

The effects of peculiar motions on the deceleration parameter

Kerkyra Asvesta

Department of Physics
Section of Astrophysics, Astronomy and Mechanics
Aristotle University of Thessaloniki

Cosmology 2023 in Miramare
August 28 - September 2 2023, Miramare, Trieste, Italy



The Standard Model of Cosmology : Λ CDM

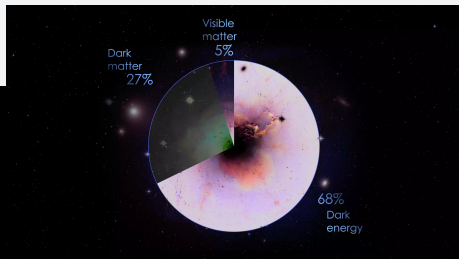
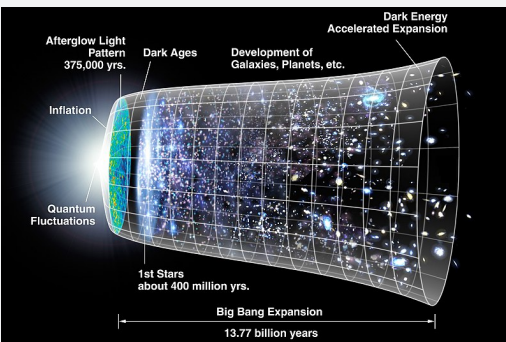
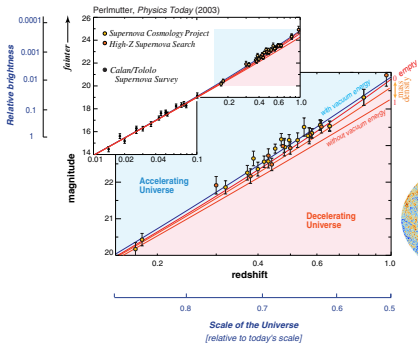


Image credit: NASA Goddard

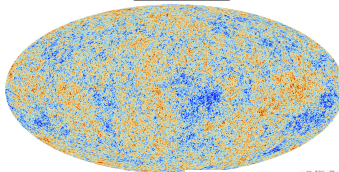
The universe is dominated by dark energy, parametrized by the cosmological constant, Λ

Accelerating expansion of the universe

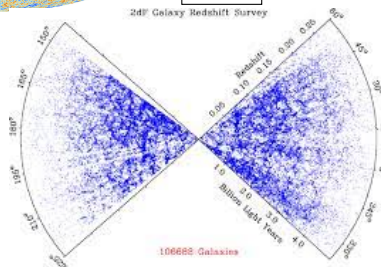
Type Ia Supernovae



CMB



LSS



Λ fits well all the observational data but lacks physical explanation

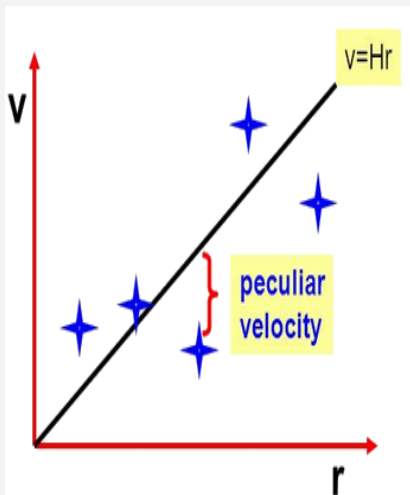
Motivation for the tilted model

- Several alternative cosmological models have been proposed to explain observations, but most of them assume some forms of dark energy or abandon FRLW
- Large-scale peculiar motions are not wisely taken into account
- No robust analysis of the peculiar-velocity effects

The tilted cosmological scenario can in principle explain the late-time cosmic acceleration without the need of dark energy/modified gravity or new physics

Peculiar velocities

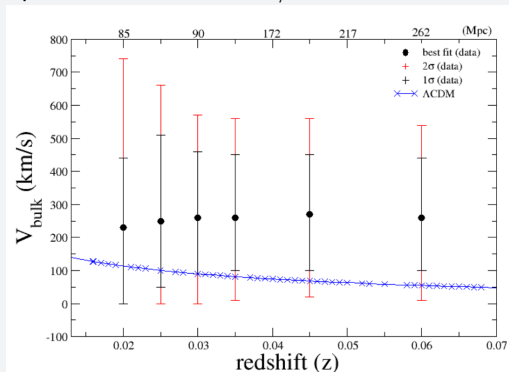
- $1 + z_{obs} = (1 + z_{cosm})(1 + \frac{v_{pec}}{c})$



- Bulk flows**

Size: Few hundred Mpc

Speed: Few hundred km/sec



Colin, Mohayaee, Sarkar, Shafieloo., 2011, MNRAS, 414, 264-271

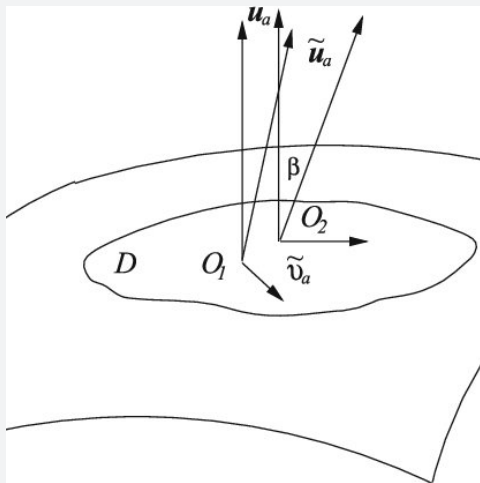
Bulk flows or Dark flows : Challenge for standard Λ CDM model?

Claims for bulk flows **inconsistent with Λ CDM**

- Kashlinsky et al., 2008 ($600 - 1000 \text{ km/s}$) at $r \geq 300h^{-1}$
- Watkins et al., 2009 ($407 \pm 81 \text{ km/s}$) and Feldman et al., 2010 ($416 \pm 78 \text{ km/s}$) within a region of radius $r \approx 100h^{-1}$ Mpc
- Macaulay et al., 2012 ($380_{-132}^{+99} \text{ km/s}$) at $r \approx 33h^{-1}$ Mpc
- Ma and Pan, 2013 ($290 \pm 30 \text{ km/s}$) at $r \approx 58h^{-1}$ Mpc
- Watkins et al., 2023 ($419 \pm 36 \text{ km/s}$) at $r \approx 200h^{-1}$ Mpc

They all approximately agree with the direction of the bulk flow (close to the CMB dipole) but not with the scale and the amplitude.

The Tilted Cosmological Model



Employ General Relativity

observers with 4-velocity $u_a \rightarrow$
idealised observers following
 the smooth Hubble expansion

observers with 4-velocity $\tilde{u}_a \rightarrow$
real observers in galaxies like
 ours, moving relative to the
 Hubble frame

tilt angle β between them
 $\cosh \beta = \tilde{\gamma} = \frac{1}{\sqrt{1-\tilde{v}^2}}$

The tilted cosmological model - Kinematics (1/2)

In a perturbed FRW universe, using linear perturbation theory:

- The three velocities are related through the reduced Lorentz boost :

$$\tilde{u}_a \approx u_a + \tilde{v}_a \quad (1)$$

for non-relativistic peculiar velocities ($\tilde{v}^2 = \tilde{v}^a \tilde{v}_a \ll 1$)

- The expansion rates between the two frames are:

$$\tilde{\Theta} = \Theta + \tilde{\vartheta} \quad \text{and} \quad \tilde{\Theta}' = \dot{\Theta} + \dot{\tilde{\vartheta}} \quad (2)$$

with $\Theta = 3H$, $\tilde{\vartheta} = \tilde{D}^a \tilde{v}_a$ and $\tilde{\vartheta}/\Theta \ll 1$ (in the linear regime).

$\tilde{\Theta} \neq \Theta$ and $\tilde{\Theta}' \neq \dot{\Theta}$ because of peculiar motion effects only

The tilted cosmological model - Kinematics (2/2)

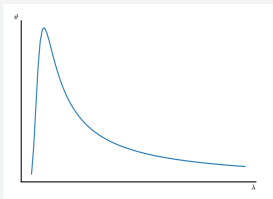
In a perturbed Einstein-de Sitter universe (with $p = 0$ and $\Omega = 1$ in the background) the deceleration parameter measured by the real observers is:

$$\tilde{q} = q + \frac{1}{9} \left(\frac{\lambda_H}{\lambda} \right)^2 \frac{\tilde{\vartheta}}{H} \quad \text{with } \lambda_H = 1/H \text{ and } |\tilde{\vartheta}|/H \ll 1 \quad (3)$$

- When $\lambda \gtrsim \lambda_H$, $\tilde{q} \rightarrow q$ and the peculiar motions fade away
- On subhorizon scales ($\lambda \ll \lambda_H$), $\tilde{q} \neq q$ and the difference can be large depending on the bulk flow scale
- The difference depends on the sign of $\tilde{\vartheta}$. For contracting bulk-flows ($\tilde{\vartheta} < 0$), $\tilde{q} < 0 \rightarrow$ **local apparent accelerated expansion for the real observers**

Parametrization of $\tilde{\vartheta}$

- We assume that locally the bulk flow contracts ($\tilde{\vartheta} < 0$) and $q = \frac{1}{2}$
- A more qualitative form ¹ of the volume scalar is $|\tilde{\theta}| = \frac{\sqrt{3}\langle v \rangle}{\lambda}$
- We consider a form of the local volume scalar $\tilde{\vartheta}$ in the tilted frame ²



$$\tilde{\vartheta} = \tilde{\vartheta}(\lambda) = \frac{m\lambda^2}{p + r\lambda^3} \quad (4)$$

- The deceleration parameter in the tilted frame now becomes

$$\tilde{q} = \tilde{q}(\lambda) = \frac{1}{2} \left(1 - \frac{m}{p + r\lambda^3} \right) \quad (5)$$

¹Tsagas, Kadiltzoglou, Phys. Rev. D 92, 043515

²K. Asvesta, L. Kazantzidis, L. Perivolaropoulos, C. Tsagas, 2022, DOI: 10.1093/mnras/stac922

- ✓ **Construct the theoretical apparent magnitude (m_{th}) out of the studied cosmological model**

Eq.5 can take the form

$$\tilde{q}(\lambda(z)) = \frac{1}{2} \left(1 - \frac{1}{\alpha + b d_r^3(z)} \right) \quad \text{with} \quad d_r(z) \equiv H_0 \bar{\chi}(z)/c \quad (6)$$

- The Hubble rate at any redshift connects with the deceleration parameter through

$$\tilde{H}(z) = H_0 \exp \left[\int_0^z \left(\frac{1 + \tilde{q}(u)}{1 + u} \right) du \right] \quad (7)$$

- The Hubble free luminosity distance of the SNIa :

$$\tilde{D}_L(z) = H_0(1+z) \int_0^z \frac{dz'}{\tilde{H}(z')} \quad (8)$$

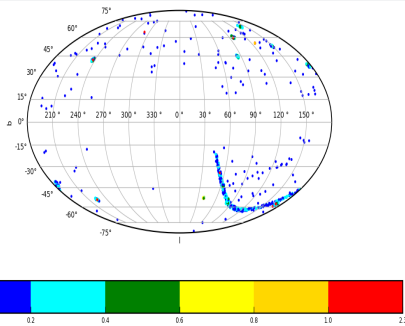
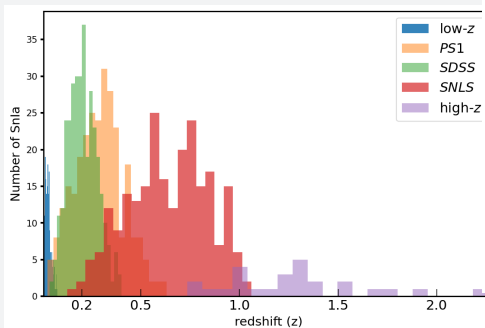
- The theoretically predicted apparent magnitude :

$$m_{th}(z) = M + 5 \log_{10} \tilde{D}_L(z) + 5 \log_{10} \left(\frac{c/H_0}{1 \text{ Mpc}} \right) + 25 = \mathcal{M} + 5 \log_{10} \tilde{D}_L(z) \quad (9)$$

The Pantheon compilation

JLA + additional SniIa from
PanStarrs and HST
(Scolnic et al. (2018) arXiv:1710.00845)

1048 SniIa out to redshift $z \sim 2.3$



K. Asvesta, L. Kazantzidis, L. Perivolaropoulos, C. Tsagas, 2022, DOI: 10.1093/mnras/stac922

Results

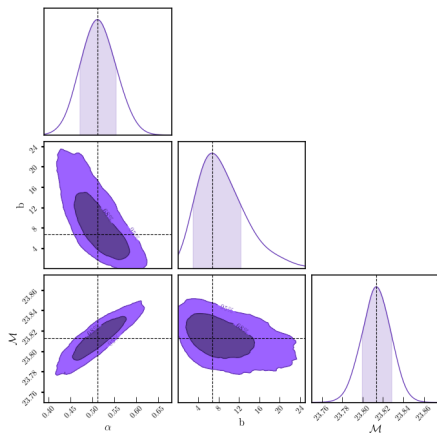
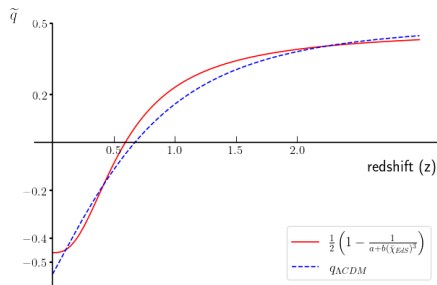
- ✓ Extract the best-fit parameters of the model by performing Monte Carlo Markov Chain (MCMC) statistical method

Model	\mathcal{M}	α	b	Ω_{0m}	χ^2_{\min}	χ^2_{red}
Λ CDM	23.809 ± 0.011	–	–	0.299 ± 0.022	1026.67	0.981
T-EdS	$23.813^{+0.015}_{-0.014}$	0.512 ± 0.041	$6.7^{+5.6}_{-3.8}$	1.0	1026.76	0.982

K. Asvesta, L. Kazantzidis, L. Perivolaropoulos, C. Tsagas, 2022, DOI: 10.1093/mnras/stac922

Result The tilted cosmological model performs equally well with Λ CDM ($\chi^2_{\text{red}} \approx 1$)

Evolutionary behaviour of \tilde{q} and confidence levels



K. Asvesta, L. Kazantzidis, L. Perivolaropoulos, C. Tsagas, 2022, DOI: 10.1093/mnras/stac922

The profile of \tilde{q} is very close to the one of ΛCDM

Fit the SNIa data to the tilted model and found an apparent late-time cosmic acceleration without the need of dark energy

The Dipole of the Pantheon+SH0ES Data

Francesco Sorrenti, Ruth Durrer and Martin Kunz

Département de Physique Théorique and Center for Astroparticle Physics,
Université de Genève, 24 quai Ernest Ansermet, 1211 Genève 4, Switzerland

E-mail: francesco.sorrenti@unige.ch, ruth.durrer@unige.ch, martin.kunz@unige.ch

Abstract. In this paper we determine the dipole in the Pantheon+ data. We find that, while its amplitude roughly agrees with the dipole found in the cosmic microwave background which is attributed to the motion of the solar system with respect to the cosmic rest frame, the direction is different at very high significance. While the amplitude depends on the lower redshift cutoff, the direction is quite stable. For redshift cuts of order $z_{\text{cut}} \simeq 0.05$ and higher, the dipole is no longer detected with high statistical significance. An important rôle seems to be played by the redshift corrections for peculiar velocities.

Compiled using MNRAS L^AT_EX style file v3.0

Tensions between the Early and the Late Universe
 Kavli Institute for Theoretical Physics, July 2019
 Verde, L., Treu, T., Riess, A.G.

Tensions between H_0 and Ω_m

Preprint 26 May 2022

Verde, L. et al.

- ¹ ICREA & ICC UB
- ² University of Ca' Foscari

The quadrupole in the local Hubble parameter: first constraints using Type Ia supernova data and forecasts for future surveys

Suhail Dhawan,^{1*} Antonin Borderies,² Hayley J. Macpherson,³ Asta Heinesen²
¹Institute of Astronomy and Kavli Institute for Cosmology, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK
²Univ Lyon, Ens de Lyon, Univ Lyon1, CNRS, Centre de Recherche Astrophysique de Lyon UMR5574, F-69607, Lyon, France
³Department of Applied Mathematics and Theoretical Physics, University of Cambridge, Cambridge CB3 0WA, UK

Abstract
 MNRAS 000, 1–12 (2022)

The cosmological principle asserts that the Universe looks spatially homogeneous and isotropic on sufficiently large scales. Given the fundamental implications of the cosmological principle, it is important to empirically test its validity on various scales. In this paper, we use the Type Ia supernova (SN Ia) magnitude-redshift relation from both the Pantheon and JLA compilations, to constrain theoretically motivated anisotropies in the Hubble flow. In particular, we constrain the quadrupole moment in the Hubble parameter and the dipole moment in the effective deceleration parameter. We find no significant quadrupole moment at scales of $\sim 100 h^{-1}$ Mpc. Our results are consistent with the theoretical expectation of a quadrupole moment that decays as $\sim h^{-1}$. We find that we can detect a $\sim 7\%$ quadrupole moment at the 5σ level, for a forecast low- z sample of 1055 supernovae in the rest-frame of the cosmic microwave background (CMB). We find a marginal $\sim 2\sigma$ dipole moment at $\sim 3\sigma$ significance. In the rest-frame of the cosmic microwave background (CMB), after applying peculiar velocity corrections, the dipole moment is consistent with zero. These results show that the cosmological principle is supported on the scales probed by current supernova surveys. However, the dipole moment is consistent with zero, but the quadrupole moment is non-zero, which yields a discrepancy between the observed dipole moment and the theoretical prediction. This discrepancy is not seen in the JLA sample, which may be due to its smaller size and higher redshift range.

Accepted XXX, Received YYY, in original form ZZZ
 MAY 2022

Tensions between the Early and Late
Kavli Institute for Theoretical
Verde, L., Treu, T., Riess, A

Tension

Late

NP Publishing
1/11/012007

THE ASTROPHYSICAL JOURNAL LETTERS, 908:L51 (6pp), 2021 February 20
© 2021, The Author(s), Published by the American Astronomical Society.
OPEN ACCESS

A Test of the Cosmological Principle with Quasars

Nathan J. Secrest¹, Sebastian von Hausegger^{2,3,4}, Jacques Colin³, Mohamed Rameez⁵, Roya Mohayaee³, Subir Sarkar⁴, and
<https://doi.org/10.3847/2041>

¹ U.S. Naval Observatory, 3450 Massachusetts Avenue NW, Washington, DC 20392-5420, USA; nathan.j.secrest.civ@mail.mil
² INRIA, 615 Rue du Jardin-Botanique, F-54600 Nancy Grand-Est, France
³ Sorbonne Université, CNRS, Institut d'Astrophysique de Paris, 98 bis Boulevard Arago, Paris F-75014, France
⁴ Rudolf Peierls Centre for Theoretical Physics, University of Oxford, Parks Road, Oxford, OX1 3PU, UK
⁵ Dept. of High Energy Physics, Tata Institute of Fundamental Research, Homi Bhabha Road, Mumbai 400005, India
Received 2020 September 29; revised 2021 January 18; accepted 2021 January 19; published 2021 February 25

Abstract

We study the large-scale anisotropy of the universe by measuring the dipole in the angular distribution of a flux-limited, all-sky sample of 1.36 million quasars observed by the Wide-field Infrared Survey Explorer (WISE). This sample is derived from the new CatWISE2020 catalog, which contains deep photometric measurements at 3.4 and 4.6 μm from the cryogenic, post-cryogenic, and reactivation phases of the WISE mission. While the direction of the dipole in the quasar sky is similar to that of the cosmic microwave background (CMB), its amplitude is over twice as large as expected, rejecting the canonical, exclusively kinematic interpretation of the CMB dipole with a p -value of 5×10^{-7} (4.9σ for a normal distribution, one-sided), the highest significance achieved to date in such studies. Our results are in conflict with the cosmological principle, a foundational assumption of the concordance ΛCDM model.

Unified Astronomy Thesaurus concepts: Large-scale structure of the universe (902); Cosmic microwave background radiation (322); Observational cosmology (1146); Infrared astronomy (786); Quasars (100); Galactic nuclei (16); Cosmology (343)

1. Introduction

The standard Friedmann–Lemaître–Robertson–Walker (FLRW) cosmology is based on the “cosmological principle,” which assumes that the universe is homogeneous and isotropic on large scales. This assumption is supported by the smooth distribution of matter on small angular scales. These fluctuations of matter density are created in the early universe and grow over time, leading to the formation of galaxies and galaxy clusters.

than ≥ 100 Mpc.

*Tensions between the Early an
Kavli Institute for Theoretical
Verde, L., Treu, T., Riess, P*

Tensor

Publishing
1/01/2007

THE ASTROPHYSICAL JOURNAL
© 2021, The Author(s). Published by
OPEN ACCESS

**Astronomy
&
Astrophysics**

Nathar

1 IC
2 *

Specialized Issues in High Energy Phys
10.1051/012007

A&A 631, L13 (2019)
<https://doi.org/10.1051/0004-6361/201936373>
© ESO 2019

LETTER TO THE EDITOR

Evidence for anisotropy of cosmic acceleration*

Jacques Colin¹, Roya Mohayaee¹, Mohamed Rameez², and Subir Sarkar³

- ¹ CNRS, UPMC, Institut d'Astrophysique de Paris, 98 bis Blvd Arago, Paris, France
² Niels Bohr Institute, University of Copenhagen, Blegdamsvej 17, 2100 Copenhagen, Denmark
³ Rudolf Peierls Centre for Theoretical Physics, University of Oxford, Parks Road, Oxford OX1 3PU, UK
e-mail: s.sarkar@physics.ox.ac.uk

Received 22 July 2019 / Accepted 18 October 2019

ABSTRACT

"bulk flow" in the local Universe which is faster and extends to much larger scales than are expected around a standard Λ CDM cosmology. This is expected to result in a scale-dependent dipolar modulation of the acceleration inferred from observations of objects within the bulk flow. From a maximum-likelihood analysis of the component aligned with the cosmic microwave background dipole, which falls exponentially with distance, we find that the deceleration parameter, in addition to a small monopole, best fit to data yields $q_{\parallel} = -8.03$ and $S = 0.0262$ ($\Rightarrow d \sim 100$ Mpc), rejecting isotropy with $q_{\parallel} = -0.157$ and consistent with no acceleration ($q_{\parallel} = 0$) at 1.4σ . Thus the cosmic acceleration is not a simple effect of our being non-Copernican observers, rather than evidence for a dominant dipole structure of Universe.

nevertheless there is no consensus yet on the nature or their origin (Schwarz et al. 2018). There are "peculiar motions" and anisotropy of surrounding space, for example our local environment.

Dipole in the deceleration parameter in the Pantheon+ SNIa compilation

- We add a dipole term in the previous form of the deceleration parameter
- We make a redshift cut in the Pantheon+ sample and we analyze SNIa with $z_{hel} \geq 0.020 \sim 82Mpc$
- We fix the dipole direction to coincide with the CMB dipole
- The anisotropic deceleration parameter in the tilted frame becomes

$$\tilde{q} = \tilde{q}_m(z) + q_d(\mathbf{n}_{SN} \cdot \mathbf{n}_{dip})\mathcal{F}_{dip} \quad (10)$$

where $\tilde{q}_m(z) = \frac{1}{2} \left(1 - \frac{1}{\alpha + b \chi_{EdS}^3(z)} \right)$

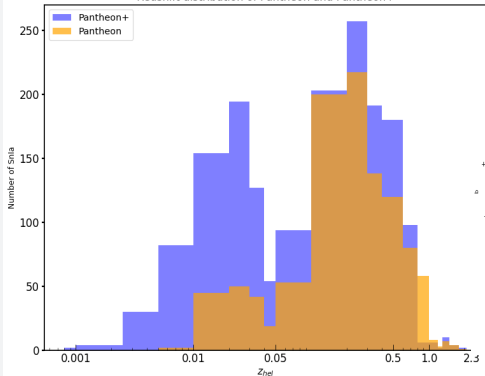
- We examine a form of the function of the dipole \mathcal{F}_{dip} which is constant, $\mathcal{F}_{dip} = 1$

The Pantheon+ S_{NIa} compilation (1/2)

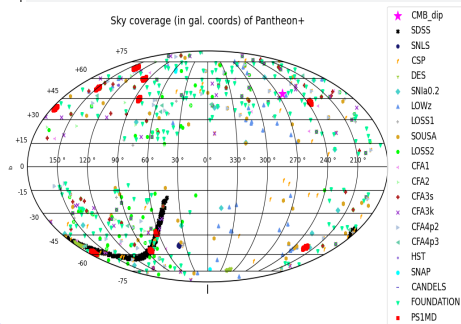
Pantheon + additional S_{NIa} from 5
low-z surveys and DES
(Scolnic et al. 2022, *Astrophys.J.* 938, 2, 113)

1701 S_{NIa} with redshift range
 $0.0008 < z < 2.3$

Redshift distribution of Pantheon and Pantheon+

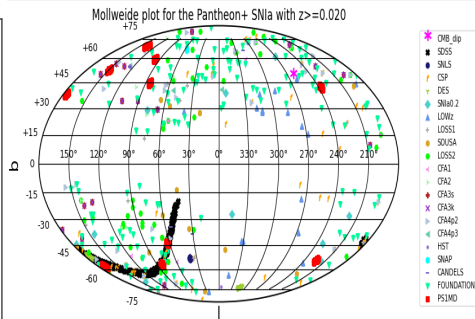
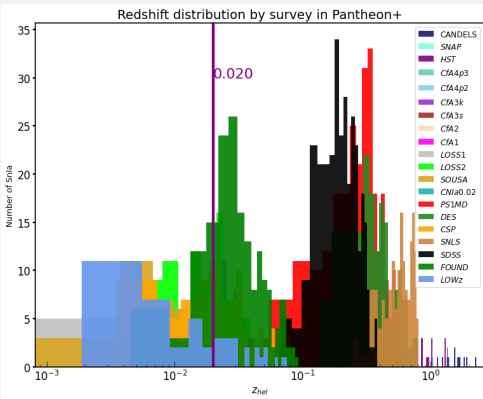


Sky coverage (in gal. coords) of Pantheon+



The Pantheon+ S_{nl}a compilation (2/2)

Make a redshift cut at $z \geq 0.020$
 In total 1429 S_{nl}a



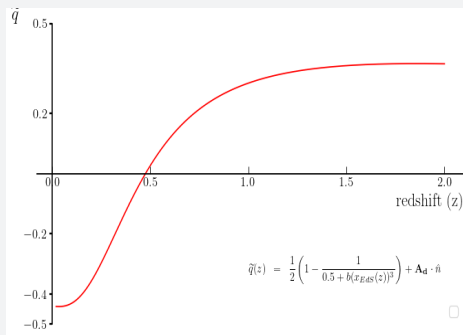
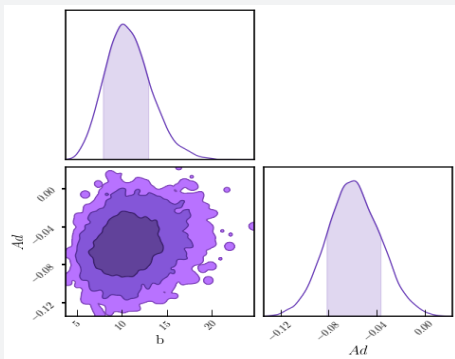
K. Asvesta + (in prep.)

Results

$$\tilde{q} = \frac{1}{2} \left(1 - \frac{1}{\alpha + b \chi_{EdS}^3(z)} \right) + q_d (\mathbf{n}_{SN} \cdot \mathbf{n}_{dip})$$

where $\mathcal{F}_{dip} = 1$

The magnitude of the dipole is
 $> 2\sigma$ away from the Λ CDM



K. Asvesta + (in prep.)

What comes next?

- Use different parametrizations of the dipolar form and check which one fits better the data
- Enlarge the number of free parameters and let for the direction of the dipole to vary
- Do a redshift tomography of the data and check in which redshift bin the dipole becomes stronger
- Allow for a different parametrization of the local contraction rate, $\tilde{\theta}$, which is physically motivated

An aerial photograph of a grand, white, multi-story castle with a prominent tower, situated on a rocky cliffside overlooking a vast blue sea. The castle features ornate architectural details, including arched windows and decorative elements. A red metal walkway leads up to the castle. In the foreground, there is a paved area with a circular green lawn and a fountain. The background shows a clear blue sky and distant hills.

Thank you for your attention!

Back-up slides

"Cosmology is the search for two numbers. The Hubble parameter H_0 and the deceleration parameter q_0 " - Allan R. Sandage

- $H = \frac{\dot{a}}{a}$
- $q = -\frac{\ddot{a}a}{\dot{a}^2}$ ($q > 0$: deceleration, $q < 0$: acceleration)

The deceleration parameters measured in the Hubble and tilted frames are:

$$q = -\left(1 + \frac{3\dot{\Theta}}{\Theta^2}\right) \quad \text{and} \quad \tilde{q} = -\left(1 + \frac{3\tilde{\Theta}'}{\tilde{\Theta}^2}\right) \quad (11)$$

$$\tilde{q} = q + \frac{\tilde{\vartheta}'}{3\dot{H}} \left(1 + \frac{1}{2}\Omega\right) \quad \text{to linear order} \quad (12)$$

In the absence of peculiar flows ($\tilde{\vartheta}' = 0$), $\tilde{q} \rightarrow q$

$$\frac{\tilde{\vartheta}'}{\dot{H}} = \frac{4}{3} \left[1 + \frac{1}{6} \left(\frac{\lambda_H}{\lambda} \right)^2 \right] \frac{\tilde{\vartheta}}{H} \quad (13)$$