Quantum Fields as sensors for fundamental physics

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NOIT

Thanks to people in my group that contributed

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http://rqinottingham.weebly.com/

Motivation



Atom interferometer



Single particle detector, local

Interferometry in the spatial domain: limited by time of flight Compatible with Newtonian physics

Phononic detector



- Uses interactions: collective excitations, entanglement between atoms
- Interferometry in the frequency (time) domain, non-local
- We use parametric amplification produced by the nonlinearity introduced by atomic collisions
- Compatible with General Relativity

Advantages of using phonons



- Can be miniaturized
- High sensitivity
- High resilience to noise

Applications in GR

- Gravitational waves
- Dark energy
- Proper acceleration
- Local gravitational fields
 (gravimetry)
- Gravitational gradients (gradiometry)
- Curvature
- Spacetime parameters
- Dark Matter!



Different principle

Interferometer arm length L

Resonance

 $\frac{\Delta L}{L}$



Weber bar



T∼ 4 K

Quantum Weber Bar

Temperature

Weber bar

T~ 4 K

BEC

 $T \sim 5 \times 10^{-10} \text{K}$

Initial quantum states Squeezing Parametric amplification

How can it work if its so small?

 $\omega \sim \frac{C_s}{L} \qquad \qquad \omega \sim \frac{C}{L}$

Speed of sound: $C_s = 10 \text{ mm/s}$ $L = 10^{-1} \cdot 10^{-3} \text{ mm}$ Speed of light: $C = 2.99 \times 10^{11}$ mm/s L = 2.99Km-2990Km

QFT description of a BEC



Bose Einstein Condensate in a box



mean field (ground state)

$$\widehat{\Phi} = \phi(1 + \widehat{\psi})$$

phonons density fluctuations due to interactions

quasi-uniform density

$$ho = \phi^{\dagger} \phi$$

Gaunt et. al. PRL 110 200406 (2013)

BEC in spacetime

A covariant formalism is available Phonons are a relativistic quantum field



Quantum field theory basics

determinant of the metric field equation: Klein Gordon $\Box \Phi = 0$ $\Box = (\sqrt{-g})^{-1} \partial_{\mu} \sqrt{-g} g^{\mu\nu} \partial_{\nu}$ solutions metric $\Phi = \sum \left[\phi_n a_n + ext{h.c.}
ight]$ creation and annihilation operators

Cavity at rest

Minkowski coordinates (t, x)

 $\Box \phi(t,x) = 0 \quad \text{ field equation}$

solutions: plane waves+ boundary

$$u_k(x,t) = \frac{1}{\sqrt{k\pi}} \sin\left[\frac{k\pi}{L}(x-x_A)\right] e^{-i\omega_k t},$$
$$\omega_k = \frac{1}{L}\sqrt{(k\pi)^2 + m^2},$$

creation and annihilation operators

$$\hat{\phi}(\mathbf{x}, \mathbf{t}) = \sum_{n} (u_n(t, x)\hat{a}_n + u_n^*(t, x)\hat{a}_n^{\dagger})$$



BEC in flat spacetime



$$\mathfrak{g}_{ab} = \left(\frac{n_0^2 c_s^{-1}}{\rho_0 + p_0}\right) \begin{pmatrix} -c_s^2 & 0 & 0 & 0\\ 0 & 1 & 0 & 0\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1 \end{pmatrix}$$

Minkowski space but with speed of sound

$$\tau = (c/c_s)t \implies ds^2 = -cdt^2 + dx^2$$

phonons in a cavity-type 1-dimensional trap

 $\omega_n = \frac{n \, \pi \, c_s}{L} \quad \text{spectrum}$

$$\phi_n = \frac{1}{\sqrt{n\,\pi}} \sin\frac{n\pi(x-x_L)}{L} \, e^{-i\,\omega_n\,t}$$

Solutions to the K-G equation

Gravitational wave spacetime



$$\mathfrak{g}_{ab} = \left(\frac{n_0^2 c_s^{-1}}{\rho_0 + p_0}\right) \begin{pmatrix} -c_s^2 & 0 & 0 & 0\\ 0 & 1 + h_+(t) & h_\times(t) & 0\\ 0 & h_\times(t) & 1 - h_+(t) & 0\\ 0 & 0 & 0 & 1 \end{pmatrix}$$

In a one-dimensional trap

$$ds^{2} = -c_{s}^{2} dt^{2} + (1 + h_{+}(t)) dx^{2}.$$

$$h_{+}(t) = \epsilon \sin \Omega t$$

 $\omega_n = \frac{n \pi c_s}{L}$ Resonance!

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$$

$$h_{\mu\nu} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & h_{+}(t) & h_{\times}(t) & 0 \\ 0 & h_{\times}(t) & -h_{+}(t) & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

Field transformations



Bruschi, Fuentes & Louko PRD (R) 2011

Bogoliubov transformations

$$\tilde{a}_m = \sum_n \left(\alpha_{mn}^* a_n - \beta_{mn}^* a_n^\dagger \right)$$
$$\alpha_{mn} = \left(\tilde{\phi}_m, \phi_n \right) \text{ and } \beta_{mn} = -\left(\tilde{\phi}_n, \phi_m^* \right)$$



$$\alpha = \alpha^{(0)} + \alpha^{(1)} + \alpha^{(2)} + O(h^3),$$

$$\beta = \beta^{(1)} + \beta^{(2)} + O(h^3),$$

computable transformations

Phonon creation by gravitational waves



Sabin, Bruschi, Ahmadi, and Fuentes, NJP 2014

Probe state: Two-mode squeezed state

$$\boldsymbol{\sigma} = \begin{pmatrix} \cosh 2r \ \mathbf{1} & \sinh 2r \ \mathbf{R}_{\theta} \\ \sinh 2r \ \mathbf{R}_{\theta} & \cosh 2r \ \mathbf{1} \end{pmatrix},$$

$$\mathbf{1} := \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix},$$
$$\mathbf{R}_{\boldsymbol{\theta}} := \begin{pmatrix} \cos \theta & \sin \theta \\ \sin \theta & -\cos \theta \end{pmatrix}.$$

Bogoliubov coeficients

$$egin{aligned} eta_{jk}(t) &= -rac{\epsilon}{2}\sqrt{rac{n}{m}}\,\omega_m\,t\,[-x_L+(-1)^{m+n}(L+x_L)]\delta_{jm}\,\delta_{kn}+\mathcal{O}(\epsilon^2)\ lpha_{jk}(t) &= 0+\mathcal{O}(\epsilon^2), \end{aligned}$$



 $\langle \psi_{\epsilon} | \psi_{\epsilon+d\epsilon} \rangle \ll 1$

Exploit quantum properties of the probe state to estimate with high precision parameters in the theory (Hamiltonian)

Quantum Metrology



Application: GW detector



gravitational wave detector

Quantum Fisher information



$$Mt^2 = N_d N_r t^2 = N_d \tau t$$

$$egin{aligned} H &= rac{1}{4} \omega_m \omega_n t^2 [1 + \sin^2(heta - \phi_eta) \sinh^2 2r] \ &= rac{1}{4} \omega_m \omega_n t^2 [1 + \sinh^2 2r] \,\, when \,\, heta = \phi_eta + rac{\pi}{2} \ & o_{r \gg 1} \,\, rac{1}{4} \omega_m \omega_n t^2 N_P^2, \end{aligned}$$

$$\Delta \epsilon \geq \frac{2}{\sqrt{M\omega_m \omega_n t^2 N_p^2}}$$

- N_p Number of phonons
- N_d Number of detectors
- M Number of measurements
- t phonon lifetime
- au integration time

 $\omega_m = (\pi m c_s / L)$

Measurement: Active interferometry with active channels

Details now in: Howl and Fuentes, arXiv:1902.09883



Based on Pumped-up SU(1,1) interferometer by Szigeti et al. PRL 2017

For persistent sources (pulsars)

Sensitivities

We get sensitivities between $10^{-19}-10^{-23}$ For frequencies $\Omega \sim \text{KHz}$ Considering with $N_o \sim 10^8 - 10^{10}$ and number of phonons $N_p \sim 10^3 - 10^8$ Phonon lifetime ~ 0.1 -15sec

Many more details on specific species coming soon!

Large atom number Bose-Einstein condensate of sodium

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We describe the setup to create a large Bose-Einstein condensate containing more than 120×10^6 atoms. In the experiment a thermal beam is slowed by a Zeeman slower and captured in a dark-spot magneto-optical trap (MOT). A typical dark-spot MOT in our experiments contains 2.0×10^{10} atoms with a temperature of 320 μ K and a density of about 1.0×10^{11} atoms/cm³. The sample is spin polarized in a high magnetic field before the atoms are loaded in the magnetic trap. Spin polarizing in a high magnetic field results in an increase in the transfer efficiency by a factor of 2 compared to experiments without spin polarizing. In the magnetic trap the cloud is cooled to degeneracy in 50 s by evaporative cooling. To suppress the three-body losses at the end of the evaporation, the magnetic trap is decompressed in the axial direction. © 2007 American Institute of Physics. [DOI: 10.1063/1.2424439]

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Squeezing in Bose–Einstein condensates with large numbers of atoms

$$\frac{N_{\mathbf{k}\neq0}^{\mathrm{1D}}(t_3)}{N} \approx \sqrt{L} \frac{1}{N} \sqrt{\frac{M U_{aa}^{\mathrm{1D}} n_a}{2\hbar^2 \pi^2}} \Lambda_a^{3/2} \cos^2 \theta f^{\mathrm{1D}}(\Lambda_a) \quad \propto \sqrt{L},$$

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View the article online for updates and enhancements.





Figure 8. Spectrum of gravitational wave sources [18, 22]. In this figure, the abbreviations are: BH, collapse to black hole; NS/NS, neutron star coalescence; NS evol, secular evolution of a nonaxisymmetric neutron star.

Ultra-Light Dark Matter (bosonic)



search for *coherent effects of the entire field*, not single hard particle scatterings

Select an area to comment on

Generic Candidates: Light pseudo-Nambu-Goldstones (axions and "axion like particles" — ALPs); Massive hidden vector bosons (aka "dark photons"); Light scalars (moduli/dilatons...)

Slide by John March-Russel





As an example of the quantities involved we show the following tables for a single sodium condensate $(N_d = 1)$ with $N_0 = 10^8$ atoms and integration time $\tau = 1$ year. Table 1 is for the detection of gravitational waves of 3kHz, and Table 2 for 100kHz. Sensitivities can be calculated using equations (3) and (4).

N_p	j	k	L	а	t	$\omega_1 = c_s/L$	<i>cs</i> (m/s)	θ	C_{nm}	sens
10 ³	5	1	6.03×10^{-4}	6.82×10^{-12}	9.9	1.61×10^{2}	9.73×10^{-2}	3.06×10^{-1}	7.16×10^{-7}	4.89×10^{-20}
10 ⁴	3	1	4.82×10^{-4}	4.87×10^{-12}	10	2.39×10^2	1.51×10^{-1}	2.83×10^{-1}	3.65×10^{-7}	6.41×10^{-21}
10 ⁵	33	31	2.221×10^{-3}	5.27×10^{-11}	10	1.51×10^{-1}	3.5×10^{-2}	3.04×10^{-1}	2.84×10^{-7}	1.25×10^{-21}
3.87×10^{5}	3	1	4.81×10^{-4}	5.16×10^{-12}	10	2.32×10^2	1.21×10^{-1}	2.96×10^{-1}	3.59×10^{-7}	1.13×10^{-21}

Table 1

Table 2

N_p	j	k	L	а	t	$\omega_1 = c_s/L$	<i>c_s</i> (m/s)	θ	C_{nm}	sens
10 ³	3	1	6.51×10^{-5}	2.42×10^{-13}	9.9	7.93×10^{3}	5.17×10^{-1}	7.65×10^{-2}	1.36×10^{-5}	6.09×10^{-21}
10 ⁴	3	1	6.63×10^{-5}	2.67×10^{-13}	7.5	7.95×10^{3}	5.28×10^{-1}	3.1×10^{-1}	7.87×10^{-7}	5.11×10^{-22}
5.62×10^{4}	3	1	6.45×10^{-5}	2.38×10^{-13}	10	8.06×10^{3}	5.2×10^{-1}	2.93×10^{-1}	9.28×10^{-7}	2.08×10^{-22}
10 ⁶	3	1	6.5×10^{-5}	2.41×10^{-13}	10	7.96 ⁻³	5.17×10^{-1}	2.91×10^{-1}	9.46×10^{-7}	4.91×10^{-23}

Screened scalar fields



$$A\left(\varphi\right) =: \exp\left[a^2\left(\varphi\right)
ight]$$

$$a^2 \ll 1$$

$$ilde{g}_{\mu
u}=\left(1+a^2+\mathcal{O}\left(a^4
ight)
ight)g_{\mu
u}$$
 .

$$a^2 = \frac{\varphi}{M_c}$$

Chameleon fields Fifth force fields

$$\tilde{g}_{\mu
u} = A\left(arphi
ight)g_{\mu
u}$$

They produces the effects of dark energy in deep space, but also gets inhibited by the presence of mass. In this way you get cosmic expansion between galaxies, but you don't see its effect in galaxies (or in our solar system).



Constraining dark energy



Constraints for the parameter space of the chameleon model n = 1. The brown area corresponds to constraints from atom interferometry and the green area to those from E ot-Wash experiments. The dotted line indicates the DE scale $\Lambda = 2.4$ meV. New constraints predicted in this work are coloured in blue, where dark blue corresponds to 1 run of the experiment

Constraining dark energy models





Constraints for the value of Mc for positive n chameleon models at $\Lambda = 2.4$ meV.

Constraints for the parameter space of the symmetron model. Different shades of blue correspond to $\mu = 10^{-4}$, $10^{-4.5}$, 10^{-5} and $10^{-5.5}$ eV in natural units respectively.

Schwarzchild spacetime (Earth)

$$oldsymbol{g} = ext{diag}\left(-f(r), rac{1}{f(r)}, r^2, r^2 \sin^2 artheta
ight)$$

 $f(r)\,=\,1-r_S/r$

Setup	Running time	Length	$\Delta r_S/r_S$
[14, 15, 17] Atom. Int.	$100\mathrm{s}-8\mathrm{h}$	$0.2-2.5\mathrm{m}$	10^{-9}
[16] BEC-chip	$100\mathrm{s}$	$10^{-2} { m m}$	10^{-10}
Phononic MZI	6 s	$10^{-4} { m m}$	10^{-8}



g

Phononic gravimeter:

Relative error bound of 10⁻¹¹ in 1 yr. Commercial gravimeters reach 10⁻⁹ in 15 days with a device that measure 100x50x70cm³.

Phononic gradiometer:

Improves the state of the art by two orders of magnitude



We need instruments that operate at scales where both quantum and relativistic effects co-exist.



Bogoliubov transformations



Bogoliubov transformation

- Realizes a linear transformation of the modes: $\tilde{a}_m = \sum_n (\alpha_{mn} a_n + \beta_{mn}^* a_n^{\dagger})$
- Alphas: passive terms (beam-splitter like)
- Betas: active terms (two-mode squeezers)



covariance matrix formalism

covariance matrix: information about the state

$$\sigma_{ij} = \langle \mathbf{X}_i \mathbf{X}_j + \mathbf{X}_j \mathbf{X}_i \rangle - 2 \langle \mathbf{X}_i \rangle \langle \mathbf{X}_j \rangle \qquad [X_i, X_j] = 2i\Omega_{ij}$$
$$\mathbf{X}_{(2n-1)} = \frac{1}{\sqrt{2}}(a_n + a_n^{\dagger}) \text{ and } \mathbf{X}_{(2n)} = \frac{-i}{\sqrt{2}}(a_n - a_n^{\dagger})$$

symplectic matrix: evolution

$$\begin{split} \tilde{\sigma} &= S\,\sigma\,S^T \\ S\,\Omega\,S^T &= \Omega \end{split}$$

Computations are much simpler

QFT in the symplectic formalism

Friis and Fuentes JMO (invited) 2012





General framework for RQM

Ahmadi, Bruschi, Sabin, Adesso, Fuentes, Nature Sci. Rep. 2014 Ahmadi, Bruschi, Fuentes PRD 2014

Fisher information in QFT: Analytical formulas in terms of general Bogoliubov coefficients



Probe states: Single-mode Two-mode channels

for small parameters

$$H = \epsilon^{-2} \Re \bigg[4 \cosh r (f_{\alpha}^{n} + f_{\beta}^{n} + f_{\alpha}^{m} + f_{\beta}^{m}) + 4 \cosh^{2} r (2|\beta_{nm}(t)|^{2} - f_{\alpha}^{n} + f_{\beta}^{n} - f_{\alpha}^{m} + f_{\beta}^{m}) - 4 \sinh^{2} r (-f_{\alpha}^{n} + f_{\beta}^{n} - f_{\alpha}^{m} + f_{\beta}^{m} + 2\beta_{nm}(t)^{2} - 2\alpha_{nm}(t)^{2} + 4 \sinh r \Re [\mathcal{G}_{nm}^{\alpha\beta} + \mathcal{G}_{nm}^{\alpha\beta}] - 4 \cosh^{4} r |\beta_{nm}(t)|^{2} - \frac{1}{2} \sinh^{2} 2r (2|\alpha_{nm}(t)|^{2} - 3|\beta_{nm}(t)|^{2} - \beta_{nm}(t)^{2} \bigg].$$

$$f_{\alpha}^{i} = \frac{1}{2} \sum_{n \neq k, k'} |\alpha_{ni}|^{2}$$
$$f_{\beta}^{i} = \frac{1}{2} \sum_{n \neq k, k'} |\beta_{ni}|^{2}$$
$$\mathcal{G}_{ij}^{\alpha\beta} = \sum_{n \neq k, k'} \alpha_{ni} \beta_{nj}^{*}$$

Resilience to noise

Sabin, Kohlrus, Bruschi and Fuentes, EPJ Quantum Technology 2016



FIG. 2: Optimal bound for the strain sensitivity as provided by the QFI for $n=1,\ m=2$, T=0 (blue, solid), T=150 nK (red,dashed) and a) $r=10,\ \omega_1=5\,10^3$ Hz, b) $r=10,\ \omega_1=5\,10^2$ Hz, c) $r=2,\ \omega_1=5\,10^3$ Hz.

$$\omega_n = \frac{n \pi}{L}$$

 c_s

Resonance

Many detectors



• We find that decoherence is of the order of a few seconds for KHz phonons

 In one dimension these processes are supressed

Howl, Sabin, Hackermüler and Fuentes, Journal of Phys B (2018)

Phonon interaction: decoherence

Non-interacting gas of quasi-particles finite lifetime, no decoherence

$$\hat{H} \approx \hat{H}_0 + \frac{g}{2} \Big(N_0 f(two \ \hat{a}_{\boldsymbol{p}}^{\dagger}, \hat{a}_{\boldsymbol{p}}) + \sqrt{N_0} f(three \ a_{\boldsymbol{p}}^{\dagger}, \hat{a}_{\boldsymbol{p}}) + f(four \ \hat{a}_{\boldsymbol{p}}^{\dagger}, a_{\boldsymbol{p}}) \Big)$$

- Interactions, decoherence
- ▶ 1. Landau: $\hat{b}_{\boldsymbol{q}}\hat{b}_{\boldsymbol{p}}\hat{b}_{\boldsymbol{p}'}^{\dagger}$
 - Requires thermal quasi-particles
- > 2. Beliaev: $\hat{b}_{\boldsymbol{q}}\hat{b}_{\boldsymbol{p}}^{\dagger}\hat{b}_{\boldsymbol{p}'}^{\dagger}$
 - ► Also present at T=0.



Sensitivities

BEC	N_0	N_P	L (nm)	$R \pmod{(\mathrm{mm})}$	t (s)	k	j	N_d	Ω (kHz)	$\Delta\epsilon$
$^{1}\mathrm{H}$	10 ¹⁰	10 ³	1	0.01	15	3	1	10	3.9	2.68×10^{-21}
$^{1}\mathrm{H}$	10 ¹⁰	10^{8}	1	0.01	15	3	1	10^{3}	3.9	8.48×10^{-25}
87 Rb	10^{10}	10^{3}	1	0.1	0.22	100	98	10	2.1	${}^{6.81 imes}_{10^{-20}}$
87 Rb	10 ¹⁰	10 ⁸	1	0.1	0.22	100	98	10 ³	2.1	2.15×10^{-23}





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Broadband: 3D

Spherical BEC





We are studying different geometries

Energy transference

Efficient thermal machine Bruschi & Fuentes arXiv: 1607.01291

Work in progress

Noise studies:

Seismic noise Trap inestabilities Decoherence in 1-d

A protocol to extract energy

Here we briefly illustrate the protocol that we employ to extract energy from a cavity that is affected by motion or gravity. This protocol has been extensively studied in literature [31].

i) Cavities R and H are identical and at the same temperature. Cavity modes are excited.ii) Motion or gravity affect cavity H, Its field, at the end, is left in a slightly excited state.



iii) The highlighted mode of choice of cavities R, H and battery B (as an example, mode n = 1) interacts through the interaction Hamiltonian H_I .





This three-dimensional projection of the Milky Way galaxy onto a transparent globe shows the probable locations of the three confirmed black-hole merger events observed by the two LIGO detectors—GW150914 (dark green), GW151226 (blue), GW170104 (magenta)—and a fourth confirmed detection (GW170814, light green, lower-left) that was observed by Virgo and the LIGO detectors. Also shown (in orange) is the lower significance event, LVT151012. Image credit: LIGO/Virgo/Caltech/MIT/Leo Singer (Milky Way image: Axel Mellinger).



Fig. 5. The estimated strength of gravitational waves from the dynamical barmode instability and the CFS instability of the f- and r-modes. The estimates are compared to the predicted noise of the various interferometers and also the possible noise curve for a dual cylinder detector.