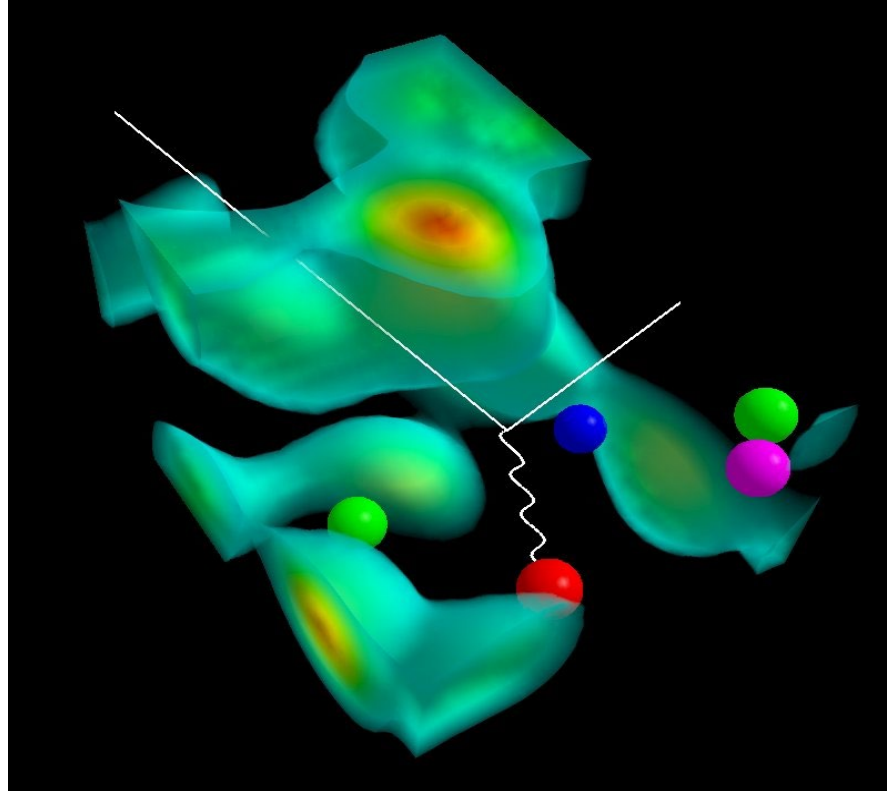


Baryon Excited States: Quark Model versus Reality



Anthony W. Thomas

**International Conference on the Structure of Baryons
Sevilla: 2-50am November 11 2022**

Outline

- I. **Excitations of the nucleon are a vital piece of the challenge to understand how hadrons are made in QCD**

- II. **New Insight into the Quark Model**
 - The $\Lambda(1405)$ IS a $K\bar{b}ar-N$ bound state
 - The Roper IS generated by $\pi N-\sigma N-\pi\Delta$ rescattering
 - But not all states are dynamically generated e.g. $N(1535)$!

- III. **The Quark Model is not so bad!**



Spectroscopy

- how do excited states emerge from QCD ?
- what are the fundamental degrees of freedom ?
- Lattice QCD provides extremely valuable information

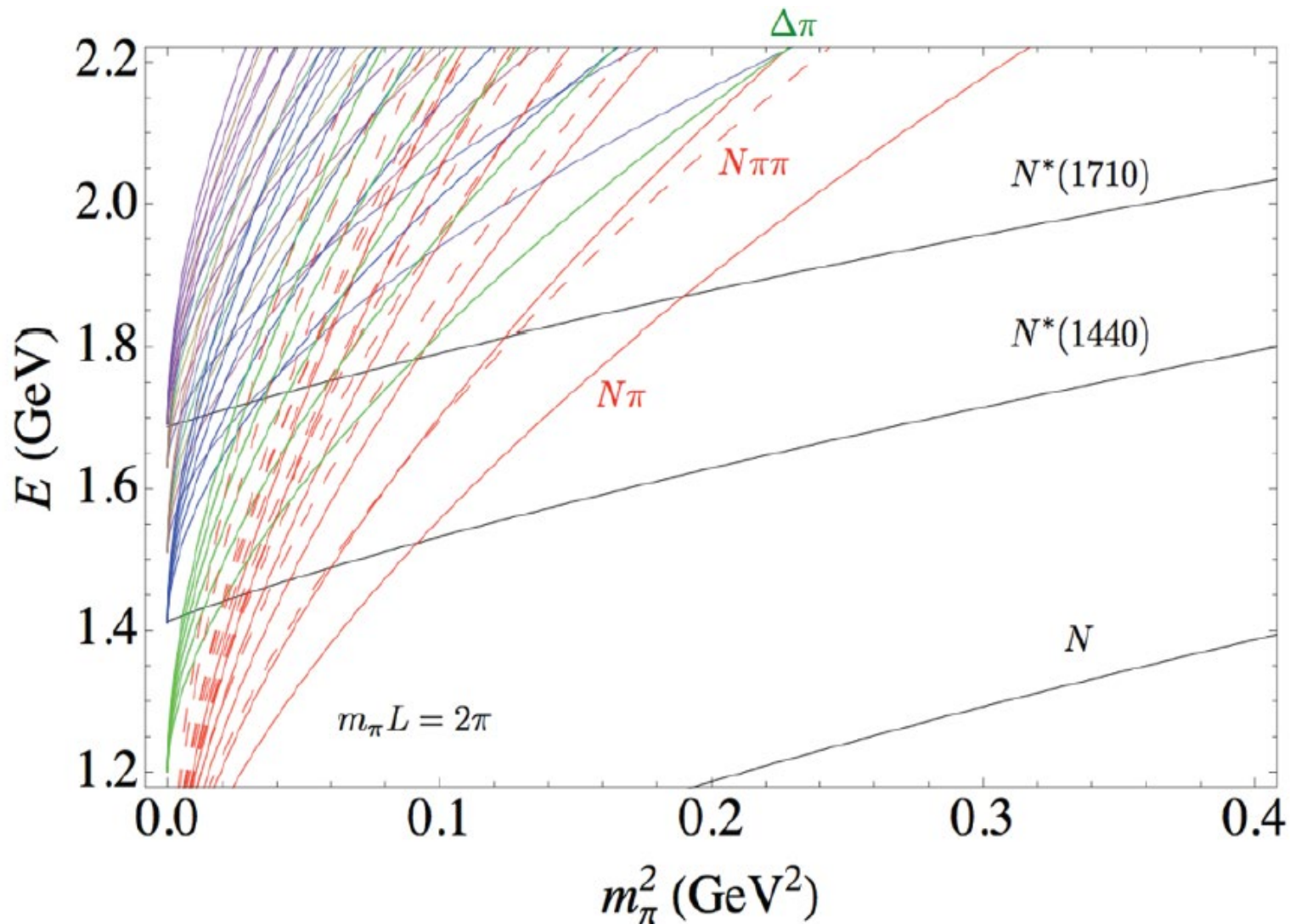
Resonances are very complicated – and the lattice is not

- **Everything is stable – an eigenstate of the QCD Hamiltonian**
- **Whereas real resonances decay like crazy.....**
- **Lüscher has a method to derive phase shifts at discrete energies when there is one open channel**
- **That approach has been generalized to coupled channels by Hansen and Sharpe (Phys.Rev. D86 (2012) 016007) and Lellouch and Lüscher (Comm.Math.Phys., 219 (2011) 31) BUT it becomes very complicated**

Interesting cases have many open channels

- at least at realistic quark masses**

In General: Multiple open channels



and then there is: σN , ωN , ρN etc....

But Lüscher does not solve all our problems

- This procedure gives no more information than we get from a phase shift analysis of experimental data
- That is, it provides no more insight into the nature of the excited states

Interesting cases

The $\Lambda(1405)$

- We have unambiguous evidence that it is a $K\bar{N}$ bound state!
50 years after speculation by Dalitz *et al.*
- To be fair Dalitz had no quark model then so there was not much else it could be at that time.
- Rather than the Lüscher method we apply **Hamiltonian Effective Field Theory**
 - shown to be equivalent for phase shifts*
 - **BUT also provides information on eigenstates**
- Carry out a Hamiltonian analysis of lattice data
- Examine the **strange magnetic form factor** of $\Lambda(1405)$

* Wu *et al.*, Phys. Rev. C 90 (2014) 5, 055206

First calculation after QCD incorporating chiral symmetry

PHYSICAL REVIEW D

VOLUME 31, NUMBER 5

1 MARCH 1985

S-wave meson-nucleon scattering in an SU(3) cloudy bag model

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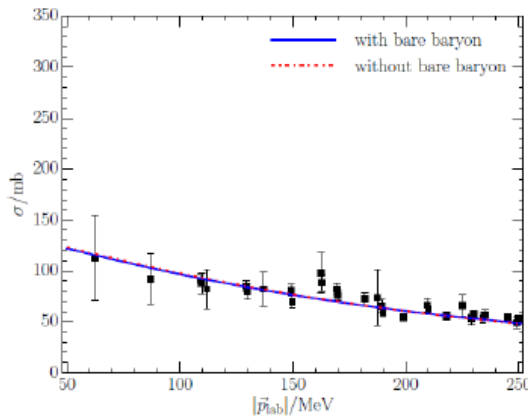
(Received 8 June 1984)

The cloudy bag model (CBM) is extended to incorporate chiral $SU(3) \times SU(3)$ symmetry, in order to describe *S*-wave KN and $\bar{K}N$ scattering. In spite of the large mass of the kaon, the model yields reasonable results once the physical masses of the mesons are used. We use that version of the CBM in which the mesons couple to the quarks with an axial-vector coupling throughout the bag volume. This version also has a meson-quark contact interaction with the same spin-flavor structure as the exchange of the octet of vector mesons. The present model strongly supports the contention that the $\Lambda^*(1405)$ is a $\bar{K}N$ bound state.

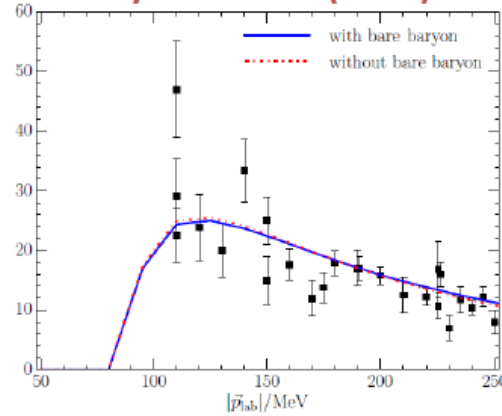
But now we can use QCD itself

Hamiltonian fit to existing data

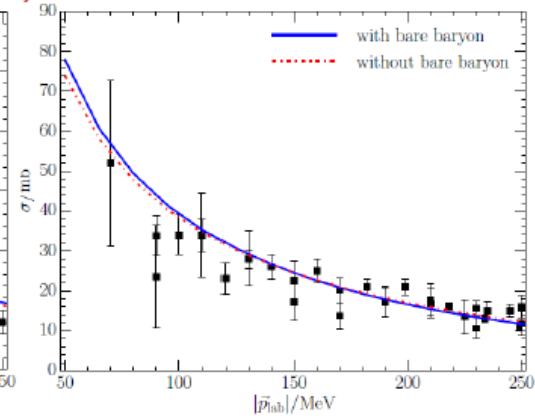
Zhan-wei Liu etc. Phys.Rev. D95 (2017) no.1, 014506



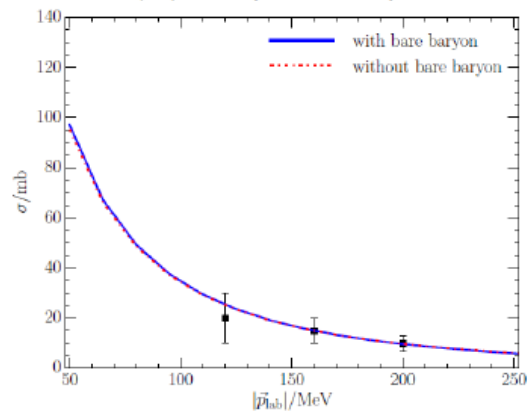
(a) $K^- p \rightarrow K^- p$



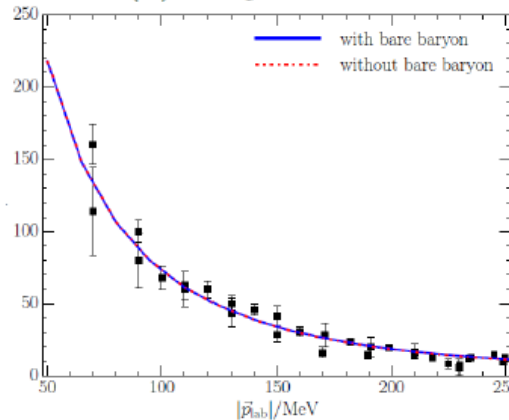
(b) $K^- p \rightarrow \bar{K}^0 n$



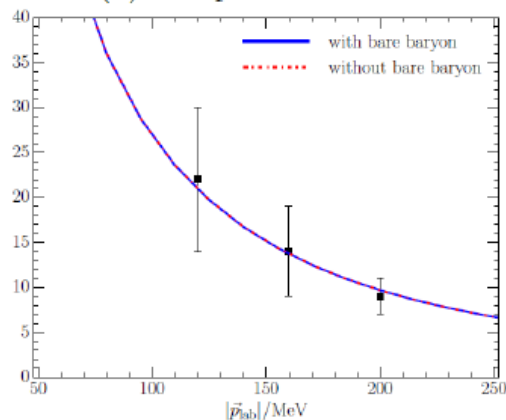
(c) $K^- p \rightarrow \pi^- \Sigma^+$



(d) $K^- p \rightarrow \pi^0 \Sigma^0$



(e) $K^- p \rightarrow \pi^+ \Sigma^-$



(f) $K^- p \rightarrow \pi^0 \Lambda$

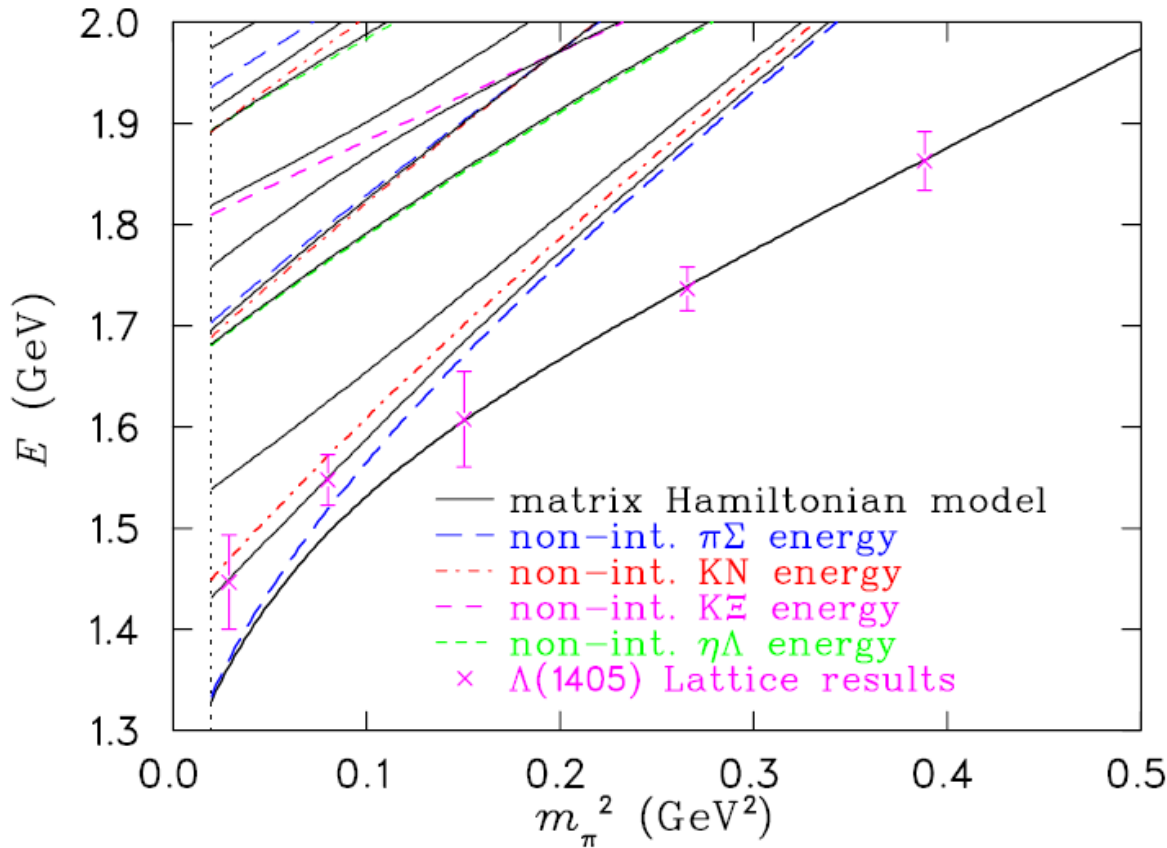
Include $\pi\Sigma$, $\bar{K}N$, $\eta\Lambda$ and $K\Xi$ channels

Similar work by Valencia, Bonn, JLab and other groups

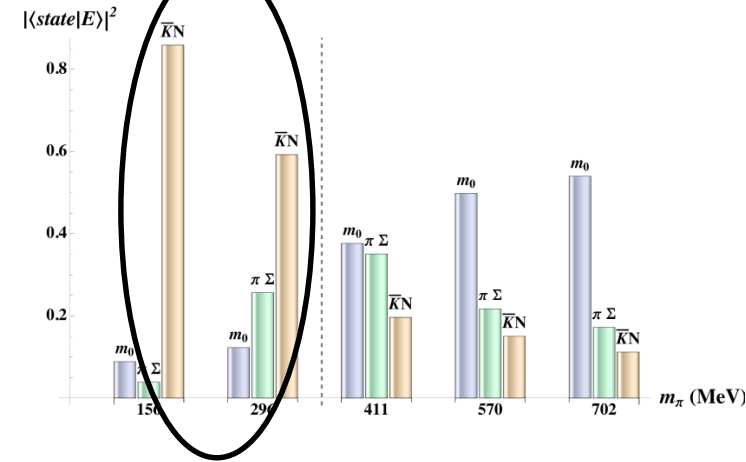
Find the same two-pole structure as other analyses

Low lying negative parity state : $\Lambda(1405)$

Clear evidence that it is a $\bar{K}N$ bound state



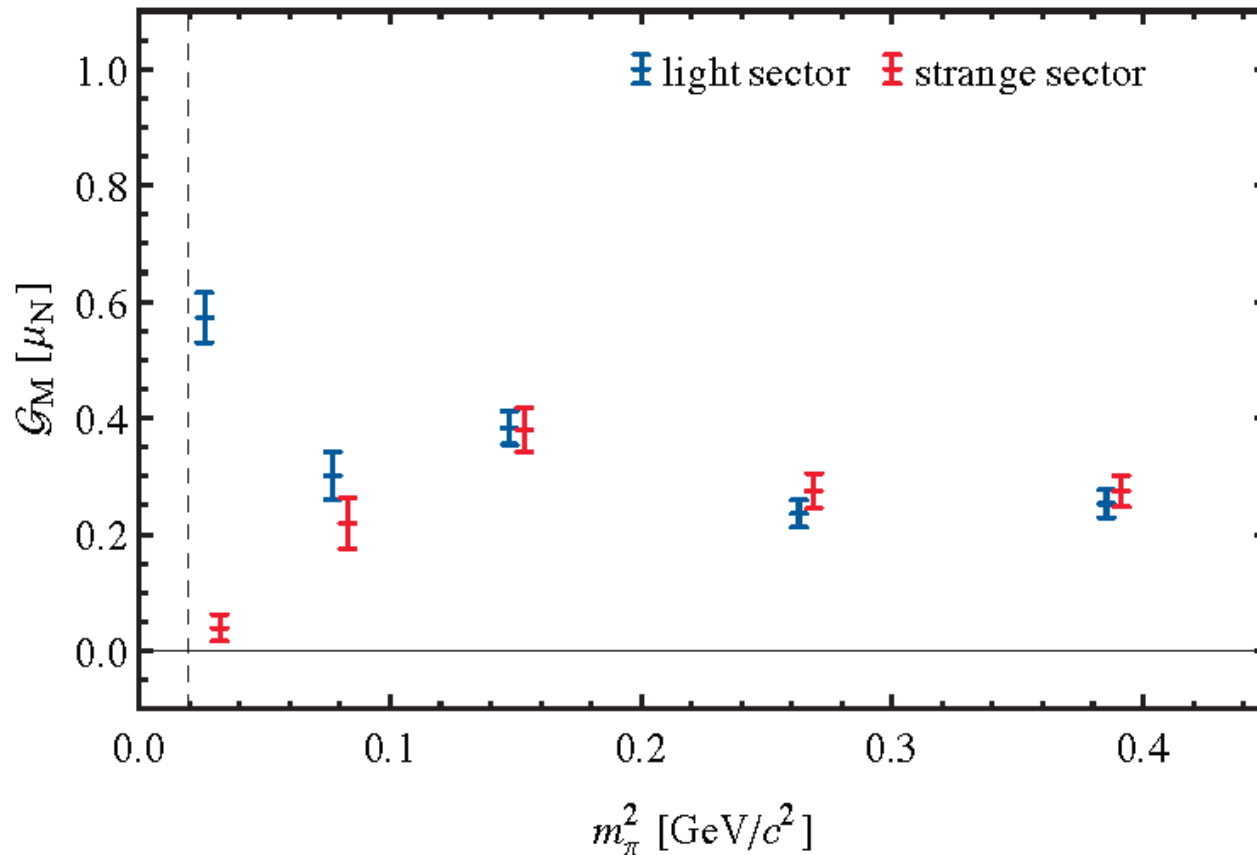
Hamiltonian approach allows one to examine the eigenstates:



Hall, Leinweber, Menadue, Young, AWT
 – Phys. Rev. Lett. 114 (2015) 13

Lattice Magnetic Form Factor Calculations

- Calculation of the individual quark contributions to the magnetic form factor confirms that it is a $K\bar{b}$ -N bound state



Only an $L=0$ $K\bar{b}$ -N state gives vanishing strange moment

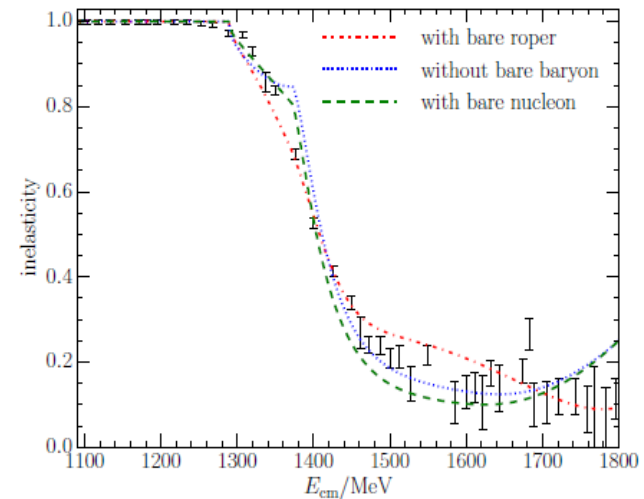
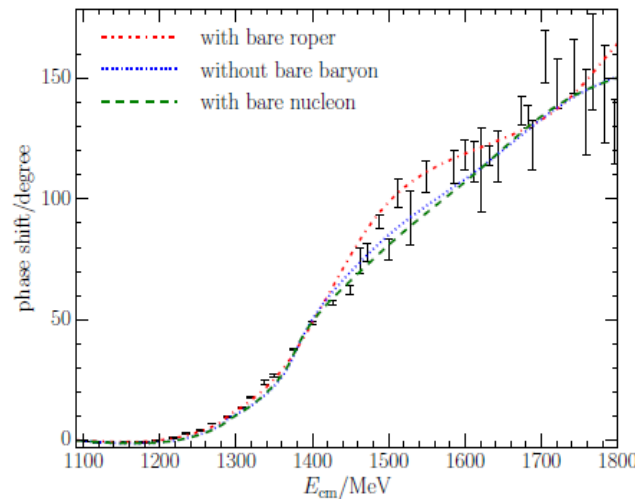
**Note that Lattice QCD allows
us to study hadron structure IN QCD as a
function of quark mass – a powerful tool***

Roper Resonance

Again this has long been a challenge for the quark model, as it is the 1st positive parity excited state and lies below the N(1535), the 1st negative parity state

Bare Roper Case: $m_0 = 2.03$ GeV

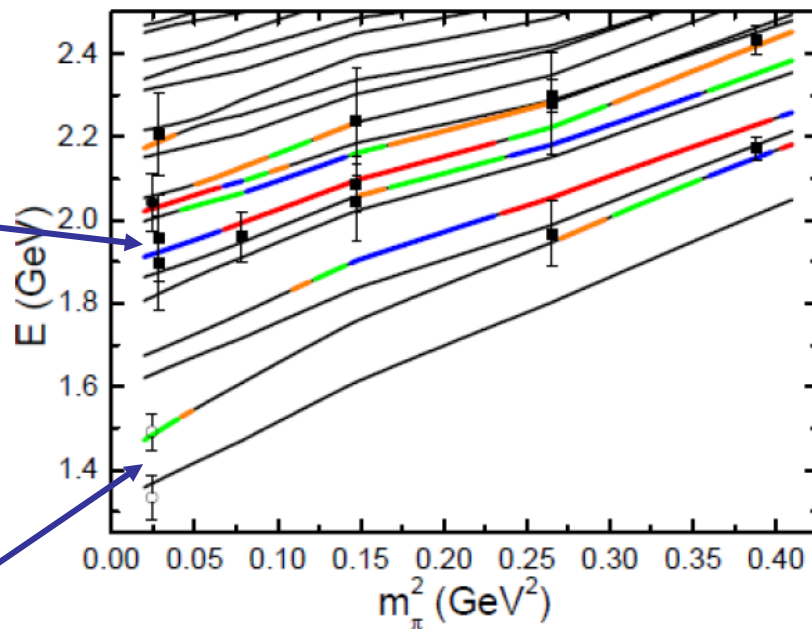
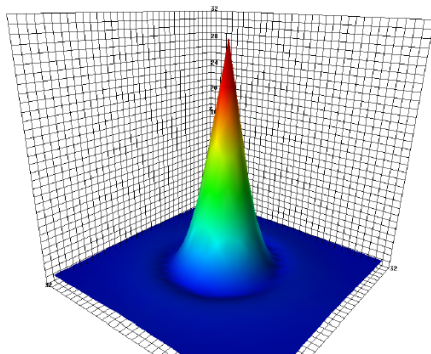
- Consider πN , $\pi\Delta$ and σN channels, dressing a bare state.
- Fit to phase shift and inelasticity



- Fit yields a pole at $1380 - i87$ MeV.
- Compare PDG estimate $1365 \pm 15 - i95 \pm 15$ MeV.

Comparison of HEFT Results with Lattice Energy Levels

- Blue indicates high “bare state” (i.e. 3-quark) content. This matches the lowest state found with a 3-quark interpolating field and looks like a 2s state

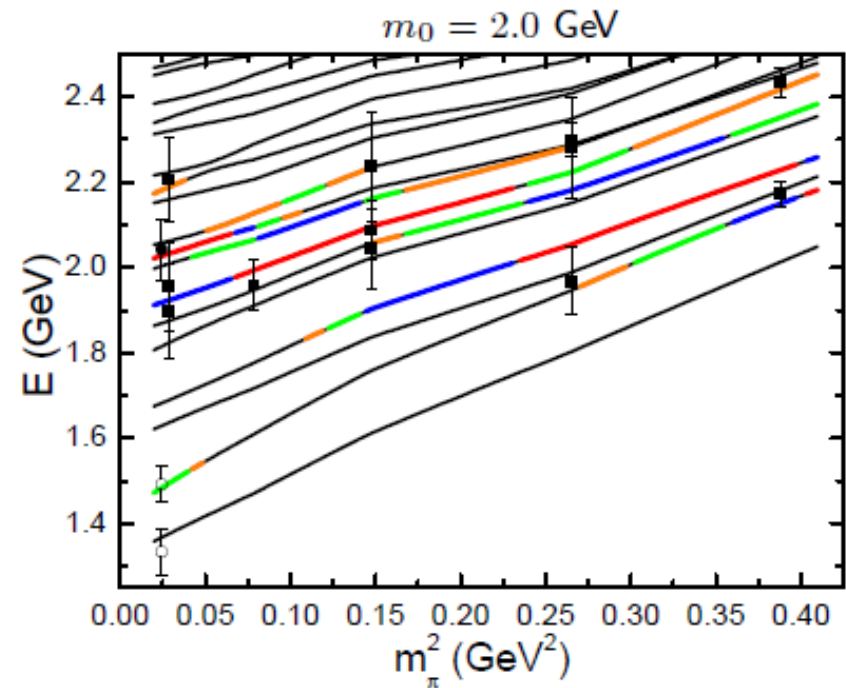
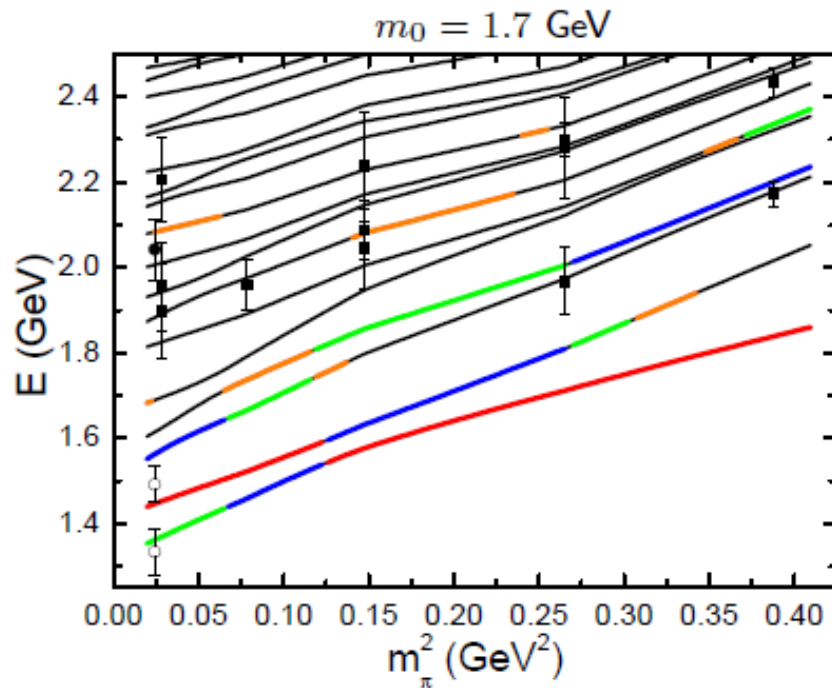


- Lattice calculations of Lang et al., Phys. Rev. D 95, 014510 (2017), using baryon-meson interpolating fields, especially $N\sigma$
- Matched by Hamiltonian levels but with little or no 3-quark content

The first scenario with a bare state for P11 around the pole at 2.0 GeV can fit both Lattice data and experimental data well, it indicates that $N^*(1440)$ seems a molecule state, and first radial excitation of nucleon should be around 2.0 GeV.

To emphasise the point

Two different descriptions of the Roper resonance



(left) Meson dressings of a quark-model like core.

(right) Resonance generated by strong rescattering in meson-baryon channels.

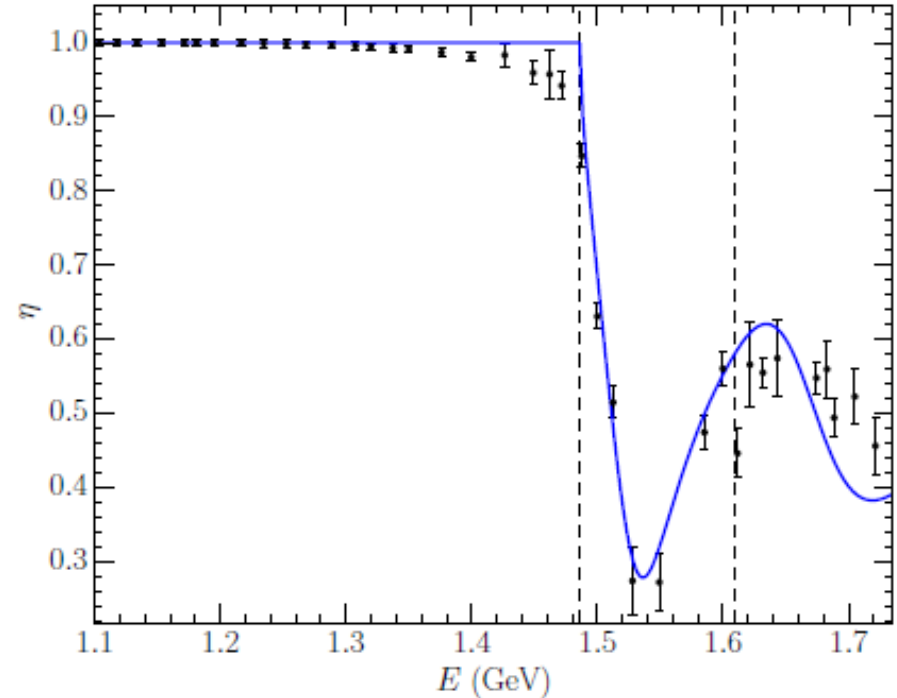
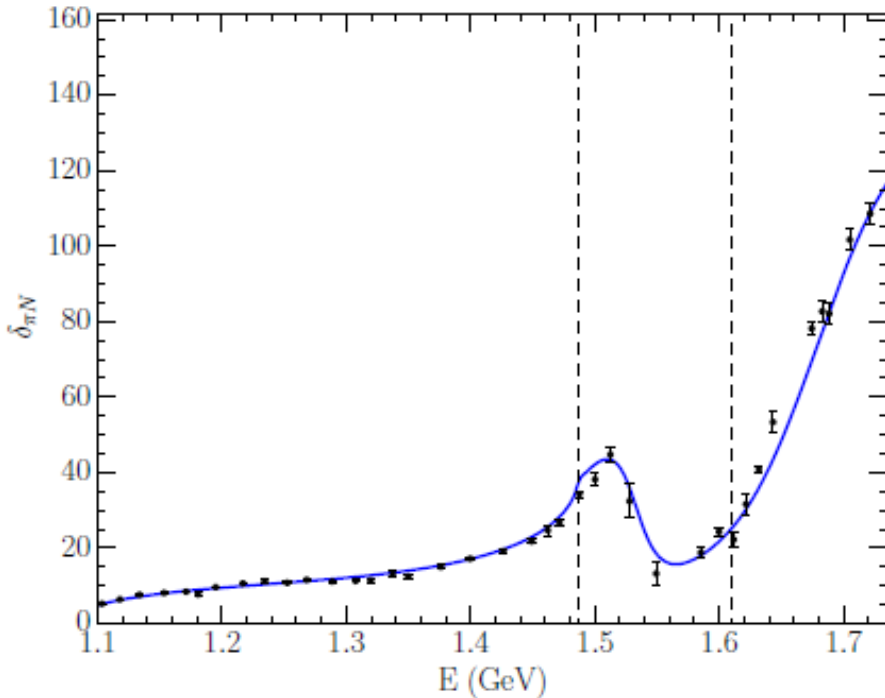
**Clear conclusion is that the Roper is
dynamically generated by coupling
to the $N\sigma$ and $\Delta\pi$ channels**

Are all states like this?

NO: The $N(1535)$ is a 3-quark state

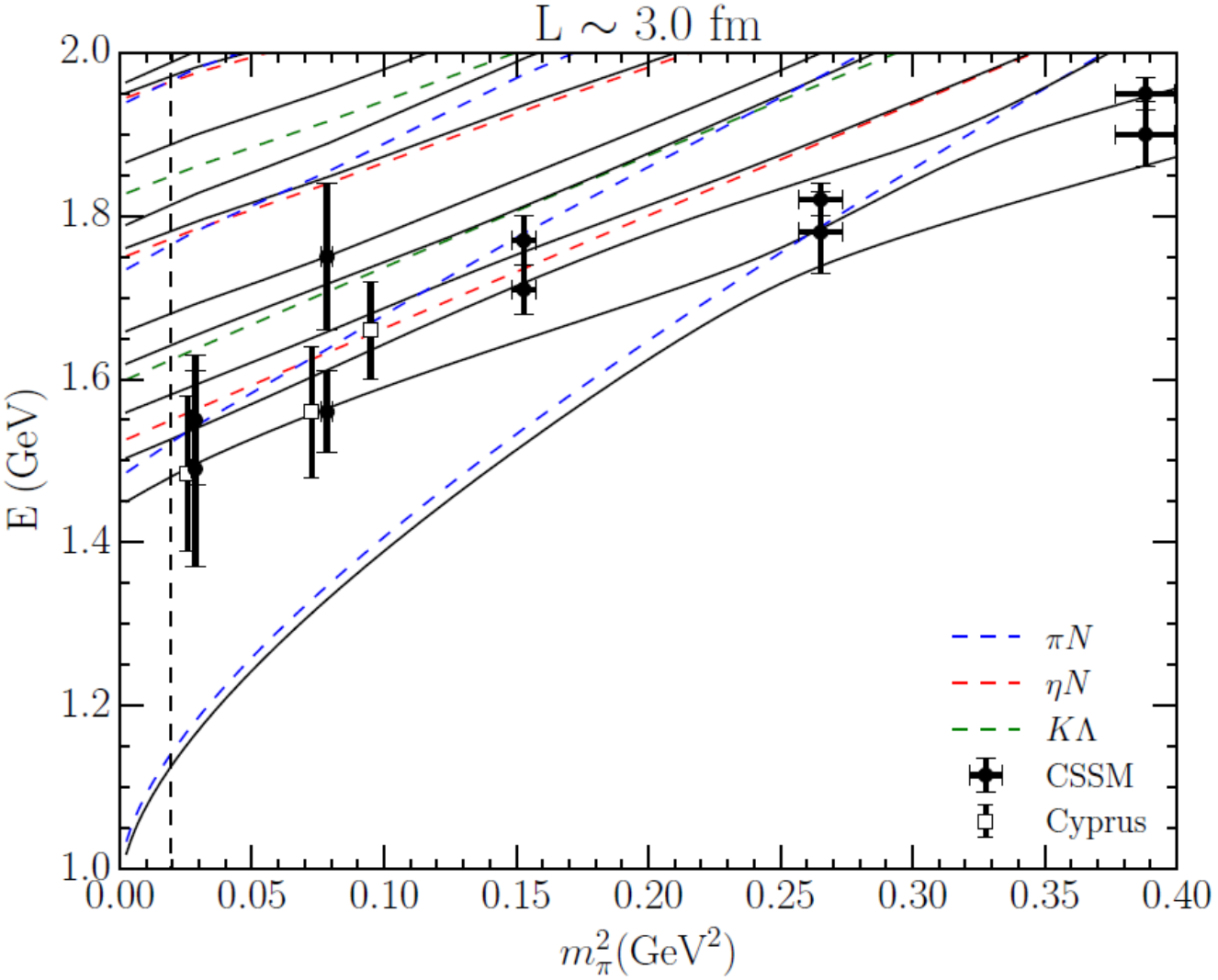
First construct a Hamiltonian to accurately describe experimental data

Pole at $1531 \pm 29 - i 88 \pm 2$ MeV



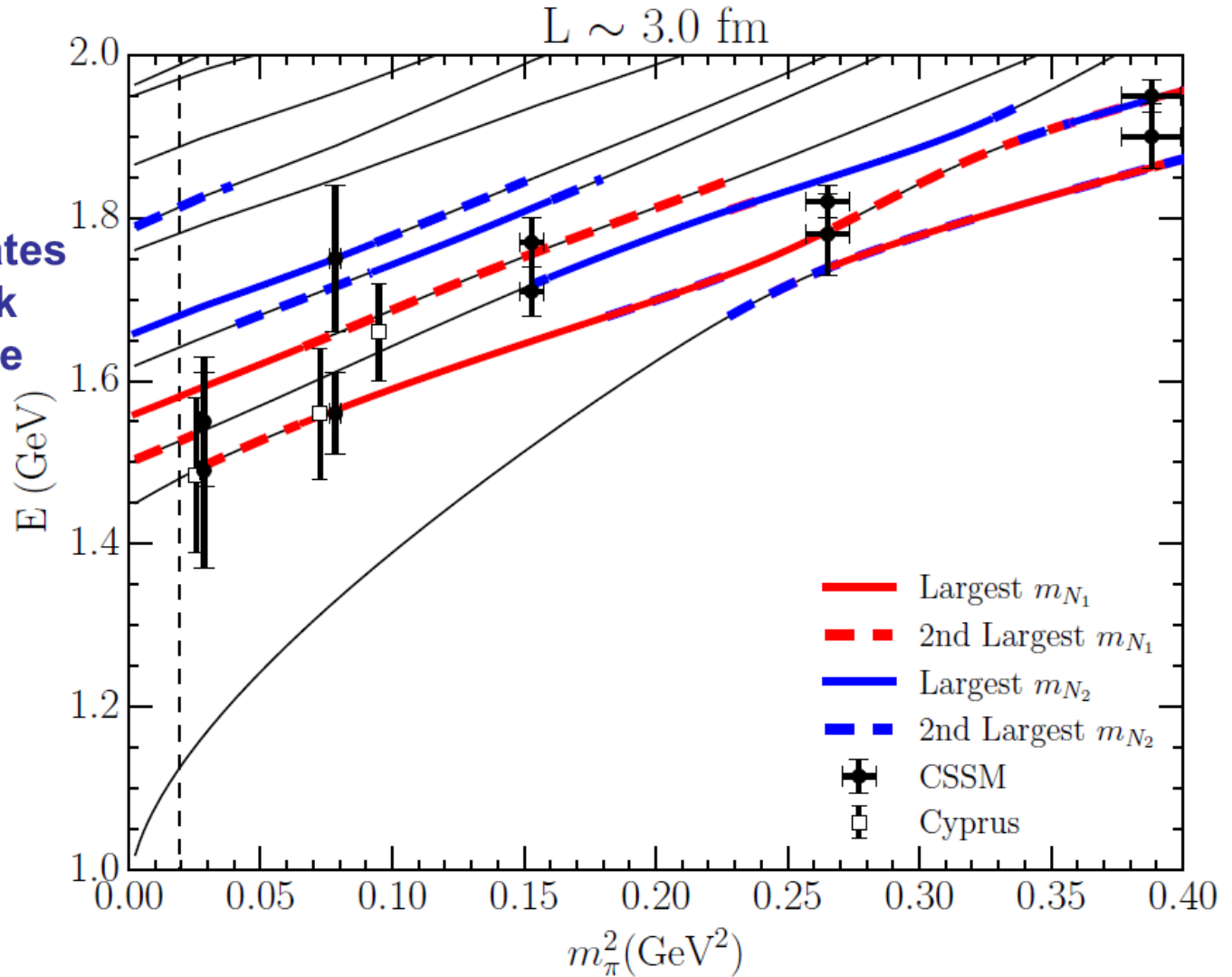
- WI08 single-energy data from SAID.
- Vertical lines indicate the opening of the ηN and $K \Lambda$ thresholds.

Finite volume predictions based on this Hamiltonian



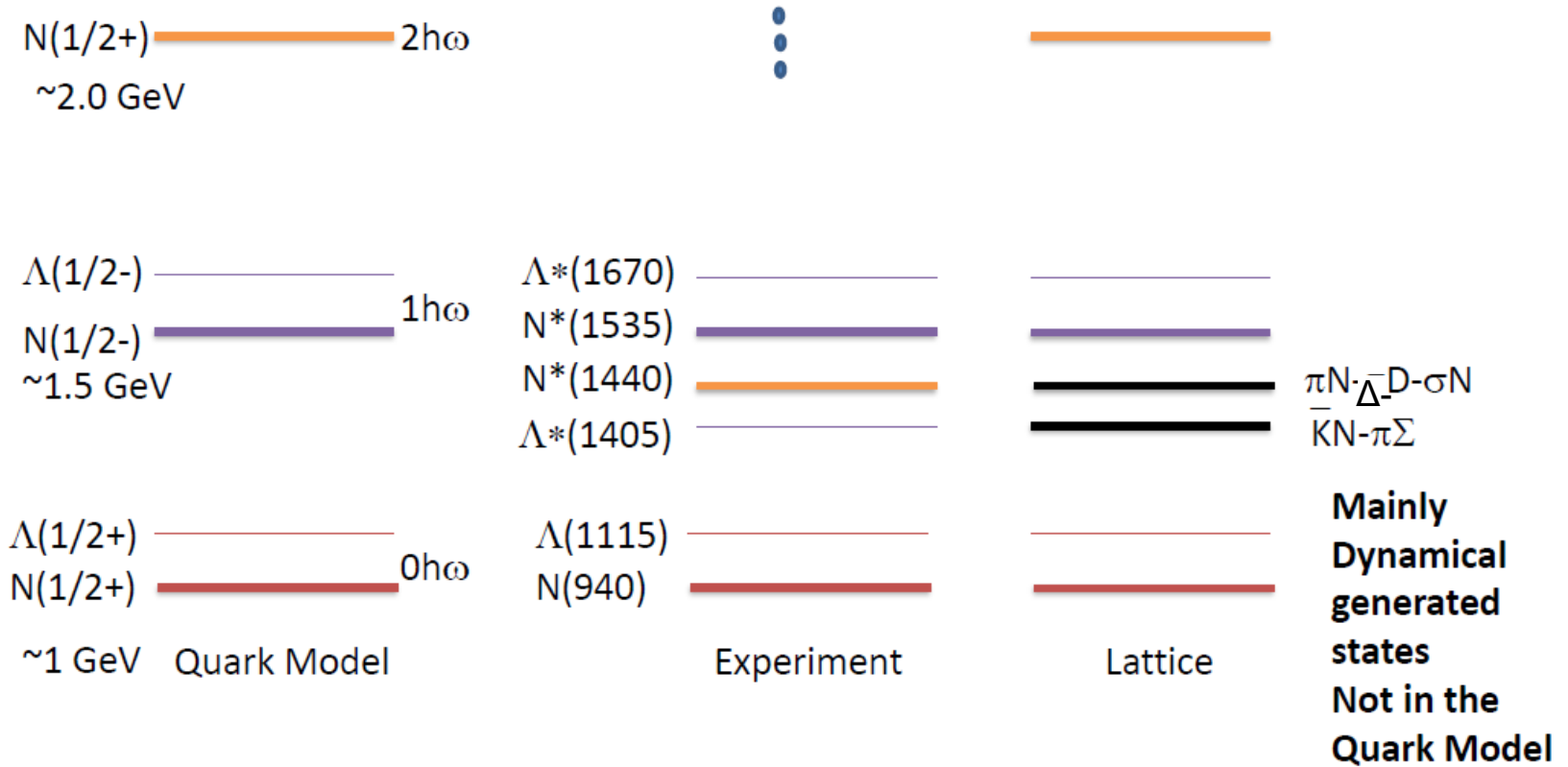
Analysis of eigenstates

Hamiltonian eigenstates dominated by 3-quark state match the lattice result with 3-quark interpolating field



Liu *et al.*, PRL 116 (2016) 082004

Once the nature of key states becomes clear the quark model makes sense



Wu, Leinweber et al., Physical Review D97, 094509 (2018)

Summary

- **New techniques applied to lattice QCD provide hitherto unimagined insights into hadron structure**
- **Neither the $\Lambda(1405)$ nor the Roper are predominantly three-quark states**
- **The quark model has new life with ordering of major shells as expected**
- **These insights may well resolve “missing state” problem**



Acknowledgements: Derek Leinweber, Zhan-Wei Liu, Jon Hall, Curtis Abell, Jiajun Wu, Waseem Kamleh, Liam Hockley

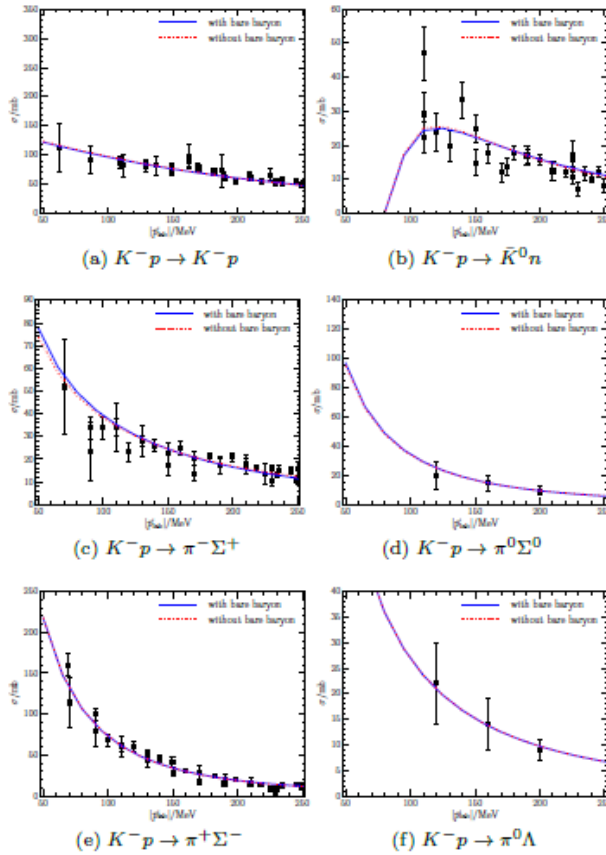


FIG. 1: Experimental data and our fits to the cross sections of K^-p . The solid lines are for our scenario with a bare-baryon component included in the $I = 0$ channel, and the dashed lines represent the results without a bare-baryon component. The experimental data are from Refs. [41–48].

indicate that the $\Lambda(1405)$ contains little of the bare baryon component at infinite volume.

TABLE I: Parameters constrained in our fits to cross sections of K^-p and the pole positions obtained with these fit parameters in our two scenarios: one in which the $\Lambda(1405)$ is dynamically generated purely from the $\pi\Sigma$, $\bar{K}N$, $\eta\Lambda$ and $K\Xi$ interactions (No $|B_0\rangle$), and one also including a bare-baryon basis state to accommodate a three-quark configuration carrying the quantum numbers of the $\Lambda(1405)$ (With $|B_0\rangle$). The underlined entries indicate they are fixed in performing the fit.

Coupling	No $ B_0\rangle$	With $ B_0\rangle$
$g_{\pi\Sigma,\pi\Sigma}^0$	-1.77	-1.59
$g_{\bar{K}N,\bar{K}N}^0$	-2.14	-1.78
$g_{\bar{K}N,\pi\Sigma}^0$	0.78	0.89
$g_{\bar{K}N,\eta\Lambda}^0$	-0.42	-0.97
$g_{\pi\Sigma,K\Xi}^0$	-0.24	-0.56
$g_{\eta\Lambda,K\Xi}^0$	0.42	0.97
$g_{K\Xi,K\Xi}^0$	-0.60	-1.37
$g_{\pi\Sigma,B_0}^0$	-	0.13
$g_{\bar{K}N,B_0}^0$	-	0.16
$g_{\eta\Lambda}^0$	-	-0.18
$g_{K\Xi}^0$	-	-0.09
m_B^0/MeV	-	1740
$g_{\pi\Sigma,\pi\Sigma}^1$	-0.14	<u>-0.14</u>
$g_{\bar{K}N,\bar{K}N}^1$	-0.06	<u>-0.06</u>
$g_{\bar{K}N,\pi\Sigma}^1$	1.36	<u>1.36</u>
$g_{\bar{K}N,\pi\Lambda}^1$	0.96	<u>0.96</u>
χ^2 (120 data)	166	177
pole 1 (MeV)	1428 - 23 i	1429 - 22 i
pole 2 (MeV)	1333 - 85 i	1338 - 89 i