

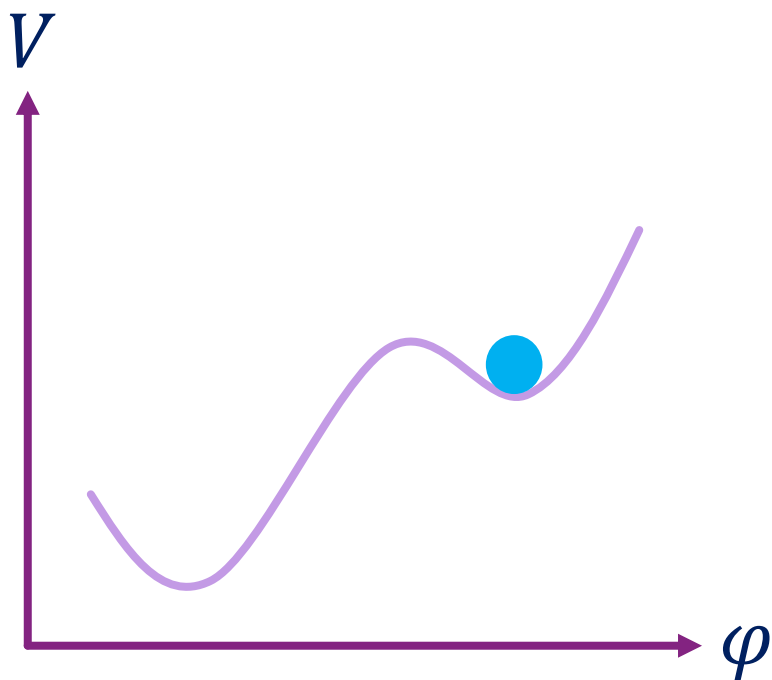
A COLD ATOM ANALOGUE FOR VACUUM DECAY IN THE EARLY UNIVERSE

KATE BROWN

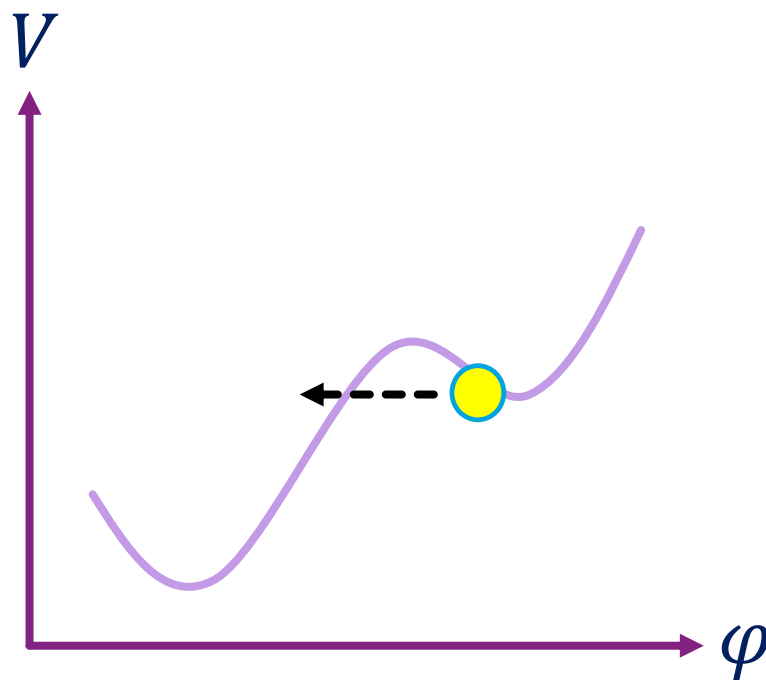
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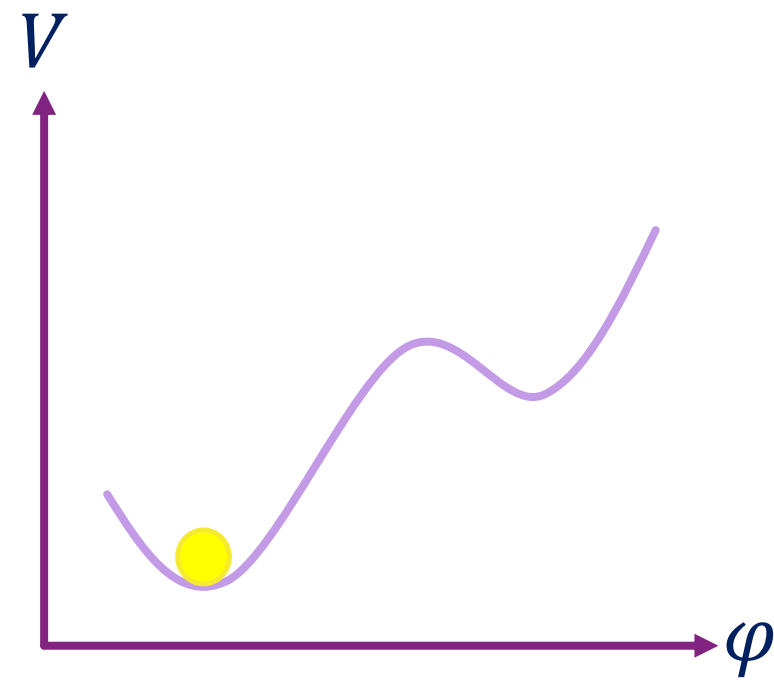
VACUUM DECAY



False Vacuum State
(Metastable)

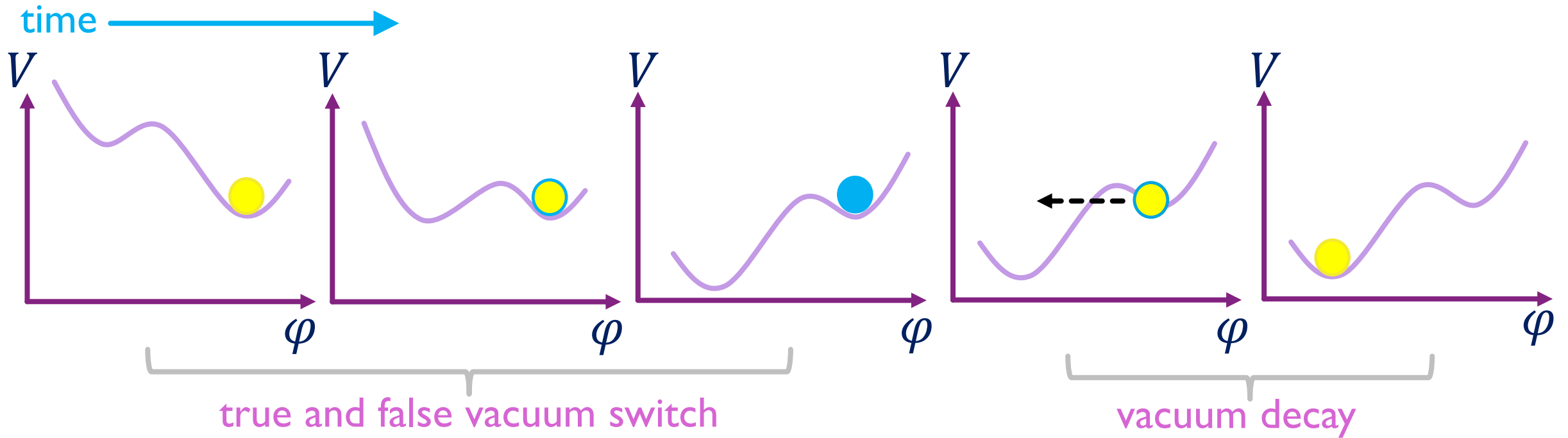


Quantum Tunnelling



True Vacuum State
(Stable)

VACUUM DECAY – EARLY UNIVERSE



Interesting applications: gravitational waves, baryon asymmetry, black holes

COLD ATOM ANALOGUE SYSTEM

- We use two components:

$$\psi_0 = \sqrt{n_0}e^{i\theta_0}, \quad \psi_1 = \sqrt{n_1}e^{i\theta_1}$$

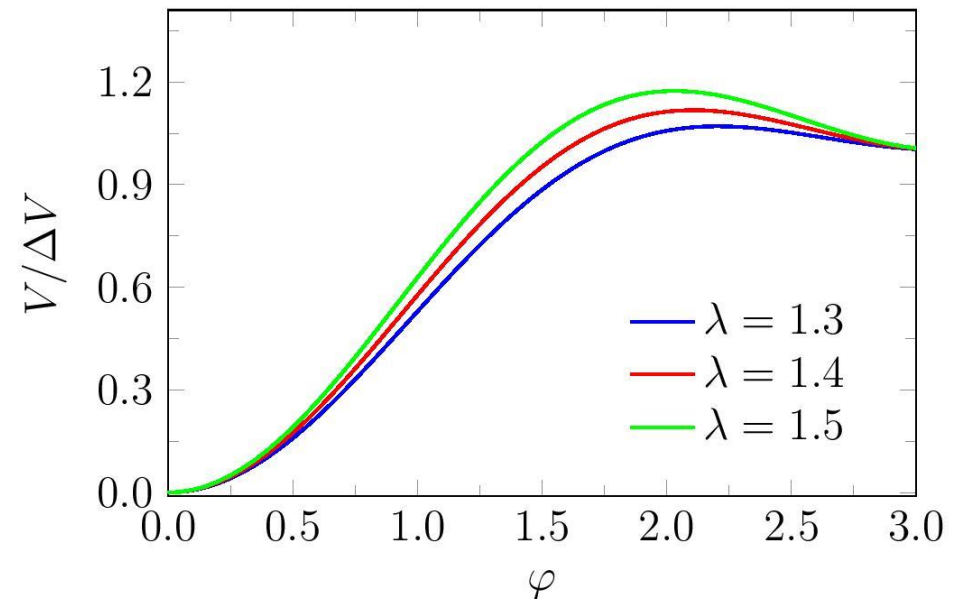
- with phase difference:

$$\varphi = \theta_0 - \theta_1$$

- and interaction potential:

$$V(\varphi) = -2\epsilon^2 - 2\epsilon^2 \cos(\varphi) + \epsilon^2 \lambda^2 \sin^2(\varphi)$$

- $\varphi = 0$ is stable (true vacuum)
- $\varphi = \pi$ is metastable (false vacuum)



NUMERICAL MODEL

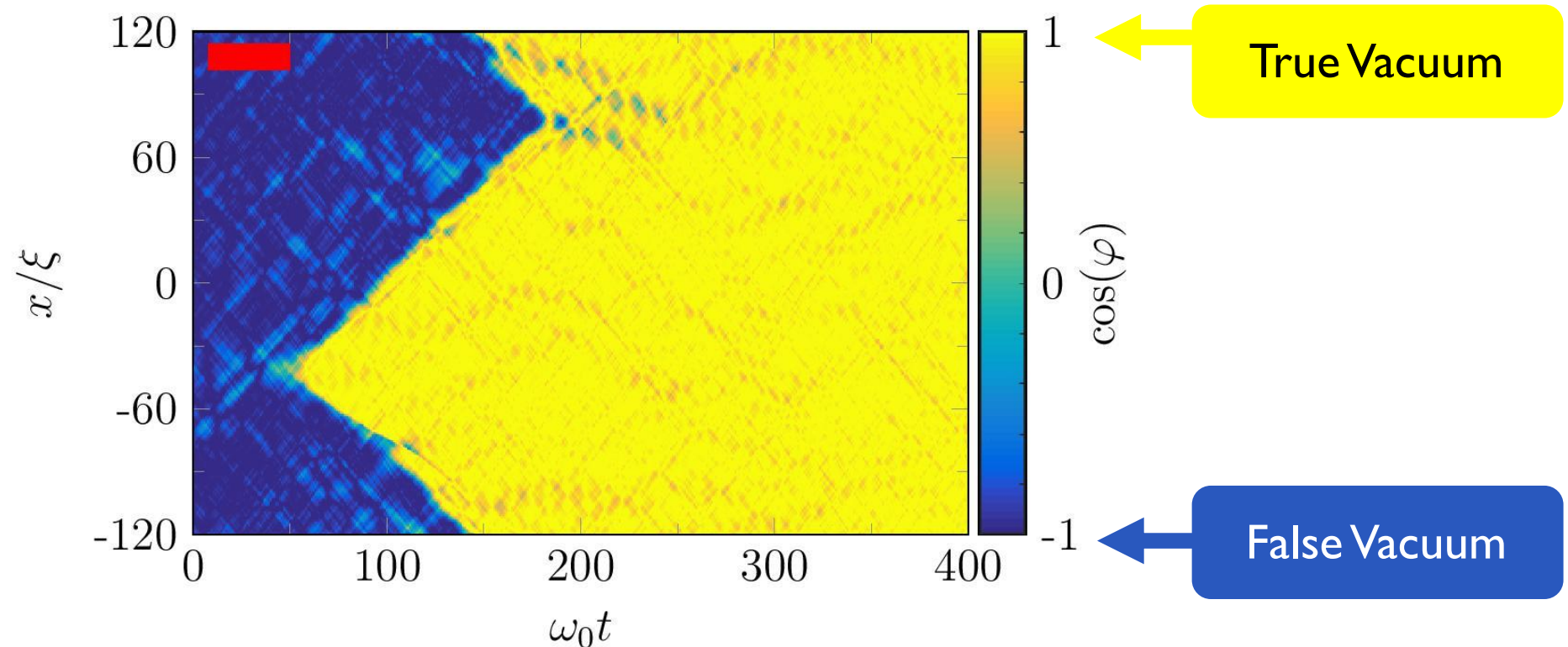
- We use a coupled pair of stochastic Gross-Pitaevskii equations (SGPE):

$$i\partial_t\psi_j = (1 - i\gamma) \left\{ -\frac{1}{2}\nabla^2\psi_j + \frac{\partial V}{\partial\psi_j^*} \right\} + \eta_j, \quad j = 0, 1$$

- γ : Damping
- η : Random fluctuations, $\langle \eta_i(x, t)\eta_j(x', t') \rangle = 2\gamma T\delta(x - x')\delta(t - t')\delta_{ij}$
- System: 1D box with periodic boundaries

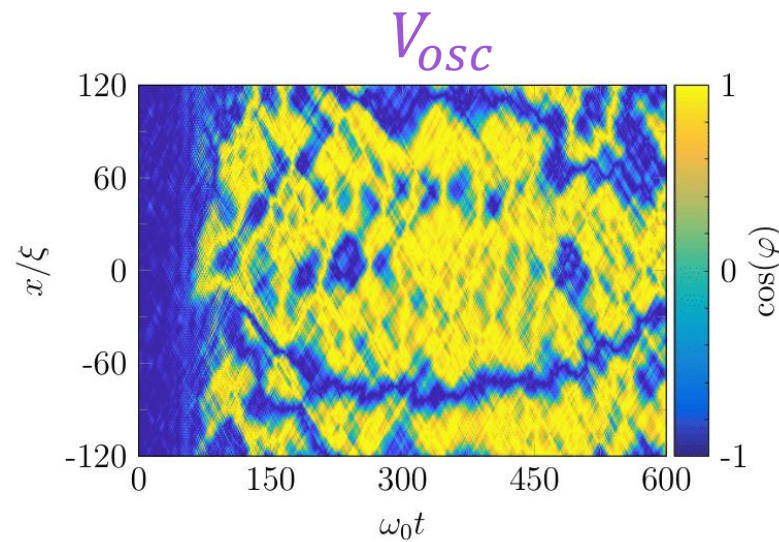
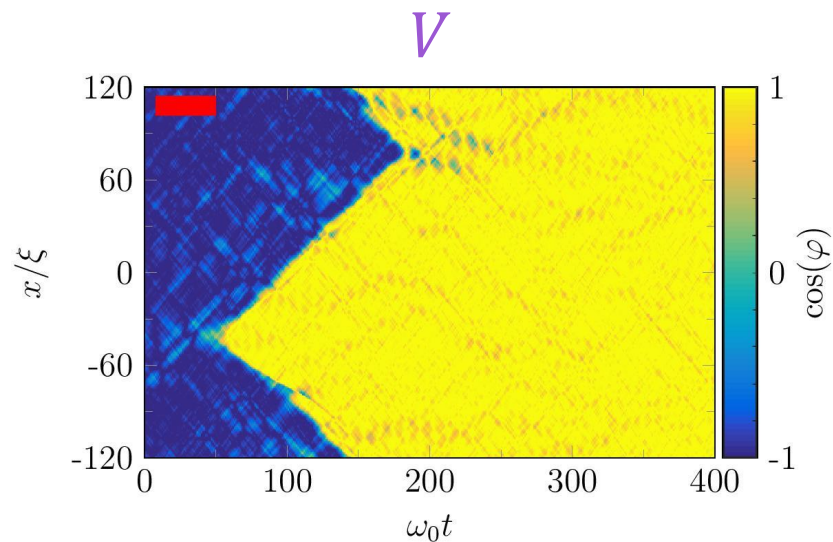
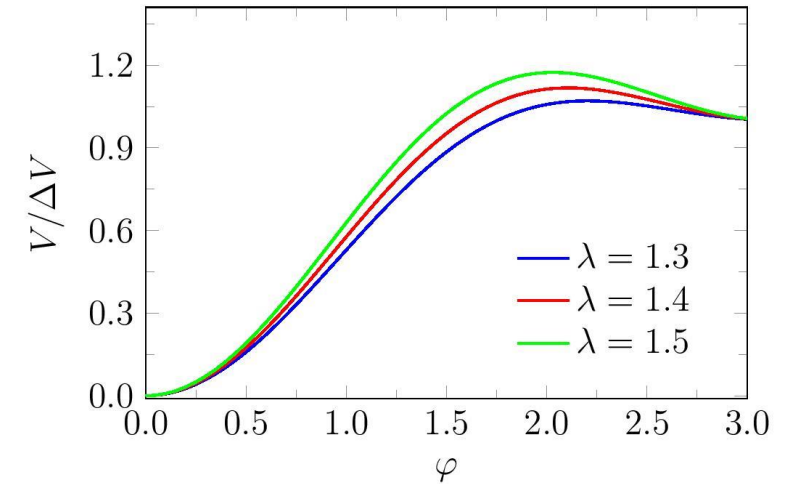
OBSERVING BUBBLES

- Protocol: initialise in the metastable state:
- System transitions from “false vacuum” to “true vacuum” via bubble growth



STATIC POTENTIAL VS OSCILLATORY POTENTIAL

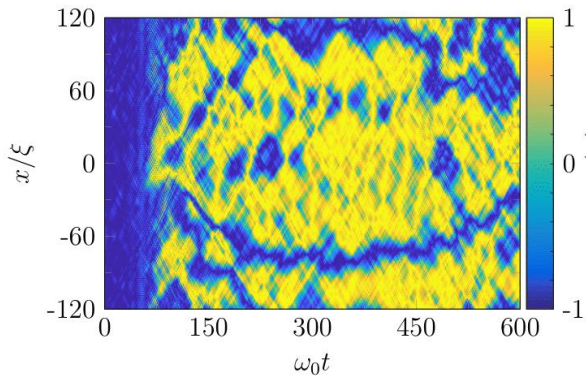
- The interaction potential, $V(\varphi)$, is static
- It's engineered from an oscillating potential, $V_{osc}(\varphi, t)$
- Instabilities can occur for V_{osc} :



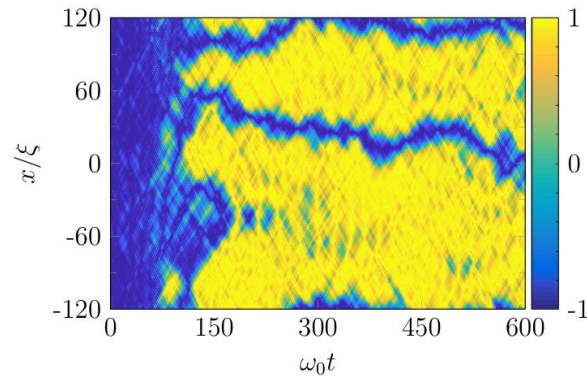
STATIC POTENTIAL VS OSCILLATORY POTENTIAL

$$\text{SGPE: } i\partial_t\psi_j = (1 - i\gamma) \left\{ -\frac{1}{2}\nabla^2\psi_j + \frac{\partial V}{\partial\psi_j^*} \right\} + \eta_j$$

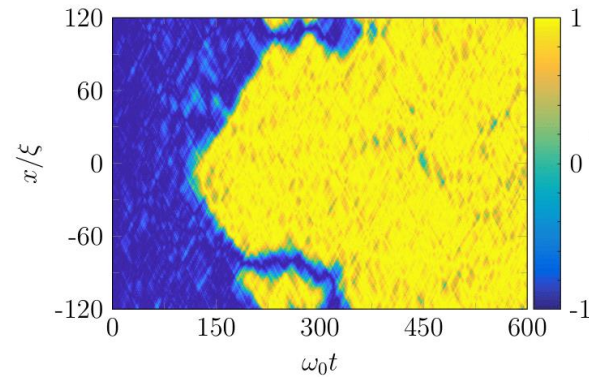
- Instabilities can be damped out by raising γ :



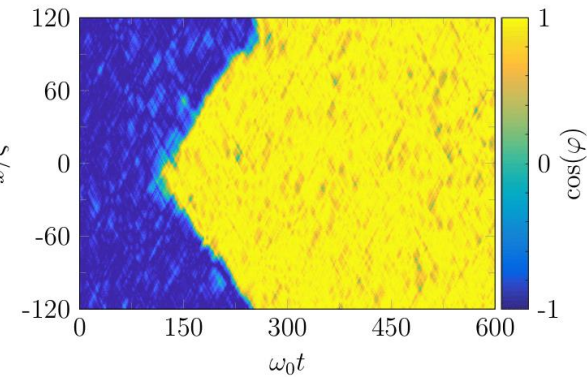
$\gamma = 0.005$



$\gamma = 0.01$



$\gamma = 0.02$



$\gamma = 0.03$

CONCLUSION

- Qualitative agreement can be reached between V & V_{osc}
- For proof of quantitative agreement (and references), see arxiv [2006.09820](#) & [2104.07428](#)

Thank you!