

# A Realistic U(2) Model of Flavor

**Robert Ziegler (KIT)**

**mainly based on arXiv: 1805.07341 with M. Linster &  
work in progress with M. Linster & J. Lopez-Pavon**

**arXiv:1308.1090 with E. Dudas, G. v.Gersdorff, S. Pokorski } SUSY**  
**arXiv:1509.01249 with A. Falkowski, M. Nardecchia } B-anomalies**  
**arXiv:1904.04121 with R. Barbieri }**

# Outline

## Realistic extension of U(2) models by Barbieri & al.

(viable CKM, neutrinos included, no SUSY)

R. Barbieri, G. Dvali, L. Hall '96  
R. Barbieri, L. Hall, A. Romanino '97....

$$m_{\{u,d,e,\nu\}} \sim \begin{pmatrix} 0 & \varepsilon^2 & 0 \\ \varepsilon^2 & \varepsilon^2 & \{\varepsilon, \varepsilon^2, \varepsilon, \varepsilon^2\} \\ 0 & \{\varepsilon, \varepsilon, \varepsilon^2, \varepsilon^2\} & \{1, \varepsilon, \varepsilon, \varepsilon^2\} \end{pmatrix}$$

$$\epsilon \sim V_{cb}$$



# The SM Flavor Puzzle

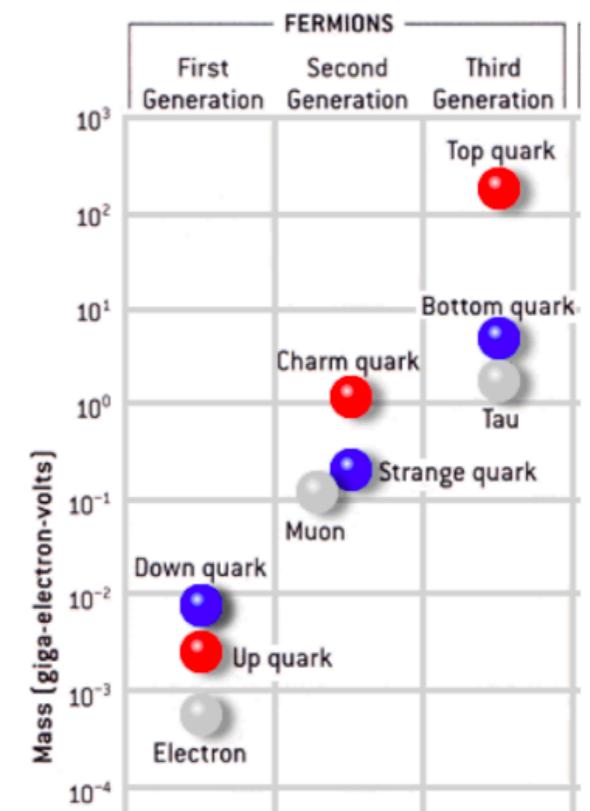
**Explain large hierarchies in fermion masses and mixings**

**CKM**

$$|V| = \begin{bmatrix} u & d & s \\ c & s & b \\ t & b & d \end{bmatrix}$$

**PMNS**

$$|U| = \begin{bmatrix} e & 1 & 2 & 3 \\ \mu & 1 & 2 & 3 \\ \tau & 2 & 3 & 1 \end{bmatrix}$$



Here: Approximate Flavor Symmetries

# Flavor Symmetries

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SM fields charged under flavor symmetry group G,  
spontaneously broken by VEVs of “**flavon**” fields  $\Phi_A$

Effective Yukawa Lagrangian requires flavon insertions  
in order to be invariant under G

$$\mathcal{L}_{\text{yuk}} = \lambda_{ij} \left( \frac{\Phi_A}{\Lambda_F} \right)^{x_{ij}^A} \bar{q}_i u_j h$$

from G selection rules

“O(1)” coefficients

UV scale

The diagram shows the effective Yukawa Lagrangian  $\mathcal{L}_{\text{yuk}}$  as a product of a coupling coefficient  $\lambda_{ij}$ , a ratio involving a flavon field  $\Phi_A$  and a UV scale  $\Lambda_F$ , and fermion fields  $\bar{q}_i u_j h$ . Three arrows point to specific parts of the equation with labels: a blue arrow points to  $\lambda_{ij}$  with the label “O(1)” coefficients; an orange arrow points to  $x_{ij}^A$  with the label from G selection rules; and a green arrow points to  $\Lambda_F$  with the label UV scale.

Yukawas given by powers of small parameters  $\epsilon_A = \langle \Phi_A \rangle / \Lambda_F$

# Prototype Example: U(1)

Froggatt, Nielsen '79

	$\Phi$	$\bar{q}_i$	$u_i$	$h$
$U(1)_F$	-1	$q_i$	$u_i$	0



$y_{ij}^u = \lambda_{ij}^u \epsilon^{q_i + u_j}$

(same as in Partial Compositeness)

Can easily reproduce all Yukawa hierarchies, e.g.

$$q_i = (3, 2, 0)$$

$$u_i = (4, 2, 0)$$

$$y_u \sim \begin{pmatrix} \epsilon^{3+4} & \epsilon^{3+2} & \epsilon^{3+0} \\ \epsilon^{2+4} & \epsilon^{2+2} & \epsilon^{2+0} \\ \epsilon^{0+4} & \epsilon^{0+2} & \epsilon^{0+0} \end{pmatrix}$$

Diagonalized by  $V_{ij} \sim \epsilon^{|f_i - f_j|}$  

$V_{us} \sim \epsilon^{|q_1 - q_2|} \sim \epsilon$   
not so small order parameter:  
charge assignment not unique

2 charge diff's for 3 CKM angles: postdict  $V_{ub} \sim V_{us} V_{cb}$

# A U(2) Model of Flavor

$$U(2)_F \equiv SU(2)_F \times U(1)_F$$

## SM quantum numbers

- compatible with SU(5) GUT  
 $\mathbf{10} = Q, U, E \quad \overline{\mathbf{5}} = L, E$
- generations transform as **2+1**  
 $\mathbf{10}_i = \mathbf{10}_a + \overline{\mathbf{10}}_3$
- need to specify 4 U(1)<sub>F</sub> charges  
 $X_{\mathbf{10}_3} = 0 \quad X_{\mathbf{10}_a} = X_{\overline{\mathbf{5}}_a} = X_{\overline{\mathbf{5}}_3} = 1$

## U(2) breaking

- 2 flavons in **2+1** with charge -1  
 $\phi = \mathbf{2}_{-1} \quad \chi = \mathbf{1}_{-1}$
  - VEVs slightly below cutoff  $\Lambda$   
 $\langle \phi \rangle = \begin{pmatrix} \varepsilon_\phi \Lambda \\ 0 \end{pmatrix} \quad \langle \chi \rangle = \varepsilon_\chi \Lambda$
- $\epsilon_\phi \sim 0.03 \quad \epsilon_\chi \sim 0.01$

	$\mathbf{10}_a$	$\overline{\mathbf{5}}_a$	$\mathbf{10}_3$	$\overline{\mathbf{5}}_3$	$H$	$\phi_a$	$\chi$
$SU(2)_F$	<b>2</b>	<b>2</b>	1	1	1	<b>2</b>	1
$U(1)_F$	1	1	0	1	0	-1	-1

Linster, RZ '18  
[old models: SO(10)]

# Up-Quark Sector

Invariant Yukawa Lagrangian needs Flavon insertions

$$\begin{aligned}\mathcal{L}_u = & \frac{\lambda_{11}^u}{\Lambda^6} \chi^4 (\phi_a^* Q_a) (\phi_b^* U_b) H + \frac{\lambda_{12}^u}{\Lambda^2} \chi^2 \epsilon_{ab} Q_a U_b H + \frac{\lambda_{13}^u}{\Lambda^3} \chi^2 (\phi_a^* Q_a) U_3 H \\ & + \frac{\lambda_{22}^u}{\Lambda^2} (\epsilon_{ab} \phi_a Q_b) (\epsilon_{cd} \phi_c U_d) H + \frac{\lambda_{23}^u}{\Lambda} (\epsilon_{ab} \phi_a Q_b) U_3 H + \frac{\lambda_{31}^u}{\Lambda^3} \chi^2 Q_3 (\phi_a^* U_a) H \\ & + \frac{\lambda_{32}^u}{\Lambda} Q_3 (\epsilon_{ab} \phi_a U_b) H + \lambda_{33}^u Q_3 U_3 H ,\end{aligned}$$

Flavon vevs generate hierarchical Yukawa structure

$$Y_u \approx \begin{pmatrix} \lambda_{11}^u \varepsilon_\phi^2 \varepsilon_\chi^4 & \lambda_{12}^u \varepsilon_\chi^2 & \lambda_{13}^u \varepsilon_\phi \varepsilon_\chi^2 \\ -\lambda_{12}^u \varepsilon_\chi^2 & \lambda_{22}^u \varepsilon_\phi^2 & \lambda_{23}^u \varepsilon_\phi \\ \lambda_{31}^u \varepsilon_\phi \varepsilon_\chi^2 & \lambda_{32}^u \varepsilon_\phi & \lambda_{33}^u \end{pmatrix} \approx \begin{pmatrix} 0 & \lambda_{12}^u \varepsilon_\chi^2 & 0 \\ -\lambda_{12}^u \varepsilon_\chi^2 & \lambda_{22}^u \varepsilon_\phi^2 & \lambda_{23}^u \varepsilon_\phi \\ 0 & \lambda_{32}^u \varepsilon_\phi & \lambda_{33}^u \end{pmatrix}$$

drop sub-leading  
corrections  $\mathcal{O}(\varepsilon_\phi^2) \sim 10^{-4}$

reproduce holomorphic  
0's in SUSY models

# Quarks and Charged Leptons

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**U(1) charge of RH\_3 +1** →

$$Y_u \approx \begin{pmatrix} 0 & \lambda_{12}^u \varepsilon_\chi^2 & 0 \\ -\lambda_{12}^u \varepsilon_\chi^2 & \lambda_{22}^u \varepsilon_\phi^2 & \lambda_{23}^u \varepsilon_\phi \\ 0 & \lambda_{32}^u \varepsilon_\phi & \lambda_{33}^u \end{pmatrix}, \quad Y_d \approx \begin{pmatrix} 0 & \lambda_{12}^d \varepsilon_\chi^2 & 0 \\ -\lambda_{12}^d \varepsilon_\chi^2 & \lambda_{22}^d \varepsilon_\phi^2 & \lambda_{23}^d \varepsilon_\phi \\ 0 & \lambda_{32}^d \varepsilon_\phi & \lambda_{33}^d \varepsilon_\chi \end{pmatrix}$$

**U(1) charge of LH\_3 +1** ↓

$$Y_e \approx \begin{pmatrix} 0 & \lambda_{12}^e \varepsilon_\chi^2 & 0 \\ -\lambda_{12}^e \varepsilon_\chi^2 & \lambda_{22}^e \varepsilon_\phi^2 & \lambda_{23}^e \varepsilon_\phi \\ 0 & \lambda_{32}^e \varepsilon_\phi \varepsilon_\chi & \lambda_{33}^e \varepsilon_\chi \end{pmatrix}.$$

# SM Flavor Structure

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1-2 mixing angles **smallish**, related to light masses

$$\theta_{12} \sim \epsilon_\chi^2 / \epsilon_\phi^2 \sim \sqrt{m_1 / m_2}$$

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2-3 angles **large** for RH d-quarks and LH leptons

$$\theta_{23}^{DR} \sim \theta_{23}^{EL} \sim \epsilon_\phi / \epsilon_\chi \sim \mathcal{O}(1)$$

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$$\theta_{23}^{\text{rest}} \sim \epsilon_\phi \sim V_{cb}$$

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1-3 angles given by **1-2** and **2-3** angles

$$\theta_{13} \sim \theta_{12} \times \theta_{23}$$

# CKM Relations

Texture zeros accurately relate masses and mixing angles

The diagram shows three CKM relation equations within a box:

$$|V_{us}| \approx \left| \sqrt{\frac{m_d}{m_s}} \sqrt{c_{23}^{Rd}} - e^{i(\phi_2 - \phi_1)} \sqrt{\frac{m_u}{m_c}} \right|$$
$$|V_{td}| \approx \sqrt{\frac{m_d}{m_s}} \sqrt{c_{23}^{Rd}} \left| |V_{cb}| - e^{i\phi_2} \frac{s_{23}^{Rd}}{c_{23}^{Rd}} \frac{m_s}{m_b} \right|$$
$$|V_{ub}| \approx \left| \sqrt{\frac{m_u}{m_c}} |V_{cb}| - e^{i\phi_1} \sqrt{\frac{m_d}{m_s}} \sqrt{c_{23}^{Rd}} \frac{s_{23}^{Rd}}{c_{23}^{Rd}} \frac{m_s}{m_b} \right|$$

A blue arrow points from the text "2-3 mixing angle in RH down sector" to the first equation. A green arrow points from the text "free phases" to the third equation.

In original U(2) models  $s_{23}^{Rd} \sim V_{cb}$   $\rightarrow |V_{ub}/V_{cb}| \approx \sqrt{m_u/m_c}$

Off by more than  $3\sigma$ : need  $s_{23}^{Rd} \sim 1$

Roberts, Ross, Romanino, Velasco-Sevilla '01

# Numerical Fit

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Fit parameters  $\{\lambda_{ij}^{u,d,e}, \varepsilon_\phi, \varepsilon_\chi\}$  with SM observables

Use quality measure for “O( $I$ )-ness” of  $\lambda_{ij}^{u,d,e}$

$$\chi_{\mathcal{O}(1)}^2 = \sum_{\lambda_{ij}^p} \frac{(\log(|\lambda_{ij}^p|))^2}{2 \cdot 0.55^2} \longrightarrow \lambda_{ij}^{u,d,e} \text{ with } 95\% \text{ prob. in } [1/3, 3]$$

e.g. for single parameter  $\lambda = \{3, 5, 7, 10, 50, 100\}$

get contribution  $\Delta\chi_{\mathcal{O}(1)}^2 = \{2, 4, 6, 9, 25, 35\}$

Fit satisfactory if

$$\begin{aligned}\chi_{\mathcal{O}(1)}^2 &\leq \#\text{pars} \\ \chi^2 &\leq \#\text{obs}\end{aligned}$$

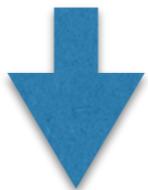
Fit	$\varepsilon_\phi$	$\varepsilon_\chi$	$\min  \lambda_{ij}^{u,d,\ell} $	$\max  \lambda_{ij}^{u,d,\ell} $	$\chi^2$	$\chi_{\mathcal{O}(1)}^2$
QL1 $_{\mathbb{R}}$	0.019	0.008	1/3.1	2.7	1.7	7.8
QL2 $_{\mathbb{R}}$	0.023	0.008	1/2.7	2.8	12	5.4

# Neutrino Sector

Majorana neutrinos don't work because leading order 1-2 entry in Weinberg operator vanishes due to SU(2) antisymmetrization

$$\epsilon_{ab} L_a L_b H H = 0$$

Can do Dirac Neutrinos with  $N_i = N_a + N_3$  &  $X_a^N = X_3^N$



$$m_\nu^D \approx v \varepsilon_\chi^{X_a^N - 1} \begin{pmatrix} 0 & \lambda_{12}^\nu \varepsilon_\chi^2 & 0 \\ -\lambda_{12}^\nu \varepsilon_\chi^2 & \lambda_{22}^\nu \varepsilon_\phi^2 & \lambda_{23}^\nu \varepsilon_\phi \varepsilon_\chi \\ 0 & \lambda_{32}^\nu \varepsilon_\phi \varepsilon_\chi & \lambda_{33}^\nu \varepsilon_\chi^2 \end{pmatrix}$$

get anarchic structure; smallness from largish U(I) charges

# Neutrino Fit & Predictions

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Good fit just for Normal Ordering

Fit	$X_a^N$	$X_3^N$	$\varepsilon_\phi$	$\varepsilon_\chi$	min $ \lambda_{ij}^{u,d,e,\nu} $	max $ \lambda_{ij}^{u,d,e,\nu} $	$\chi^2$	$\chi^2_{\mathcal{O}(1)}$
QL $\nu_D$ -1 (NO)	6	6	0.026	0.012	1/2.9	2.6	0.5	10
QL $\nu_D$ -2 (NO)	6	6	0.024	0.013	1/2.6	2.2	18	9
QL $\nu_D$ -3 (NO)	5	5	0.022	0.006	1/3.1	3.8	1.0	13
QL $\nu_D$ -4 (NO)	5	5	0.021	0.006	1/2.5	2.4	18	9

Predict overall mass scale from scanning over successful fits

Quantity	Range [meV]	Preferred values [meV]
$\sum m_i$	58 – 110	60 – 65
$m_\beta$	8 – 26	9 – 10

No chance for KATRIN

**PLANCK bound automatically satisfied!**

$$m_\beta = \sqrt{\sum_i m_i^2 |U_{ei}|^2}$$

# Majorana Neutrinos from $D_6 \times U(1)$

Consider dihedral  $D_6 = D_3 \times Z_2$  instead of  $SU(2)$

	$\mathbf{10}_a$	$\bar{\mathbf{5}}_a$	$\mathbf{10}_3$	$\bar{\mathbf{5}}_3$	$H$	$\phi_a$	$\chi$
$D_3 \times Z_2$	$\mathbf{2}_-$	$\mathbf{2}_-$	$\mathbf{1}_+$	$\mathbf{1}_+$	$\mathbf{1}_+$	$\mathbf{2}_-$	$\mathbf{1}_+$
$U(1)_F$	1	1	0	1	0	-1	-1

$$(\psi \otimes \phi)_{\mathbf{1}} = \psi_1 \phi_2 + \psi_2 \phi_1$$

$$(\psi \otimes \phi \otimes \chi)_{\mathbf{1}} = \psi_1 \phi_1 \chi_1 + \psi_2 \phi_2 \chi_2$$

**Mimics  $U(2)$  structure except for symmetric  $\mathbf{1-2}$ :  
Weinberg operator fixed from charged lepton sector**

$\begin{matrix} \mathbf{2} & \mathbf{1} \\ \mathbf{1} & \mathbf{0} \end{matrix}$

$$m_u \approx v \begin{pmatrix} 0 & \lambda_{12}^u \varepsilon_\chi^2 & 0 \\ \lambda_{12}^u \varepsilon_\chi^2 & \lambda_{22}^u \varepsilon_\phi^2 & \lambda_{23}^u \varepsilon_\phi \\ 0 & \lambda_{32}^u \varepsilon_\phi & \lambda_{33}^u \end{pmatrix},$$

$$m_d \approx v \begin{pmatrix} 0 & \lambda_{12}^d \varepsilon_\chi^2 & 0 \\ \lambda_{12}^d \varepsilon_\chi^2 & \lambda_{22}^d \varepsilon_\phi^2 & \lambda_{23}^d \varepsilon_\phi \varepsilon_\chi \\ 0 & \lambda_{32}^d \varepsilon_\phi & \lambda_{33}^d \varepsilon_\chi \end{pmatrix}$$

$\begin{matrix} \mathbf{2} & \mathbf{2} \\ \mathbf{1} & \mathbf{1} \end{matrix}$

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$$m_e \approx v \begin{pmatrix} 0 & \lambda_{12}^e \varepsilon_\chi^2 & 0 \\ \lambda_{12}^e \varepsilon_\chi^2 & \lambda_{22}^e \varepsilon_\phi^2 & \lambda_{23}^e \varepsilon_\phi \\ 0 & \lambda_{32}^e \varepsilon_\phi \varepsilon_\chi & \lambda_{33}^e \varepsilon_\chi \end{pmatrix},$$

$$m_\nu \approx \frac{v^2}{M} \begin{pmatrix} 0 & \lambda_{12}^\nu \varepsilon_\chi^2 & 0 \\ \lambda_{12}^\nu \varepsilon_\chi^2 & \lambda_{22}^\nu \varepsilon_\phi^2 & \lambda_{23}^\nu \varepsilon_\phi \varepsilon_\chi \\ 0 & \lambda_{23}^\nu \varepsilon_\phi \varepsilon_\chi & \lambda_{33}^\nu \varepsilon_\chi^2 \end{pmatrix}$$

$\begin{matrix} \mathbf{2} & \mathbf{2} \\ \mathbf{2} & \mathbf{2} \end{matrix}$

# Majorana Neutrino Fit

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**Neutrino mass matrix automatically anarchic:  
better fit with less parameters**

Fit	$\varepsilon_\phi$	$\varepsilon_\chi$	min $ \lambda_{ij}^{\text{u,d},\ell} $	max $ \lambda_{ij}^{\text{u,d},\ell} $	$\chi^2$	$\chi^2_{\mathcal{O}(1)}$	$M [10^{11} \text{ GeV}]$
QL $\nu_M$ -1	0.025	0.009	1/2.8	2.1	0.7	7.9	4.1
QL $\nu_M$ -2	0.024	0.009	1/2.6	1.9	18	6.3	3.3

Predict overall mass scale from scanning over successful fits

Quantity	Range [meV]	Preferred values [meV]
$\sum m_i$	59 – 78	60, 70
$m_\beta$	8 – 15	9 – 10, 11 – 12
$m_{\beta\beta}^{\text{max}}$	3 – 16	5, 9

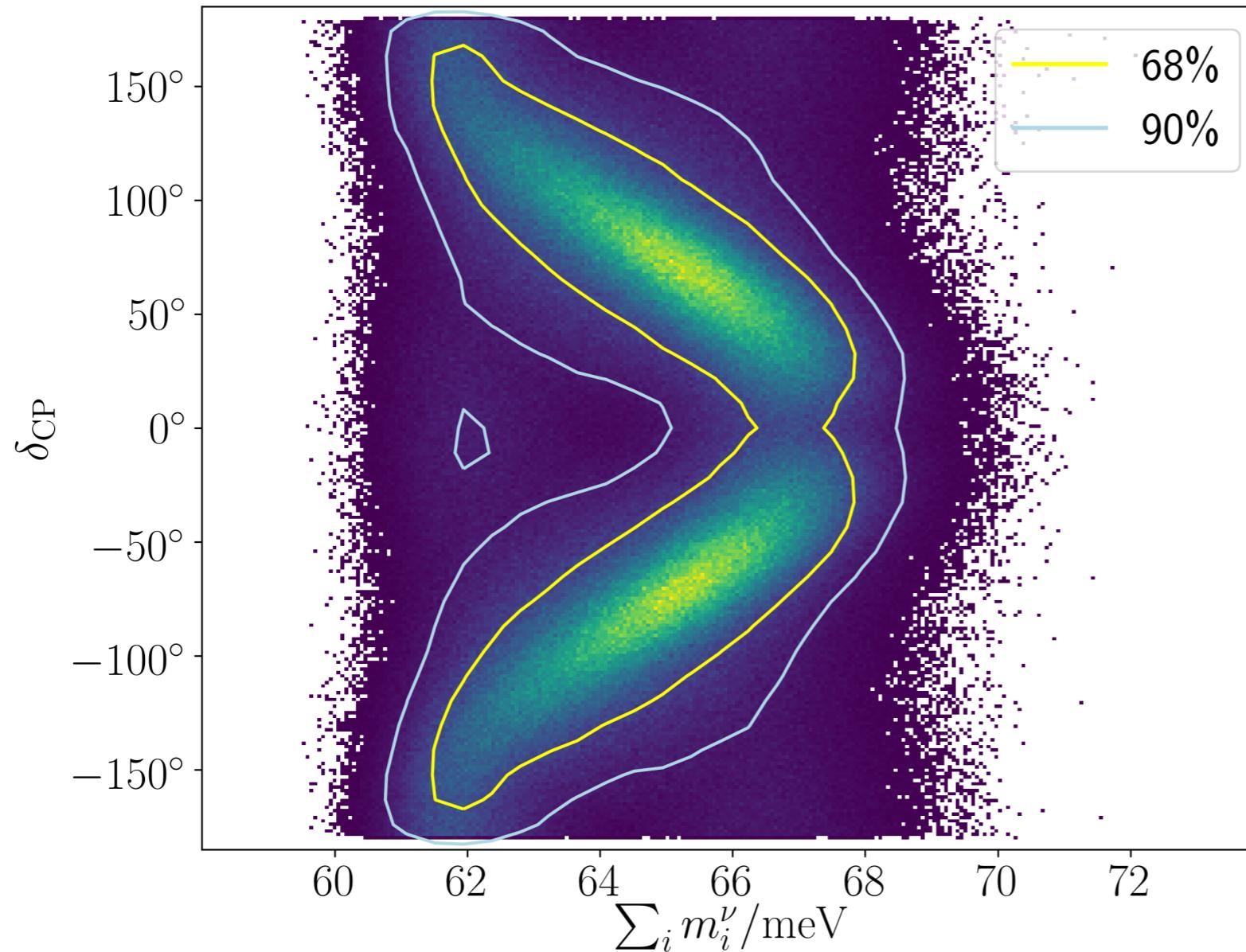
Similar to Dirac case, neutrinoless double beta decay hopeless

$$m_{\beta\beta} = |\sum U_{ei}^2 m_i|$$

# Neutrino Sector Predictions

## Correlation of Dirac phase and absolute mass scale

work in progress with J. Lopez-Pavon & M. Linster



**just using  
neutrino mass  
textures and**

$$s_{12}^e \approx s_{13}^e \approx 0$$

# Testability

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- Neutrino sector predictions
- Low-energy UV completion?
- Full-fledged SU(5) model?
- **The U(2) Axiflavor**

$U(1)_F$  spontaneously broken and has QCD anomaly:  
Goldstone is QCD axion solving Strong CP [“axiflavor”]

Wilczek '82; Ema, Hamaguchi, Moroi, Nakayama '16; Calibbi, Goertz, Redigolo, RZ, Zupan '16

Predict flavor-violating axion couplings, fix cutoff by Axion DM

# The U(2) Axiflaviton

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$$\mathcal{L}_a = \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu \left[ C_{f_i f_j}^V + C_{f_i f_j}^A \gamma_5 \right] f_j + \frac{E}{N} \frac{a(x)}{f_a} \frac{\alpha_{\text{em}}}{8\pi} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

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 U(I)<sub>F</sub> charges give  
anomaly coefficients

$$N_{\text{DW}} = 2N = 9$$
$$E/N = 8/3 \quad [\text{SU}(5)]$$

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 Flavon breaking scale  
(-cutoff) sets mass scale

$$f_a \sim \sqrt{\epsilon_\chi^2 + \epsilon_\phi^2} \Lambda$$
$$m_a = 5.7 \mu\text{eV} \left( \frac{10^{12} \text{GeV}}{f_a} \right)$$

---

 Yukawa structure gives  
axion-fermion couplings

$$C_{f_i f_j}^V = (V_{fL})_{ki} X_{f_k} (V_{fL})_{kj}^*$$
$$C_{f_i f_j}^A = (V_{fR})_{ki}^* X_{f_k^c} (V_{fR})_{kj}$$

# The U(2) Axiflavor

$$\begin{aligned}
 C_{u_i u_j}^V &= \frac{\varepsilon_{L,ij}^u - \varepsilon_{R,ij}^u}{9}, & C_{u_i u_j}^A &= \frac{2\delta_{ij} - \varepsilon_{L,ij}^u - \varepsilon_{R,ij}^u}{9}, \\
 C_{d_i d_j}^V &= \frac{\varepsilon_{L,ij}^d}{9}, & C_{d_i d_j}^A &= \frac{2\delta_{ij} - \varepsilon_{L,ij}^d}{9}, \\
 C_{e_i e_j}^V &= -\frac{\varepsilon_{R,ij}^e}{9}, & C_{e_i e_j}^A &= \frac{2\delta_{ij} - \varepsilon_{R,ij}^e}{9},
 \end{aligned}$$

$$\varepsilon_L^u \sim \varepsilon_R^u \sim \varepsilon_L^d \sim \varepsilon_R^e \sim \begin{pmatrix} \lambda^6 & \lambda^5 & \lambda^3 \\ \lambda^5 & \lambda^4 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$

SU(2)/D<sub>6</sub> protects s-d transitions, strongest bound from SN

Coupling	$m_a^{\max}/C$ [eV]	$m_a^{\max, \text{U}(2)}$ [eV]	$f_a^{\min, \text{U}(2)}$ [GeV]	Constraint
$C_{bs}^V$	$9.1 \cdot 10^{-2}$	16	$3.6 \cdot 10^5$	$B^+ \rightarrow K^+ a$ [28]
$C_{sd}^V$	$1.7 \cdot 10^{-5}$	0.58	$9.8 \cdot 10^6$	$K^+ \rightarrow \pi^+ a$ [29]
$C_{ee}^A$	$3.1 \cdot 10^{-3}$	0.014	$4.1 \cdot 10^8$	WD Cooling [30]
$C_N$	$3.5 \cdot 10^{-3}$	0.0092	$6.2 \cdot 10^8$	SN1987A [31]

# U(2) Axiflavor Phenomenology

$U(1)_F$  broken before inflation:

$$\Omega_{DM} h^2 \approx 0.12 \left( \frac{6 \mu\text{eV}}{m_a} \right)^{1.165} \theta^2$$

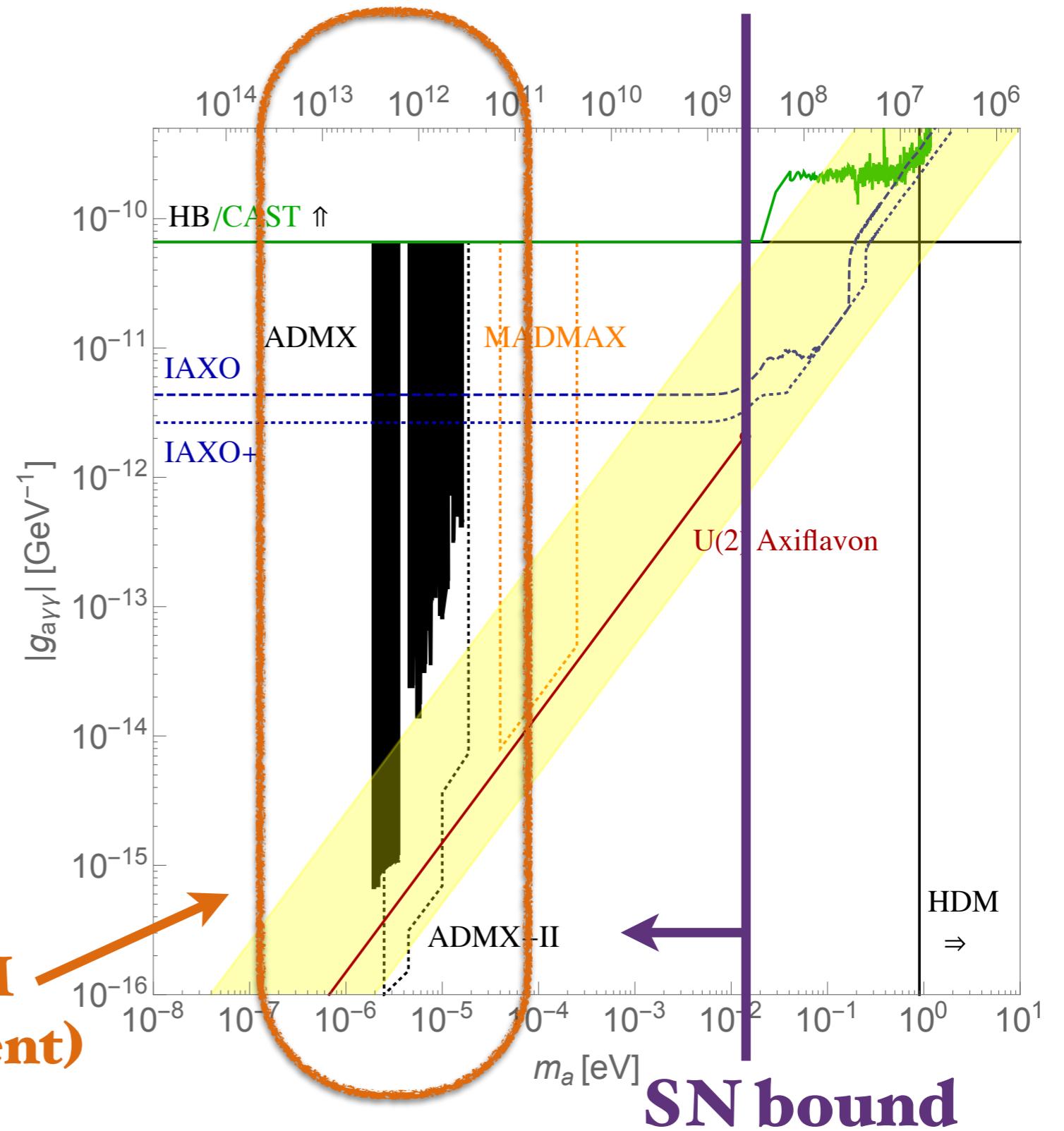
with misalignment angle

$$\theta \in [-\pi, \pi]$$

Axion DM gives preferred range for cutoff

$$\Lambda \sim (10^{13} \div 10^{15}) \text{ GeV}$$

**Natural Axion DM window (misalignment)**



# A U(2) Model of Flavor Anomalies

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Vector Leptoquark model with U(2) governing all couplings

[arxiv:1904.04121](#) with R. Barbieri

I) Vector Leptoquark couples only to heavy vector-like family

$$\mathcal{L}_{int} = g_V V_\mu^a (\bar{Q}_i^a \gamma_\mu L_i + \bar{D}_i^a \gamma_\mu E_i) + h.c.$$

$$V_\mu^a = (\mathbf{3}, 1)_{2/3}$$

2) Heavy vector-like family mixes with chiral fields

$$\mathcal{L}_{\text{mass}} = M_Q \bar{Q}_i Q_i + \bar{Q}_i (m_Q)_{ij} q_j + \bar{q}_i (\lambda_u)_{ij} u_j h + \dots$$

3) Get Leptoquark couplings to light fields through mixing;  
fit CC and NC anomalies & constraints from loop  $\Delta F = 2$

# Mass Mixing

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Take vectorlike quantum numbers  $Q_a^c \sim q_a, Q_3^c \sim q_3 \dots$   
[ and SU(4) compatible charges instead of SU(5):  $e^c \leftrightarrow \ell$  ]

**Mixing sizable only for 3rd generation doublets!**

$$m_q = \begin{pmatrix} \epsilon^2 \epsilon'^4 & \epsilon'^2 & \epsilon \epsilon'^2 \\ -\epsilon'^2 & \epsilon^2 & \epsilon \\ \epsilon \epsilon'^2 & \epsilon & 1 \end{pmatrix} \quad m_d = \begin{pmatrix} \epsilon^2 \epsilon'^4 & \epsilon'^2 & \epsilon \epsilon'^3 \\ -\epsilon'^2 & \epsilon^2 & \epsilon \epsilon' \\ \epsilon \epsilon'^3 & \epsilon \epsilon' & \epsilon'^2 \end{pmatrix}$$



$$\mathcal{L}_{\text{LQ}} \approx g_V s_{q3} s_{\ell 3} V_\mu^a (\bar{q}_3^a \gamma^\mu \ell_3)$$

**LQ couples only to 3rd generation in gauge basis**

# Effective Leptoquark Couplings

**LQ couplings determined by LH Yukawa sector**

$$\mathcal{L}_{int}^{physical} = g_V s_{q3} s_{l3} V_\mu^a (\bar{d}_{iL}^a \gamma_\mu F_{ij}^D e_{jL} + \bar{u}_{iL}^a \gamma_\mu F_{ij}^U \nu_{jL}) + h.c.$$

$$F_{ij}^D = D_{3i}^{L*} E_{3j}^L \quad F_{ij}^U = U_{3i}^{L*} E_{3j}^L$$

$$V_{ij} = \sum_k U_{ki}^{L*} D_{kj}^L$$

**Good fit to B-anomalies with largish CL rotations only prevented by sign**

$$\Delta R_D = 0.06 \left( \frac{\text{TeV}}{M_{\text{eff}}} \right)^2 \left[ 1 - \mathcal{R}e \left( \frac{D_{23}}{V_{cb}} \right) \right]$$

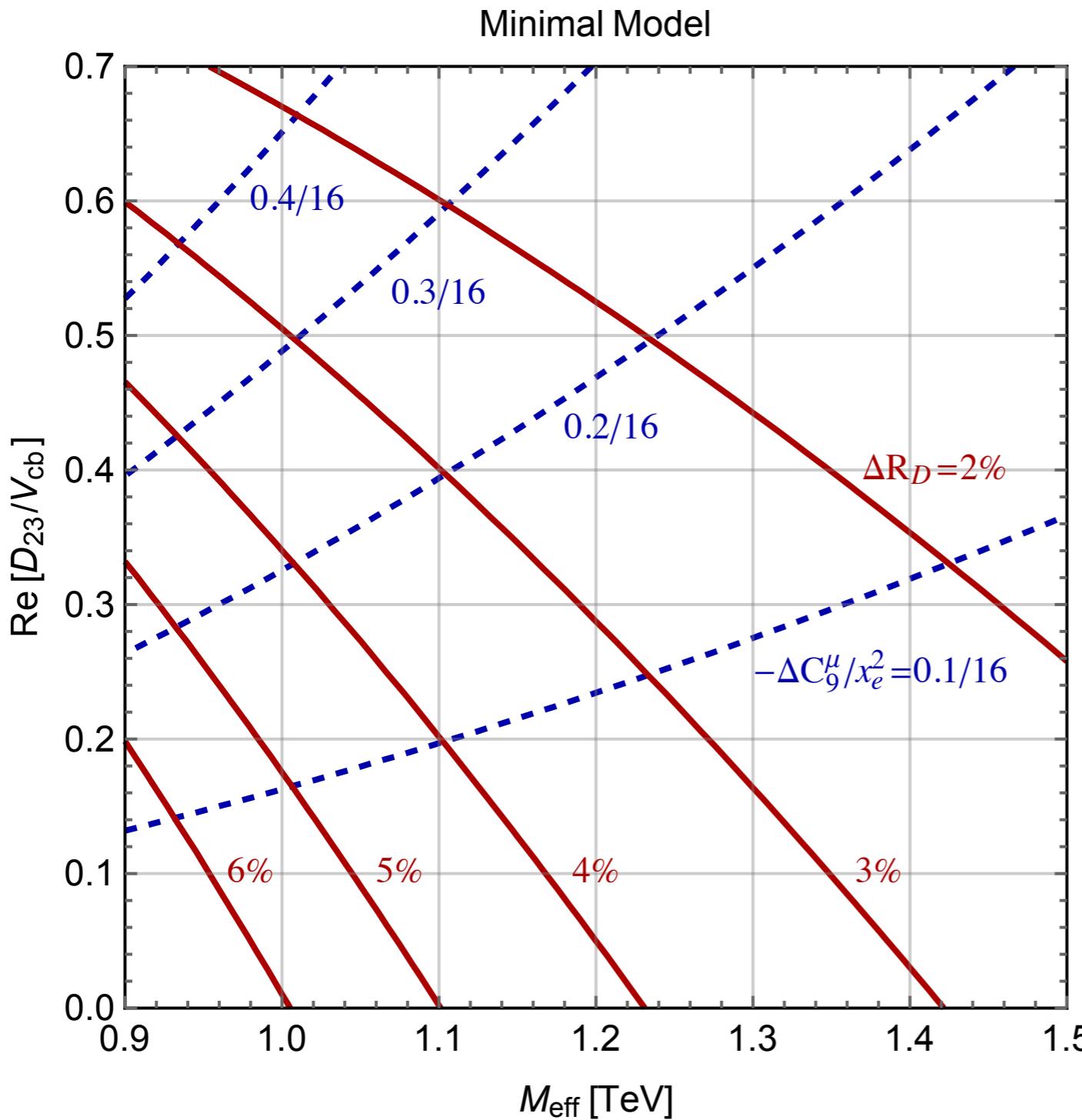
$$\Delta R_D = (14 \pm 4) \%$$

$$\Delta C_9^\mu = -0.04 \left( \frac{\text{TeV}}{M_{\text{eff}}} \right)^2 \left| \frac{E_{23}}{V_{cb}} \right|^2 \mathcal{R}e \left( \frac{D_{23}}{V_{cb}} \right)$$

$$\Delta C_9^\mu = -(0.53 \pm 0.09)$$

$$M_{\text{eff}} = \frac{M_V}{g_V s_{q3} s_{l3} c_{ql}}$$

# Effective Leptoquark Couplings



$$x_e = |E_{23}/V_{cb}| \sim \mathcal{O}(1)$$

$$\Delta R_D = (14 \pm 4) \%$$

$$\Delta C_9^\mu = -(0.53 \pm 0.09)$$

# Summary

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- Simple and realistic model of flavor from  $U(2)$ ; viable CKM, non-SUSY, includes neutrinos
- Majorana Neutrinos are automatically anarchic; can predict absolute neutrino mass scale
- Naturally get QCD Axion as DM from  $U(1)_F$ ; fixes flavor scale;  $SU(2)$  strongly suppresses flavor violation
- With leptoquark and vector-like fermions get too predictive model for flavor anomalies