



# Introduction for Magnets

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2. Fundamentals 1: Maxwell and friends
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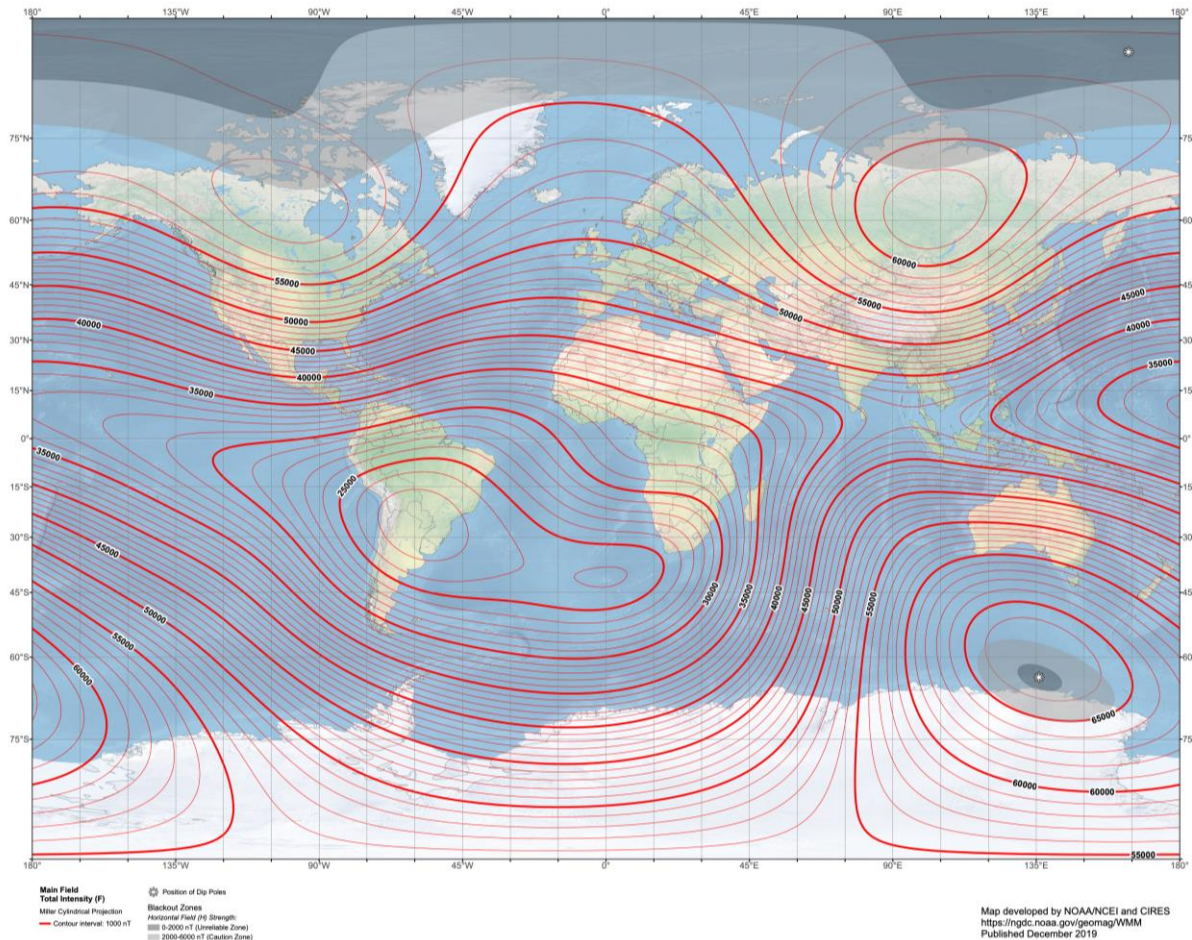
This lecture is based on previous lectures by Attilio Milanese and Davide Tommasini



# Earth magnetic field

At CERN (bld30), on 26/02/2020, the (estimated) magnetic field (flux density) is  
 $|B| = 47587 \text{ nT} = 0.047587 \text{ mT} = 4.7587 \cdot 10^{-5} \text{ T} \approx 0.5 \text{ Gauss}$

US/UK World Magnetic Model - Epoch 2020.0  
Main Field Total Intensity (F)





# Magnet types, functional view

We can classify magnets based on their geometry (that is, what they do to the beam)

dipole

bend

quadrupole

focus

sextupole

Chromatic effects

octupole

damping

kicker / septum

Injection - extraction

solenoid

focus

combined function  
bending

Bend and focus

corrector

Correct errors

skew magnet

coupling

undulator / wiggler

Synchrotron light



# Magnet types, technological view

We can also classify magnets based on their technology

electromagnet

permanent magnet

iron dominated

coil dominated

normal conducting  
(resistive)

superconducting

static

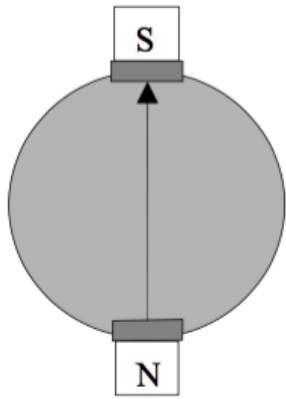
cycled / ramped  
slow pulsed

fast pulsed

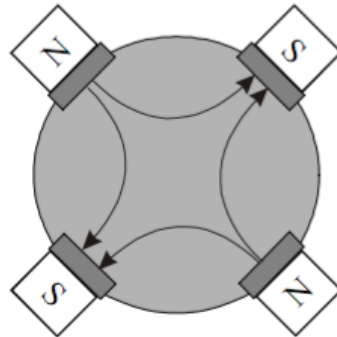


# Types of iron dominated, resistive magnet fields for accelerators

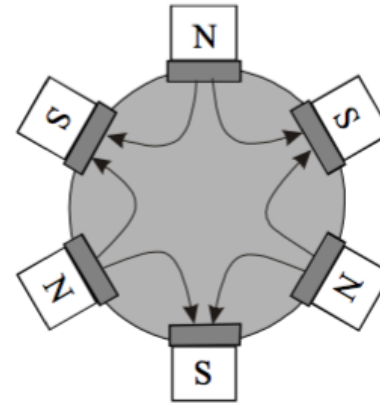
**NORMAL** : vertical field on mid-plane



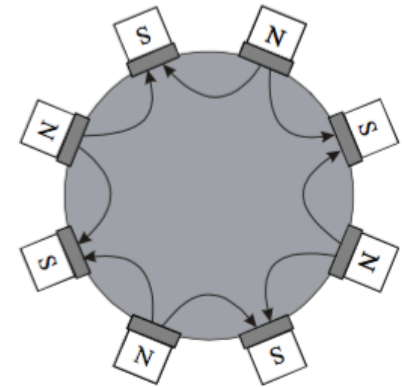
Dipole  
 $|B|=const$



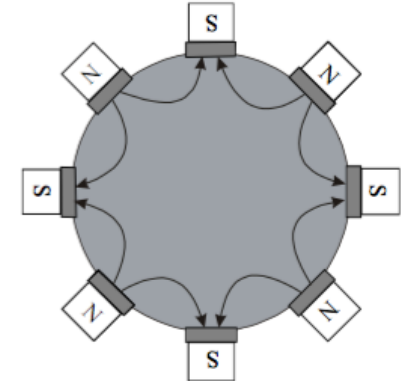
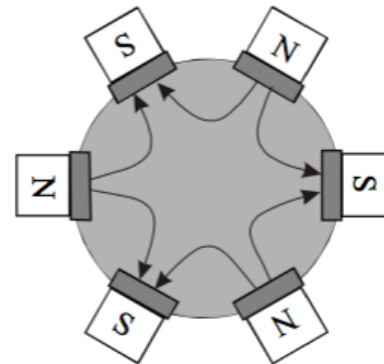
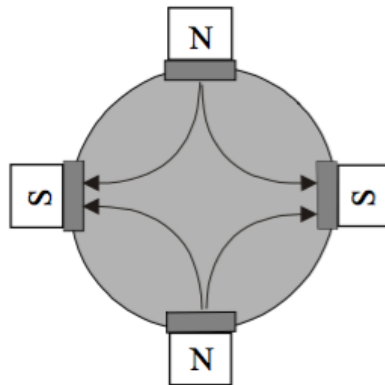
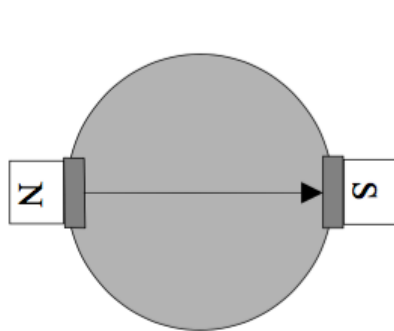
Quadrupole  
 $|B|=G \cdot r$



Sextupole  
 $|B|=1/2 \cdot B'' \cdot r^2$



Octupole  
 $|B|=1/6 \cdot B''' \cdot r^3$



**SKREW** : horizontal field on mid-plane



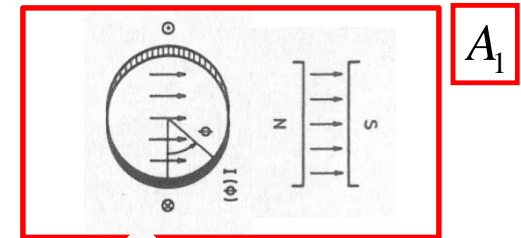
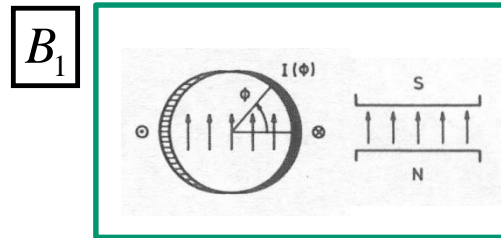
# Types of superconducting magnet fields for accelerators

a “pure” multipolar field can be generated by a specific coil geometry

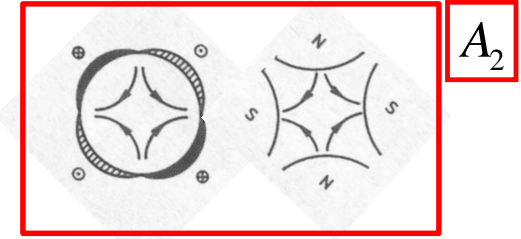
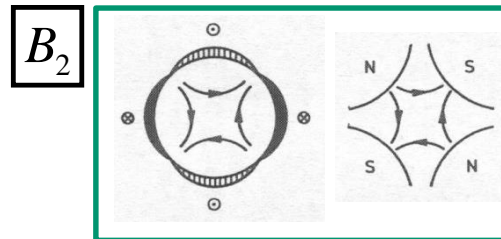
normal

skew

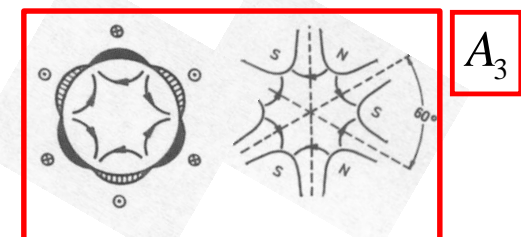
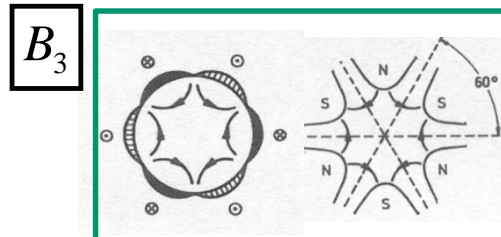
dipole  $n=1$



quadrupole  $n=2$



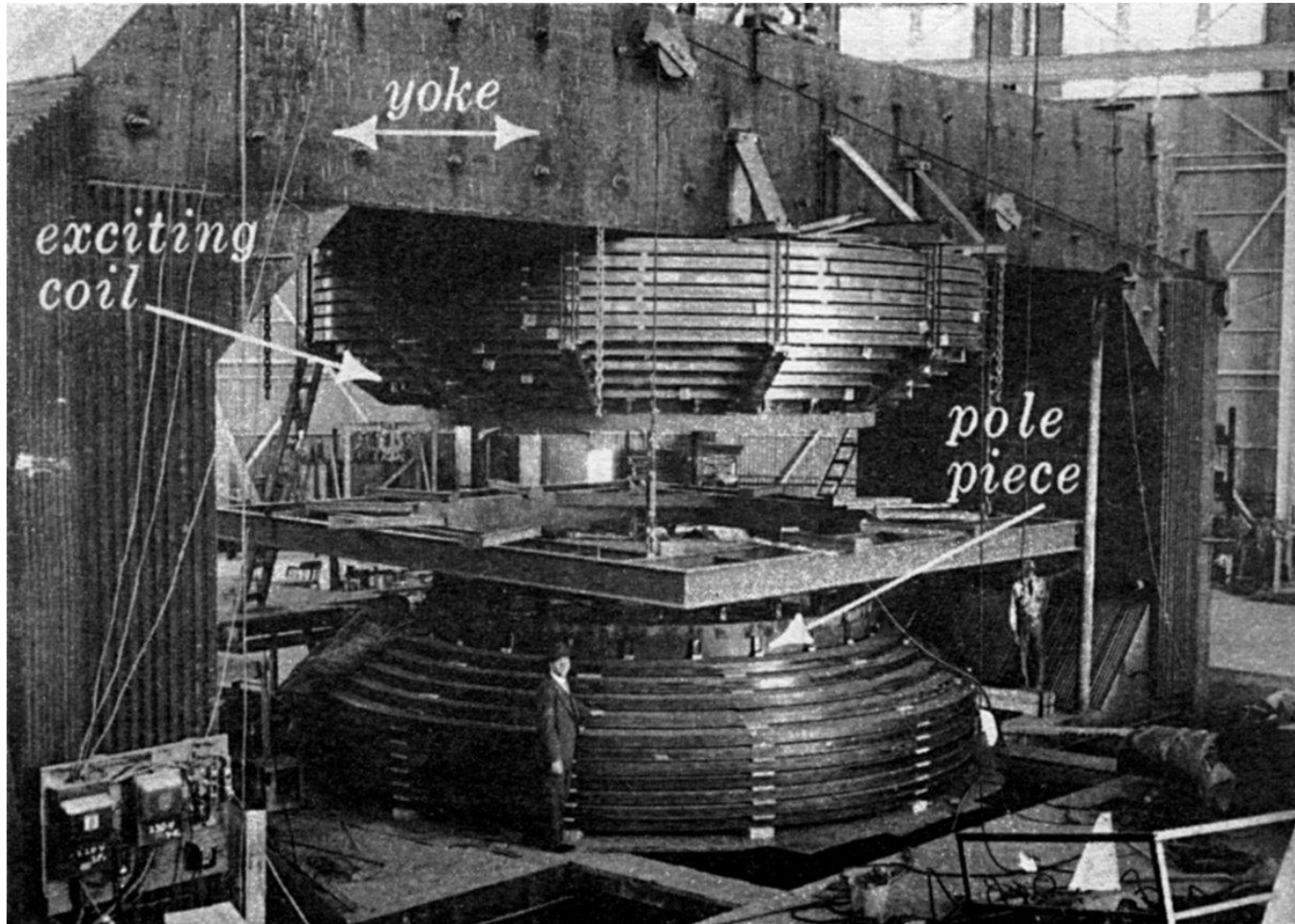
sextupole  $n=3$



Courtesy P. Ferracin, CERN

# Early Cyclotron

The 184" (4.7 m) cyclotron at Berkeley (1942)

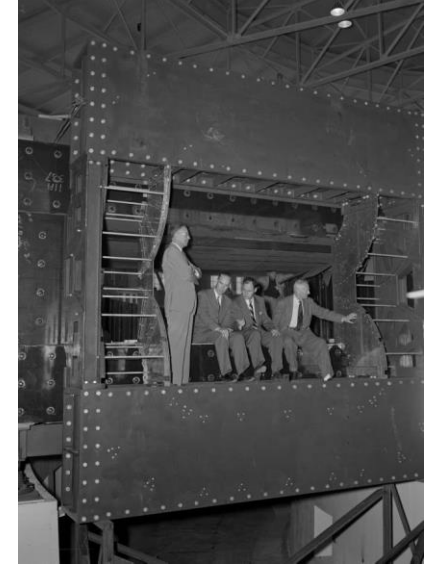




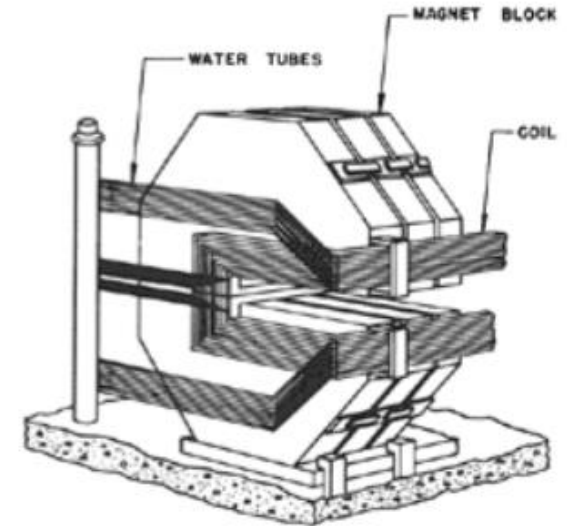
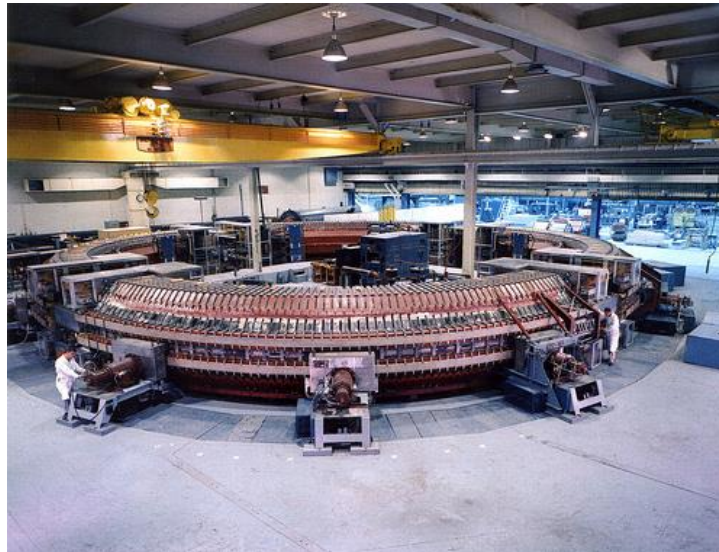


# Some early synchrotron magnets (early 1950-ies)

Bevatron  
(Berkeley)  
1954, 6.2 GeV



Cosmotron  
(Brookhaven)  
1953, 3.3 GeV  
Aperture:  
20 cm x 60 cm



# PS combined function dipole (1959)

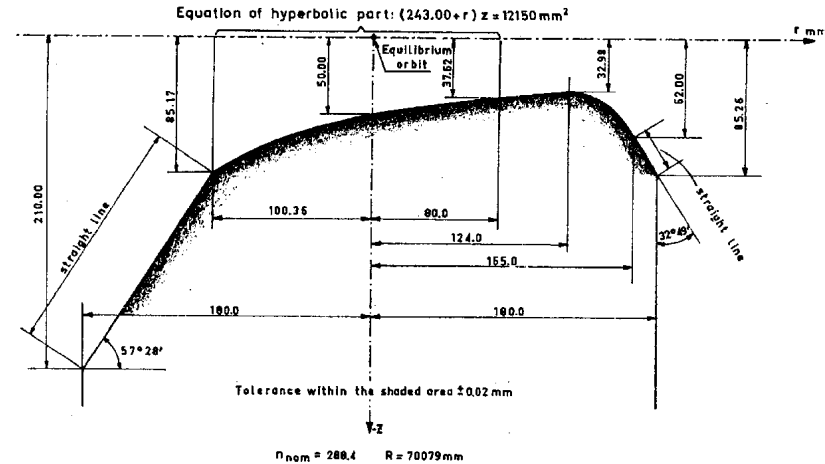
*Magnetic field:*

at injection	147 G
for 24.3 GeV	1.2 T
maximum	1.4 T
Weight of one magnet unit	38 t

Gradient @ 1.2 T : 5 T/m

Equipped with pole-face windings for higher order corrections

Water cooled Al race-track coils



FINAL POLE PROFILE.

Fig. 9: Final pole profile.

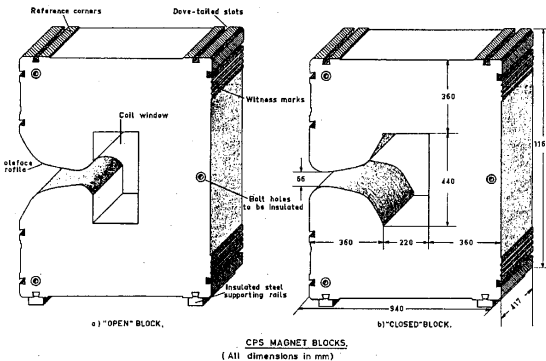
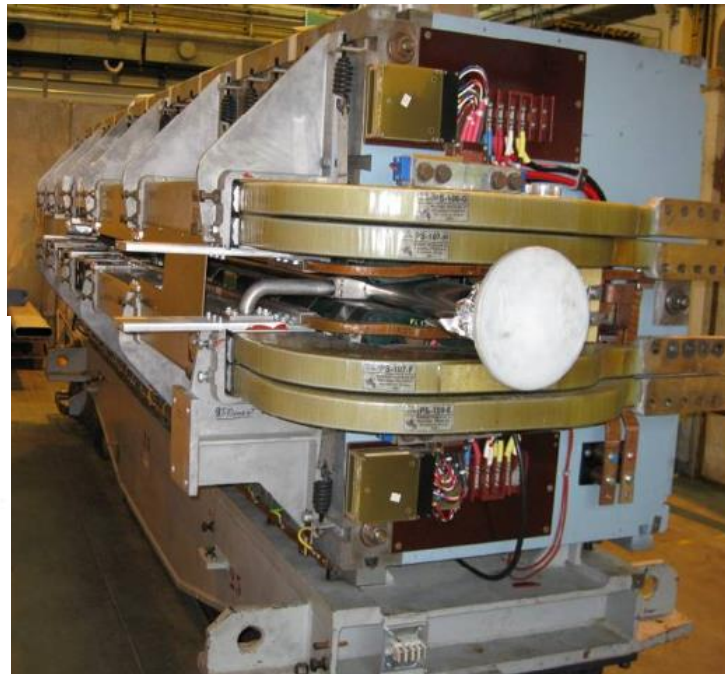
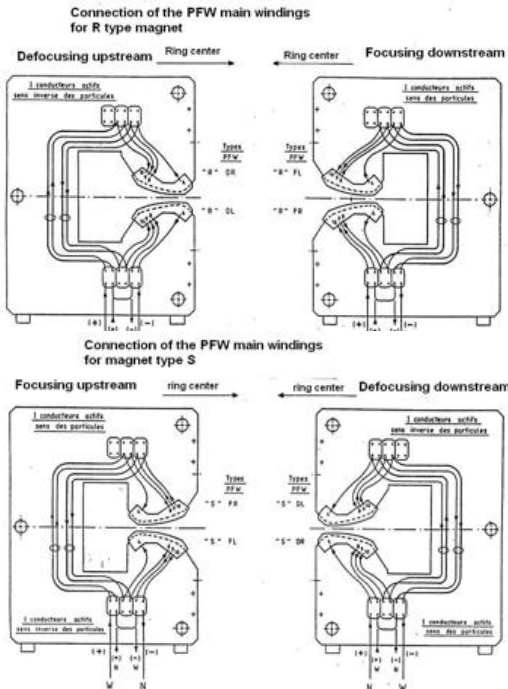
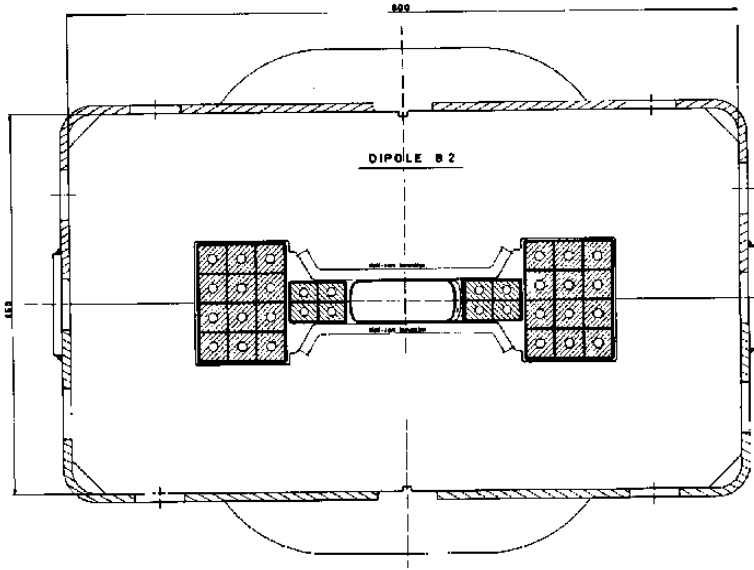


Fig. 12: Final form of the magnet blocks.

# dipole magnet : SPS dipole (1975)



H magnet type MBB

$B = 2.05 \text{ T}$

Coil : 16 turns

$I_{max} = 4900 \text{ A}$

Aperture =  $52 \times 92 \text{ mm}^2$

$L = 6.26 \text{ m}$

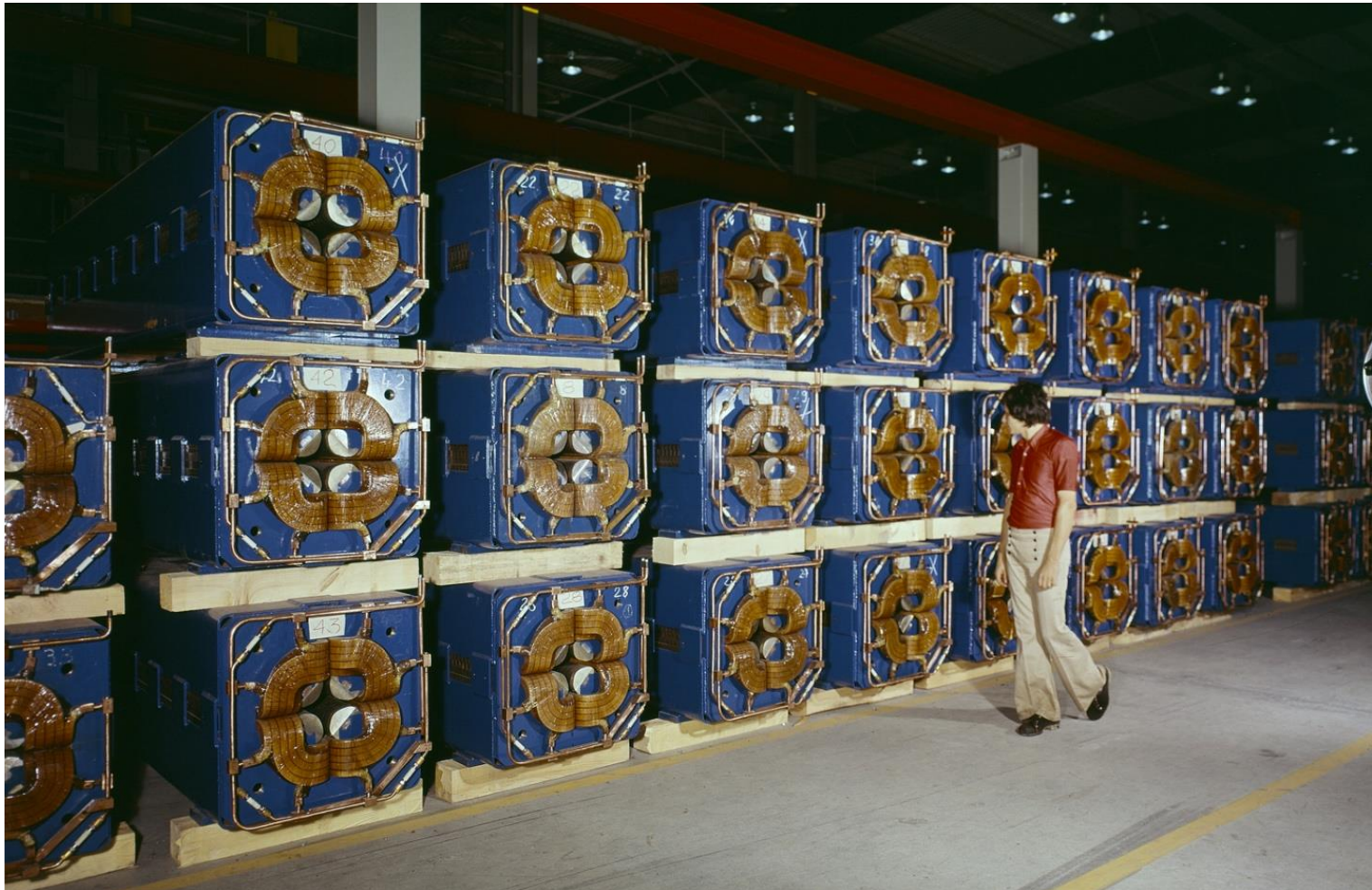
Weight = 17 t





# SPS main dipole

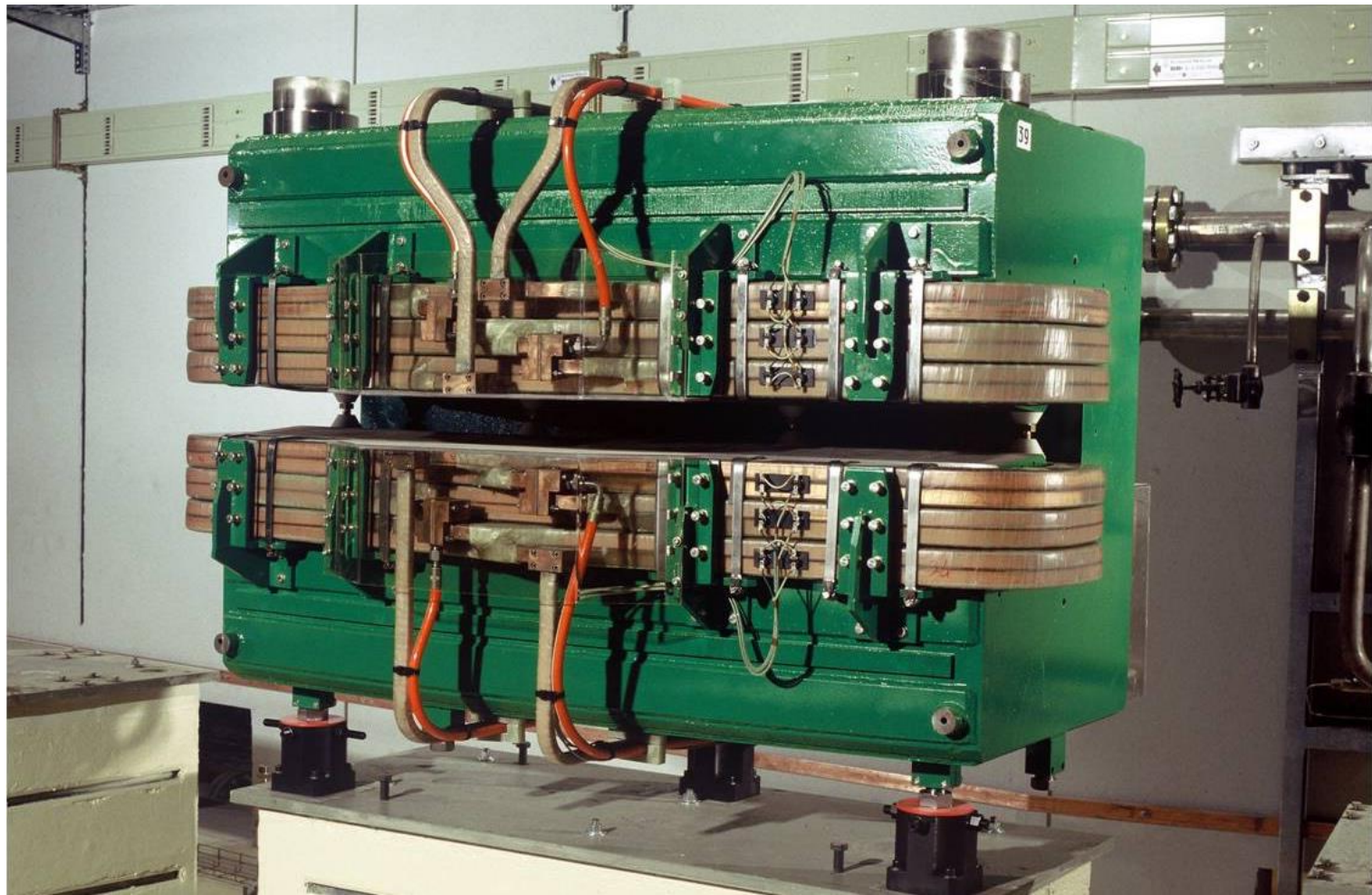
These are main quadrupoles of the SPS at CERN:  $22 \text{ T/m} \times 3.2 \text{ m}$





# Elettra combined function magnet

This is a combined function bending magnet of the ELETTRA light source





# SESAME sextupoles

These are sextupoles (with embedded correctors) of the main ring of the SESAME light source





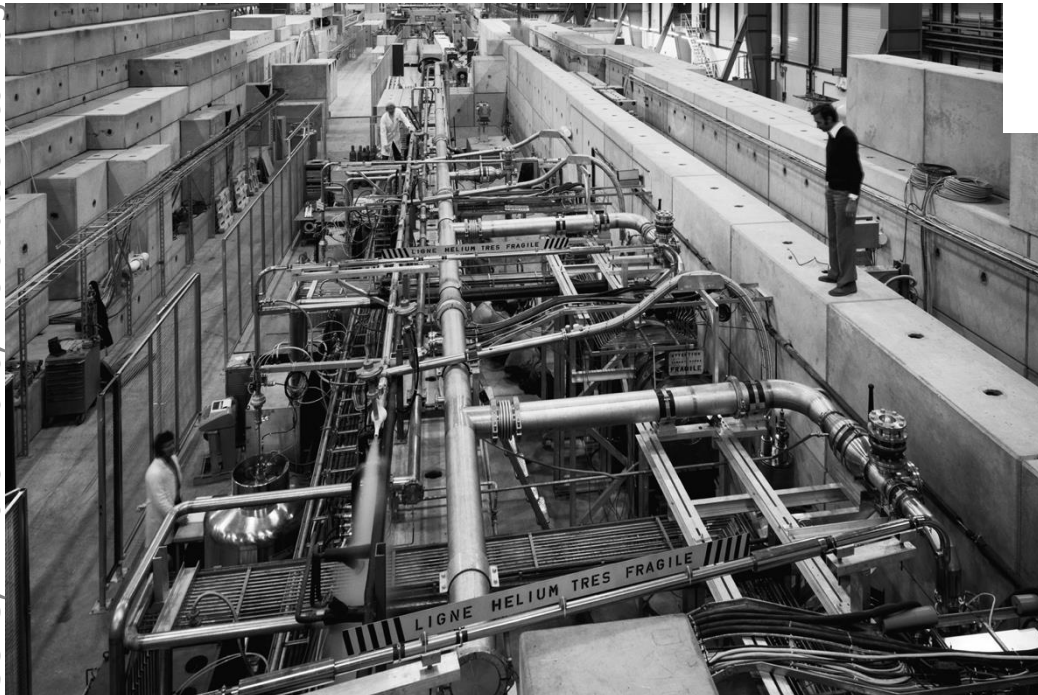
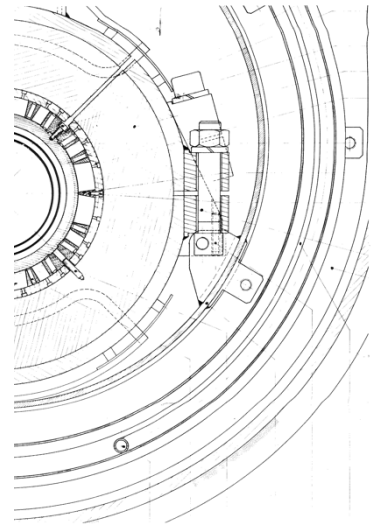
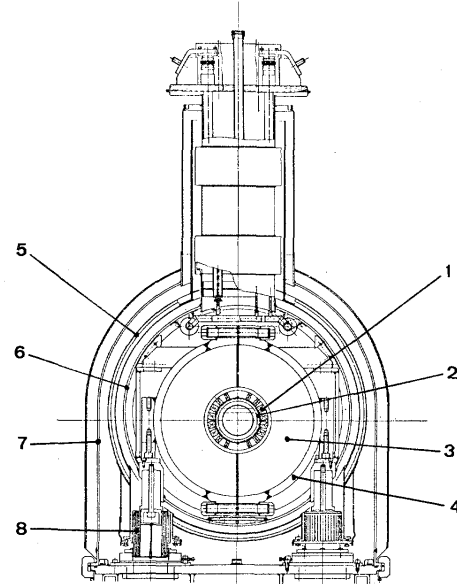
# Beam Transfer line magnets: Castor and Cesar

1977: Very first SC magnets at CERN in an SPS beam line

- CESAR dipole: aperture 150 mm,  $B=4.5\text{ T}$   
 $l = 2\text{ m}$
- CASTOR quadrupole

Both use a monolithic conductor wound into a  $\cos\theta$  coil

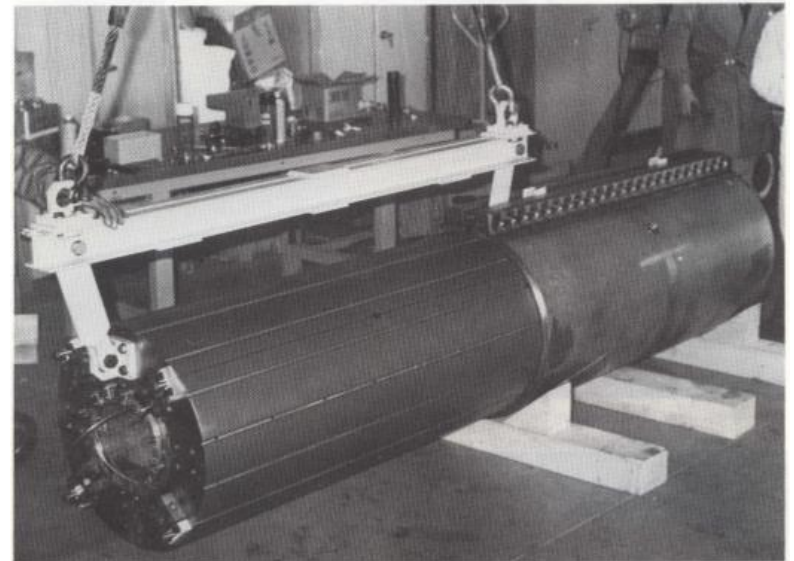
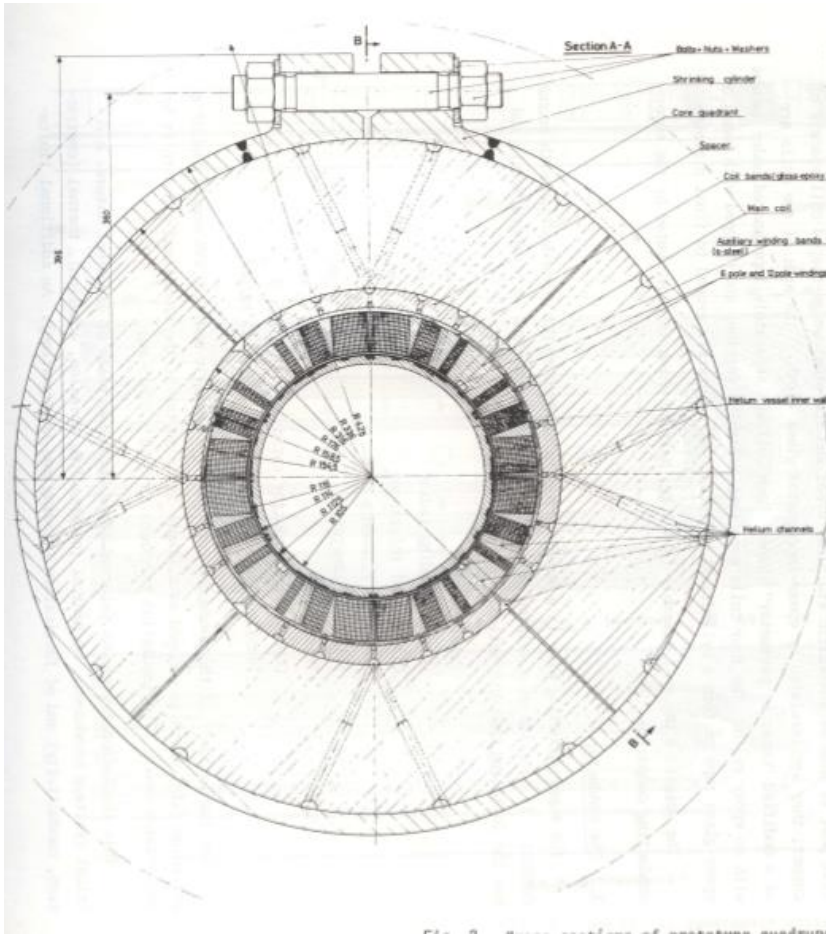
D.F. Leroy\*\*





# ISR Insertion quadrupole

- Nb-Ti monolithic conductor
- fully impregnated coil
- Prestress from yoke + shell

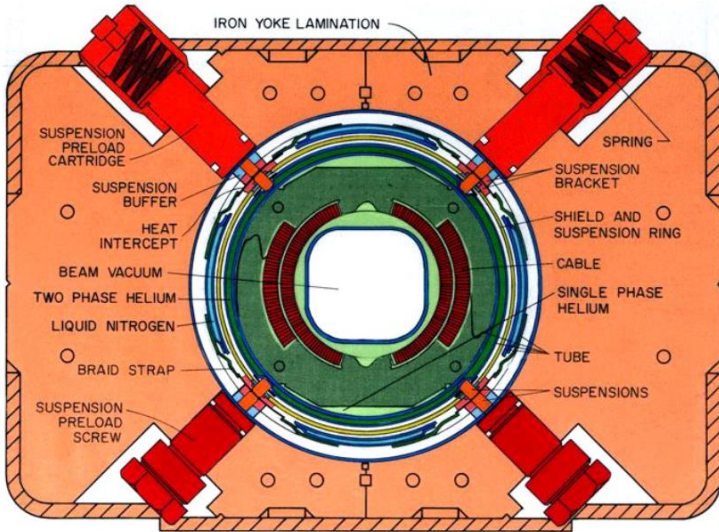




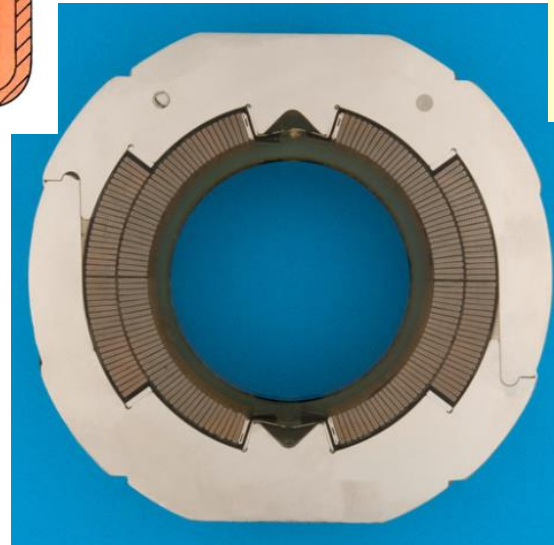


# Tevatron proton-antiproton ring

- Nb-Ti conductor at 4.2 K
- Collars for prestress
- warm iron



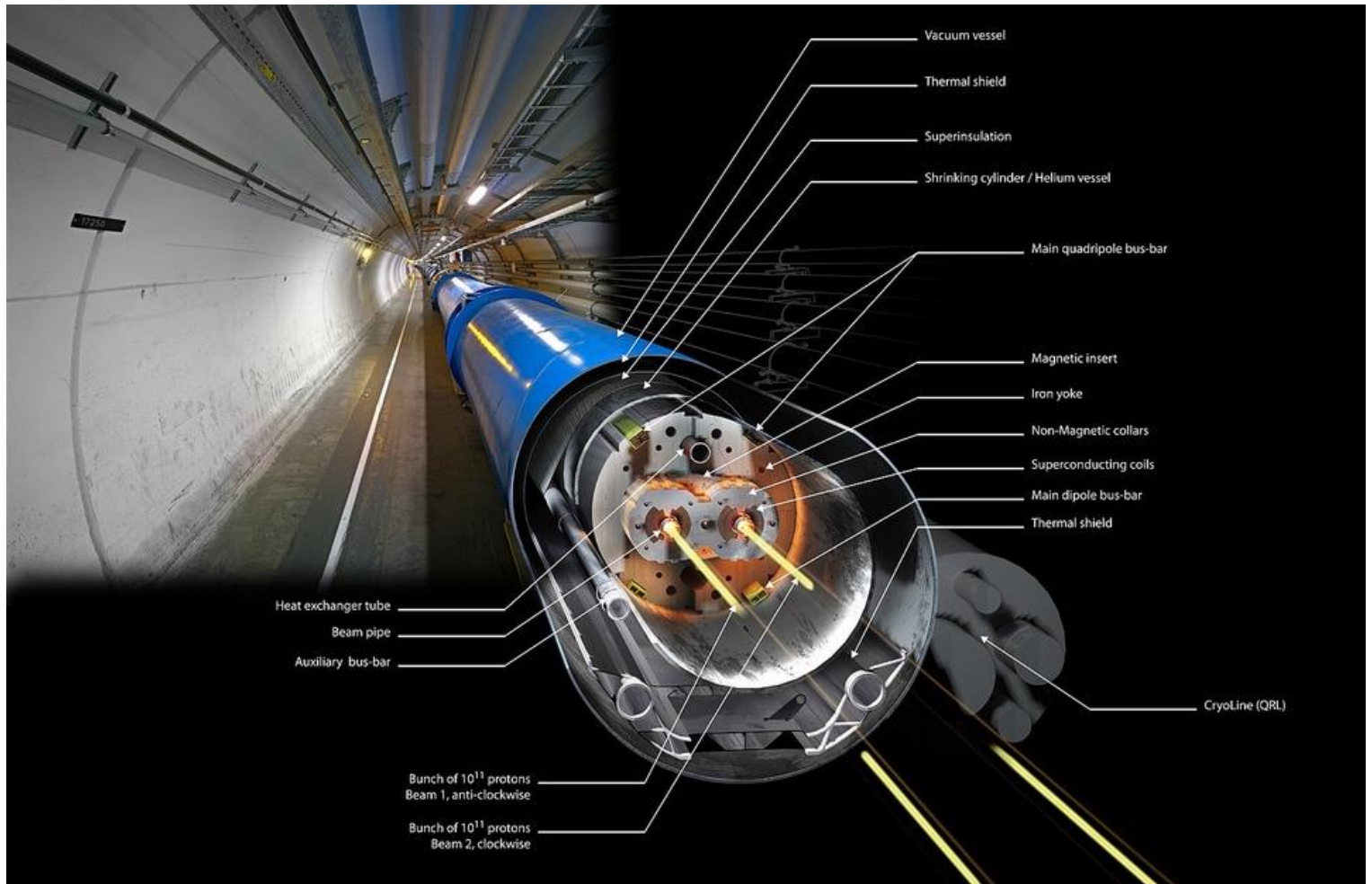
**Tevatron dipoles: 4.2 T  
single aperture, warm yoke**





# LHC dipole

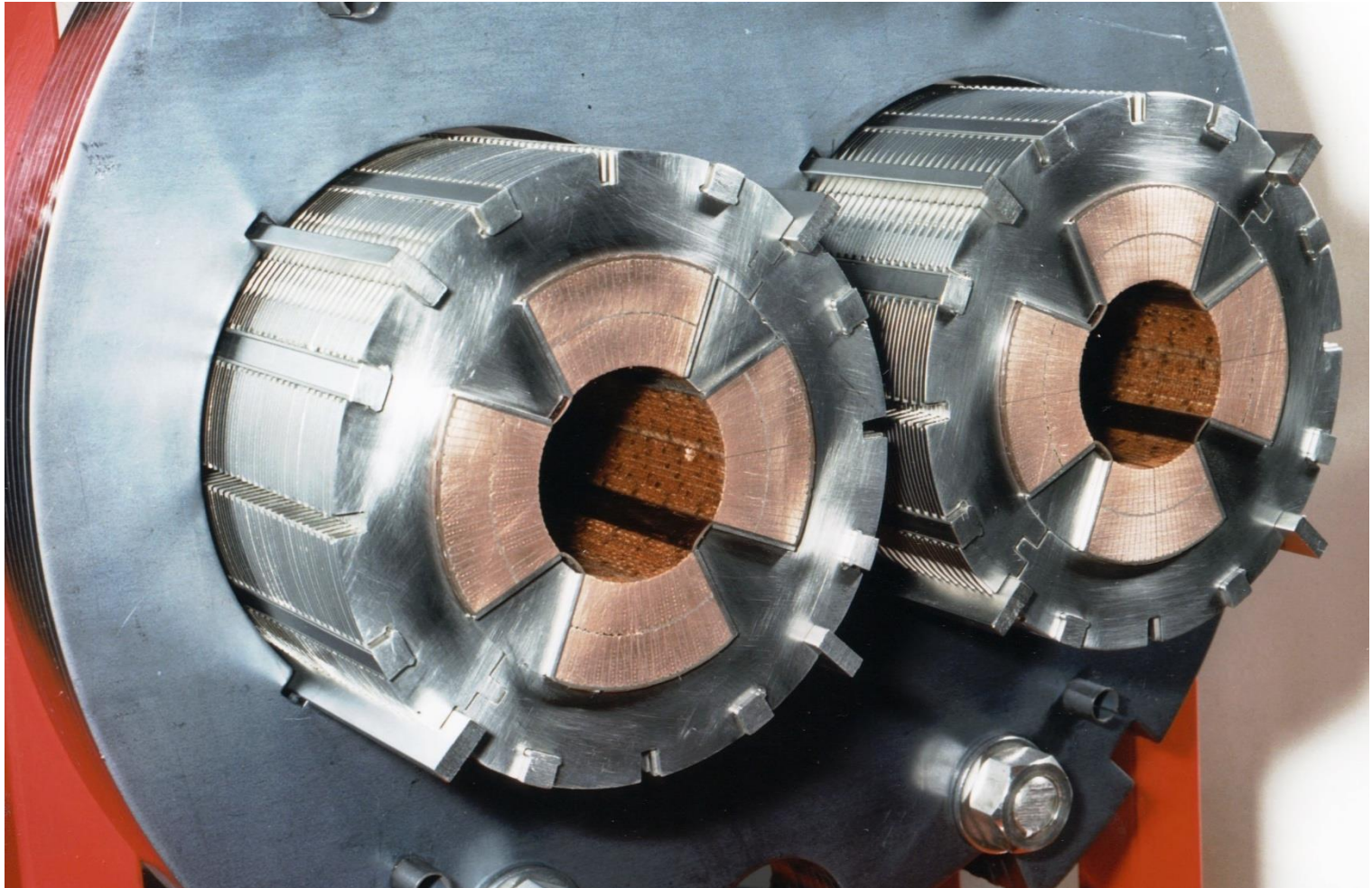
This is a main dipole of the LHC at CERN: 8.3 T × 14.3 m





# LHC main quadrupole

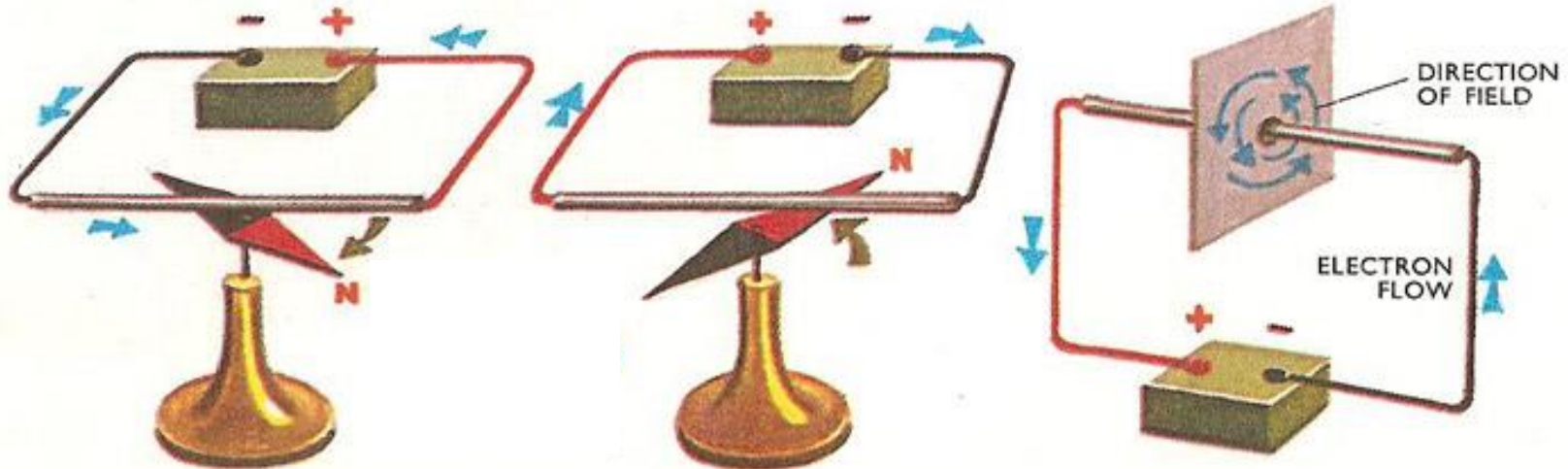
This is a cross section of a main quadrupole of the LHC at CERN:  
223 T/m  $\times$  3.2 m





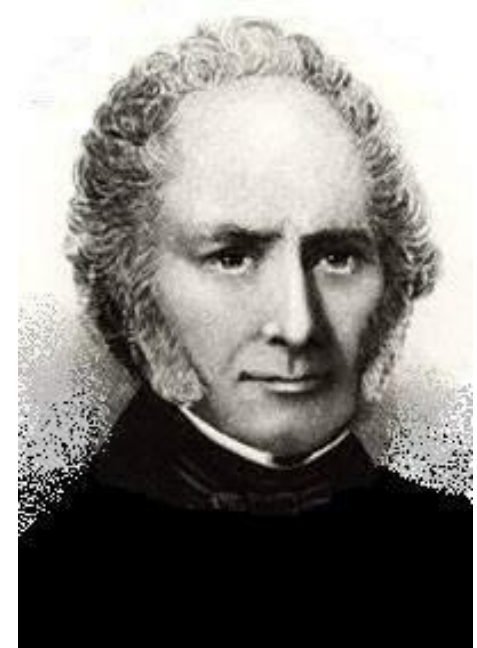
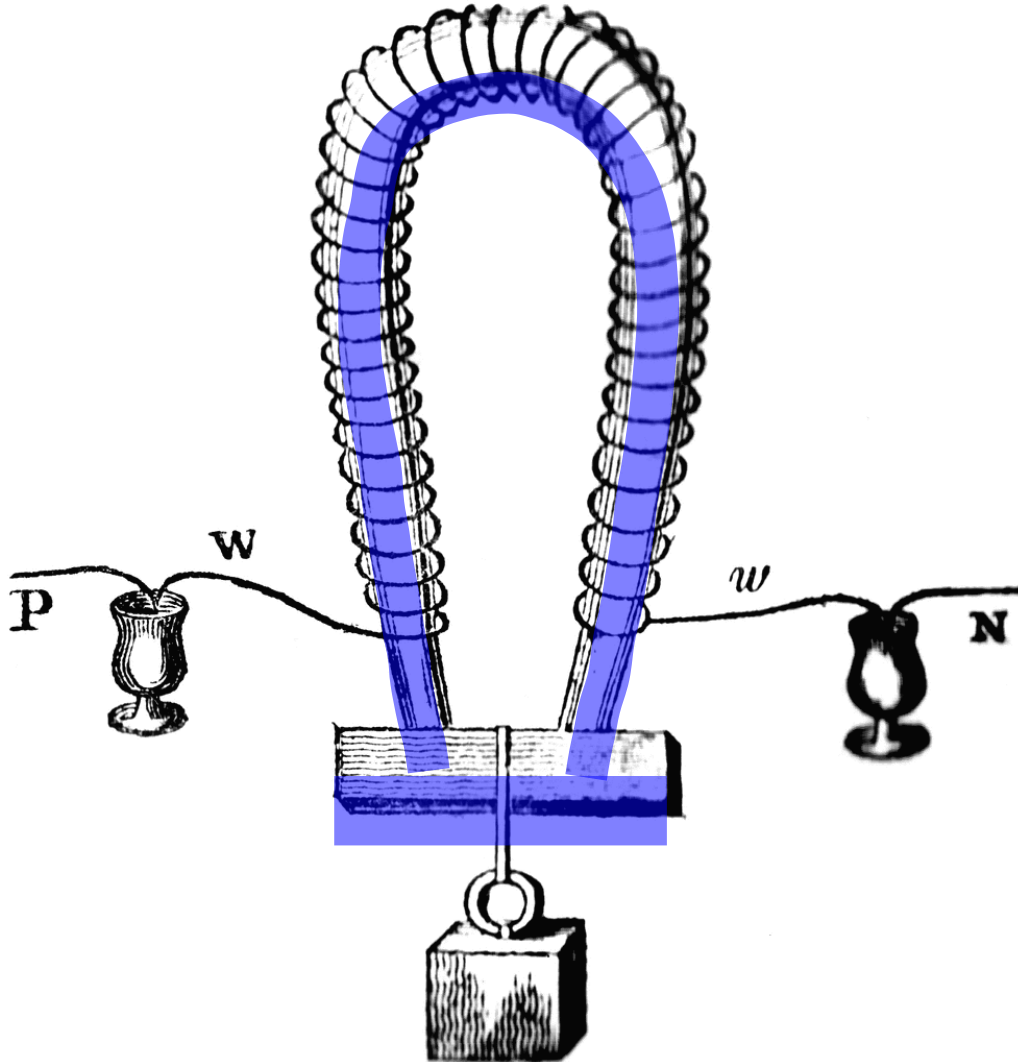
# Electro-magnetism

Ørsted showed in 1820 that electricity and magnetism were somehow related



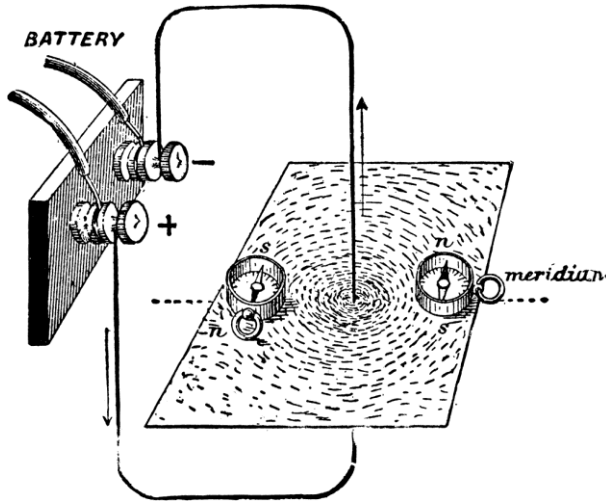
# Electromagnet

The first electromagnet was built in 1824 by Sturgeon

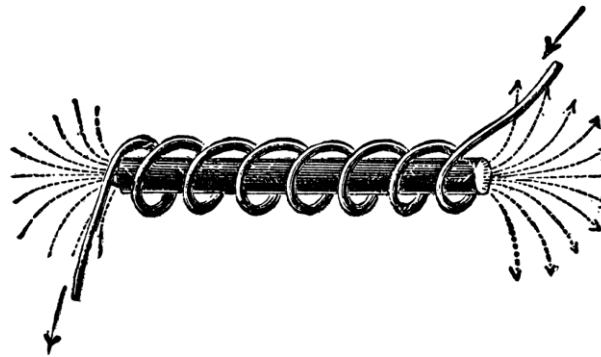
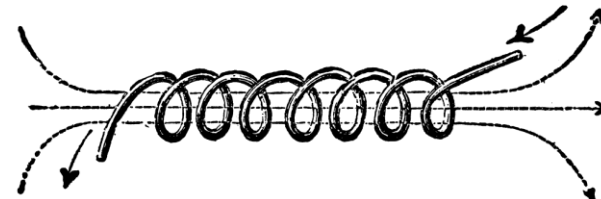


# Basic magnet type

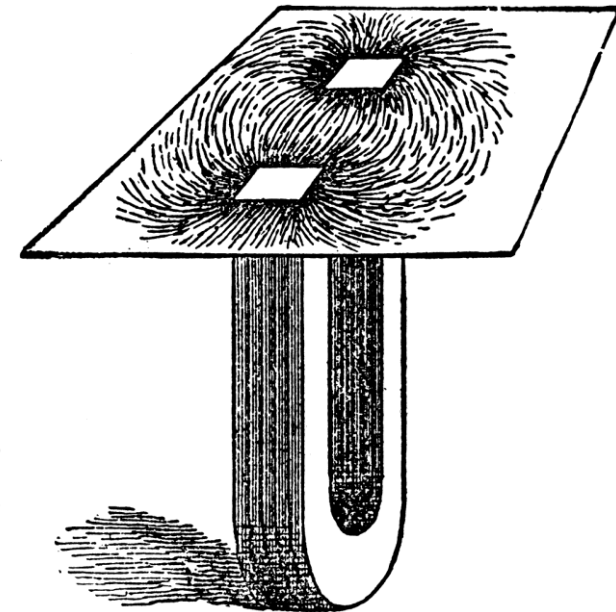
Our magnets work on a few basic principles (steady state only)



an electrical current induces a magnetic effect



some materials (e.g. iron) greatly enhance these effects



some other materials produce these effects even without electrical currents



1. Introduction
2. Fundamentals 1: Maxwell and friends
3. Fundamentals 2: harmonics
4. A few practical considerations



# So, how do we properly describe all this? I

## Maxwell Equations

Integral form

$$\oint \vec{H} d\vec{s} = \int_A \left( \vec{J} + \frac{\partial \vec{D}}{\partial t} \right) d\vec{A}$$

Ampere's law

$$\oint \vec{E} d\vec{s} = -\frac{\partial}{\partial t} \int_A \vec{B} d\vec{A}$$

Faraday's equation

$$\int_A \vec{B} d\vec{A} = 0$$

Gauss's law for magnetism

$$\int_A \vec{D} d\vec{A} = \int_V \rho dV$$

Gauss's law

Differential form

$$\text{rot} \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$$

$$\text{rot} \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\text{div} \vec{B} = 0$$

$$\text{div} \vec{D} = \rho$$

With:  $\vec{B} = \mu \vec{H} = \mu_0 (\vec{H} + \vec{M})$

$$\vec{D} = \varepsilon \vec{E} = \varepsilon_0 (\vec{E} + \vec{P})$$

$$\vec{J} = \kappa \vec{E} + J_{imp.}$$



James Maxwell  
1831 – 1879



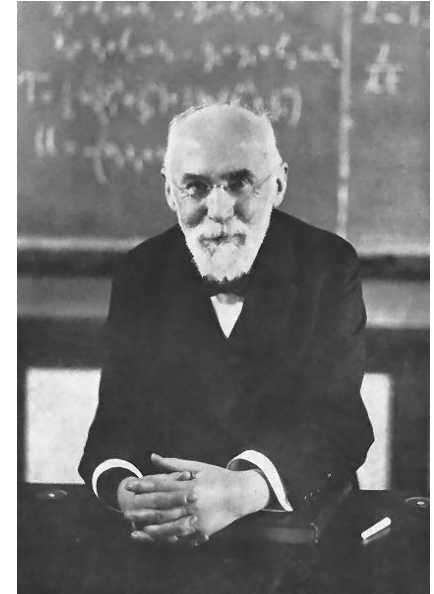
## Lorentz force

$$\vec{F}_m = q(\vec{v} \times \vec{B})$$

for charged beams

$$\vec{F}_m = I\vec{\ell} \times \vec{B}$$

for conductors



Hendrik Lorentz  
1853 –1928



# Nomenclature

<b>B</b>	flux density magnetic field B field magnetic induction		<b>T (Tesla)</b>	<b>(Wb.m<sup>-2</sup> or kg.s<sup>-2</sup>.A<sup>-1</sup>)</b>
<b>H</b>	magnetic field magnetic field strength H field		<b>A/m (Ampere/m)</b>	
<b>Flux</b>	magnetic flux (quantized: $h/2e = 2.067 \cdot 10^{-15}$ Wb)		<b>Wb (Weber)</b>	<b>(kg.m<sup>2</sup>.s<sup>-2</sup>.A<sup>-1</sup>)</b>
<b><math>\mu_0</math></b>	permeability of vacuum	<b><math>4\pi \cdot 10^{-7}</math></b>	<b>H/m (Henry/m)</b>	<b>(kg.m.s<sup>-1</sup>.A<sup>-2</sup>)</b>
<b><math>\mu_r</math></b>	relative permeability		dimensionless	
<b><math>\mu</math></b>	permeability, $\mu = \mu_0 \mu_r$		<b>H/m</b>	<b>(kg.m.s<sup>-1</sup>.A<sup>-2</sup>)</b>



# Magnetostatics

Let's have a closer look at the 3 equations that describe magnetostatics

Gauss law of magnetism

$$(1) \quad \operatorname{div} \vec{B} = 0$$

always holds

Ampere's law with no time dependencies

$$(2) \quad \operatorname{rot} \vec{H} = \vec{j}$$

holds for magnetostatics

Relation between  $\vec{H}$  field and the flux density  $\vec{B}$

$$(3) \quad \vec{B} = \mu_0 \mu_r \vec{H}$$

holds for linear materials

# Divergence free fields

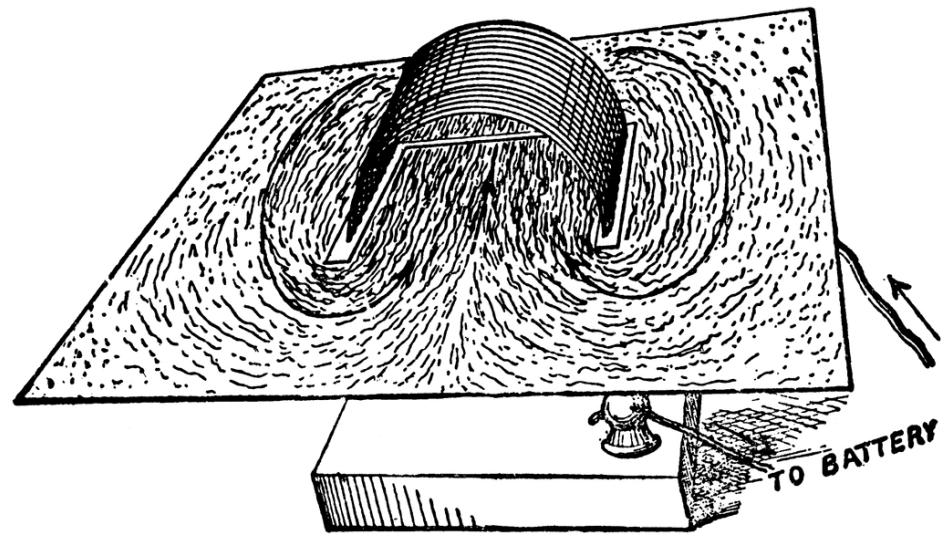
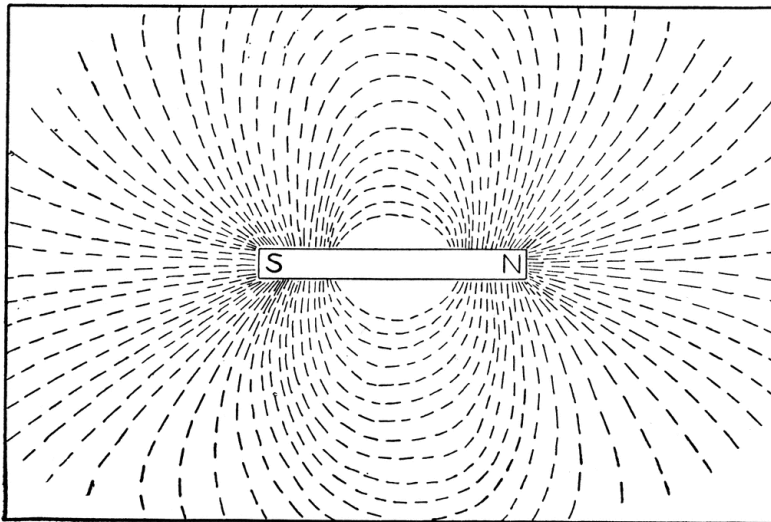
Gauss law of magnetism:

the magnetic flux tubes wrap around, with neither sources nor sinks

$$\operatorname{div} \vec{B} = \frac{\partial B_x}{\partial x} + \frac{\partial B_y}{\partial y} + \frac{\partial B_z}{\partial z} = 0$$

$$\oiint \vec{B} \cdot \vec{dS} = \iiint \operatorname{div} \vec{B} dV = 0$$

divergence / Gauss theorem



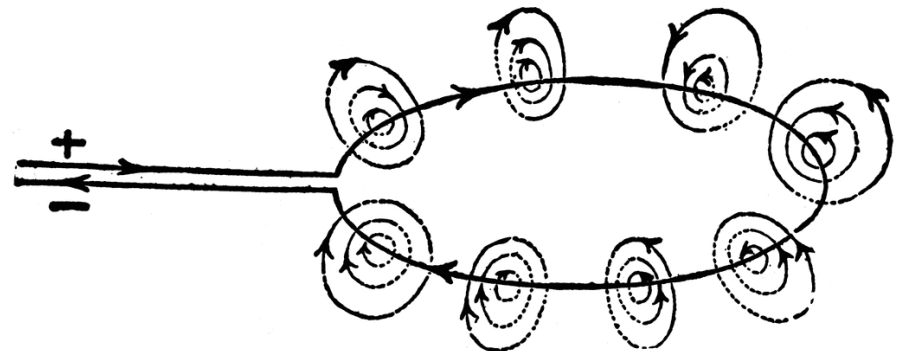
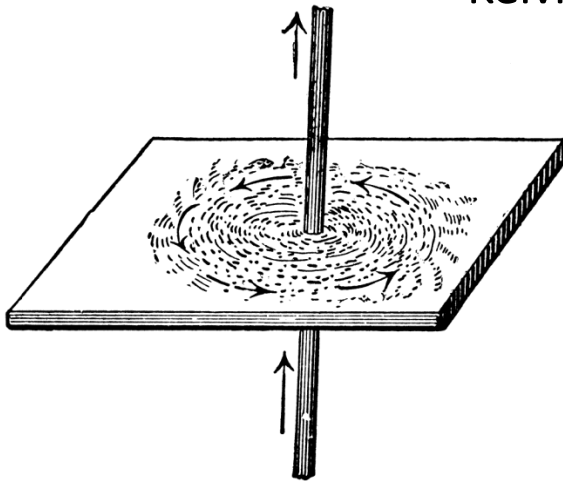
Ampere's law:

electrical currents generate (“stir up”) a magnetic field

$$\text{rot } \vec{H} = \left( \frac{\partial H_z}{\partial y} - \frac{\partial H_y}{\partial z} \right) \vec{i}_x + \left( \frac{\partial H_x}{\partial z} - \frac{\partial H_z}{\partial x} \right) \vec{i}_y + \left( \frac{\partial H_y}{\partial x} - \frac{\partial H_x}{\partial y} \right) \vec{i}_z = \vec{j}$$

$$\oint \vec{H} \cdot d\vec{l} = \iint \text{rot } \vec{H} dS = \iint \vec{j} dS = NI$$

Kelvin–Stokes theorem



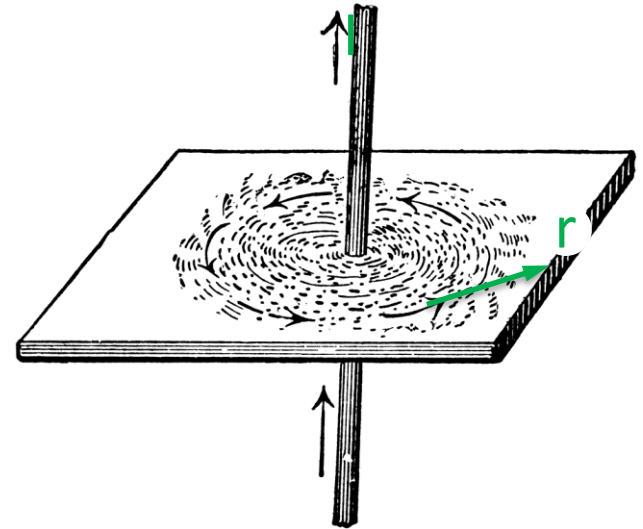
From Ampere's law without time dependencies and Gauss law we can derive the Biot & Savart law

$$\oint \vec{H} \cdot d\vec{l} = I \quad \rightarrow$$

$$H (2\pi r) = I \quad \rightarrow$$

$$H = \frac{I}{2\pi r}$$

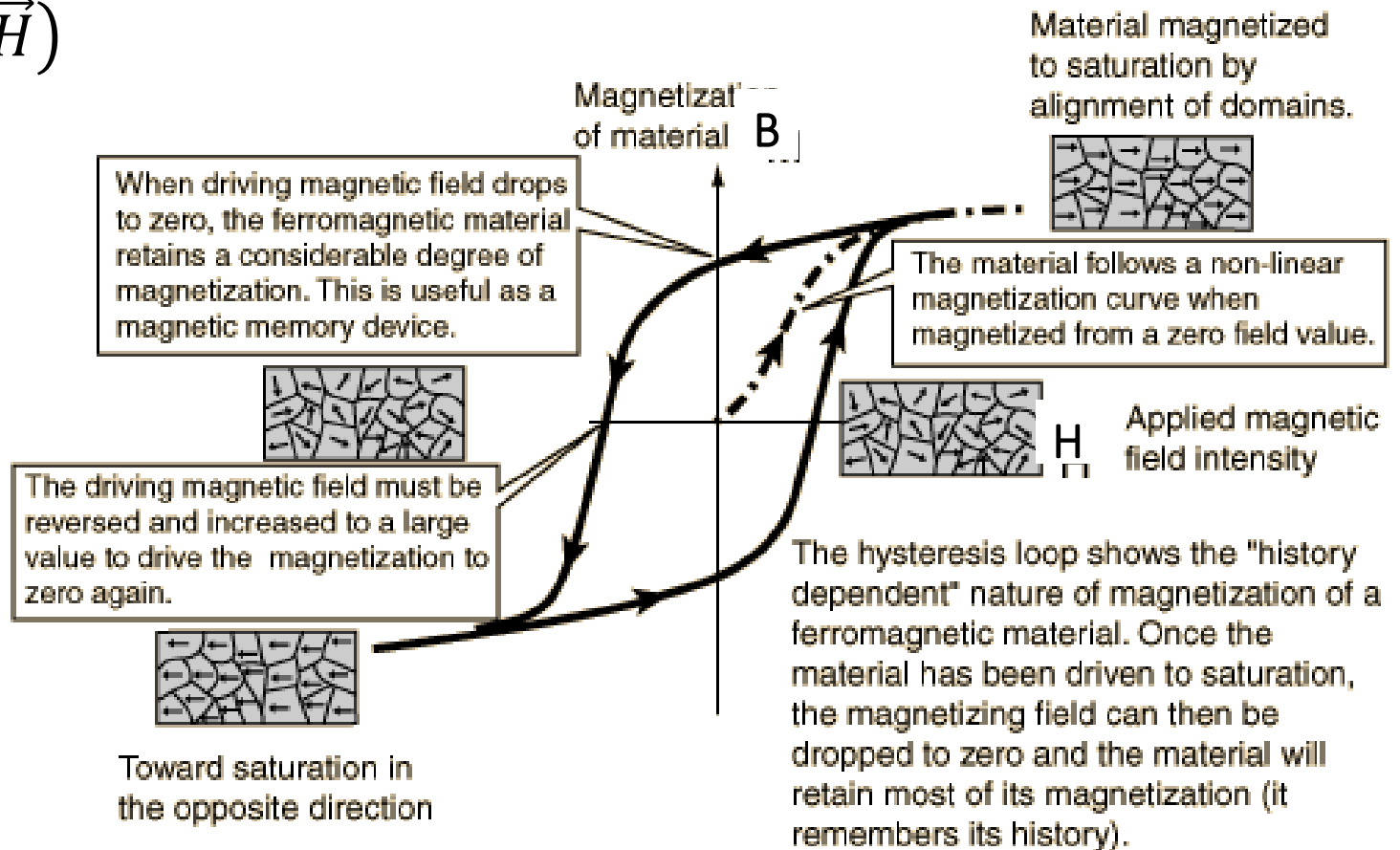
$$\vec{B} = \mu_0 \vec{H} \quad \rightarrow \quad B = \mu_0 H = \frac{\mu_0 I}{2\pi r}$$



# Non-linear materials - magnetisation

In a nonlinear material (with for ex. saturation and hysteresis), the constitutive law becomes more complex

$$\vec{B} = \mu_0 \vec{f}(\vec{H})$$



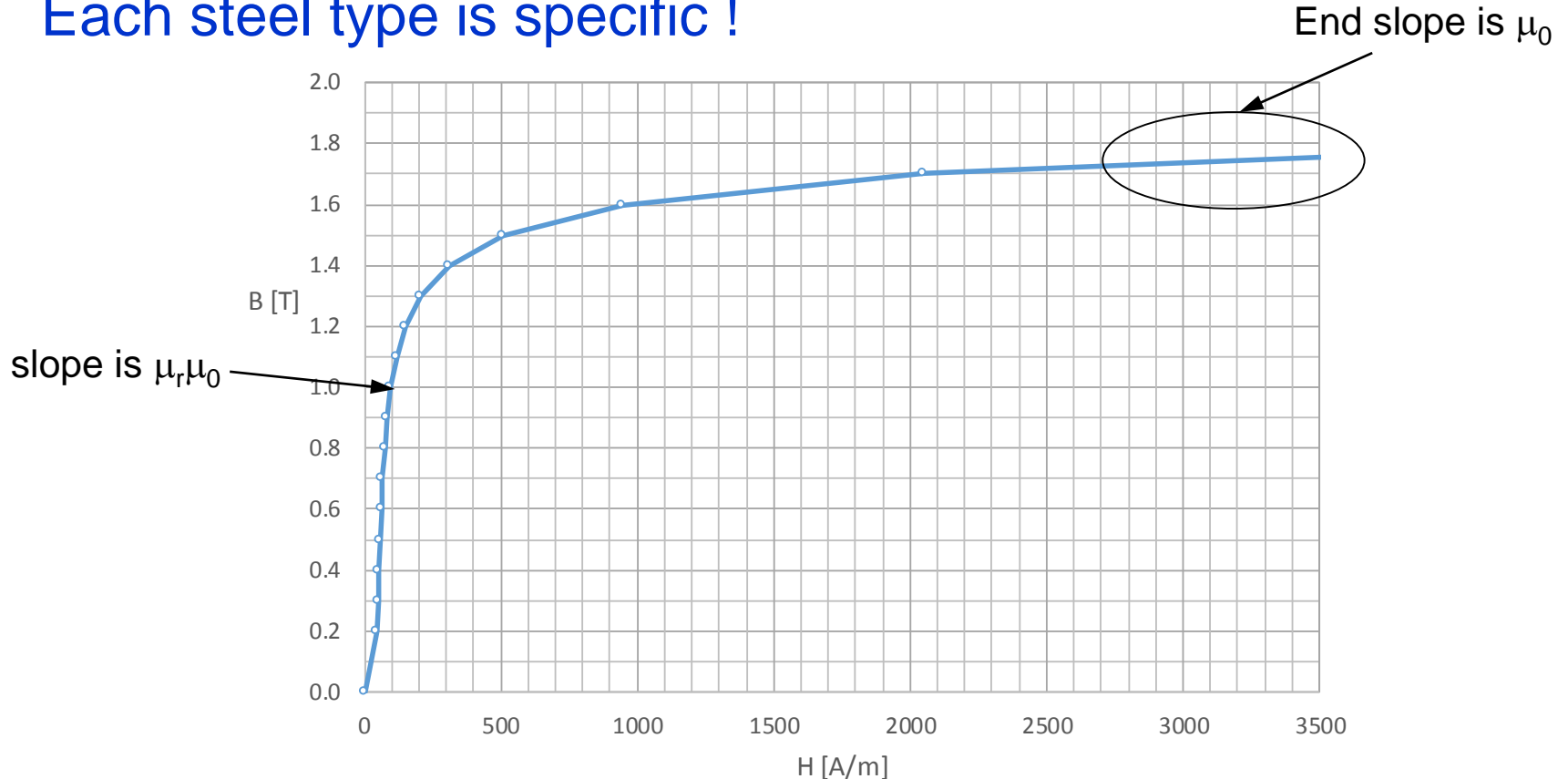


# Non-linear materials: BH curves

In most of our simulations we use a simple BH model for the material: this is a typical curve for an electrical steel.

The flattening-off is called “saturation”

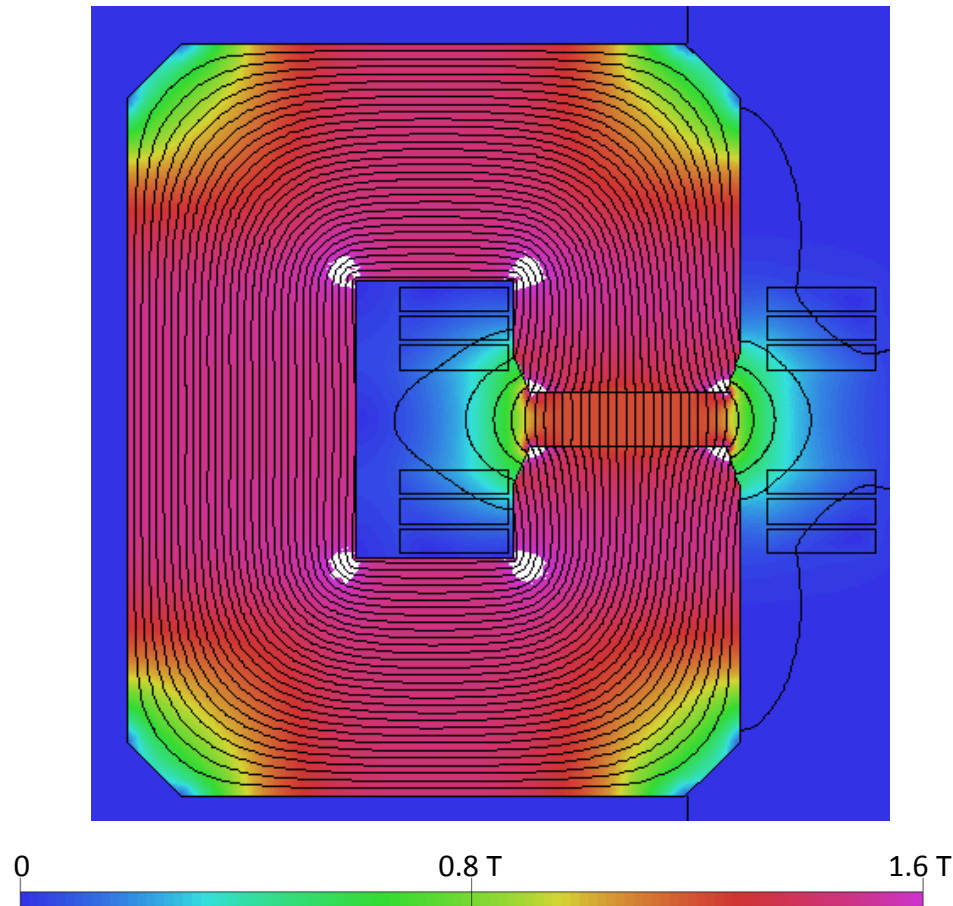
Each steel type is specific !





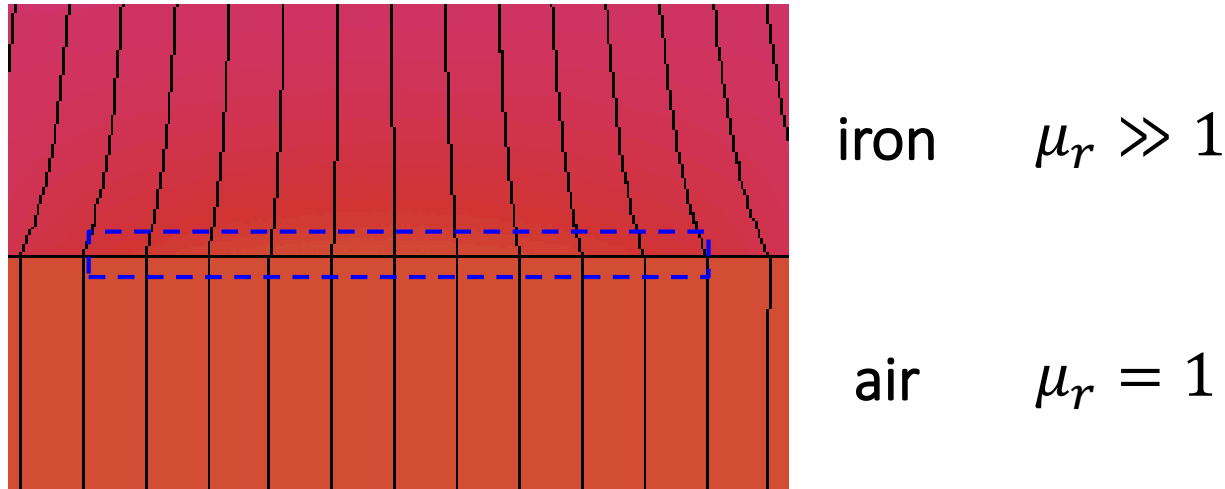
# Field in a magnet with a steel yoke I

Now, why do the flux lines come out perpendicular to the iron?



# Field in a magnet with a steel yoke II

Because they obey to Maxwell!!



$$H_{\parallel, \text{air}} = H_{\parallel, \text{iron}}$$

$$B_{\parallel, \text{air}} = \frac{B_{\parallel, \text{iron}}}{\mu_{r, \text{iron}}} \approx 0$$

$$B_{\perp, \text{air}} = B_{\perp, \text{iron}}$$



# Vector potential $\vec{A}$

This is an “advanced introduction”, so let’s introduce the vector potential (3D)

Definition:  $\vec{B} = \text{rot } \vec{A}$

In magnetostatics, we can combine Eqs. 1 to 3 in a more compact form (3D)

$$\left. \begin{array}{l} \text{div } \vec{B} = 0 \\ \text{rot } \vec{H} = 0 \\ \vec{B} = \mu_0 \vec{H} \end{array} \right\} \nabla^2 \vec{A} = \vec{0} \quad \begin{array}{l} \text{holds for} \\ \text{magnetostatics} \\ \text{and in air} \end{array}$$

In 2D this becomes a scalar Laplace equation

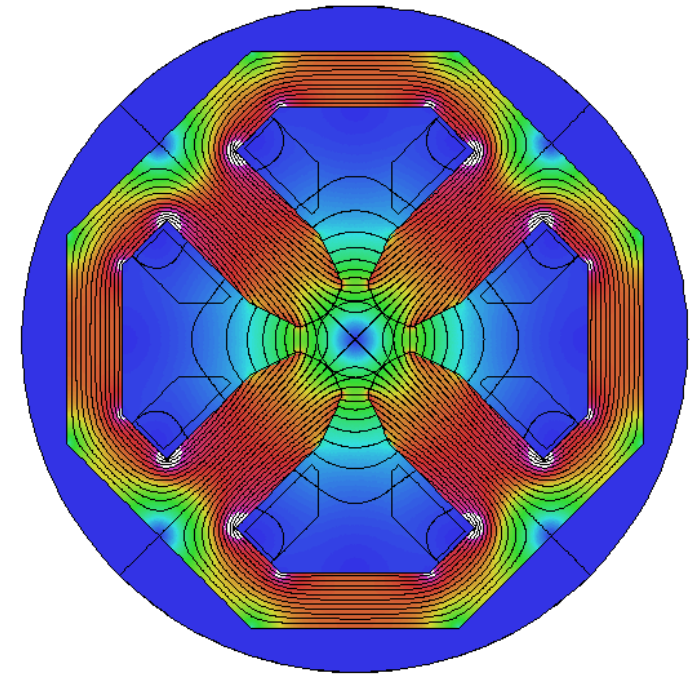
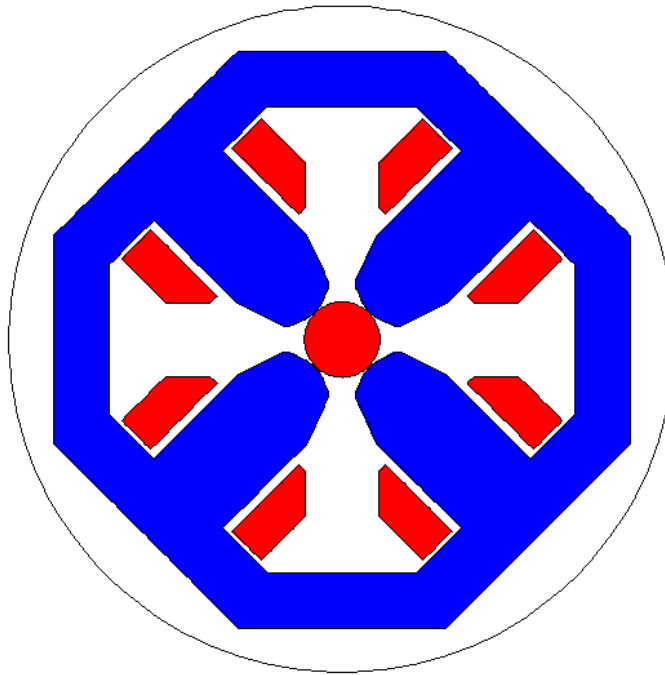
$$\nabla^2 A_z = 0 \quad \frac{\partial^2 A_z}{\partial x^2} + \frac{\partial^2 A_z}{\partial y^2} = 0 \quad \begin{array}{l} \text{holds for} \\ \text{magnetostatics} \\ \text{and in air} \end{array}$$



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# Multipoles I, quadrupole

We look at the 2D first: how can we conveniently describe the field in the aperture, for ex. in a quadrupole?

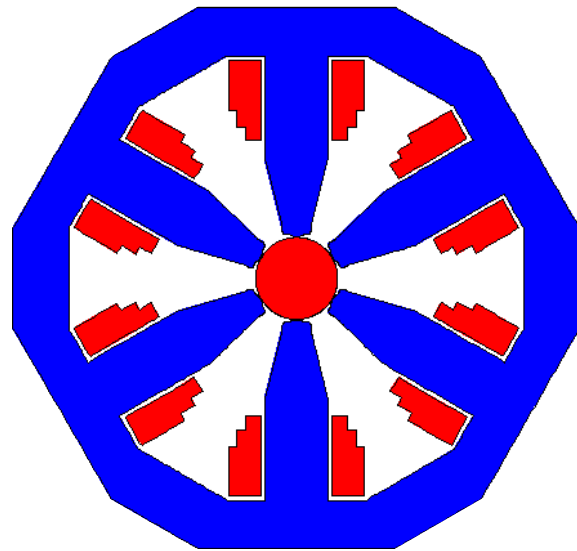


SESAME quadrupole  
 $B_{\text{pole}} = 0.6 \text{ T}$

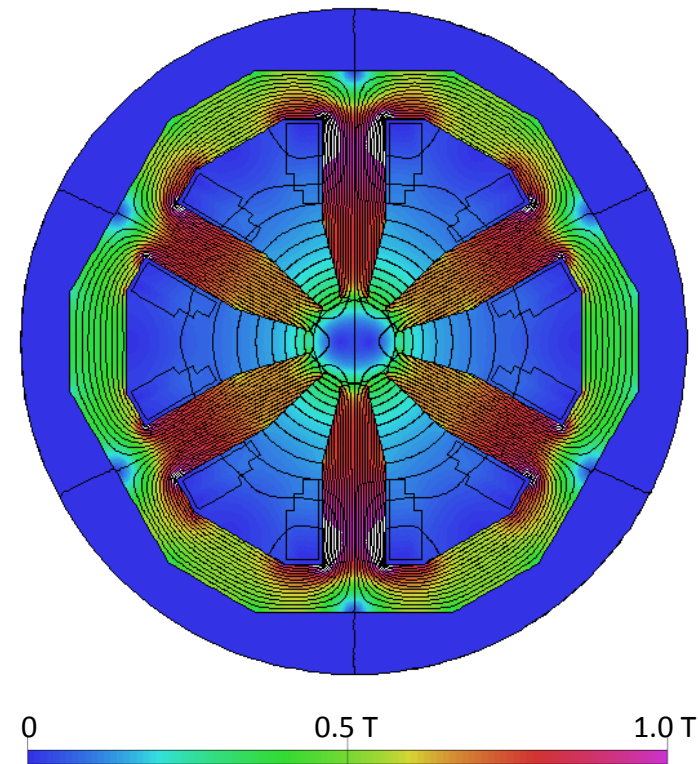


# Multipoles III, sextupole

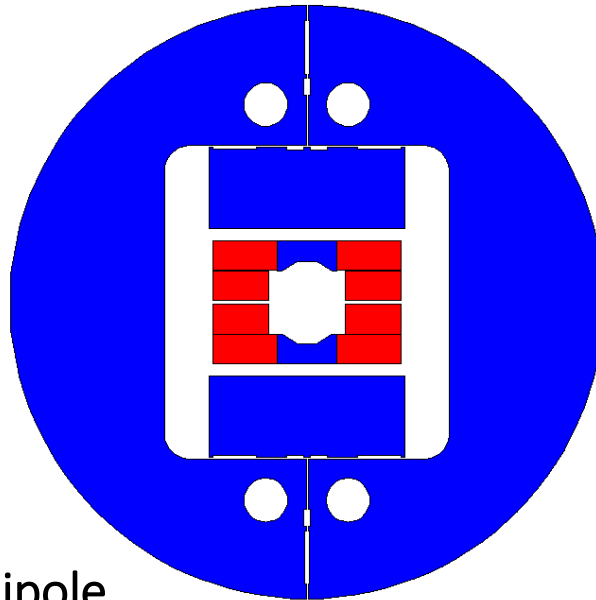
And in another resistive magnet, with a different configuration?



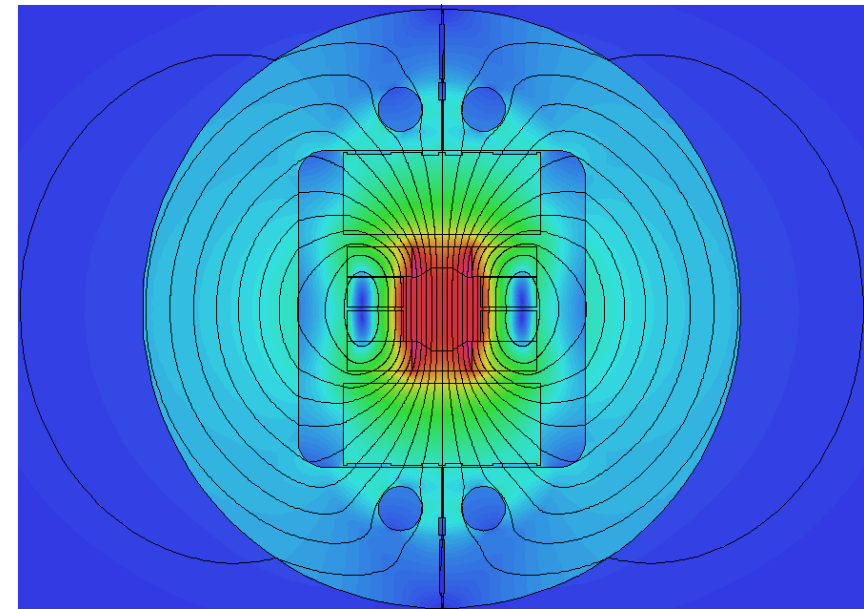
SESAME sextupole  
+ vertical dipole corrector



Can the same formalism also describe the field in the aperture of a superconducting dipole?

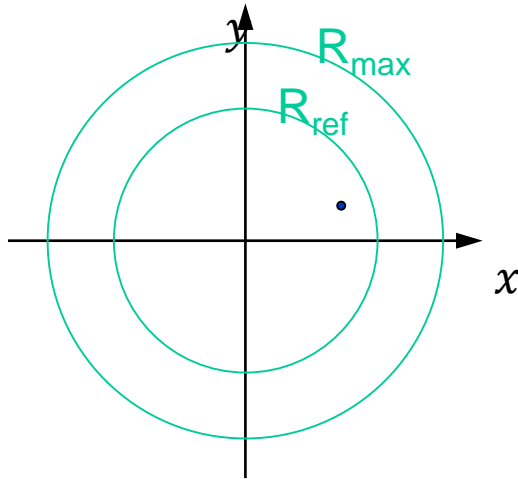


FRESCA2 dipole  
13 T



# Multipoles V, harmonic expansion

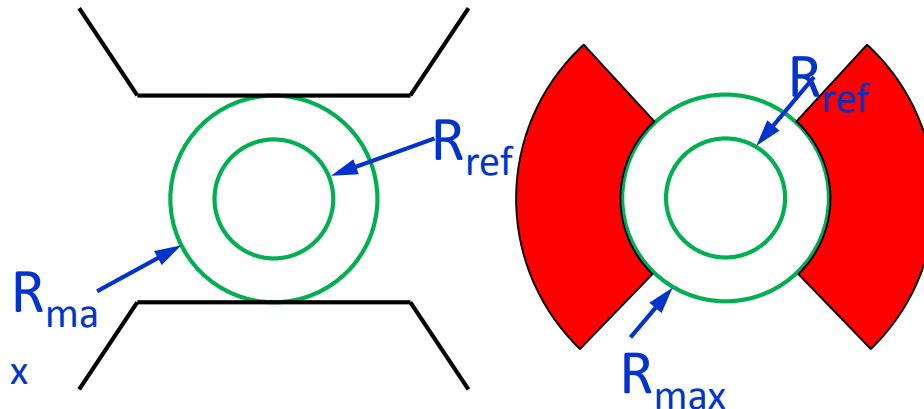
The solution is a harmonic (or multipole) expansion, describing the field (within a circle of validity) with scalar coefficients



$$(4) \quad B_y(z) + iB_x(z) = \sum_{n=1}^{\infty} (B_n + iA_n) \left( \frac{z}{R_{ref}} \right)^{n-1}$$

$$\text{with: } z = x + iy = r e^{i\theta}$$

This decomposition has two characteristic radii:  $R_{ref}$  and  $R_{max}$

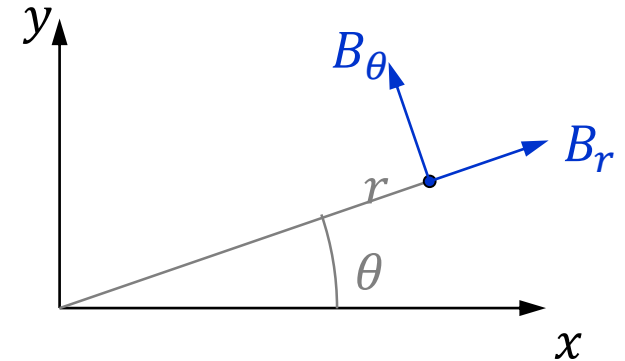




Expanding Eq. 4 in terms of radial and tangential components, we find sin and cos terms

$$B_r = \sum_{n=1}^{\infty} \left( \frac{r}{R_{ref}} \right)^{n-1} [B_n \sin(n\theta) + A_n \cos(n\theta)]$$

$$B_\theta = \sum_{n=1}^{\infty} \left( \frac{r}{R_{ref}} \right)^{n-1} [B_n \cos(n\theta) - A_n \sin(n\theta)]$$





# Multipoles VII, normalized coefficients

In most cases, there is a main fundamental component, to which the other terms are normalized

take: (4) 
$$B_y(z) + iB_x(z) = \sum_{n=1}^{\infty} (B_n + iA_n) \left( \frac{z}{R_{ref}} \right)^{n-1}$$

define: 
$$b_n = 10000 \frac{B_n}{B_N} \quad a_n = 10000 \frac{A_n}{B_N}$$

hence: 
$$B_y(z) + iB_x(z) = B_N \sum_{n=1}^{\infty} \frac{b_n + ia_n}{10000} \left( \frac{z}{R_{ref}} \right)^{n-1}$$

field strength

field shape

NB. The multipole coefficients  $b_n$  and  $a_n$  dimensions are referred to as “units”<sub>42</sub>

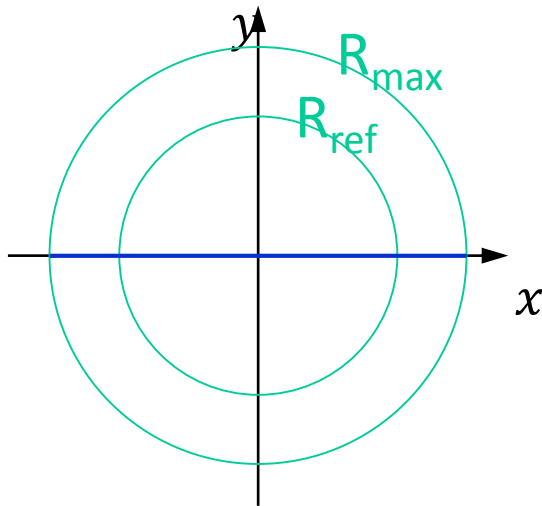


# Multipoles VIII, midplane field

Another useful expansion derived from Eq. 4 is that of  $B_y$  and  $B_x$  on the midplane, i.e. at  $y = 0$

$$B_y(x) = \sum_{n=1}^{\infty} B_n \left( \frac{x}{R_{ref}} \right)^{n-1} = B_1 + B_2 \frac{x}{R_{ref}} + B_3 \left( \frac{x}{R_{ref}} \right)^2 + \dots$$

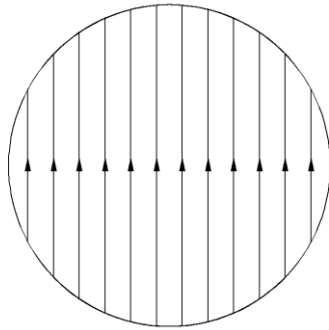
$$B_x(x) = \sum_{n=1}^{\infty} A_n \left( \frac{x}{R_{ref}} \right)^{n-1} = A_1 + A_2 \frac{x}{R_{ref}} + A_3 \left( \frac{x}{R_{ref}} \right)^2 + \dots$$



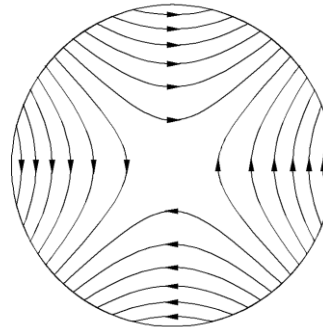
# Multipoles IX, multipole fields

Each multipole corresponds to a field distribution: adding them up, we can describe everything (this is nicely compatible with Maxwell)

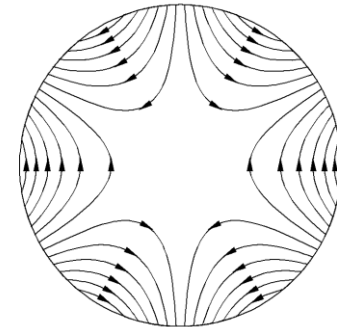
$B_1$ : normal dipole



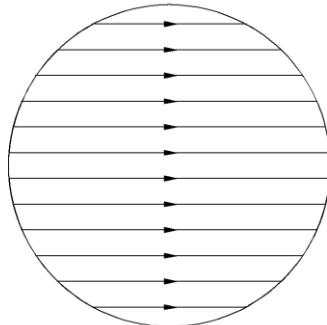
$B_2$ : normal quadrupole



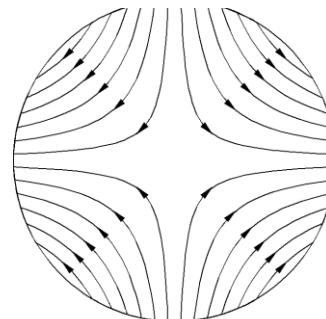
$B_3$ : normal sextupole



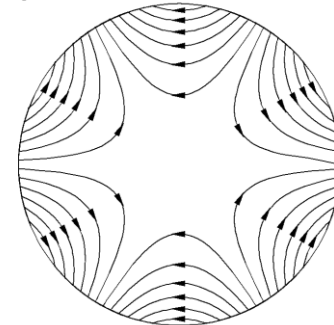
$A_1$ : skew dipole



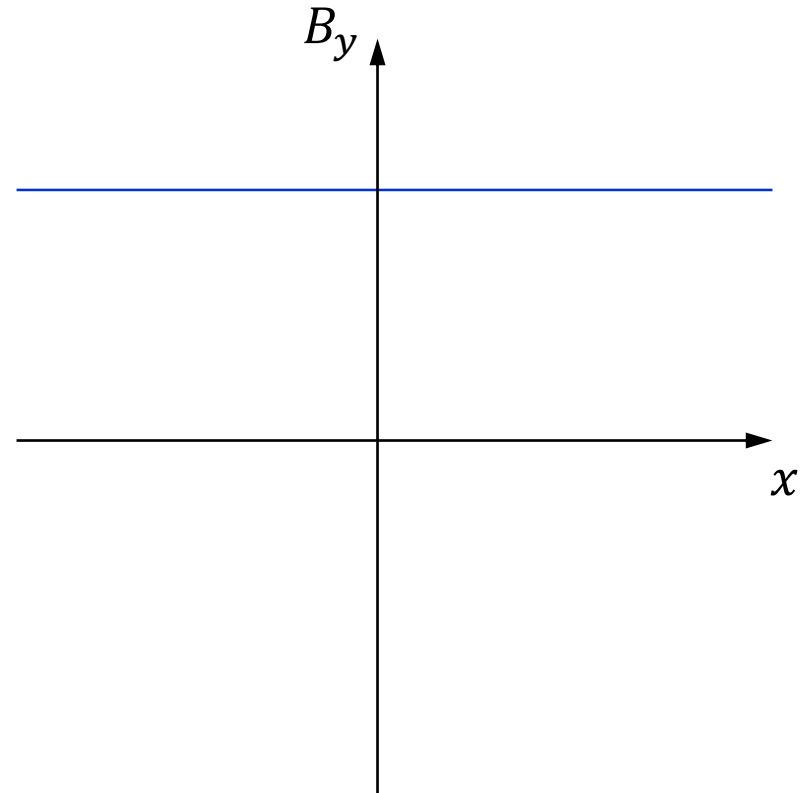
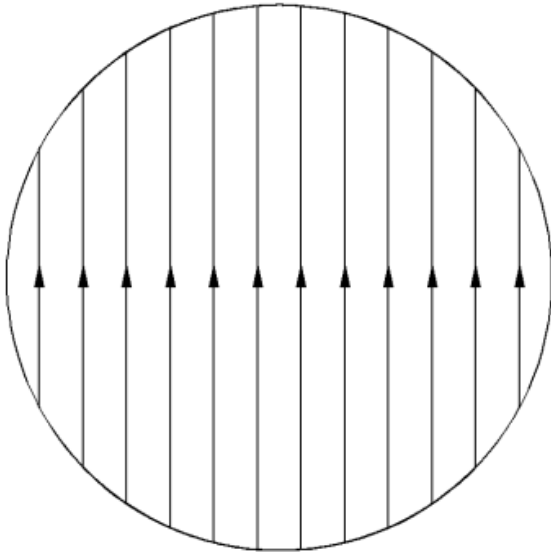
$A_2$ : skew quadrupole



$A_3$ : skew sextupole

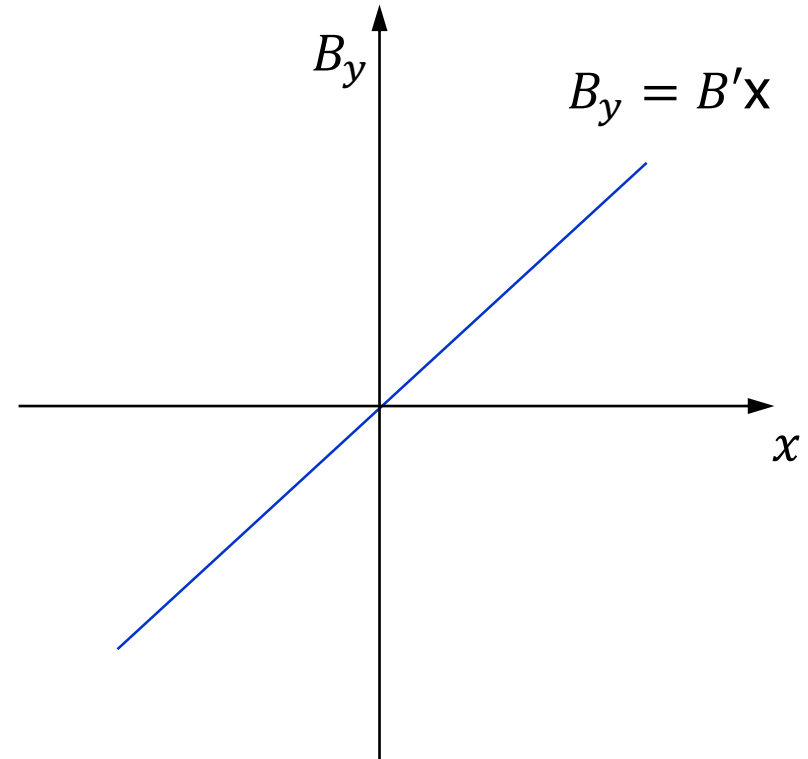
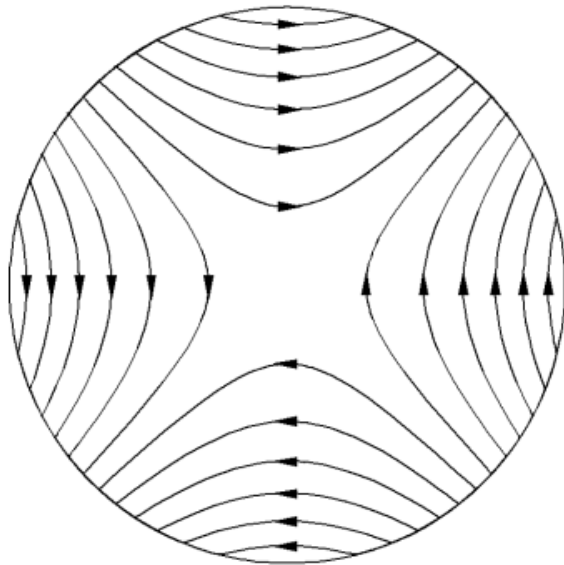


$B_1$  is the normal dipole



# Multipoles XI, quadrupole field

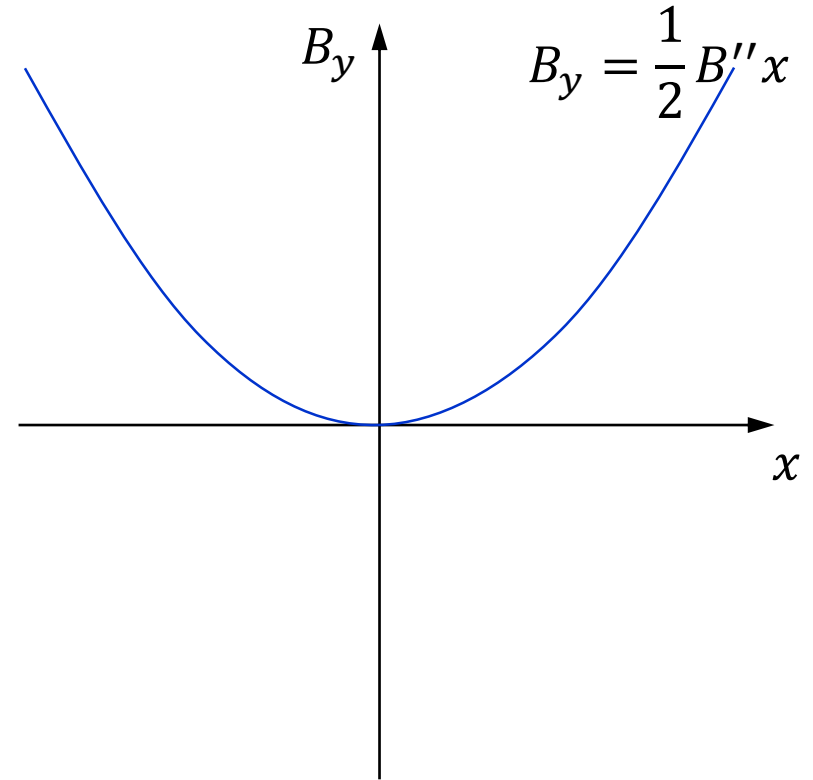
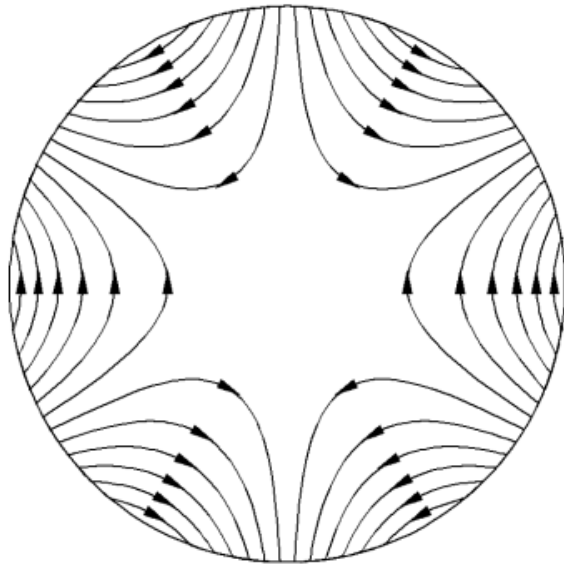
$B_2$  is the normal quadrupole



gradient: 
$$G = \frac{B_2}{R} = \frac{\partial B_y}{\partial x} = B'$$

field on the pole tip: 
$$B_{pole} = B'R_{pole}$$

$B_3$  is the normal sextupole

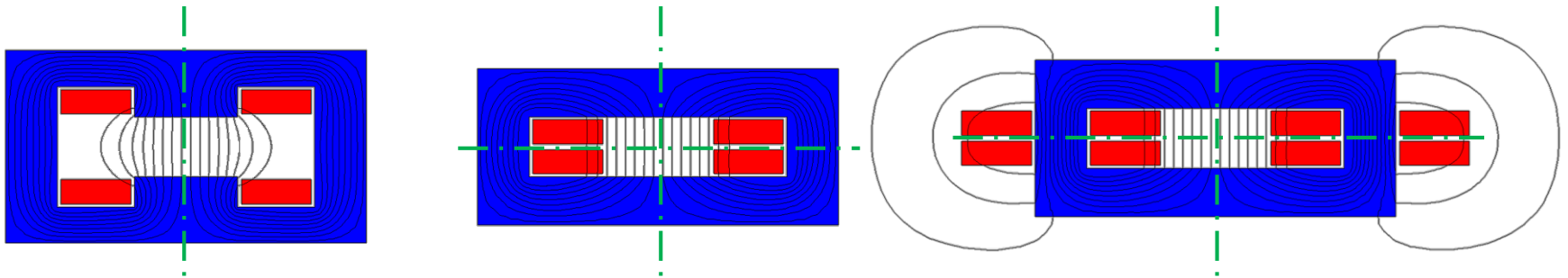


gradient: 
$$B'' = \frac{\partial^2 B_y}{\partial x^2} = \frac{2B_3}{R^2}$$

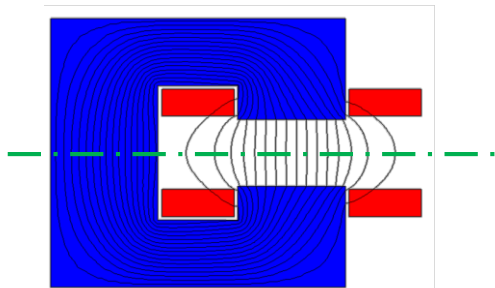
field on the pole tip: 
$$B_{pole} = \frac{1}{2} B'' R_{pole}^2$$

# Multipoles XIII, allowed multipoles

The allowed / not-allowed harmonics refer to the terms that shall / shall not cancel out thanks to design symmetries



fully symmetric dipoles: only  $B_1, b_3, b_5, b_7, b_9$ , etc.



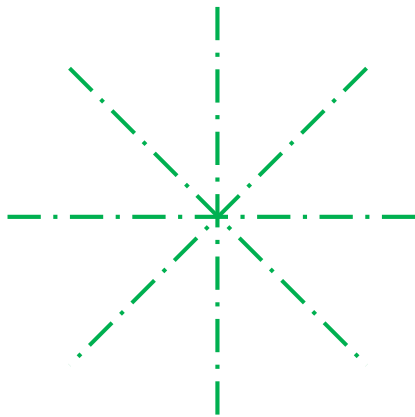
half symmetric dipoles:  $B_1, b_2, b_3, b_4, b_5$ , etc.



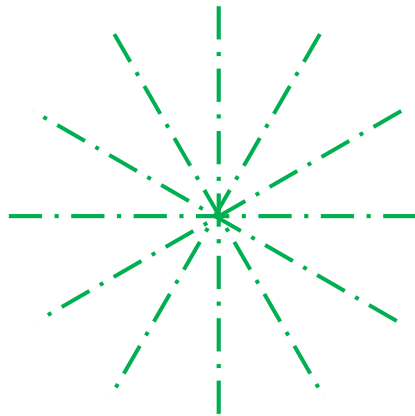


# Multipoles XIV, allowed multipoles

These are the allowed harmonics for fully symmetric quadrupoles and sextupoles

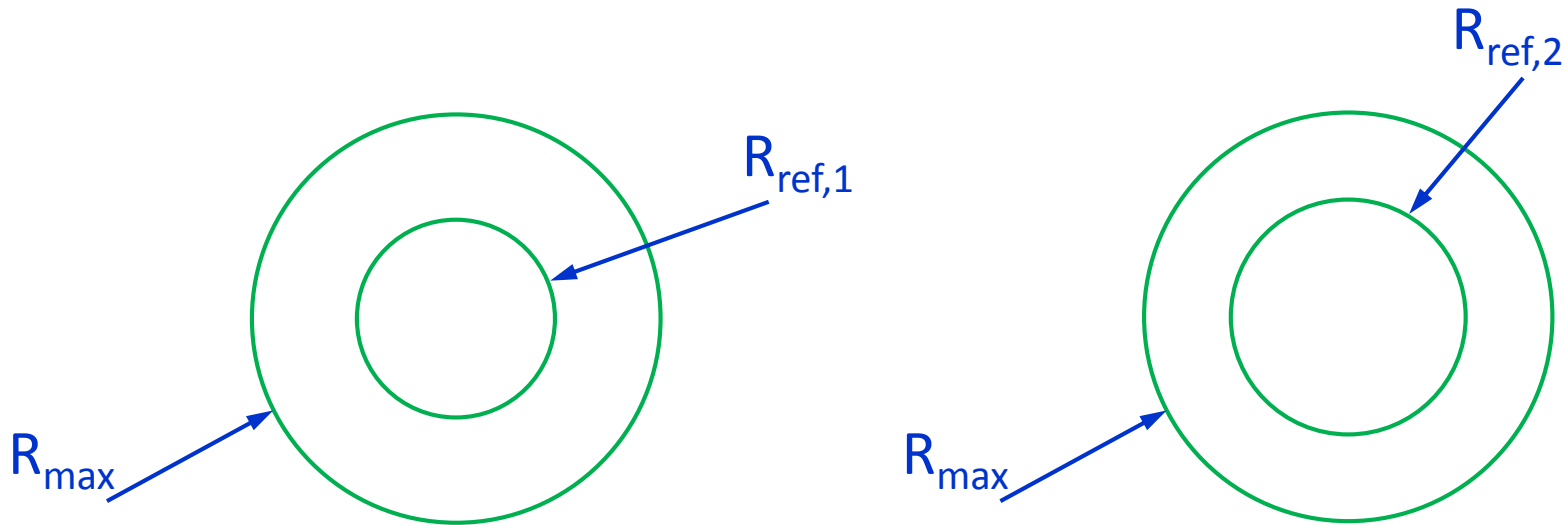


fully symmetric quadrupoles:  $B_2, b_6, b_{10}, b_{14}, b_{18}, \text{etc.}$



fully symmetric sextupoles:  $B_3, b_9, b_{15}, b_{21}, \text{etc.}$

We can change  $R_{\text{ref}}$  and scale up (or down) the harmonics

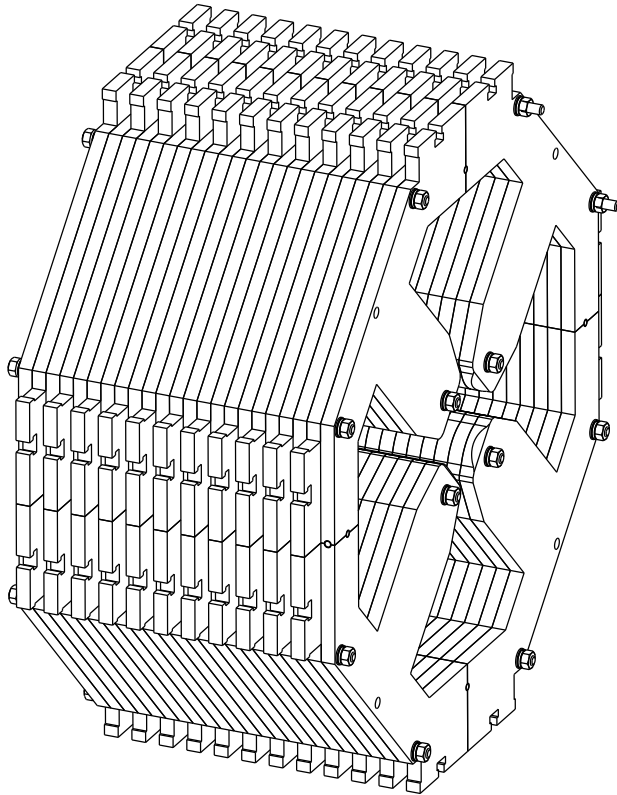


$$B_{n,2} = B_{n,1} \left( \frac{R_{\text{ref},2}}{R_{\text{ref},1}} \right)^{n-1}$$

$$b_{n,2} = b_{n,1} \left( \frac{R_{\text{ref},2}}{R_{\text{ref},1}} \right)^{n-N}$$

# Multipoles XVI, example

Let's have a look at a real case: the measurements of 33 quadrupoles built for SESAME

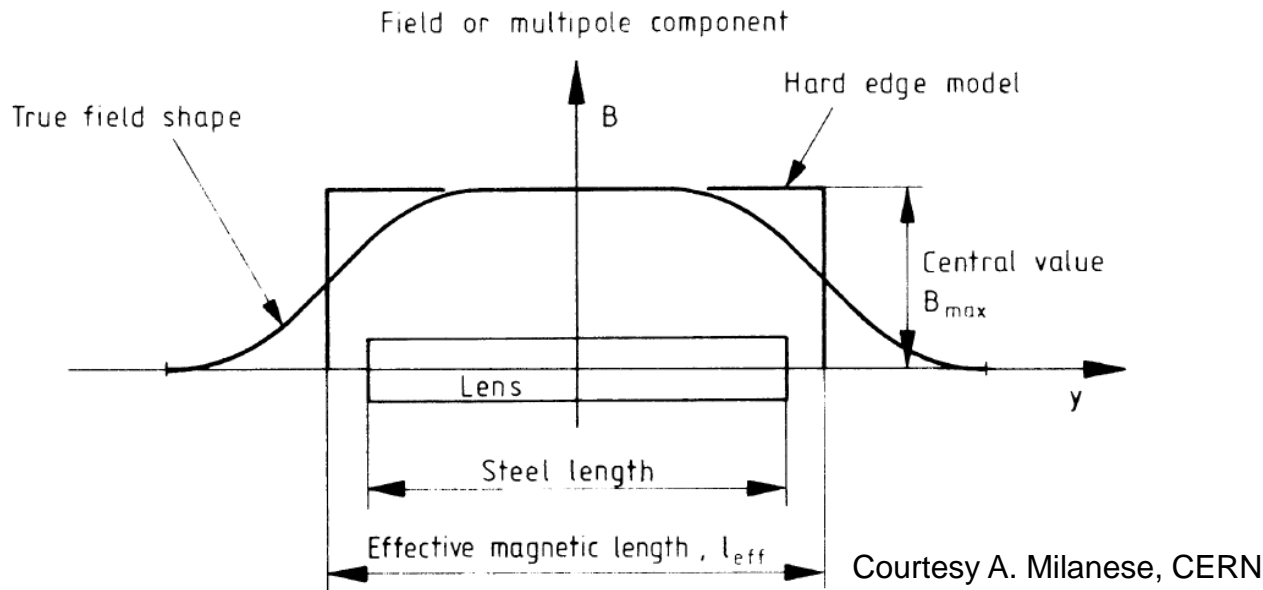


SESAME QF

mean $\pm$ rms	QF @ 250 A
$b_3$	$-0.2 \pm 0.8$
$a_3$	$-0.1 \pm 0.9$
$b_4$	$0.3 \pm 0.4$
$a_4$	$-0.3 \pm 0.1$
$b_5$	$0.0 \pm 0.1$
$a_5$	$0.0 \pm 0.1$
$b_6$	$-0.1 \pm 0.1$
$b_{10}$	$-0.3 \pm 0.0$
$b_{14}$	$0.3 \pm 0.0$

harmonics in  $10^{-4}$  at 24 mm radius

In 3D, the longitudinal dimension of the magnet is described by the magnetic length



$$l_m B_0 = \int_{-\infty}^{\infty} B(z) dz$$

magnetic length  $L_{\text{mag}}$  as a first approximation in an iron dominated magnet :

- For dipoles  $L_{\text{mag}} = L_{\text{yoke}} + d$
- For quadrupoles:  $L_{\text{mag}} = L_{\text{yoke}} + r$

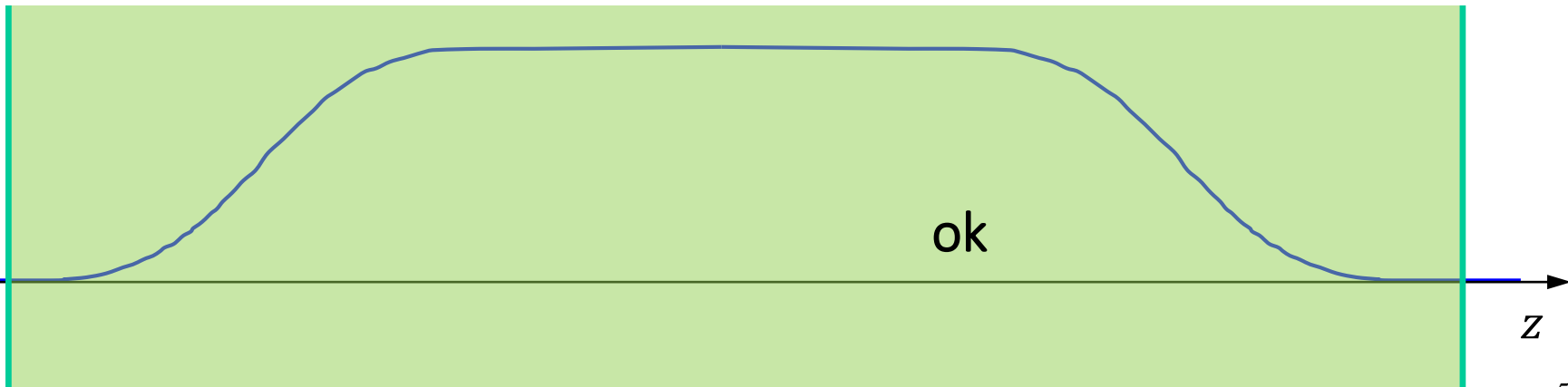
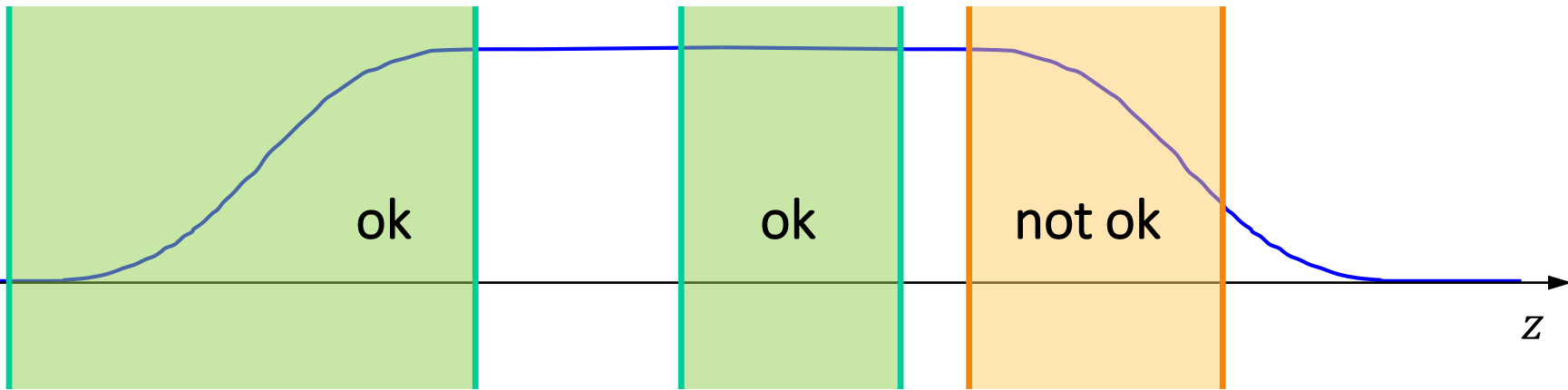
$d$  = pole distance

$r$  = radius of the inscribed circle between the 4 poles



# Multipoles along a magnet

This 2D decomposition holds also for the integrated 3D field, as long as at the start / end B is constant along z







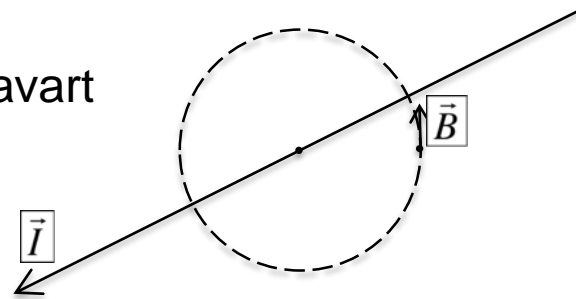
1. Introduction
2. Fundamentals 1: Maxwell and friends
3. Fundamentals 2: harmonics
4. A few practical considerations

# Magnetic fields, order of magnitudes

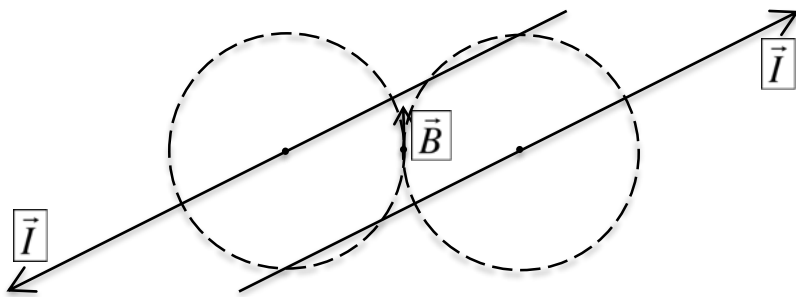
From Ampere's law with no time dependencies

(Integral form) 
$$\oint_C \vec{B} \times d\vec{l} = \mu_0 I_{encl.}$$

We can derive the law of Biot and Savart



$$\vec{B} = \frac{\mu_0 I}{2\pi r} \hat{j}$$



If you wanted to make a  $B = 1.5$  T magnet with just two infinitely thin wires placed at 100 mm distance in air one needs :

$$I = 187500 \text{ A}$$

- To get reasonable fields ( $B > 1$  T) one needs large currents
- Moreover, the field homogeneity will be poor



# Iron dominated magnets, simple example

With the help of an iron yoke we can get fields with less current

$$\oint_C \vec{H} \times d\vec{l} = N \times I$$

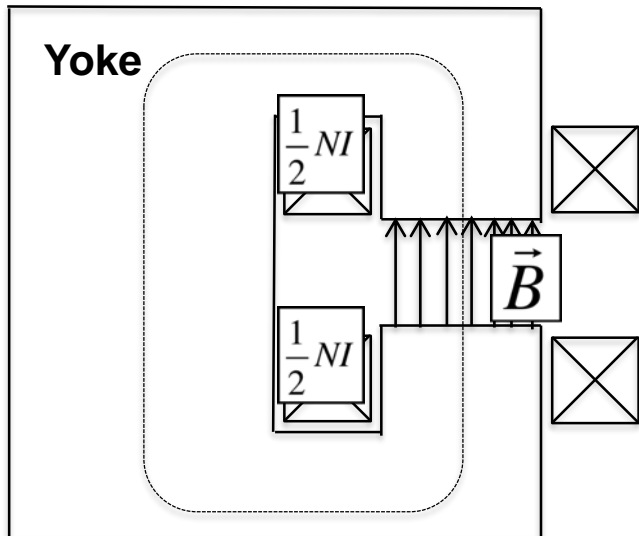
$$N \times I = H_{iron} \times l_{iron} + H_{airgap} \times l_{airgap} \quad \text{D}$$

$$N \times I = \frac{B}{\mu_0 \mu_r} \times l_{iron} + \frac{B}{\mu_0} \times l_{airgap} \quad \text{D}$$

$$N \times I = \frac{l_{airgap} \times B}{\mu_0}$$

This is valid as  $\mu_r \gg \mu_0$  in the iron : limited to  $B < 2 \text{ T}$

Example: C shaped dipole for accelerators



coil

$B = 1.5 \text{ T}$

Gap = 50 mm

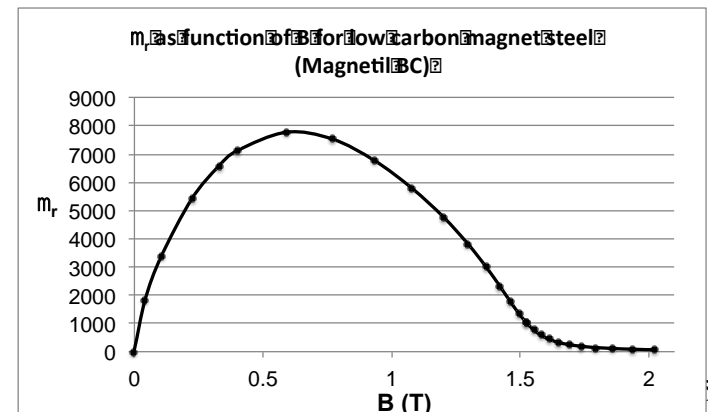
$N \cdot I = 59683 \text{ A}$

2 x 30 turn coil

$I = 994 \text{ A}$

@5 A/mm<sup>2</sup>, 200 mm<sup>2</sup>

14 x 14 mm Cu





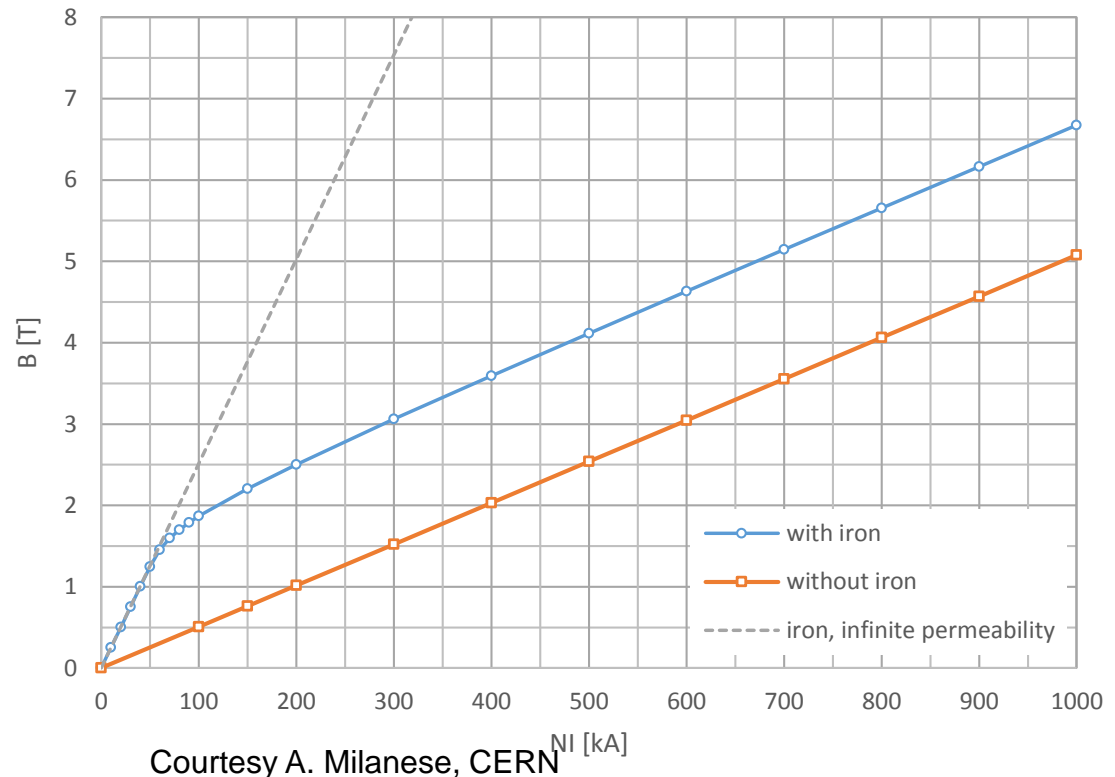
# Comparison : iron magnet and air coil

Imagine a magnet with a 50 mm vertical gap ( horizontal width ~100 mm)

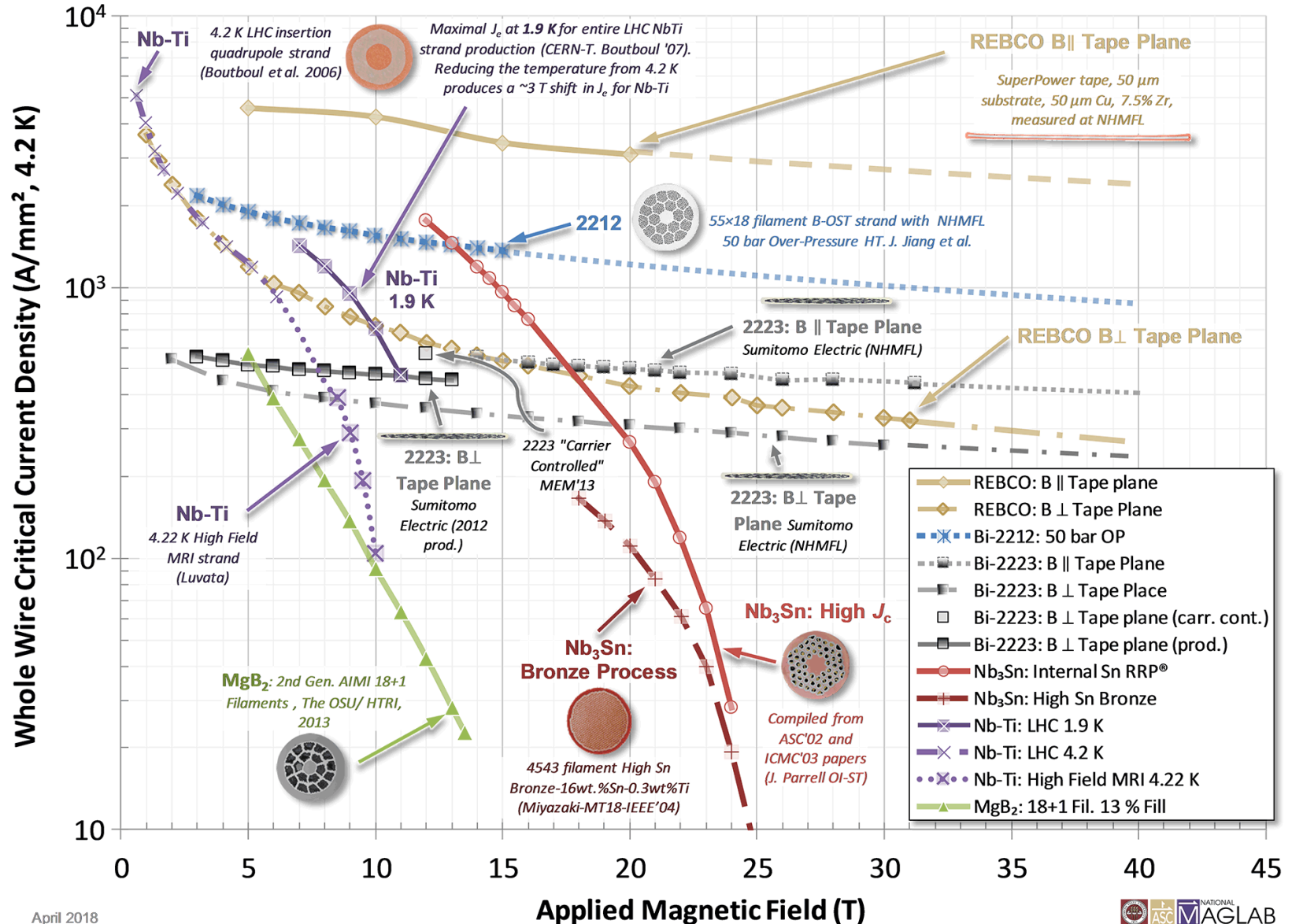
Iron magnet wrt to an air coil:

- Up to 1.5 T we get ~6 times the field
- Between 1.5 T and 2 T the gain flattens of : the iron saturates
- Above 2 T the slope is like for an air-coil: currents become too large to use resistive coils

These two curves are the transfer functions – B field vs. current – for the two cases



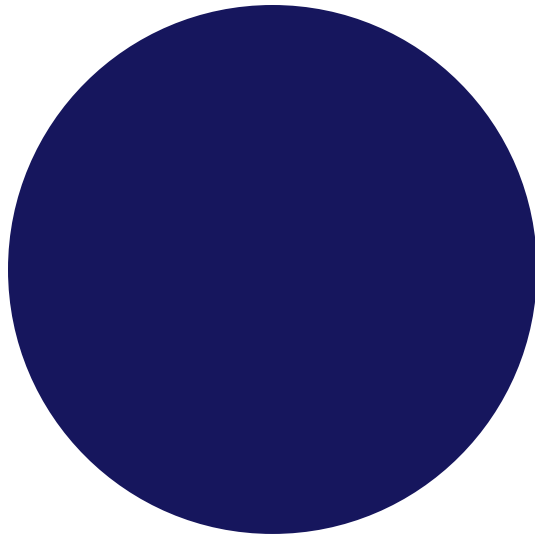
# Superconductors: what is available ?



# Comparing wires, LTS Superconductors vs Copper

Typical operational conditions (0.85 mm diameter strand)

Cu

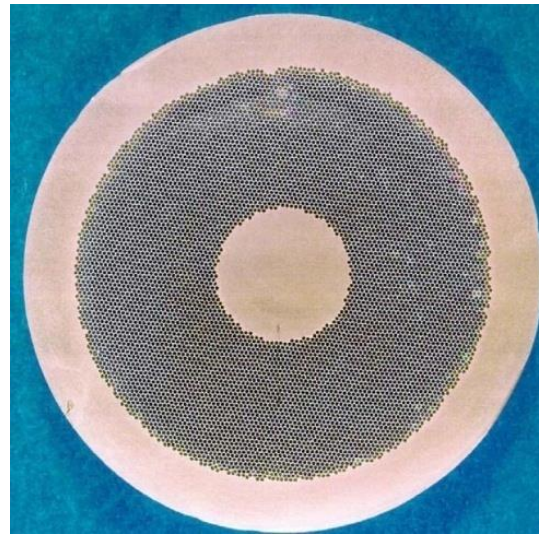


$J \sim 5 \text{ A/mm}^2$

$I \sim 3 \text{ A}$

$B = 2 \text{ T}$

Nb-Ti

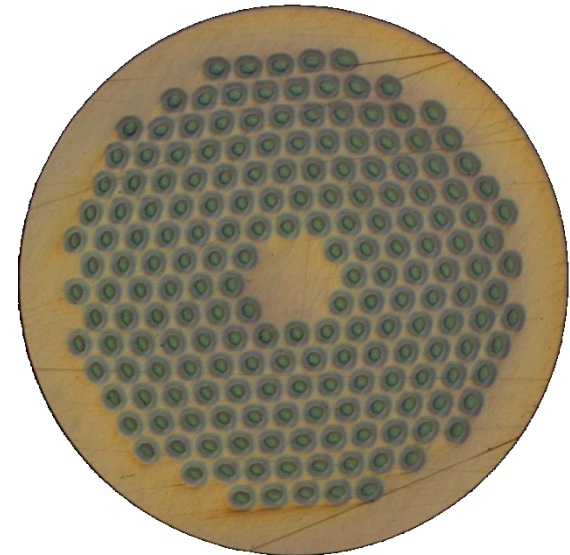


$J \sim 1500\text{-}2000 \text{ A/mm}^2$

$I \sim 400 \text{ A}$

$B = 8\text{-}9 \text{ T}$

Nb<sub>3</sub>Sn



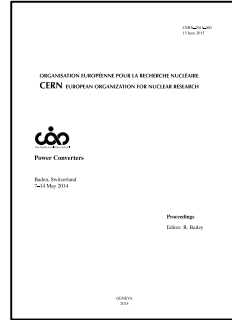
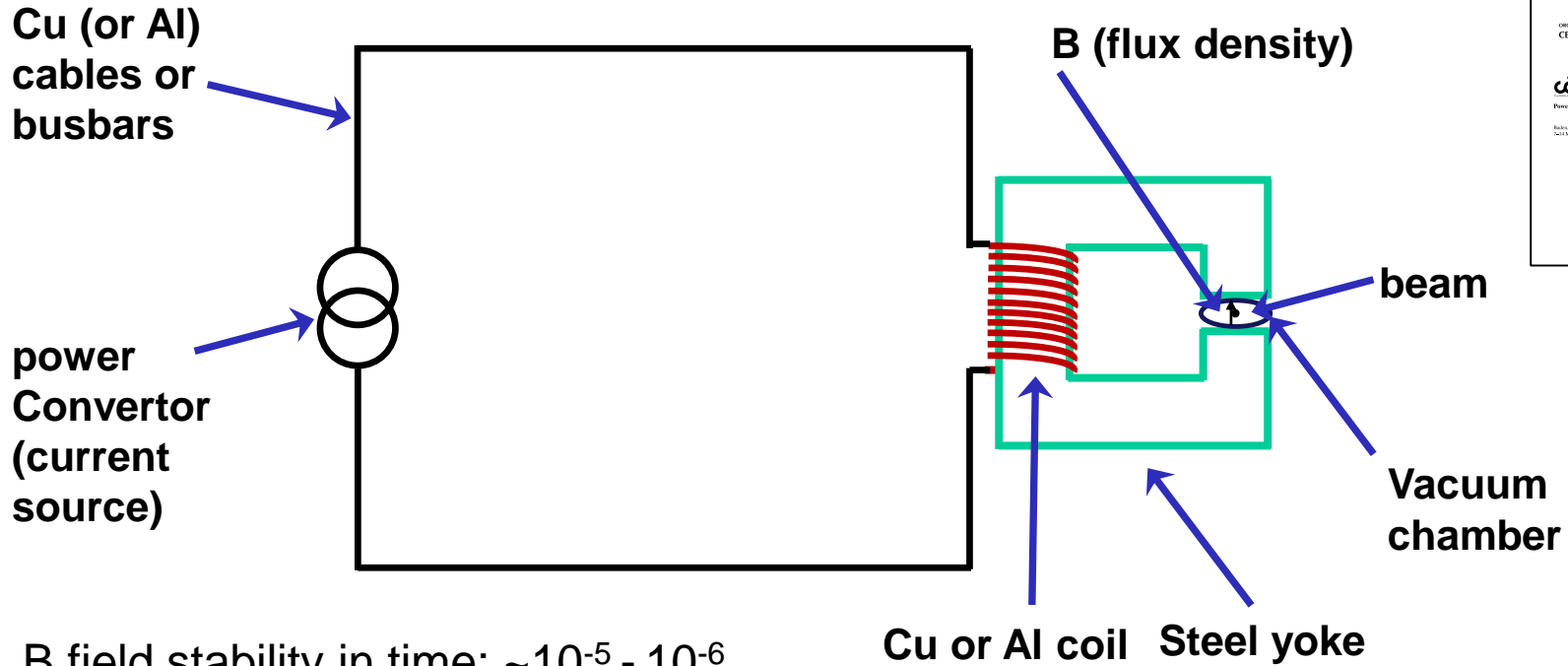
$J \sim 1500\text{-}2000 \text{ A/mm}^2$

$I \sim 400 \text{ A}$

$B = 12\text{-}13\text{-}16 \text{ T}$



# Magnets in an accelerator: power convertor and circuit



- B field stability in time:  $\sim 10^{-5} - 10^{-6}$
- Typical R of a magnet  $\sim 20\text{m}\Omega - 60\text{m}\Omega$
- Typical L of a magnet  $\sim 20\text{mH} - 200\text{mH}$
- Powering cable (for 500A): Cu  $250\text{ mm}^2$  (Cu:  $17\text{ n}\Omega\cdot\text{m}$ )  $R = 70\text{ }\mu\Omega/\text{m}$ , for 200m:  $R = 13\text{m}\Omega$
- Take a typical rise time 1s

Then the Power Convertor has to Supply : 0-500 A with a stability of a few ppm.

Voltage up to 40 V (resistive)  
And 100 V (inductive)



# Literature on Magnets

## Books

- 1) M. Wilson, Superconducting magnets / Oxford : Clarendon Press, 1983 (Repr. 2002). - 335 p
- 2) K-H. Mess, P. Schmüser, S. Wolff, Superconducting Accelerator Magnets, Singapore, World Scientific, 1996. - 218 p.
- 3) Y. Iwasa, Case studies in superconducting magnets : design and operational issues . - 2nd ed. Berlin : Springer, 2009. - 682 p.
- 4) S. Russenschuck, Field computation for accelerator magnets : analytical and numerical methods for electromagnetic design and optimization / Weinheim : Wiley, 2010. - 757 p.
- 5) CERN Accelerator school, Magnets, Bruges, Belgium 16 – 25 June 2009, Editor: D. Brandt, CERN–2010–004
- 6) G.E.Fisher, “Iron Dominated Magnets” AIP Conf. Proc., 1987 -- Volume 153, pp. 1120-1227
- 7) J. Tanabe, “Iron Dominated Electromagnets”, World Scientific, ISBN 978-981-256-381-1, May 2005
- 8) P. Campbell, Permanent Magnet Materials and their Application, ISBN-13: 978-0521566889

## Schools

1. CAS Bruges, 2009, specialized course on magnets, 2009, CERN-2010-004
2. CAS Frascati 2008, Magnets (Warm) by D. Einfeld
3. CAS Varna 2010, Magnets (Warm) by D. Tommasini
4. N. Marks, Magnets for Accelerators, J.A.I., Jan. 2015
5. Superconducting magnets for particle accelerators in USPAS

## Conference series

1. Magnet Technology, MT
2. Applied Superconductivity, ASC
3. European Applied superconductivity, EUCAS



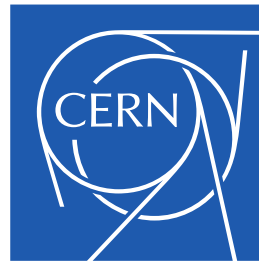
# Literature on Magnets

## Papers and reports

- 1) D. Tommasini, "Practical definitions and formulae for magnets," CERN, Tech. Rep. EDMS 1162401, 2011
- 2) S. Caspi, P. Ferracin, "Limits of Nb3Sn accelerator magnets", *Particle Accelerator Conference (2005)* 107-11.
- 3) S. Caspi, P. Ferracin, S. Gourlay, "Graded high field Nb3Sn dipole magnets", *19th Magnet Technology Conference, IEEE Trans. Appl. Supercond.*, (2006) in press.
- 4) E. Todesco, L. Rossi, "Electromagnetic Design of Superconducting Dipoles Based on Sector Coils", *Phys. Rev. Spec. Top. Accel. Beams* 10 (2007) 112401
- 5) E. Todesco, L. Rossi, AN ESTIMATE OF THE MAXIMUM GRADIENTS IN SUPERCONDUCTING QUADRUPOLES, CERN/AT 2007-11(MCS),
- 6) P. Fessia, et al., Parametric analysis of forces and stresses in superconducting dipoles, *IEEE, trans. Appl, Supercond.* Vol 19, no3, June 2009.
- 7) P. Fessia, et al., Parametric analysis of forces and stresses in superconducting quadrupole sector windings, sLHC Project Report 0003
- 8) A. Devred, Practical Low-Temperature Superconductors for Electromagnets, CERN yellow report

## Websites

- 1) <http://www.magnet.fsu.edu/magnettechnology/research/asc/plots.html>



[www.cern.ch](http://www.cern.ch)