

Magnetogenesis from rotating scalar: a la scalar chiral magnetic effect

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at IBS BUSAN workshop on BSM Dec 5, 2019

Outlines

Cosmic Magnetic Fields

Generation of Cosmic Magnetic Fields

A Concrete Example of Scalar CME

Cosmic Magnetic Fields

Magnetic fields in the Universe

Cosmological magnetic fields are discovered (constrained) for different magnitudes with different scales



 $B_{\rm earth}$ 0.25 - 25 G

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Intergalactic magnetic fields

Observation of TeV blazars: indirect way to probe the magnetic fields for given coherence lengths in the cosmic void



Intergalactic magnetic fields

Observation of TeV blazars: indirect way to probe the magnetic fields for given coherence lengths in the cosmic void

Magnetic fields B_{λ} with a coherence length λ

rays from the blazar ($E_{\gamma} \sim TeV$)

 $heta_{
m deflection} \propto B_{\lambda} \sqrt{\lambda} \ for \ \lambda \ll 100 \
m kpc$ $B_{\lambda} \ for \ \lambda \gg 100 \
m kpc$



Evidence or constraints for intergalactic magnetic fields

No observation of secondary GeV photons \rightarrow evidence of intergalactic magnetic fields





Slides from Neronov UHECR 2018

Magnetic helicity

Magnetic helicity is the topological quantity which quantifies e.g. twist, kink, linkage, handedness of magnetic field lines





It can be written as the difference between the RH and LH circular polarization modes

$$\frac{dH_m}{dV} \equiv h_m = \int \frac{d^3k}{(2\pi)^3} k\left(\left|A_k^R\right| - \left|A_k^L\right|^2\right)$$



Time dependence of the helicity:

$$\frac{\partial h_m}{\partial t} = -2 \vec{E} \cdot \vec{B} = \frac{1}{2} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

(hyper) helicity of the magnetic fields can be important for the cosmological evolution in the Early Universe.

$$\partial_{\mu}J_{B} = \partial_{\mu}J_{L} = \frac{3g^{2}}{16\pi^{2}} \operatorname{Tr}\left[W_{\mu\nu}\widetilde{W}^{\mu\nu}\right] - \frac{3g'^{2}}{32\pi^{2}}B_{\mu\nu}\widetilde{B}^{\mu\nu}$$
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Generation of Cosmic Magnetic fields

New physics beyond the Standard Model can provide the explanation of amplification mechanism from the quantum fluctuations to the primordial magnetic fields for given coherence scales



Amplify by New Physics



*B*_{quantum}



*B*_{primordial}

Amplify by Standard Physics







Generation of Cosmic Magnetic Fields

Chiral Magnetic Effect

Step1) Chirality imbalance of (relativistic) fermions ($n_R \neq n_L$) + Magnetic fields \rightarrow Electric current



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Magnetogenesis via Chiral Magnetic Effect

Step2) From Maxwell equations (ignoring fluid vorticity)

Joyce, Shaposhnikov 9703005 Tashiro, Vachaspati, Vilenkin 1206.5549

dt

$$\nabla \times \vec{B} = \frac{\partial \vec{E}}{\partial t} + \vec{J}, \qquad \nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} \qquad \left(J \simeq J_{\text{Ohm}} + J_{\text{CME}} = \sigma \left(\vec{E} + \vec{v} \times \vec{B} \right) + \frac{e^2}{2\pi^2} \mu_5 \vec{B} \right)$$

for the length scale of interest $\lambda \sim \nabla^{-1} \gg \frac{1}{\sigma v}, \frac{1}{e^2 T}$, $(\sigma \sim T/e^2)$

$$\partial_t \vec{B} \approx \frac{1}{\sigma} \left(\nabla^2 \vec{B} + \frac{e^2 \mu_5}{2\pi^2} \nabla \times \vec{B} \right) \quad \to \quad \frac{d}{d\tau} \vec{B}_k^{\pm} + \frac{1}{\sigma} k \left(k \mp \frac{e^2 \mu_5}{2\pi^2} \right) \vec{B}_k^{\pm} = 0 \qquad \left(d\tau = \frac{d\tau}{a(t)} \right)$$

could yield the instability of one polarization mode for the coherence length $\lambda \sim 1/k_{peak}$ $\begin{aligned} \left|\vec{B}_{k}^{\pm}\right| \sim |B_{0}^{\pm}| \exp\left(\frac{\tau}{\sigma}k_{peak}^{2}\right) e^{-\frac{\tau}{\sigma}(k \mp k_{peak})^{2}} \right| \left(k_{peak} = \frac{e^{2}\mu_{5}}{2\pi^{2}}\right) \vec{B}_{k}^{\pm 1.0} \vec$

Helicity density is given by

$$h_m \sim \frac{T^3 |B_0^+|^2}{\sqrt{2\pi^2 \tau / \sigma}} k_{peak} \exp\left(2\frac{\tau}{\sigma} k_{peak}^2\right)$$

And μ_5 will rapidly decrease as the helicity increases exponentially : saturated around $h_{msat} \sim (4\pi/e^2)\mu_{5in}T^2$

$$\frac{d\mu_{5}}{dt} \simeq -\frac{e^{2}}{4\pi T^{2}} \frac{dh_{m}}{dt} \to \mu_{5}(\tau) \simeq \mu_{5in} - \frac{e^{2}}{4\pi} \frac{T |B_{0}^{+}|^{2}}{\sqrt{2\pi^{2}\tau/\sigma}} k_{peak} \exp\left(2\frac{\tau}{\sigma}k_{peak}^{2}\right)$$
¹⁶

Axion-Like Particle with Anomalous Coupling

In the case with CME, the origin of $\mu_5 \neq 0$ is unclear. Axion-like particle can give the alternative source of μ_5

$$\mathcal{L} = \frac{1}{2} \left(\partial_{\mu} \phi \right)^{2} + \Lambda^{4} \cos \frac{\phi}{f} + \frac{g_{\phi\gamma}}{32\pi^{2} f} \phi F_{\mu\nu} \tilde{F}^{\mu\nu}$$

The Maxwell equations:

 $\nabla \times \vec{B} = \frac{\partial \vec{E}}{\partial t} + \frac{g_{\phi\gamma} \dot{\phi}}{8\pi^2 f} \vec{B} \rightarrow \vec{J}_{eff} = \frac{g_{\phi\gamma} \dot{\phi}}{8\pi^2 f} \vec{B}$

Instability arises around the mode
$$k \sim \xi(\tau)/\tau$$

$$\frac{d^2}{d\tau^2}\vec{A}_k^{\pm} + k^2\left(1\pm\frac{\xi(\tau)}{k\tau}\right)\vec{A}_k^{\pm} = 0$$



Anber Sorbo 0606534 and many others

(_{z _}	$g_{\phi\gamma}\dot{\phi}$
$\zeta =$	$\overline{16\pi^2 Hf}$

e.g. During inflation for the light axion ($m_{\phi} \leq H$), $3H\dot{\phi} \simeq -\partial_{\phi}V \sim -m_{\phi}^2\phi \sim m_{\phi}^2f$, Tachyonic instability happens if $\xi \pi \gg 1$

$$\left|\vec{B}\right| \sim \frac{10^{-2} \exp(\pi\xi)}{\xi^{\frac{5}{2}}} H_{inf}^{2}, \qquad \lambda \sim \frac{\pi\xi}{H_{inf}}, \qquad \frac{dh}{dt} \sim \xi \left|\vec{B}\right|^{2} \qquad \left(\text{However ... } \xi\pi = \frac{g_{\phi\gamma} \dot{\phi}}{16\pi Hf} \sim \frac{g_{\phi\gamma} m_{\phi}^{2}}{16\pi H^{2}} \gg 1 \rightarrow g_{\phi\gamma} \gtrsim O(100)\right)$$

Axion-Like Particle with Anomalous Coupling

In the case with CME, the origin of $\mu_5 \neq 0$ is unclear. Axion-like particle can give the alternative source of μ_5



After reheating: parametric resonance can occur since $\dot{\phi} \sim \cos m_{\phi} t$ (both RH, LH modes are produced)

In any case $g_{\phi\gamma} \gtrsim O(100)$ is necessary.

Another problem: If there are the light charged fermions ψ , $\phi F \tilde{F}$ coupling can be shifted to $\partial_{\mu} \phi \bar{\psi} \gamma^{\mu} \psi$ by chiral rotation. gauge field production \rightarrow fermion production: Schwinger effects etc. prevent the exponential growing of B-fields During inflation case : $|\vec{B}| \leq 3\pi^2 \xi^2 H_{inf}^2$ Domcke, Mukaida 1806.08769 18

Rotating scalar field

Considering the complex scalar field with a kinetic energy along θ direction for $V(\phi) = m^2 |\phi|^2$ If the charged fermion has the mass by ϕ as

$$\mathcal{L}_{fermion} = \bar{\psi} i \gamma^{\mu} (\partial_{\mu} - i q A_{\mu}) \psi - (y \phi \psi_L \psi_R + h. c.),$$

during rotation along θ direction, the fermion becomes heavy with the mass $m_{\psi} = y\rho$. Integrating out the fermion yields

$$\mathcal{L}_{eff} = c_A \frac{e^2}{16\pi^2} \theta(\mathbf{x}) F_{\mu\nu} \tilde{F}^{\mu\nu}$$



Nonzero $\dot{\theta}$ implies the nonzero PQ charge $(U(1)_{PQ}: \phi \to \phi e^{i\alpha}, \psi_L \psi_R \to e^{-i\alpha} \psi_L \psi_R)$,

$$J_{PQ}^0 = 2\rho^2 \dot{\theta}$$

which is conserved until the breaking effect by the exponentially increasing B(E)-fields becomes important

$$\partial_{\mu}J^{\mu}_{PQ} \simeq 2\rho^2 \ddot{\theta} = -c \frac{e^2}{16\pi^2} F\tilde{F} = -c_A \frac{e^2}{8\pi^2} \frac{dh_m}{dt} \rightarrow h_{msat} = \frac{16\pi^2}{c_A e^2} \rho^2 \dot{\theta}_{in}$$

Rotating scalar field

Tachyonic instability happens if $\theta(t)$ cycles many times within a Hubble time

No charged light fermions during magnetogenesis,

Maximally helical,

Long time evolution by approximate $U(1)_{PQ}$ like a chiral symmetry at high temperature



But how can we give such initial conditions (the large value of ρ , and initial kick along θ -direction)?

A Concrete Example of Scalar CME

Kamada CSS, 1905.06966

Dynamical origin of the rotating scalar

Affleck-Dine mechanism

Scalar potential = PQ symmetric term + small PQ breaking term + Hubble induced negative mass squares e.g.

$$V(\phi) = (m^2 + c H^2) |\phi|^2 - (\epsilon \phi^4 + h.c.) + \frac{|\phi|^6}{\Lambda^2} \qquad \left(m^2 > 0, c < 0, \epsilon \sim \frac{m}{\Lambda} \text{ (SUSY case), } H^2 = \frac{\rho_{tot}}{3M_P^2} \propto \frac{1}{a^3}\right)$$

The Hubble induced negative mass squared is dominant at the early Universe : $H^2 \gg m^2 \rightarrow \langle \phi \rangle = \rho \sim \sqrt{H\Lambda} \gg m$

$$V(\rho,\theta) = (m^{2} + cH^{2})\rho^{2} - 2\epsilon\rho^{4} + \frac{\rho^{6}}{\Lambda^{2}} - 2\epsilon\rho^{4} (\cos 4\theta - 1)$$

During $H^2 \gg m^2$, along the θ direction, the field is frozen since $m_{\theta}^2 \sim \epsilon \rho^2 \sim m H \ll H^2$

Small PQ breaking terms plays the important when $H \sim m$ to induce "rolling" and "kicking"

Dynamical origin of the rotating scalar

 $V(\phi) = (m^2 + c H(t)^2) |\phi|^2 - (\epsilon \phi^4 + h.c.) + \frac{|\phi|^6}{\Lambda^2}$



Dynamical origin of the rotating scalar

Along the θ direction, as $\rho(t)$ decreases, the potential barrier becomes lower. The axion has the enough kinetic energy to go over the wall, and rotates for a long time

 $V_{eff}(\theta) = 2\epsilon\rho(t)^4 \left(1 - \cos 4\theta\right)$



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Generation of *B*-field and helicity

B-fields, helicity are exponentially growing and saturated during the rotation of theta-field.

When they are generated

$$y \text{ are generated} \\ B_{sat} \simeq \left(\frac{k_{peak}}{a(\tau_{osc})}\frac{h_{sat}}{a(\tau_{osc})^3}\right)^{\frac{1}{2}} \simeq 10^{12} GeV \left(\frac{\rho_{osc}}{10^{12} GeV}\right) \left(\frac{\dot{\theta}}{10^3 GeV}\right) \\ \lambda_{coh} \simeq 2\pi \left(\frac{k_{peak}}{a(\tau_{osc})}\right)^{-1} \simeq \left(\frac{3}{c_A GeV}\right) \left(\frac{\dot{\theta}}{10^3 GeV}\right)^{-1} \\ \end{pmatrix}^{-1}$$

At the present Universe, adiabatic evolution and conserved comoving helicity ($\lambda B^2 \propto 1/a^3$) followed by magnetohydrodynamics to rearrange the fields as ($\lambda(t_0) \sim 1pc \left(\frac{B(t_0)}{10^{-14}G}\right)$)

$$B(t_0) \simeq 10^{-16} G \left(\frac{T_{RH}}{10^8 GeV}\right)^{1/3} \left(\frac{H_{osc}}{GeV}\right)^{-\frac{2}{3}} \left(\frac{\rho_{osc}}{10^{12} GeV}\right)^{\frac{2}{3}} \left(\frac{\dot{\theta}}{10^3 GeV}\right)^{1/3}$$
$$A_{coh}(t_0) \simeq 10^{-2} pc \left(\frac{T_{RH}}{10^8 GeV}\right)^{1/3} \left(\frac{H_{osc}}{GeV}\right)^{-\frac{2}{3}} \left(\frac{\rho_{osc}}{10^{12} GeV}\right)^{\frac{2}{3}} \left(\frac{\dot{\theta}}{10^3 GeV}\right)^{1/3}$$

Two Higgs Doublet Model

In the minimal extension of the Standard Model, the Higgs is a good candidate for the AD field. To impose the PQ symmetry, two Higgs doublet model can be naturally taken.

$$-\mathcal{L} = \dots + Y_u Q H_u u^c + Y_d Q H_d d^c + Y_e L H_d e^c + h.c. + V(H_u, H_d)$$

with $U(1)_{PQ}$: $H_u \rightarrow e^{i\alpha}H_u$, $H_d \rightarrow e^{i\alpha}H_d$, $Qu^c \rightarrow e^{-i\alpha}Qu^c$, $Qd^c \rightarrow e^{-i\alpha}Qd^c$, $Le^c \rightarrow e^{-i\alpha}Le^c$

Motivated by SUSY,

$$V(H_u, H_d) = m_u^2 |H_u|^2 + m_d^2 |H_d|^2 - \left(\frac{A}{\Lambda} (H_u H_d)^4 + h.c.\right) + g^2 (|H_u|^2 - |H_d|^2)^2 + \frac{(|H_u|^2 + |H_d|^2)|H_u H_d|^2}{\Lambda^2} + \frac{(b(S)H_u H_d + h.c.)}{(b(S)H_u H_d + h.c.)}$$

Along the direction, $|H_u| = |H_d| = \rho(x)$, $H_u H_d \to \rho(x)^2 e^{i\theta(x)}$, and all charged fermions become massive with $m_{\psi} = Y_{\psi}\rho$. Also $SU(2)_L \times U(1)_Y \to U(1)_{EM}$ gauge bosons massive $m_{W/Z} \sim g\rho$

Massless degrees: photon, and neutrino, gluon. Light scalars: ρ and θ . Integrating out all charged fermions

$$\mathcal{L}_{eff} = (\partial_{\mu}\rho)^{2} + \rho^{2}(\partial_{\mu}\theta)^{2} - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} - V(\rho,\theta) + \frac{e^{2}}{2\pi^{2}}\theta F_{\mu\nu}\tilde{F}^{\mu\nu} + L(G_{\mu},\nu)$$
²⁶

can be generated after magnetogenesis

Implication for baryogenesis

As $\rho(t) \to 0$, m_W , $m_{\psi} \to 0$, and $SU(2)_L \times U(1)_Y$ is recovered:

 $F_{\mu\nu} \rightarrow W^3_{\mu\nu} + B_{\mu\nu}$

After the reheating, the non-abelian magnetic field $(W^3_{\mu\nu})$ will quickly decay though its screening mass of $O(m_W \sim g^2 T)$, while there is no such a screening for the hyper-magnetic field $(B_{\mu\nu})$ with a helicity H_m from magnetogenesis.

Then from quantum anomaly for baryon number

$$\partial_{\mu}J_{B} = \partial_{\mu}J_{L} = \frac{3g^{2}}{16\pi^{2}}\operatorname{Tr}\left[W_{\mu\nu}\widetilde{W}^{\mu\nu}\right] - \frac{3g'^{2}}{32\pi^{2}}B_{\mu\nu}\widetilde{B}^{\mu\nu}$$

The change of hyper magnetic helicity can be the source of baryogenesis

$$\Delta B = \Delta L = 3 \ \Delta N_{CS} - \frac{3g'^2}{16\pi^2} \Delta H_{mY}$$

Electroweak phase transition is smooth (crossover). Massless $U_X(1)$ gauge boson is adiabatically decomposed as

$$X_{\mu}(T) = B_{\mu} \cos \theta_{W}(T) + W_{\mu\nu}^{3} \sin \theta_{W}(T) \quad \left(X_{\mu}(T \gg m_{W}) \to B_{\mu}, X_{\mu}(T \ll m_{W}) \to A_{\mu}\right)$$

conserving the helicity as $H_m(X_\mu(T \gg m_W)) = H_m(X_\mu(T \ll m_W))$ which gives $\Delta H_{mY} \sim \Delta \theta_W H_m$, $\Delta N_{CS} \sim \Delta \theta_W H_m \rightarrow \Delta B \propto \Delta \theta_W H_m$

$$\frac{n_B}{s} = \left(\frac{a_{osc}}{a_{RH}}\right)^3 \left(\frac{\theta \rho_{osc}^2}{s(T_{RH})}\right) \sim 10^{-10}$$
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Kamada, Long 1610.03074 Kamada CSS, 1905.06966

Comparing with AD baryogenesis, Spontaneous baryogenesis





 $\begin{array}{ll} U(1)_B &: \ \phi \to e^{i\alpha} \phi \\ \phi \ \text{is the scalar baryon} \\ J^0_B &= 2\rho^2 \ \dot{\theta} \\ \text{Baryon number is generated} \\ \phi \to q \ell \\ \text{Decay to light quarks (baryons)} \end{array}$

Affleck Dine 1985 Nucl. Phys. B 249 361

Axionic Spontanoueous baryogenesis



$$\frac{g^2}{16\pi^2} \frac{\phi}{f} \operatorname{Tr} \left[W_{\mu\nu} \widetilde{W}^{\mu\nu} \right]$$

$$\phi \text{ is neutral under } U(1)_B$$

$$\dot{n}_B = \frac{3}{2} \frac{\Gamma_{sph}}{T} \left(\frac{\dot{\phi}}{f} - \frac{13}{2} \frac{n_B}{T^2} \right)$$

Baryon number is generated via rolling of ϕ , sphaleron process

Jeong, Jung, CSS 1811.03294, etc.

Comparing with AD baryogenesis, Spontaneous baryogenesis

Our magneto-baryogenesis



$$U(1)_{PQ}: \phi \to e^{i\alpha}\phi$$

$$J_{PQ}^{0} = 2\rho^{2}\dot{\theta}$$
PQ number is generated
$$\frac{e^{2}}{16\pi^{2}}\dot{\theta} (B_{\mu\nu}\tilde{B}^{\mu\nu} + W_{\mu\nu}^{3}W^{3\mu\nu} + \text{mixing})$$
Helical B-field is generated before reheating
$$\dot{n}_{B} = -\frac{3g'^{2}}{16\pi^{2}}\frac{dh_{Y}}{dt} + \cdots$$
Baryon number is generated
during EWPT

Summary

The intergalactic magnetic field is the interesting subject to understand the origin of cosmic magnetic fields, and the TeV gamma-ray spectrum

There are several ideas to generate primordial magnetic fields. For each case, there is some limitation from the UV point of view.

The Affleck-Dine type rotating scalar fields driven by small PQ breaking terms generate maximally helical magnetic fields like the case from Chiral Magnetic Effect. This idea can overcome several problems raised in magnetogenesis.

Thanks to the helicity, baryon asymmetry also can be generated with a reasonable value.