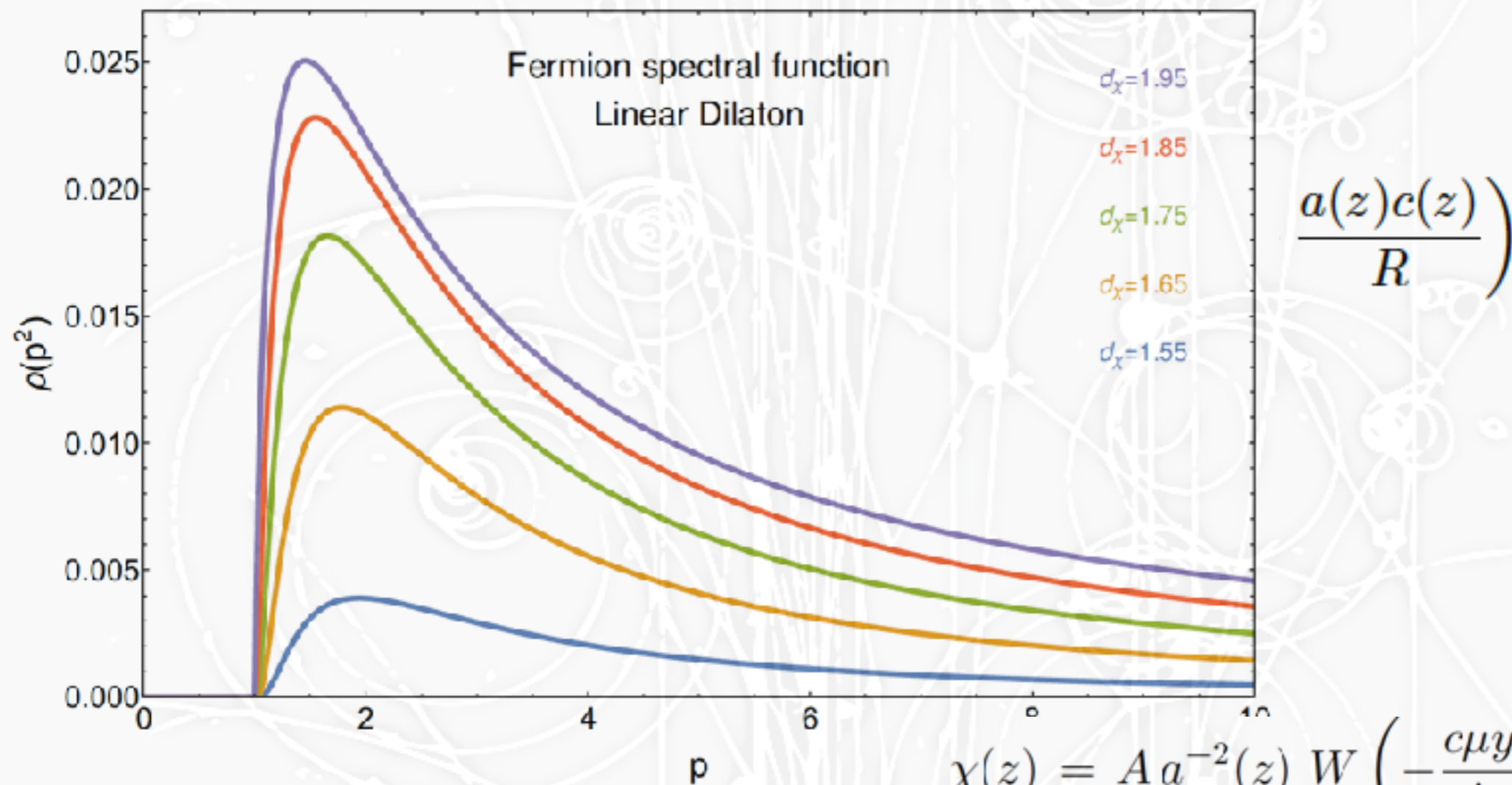
$$\chi(z) = A a^{-2}(z) W \left( -\frac{c\mu y}{\Delta}, c + \frac{1}{2}, 2\Delta z \right),$$

$$\psi(z) = A a^{-2}(z) W \left( -\frac{c\mu y}{\Delta}, c - \frac{1}{2}, 2\Delta z \right) \frac{\mu y - \Delta}{p},$$

- profile of continuum depends on the scaling dimension of the fields

# Gapped Continuum

Csaki, Lombardo, Lee, SL, Telem



$$\chi(z) = A a^{-2}(z) W \left( -\frac{c\mu y}{\Delta}, c + \frac{1}{2}, 2\Delta z \right),$$

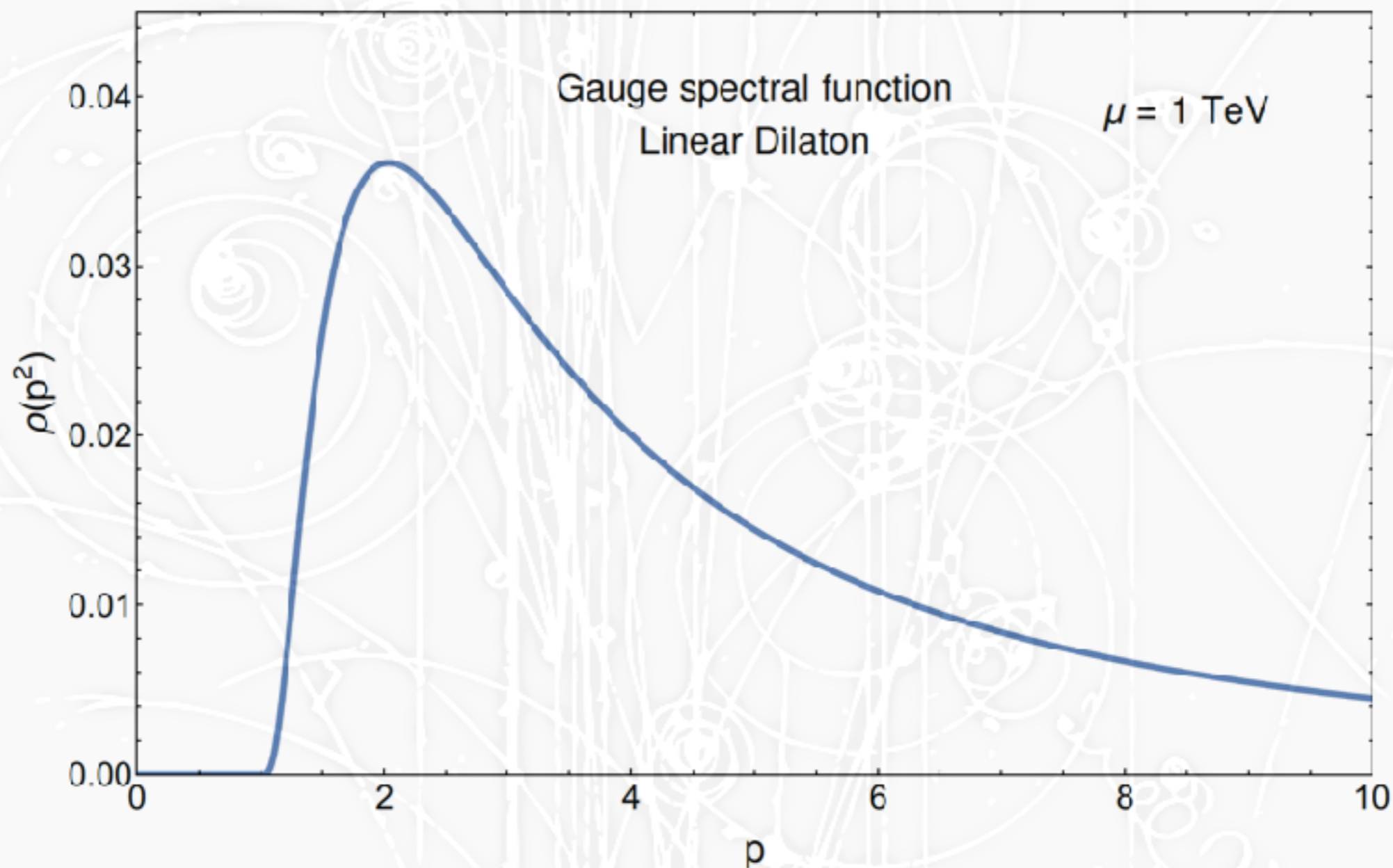
$$\psi(z) = A a^{-2}(z) W \left( -\frac{c\mu y}{\Delta}, c - \frac{1}{2}, 2\Delta z \right) \frac{\mu y - \Delta}{p},$$

- profile of continuum depends on the scaling dimension of the fields

# Gapped Continuum

Csaki, Lombardo, Lee, SL, Telem

## ◆ Similar story for Gauge Boson



$$\rho(s) = \frac{1}{\pi} \overline{\lim}_{z \rightarrow 0} \text{Im} \frac{A(z)}{A'(z)} = \frac{1}{2\pi s} \left[ 1 + i\psi \left( \frac{1}{2} + \frac{\mu}{2\Delta} \right) - i\psi \left( \frac{1}{2} - \frac{\mu}{2\Delta} \right) \right]$$

# A Realistic Model

◆ Need the usual Composite Higgs setup in addition

◆ Bulk gauge group  $G = SO(5) \times U(1)_X \rightarrow SO(4) \times U(1)_X$   
breaking on IR brane via BCs

◆ On UV brane,  $G = SO(5) \times U(1)_X \rightarrow SU(2)_L \times U(1)_Y$   
 $Y = T_R^3 + X$

◆ Wilson line for Higgs:  $ig_5 \int_R^{R'} A_5 dz$   
(No other physical Wilson line beyond IR brane)

◆ Bulk fermions

$$Q_L(\mathbf{5})_{\frac{2}{3}} \rightarrow q_L(\mathbf{2})_{\frac{1}{6}} + \tilde{q}_L(\mathbf{2})_{\frac{7}{6}} + y_L(\mathbf{1})_{\frac{2}{3}},$$

$$T_R(\mathbf{5})_{\frac{2}{3}} \rightarrow q_R(\mathbf{2})_{\frac{1}{6}} + \tilde{q}_R(\mathbf{2})_{\frac{7}{6}} + t_R(\mathbf{1})_{\frac{2}{3}},$$

$$B_R(\mathbf{10})_{\frac{2}{3}} \rightarrow q'_R(\mathbf{2})_{\frac{1}{6}} + \tilde{q}'_R(\mathbf{2})_{\frac{7}{6}} + x_R(\mathbf{3})_{\frac{2}{3}} + y_R(\mathbf{1})_{\frac{7}{6}} + \tilde{y}_R(\mathbf{1})_{\frac{1}{6}} + b_R(\mathbf{1})_{-\frac{1}{3}}$$

# A Realistic Model

- ◆ To generate Yukawa couplings, need localized mass terms

$$S_{\text{IR}} = \int d^4x \sqrt{g_{\text{ind}}} \left[ M_1 \bar{z}_L t_R + M_4 (\bar{q}_L q_R + \bar{\tilde{q}}_L \tilde{q}_R) + M_b (\bar{q}_L q'_R + \bar{\tilde{q}}_L \tilde{q}'_R) \right]$$

- ◆ A realistic benchmark point

$$R/R' = 10^{-16}, \quad 1/R' = 2.81 \text{ TeV}, \quad \mu = 1 \text{ TeV}, \quad y = 1.75,$$

$$r = 0.975, \quad \sin \theta = 0.39,$$

$$c_Q = 0.2, \quad c_T = -0.22, \quad c_B = -0.03,$$

$$M_1 = 1.2, \quad M_4 = 0, \quad M_b = 0.017.$$

- ◆ All SM parameters correctly reproduced with top slightly a bit light
- ◆ Choose safe point where gauge cont. at 1 TeV, fermion at 1.75 TeV



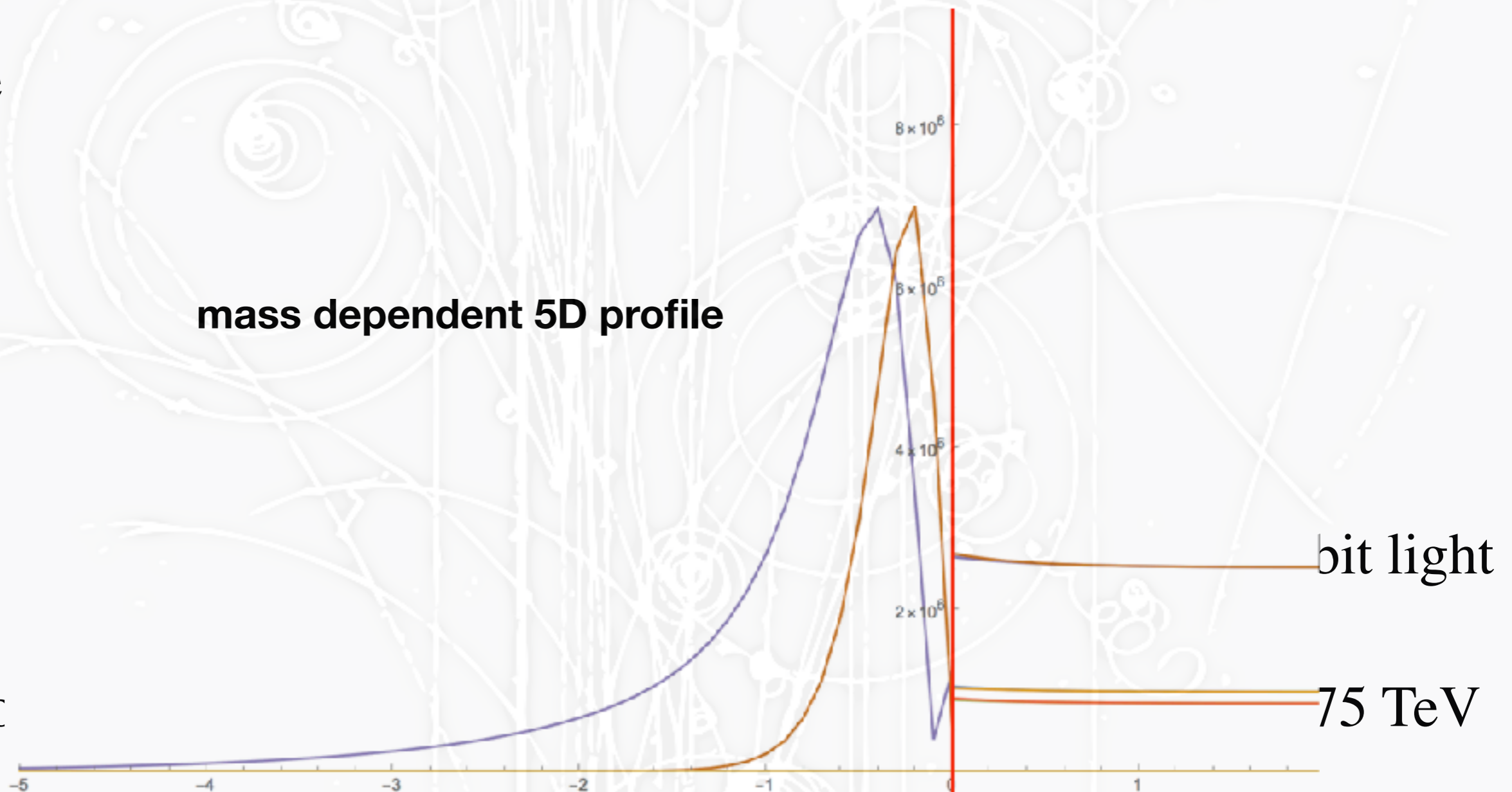
# A Realistic Model

- ◆ To generate Yukawa couplings, need localized mass terms

$$S_{\text{IR}} = \int d^4x \sqrt{g_{\text{ind}}} \left[ M_1 \bar{z}_L t_R + M_4 (\bar{q}_L q_R + \bar{\tilde{q}}_L \tilde{q}_R) + M_b (\bar{q}_L q'_R + \bar{\tilde{q}}_L \tilde{q}'_R) \right]$$

- ◆ Are

mass dependent 5D profile

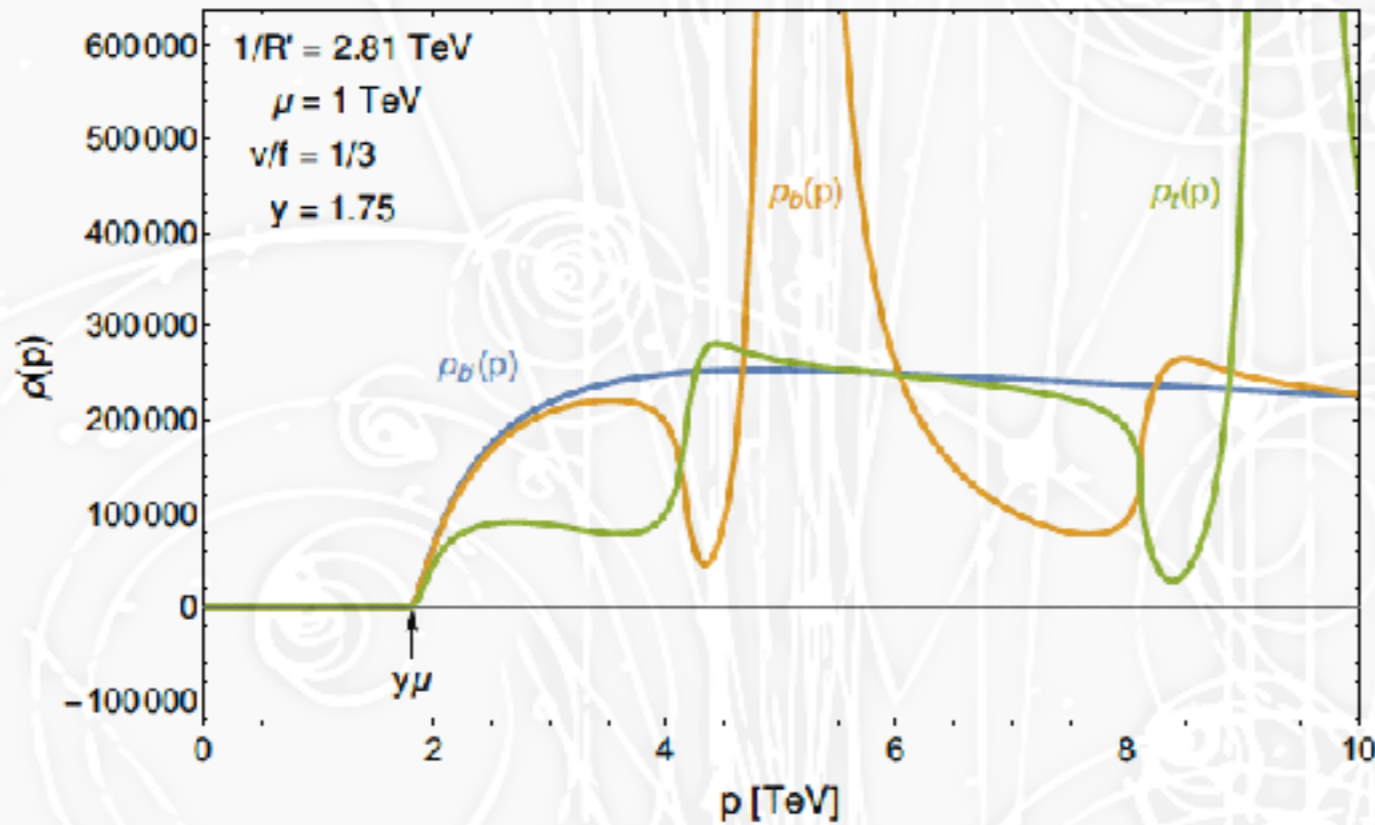


- ◆ All

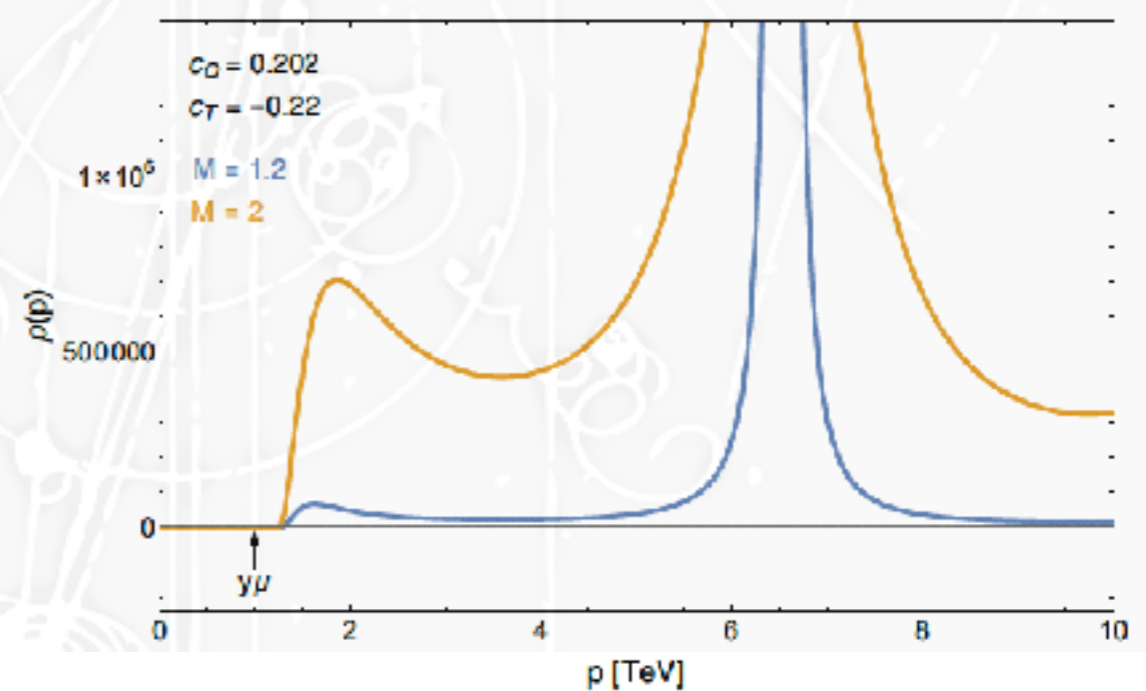
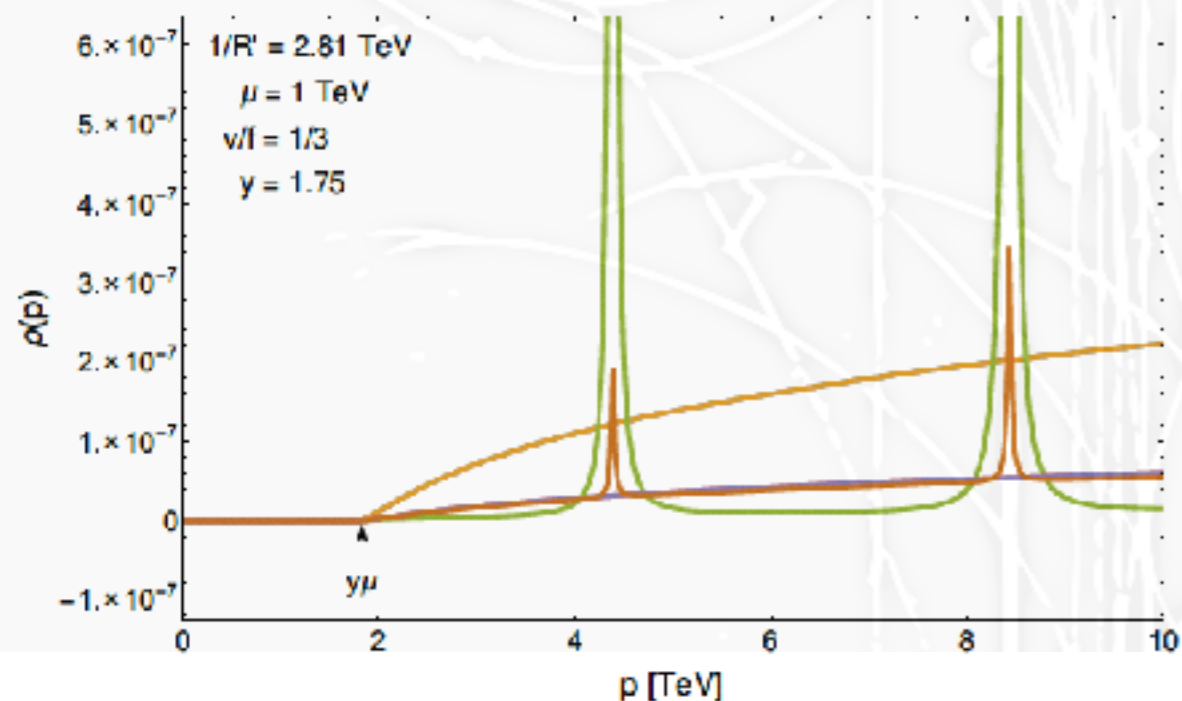
- ◆ Chc

# Fermionic Spectrum

- ◆ Fermion spectral densities. 3rd generation all very broad



- ◆ Exotic top partners- model dependent, could be probed as resonance at 100TeV collider

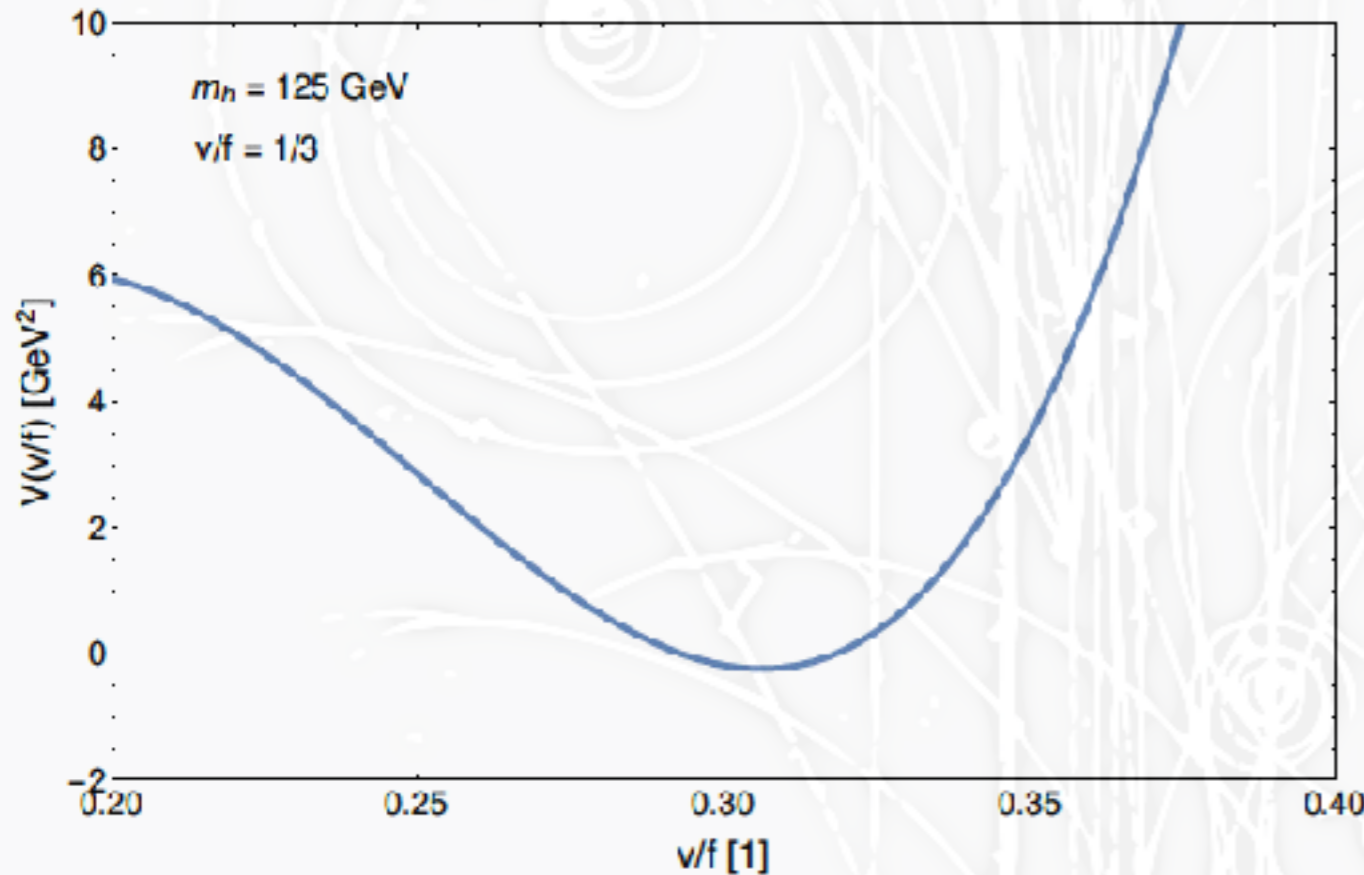


# Continuum Top Partners

Csaki, Lombardo, Lee, SL, Telem; to appear soon

◆ Higgs Potential: 
$$V(h) = \frac{3}{16\pi^2} \int dp p^3 \left[ -4 \sum_{j=1}^{20} \log G_{f_j}(ip) + \sum_{k=1}^4 \log G_{g_k}(ip) \right]$$

tuning = 
$$\left[ \max_i \frac{d \log v}{d \log p_i} \right]^{-1} \quad p_i \in \{R, R', \mu, r, \theta, y, c_Q, c_T, c_B, M_1, m_4, M_d\}$$



$$R/R' = 10^{-16}, \quad 1/R' = 2.81 \text{ TeV}, \quad \mu = 1 \text{ TeV}, \quad y = 1.75,$$

$$r = 0.975, \quad \sin \theta = 0.39,$$

$$c_Q = 0.2, \quad c_T = -0.22, \quad c_B = -0.03,$$

$$M_1 = 1.2, \quad M_4 = 0, \quad M_b = 0.017.$$

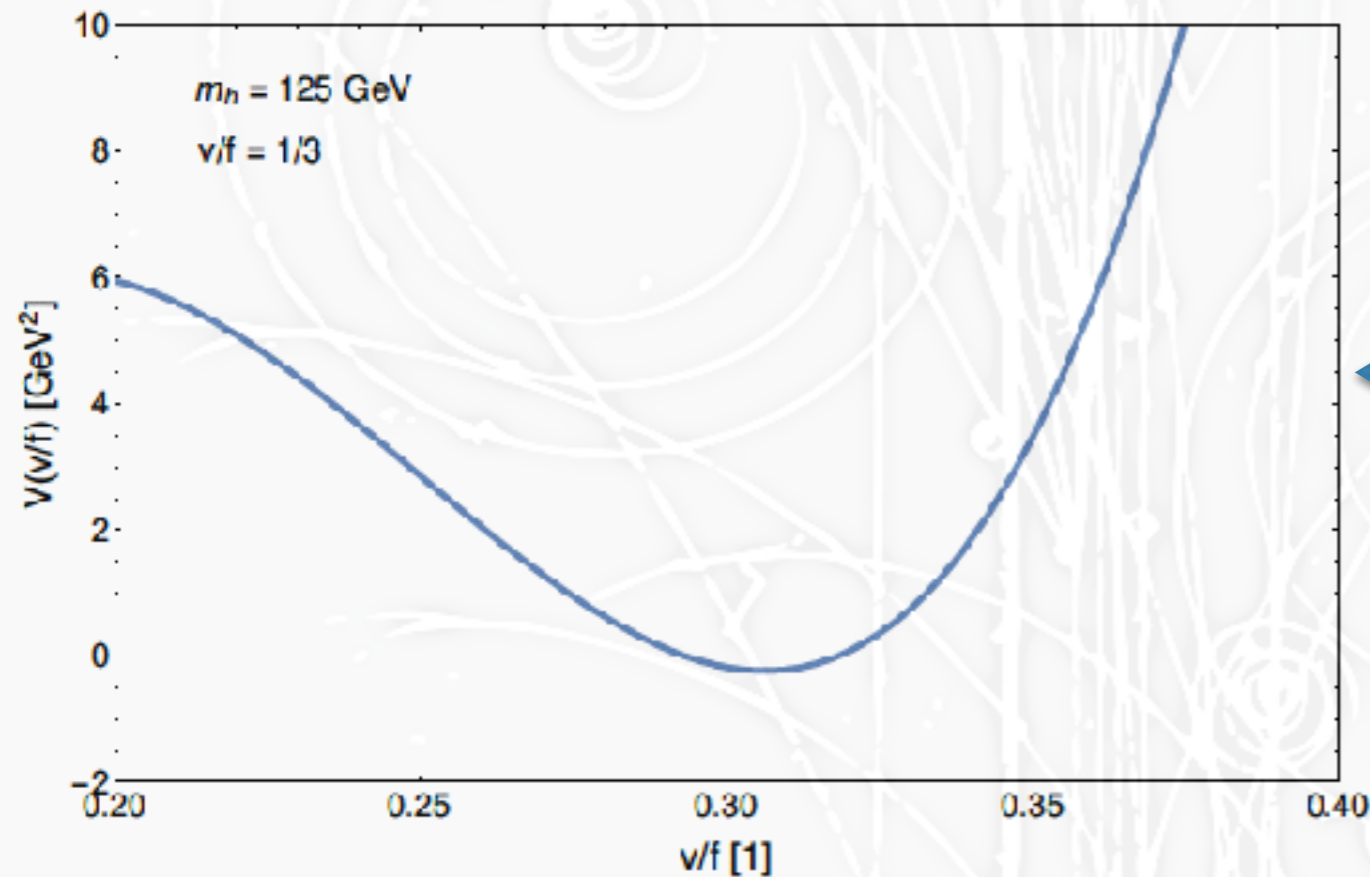
fermion continuum starts at  $y\mu = 1.75 \text{ TeV}$

# Continuum Top Partners

Csaki, Lombardo, Lee, SL, Telem; to appear soon

◆ Higgs Potential: 
$$V(h) = \frac{3}{16\pi^2} \int dp p^3 \left[ -4 \sum_{j=1}^{20} \log G_{f_j}(ip) + \sum_{k=1}^4 \log G_{g_k}(ip) \right]$$

tuning = 
$$\left[ \max_i \frac{d \log v}{d \log p_i} \right]^{-1} \quad p_i \in \{R, R', \mu, r, \theta, y, c_Q, c_T, c_B, M_1, m_4, M_d\}$$



→ usual  
1% tuning

with our conservative choice of  
parameters

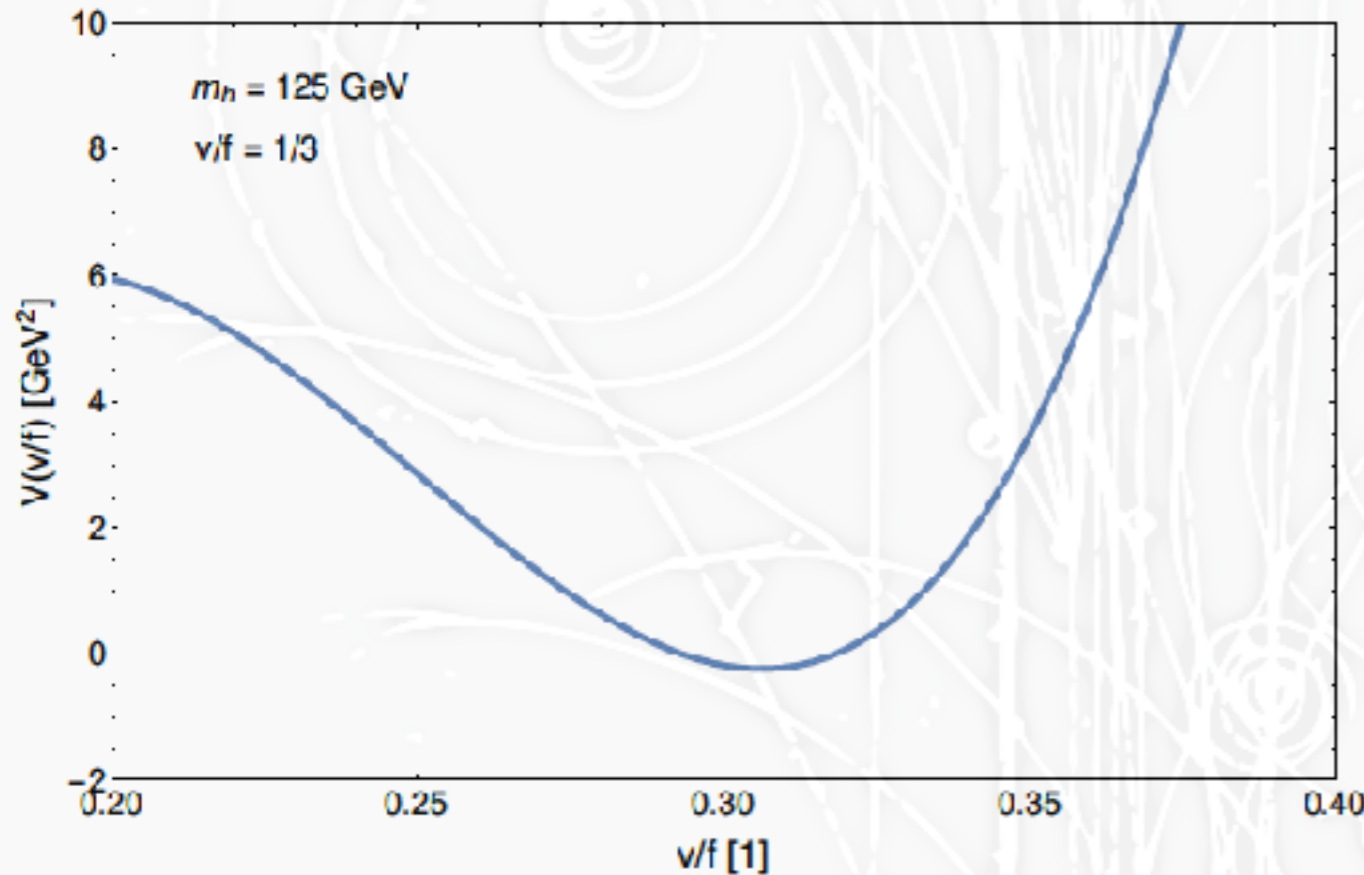
fermion continuum starts at  $y\mu = 1.75 \text{ TeV}$

# Continuum Top Partners

Csaki, Lombardo, Lee, SL, Telem; to appear soon

◆ Higgs Potential: 
$$V(h) = \frac{3}{16\pi^2} \int dp p^3 \left[ -4 \sum_{j=1}^{20} \log G_{f_j}(ip) + \sum_{k=1}^4 \log G_{g_k}(ip) \right]$$

tuning = 
$$\left[ \max_i \frac{d \log v}{d \log p_i} \right]^{-1} \quad p_i \in \{R, R', \mu, r, \theta, y, c_Q, c_T, c_B, M_1, m_4, M_d\}$$



$$R/R' = 10^{-16}, \quad 1/R' = 2.81 \text{ TeV}, \quad \mu = 1 \text{ TeV}, \quad y = 1.75,$$

$$r = 0.975, \quad \sin \theta = 0.39,$$

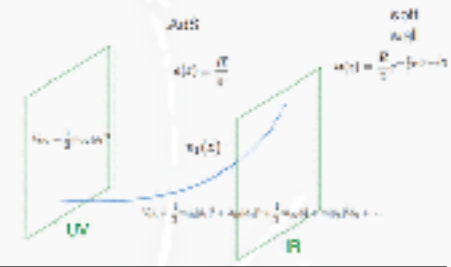
$$c_Q = 0.2, \quad c_T = -0.22, \quad c_B = -0.03,$$

$$M_1 = 1.2, \quad M_4 = 0, \quad M_b = 0.017.$$

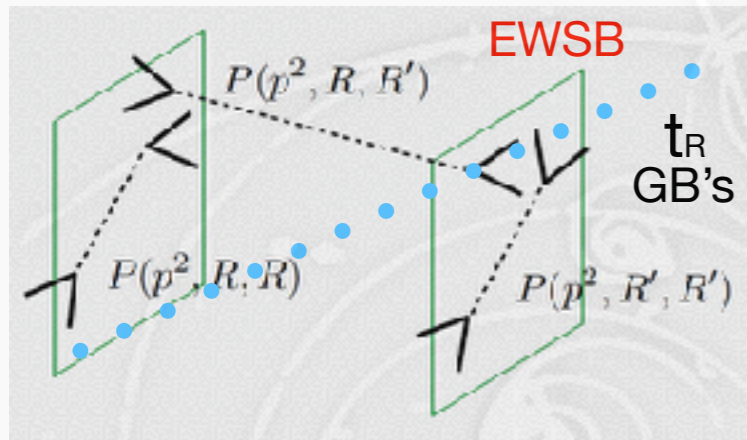
fermion continuum starts at  $y\mu = 1.75 \text{ TeV}$

# Continuum Naturalness?

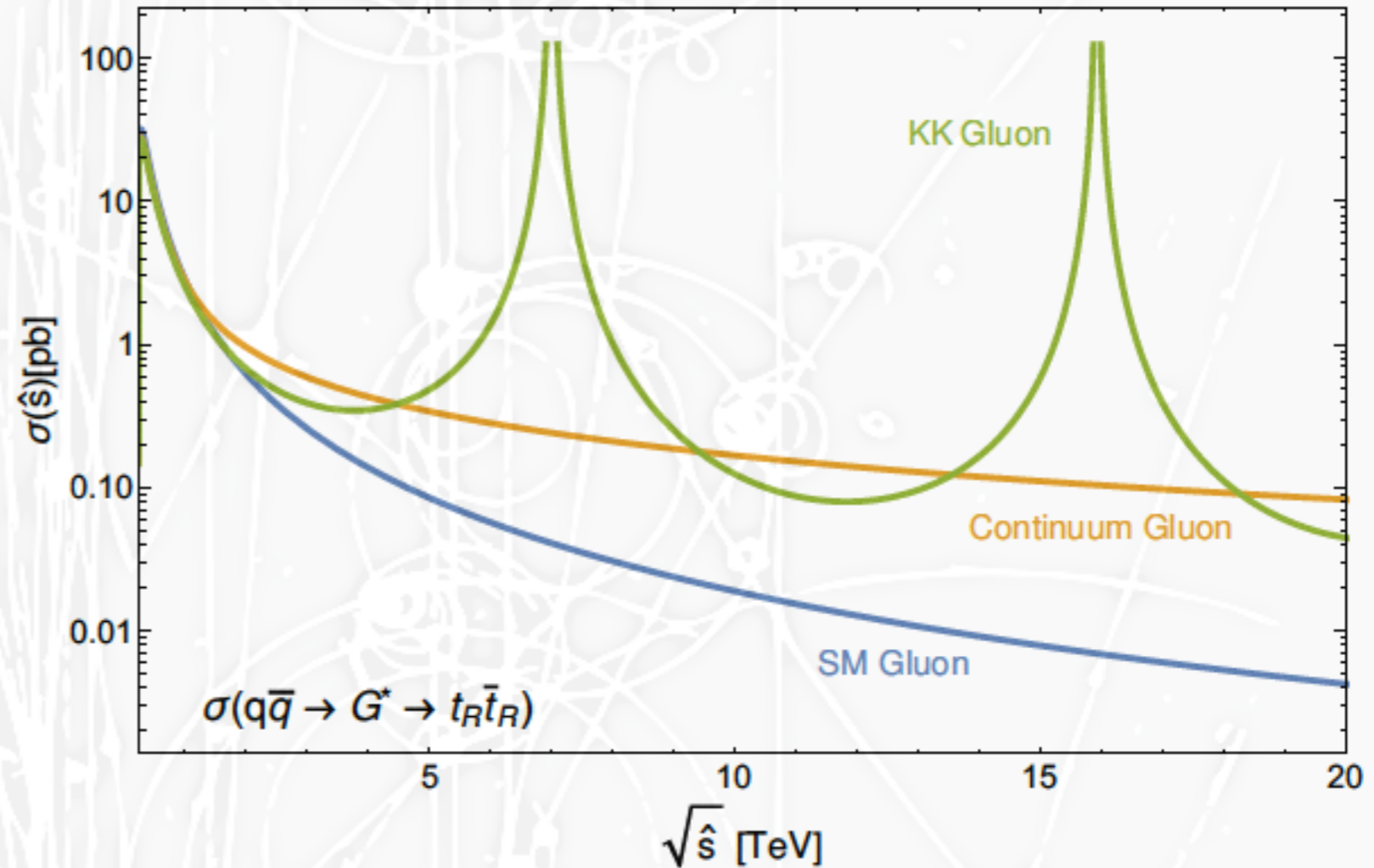
Csaki, Lombardo, Lee, SL, Telem



- ◆ New Physics (e.g. Top partner) appear solely as a continuum
  - KK gluon / colored  $\rho_c$

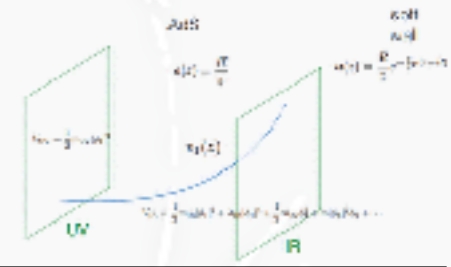


$$\mathcal{L}_E = a(z) e^{-\frac{4}{3}\mu(z-R)} \left[ \frac{1}{4} F^{MN} F_{MN} \right]$$

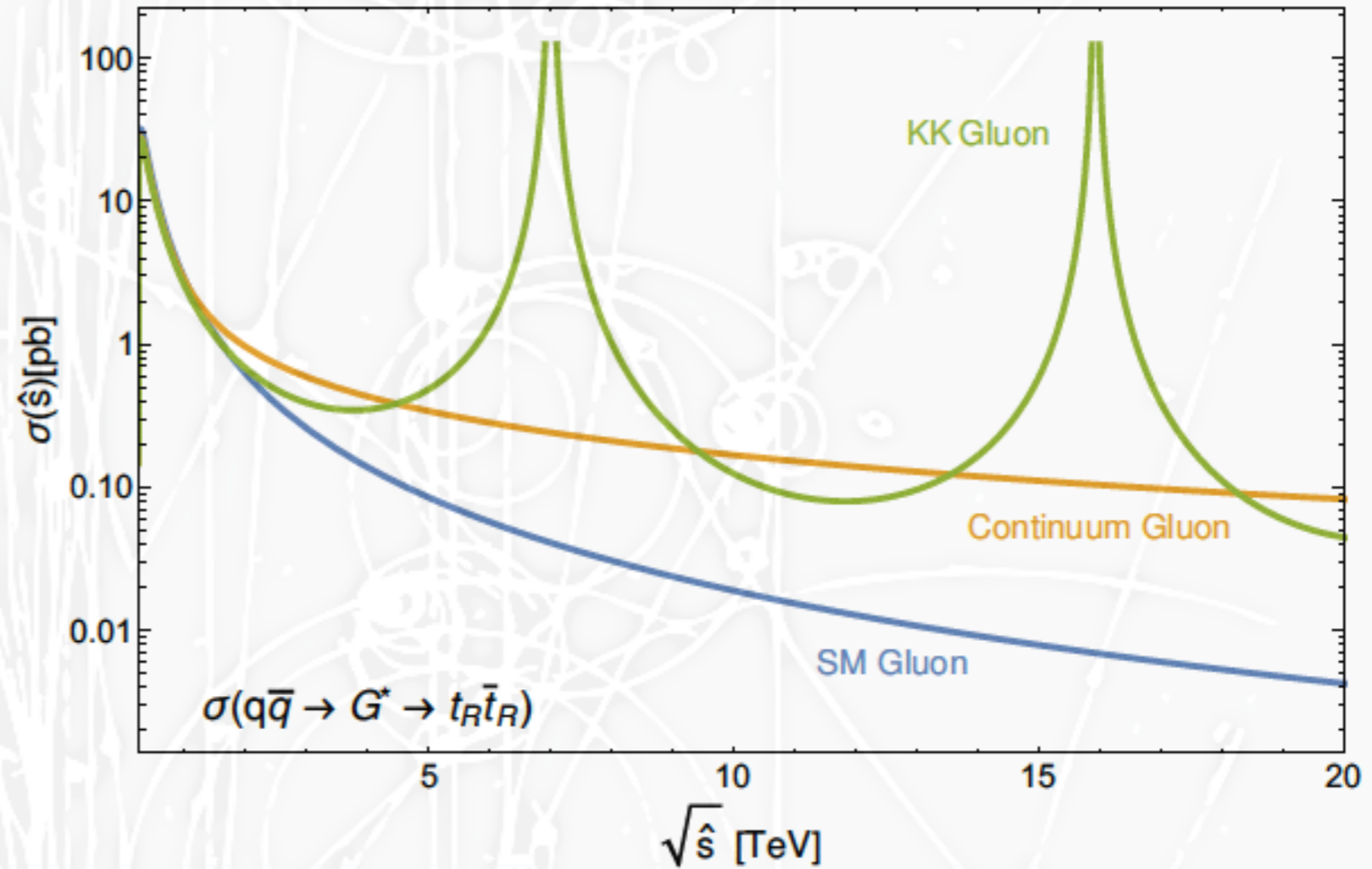
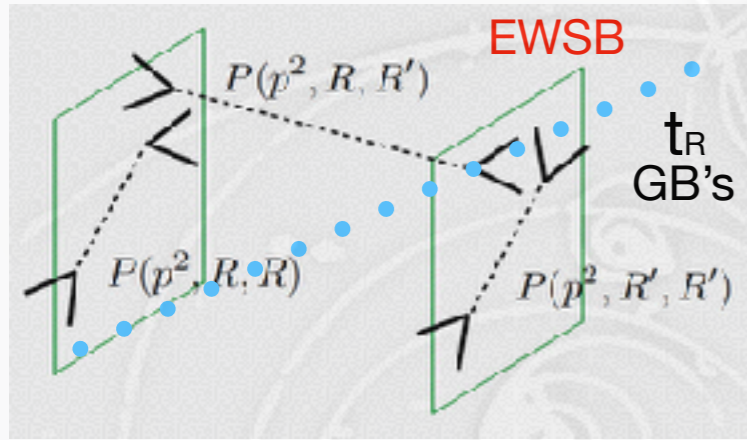


# Continuum Naturalness?

Csaki, Lombardo, Lee, SL, Telem



- ◆ New Physics (e.g. Top partner) appear solely as a continuum
  - KK gluon / colored  $\rho_c$



$$\mathcal{L}_E = a(z) e^{-\frac{4}{3}\mu(z-R)} \left[ \frac{1}{4} F^{MN} F_{MN} \right]$$

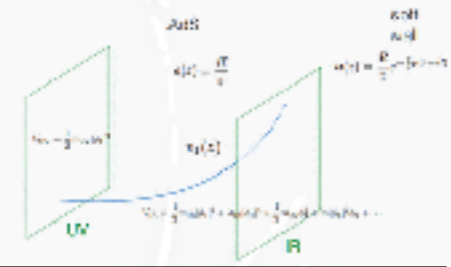
$$-\hat{A}''(z) + V_{\text{eff}}(z)\hat{A}(z) = p^2\hat{A}(z)$$

$$\hat{A}(z) = \sqrt{\frac{R}{z}} e^{-\mu(z-R)} A(z)$$

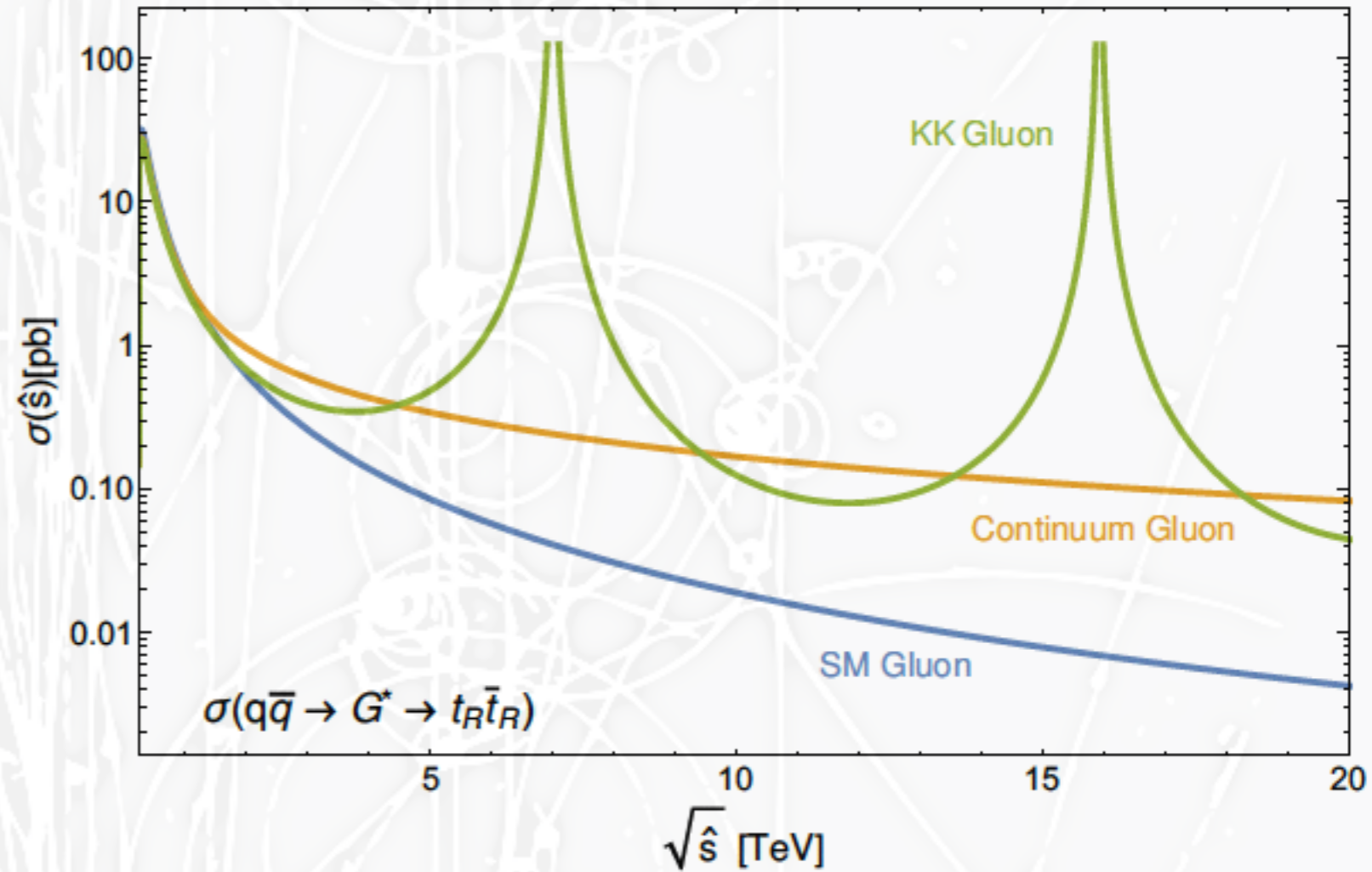
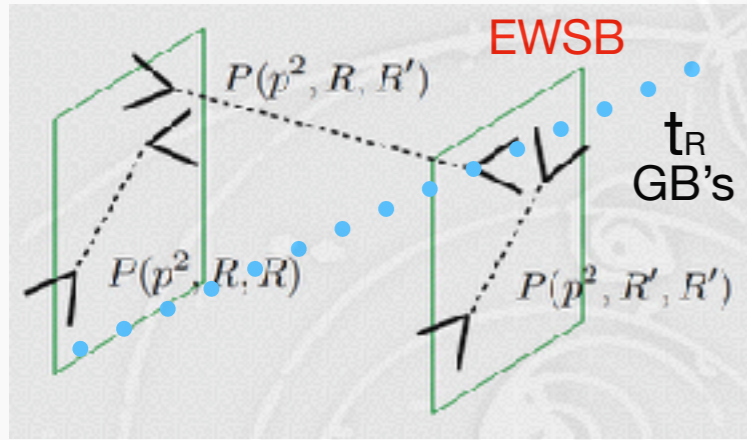
$$V_{\text{eff}}(z) = \mu^2 + \frac{\mu}{z} + \frac{3}{4z^2}$$

# Continuum Naturalness?

Csaki, Lombardo, Lee, SL, Telem



- ◆ New Physics (e.g. Top partner) appear solely as a continuum
  - KK gluon / colored  $\rho_c$



$$\mathcal{L}_E = a(z) e^{-\frac{4}{3}\mu(z-R)} \left[ \frac{1}{4} F^{MN} F_{MN} \right]$$

$$-\hat{A}''(z) + V_{\text{eff}}(z)\hat{A}(z) = p^2\hat{A}(z)$$

$$\hat{A}(z) = \sqrt{\frac{R}{z}} e^{-\mu(z-R)} A(z)$$

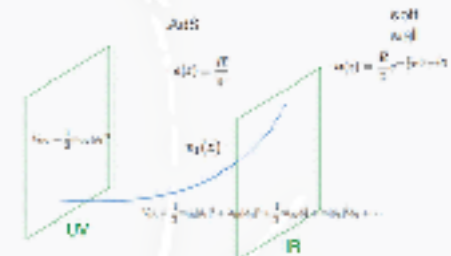
$$V_{\text{eff}}(z) = \mu^2 + \frac{\mu}{z} + \frac{3}{4z^2}$$

$$V_{\text{eff}}(z \rightarrow \infty) = \mu^2$$

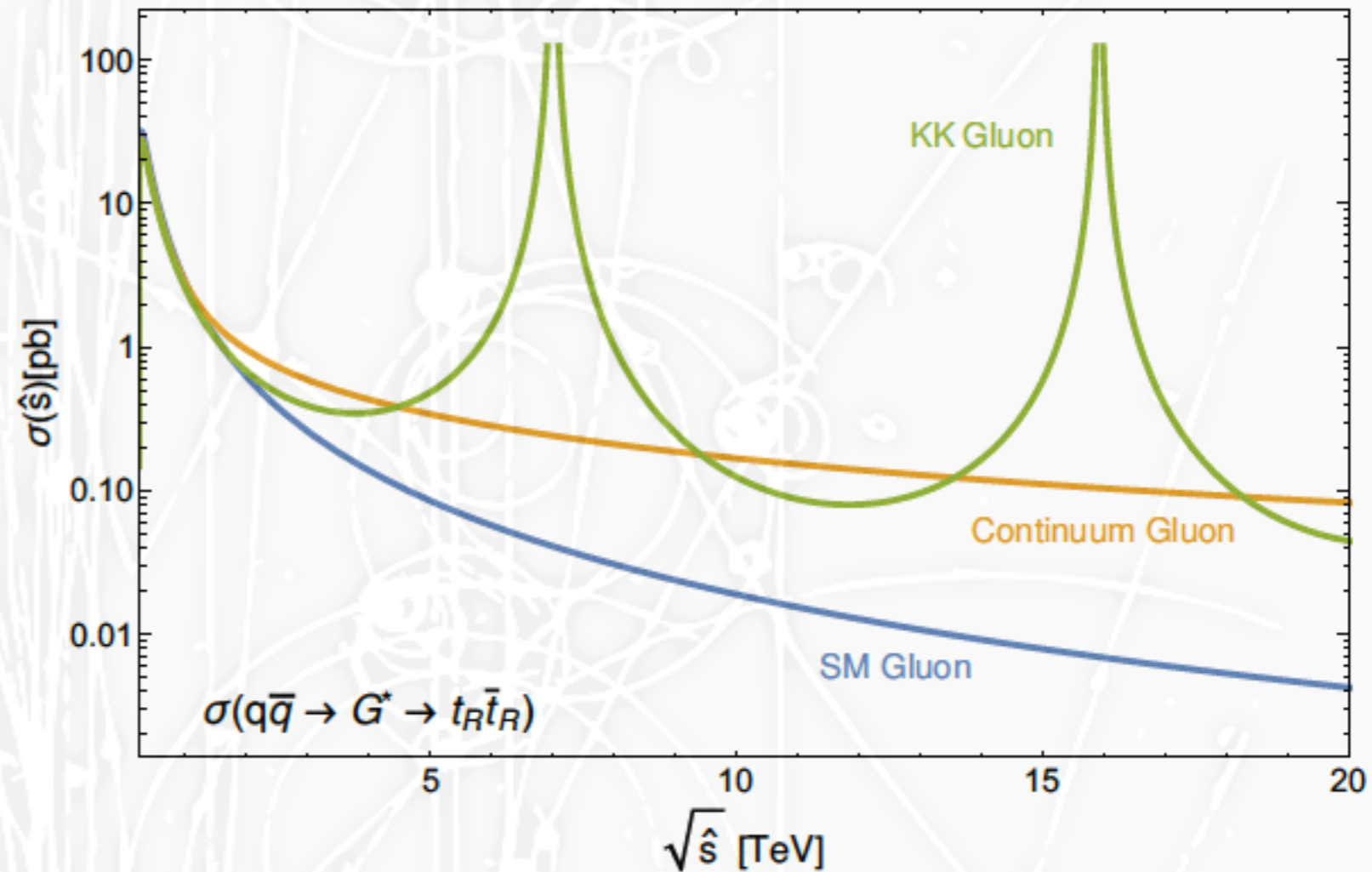
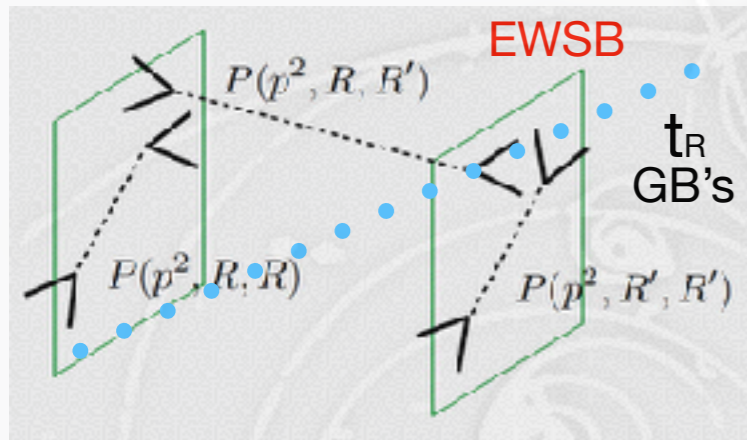


# Continuum Naturalness?

Csaki, Lombardo, Lee, SL, Telem



- ◆ New Physics (e.g. Top partner) appear solely as a continuum
  - KK gluon / colored  $\rho_c$



$$\mathcal{L}_E = a(z) e^{-\frac{4}{3}\mu(z-R)} \left[ \frac{1}{4} F^{MN} F_{MN} \right]$$

$$-\hat{A}''(z) + V_{\text{eff}}(z)\hat{A}(z) = p^2\hat{A}(z)$$

$$\hat{A}(z) = \sqrt{\frac{R}{z}} e^{-\mu(z-R)} A(z)$$

$$V_{\text{eff}}(z) = \mu^2 + \frac{\mu}{z} + \frac{3}{4z^2}$$

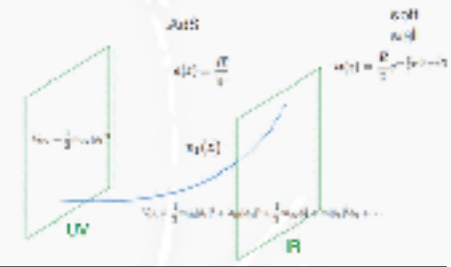
$$A(z) = A \sqrt{\frac{z}{R}} e^{\mu(z-R)} W\left(-\frac{\mu}{2\Delta}, 1; 2\Delta z\right) \quad \Delta = \sqrt{\mu^2 - p^2}$$

$$V_{\text{eff}}(z \rightarrow \infty) = \mu^2$$

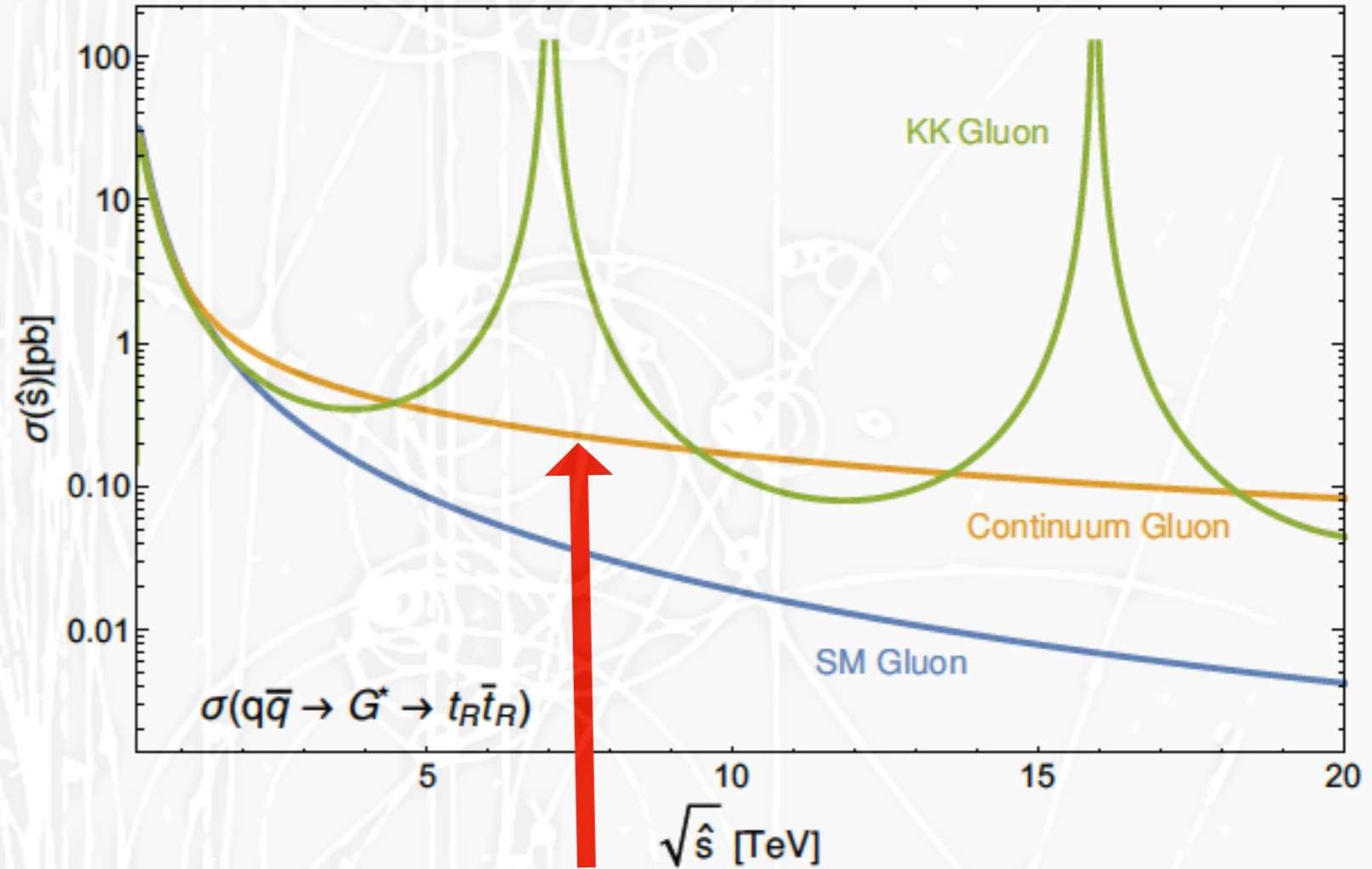
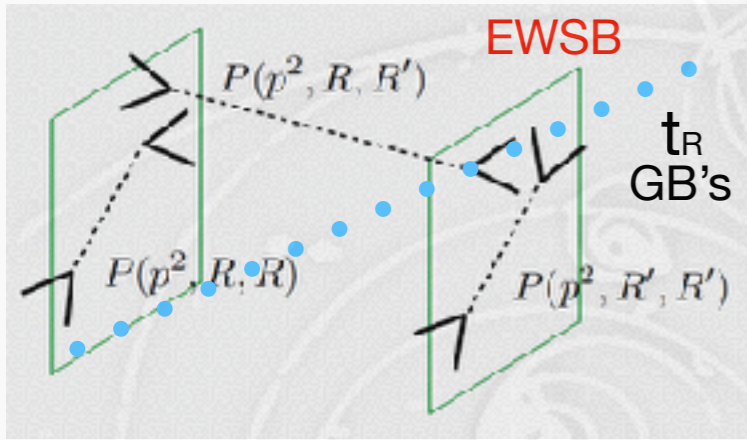
$$\rho(s) = \frac{1}{\pi} \overline{\lim}_{z \rightarrow 0} \text{Im} \frac{A(z)}{A'(z)} = \frac{1}{2\pi s} \left[ 1 \mid i\psi \begin{pmatrix} 1 & \mu \\ 2 & 2\Delta \end{pmatrix} \quad i\psi \begin{pmatrix} 1 & \mu \\ 2 & 2\Delta \end{pmatrix} \right]$$

# Continuum Naturalness?

Csaki, Lombardo, Lee, SL, Telem



- ◆ New Physics (e.g. Top partner) appear solely as a continuum
  - KK gluon / colored  $\rho_c$



New Physics is hidden in the tail region!!

$$\mathcal{L}_E = a(z) e^{-\frac{4}{3}\mu(z-R)} \left[ \frac{1}{4} F^{MN} F_{MN} \right]$$

$$-\hat{A}''(z) + V_{\text{eff}}(z)\hat{A}(z) = p^2\hat{A}(z)$$

$$\hat{A}(z) = \sqrt{\frac{R}{z}} e^{-\mu(z-R)} A(z)$$

$$V_{\text{eff}}(z) = \mu^2 + \frac{\mu}{z} + \frac{3}{4z^2}$$

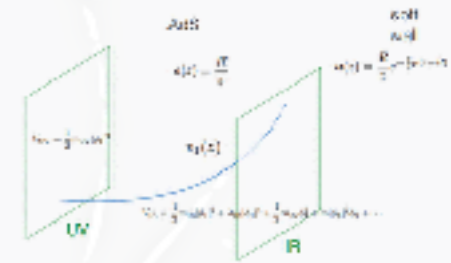
$$V_{\text{eff}}(z \rightarrow \infty) = \mu^2$$

$$A(z) = A \sqrt{\frac{z}{R}} e^{\mu(z-R)} W\left(-\frac{\mu}{2\Delta}, 1; 2\Delta z\right) \quad \Delta = \sqrt{\mu^2 - p^2}$$

$$\rho(s) = \frac{1}{\pi} \overline{\lim}_{z \rightarrow 0} \text{Im} \frac{A(z)}{A'(z)} = \frac{1}{2\pi s} \left[ 1 \mid i\psi \begin{pmatrix} 1 & \mu \\ 2 & 2\Delta \end{pmatrix} \quad i\psi \begin{pmatrix} 1 & \mu \\ 2 & 2\Delta \end{pmatrix} \right]$$

# Continuum Naturalness?

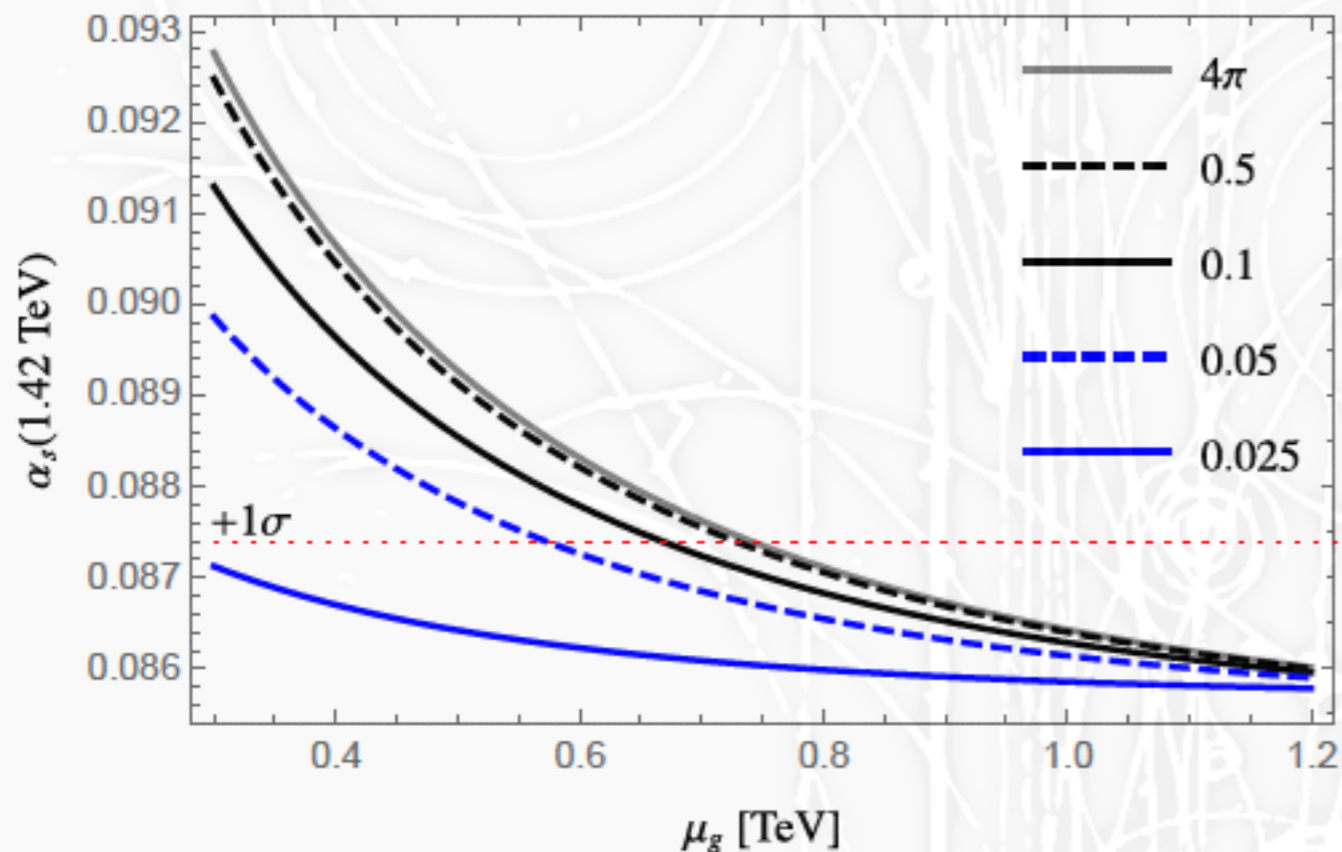
Csaki, Lombardo, Lee, SL, Telem



- ◆ New Physics (e.g. Top partner) appear solely as a continuum
  - **KK gluon / colored octet example: running of strong coupling**

e.g. CMS bound:  $\alpha_s$  up to  $Q \sim 1.42$  TeV

$$\frac{1}{g^2(Q)} = \frac{1}{g_5^2} \int_R^{1/Q} dz a(z) + \frac{1}{g_{UV}^2} - \frac{b_{UV}}{8\pi^2} \log\left(\frac{1}{RQ}\right)$$



$\mu_g > 600 - 700$  GeV

# Continuum Top Partners

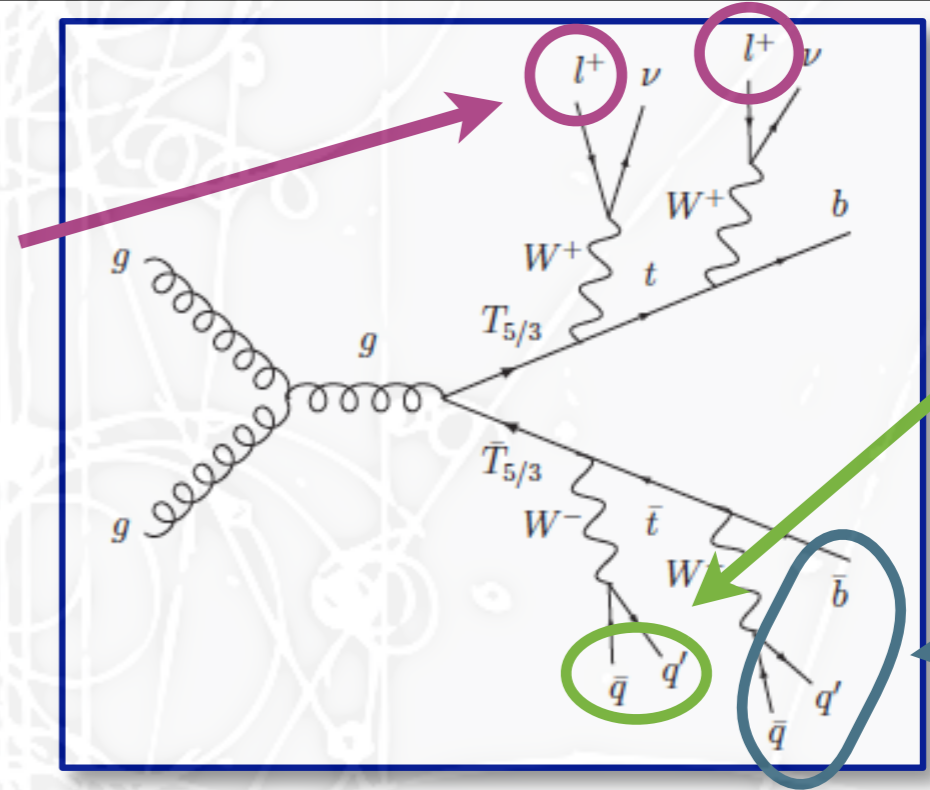
Csaki, Lombardo, Lee, SL, Telem; to appear soon

- ◆ Can we hide top partners at the LHC?

same-sign  
dileptons

$$\sigma(q\bar{q} \rightarrow \chi^\dagger \chi) = \frac{32\pi\alpha_s}{9s} \text{Im}\Pi(s)$$

$$i\Pi^{\mu\nu,ab}(q) = \left( -g^{\mu\nu} + \frac{q^\mu q^\nu}{q^2} \right) \delta^{ab} i\Pi(q^2)$$

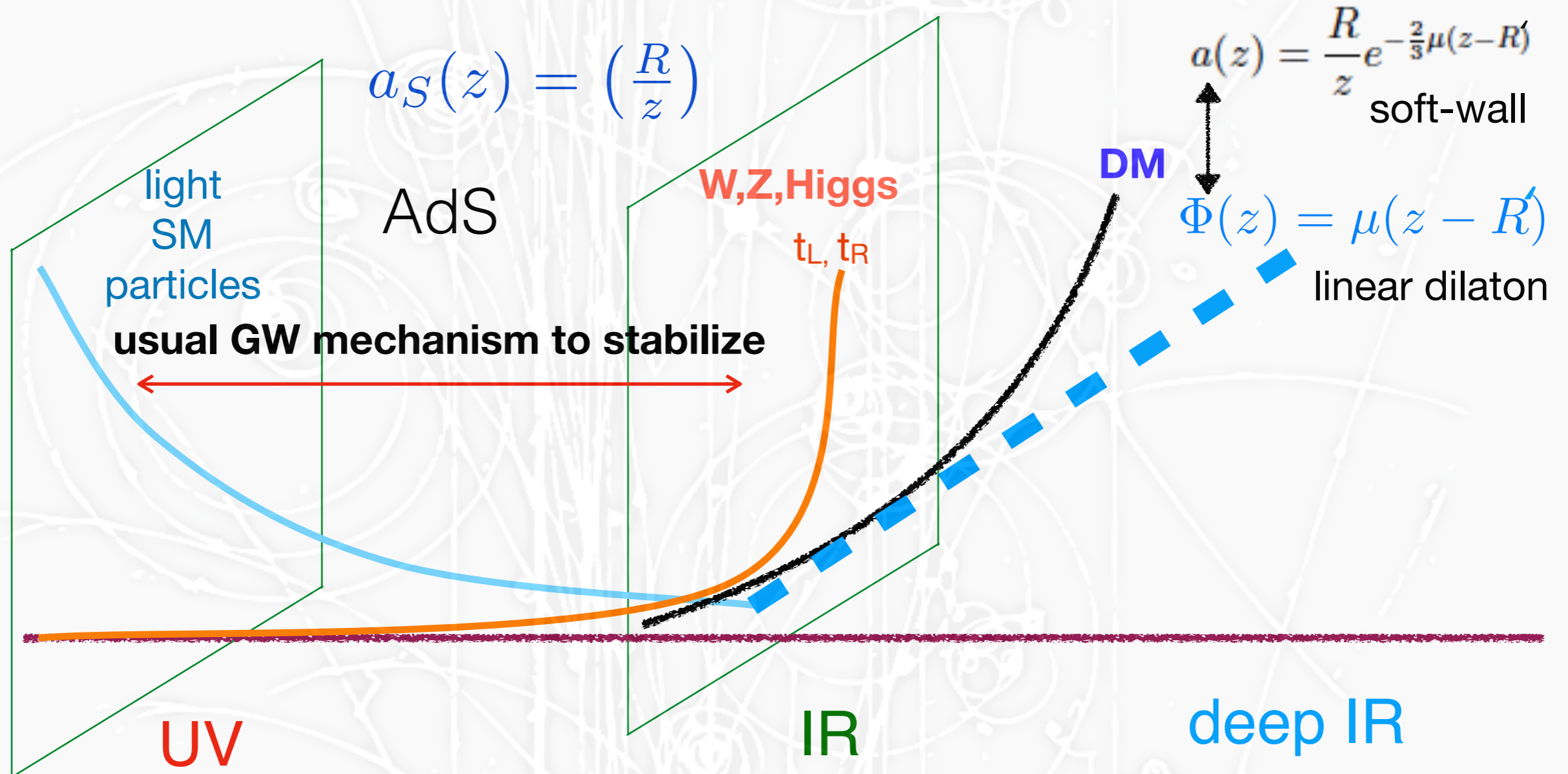


- depending on profile of the spectral density
- calculate top partner production for a given



- need to calculate loop with continuum states (work in progress)

# Continuum Dark Matter



# Summary

---

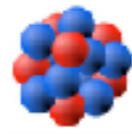
- ◆ Searches at the LHC have placed the naturalness paradigm under pressure
- ◆ We provided a natural model (continuum composite Higgs model), where top and gauge partners could be continuum states from the strong dynamics of confinement
- ◆ The new continuum states in this scenario cannot be described as Breit-Wigner resonances, drastically changing their LHC pheno
- ◆ No bounds from bump huntings, but still bounds from running of alpha, and pair production (work in progress).



*Thank You*







# Composite Higgs

Georgi, Kaplan '84; Kaplan '91; Agashe, Contino, Pomarol '05; Agashe et al '06; Giudice et al '07; Contino et al '07; Csaki, Falkowski, Weiler '08; Contino, Servant '08; Mrazek, Wulzer '10; Panico, Wulzer '11; De Curtis, Redi, Tesi '11, Marzocca, Serone, Shu '12; Pomarol, Riva '12; Bellazini et al '12; De Simone et al '12, Grojean, Matsedonskyi, Panico '13,...

composite sector originated at some UV scale: e.g. assuming a conformal fixed point below UV, ...

strong dynamics

Higgs mass term is irrelevant above  $\Lambda_{IR}$

IR scale is dynamically generated  $f \Leftrightarrow$  a symmetry breaking scale

heavy resonances

$$\Lambda_{UV} \quad \mathcal{L}_{comp}^{UV} + \mathcal{L}_{el,mix}^{UV}$$

$$\Lambda_{IR} \sim g_\rho f$$
$$g_\psi f$$

PNGB model often requires  $g_\psi f \neq g_\rho f$  for less fine-tuning to get  $\sim 125$  GeV higgs

$$\Lambda_{EW}$$

weak dynamics

$$m_h^2 \sim \frac{N_c}{2\pi^2} \frac{v^2}{f^2} M_T$$