

$$B_s^0 \rightarrow K^- \mu^+ \nu_\mu @ \text{LHCb}$$

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Challenges in Semileptonic B Decays, Barolo, April 21, 2022



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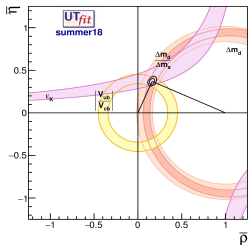


Disclaimer

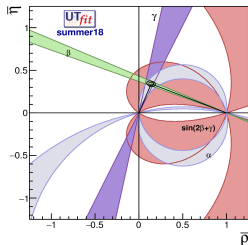
- The purpose of these slides is to provoke discussions and spark ideas **not to present formal LHCb statements**
- My (messy) slides **are the discussion** which follows a formal talk ... not the actual talk!
 - Formal LHCb results are shown at **CKM 2021**
 - Slides assume you are aware of $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ **results @ LHCb** and familiar/aware with LHCb Upgrades plans
- Slides contain combination of theory work(not all of them), formal results and *personal* projections [Please do not quote them outside the workshop]

$B_s^0 \rightarrow K^- \mu^+ \nu_\mu$: Constrain CKM picture

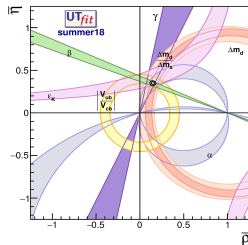
- β and V_{ub}/V_{cb} over-constrain the same side of B^0 unitary angle
- Tensions are a clear sign for New Physics



CP conserving



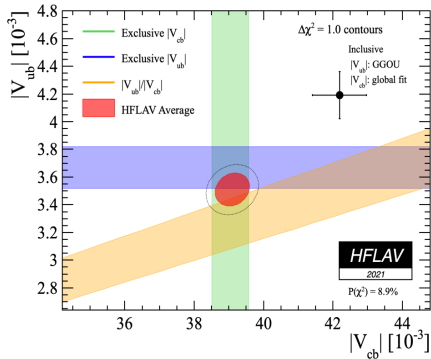
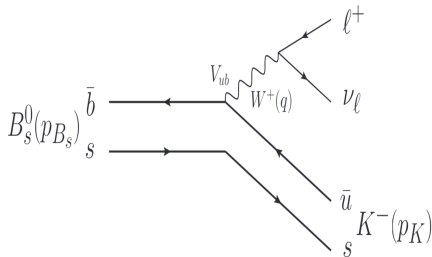
CP violating



All

$B_s^0 \rightarrow K^- \mu^+ \nu_\mu$: V_{ub} exclusive/inclusive

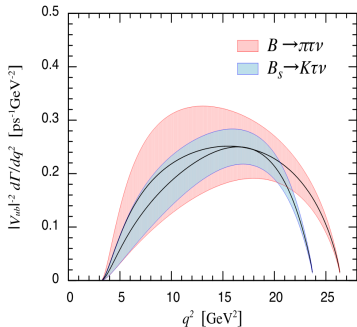
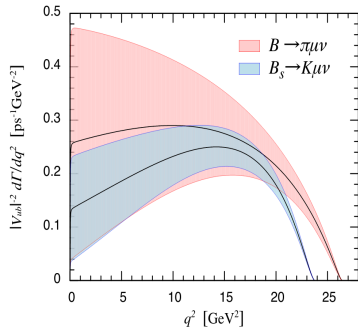
- $b \rightarrow u$ transition: measure V_{ub}
- Inclusive & exclusive measurements are in disagreement ($\sim 3\sigma$)



HFLAV 2021

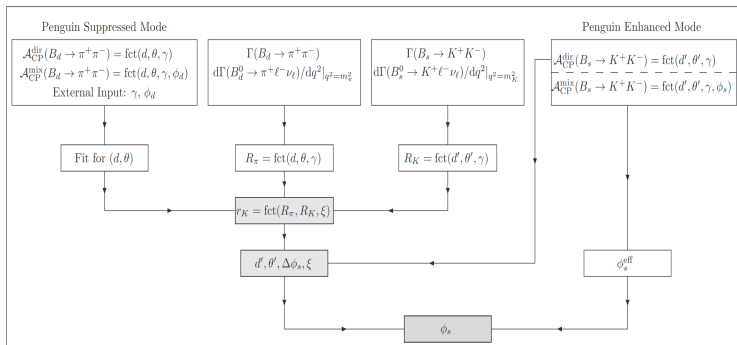
$B_s^0 \rightarrow K^- \mu^+ \nu_\mu$: V_{ub} Golden mode

- Better Lattice precision for $|V_{ub}|$ due to favorable Kaon mass for the Lattice
- Comparison from [Phys. Rev. D 91, 074510 \(2015\)](#)



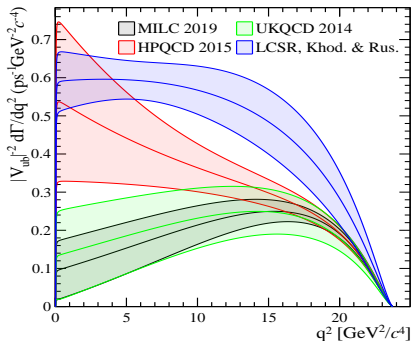
$B_s^0 \rightarrow K^- \mu^+ \nu_\mu$: Control penguins

- Upgrade era: need to control penguin contributions for CPV phases very precisely
- Semileptonic differential decay rates can be used to control penguins!
 - 1 Cross check penguin pollution for $B^0 \rightarrow J/\psi K_S^0$ ($\sin(2\beta)$) using new strategy [arxiv.2010.14423]
 - 2 Provide better strategy [arxiv.1608.00901] to precisely control penguins for $B_s^0 \rightarrow K^+ K^-$ (ϕ_s)
- These strategies requires measurement of the decay rate shape at $q^2 = m_{J/\psi} (m_{K^+})$



$B_s^0 \rightarrow K^- \mu^+ \nu_\mu$: Form Factor disagreement

- Solve long-standing disagreement between LCSR and some LQCD calculations



- Measure of BRs ratio of $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ & $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$

$$\underbrace{\frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)}}_{\text{experiment}} = \frac{|V_{ub}|^2}{|V_{cb}|^2} \times \underbrace{\frac{d\Gamma(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)/dq^2}{d\Gamma(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)/dq^2}}_{\text{theory input}}$$

- Convert to $|V_{ub}|/|V_{cb}|$: requires calculations of Form Factors
- Theory input: Complementary approaches, decay rates predicted as a function of q^2 ($\mu\nu$ invariant mass)
 - $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$: LCSR(precise at low q^2) & LQCD(precise at high q^2)
 - $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$: LQCD(precise over full q^2 spectrum)

1 Ratio of Branching fractions of $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ & $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$

$$\frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)}$$

2 Two partial BRs ratios:

- Split in two q^2 regions for $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ ($q^2_{B_s^0 \rightarrow K^- \mu^+ \nu_\mu} < (>) 7 \text{ GeV}^2$)
- Use the full q^2 spectrum of $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$

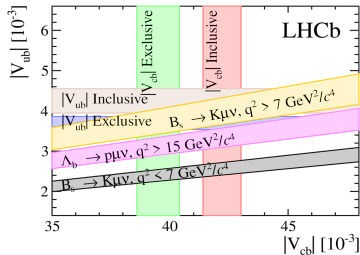
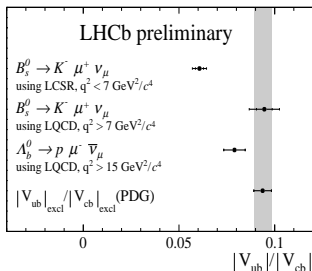
$$\frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)_{q^2 < 7}}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)_{\text{Full } q^2}}, \quad \frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)_{q^2 > 7}}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)_{\text{Full } q^2}}$$

- q^2 Bin choice: balance visible yields with theory uncertainty \rightarrow worse FF uncertainty
- Will be optimized in future (full Run1+Run2 data) to exploit the precise FF prediction at very high q^2

Results: $\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)$ [Phys. Rev. Lett. 126 (2021) 081804]

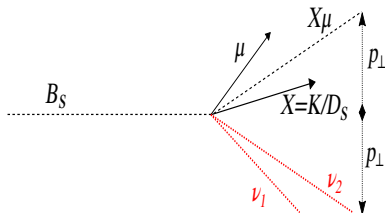
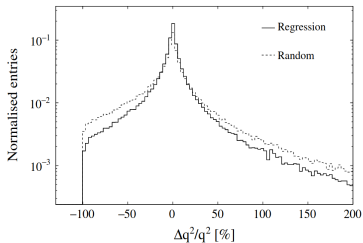
$$|V_{ub}|/|V_{cb}|(\text{low}) = 0.0607 \pm 0.0015(\text{stat}) \pm 0.0013(\text{syst}) \pm 0.0008(D_s) \pm 0.0030(\text{FF})$$

$$|V_{ub}|/|V_{cb}|(\text{high}) = 0.0946 \pm 0.0030(\text{stat})_{-0.0025}^{+0.0024}(\text{syst}) \pm 0.0013(D_s) \pm 0.0068(\text{FF})$$



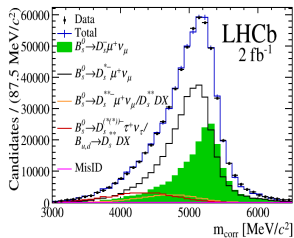
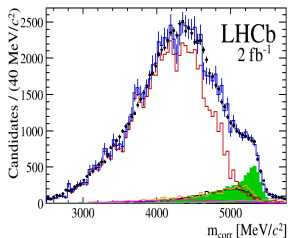
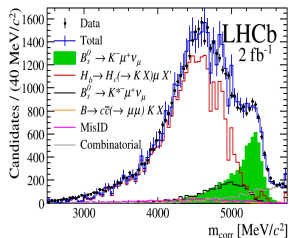
- $|V_{ub}|/|V_{cb}|(\text{high})$: compatible with $\Lambda_b \rightarrow p \mu^- \nu_\mu$, similar experimental uncertainties
- Discrepancy $|V_{ub}|/|V_{cb}|(\text{low})$: clash in theory predictions \rightarrow solved when measuring full q^2 shape of $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$

- Analysis requires q^2 reconstruction:
 - Infer P_ν from B_s^0 topology \rightarrow two-fold ambiguity
 - Use linear regression (JHEP 02 (2017) 021) to choose correct P_ν solution
- $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ & $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$
 - Fit data using "corrected mass"
 - $M_{corr} = \sqrt{M_{X\mu}^2 + p_\perp^2} + p_\perp$
- Similar vetoes to select/reconstruct $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ & $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$
 - Use inclusive $D_s^- \rightarrow K^+ K^- \pi^-$ decays



Yields: $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ & $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$ [Phys. Rev. Lett. 126 (2021) 081804]

- Statistical uncertainty is dominated by $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$
- Analysis uses only 2 fb^{-1} of LHCb data, $\sim 20\%$ of available data
 - Potential for $\times 2$ improvement on statistical uncertainty
- Large backgrounds contributions reduce fit sensitivity
 - New method is currently underway to reduce it



$$N_{K(\text{low})} = 6922 \pm 285, \quad N_{K(\text{high})} = 6399 \pm 370, \quad N_{D_s} = 201450 \pm 5200$$

Systematics breakdown [Phys. Rev. Lett. 126 (2021) 081804]

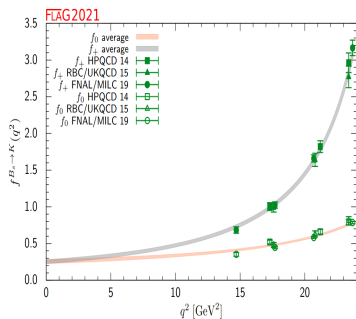
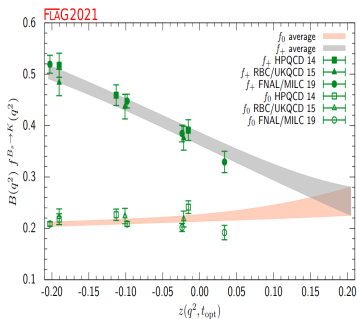
Uncertainty	$\frac{\mathcal{B}(B_s \rightarrow K\mu\nu)}{\mathcal{B}(B_s \rightarrow D_s\mu\nu)}$ [%]		
	No q^2 sel.	low q^2	high q^2
Tracking	2.0	2.0	2.0
Trigger	1.4	1.2	1.6
Particle ID	1.0	1.0	1.0
m_{CORR} error	0.5	0.5	0.5
Isolation	0.2	0.2	0.2
Charged BDT	0.6	0.6	0.6
Neutral BDT	1.1	1.1	1.1
q^2 migration		2.0	2.0
ϵ gen& reco	1.2	1.6	1.6
Fit template	+2.3 -2.9	+1.8 -2.4	+3.0 -3.4
Total	+4.0 -4.3	+4.3 -4.5	+5.0 -5.3
$\mathcal{B}(D_s^- \rightarrow K^- K^+ \pi^-)$	2.8	2.8	2.8

- Better strategy is developed to reduce the number of systematic sources
- Multiple Systematic sources for ϵ relies on $B^+ \rightarrow J/\psi K^+$ as control channel \rightarrow reducible with larger data sets
- Fit systematics dominated by simulation size \rightarrow we produced $\sim 10\times$ larger sample to reduce this effect
- BESIII: Plans to better measure $\mathcal{B}(D_s^- \rightarrow K^- K^+ \pi^-) \rightarrow \sim 1.5\%$ on $|V_{ub}|/|V_{cb}|$

Form Factor systematic

- Recent average from FLAG in 2021:

<http://cds.cern.ch/record/2791030/files/2111.09849.pdf>



- Our choice of bins for high q^2 caused higher FF uncertainty
- Next measurement will have finer bins any way

Form Factor systematic

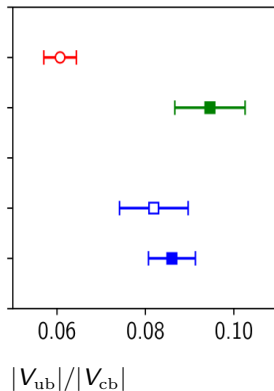
- At CKM 2021: reduction of FF uncertainty by 40% @ high q^2

LCSR low q^2 (Khodjamirian & Rusov 2017)

Lattice QCD high q^2 (FNAL/MILC 2019)

Lattice QCD low q^2 (FLAG 2021)

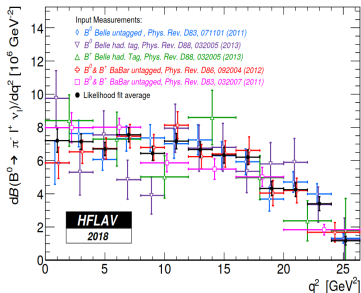
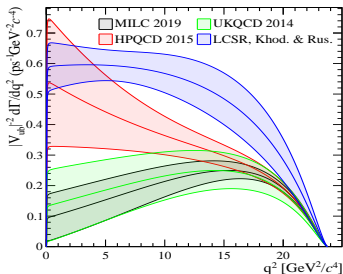
Lattice QCD high q^2 (FLAG 2021)



- We plan to use FLAG average instead of individual results in future measurements

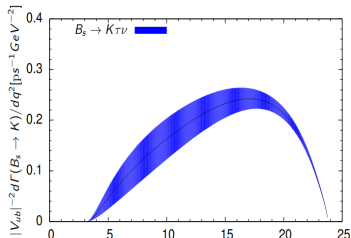
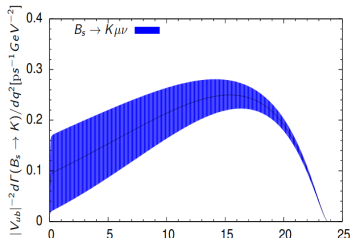
Form Factor measurement

- Measuring the partial Decay rate for $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ in **more** bins of q^2
- This will enable determining the shape similarly to BaBar and Belle approach
 - At LHCb we have to normalize to a known channel, $B^+ \rightarrow J/\psi K^+$?
 - B^+ Lifetime as input (possibly f_s/f_d)
- Run 2 has enough stats. to divide the q^2 into 6-8 bins
- Important feed-back to theory community and our simulation and for ...



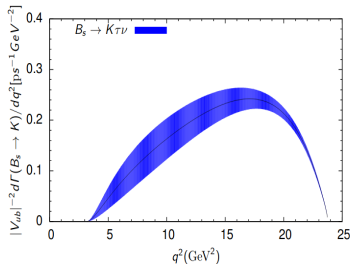
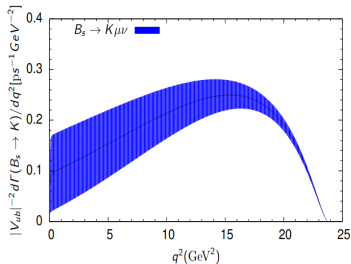
Extreme precision on $|V_{ub}|/|V_{cb}|$

- $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ is dubbed "Golden-mode" for lattice QCD due to precise FF calculations
- Those are quite precise in the "last" bin of the q^2 spectrum
- Plots below inform us (Phys. Rev. D 100, 034501 (2019)):
 - Current estimation: 3.5% in the bin 17-23 GeV/c^2 using $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$
 - Current estimation: 1.5% in the bin 17-23 GeV/c^2 using $B_s^0 \rightarrow K^- \tau^+ \nu_\tau$
- That bin has little stat. ($O(100)$) with Run1 + Run2 data
- for $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$: Run 3 provides the needed statistics ($\sim 10\times$ current) to be at theory level



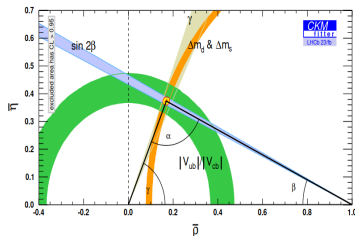
Extreme precision on $|V_{ub}|/|V_{cb}|$

- Future Lattice QCD plans (numbers extracted from Belle II Physics book):
 - $\sim 1\%$ in the bin 17-23 GeV/c^2 using $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$
 - $< .5\%$ in the bin 17-23 GeV/c^2 using $B_s^0 \rightarrow K^- \tau^+ \nu_\tau$
- For the $B_s^0 \rightarrow K^- \tau^+ \nu_\tau$ mode: we need to wait till the end of HL-LHC to be as good as the future theory projections
- Experimentally $B_s^0 \rightarrow K^- \tau^+ \nu_\tau$ is quite challenging but still feasible as demonstrated by measurements of $\mathcal{R}(D^{*-})$ -and-friends at LHCb

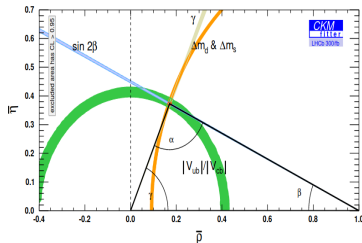


About LHCb upgrade ...

- LHCb Upgrades document [arXiv:1808.08865] provide projections for V_{ub}



Upgrade I (23 fb^{-1}),

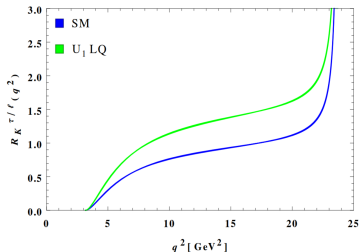
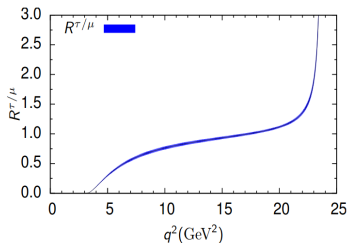


Upgrade II (300 fb^{-1})

- $|V_{ub}|/|V_{cb}|$: for Upgrade I $\sigma \sim 3\%$, while Upgrade II $\sigma \sim 1\%$ (total experimental uncertainty)
- Improvement of PID(TORCH) and enhancement of VELO design will improve M_{corr} variable greatly

Lepton Flavour Universality in $b \rightarrow ul\nu_\ell$ transitions

- LFU anomalies in $b \rightarrow cl\nu_\ell$ transitions ($R(D^{*-}), R(D^-)$)
- SM versus NP [1], [2], [3], [4] + other I probably forgot!
 - $R(K^-)_{SL}^{SM} = \frac{B_{s^0 \rightarrow K^- \tau^+ \nu_\tau}^0}{B_{s^0 \rightarrow K^- \mu^+ \nu_\mu}^0} = 0.836 \pm 0.034$
 - $R(K^-)_{SL}^{NP} = \frac{B_{s^0 \rightarrow K^- \tau^+ \nu_\tau}^0}{B_{s^0 \rightarrow K^- \mu^+ \nu_\mu}^0} = 1.133 \pm 0.104$
- Stat. are needed to prob the $R(K^-)_{SL}$ in full and (per-bin of) q^2 spectrum
- Need Upgrade II to be at the level of theory



Phys. Rev. D 100, 034501 (2019) , Nucl. Part. Phys. 48 (2021) 075006

Conclusion

- It has been two years since we published $|V_{ub}|/|V_{cb}|$ using $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ and $B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu$ in two q^2 regions
 - The Form Factor measurement of $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ is starting
 - But slowly ...
- $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ program and LHCb upgrades need each other:
 - Form Factors, extreme precision on $|V_{ub}|/|V_{cb}|$ and LFU ideal place to look for NP
 - $B_s^0 \rightarrow K^- \mu^+ \nu_\mu$ is also crucial to control penguins for mixing phases $\phi_s, \sin(2\beta)$ at Upgrade era
 - + $B_s^0 \rightarrow K^{*-} \mu^+ \nu_\mu$ and $B^+ \rightarrow \phi \mu^+ \nu_\mu$
 - HI-LHC era is the ideal place to perform such measurements
- However start is complicated by:
 - Demanding activities around Run 3 (hardware, software)
 - Availability of resources