

2020 Joint Universities Accelerator School

Superconducting Magnets Section II

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Outline

• Section I

- Particle accelerators and magnets
- Superconductivity and practical superconductors

• Section II

Magnetic design

• Section III

- Coil fabrication
- Forces, stress, pre-stress
- Support structures

• Section IV

• Quench, training, protection

Magnetic design Introduction

- The magnetic design is one of the first steps in the a superconducting magnet development
- It starts from the **requirements** (from accelerator physicists, researchers, medical doctors...others)
 - A field "shape"
 - Dipole, quadrupole, etc
 - A field magnitude
 - Usually with low T superconductors from 5 to 20 T
 - A field homogeneity
 - Uniformity inside a solenoid, harmonics in a accelerator magnet
 - A given **aperture** (and **volume**)
 - Some cm diameter for accelerator magnets, much more for detectors and fusion magnets

Magnetic design

- How much conductor do we need to meet the requirements?
- And in **which configuration**?

• Outline

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- How do we create a **perfect field**?
- How do we express the field and its "**imperfections**"?
- How do we **design a coil** to minimize field errors?
- Which is the **maximum field** we can get?
- **Overview** of different designs



References

- Magnetic design
 - K.-H. Mess, P. Schmuser, S. Wolff, "Superconducting accelerator magnets", Singapore: World Scientific, 1996.
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 Within a cylinder carrying *j*₀, the field is perpendicular to the radial direction and proportional to the distance to the centre *r*:

$$B = -\frac{\mu_0 j_0 r}{2}$$

• Combining the effect of two intersecting cylinders

$$B_{x} = \frac{\mu_{0} j_{0} r}{2} \left\{ -r_{1} \sin \theta_{1} + r_{2} \sin \theta_{2} \right\} = 0$$

$$B_{y} = \frac{\mu_{0} j_{0} r}{2} \left\{ -r_{1} \cos \theta_{1} + r_{2} \cos \theta_{2} \right\} = -\frac{\mu_{0} j_{0}}{2} s$$

- A uniform current density in the area of two **intersecting circles** produces a pure dipole
 - The aperture is not circular
 - Not easy to simulate with a flat cable
- Similar proof for **intersecting ellipses**







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Perfect dipole field Thick shell with $cos\theta$ current distribution

• If we assume

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- $J = J_0 \cos \theta$ where $J_0 [A/m^2]$ is \perp to the crosssection plane
- Inner (outer) radius of the coils = *a*1 (*a*2)
- The generated field is a **pure dipole**

$$B_{y} = -\frac{\mu_0 J_0}{2} (a_2 - a_1)$$

- Linear dependence on **coil width**
- **Easier** to achieve with a Rutherford cable



Perfect quadrupole field

- Intercepting ellipses or circles
- Thick shell with *cos2θ* current distribution
- If we assume
 - $J = J_0 \cos 2\theta$ where $J_0 [A/m^2]$ is \perp to the crosssection plane
 - Inner (outer) radius of the coils = *a*1 (*a*2)

$$G = \frac{B_{y}}{r} = -\frac{\mu_0 J_0}{2} \ln \frac{a_2}{a_1}$$

• And so on...

- Perfect sextupoles: $\cos 3\theta$ or **3** intersect. ellipses
- Perfect 2n-poles: $\cos n\theta$ or n intersecting ellipses





From ideal to practical configuration

- How can I reproduce **thick shell with a** *cosθ* distribution with a cable?
 - Rectangular cross-section and constant *J*
- First "rough" approximation
 - Sector dipole
- Better ones
 - More **layers** and **wedges** to reduce *J* towards 90°

- As a result, the field is **not perfect** anymore
 - How can I express in improve the "imperfect" field inside the aperture?







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Field representation <u>Max</u>well equations

Maxwell equations for magnetic field

$$\nabla \cdot B = \frac{\partial B_x}{\partial x} + \frac{\partial B_y}{\partial y} + \frac{\partial B_z}{\partial z} = 0 \qquad \nabla \times B = \mu_0 J + \mu_0 \varepsilon_0 \frac{\partial E}{\partial t}$$

• In absence of charge and magnetized material

$$\nabla \times B = \left(\frac{\partial B_y}{\partial z} - \frac{\partial B_z}{\partial y}, \frac{\partial B_z}{\partial x} - \frac{\partial B_x}{\partial z}, \frac{\partial B_x}{\partial y} - \frac{\partial B_y}{\partial x}\right) = 0$$



• If $\frac{\partial B_z}{\partial z} = 0$ (constant longitudinal field), then

$$\frac{\partial B_x}{\partial x} + \frac{\partial B_y}{\partial y} = 0 \qquad \qquad \frac{\partial B_x}{\partial y} - \frac{\partial B_y}{\partial x} = 0$$

Field representation Analytic functions



Maxwell gives

$$\frac{\partial B_{y}}{\partial x} - \frac{\partial B_{x}}{\partial y} = 0$$
$$\frac{\partial B_{y}}{\partial y} + \frac{\partial B_{x}}{\partial x} = 0$$

$$\begin{cases} \frac{\partial f_x}{\partial x} - \frac{\partial f_y}{\partial y} = 0\\ \frac{\partial f_x}{\partial y} + \frac{\partial f_y}{\partial x} = 0 \end{cases}$$

Cauchy-Riemann conditions

and therefore the function $B_y + iB_x$ is analytic

$$B_{y}(x, y) + iB_{x}(x, y) = \sum_{n=1}^{\infty} C_{n}(x + iy)^{n-1}$$

where *C*_n are **complex coefficients**

$$B_{y}(x, y) + iB_{x}(x, y) = \sum_{n=1}^{\infty} C_{n}(x + iy)^{n-1} = \sum_{n=1}^{\infty} (B_{n} + iA_{n})(x + iy)^{n-1}$$

• Advantage: we reduce the description of the field to a (simple) series of complex coefficients

Field representation Harmonics

• What are these coefficients (or **harmonics**)?

 $B_{y} + iB_{x} \Longrightarrow (B_{2} + iA_{2})(x + iy) = (B_{2}x + iB_{2}y) + (iA_{2}x - A_{2}y)$

$$B_{y}(x, y) + iB_{x}(x, y) = \sum_{n=1}^{\infty} C_{n}(x + iy)^{n-1} = \sum_{n=1}^{\infty} (B_{n} + iA_{n})(x + iy)^{n-1}$$

• For $n=1 \rightarrow dipole$ $B_{v} + iB_{x} \Rightarrow (B_{1} + iA_{1})$

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• For $n=2 \rightarrow quadrupole$





by K.-H. Mess, et al.

Field representation Harmonics

• So, each coefficient corresponds to a "pure" multipolar field

$$B_{y}(x, y) + iB_{x}(x, y) = \sum_{n=1}^{\infty} C_{n}(x + iy)^{n-1} = \sum_{n=1}^{\infty} (B_{n} + iA_{n})(x + iy)^{n-1}$$







by K.-H. Mess, et al.

• The field harmonics are rewritten as (EU notation)

$$B_{y} + iB_{x} = 10^{-4} B_{1} \sum_{n=1}^{\infty} (b_{n} + ia_{n}) \left(\frac{x + iy}{R_{ref}}\right)^{n-1}$$

- We factorize the main component (*B*₁ for dipoles, *B*₂ for quadrupoles)
- We introduce a reference radius R_{ref} to have dimensionless coefficients
- We factorize 10⁻⁴ since the deviations from ideal field are ~0.01%
- The coefficients $b_{n'} a_n$ are called <u>normalized multipoles</u>
 - b_n are the <u>normal</u>, a_n are the <u>skew</u> (adimensional)

Field representation Harmonics



- The coefficients b_n , a_n are called <u>normalized multipoles</u>
 - b_n are the <u>normal</u>, a_n are the <u>skew</u> (adimensional)
- Reference radius is usually chosen as 2/3 of the aperture radius



Field representation Harmonics

- One can demonstrate that with line currents with a **dipole** or a **quadrupole symmetry**, most of the **multipoles cancelled**
- For $n=1 \rightarrow dipole$
 - Only b_3 , b_5 , b_7 , are present
- For $n=2 \rightarrow quadrupole$
 - Only b_6 , b_{10} , b_{14} , are present
- ...and so on
- These multipoles are called *allowed multipoles*
- The field quality optimization of a coil lay-out concerns only a few quantities
 - For a dipole, usually *b*3 , *b*5 , *b*7 , and possibly *b*9 , *b*11



Back to the original issue: From ideal to practical configuration

- How can I reproduce **thick shell with a** *cosθ* distribution with a cable?
 - Rectangular cross-section and constant *J*
- First "rough" approximation
 - Sector dipole
- Better ones

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• More **layers** and **wedges** to reduce *J* towards 90°

• Now, I can use the multipolar expansion to **optimize** my "practical" **cross-section**



Magnetic design

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A "good" field quality dipole Sector dipole

- We compute the central field given by a **sector dipole** with uniform current density *j*
- We start from **Biot-Savart law** and integrate

 $I \rightarrow j\rho d\rho d\theta$

And we obtain

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$$B_1 = -2\frac{j\mu_0}{2\pi} \int_{-\alpha}^{\alpha} \int_{r}^{r+w} \frac{\cos\theta}{\rho} \rho d\rho d\theta = -\frac{2j\mu_0}{\pi} w\sin\alpha$$

$$B_n = -\frac{j\mu_0 R_{ref}^{n-1}}{\pi} \frac{2\sin(\alpha n)}{n} \frac{(r+w)^{2-n} - r^{2-n}}{2-n}$$

Multipoles *n* are proportional to sin (*n* angle of the sector)
They can be made equal to zero !

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A "good" field quality dipole Sector dipole

• First allowed multipole *B*₃ (sextupole)

$$B_{3} = \frac{\mu_{0} j R_{ref}^{2}}{\pi} \frac{\sin(3\alpha)}{3} \left(\frac{1}{r} - \frac{1}{r+w}\right)$$

for $\alpha = \pi/3$ (i.e. a 60° sector coil) one has $B_3 = 0$

• Second allowed multipole *B*₅ (decapole)

$$B_{5} = \frac{\mu_{0} j R_{ref}^{4}}{\pi} \frac{\sin(5\alpha)}{5} \left(\frac{1}{r^{3}} - \frac{1}{(r+w)^{3}} \right)$$

for $\alpha = \pi/5$ (i.e. a 36° sector coil) or for $\alpha = 2\pi/5$ (i.e. a 72° sector coil) one has $B_5=0$

• With one sector one cannot set to zero both multipoles ... let us try with more sectors !

A "good" field quality dipole Sector dipole

• Coil with **two sectors**

$$B_{3} = \frac{\mu_{0} j R_{ref}^{2}}{\pi} \frac{\sin 3\alpha_{3} - \sin 3\alpha_{2} + \sin 3\alpha_{1}}{3} \left(\frac{1}{r} - \frac{1}{r+w}\right)$$
$$B_{5} = \frac{\mu_{0} j R_{ref}^{4}}{\pi} \frac{\sin 5\alpha_{3} - \sin 5\alpha_{2} + \sin 5\alpha_{1}}{5} \left(\frac{1}{r^{3}} - \frac{1}{(r+w)^{3}}\right)$$

- Note: we have to work with **non-normalized multipoles**, which can be added together
- Equations to set to zero B_3 , B_5 and B_5

$$\begin{cases} \sin(3\alpha_3) - \sin(3\alpha_2) + \sin(3\alpha_1) = 0\\ \sin(5\alpha_3) - \sin(5\alpha_2) + \sin(5\alpha_1) = 0 \end{cases}$$

• There is a **one-parameter family of solutions**, for instance (48°,60°,72°) or (36°,44°,64°) are solutions

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A "good" field quality dipole Sector dipole

- With one wedge one can set to zero three multipoles $(B_3, B_5 \text{ and } B_7)$
- What about two wedges ?

 $\sin(3\alpha_5) - \sin(3\alpha_4) + \sin(3\alpha_3) - \sin(3\alpha_2) + \sin(3\alpha_1) = 0$

 $\sin(5\alpha_5) - \sin(5\alpha_4) + \sin(5\alpha_3) - \sin(5\alpha_2) + \sin(5\alpha_1) = 0$

 $\sin(7\alpha_5) - \sin(7\alpha_4) + \sin(7\alpha_3) - \sin(7\alpha_2) + \sin(7\alpha_1) = 0$

 $\sin(9\alpha_5) - \sin(9\alpha_4) + \sin(9\alpha_3) - \sin(9\alpha_2) + \sin(9\alpha_1) = 0$

 $\sin(11\alpha_{5}) - \sin(11\alpha_{4}) + \sin(11\alpha_{3}) - \sin(11\alpha_{2}) + \sin(11\alpha_{1}) = 0$

One can **set to zero five multipoles** (*B*₃, *B*₅, *B*₇, *B*₉ and *B*₁₁) ~[0°-33.3°, 37.1°-53.1°, 63.4°-71.8°]



One wedge, b₃=b₅=b₇=0 [0°-43.2°,52.2°-67.3°]



Two wedges, b₃=b₅=b₇=b₉=b₁₁=0 [0°-33.3°,37.1°-53.1°,63.4°-71.8°]

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A "good" field quality dipole Sector dipole

- Let us see two coil lay-outs of real magnets
 - The **RHIC dipole** has **four blocks**



A "good" field quality dipole Sector dipole

- Limits due to the cable geometry
 - Finite thickness → one cannot produce sectors of any width
 - Cables cannot be key-stoned beyond a certain angle, some wedges can be used to better follow the arch
- One does not always aim at having zero multipoles
 - There are other contributions (iron, persistent currents ...)



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A "good" field quality dipole Sector quadrupole

- For a sector coil **with one layer**, the same results of the dipole case hold with the following transformation
 - Angles have to be divided by two
 - Multipole orders have to be multiplied by two
- First allowed multipole *B*₆ (dodecapole)

$$B_6 = \frac{\mu_0 j R_{ref}^5}{\pi} \frac{\sin(6\alpha)}{6} \left(\frac{1}{r^4} - \frac{1}{(r+w)^4} \right)$$

for $\alpha = \pi/6$ (i.e. a **30° sector coil**) one has *B***₆=0**





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- We recall the equations for the critical surface
 - Nb-Ti (linear approximation)

$$j_{sc,c}(B) = s(B_{c2}^* - B),$$

• with $s \sim 6.0 \times 10^8$ [A/(T m²)] and $B_{c2}^* \sim 10$ T at 4.2 K or 13 T at 1.9 K



- The current density flowing in the insulated cable is reduced by a factor *k* (filling ratio)
 - It ranges from ¹/₄ to 1/3

$$j_c(B) \equiv \kappa j_{sc,c}(B)$$
 $j_c(B) = \kappa s(B_{c2}^* - B)$



• We characterize the coil by two parameters

$$B \equiv \gamma_c j \qquad \qquad B_p \equiv \lambda B = \lambda \gamma_c j$$

- γ_c : how much field in the centre is given per unit of current density
 - For a sector dipole

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- $B_1 = -\frac{2\mu_0 j}{\pi} w \sin \alpha$ • λ : ratio between peak field and central field
 - For a sector and in general is λ = 1.05 1.15
 - hyperbolic fit: *a*~0.045

$$\lambda(w,r) \sim 1 + \frac{ar}{w}$$







 We can now compute what is the highest peak field that can be reached in the dipole

$$B_{p,ss} = \frac{\lambda \gamma_c \kappa s}{1 + \lambda \gamma_c \kappa s} B_{c2}^*$$



- The maximum current density in the superconductor
 - short sample limit

$$j_{ss} = \frac{\kappa s}{1 + \lambda \gamma_c \kappa s} B_{c2}^*$$

• And the **bore short sample field** (in the centre not on the conductor)

$$B_{ss} = \frac{\gamma_c \kappa s}{1 + \lambda \gamma_c \kappa s} B_{c2}^*$$



• Maximum bore field



- Magnets have to work at a given distance from the critical surface, i.e. they are never operated at short sample conditions
 - At short sample, any small perturbation quenches the magnet
 - One usually operates at a **fraction of the loadline: 60% to 90%**

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Maximum gradient and coil thickness Quadrupoles

We characterize the coil by two parameters

$$\gamma_c \equiv \frac{G}{j} \qquad \lambda \equiv \frac{B_p}{rG}$$

• *γ_c*: how much **gradient** is given **per unit of current density**

• For a sector quadrupole G =

$$= -\frac{2j_o\mu_0}{\pi} \left[\sin 60\right] \ln \left(1 + \frac{v}{r}\right)$$

- λ: ratio between peak
 field and gradient · r
 - A good fit, with $a_{-1} \sim 0.04$ and $a_{1} \sim 0.11$ is

$$\lambda(w,r) = a_{-1}\frac{r}{w} + 1 + a_1\frac{w}{r}$$

• reasonable values is $\lambda \sim \lambda_0 = 1.15$



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Maximum gradient and coil thickness Quadrupoles

• Therefore, the maximum field, current and gradient





Unlike dipoles, no point in making coils extremely large!

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Iron yoke

- Keep the **return magnetic flux** close to the coils, thus avoiding fringe fields
- In some cases the iron is partially or totally contributing to the mechanical structure
- Considerably **enhance the field** for a given current density
 - The increase is relevant (10-30%), getting higher for thin coils
 - This allows using lower currents, easing the protection





Iron yoke

- A **rough estimate** of the **iron thickness** necessary to avoid fields outside the magnet
 - The iron cannot withstand more than 2 T
 - Shielding condition for dipoles:

$$rB \sim t_{iron}B_{sat}$$

- i.e., the iron thickness times 2 T is equal to the central field times the magnet aperture One assumes that all the field lines in the aperture go through the iron (and not for instance through the collars)
- Example: in the LHC main dipole the iron thickness is 150 mm

$$t_{iron} \sim \frac{rB}{B_{sat}} = \frac{28*9}{2} \sim 130 \text{ mm}$$

• Shielding condition for quadrupoles:



Iron yoke

- The iron yoke contribution can be estimated analytically for simple geometries
 - Circular, non-saturated iron: image currents method

 $\rho' = \frac{R_I^2}{\rho}$ $I' = \frac{\mu - 1}{I}I$

 $\mu + 1$

• Iron effect is equivalent to add to each current line a second one



- with current
- Limit of the approximation: iron is not saturated (less than 2 T)



Iron yoke

- Impact of the iron yoke on short sample field
 - Large effect (25%) on RHIC dipoles (thin coil and collars)
 - Between 4% and 10% for most of the others (both Nb-Ti and Nb₃Sn)



100

80

Iron yoke

- Similar approach can be used in quadrupoles
 - Large effect on RHIC quadrupoles (thin coil and collars)
 - Between 2% and 5% for most of the others
 - The effect is smaller than in dipoles since the contribution to *B*₂ is smaller than to *B*₁







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A review of dipole lay-outs

• Tevatron MB



П

A review of dipole lay-outs

• RHIC MB



Π

A review of dipole lay-outs

• HERA MB



Π

A review of dipole lay-outs

• SSC MB





Π

A review of dipole lay-outs

• HFDA dipole



A review of dipole lay-outs

• LHC MB



п

A review of dipole lay-outs

• FRESCA



A review of dipole lay-outs

• MSUT

Π



A review of dipole lay-outs

• D20



A review of dipole lay-outs

• HD2

П





Π

Review of quadrupole lay-outs







П

Review of quadrupole lay-outs







п

Review of quadrupole lay-outs

LEP II MQC





Π

Review of quadrupole lay-outs





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Review of quadrupole lay-outs

Tevatron MQ





Π

Review of quadrupole lay-outs





BERKELEY LAB

П

Review of quadrupole lay-outs

LHC MQM



BERKELEY LAB

Π

Review of quadrupole lay-outs

LHC MQY



BERKELEY LAB

п

Review of quadrupole lay-outs

LHC MQXB



BERKELEY LAB

Review of quadrupole lay-outs



П





Review of quadrupole lay-outs

LHC MQ

п





п

Review of quadrupole lay-outs

LHC MQXA





П

Review of quadrupole lay-outs







П

Review of quadrupole lay-outs









Field representation Harmonics

Important property: starting by the multipolar expansion of a current line (Biot-Savart law)

$$B(z) = B_{y}(z) + iB_{x}(z)$$
$$B(z) = \frac{I\mu_{0}}{2\pi(z - z_{0})} = -\frac{I\mu_{0}}{2\pi z_{0}} \frac{1}{1 - \frac{z}{z_{0}}}$$

$$\begin{array}{c|c} y \\ z_0 = x_0 + iy_0 \\ \vdots \\ B = B_y + iB_x \\ \vdots \\ z = x + iy \end{array}$$

$$B(z) = -\frac{I\mu_0}{2\pi z_0} \sum_{n=1}^{\infty} \left(\frac{z}{z_0}\right)^{n-1} = -\frac{I\mu_0}{2\pi z_0} \sum_{n=1}^{\infty} \left(\frac{R_{ref}}{z_0}\right)^{n-1} \left(\frac{x+iy}{R_{ref}}\right)^{n-1}$$

 Z_0

$$B_{y} + iB_{x} = 10^{-4} B_{1} \sum_{n=1}^{\infty} (b_{n} + ia_{n}) \left(\frac{x + iy}{R_{ref}}\right)^{n-1} \qquad b_{n} + ia_{n} = -\frac{I\mu_{0} 10^{4}}{2\pi z_{0} B_{1}} \left(\frac{R_{ref}}{z_{0}}\right)^{n-1}$$

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A "good" field quality dipole Sector quadrupole

- Let's look at the quadrupoles
- First allowed multipole *B*₆ (dodecapole)

$$B_6 = \frac{\mu_0 j R_{ref}^5}{\pi} \frac{\sin(6\alpha)}{6} \left(\frac{1}{r^4} - \frac{1}{(r+w)^4} \right)$$

for $\alpha = \pi/6$ (i.e. a **30° sector coil**) one has *B***₆=0**

• Second allowed multipole *B*₁₀

$$B_{10} = \frac{\mu_0 j R_{ref}^8}{\pi} \frac{\sin(10\alpha)}{10} \left(\frac{1}{r^8} - \frac{1}{(r+w)^8}\right)$$

for $\alpha = \pi/10$ (i.e. a **18° sector coil**) or for $\alpha = \pi/5$ (i.e. a **36° sector coil**) one has **B**₁₀**=0**

• The conditions look similar to the dipole case ...

