

# Correlation between $v_n$ and $p_T$ in Pb+Pb and Xe+Xe collisions with ATLAS

ATLAS-CONF-2021-001

**Arabinda Behera**

For the ATLAS Collaboration

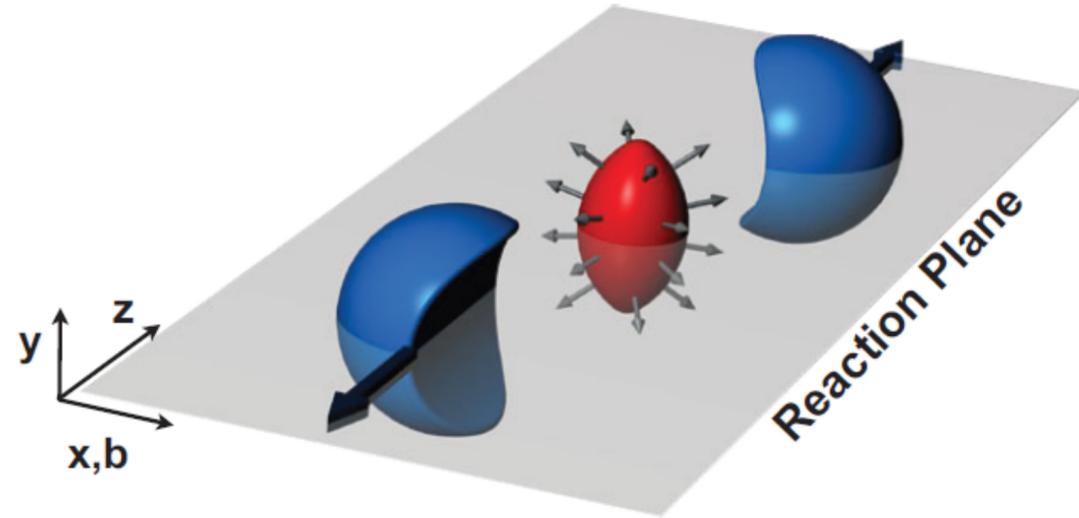
12th January, 2021

Poster by  
Somadutta Bhatta,  
Tuesday 12th

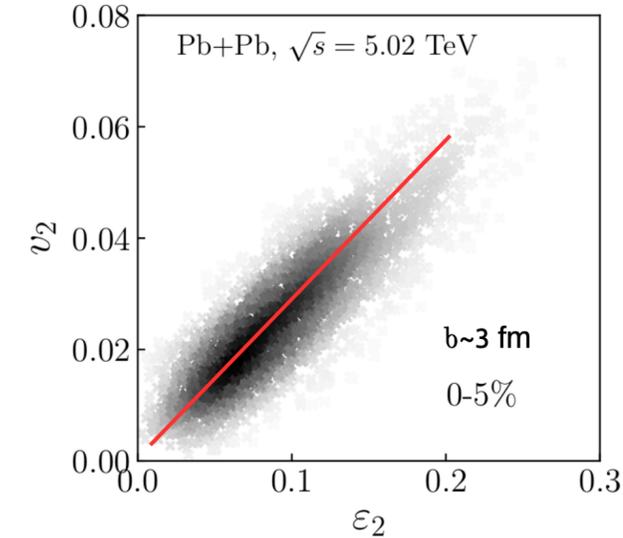
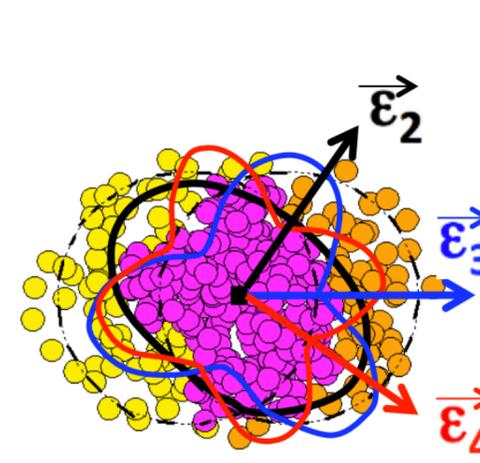


# $v_n$ - $[p_T]$ Correlation

- In HIC - collision overlap has shape and size

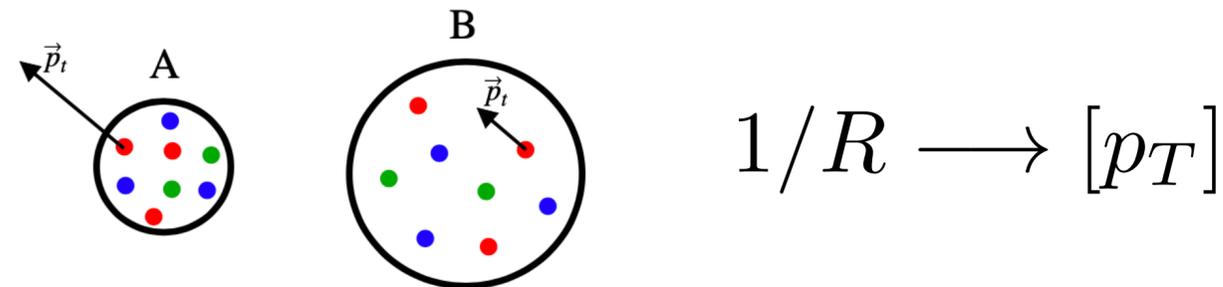


- Shape  $\longrightarrow$  anisotropic flow



$$v_n \propto \epsilon_n$$

- Size  $\longrightarrow$  radial flow - avg. momentum

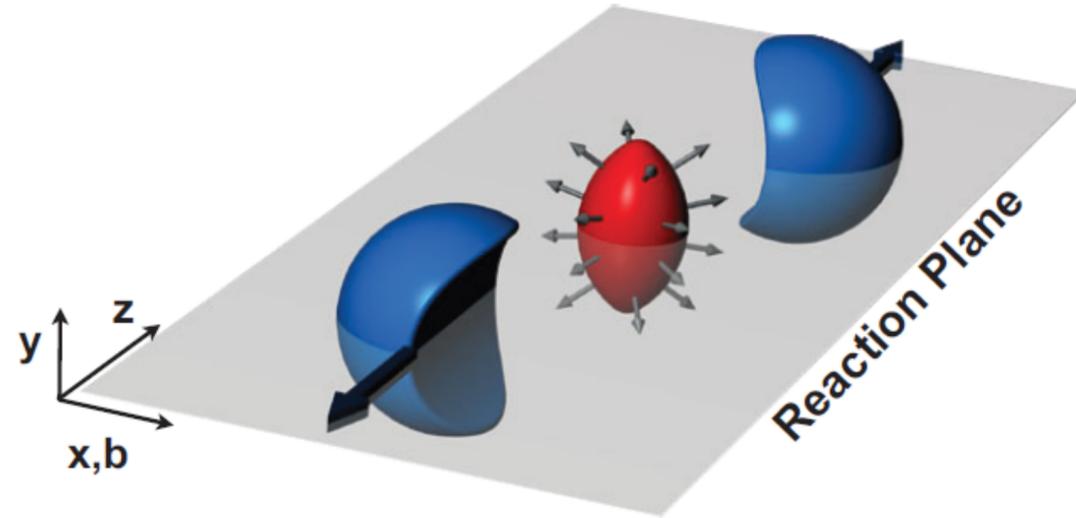


$$\begin{array}{|c|} \hline S_A = S_B \\ R_A < R_B \\ \hline \end{array} \implies T_A > T_B \implies \langle p_t \rangle_A > \langle p_t \rangle_B$$

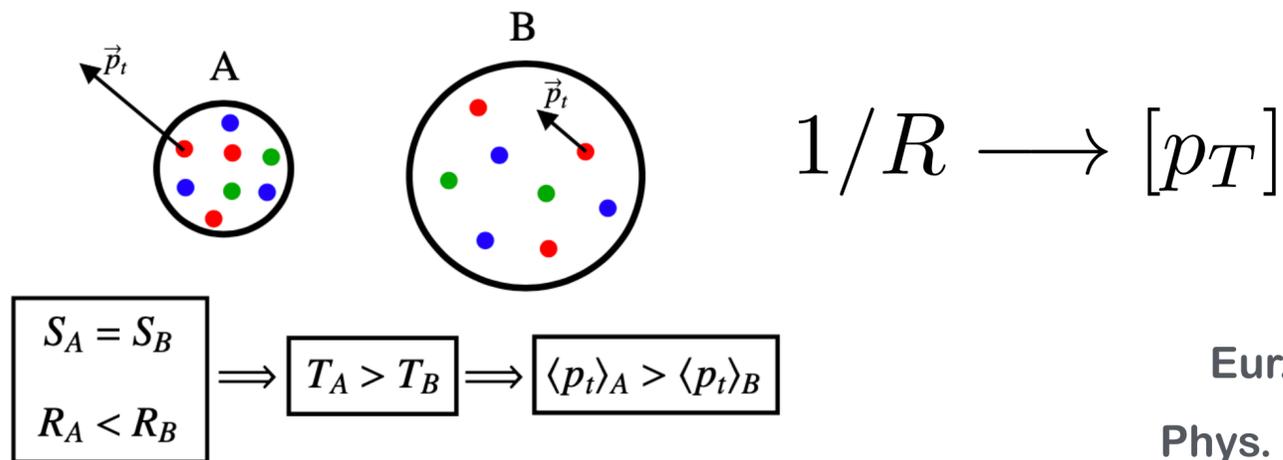
- Initial State - correlation and fluctuations of shape and size
- Final State - correlation between  $v_n$  and  $[p_T]$

# $v_n - [p_T]$ Correlation

- In HIC - collision overlap has shape and size



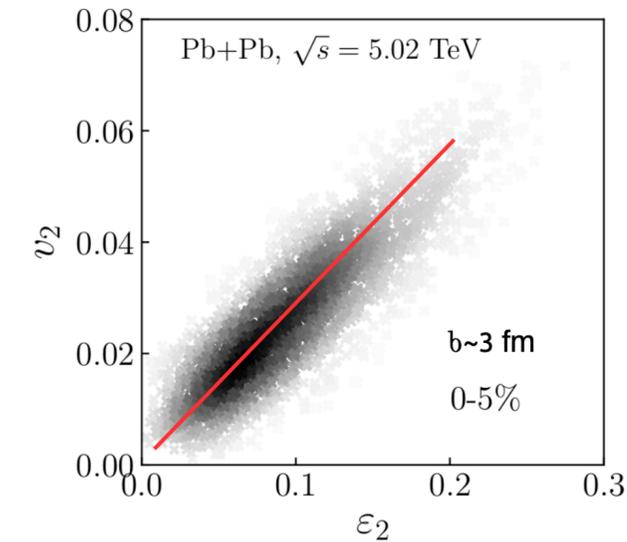
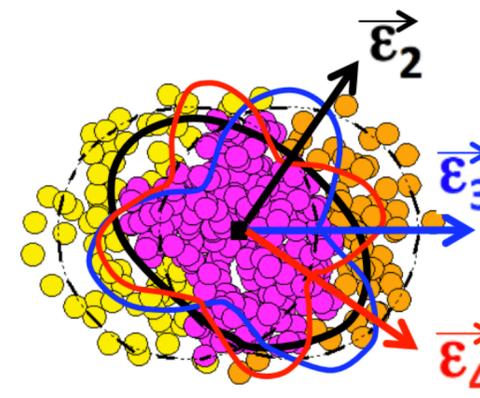
- Size  $\rightarrow$  radial flow - avg. momentum



Eur. Phys. J. C 79 (2019) 985  
Phys. Rev. C 102, 034905 (2020)

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- Final State - correlation between  $v_n$  and  $[p_T]$

- Shape  $\rightarrow$  anisotropic flow

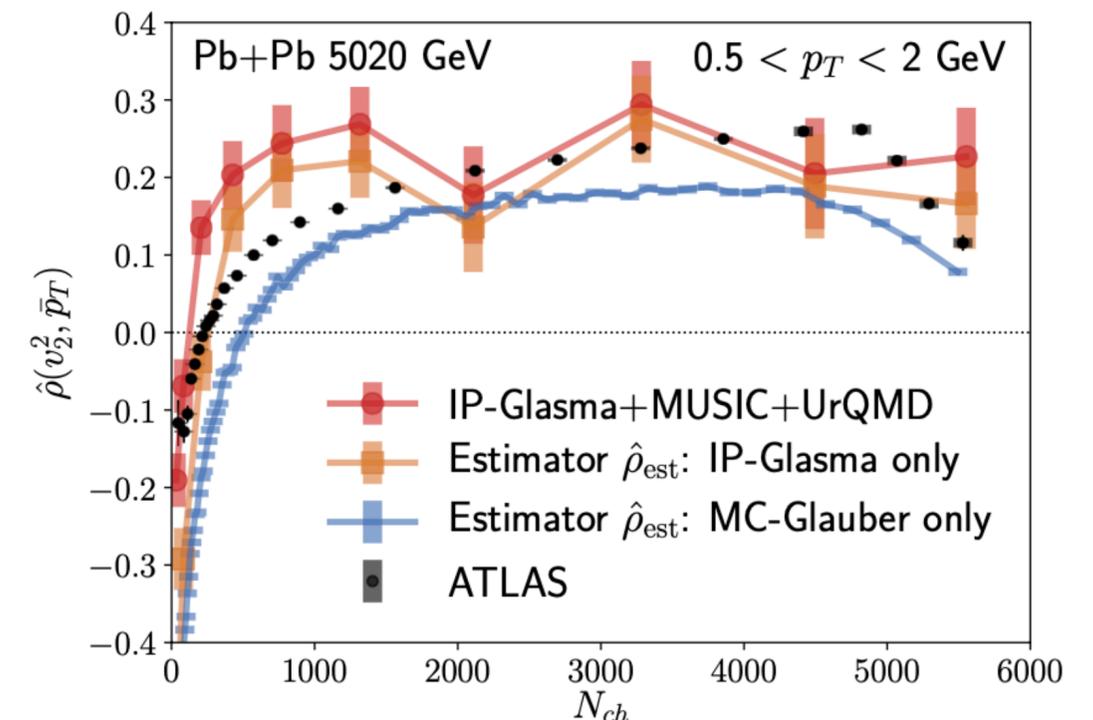


arXiv:2101.00168

$$v_n \propto \epsilon_n$$

- Pearson's correlation coefficient

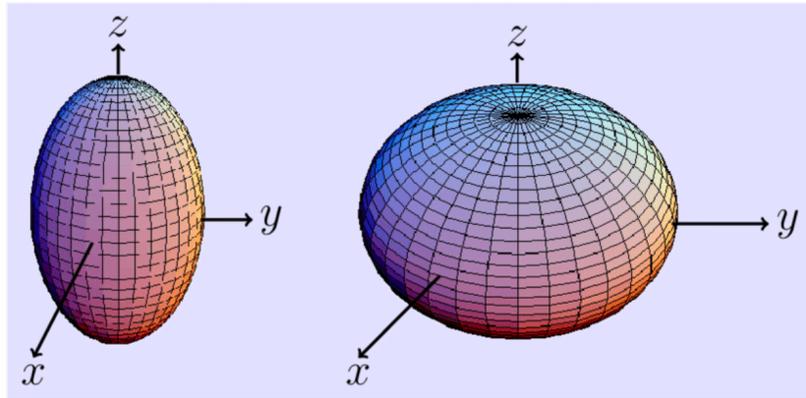
$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{var}(v_n^2)} \sqrt{\text{var}([p_T])}}$$



# $v_n - [p_T]$ Correlation

- Nuclear deformation

$$D_{WS}(r) = \frac{D_0}{1 + e^{(r - R_0(1 + \beta Y_{20}))/a}}$$



$\beta > 0$  Prolate

$\beta < 0$  Oblate

— LHC - Pb+Pb ( $\beta \approx 0$ ), Xe+Xe ( $\beta \approx 0.16$ )

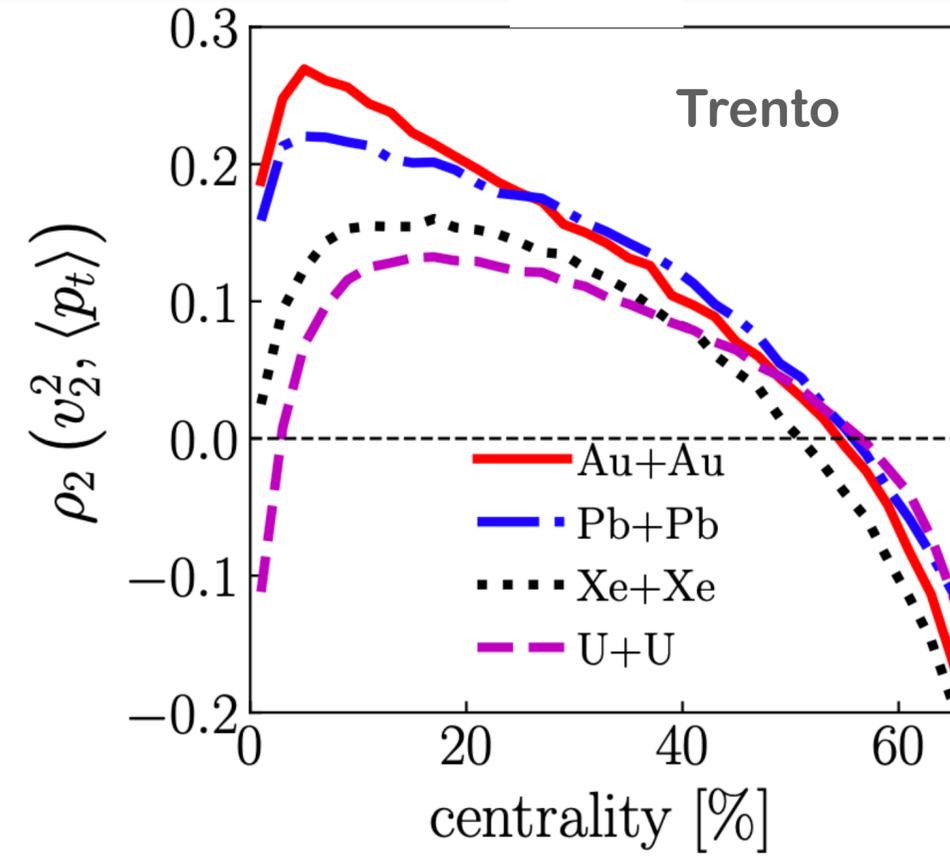
- Trento results

— Smaller  $\rho_2$  in Xe+Xe than Pb+Pb

— Deformation lowers  $\rho_2$  in the central region

Phys. Rev. C 102, 024901 (2020)

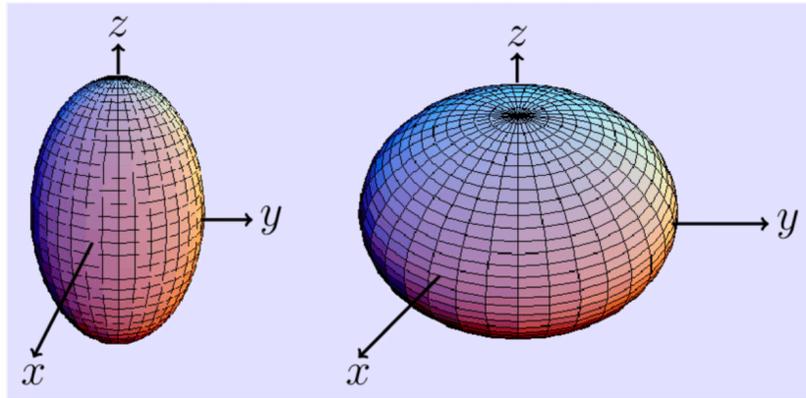
G. Giacalone



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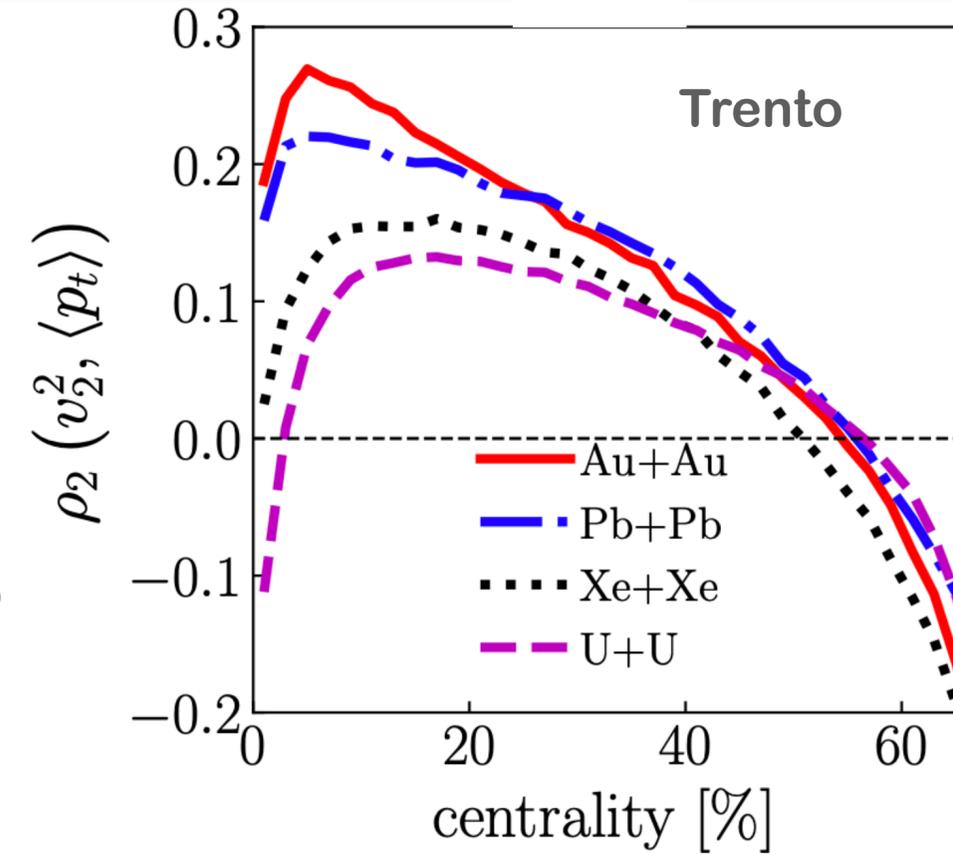
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Phys. Rev. C 102, 024901 (2020)

G. Giacalone



- Centrality fluctuations

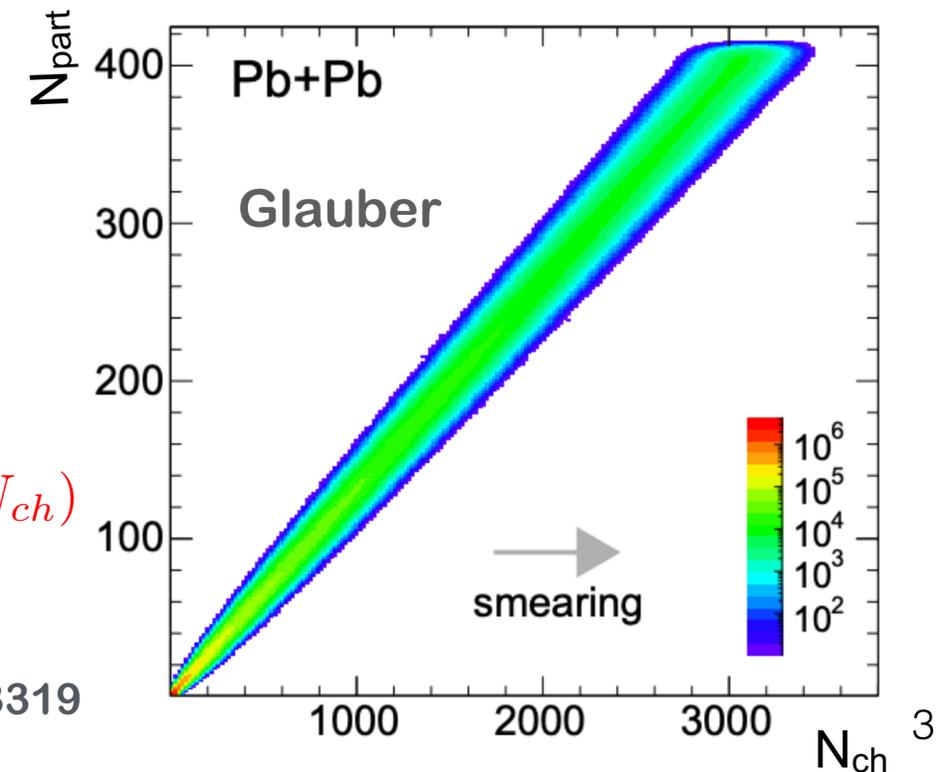
— Smearing between  $N_{part}$  and  $N_{ch}$

Same  $N_{part}$  - different  $N_{ch}$

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$$p(Obs. | N_{ch}) = \sum_{cent} p(Obs. | cent) \otimes p(cent | N_{ch})$$

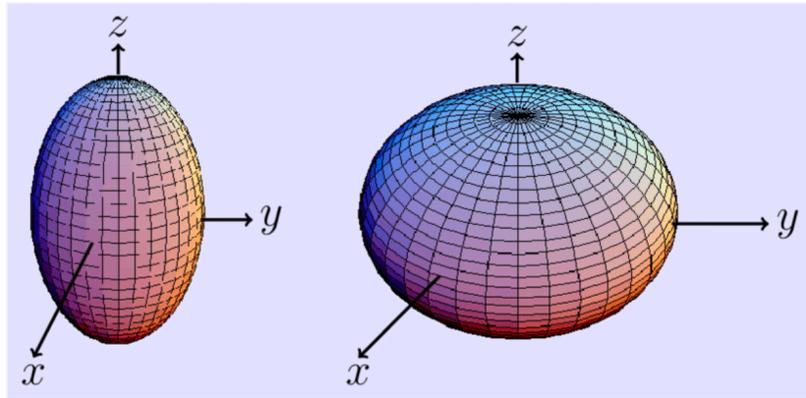
Phys. Rev. Research 2, 023319 (2020)



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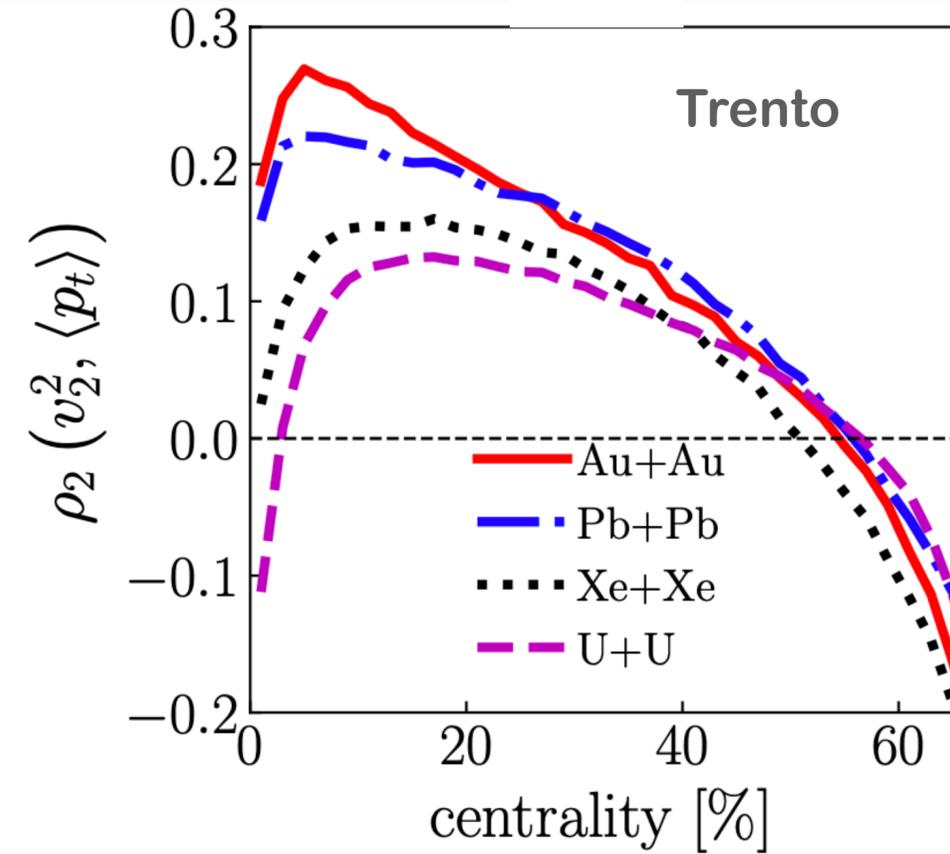
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Phys. Rev. C 102, 024901 (2020)

G. Giacalone



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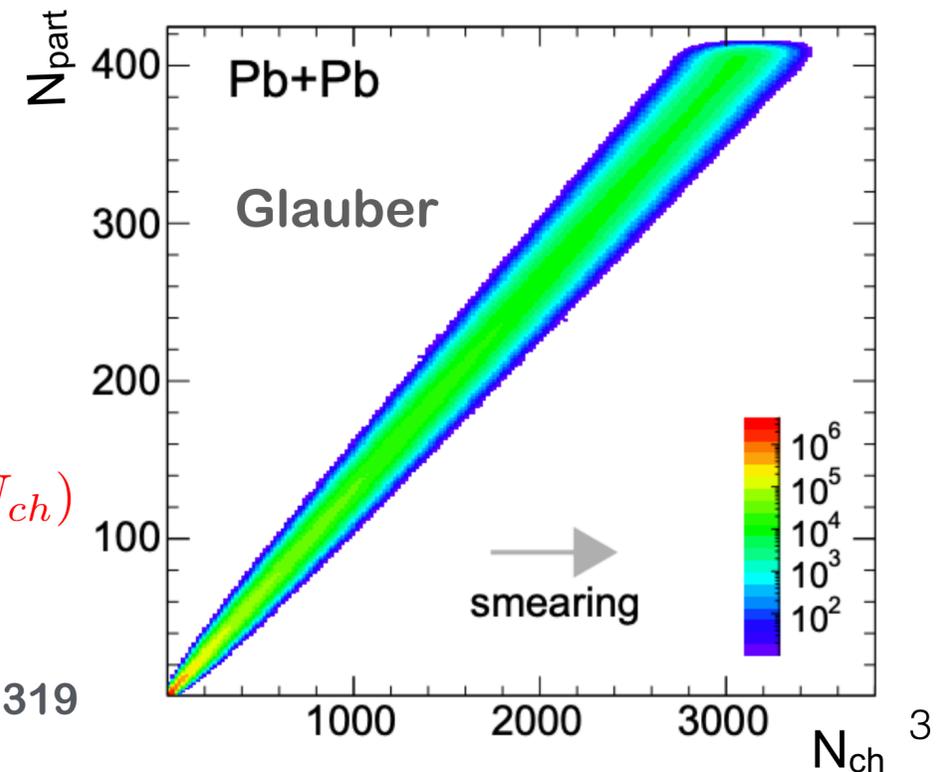
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Phys. Rev. Research 2, 023319 (2020)



## $v_n - [p_T]$ Correlation - Pb+Pb vs Xe+Xe

- System-size dependence
- Centrality fluctuation
- Deformation effects

# Observable

- Pearson's Correlation Coefficient

$$cov(v_n^2, [p_T]) = \langle\langle e^{in(\phi_i - \phi_j)} (p_{T,k} - \langle [p_T] \rangle) \rangle\rangle_{ev}$$

Phys. Rev. C 93, 044908 (2016)

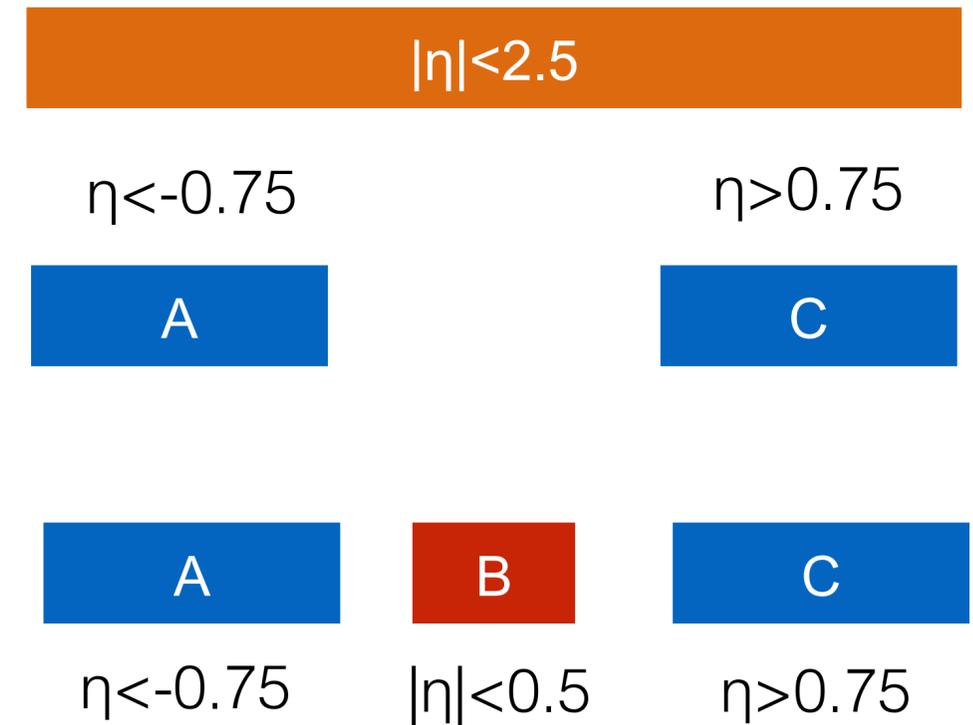
$$\rho(v_n^2, [p_T]) = \frac{cov(v_n^2, [p_T])}{\sqrt{var(v_n^2)} \sqrt{c_k}}$$

$$\begin{aligned} var(v_n^2) &= v_n\{2\}^4 - v_n\{4\}^4 \\ &= \langle\langle e^{in(\phi_i + \phi_k - \phi_j - \phi_l)} \rangle\rangle_{ev} - \langle\langle e^{in(\phi_i - \phi_j)} \rangle\rangle_{ev}^2 \end{aligned}$$

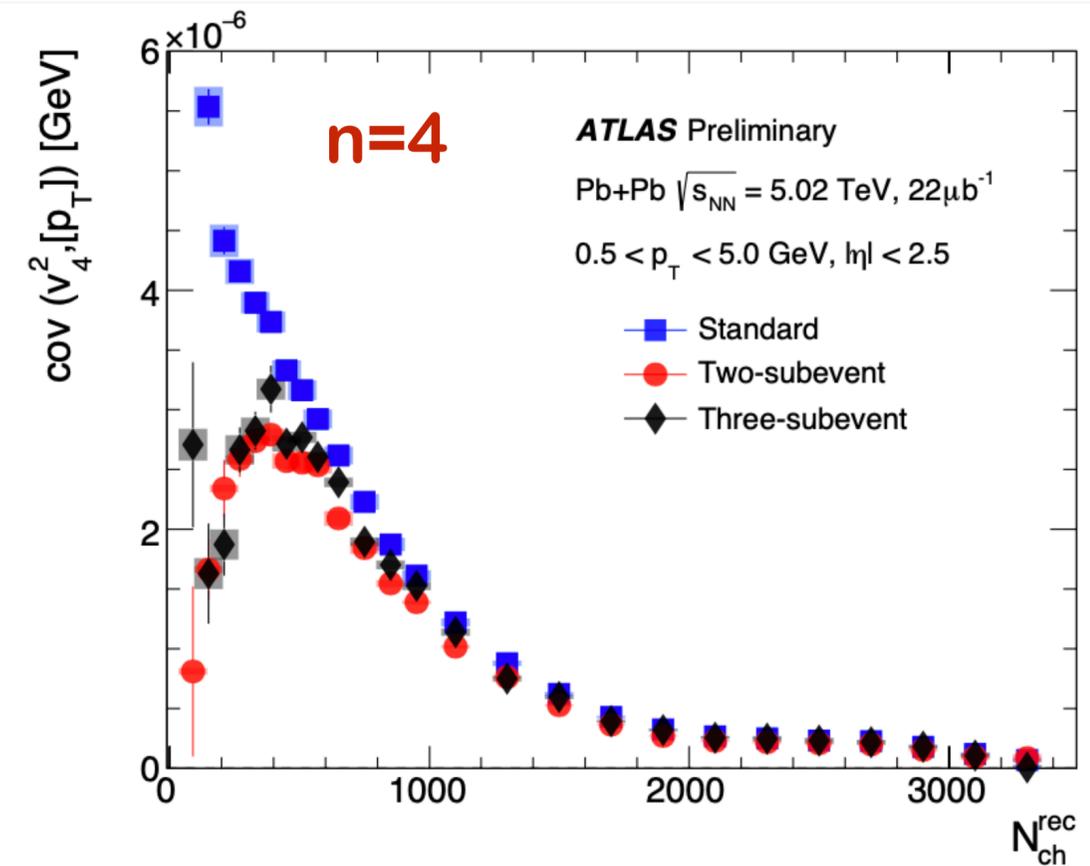
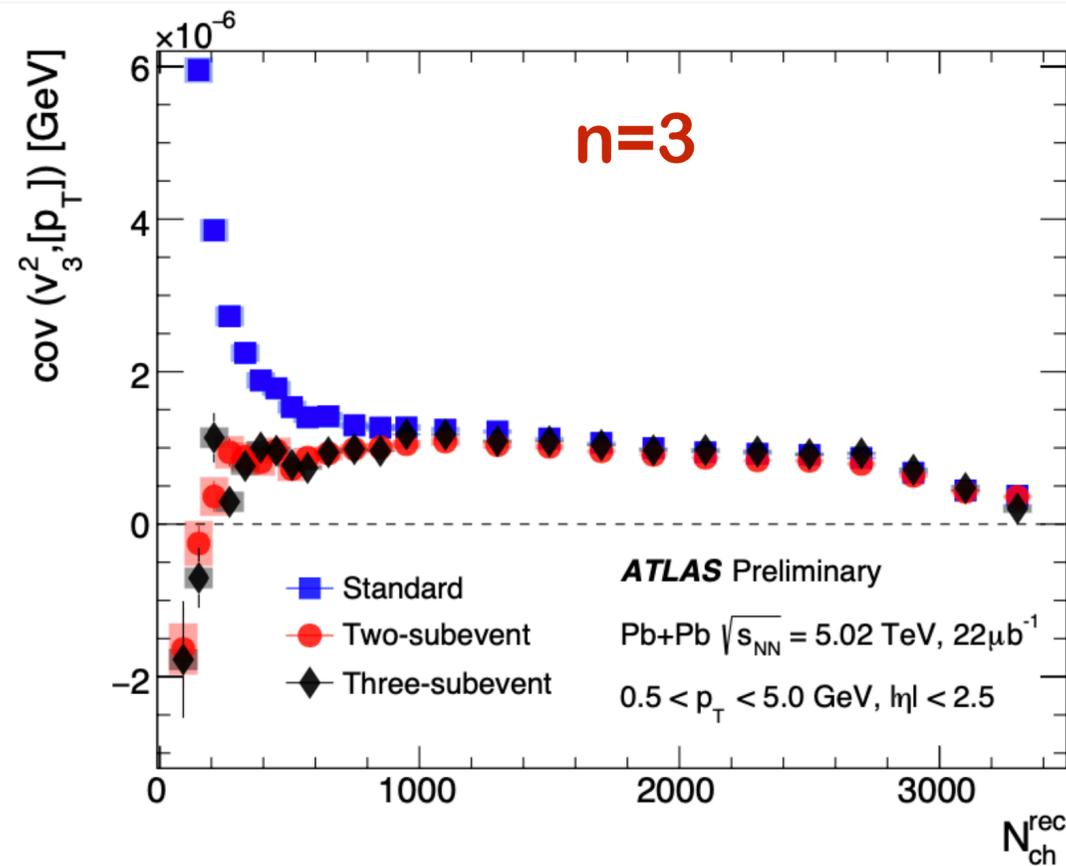
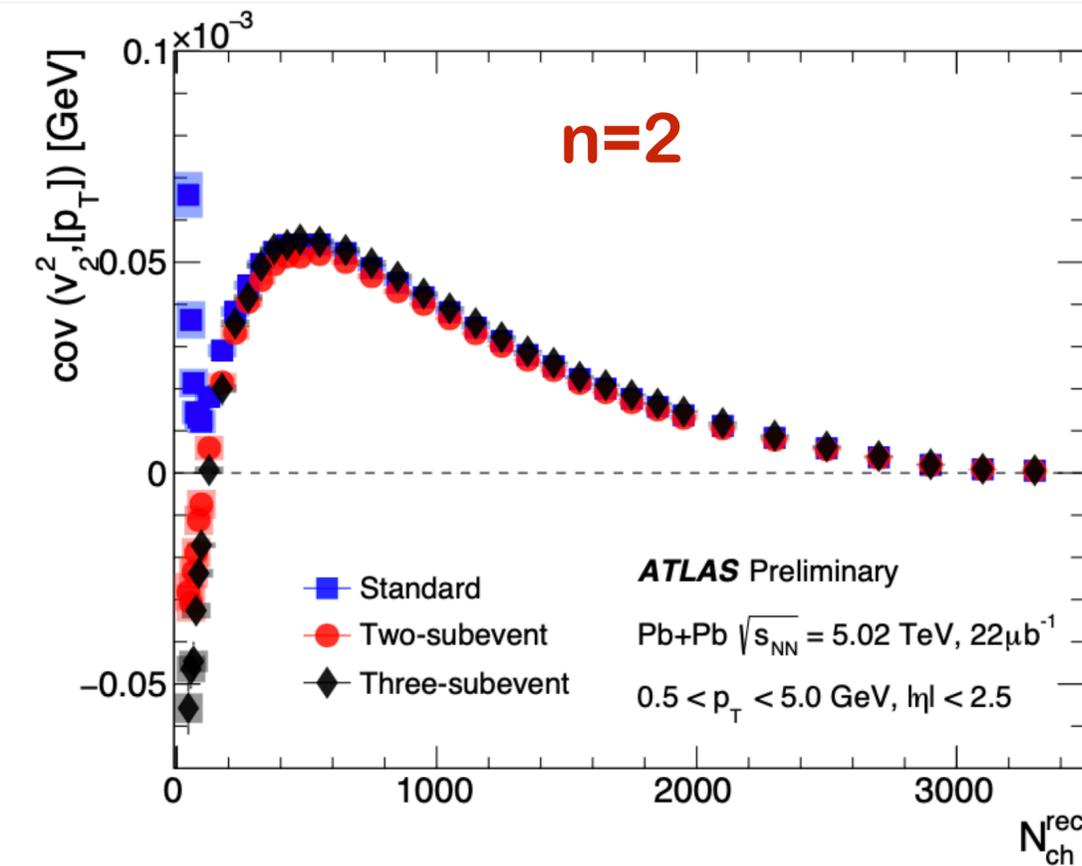
$$c_k = \langle\langle (p_{T,i} - \langle [p_T] \rangle)(p_{T,j} - \langle [p_T] \rangle) \rangle\rangle_{ev}$$

- $cov(v_n^2, [p_T])$  - triplet of particles

- Standard, two-subevent and three-subevent methods
- Subevent methods can suppress non-flow



# Comparison of $\text{cov}(v_n^2, [p_T])$ - subevents methods



$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{var}(v_n^2)}\sqrt{c_k}}$$

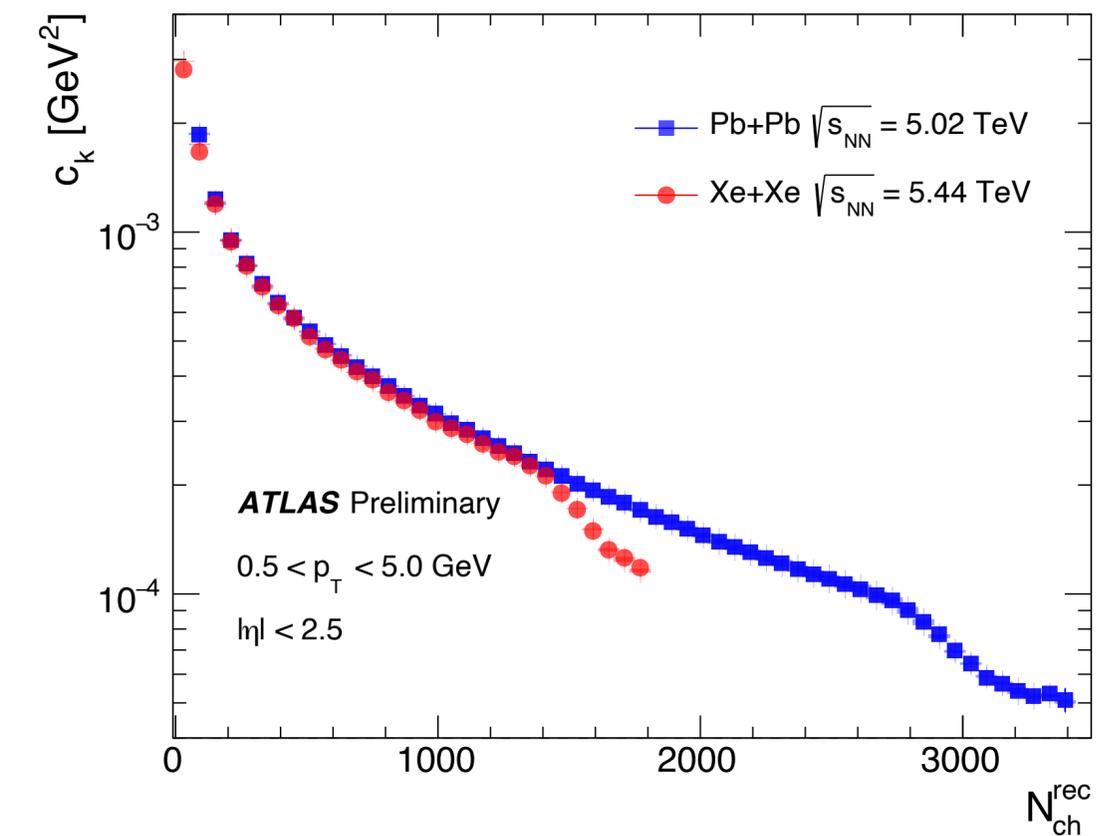
- **Non-flow** significant in standard method at low  $N_{ch}$
- Difference between subevent methods are expected
  - different in  $[p_T]$  and  $v_n$  along  $\eta$
  - different decorrelation of  $v_n$  and  $[p_T]$  along  $\Delta\eta$
- **Combined-subevent method** - final results are average of two- and three-subevent methods

# Results

Focus on  $v_2$  and  $v_3$  results

$v_4$  results in backup slides

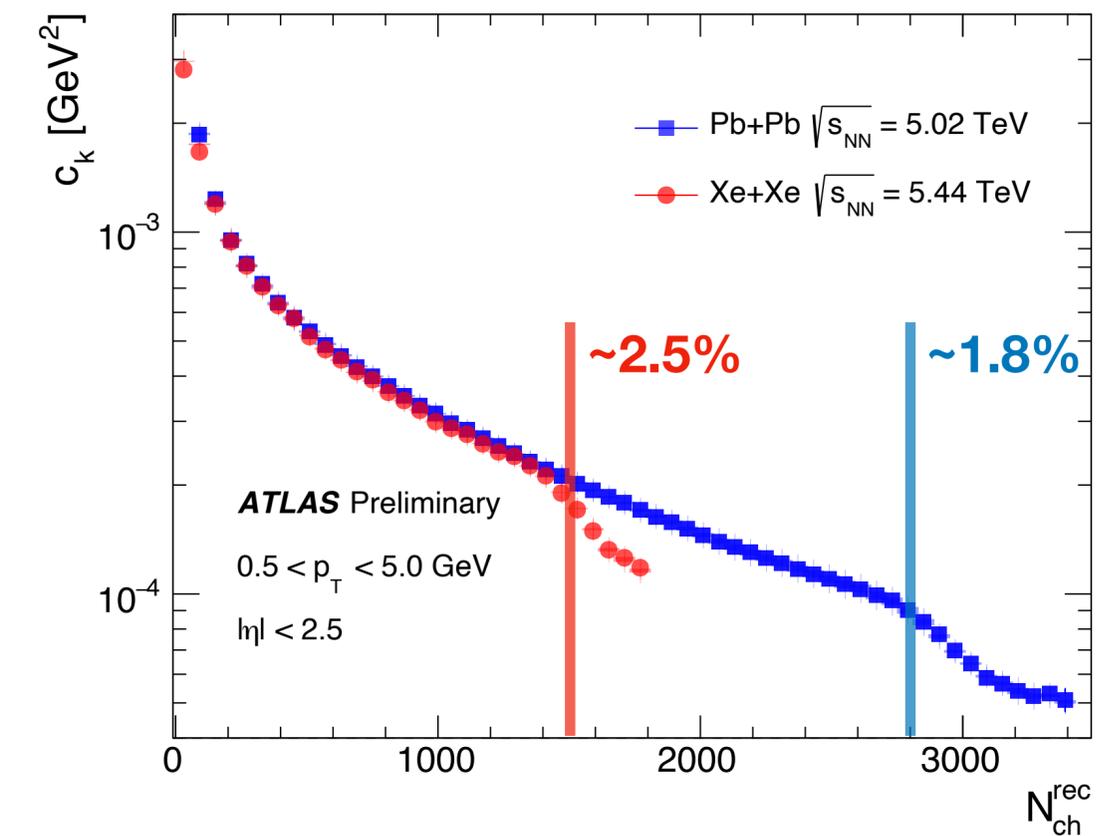
# Variiances of $v_n$ and $[p_T]$



- $c_k$  follows common power-law in Pb+Pb and Xe+Xe

$$\rho(v_n^2, [p_T]) = \frac{cov(v_n^2, [p_T])}{\sqrt{var(v_n^2)} \sqrt{c_k}}$$

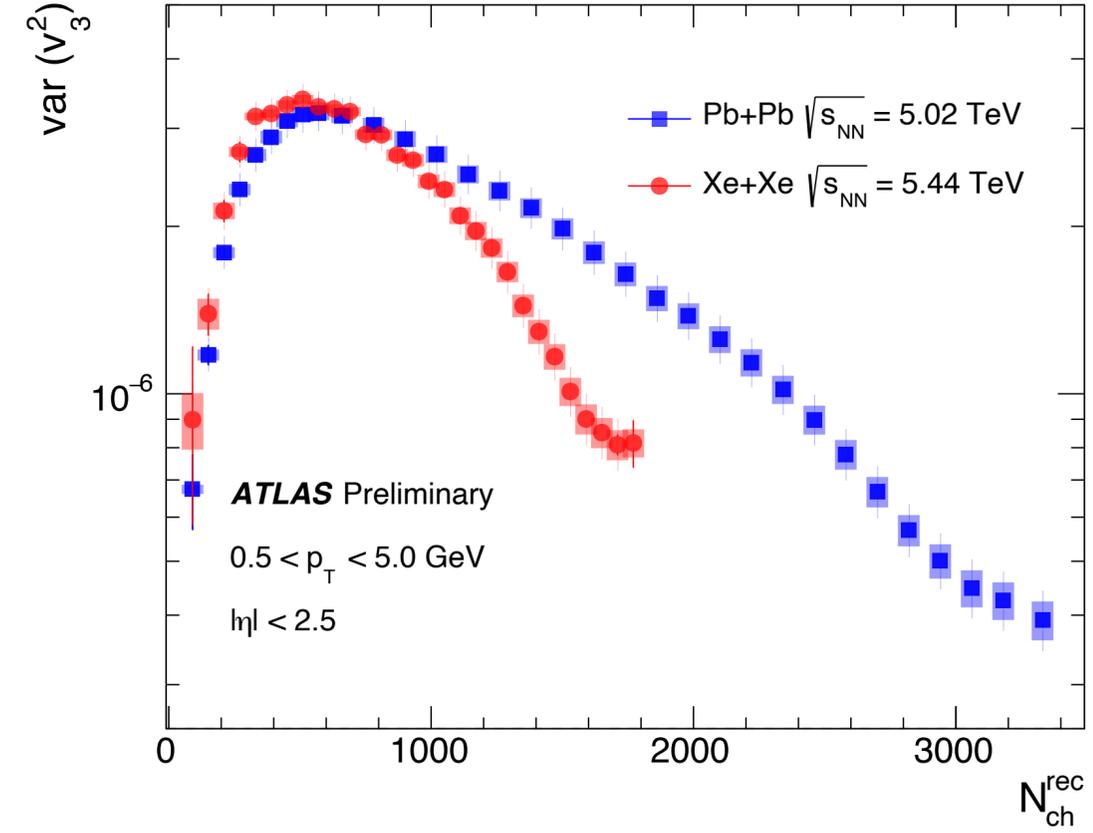
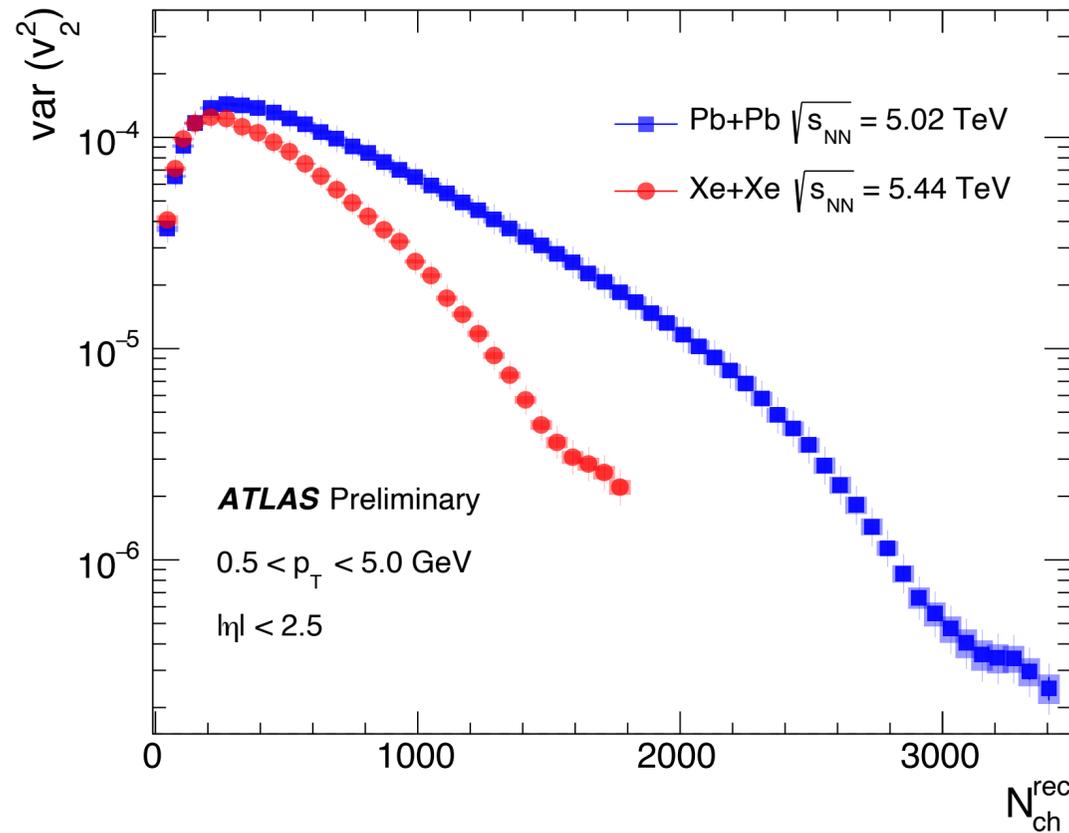
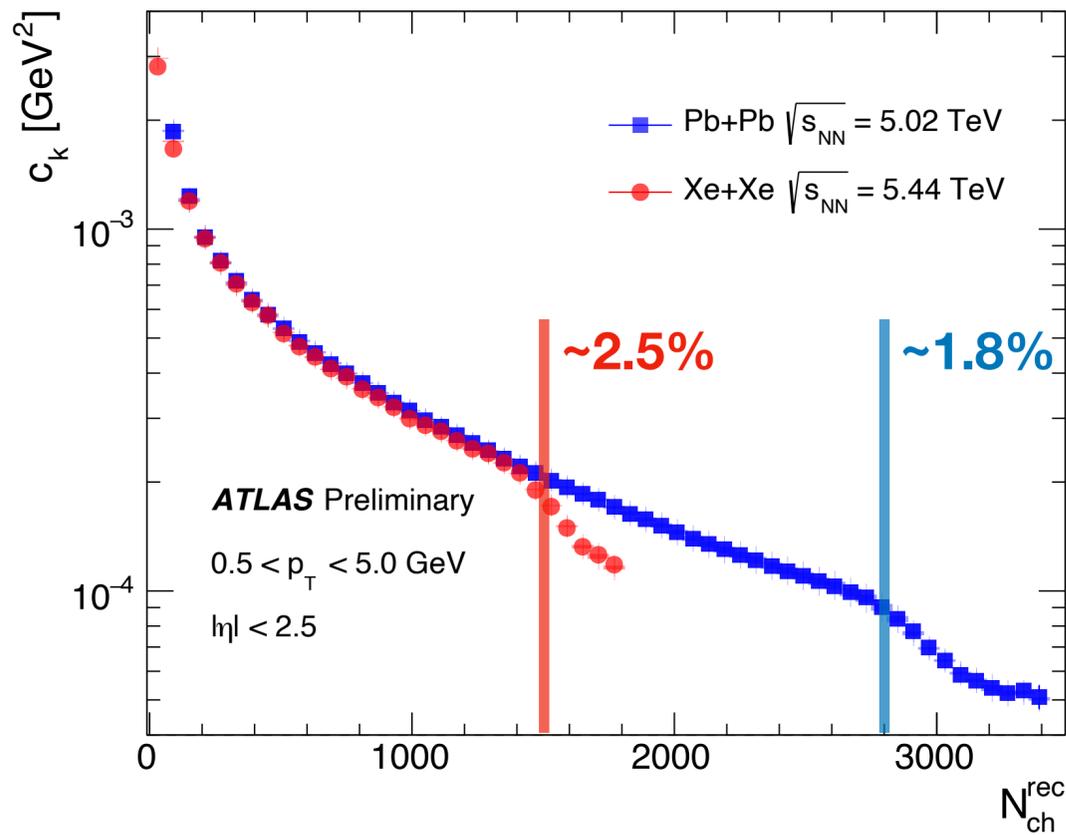
# Variiances of $v_n$ and $[p_T]$



- $c_k$  follows common power-law in Pb+Pb and Xe+Xe
- Departure from power-law in ultra central region - due to upper boundary effect

$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{var}(v_n^2)} \sqrt{c_k}}$$

# Variiances of $v_n$ and $[p_T]$



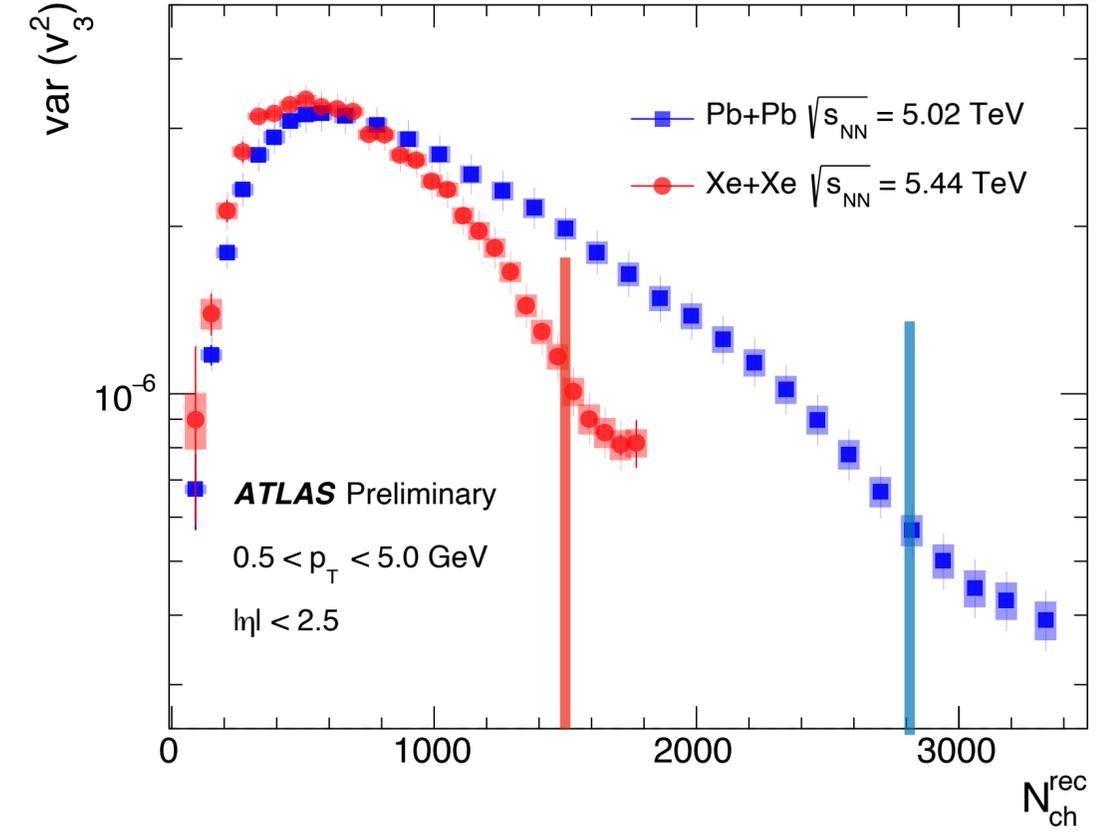
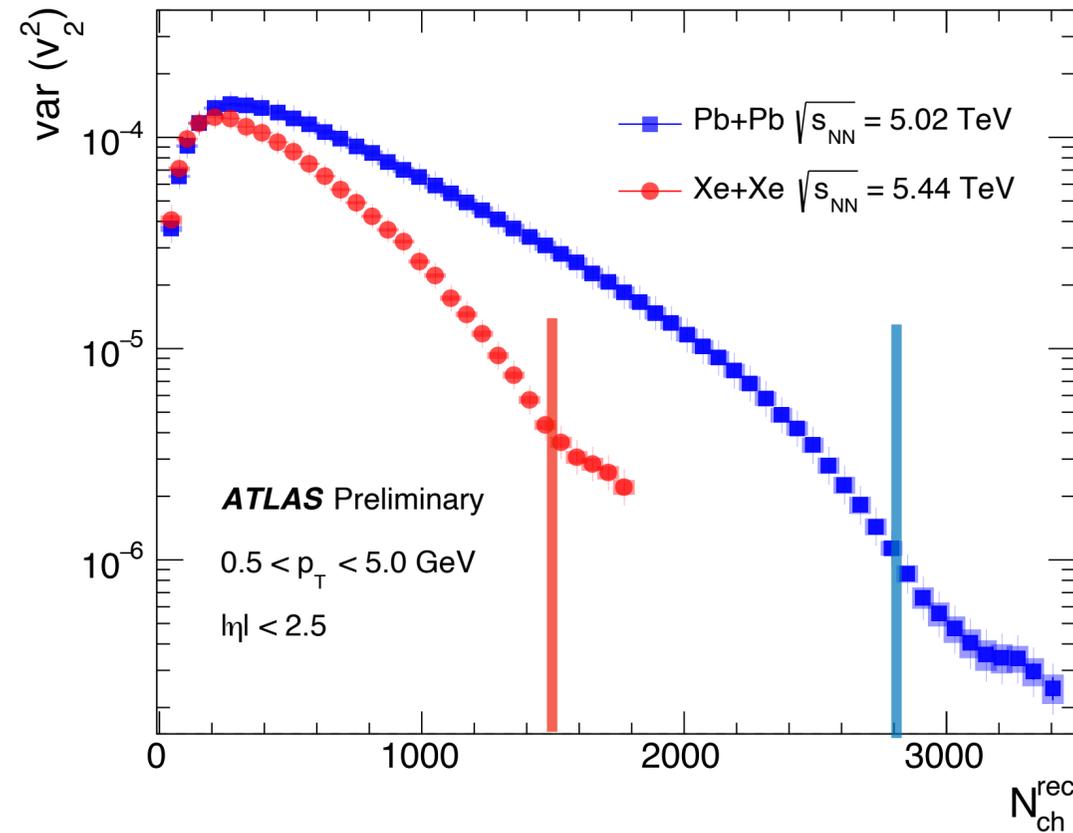
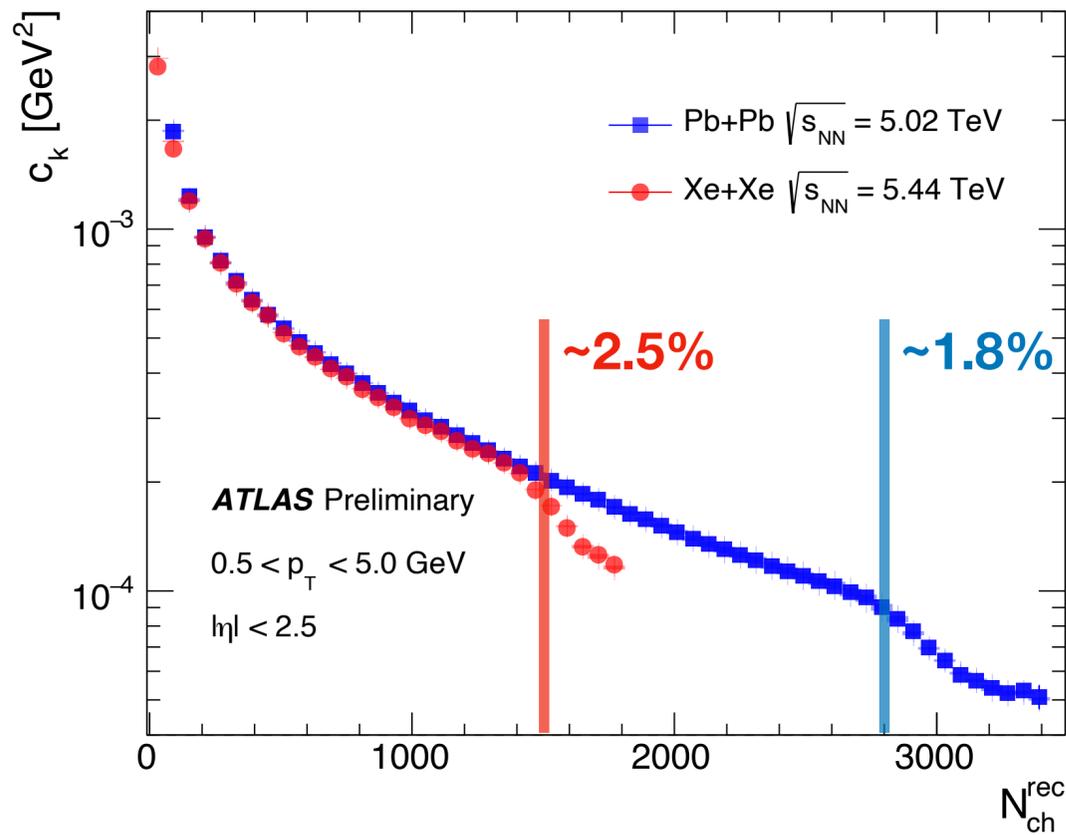
- $c_k$  follows common power-law in Pb+Pb and Xe+Xe
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- $\text{var}(v_n^2)$  follows similar  $N_{\text{ch}}$  dependence in both system
- The ordering and trends are similar to  $v_n$

Phys. Rev. C 101 (2020), 024906

$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{var}(v_n^2)} \sqrt{c_k}}$$

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Phys. Rev. C 101 (2020), 024906

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- $\text{var}(v_n^2)$  shows some upper boundary effects

# Comparisons - Pb+Pb vs Xe+Xe

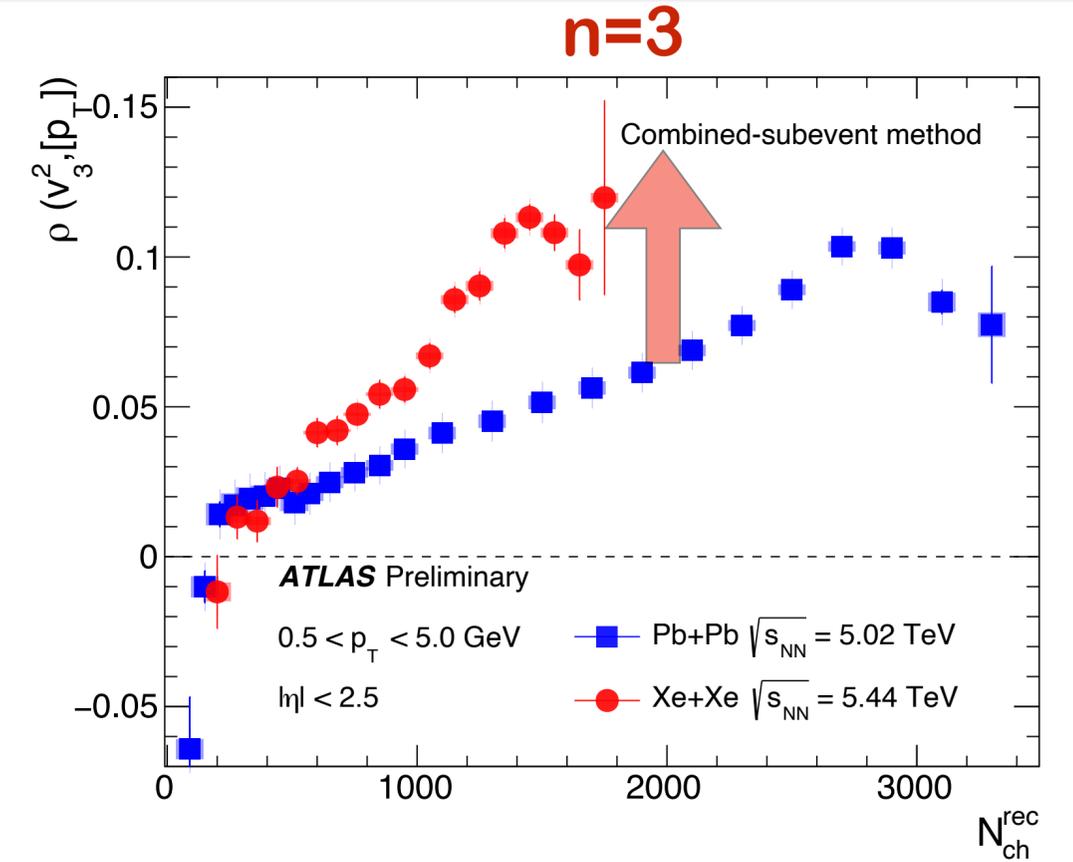
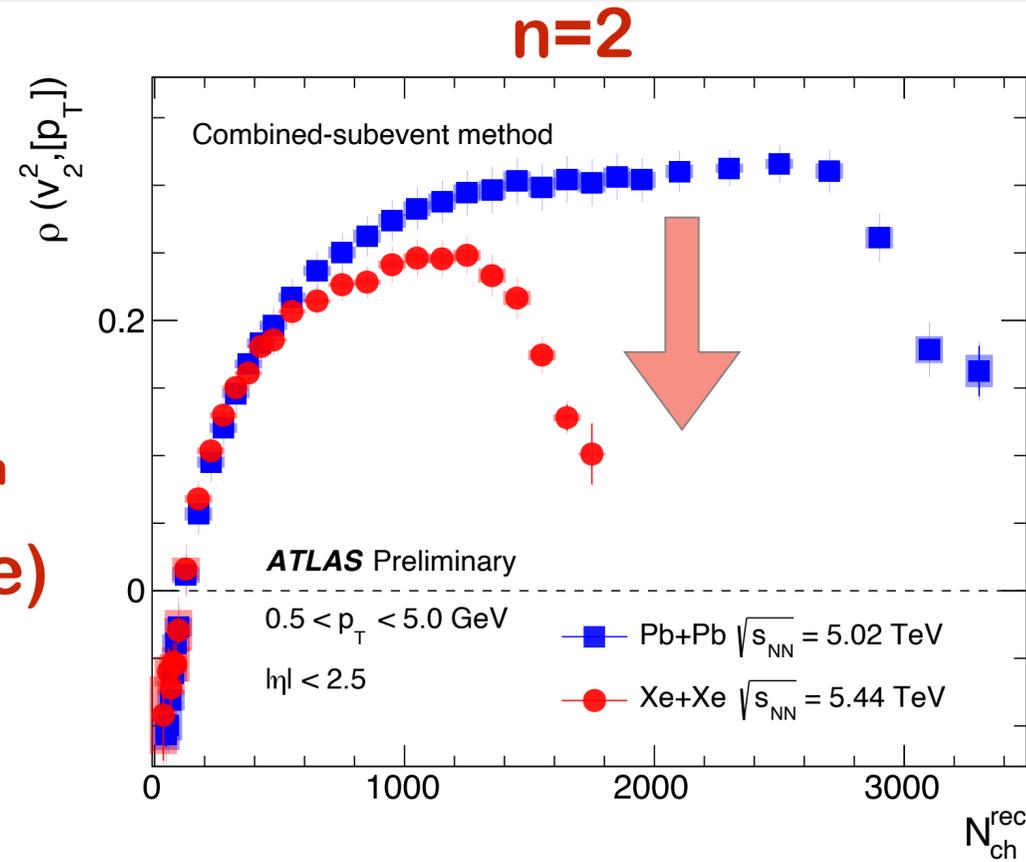
$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{var}(v_n^2)}\sqrt{c_k}}$$

- As a function of  $N_{\text{ch}}$ 
  - Low  $N_{\text{ch}}$  - similar values
  - High  $N_{\text{ch}}$  - **Opposite ordering between  $n=2$  and  $n=3$**

$$\rho_2^{\text{Xe+Xe}} < \rho_2^{\text{Pb+Pb}}$$

$$\rho_3^{\text{Xe+Xe}} > \rho_3^{\text{Pb+Pb}}$$

$N_{\text{ch}}$   
(size)



# Comparisons - Pb+Pb vs Xe+Xe

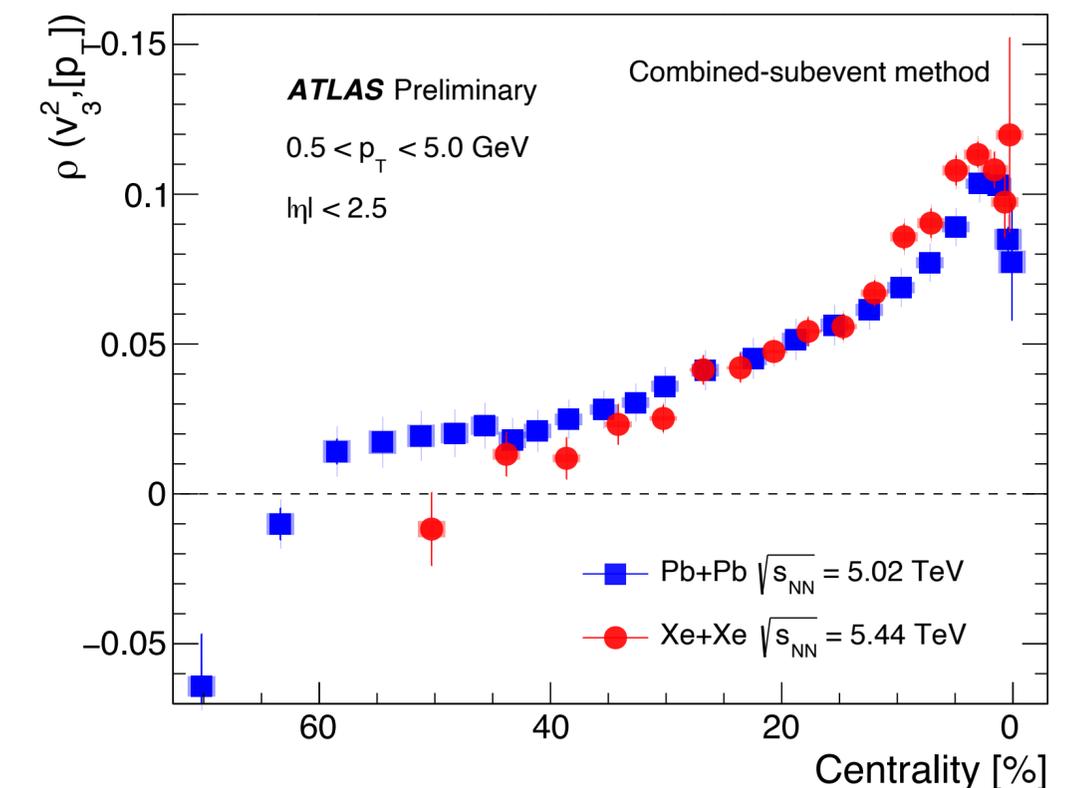
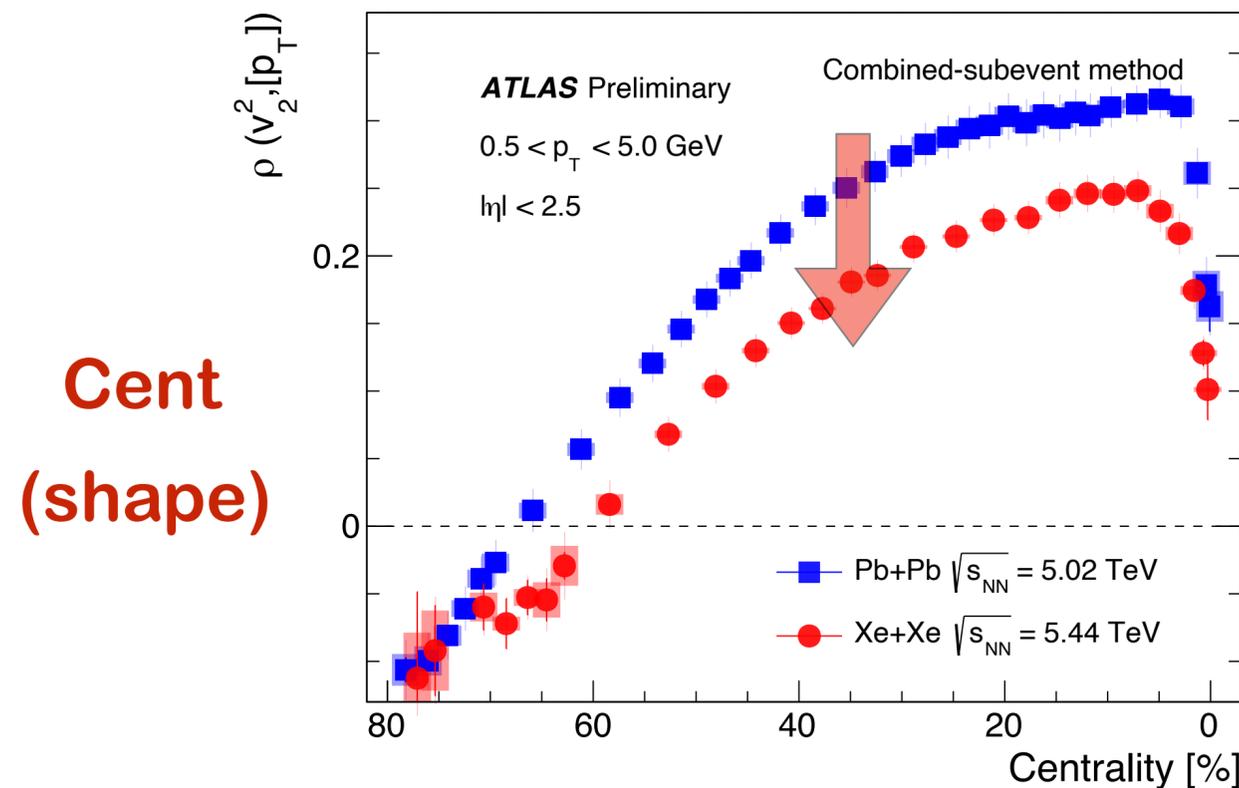
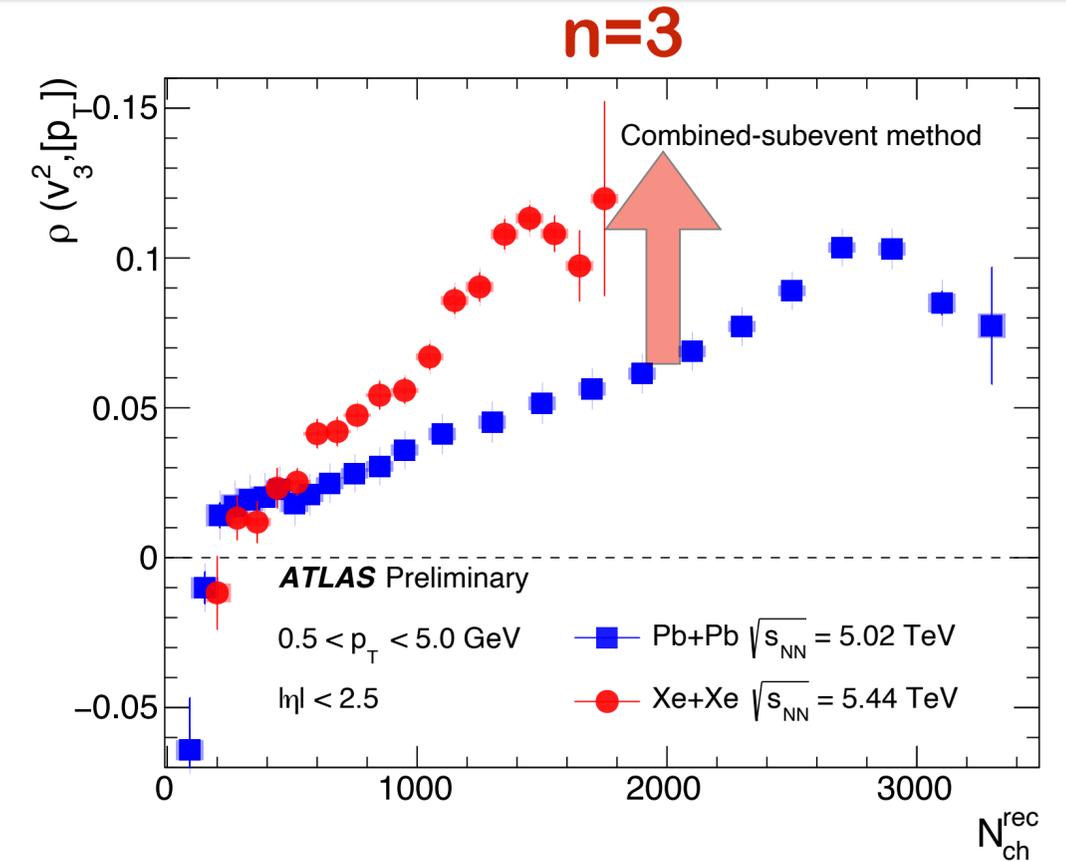
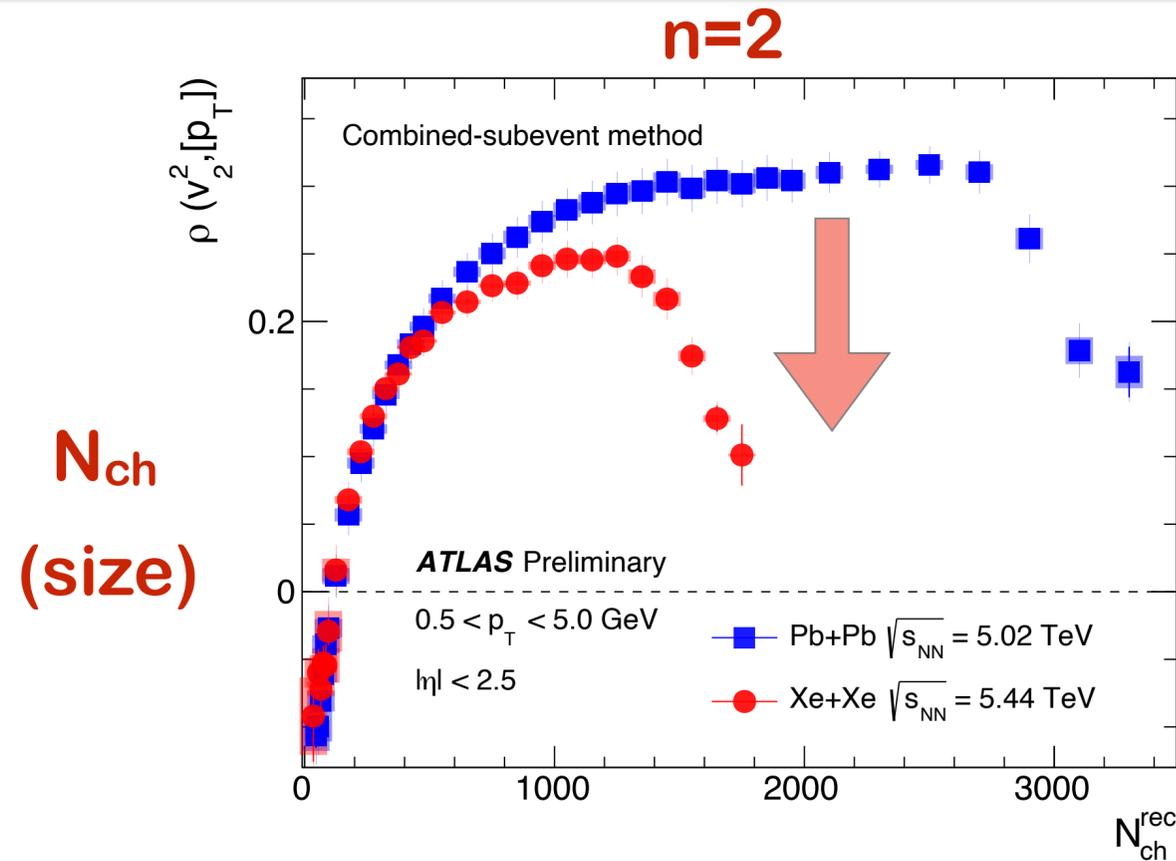
$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{var}(v_n^2)}\sqrt{c_k}}$$

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$$\rho_2^{\text{Xe+Xe}} < \rho_2^{\text{Pb+Pb}}$$

$$\rho_3^{\text{Xe+Xe}} > \rho_3^{\text{Pb+Pb}}$$

- As a function of centrality
  - $\rho_{v_2}$  is smaller in Xe+Xe
  - but  $\rho_{v_3}$  is comparable

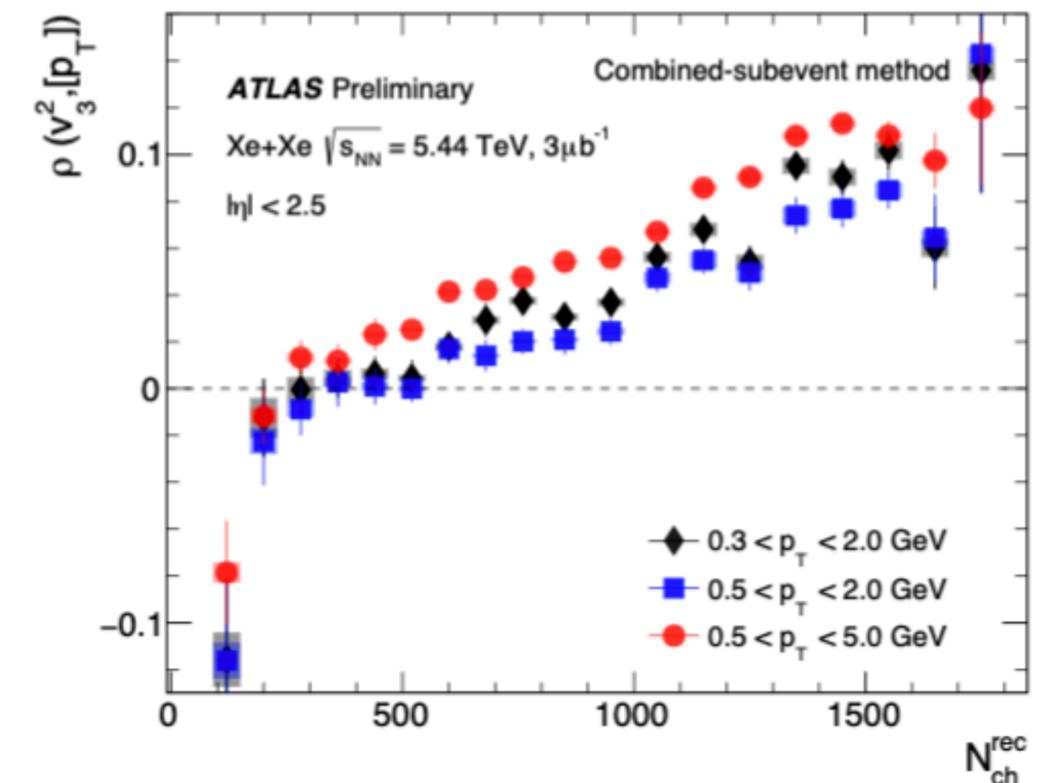
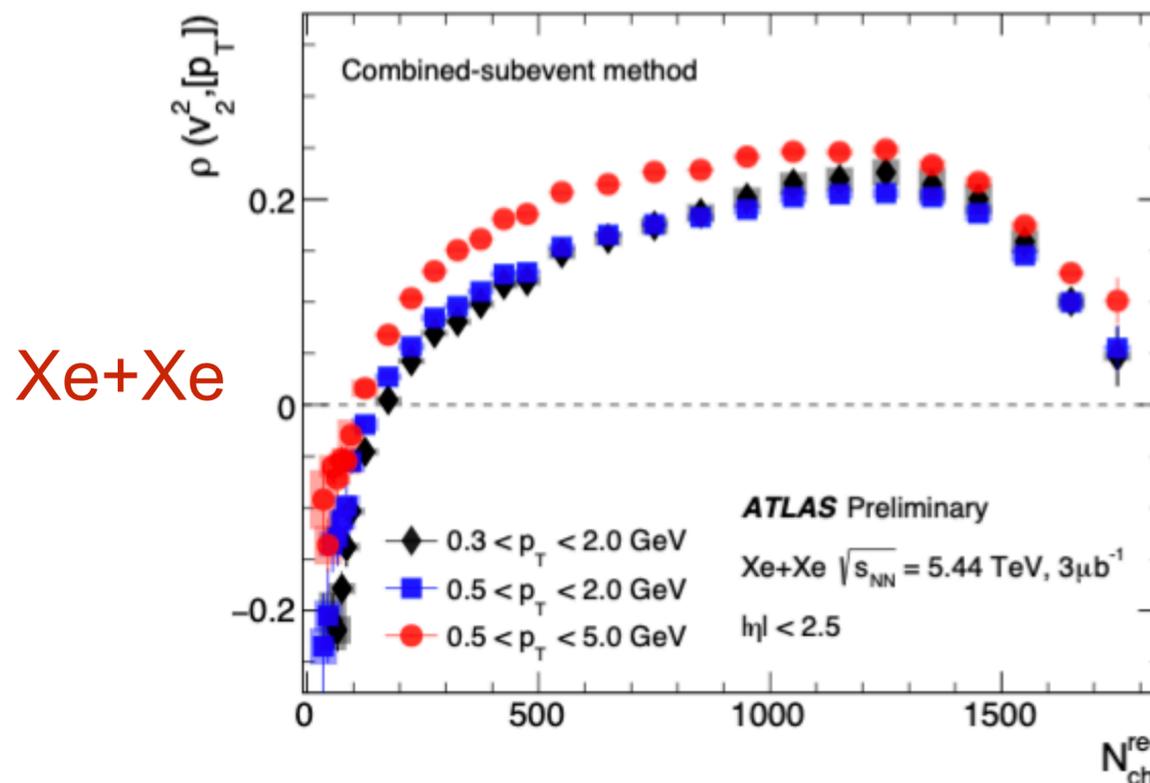
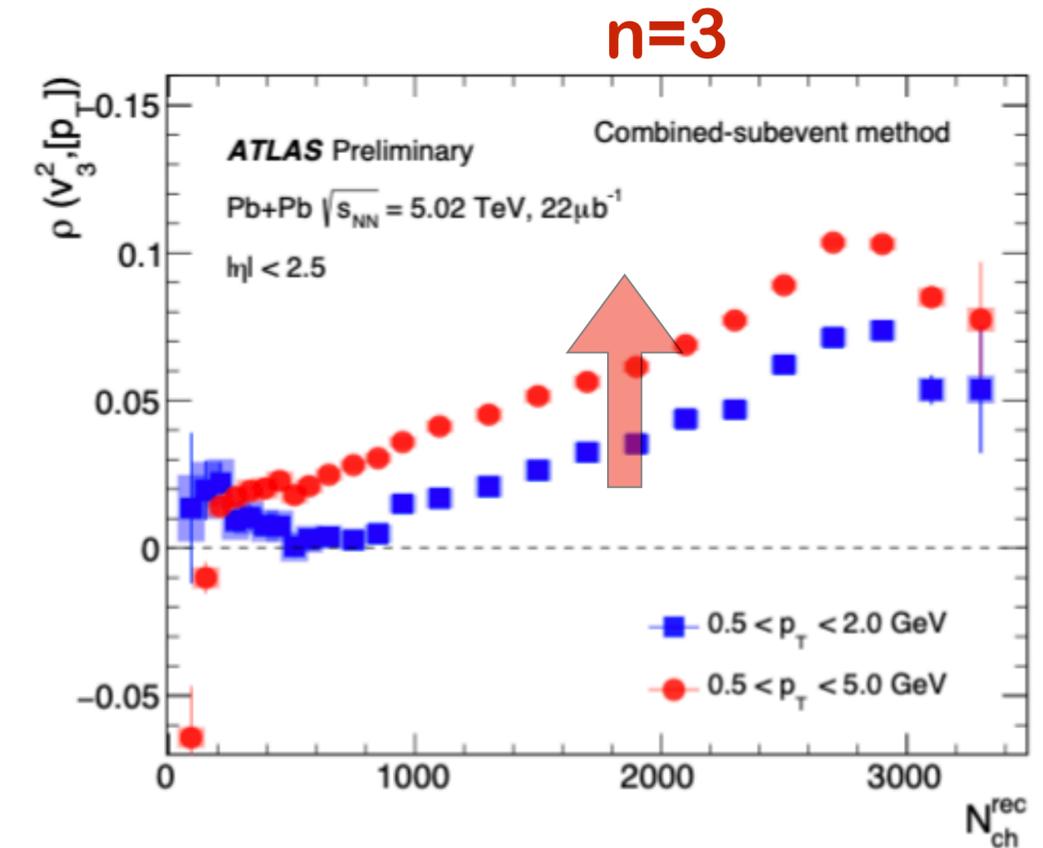
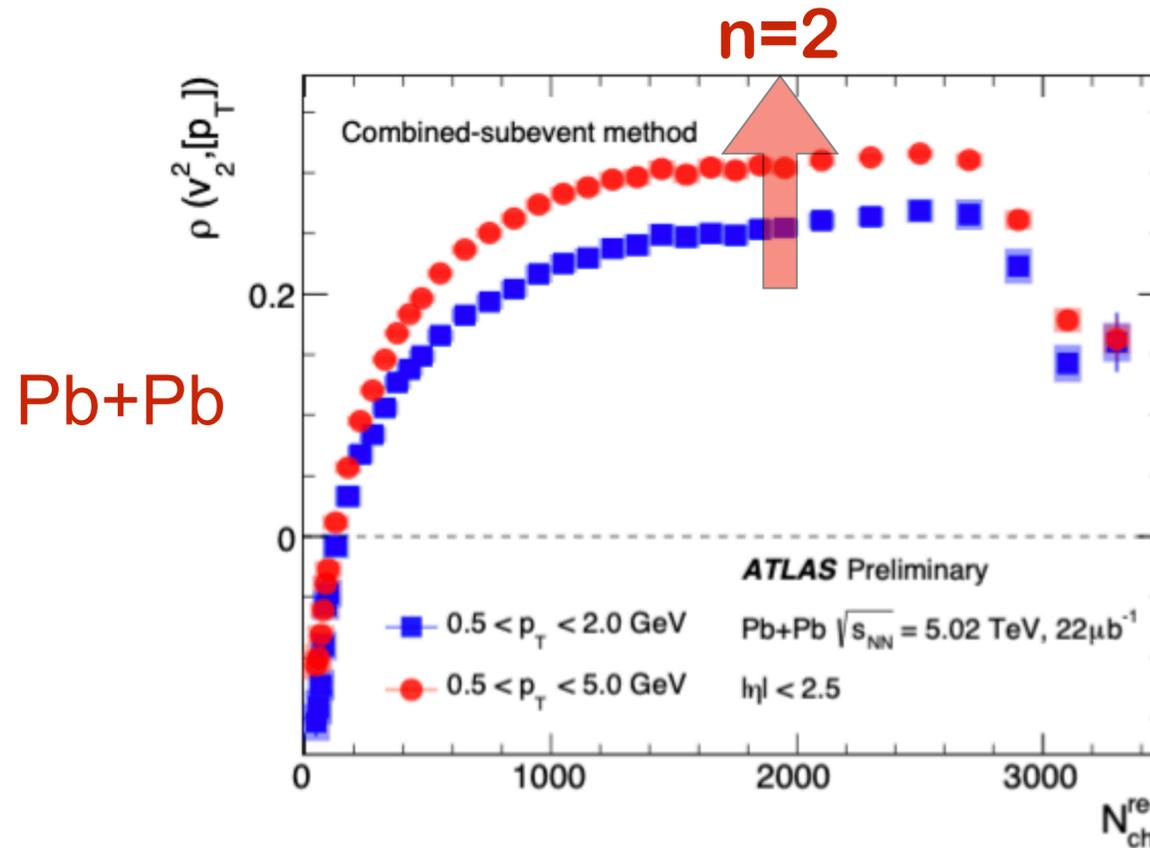


# Dependence on $p_T$ range

- In both systems  $\rho$  is larger for  $0.5 < p_T < 5.0$  GeV than  $0.5 < p_T < 2.0$  GeV - **increase due to high  $p_T$  particles**

- In Xe+Xe :  $\rho$  is consistent for  $0.5 < p_T < 2.0$  GeV and  $0.3 < p_T < 2.0$  GeV

- Low  $p_T$  region well described by hydrodynamics - **little effect to more low- $p_T$  particles**



# Dependence on $\eta$ -range (Pb+Pb)

- Two eta ranges compared

$$|\eta| < 2.5$$

$$|\eta| < 1.0$$

A :  $\eta < -0.35$

B :  $|\eta| < 0.3$

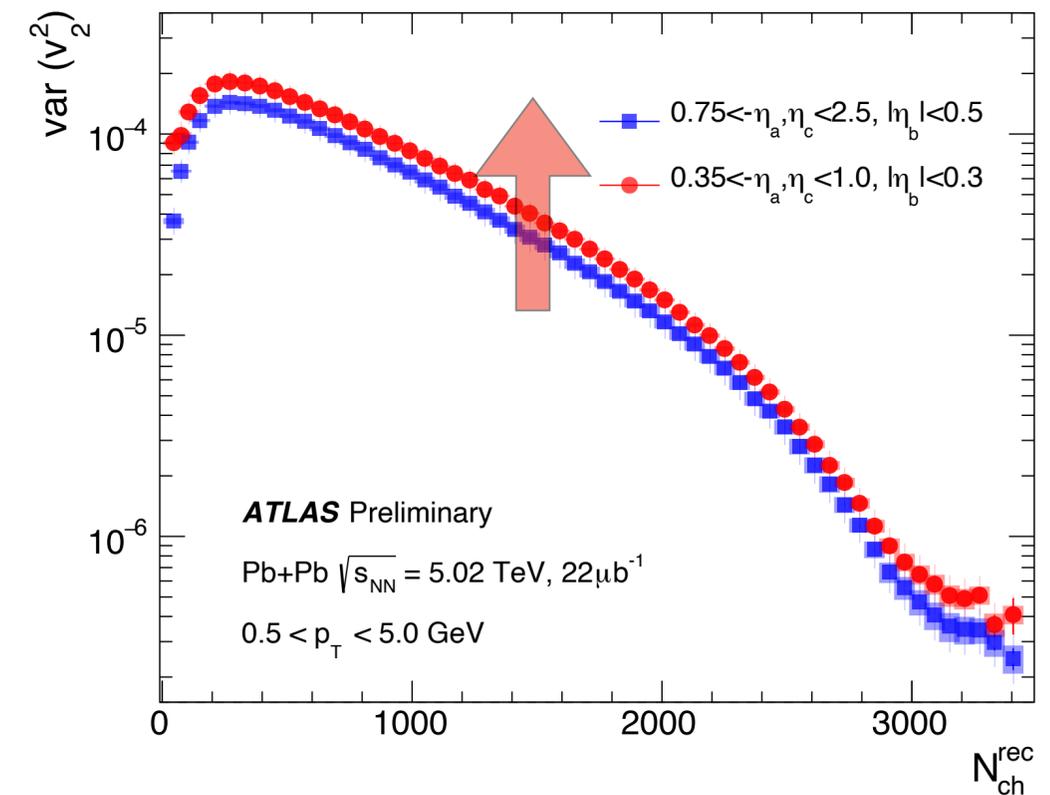
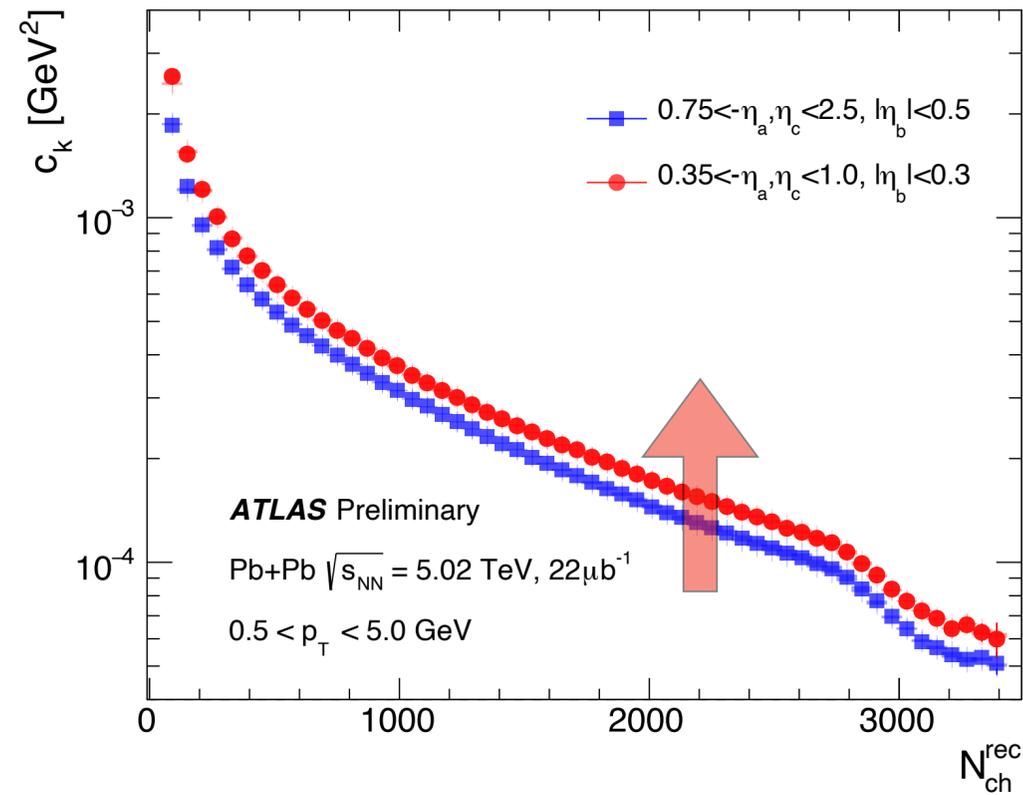
C :  $\eta > 0.35$

- $c_k$  is larger by 10% for  $|\eta| < 1$

- $\text{var}(v_n^2)$  is larger by 10-20% for  $|\eta| < 1$

- Reasons

- The  $v_n$  and  $[p_T]$  magnitudes are larger for  $|\eta| < 1$
- Decorrelation smaller for  $|\eta| < 1$



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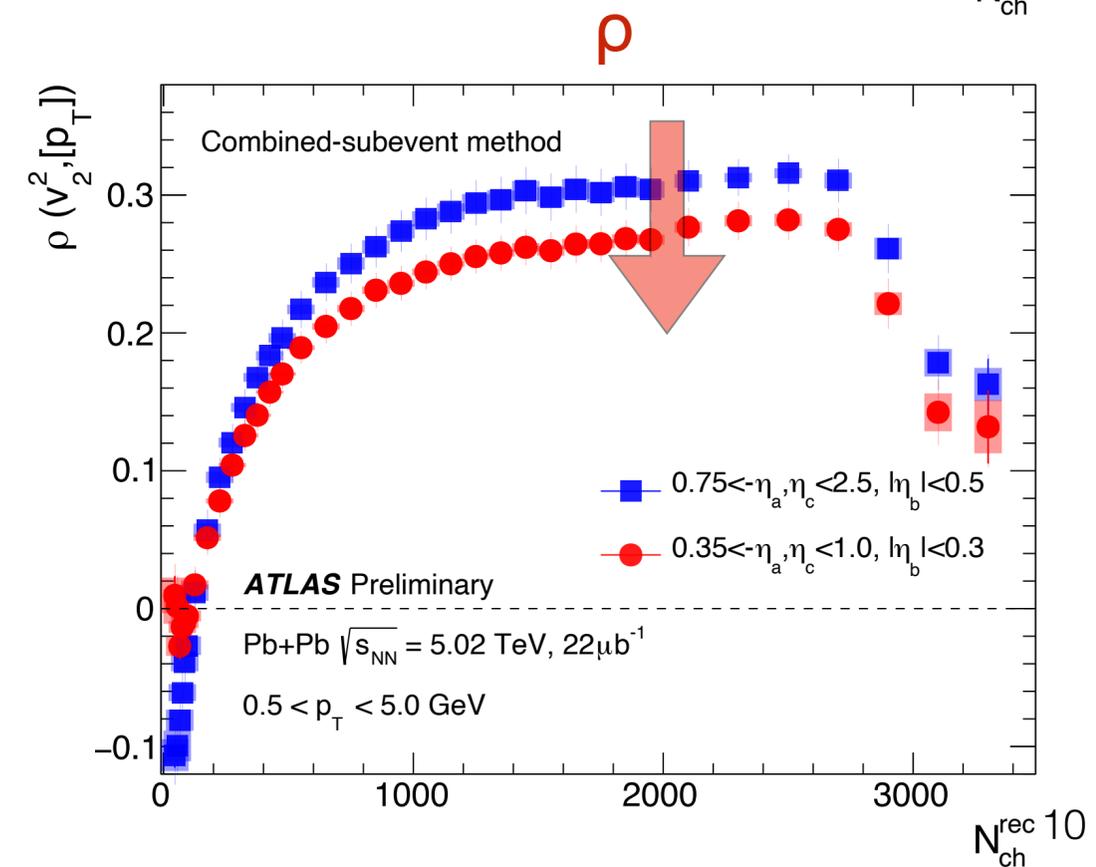
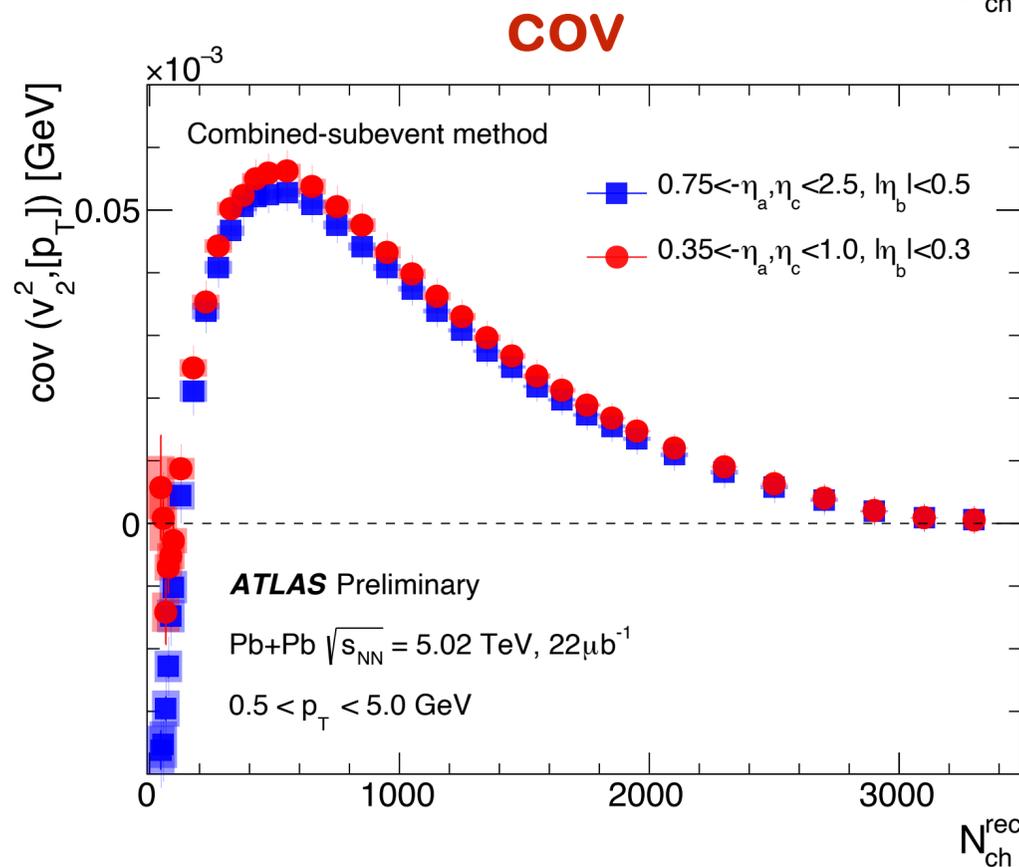
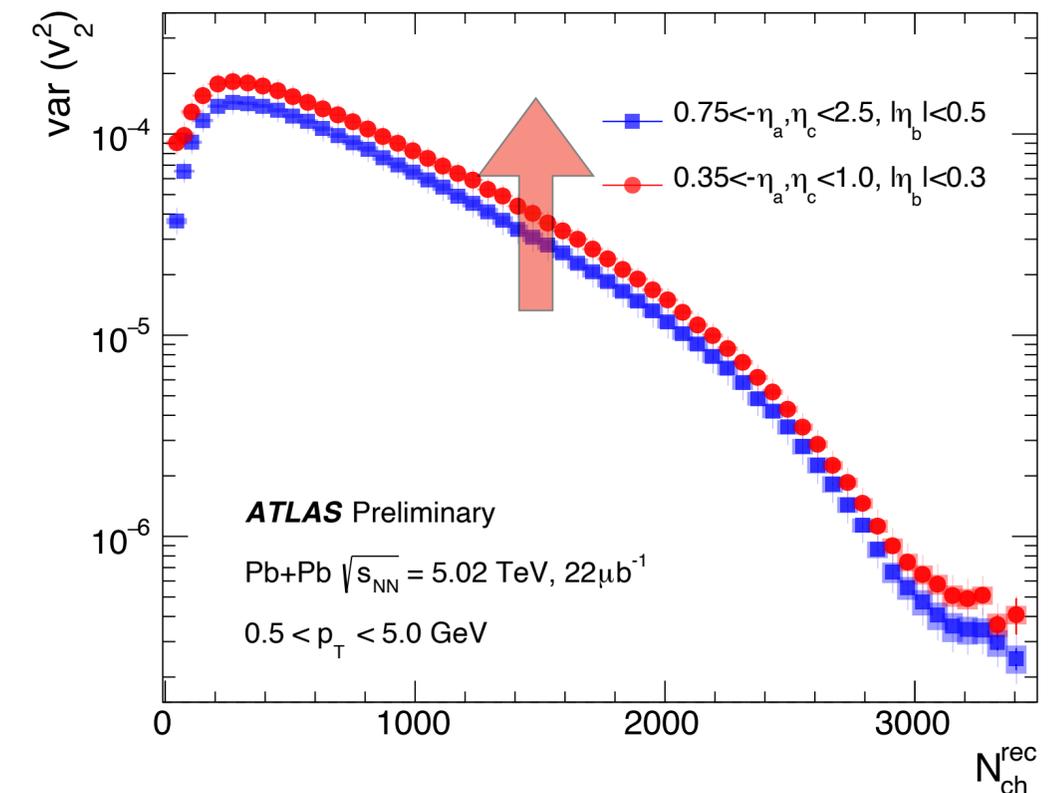
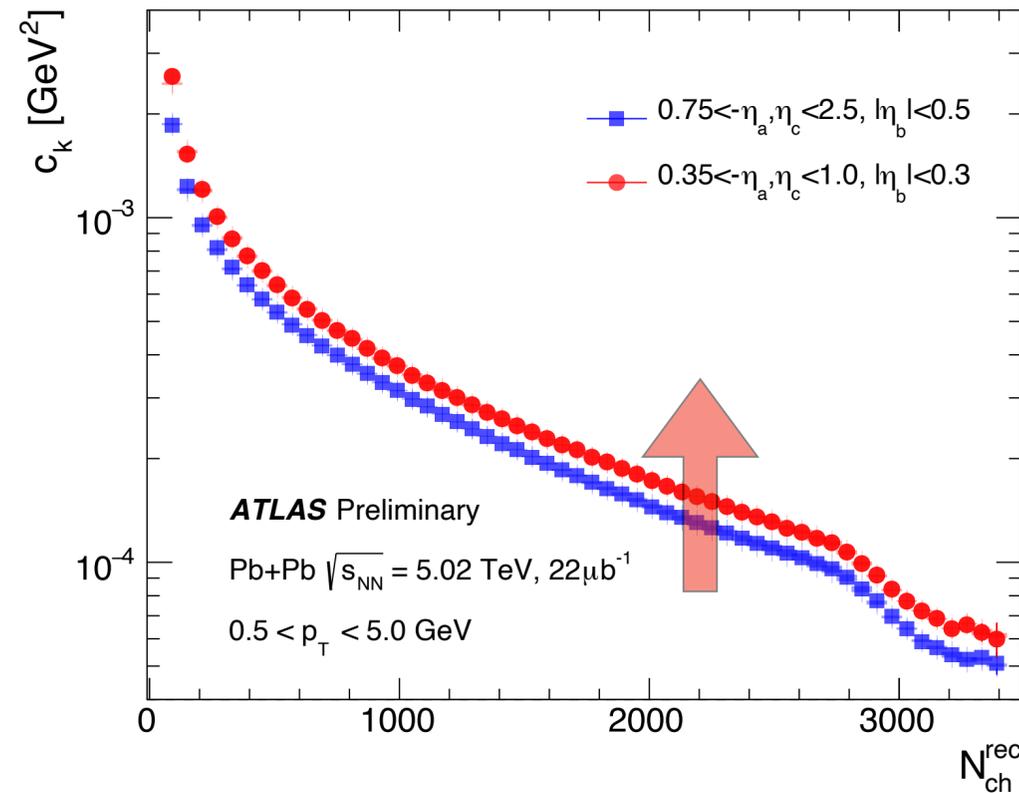
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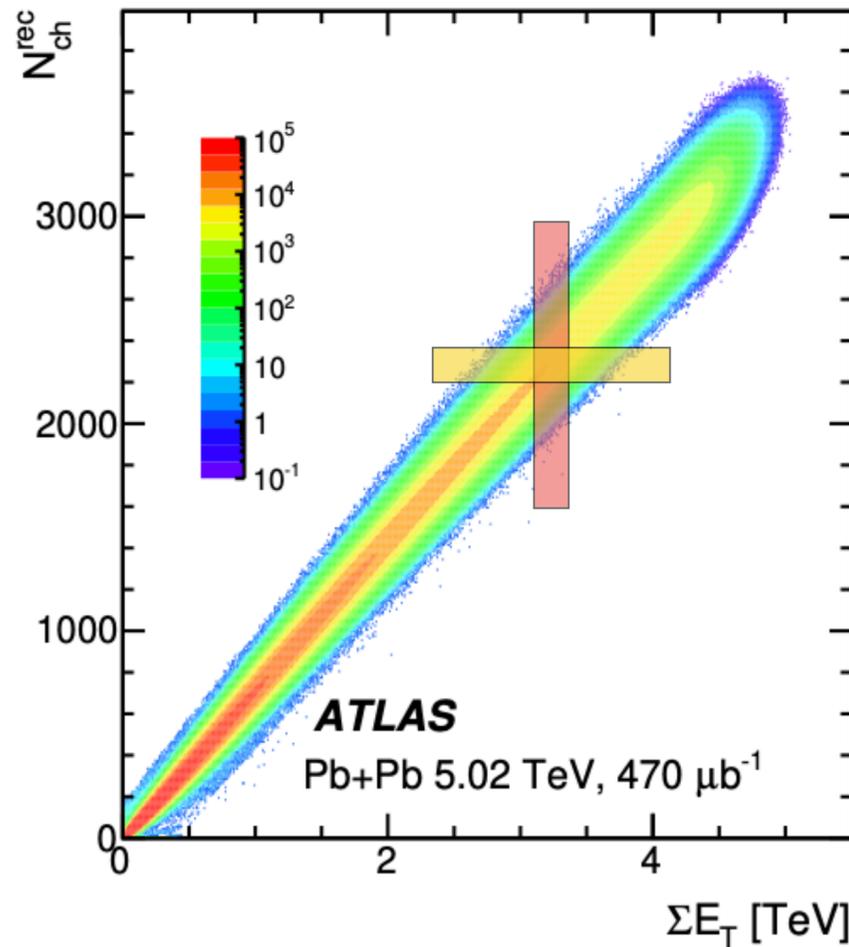
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- Covariances show good agreement between  $\eta$ -ranges

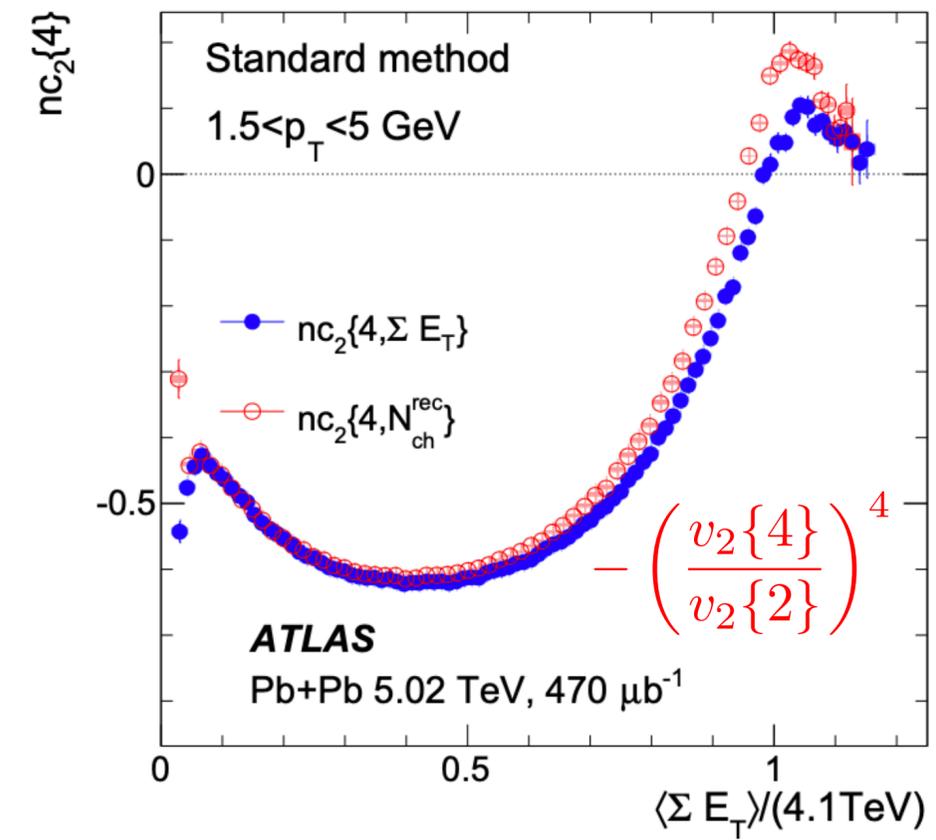
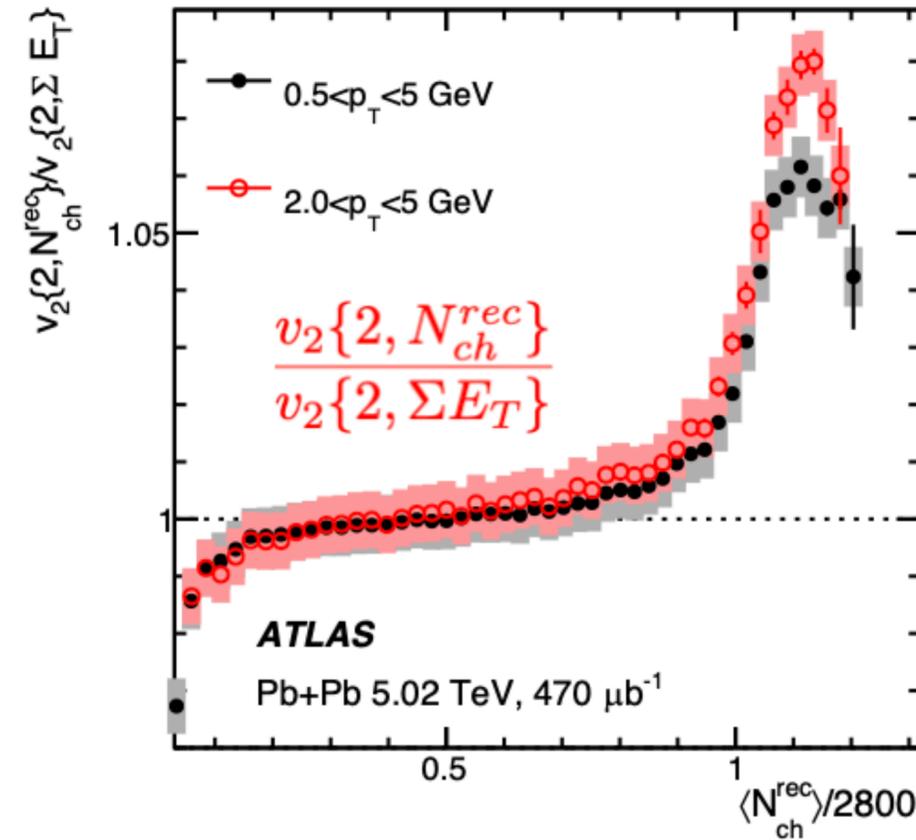
- $\rho_{v_n}$  are systematically smaller for  $|\eta| < 1$  due to smaller  $c_k$  and  $\text{var}(v_n^2)$



# Centrality fluctuations in $v_n$



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$$p(\text{Obs.} | N_{ch}) = \sum_{cent} p(\text{Obs.} | cent) \otimes p(cent | N_{ch})$$

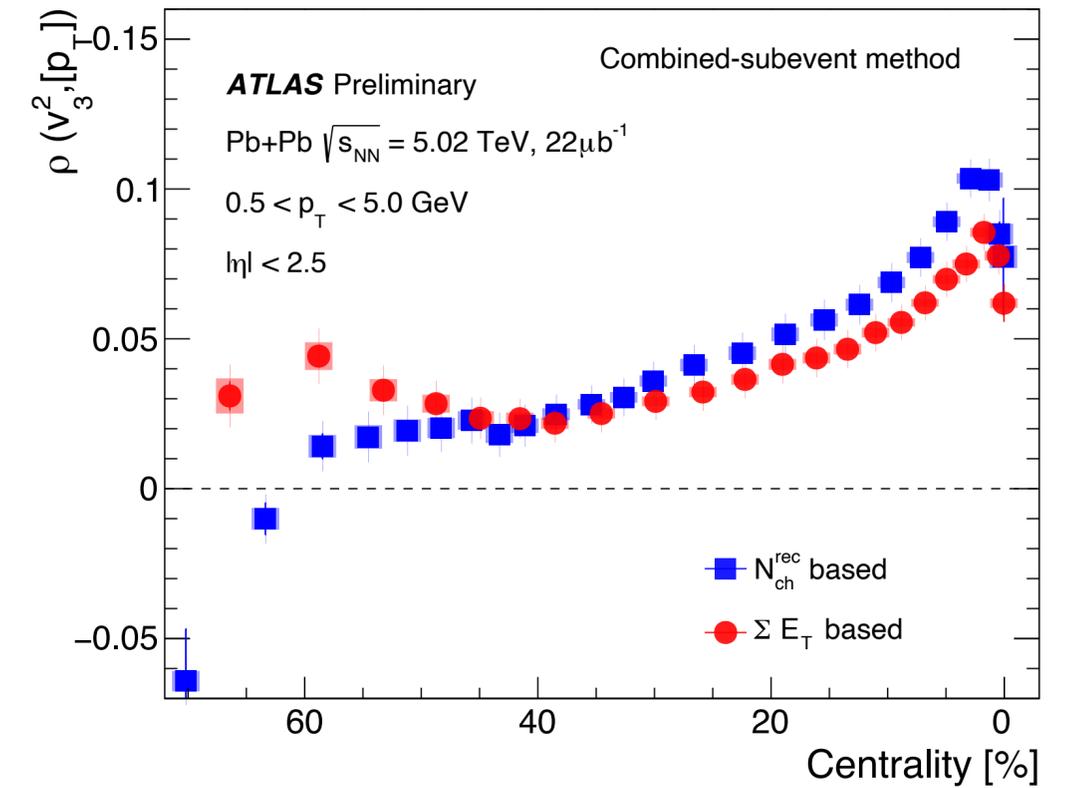
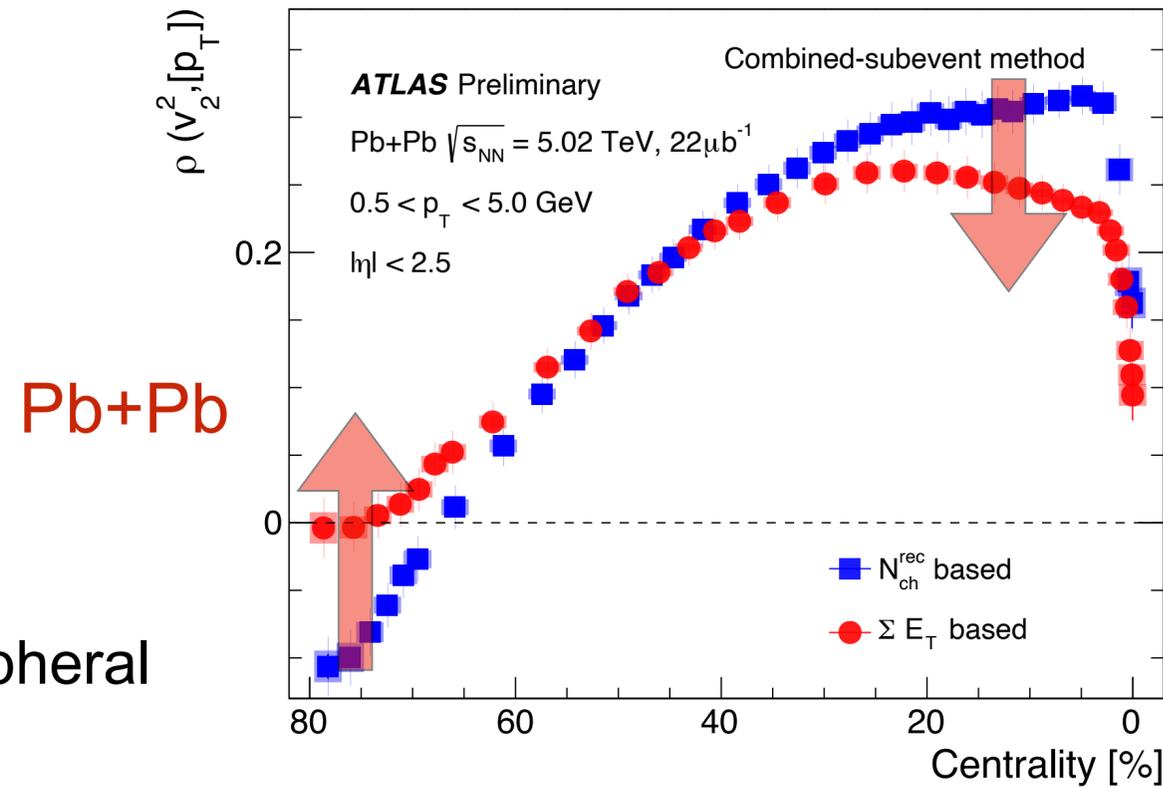
- True centrality unknown
- Smearing between  $N_{ch}$  and  $E_T$  - Same  $N_{ch}$  but different  $E_T$ , Same  $E_T$  but different  $N_{ch}$
- Event averaging in  $N_{ch}$  and  $E_T$  bins - centrality fluctuations

- Centrality fluctuation - large effect for  $v_2\{2\}$  in central region
- Larger centrality fluctuation effect for higher particle-cumulants
- Effect present in much broader centrality range for both  $n=2$  and  $n=3$

# Centrality fluctuations in $v_n$ -[ $p_T$ ] correlation

- $E_T$  and  $N_{ch}$  are mapped to centrality (based on  $E_T$  cuts)

- Significantly large centrality fluctuations in central and peripheral

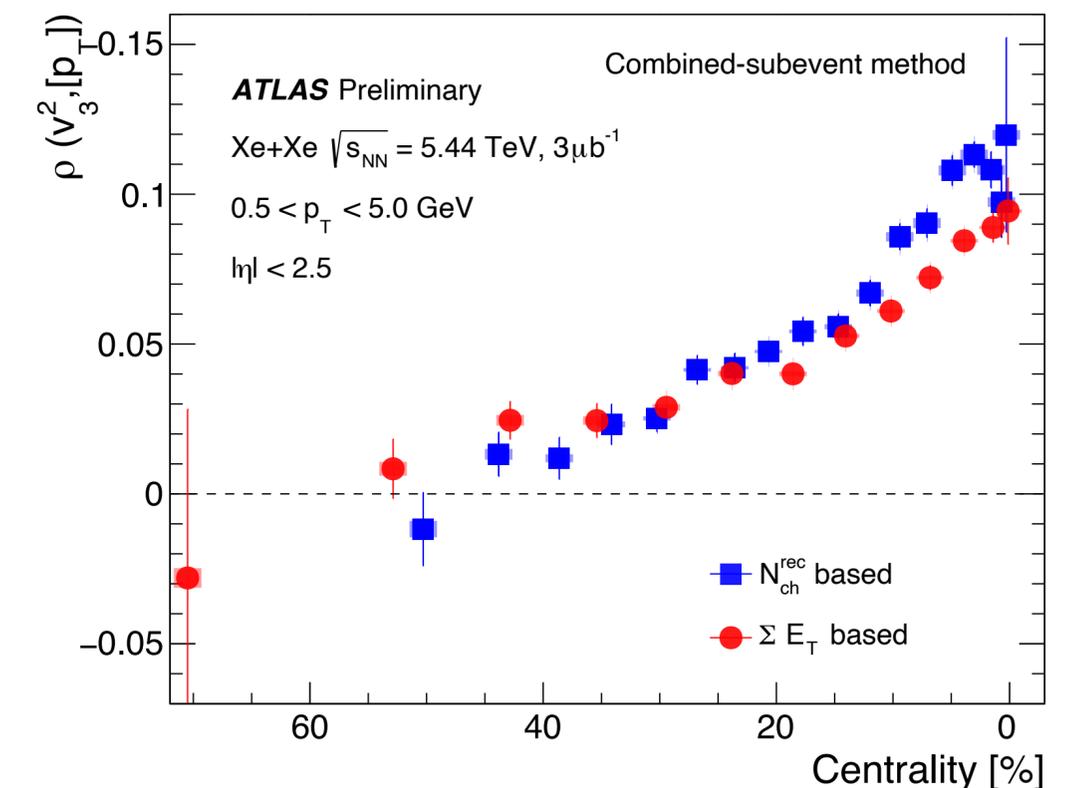
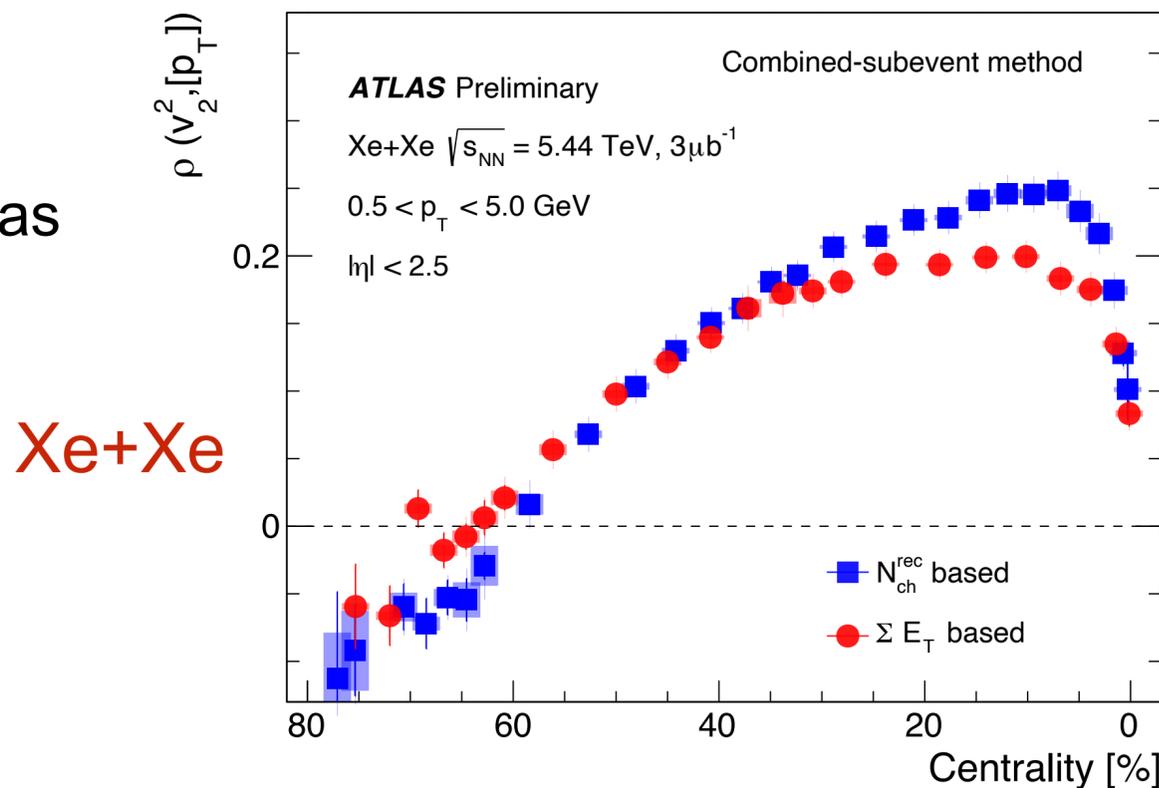
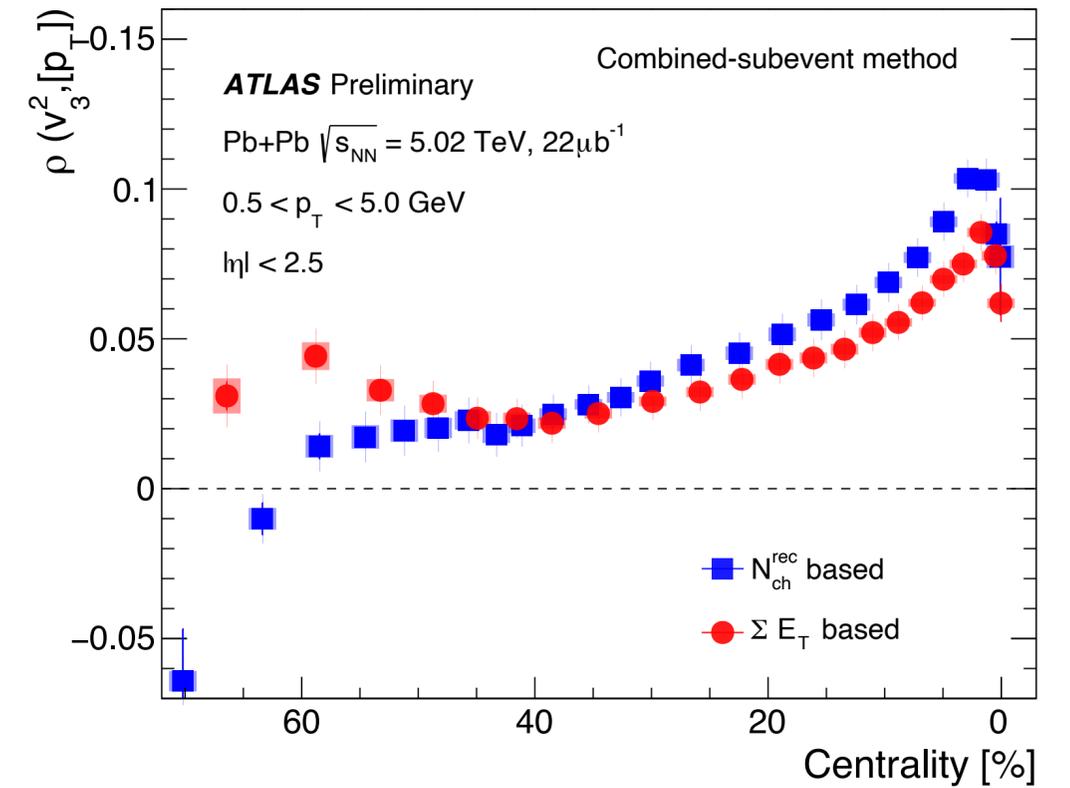
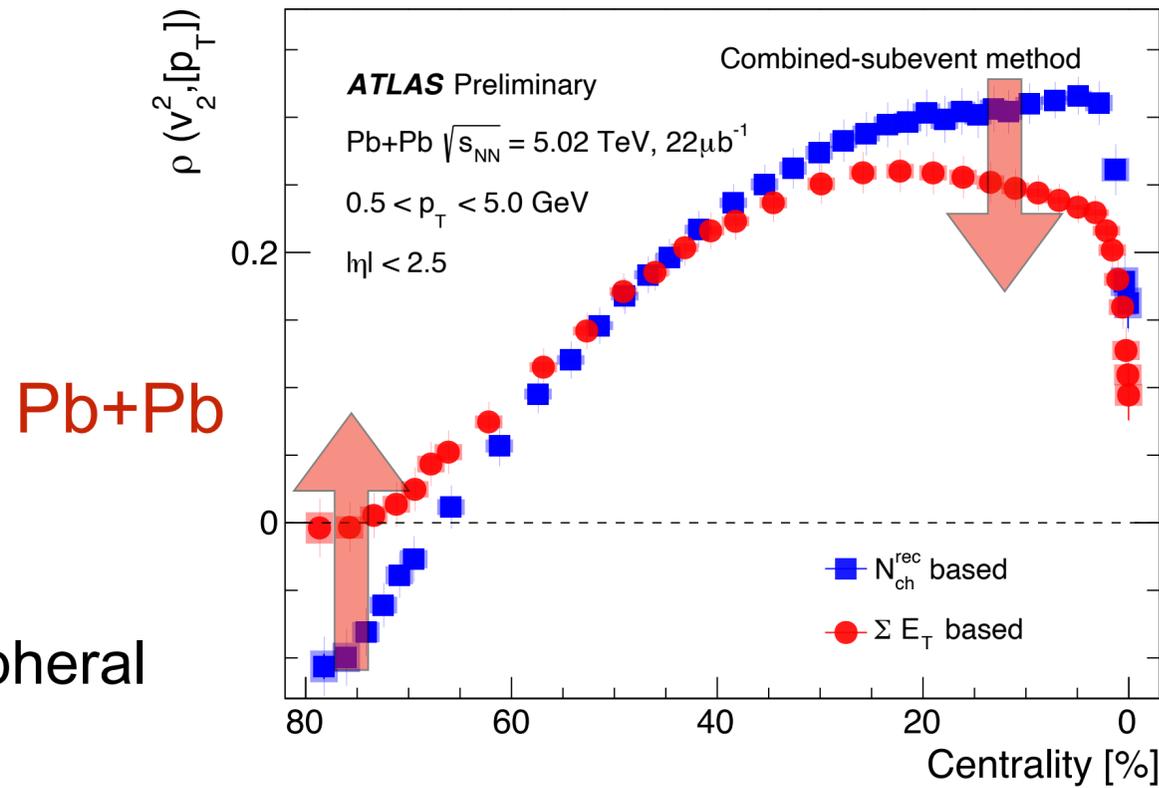


# Centrality fluctuations in $v_n$ -[ $p_T$ ] correlation

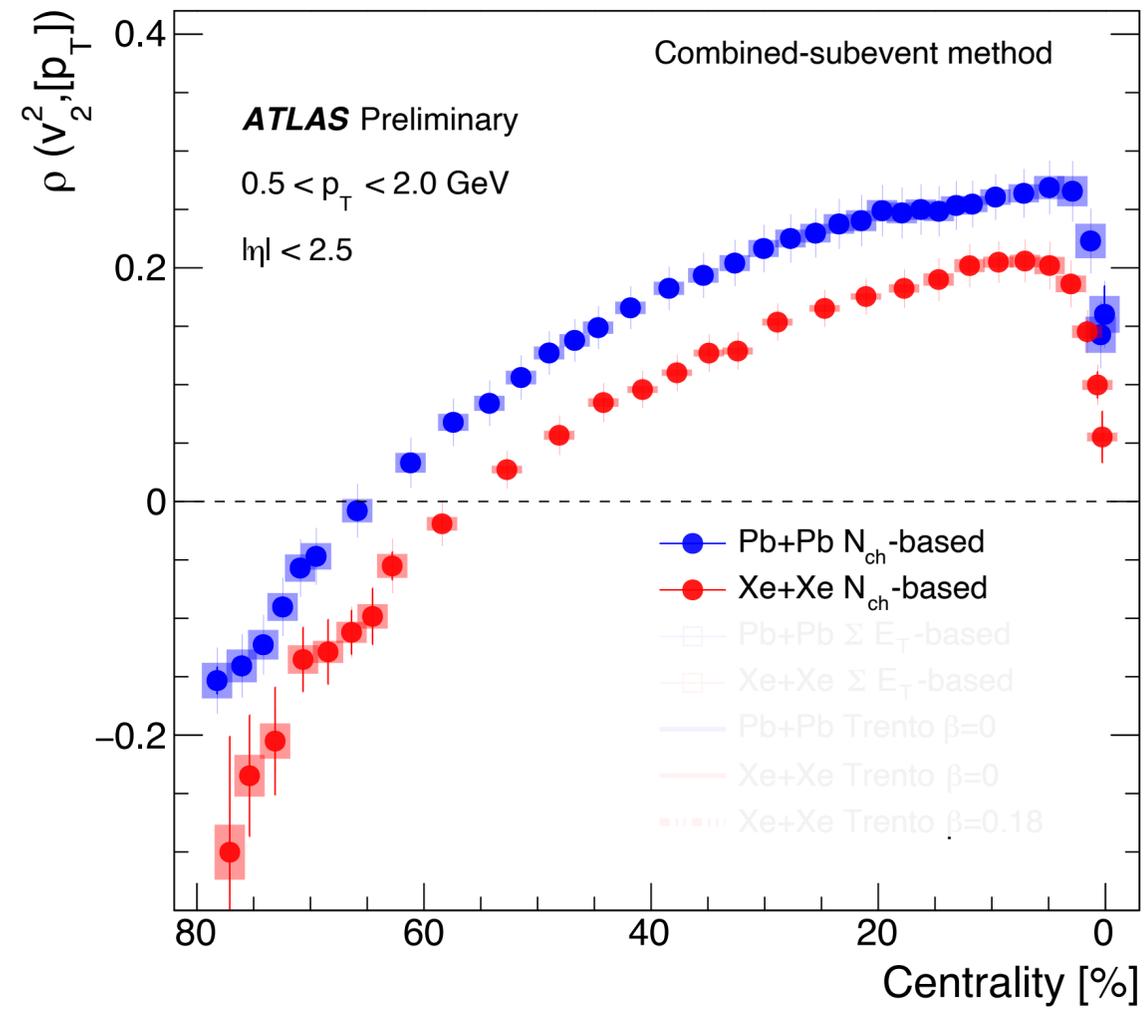
- $E_T$  and  $N_{ch}$  are mapped to centrality (based on  $E_T$  cuts)

- Significantly large centrality fluctuations in central and peripheral

- Less prominent in Xe+Xe but has similar trends - lower centrality resolution in Xe+Xe



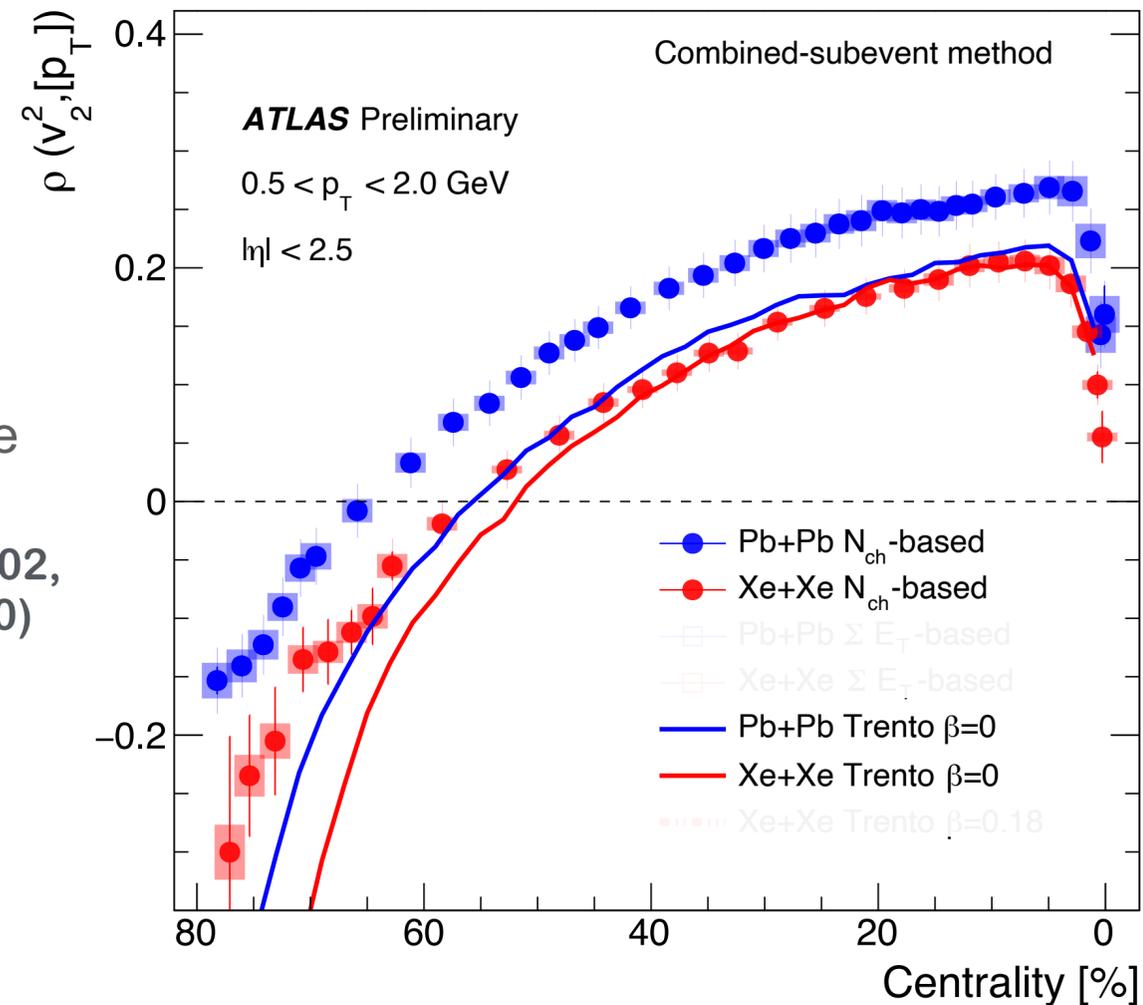
# Comparison with Theory models



● ATLAS  $N_{ch}$ -based

# Comparison with Theory models

## Trento



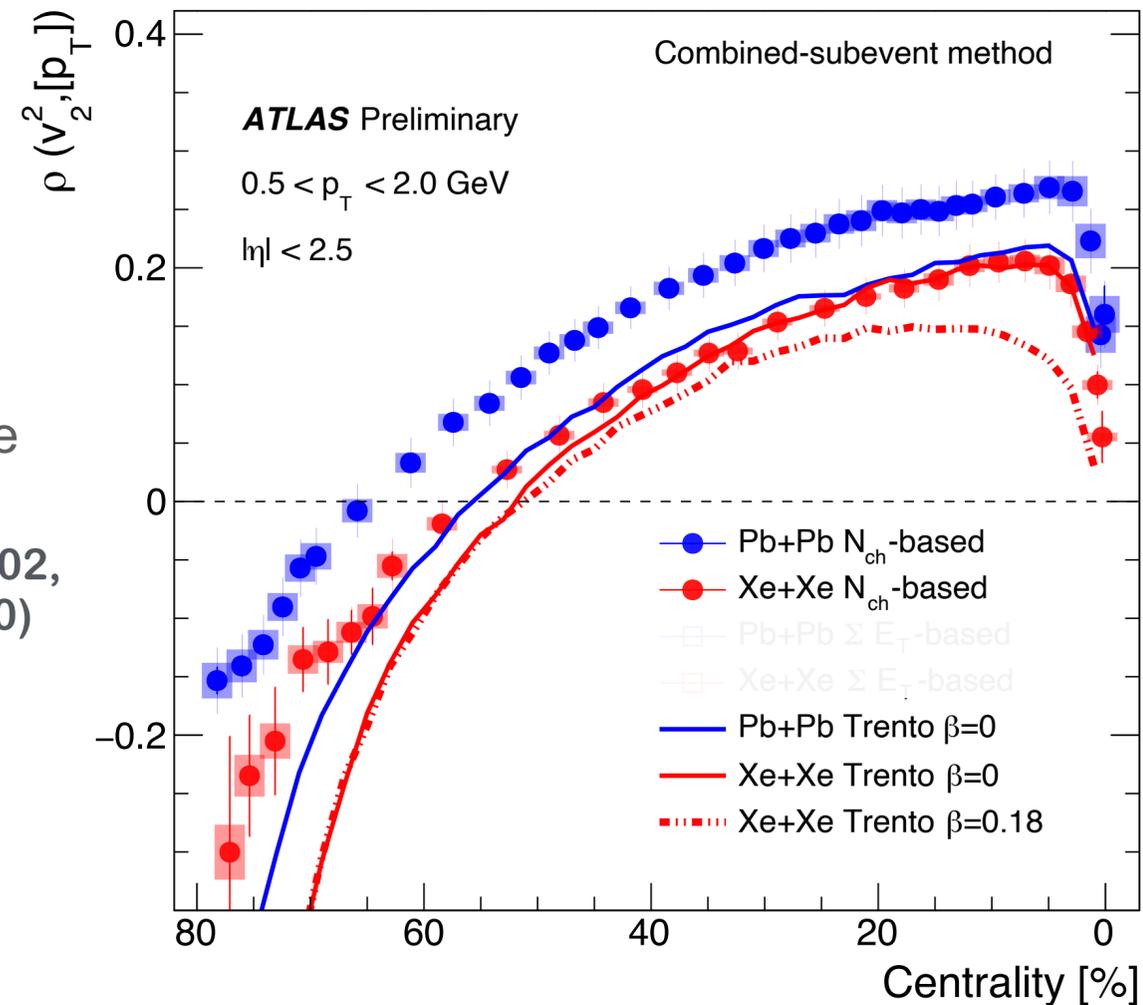
G. Giacalone

Phys. Rev. C 102,  
024901 (2020)

- ATLAS  $N_{ch}$ -based, Trento spherical
- Model captures centrality trends of data
- In contrast to data - little difference between Pb+Pb & Xe+Xe in the model

# Comparison with Theory models

## Trento



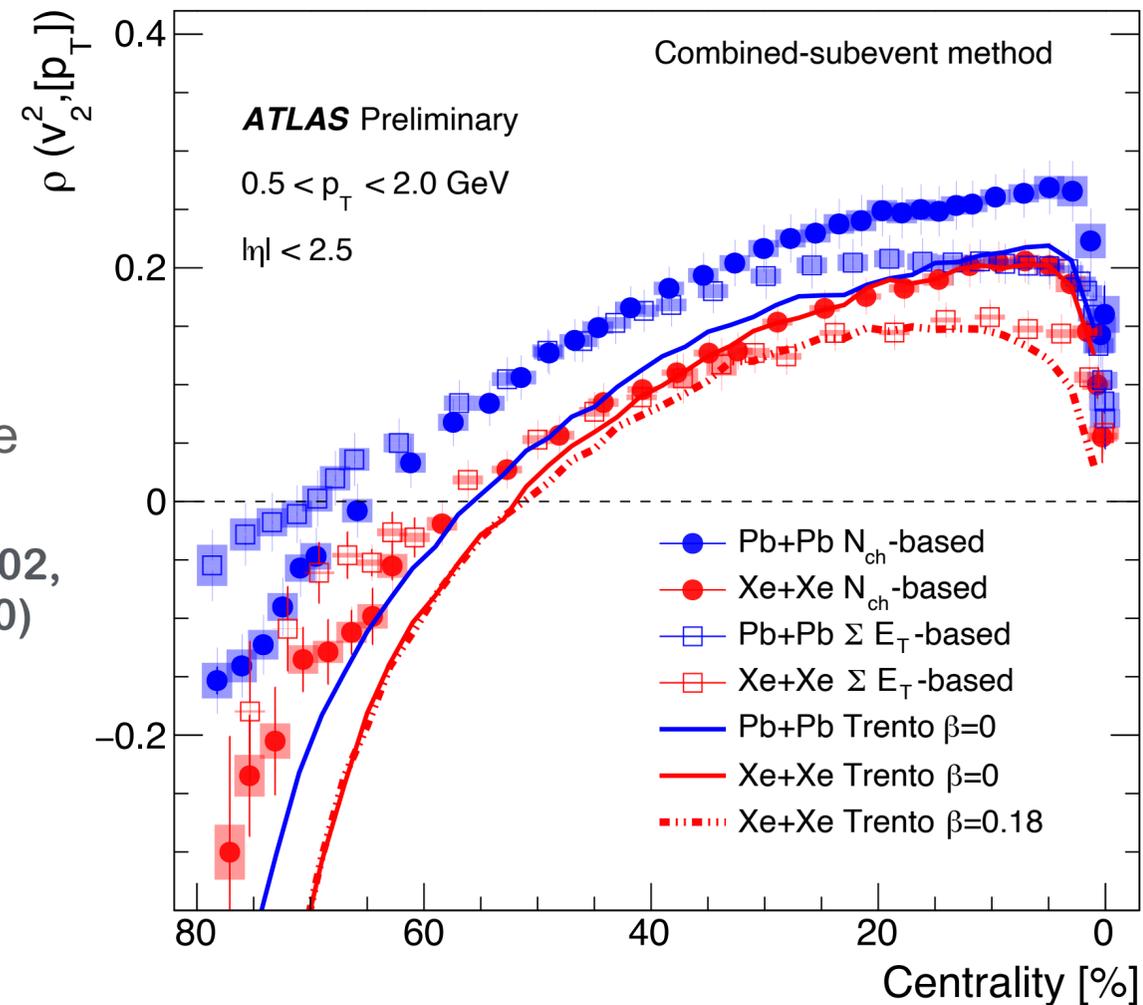
G. Giacalone

Phys. Rev. C 102,  
024901 (2020)

- ATLAS  $N_{ch}$ -based, Trento spherical, Trento deformed Xe+Xe
- Model captures centrality trends of data
- Deformed Xe+Xe - larger difference from Pb+Pb

# Comparison with Theory models

## Trento



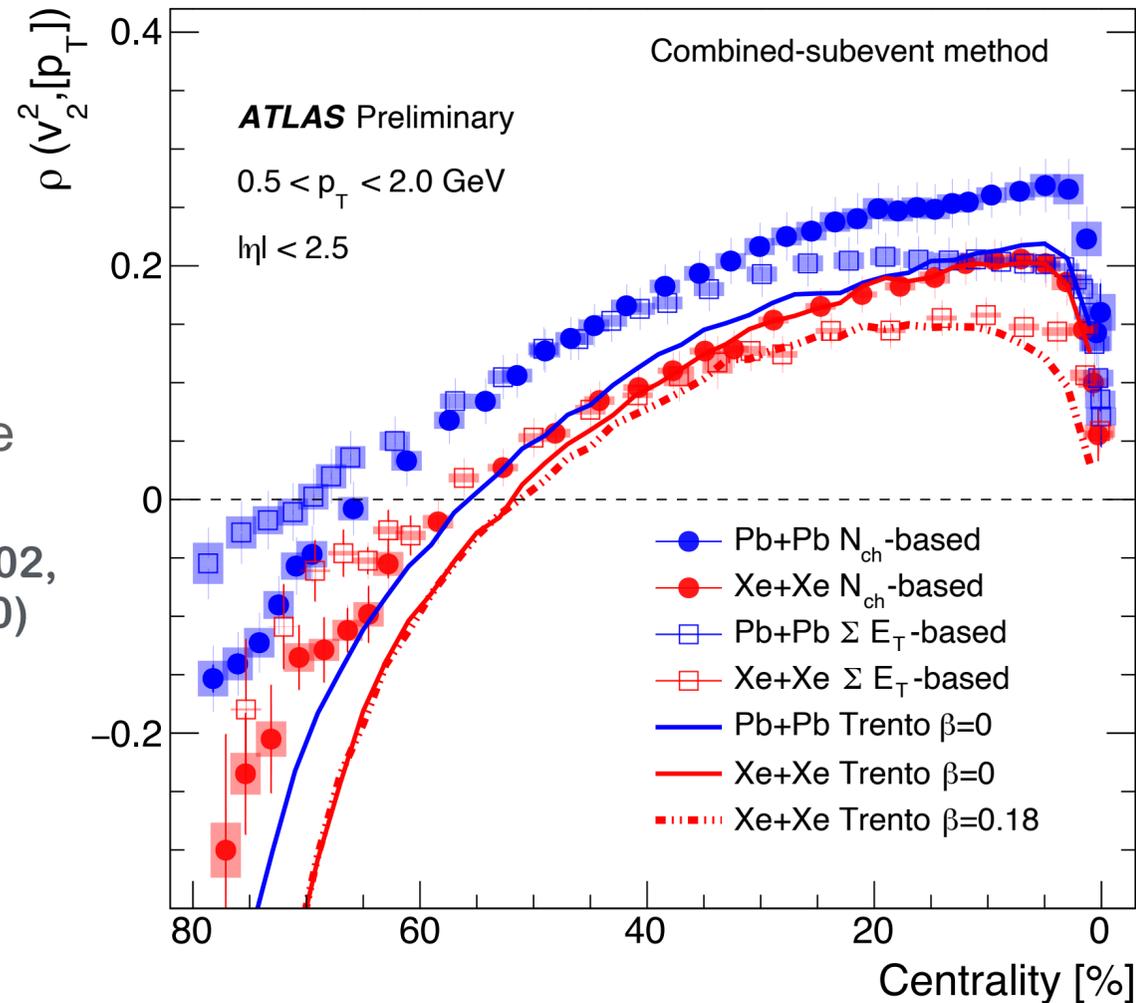
G. Giacalone

Phys. Rev. C 102,  
024901 (2020)

- ATLAS  $N_{ch}$ -based, Trento spherical, Trento deformed Xe+Xe, ATLAS  $E_T$ -based
- Results based on  $E_T$  - comparison to Trento better in central but worse in peripheral
- Trento model captures qualitative trends in data but cannot explain data quantitatively

# Comparison with Theory models

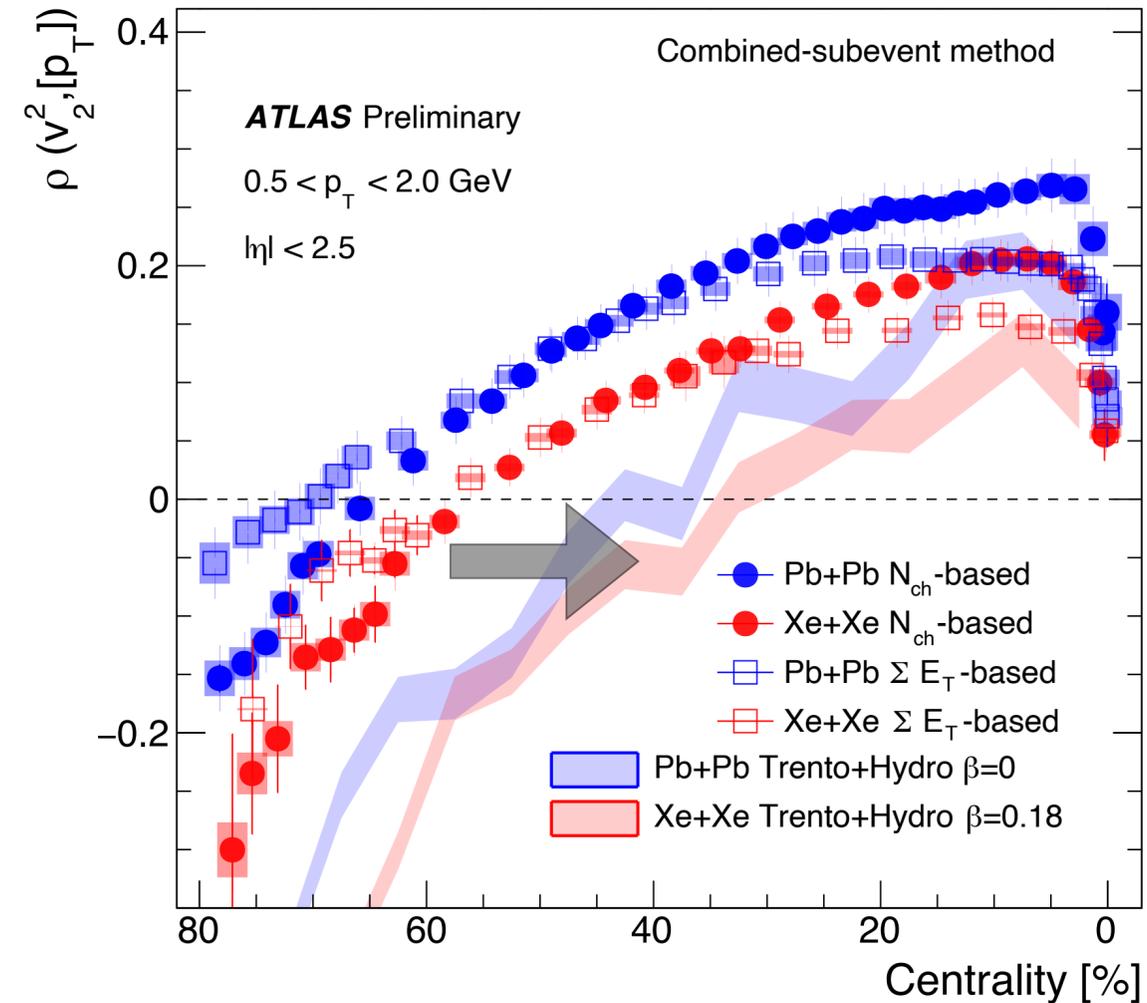
## Trento



G. Giacalone

Phys. Rev. C 102,  
024901 (2020)

## Trento+Hydro



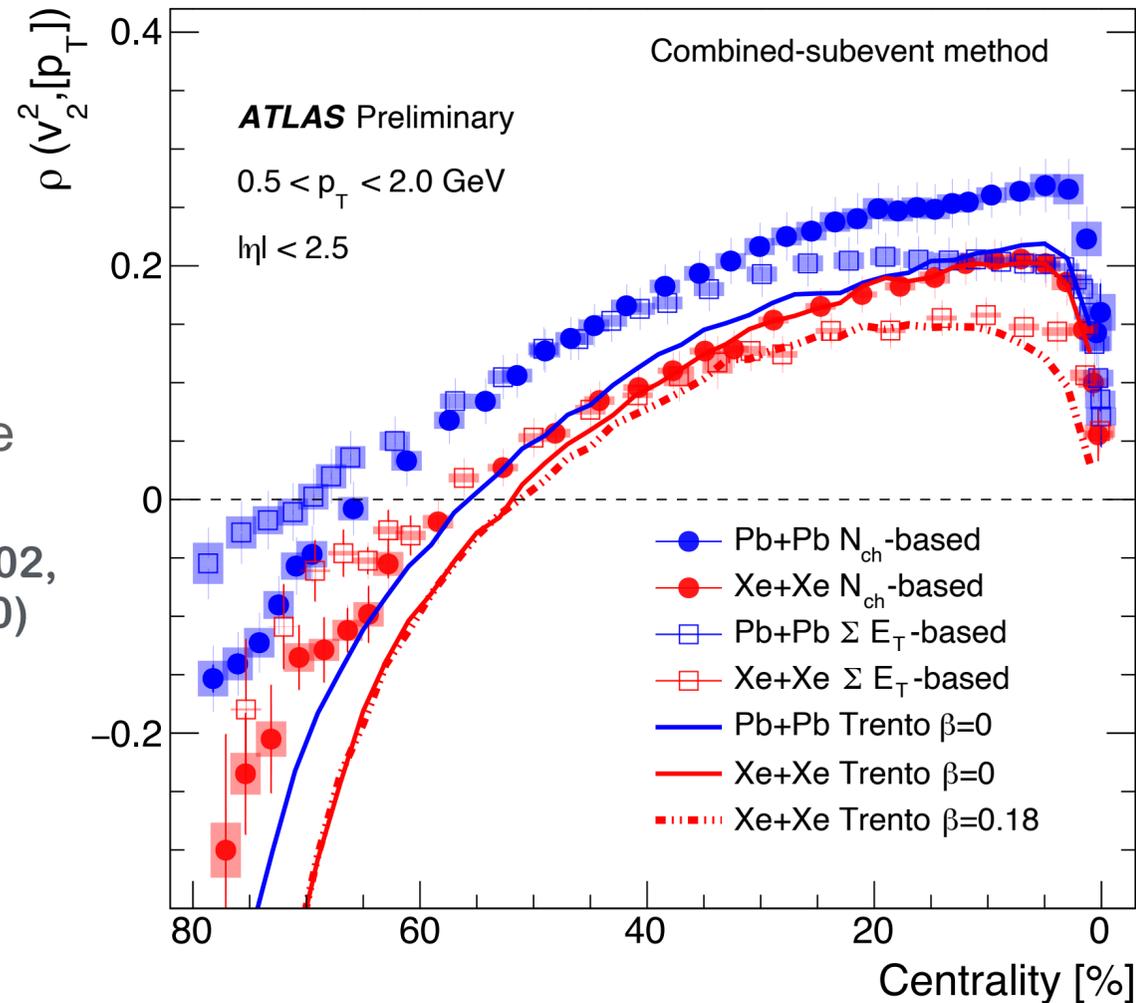
arXiv:2004.01765

- ATLAS  $N_{ch}$ -based, Trento spherical, Trento deformed Xe+Xe, ATLAS  $E_T$ -based
- Results based on  $E_T$  - comparison to Trento better in central but worse in peripheral
- Trento model captures qualitative trends in data but cannot explain data quantitatively

- Turning on final state hydrodynamic calculation
- Agreement with data becomes worse - shift of sign-change to lower centrality

# Comparison with Theory models

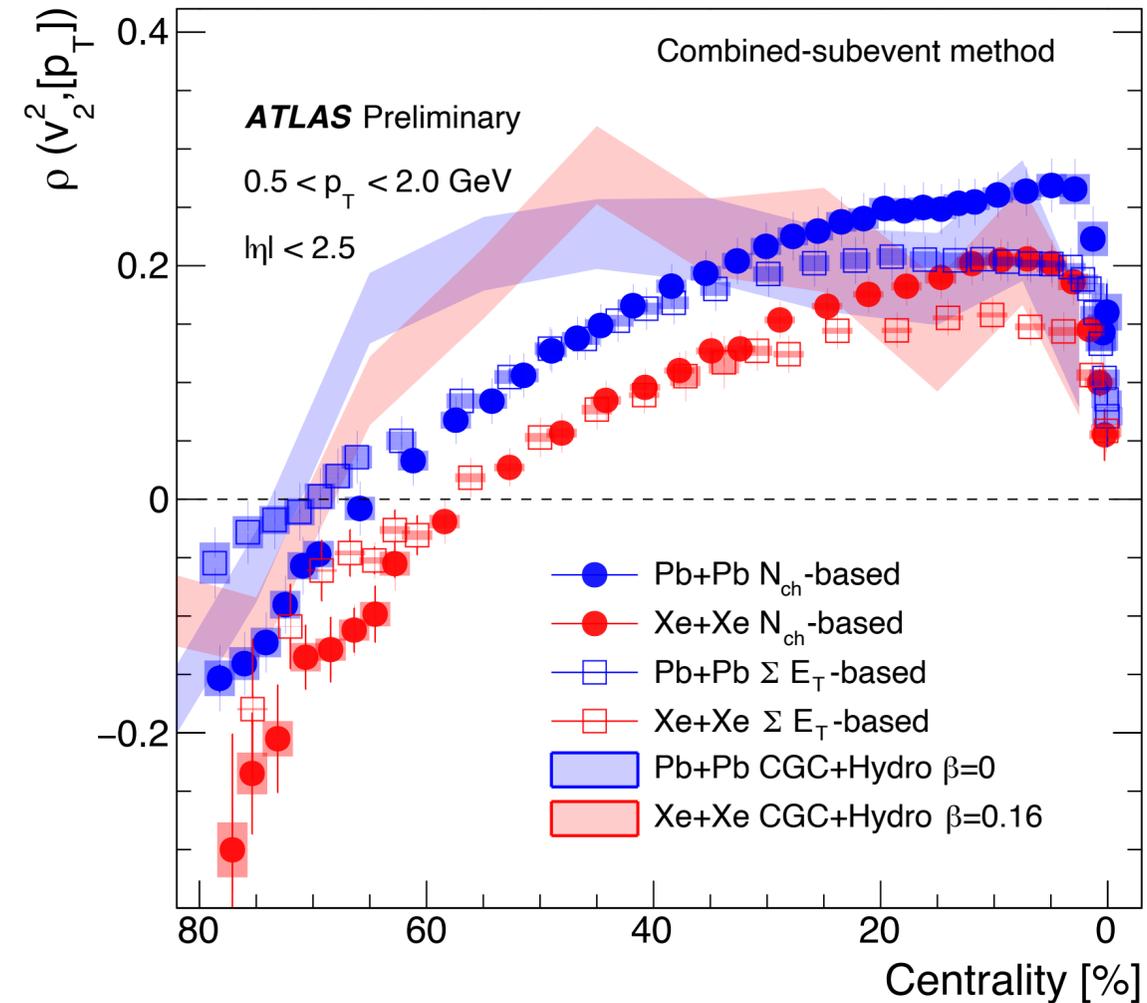
## Trento



G. Giacalone

Phys. Rev. C 102,  
024901 (2020)

## CGC+Hydro



B. Schenke

Phys. Rev. C 102,  
034905 (2020)

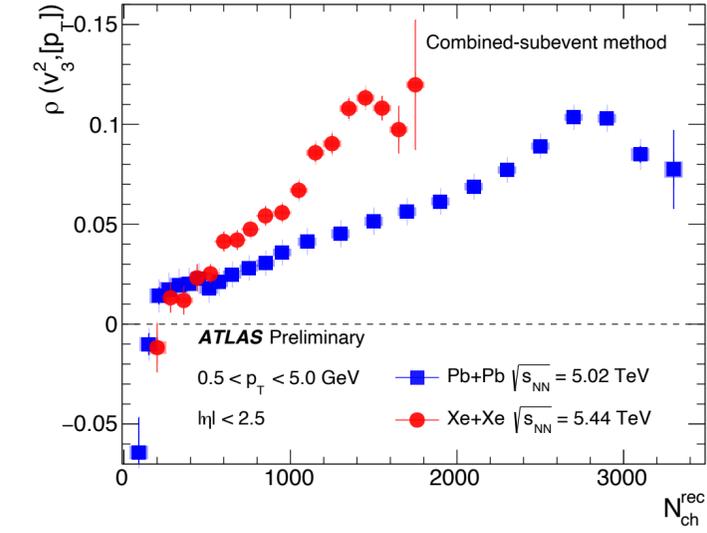
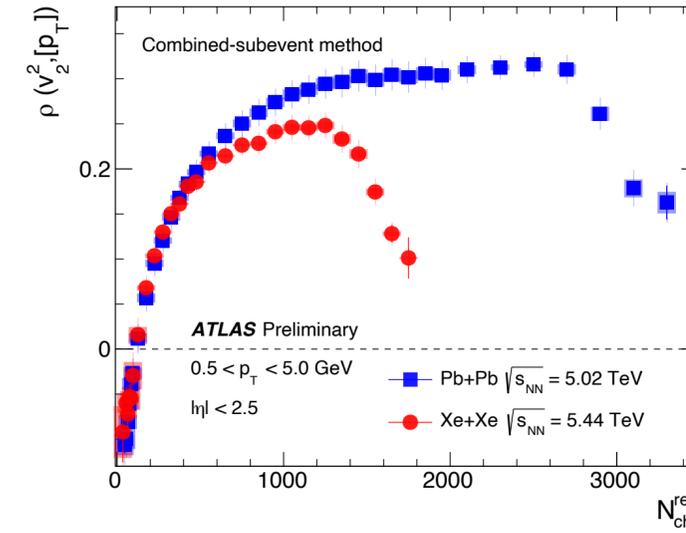
Phys. Rev. Lett. 125,  
192301 (2020)

- ATLAS  $N_{ch}$ -based, Trento spherical, Trento deformed Xe+Xe, ATLAS  $E_T$ -based
- Results based on  $E_T$  - comparison to Trento better in central but worse in peripheral
- Trento model captures qualitative trends in data but cannot explain data quantitatively

- Different hydrodynamic calculation with CGC initial conditions
- Does not see any significant difference between Pb+Pb and Xe+Xe
- Better agreement but still cannot describe data quantitatively

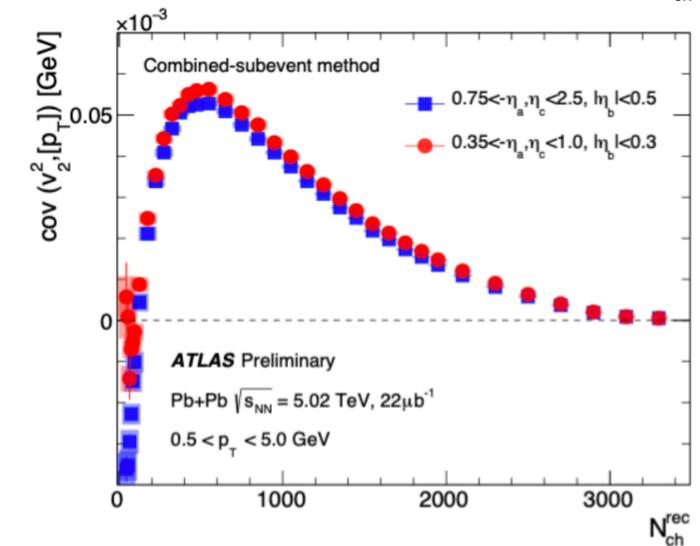
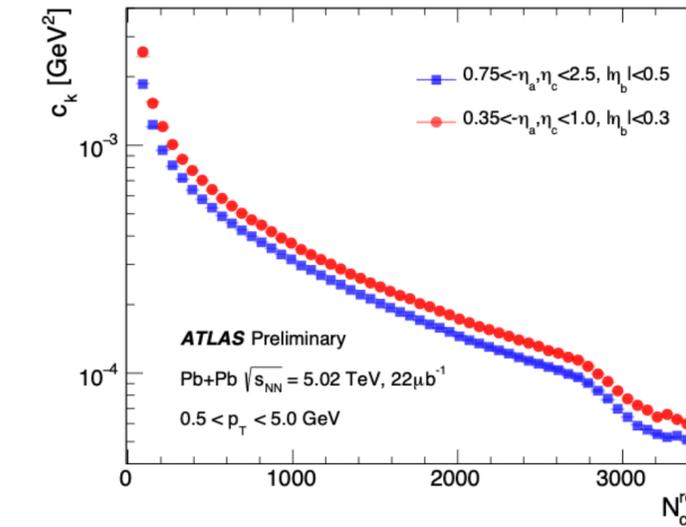
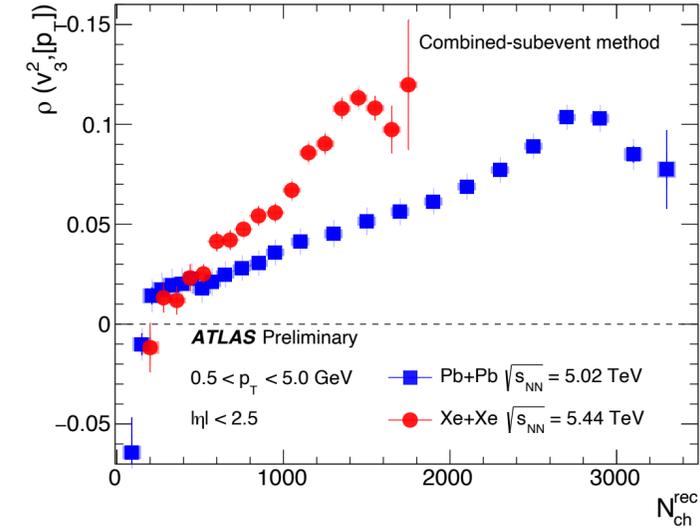
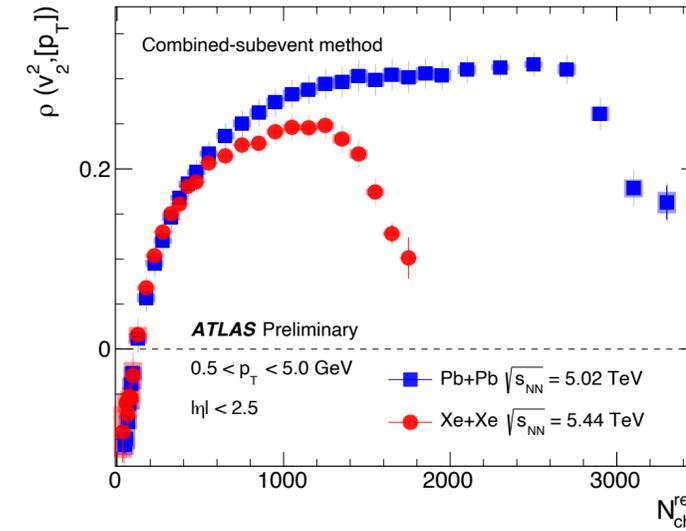
# Summary

- Flow and mean-momentum correlations show strong system-size dependence
  - Smaller magnitude of  $\rho_{v_n}$  in XeXe for  $n=2$
  - Larger magnitude in XeXe for  $n=3$



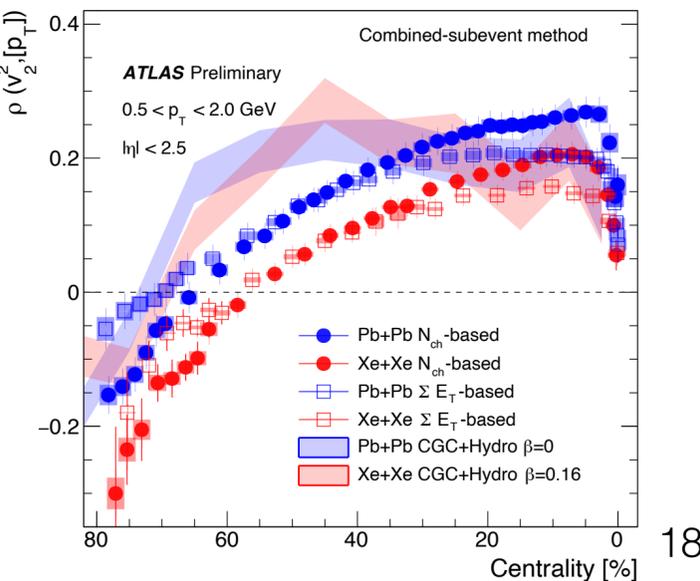
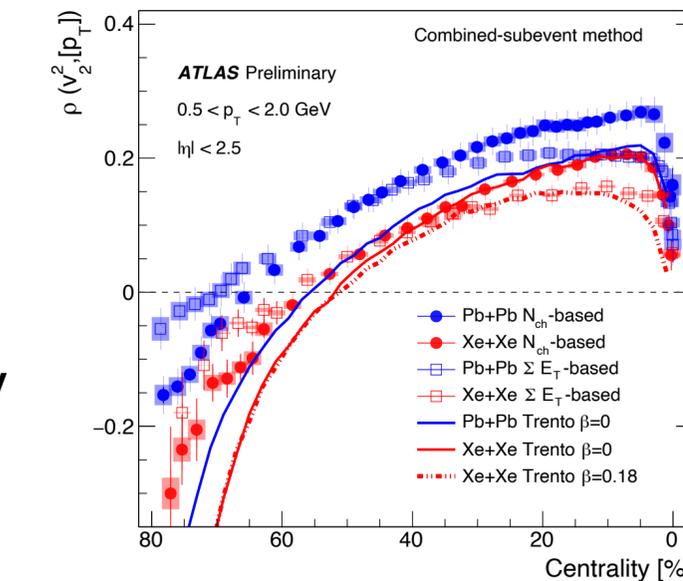
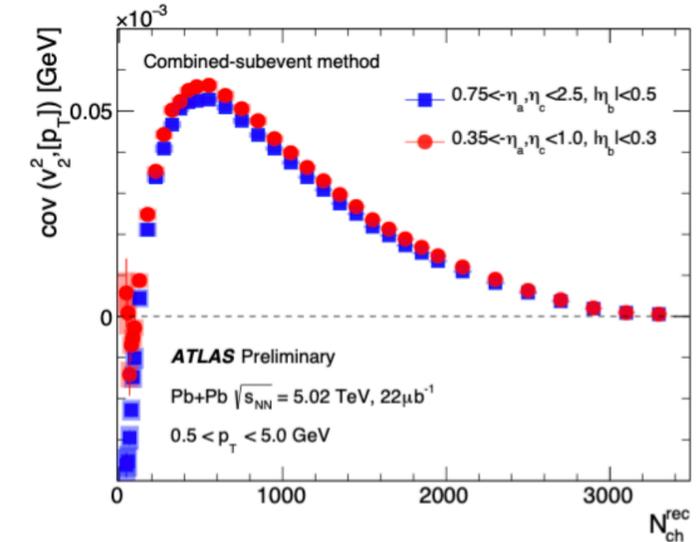
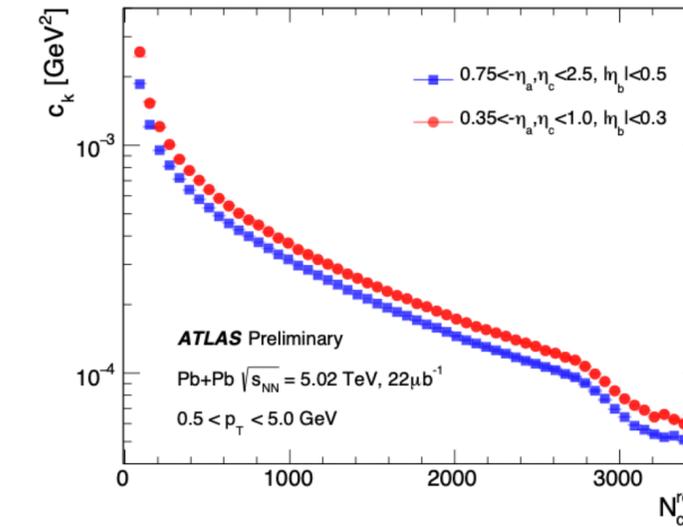
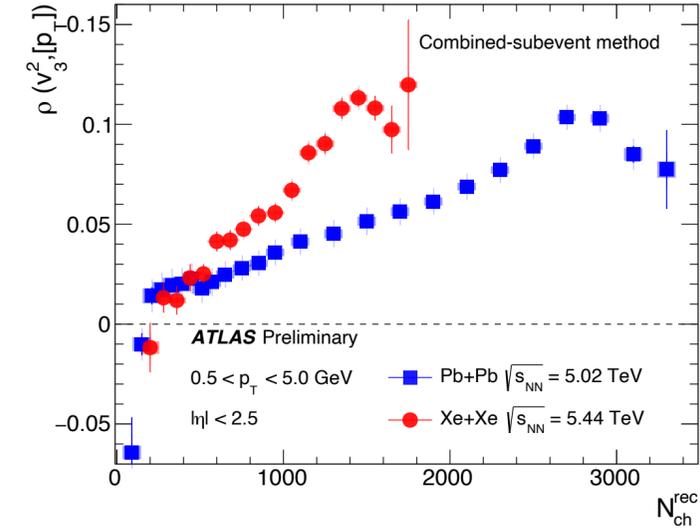
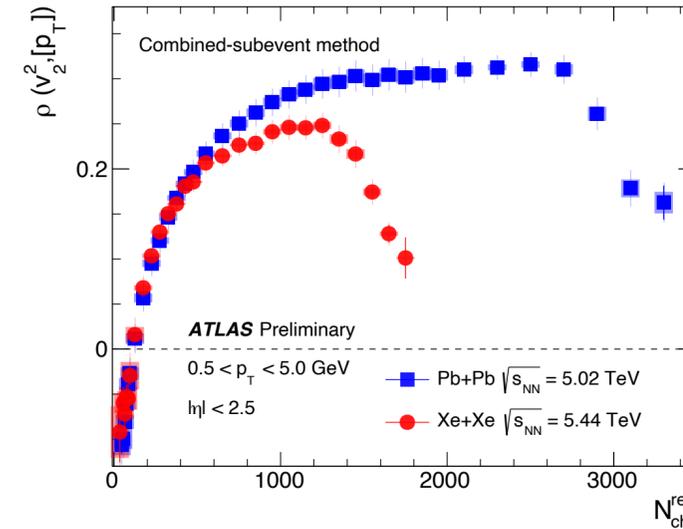
# Summary

- Flow and mean-momentum correlations show strong system-size dependence
  - Smaller magnitude of  $\rho_{v_n}$  in XeXe for  $n=2$
  - Larger magnitude in XeXe for  $n=3$
- Sensitive to  $p_T$  and  $\eta$  ranges
  - Increase in  $\rho_{v_n}$  with more high  $p_T$  particles
  - Larger variances for smaller  $\eta$  range ( $|\eta| < 1$ )
  - Covariance depends weakly on  $\eta$  range selection



# Summary

- Flow and mean-momentum correlations show strong system-size dependence
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  - Larger variances for smaller  $\eta$  range ( $|\eta| < 1$ )
  - Covariance depends weakly on  $\eta$  range selection
- Significant Centrality fluctuations -  $N_{ch}$  vs  $E_T$  binnings
- Compared results with theory
  - Trento model captures qualitative trends in data
  - Models do not explain the measurements quantitatively



Poster by Somadutta Bhatta - Tuesday 12th

# Backup

# Observable

- Pearson's Correlation coefficient

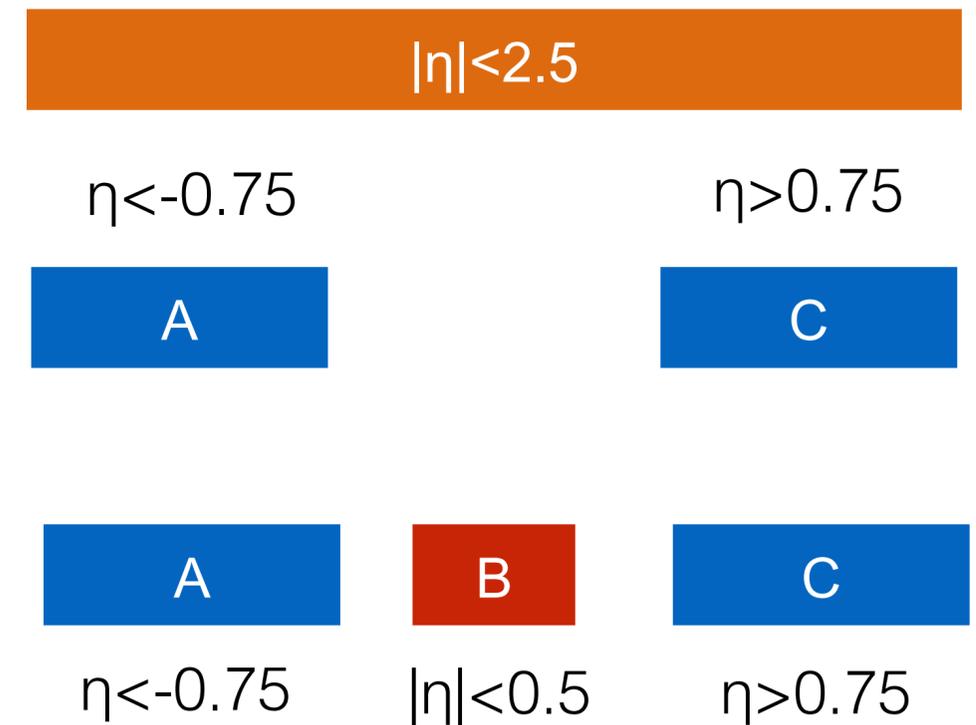
$$\rho(v_n\{2\}^2, [p_T]) = \frac{\text{cov}(v_n\{2\}^2, [p_T])}{\sqrt{\text{var}(v_n\{2\}^2)c_k}},$$

$$\delta p_T = p_T - [p_T]$$

$$\text{cov}(v_n\{2\}^2, [p_T]) = \langle\langle v_n^2 \delta p_T \rangle\rangle, \quad \text{var}(v_n\{2\}^2) = \langle v_n^4 \rangle - \langle v_n^2 \rangle^2, \quad c_k = \langle\langle \delta p_T \delta p_T \rangle\rangle$$

- Covariance - from three methods

- Standard - full  $\eta$ -range  $|\eta| < 2.5$
- 2-SE - A and C with  $\Delta\eta = 1.5$ ,  $[p_T]$  from A+C
- 3-SE - A and C with  $\Delta\eta = 1.5$ ,  $[p_T]$  from B ( $|\eta| < 0.5$ )



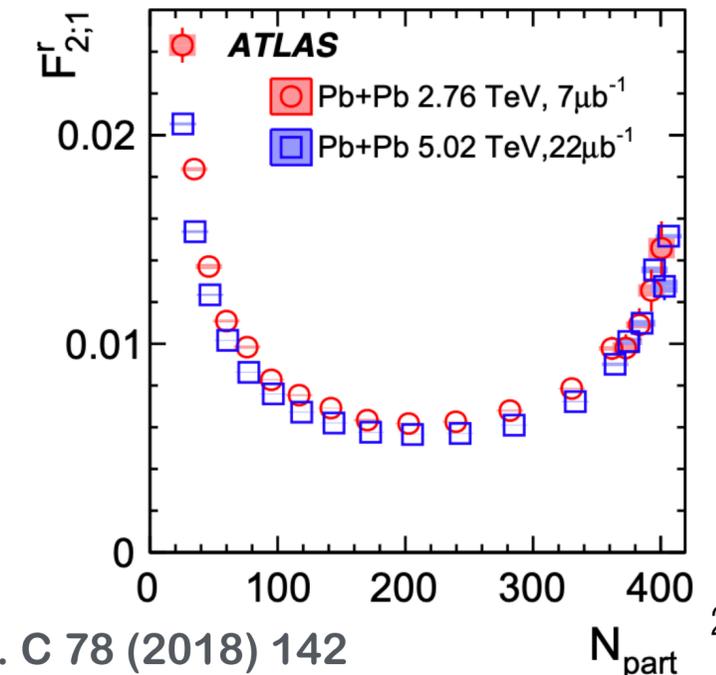
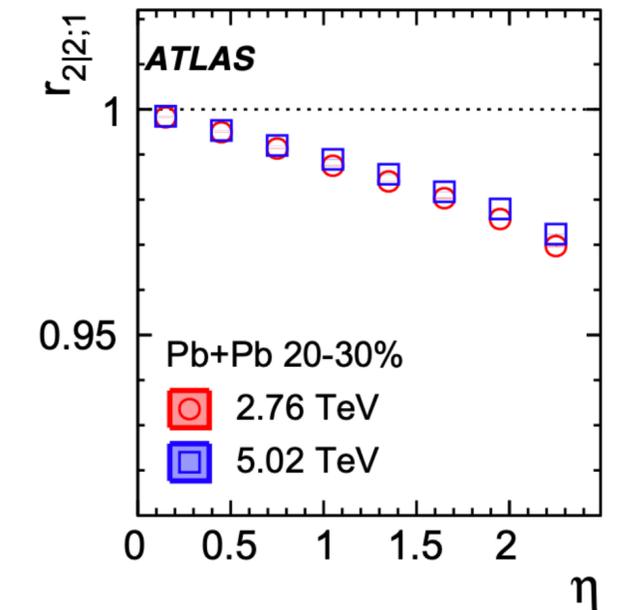
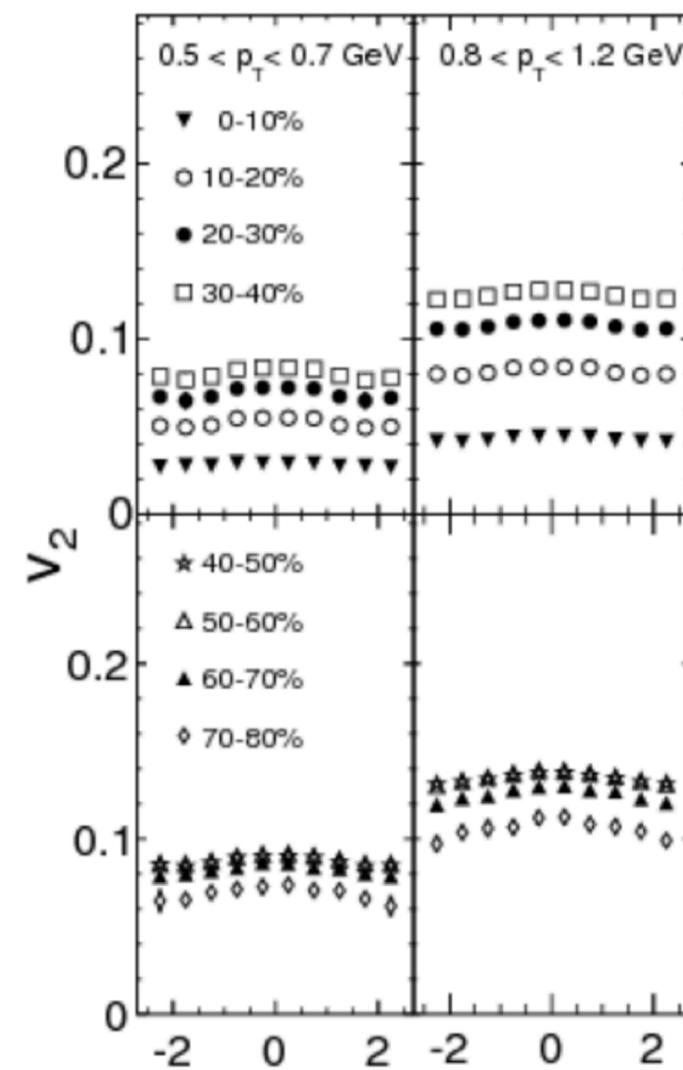
- $C_k$  - Standard -  $|\eta| < 2.5$

- Variance  $v_n$ :  $\text{var}(v_n\{2\}^2) = c_n\{4\}_{\text{standard}} + c_n\{2\}_{\text{two-sub}}^2$

# Other physics sources

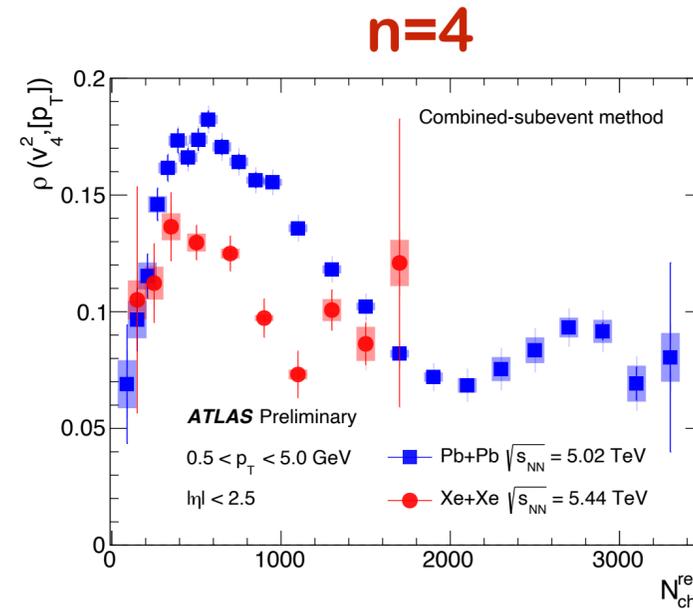
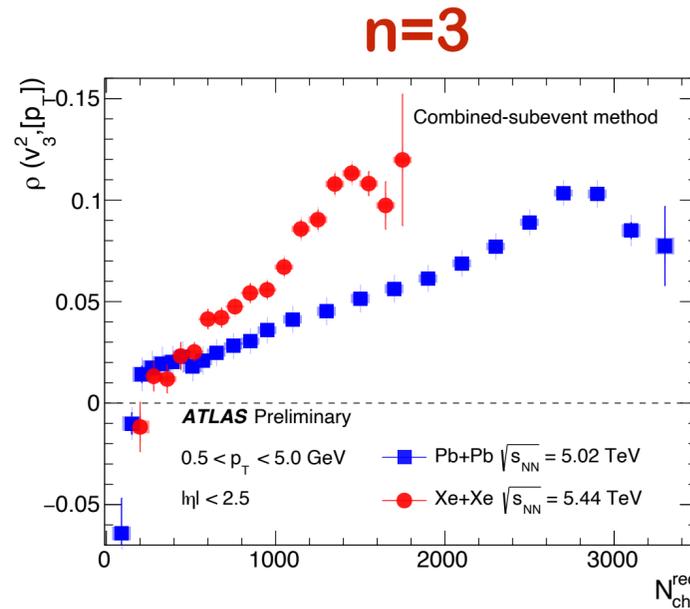
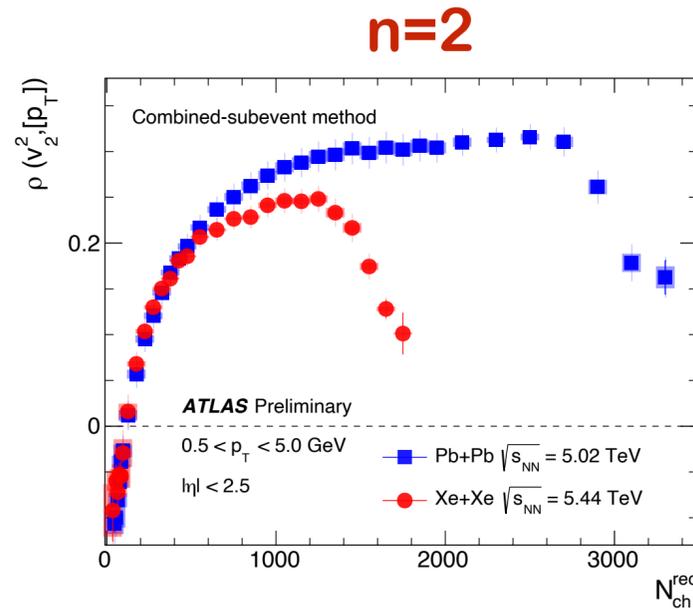
- Non-flow
  - Short-range non-flow (single jets, resonance decays, etc.) suppressed in subevent methods
  - Long-range non-flow (dijets) - contribute to atmost 2-subevents and scale as  $1/\sqrt{N}$
- Eta-dependence of  $v_n$ 
  - $v_n$  smaller at larger eta
  - Stronger dependence in peripheral
- $v_n$  decorrelation
  - Smaller signal at larger  $\Delta\eta$
  - Stronger in central and peripheral
- Flow and non-flow depends on  $\eta$  range, location of subevents and gap.

non-flow (dijets)



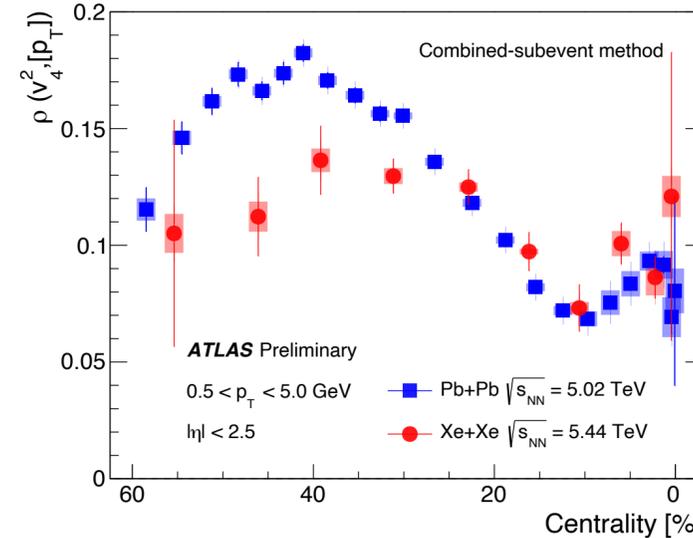
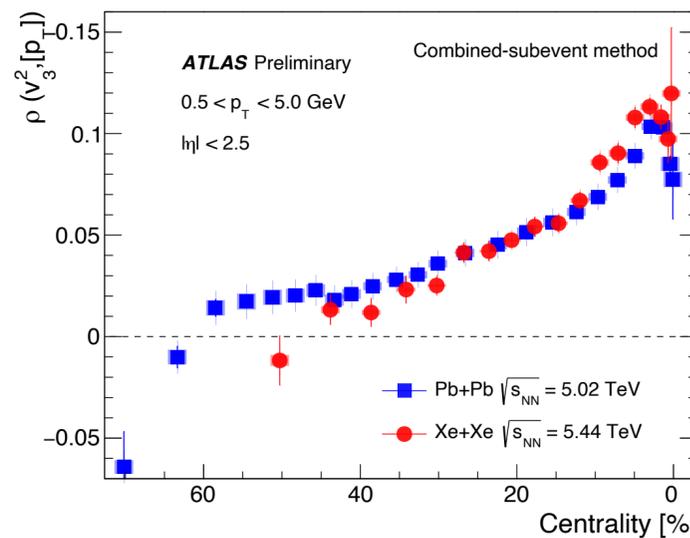
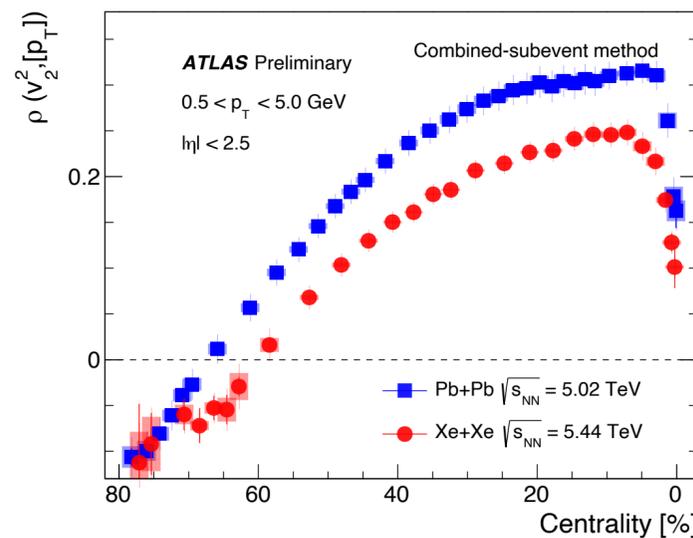
# Comparisons - Xe+Xe vs Pb+Pb

$N_{ch}$



Size

Cent

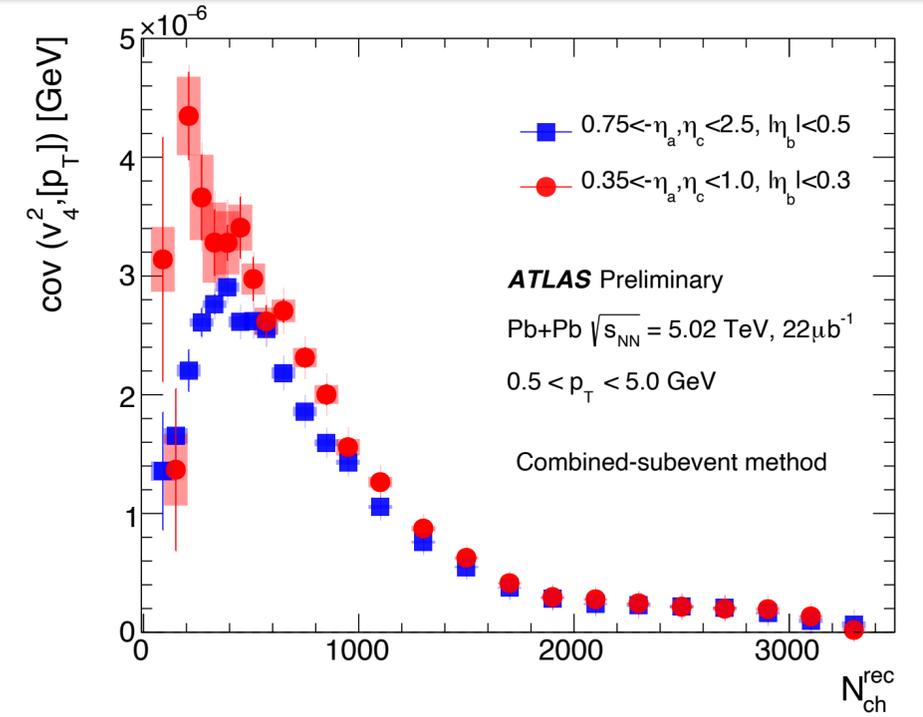
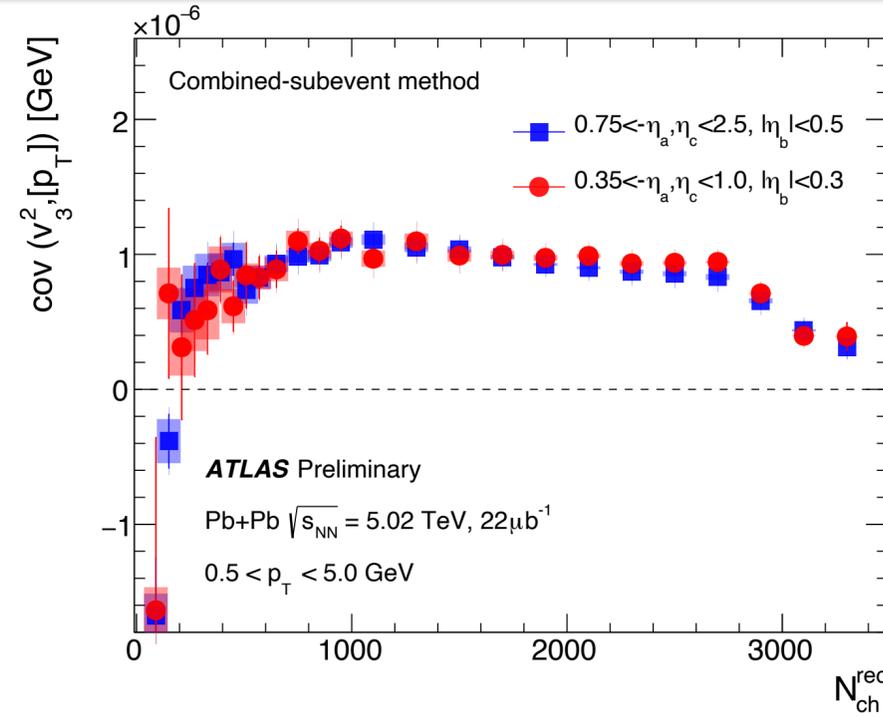
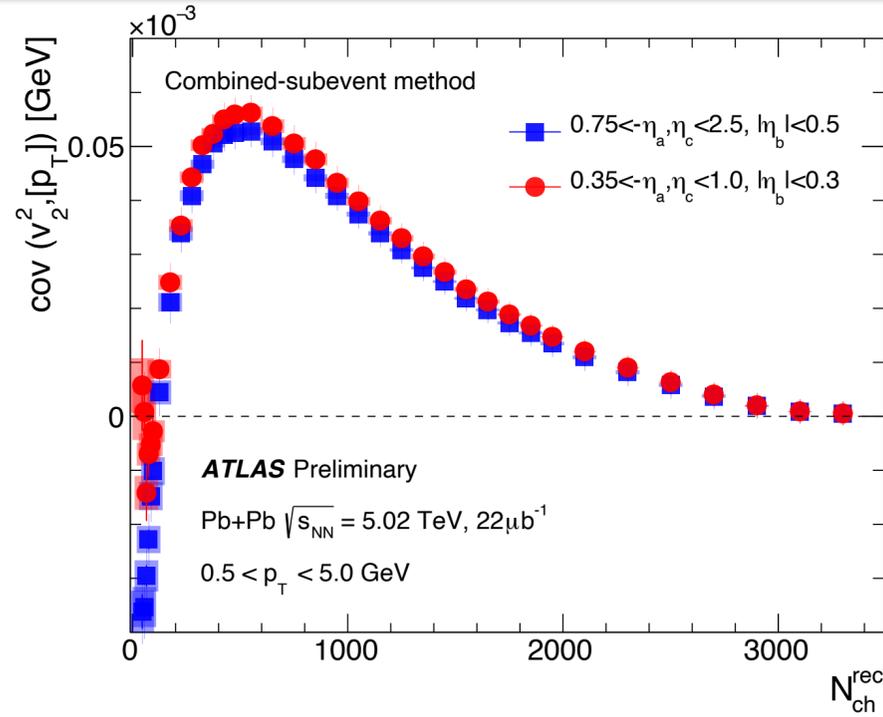


Shape

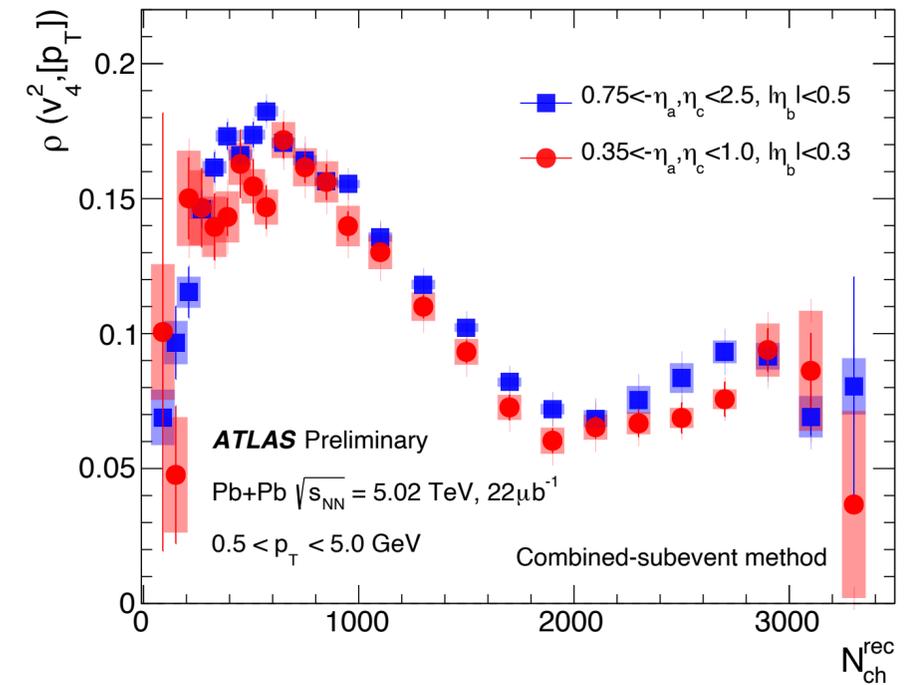
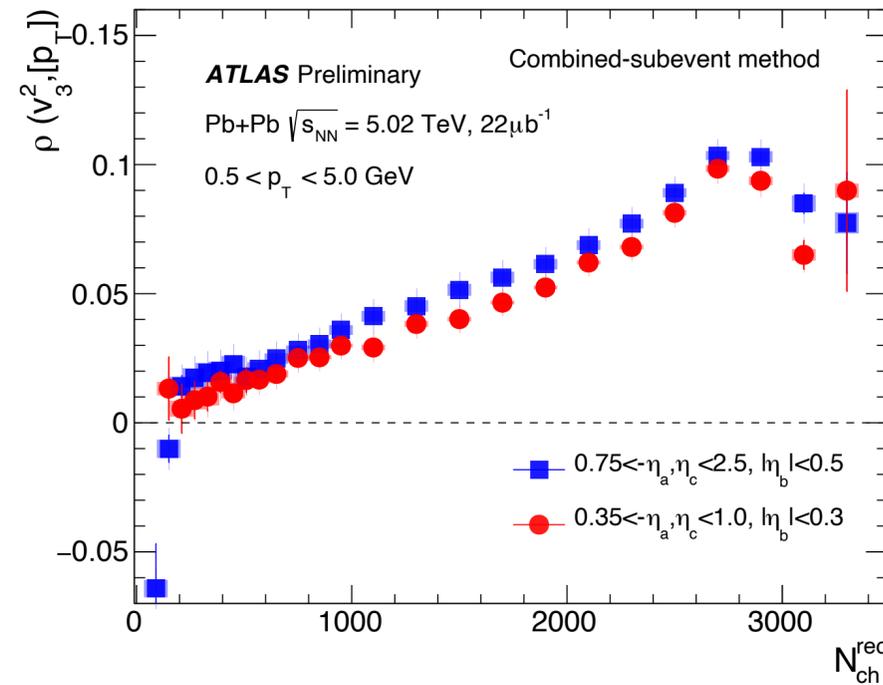
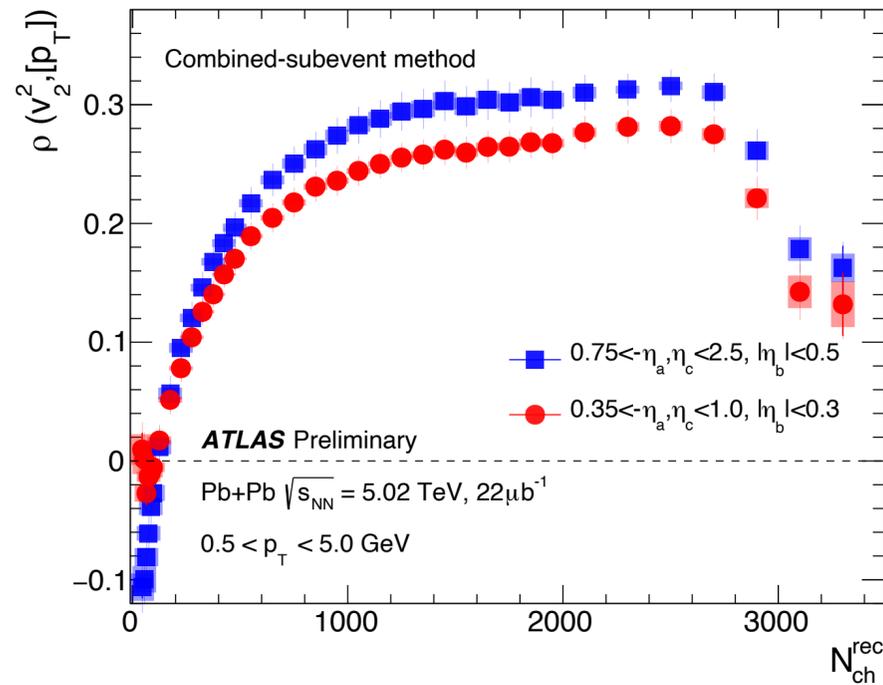
- Both Xe+Xe and Pb+Pb go -ve in very low  $N_{ch}$  for  $n=2$
- **Smaller** magnitude in Xe+Xe for  $n=2$  &  $n=4$
- **Larger** magnitude in Xe+Xe for  $n=3$  due to larger fluctuations in smaller system
- As a function of centrality,  $\rho_2$  is smaller in Xe+Xe but  $\rho_3$  and  $\rho_4$  are comparable

# $\eta$ -dependence in Pb+Pb

Cov

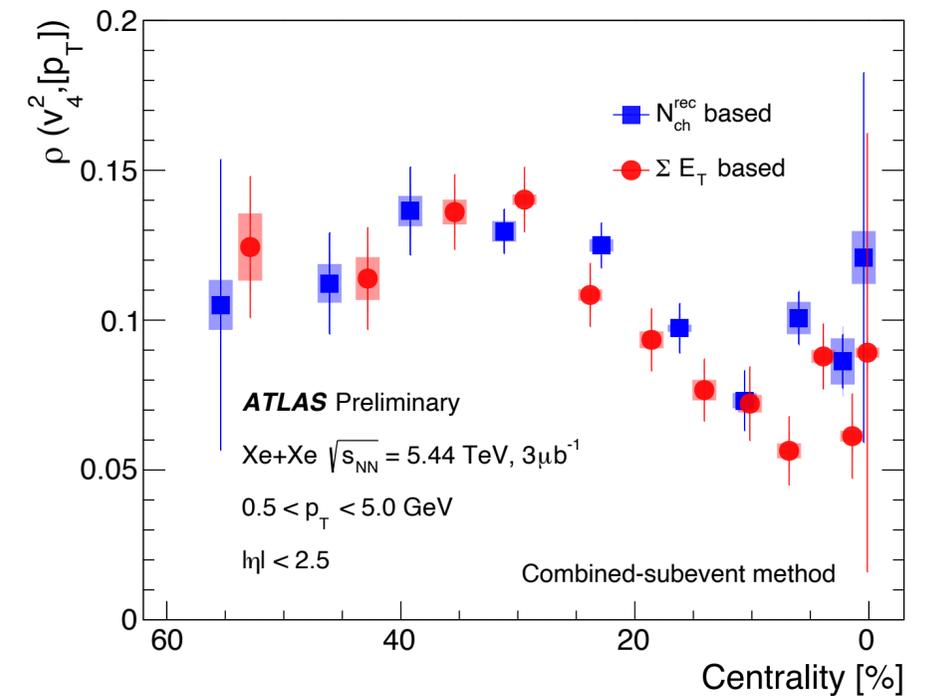
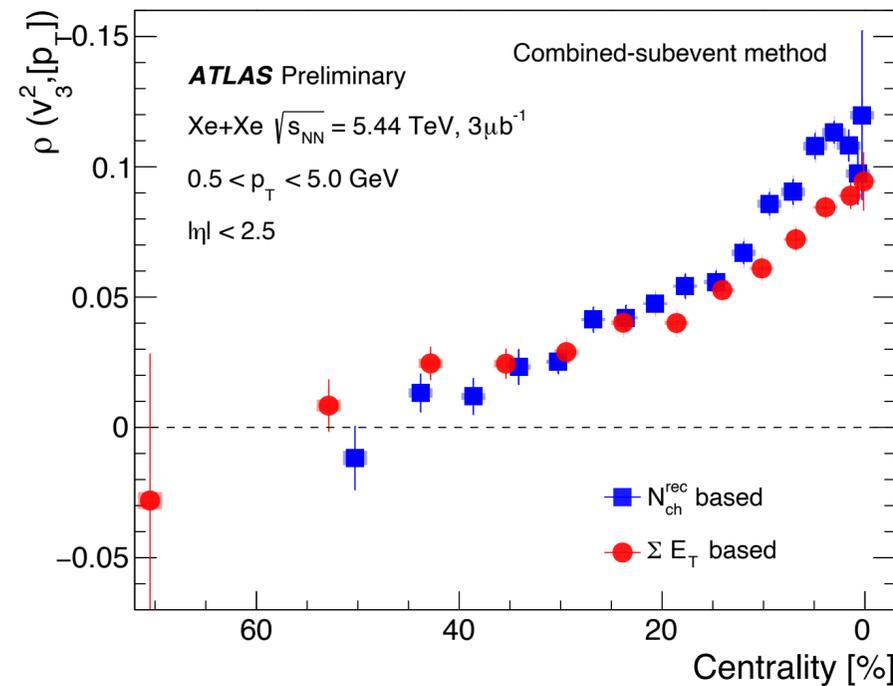
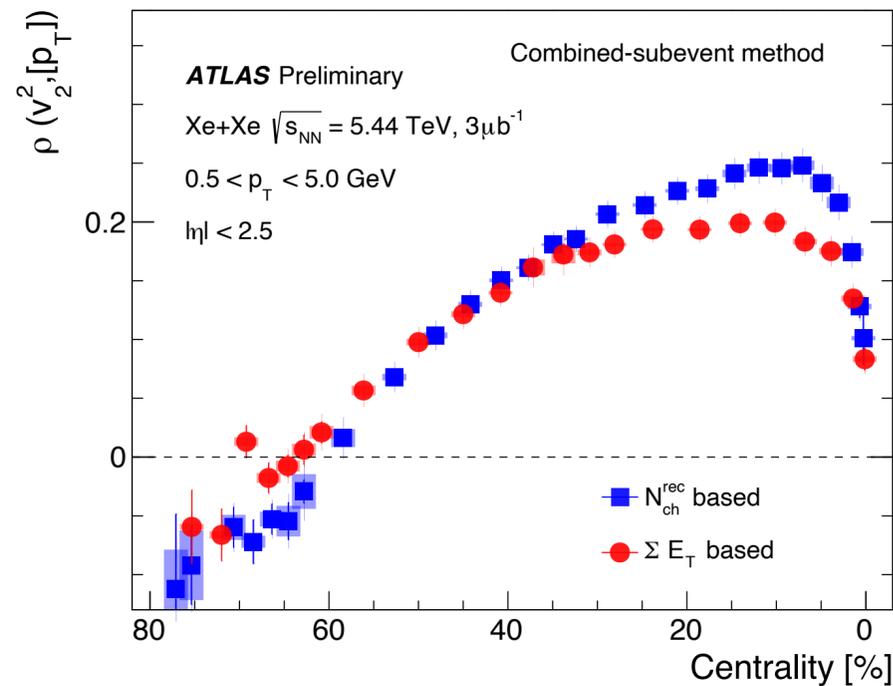
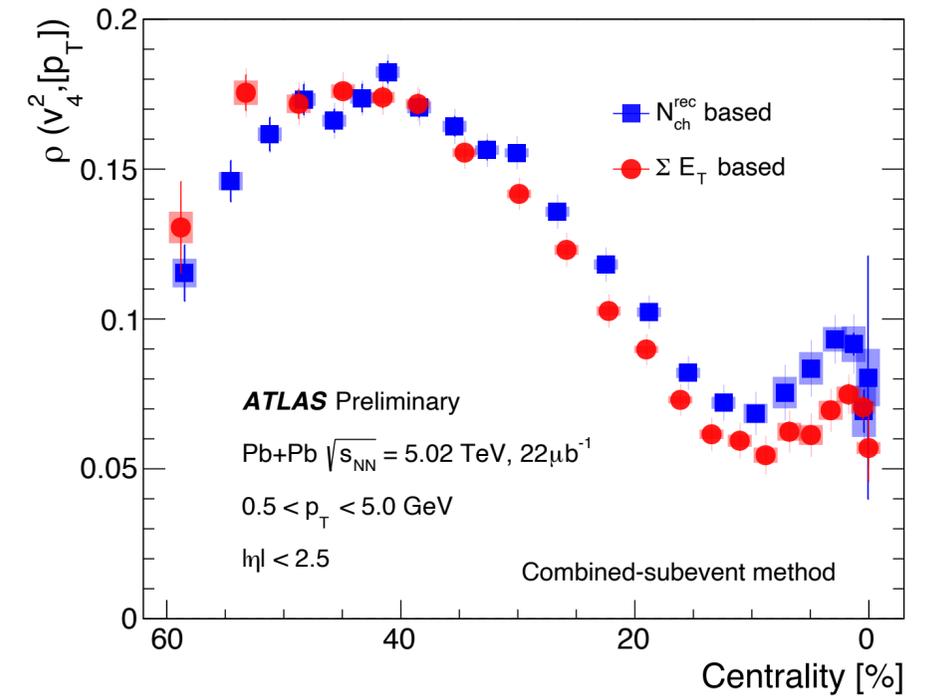
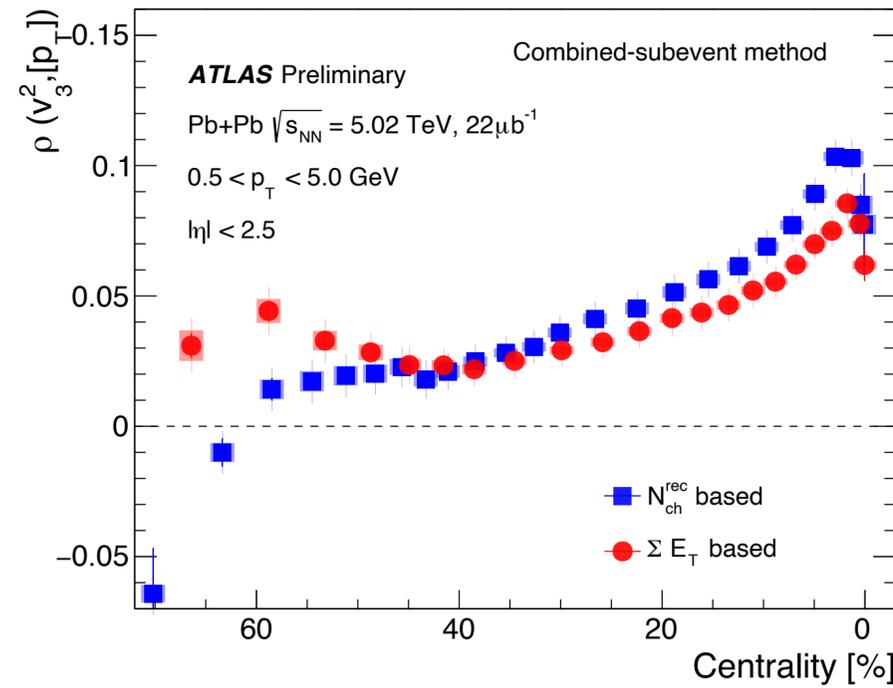
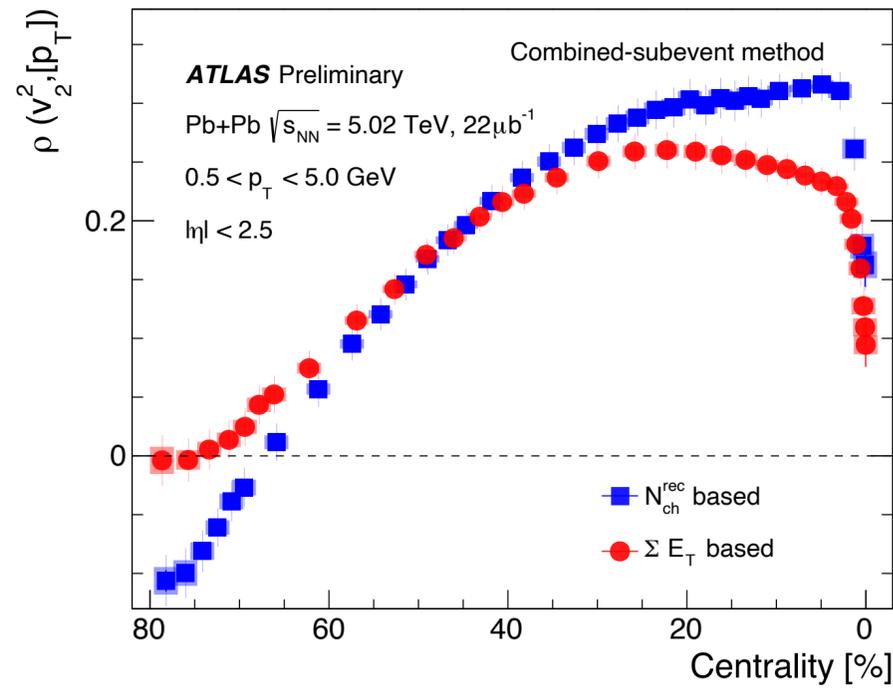


$\rho$



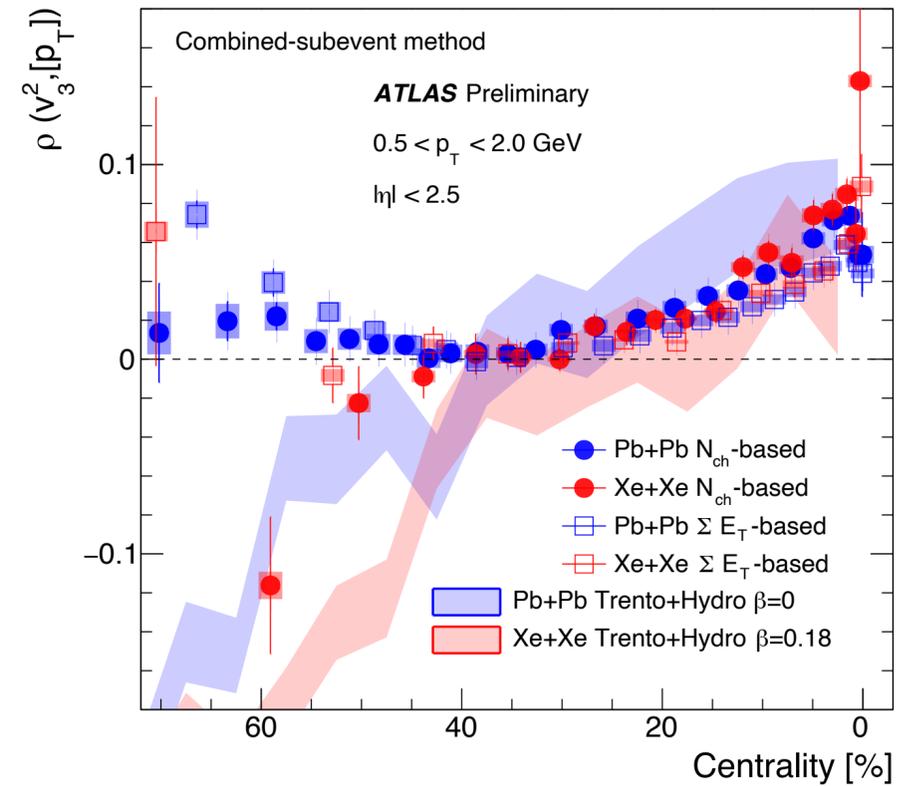
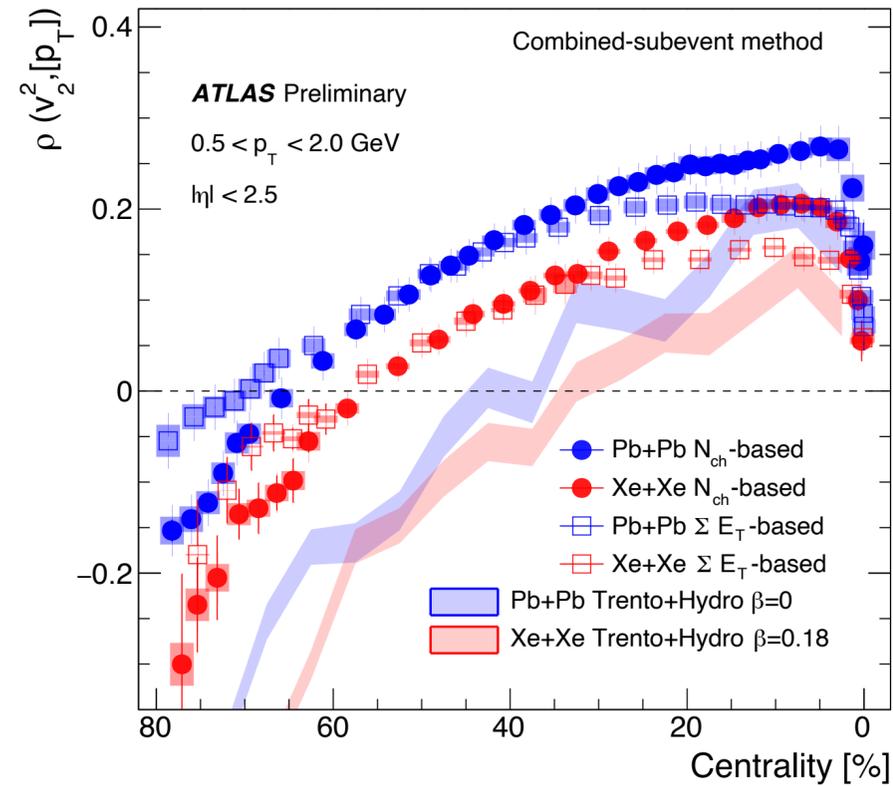
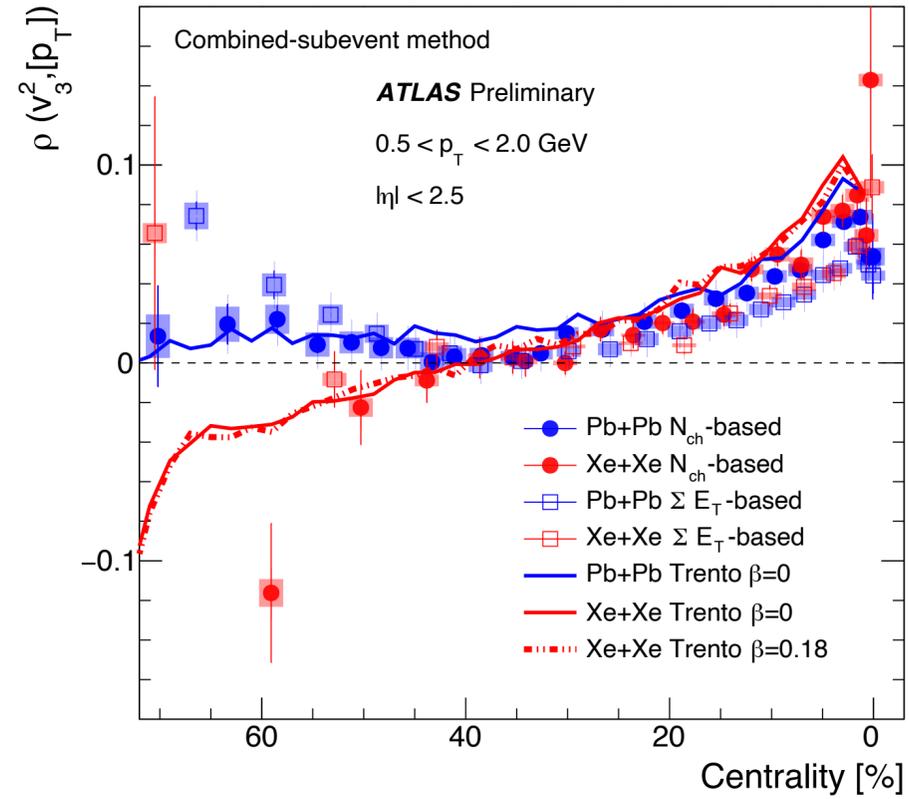
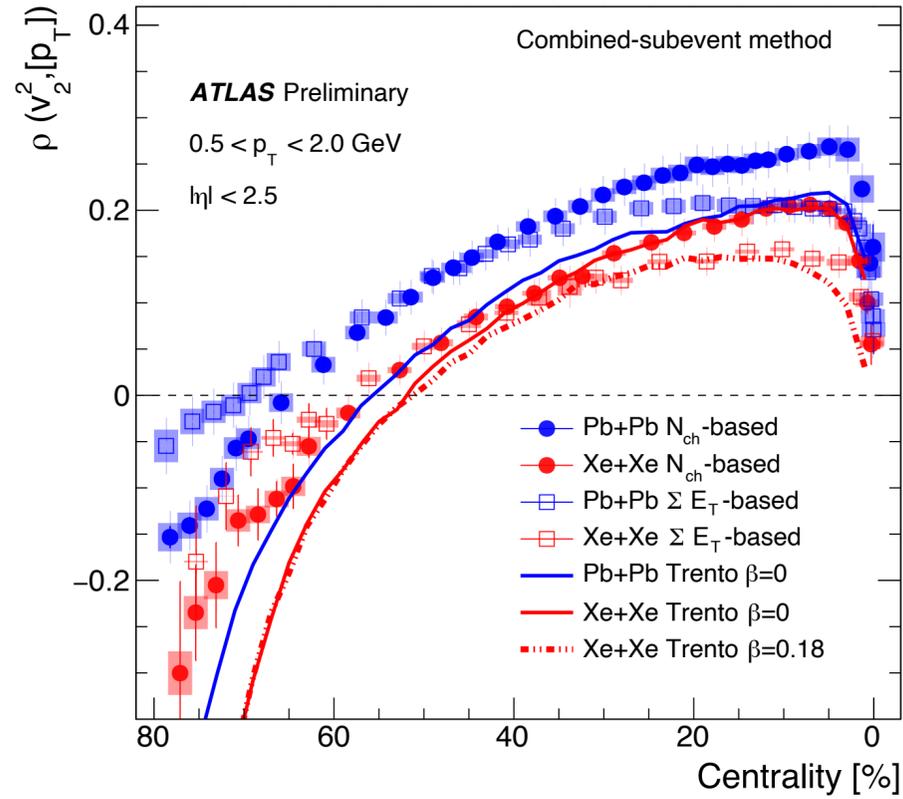
- Covariances show good agreement between eta-ranges except for  $n=4$  at low  $N_{ch}$
- $\rho$  is systematically smaller for  $|\eta| < 2.5$  due to smaller  $c_k$  and  $\text{var}(v_n)$

# Centrality fluctuations in $v_n$ - $[p_T]$ correlation

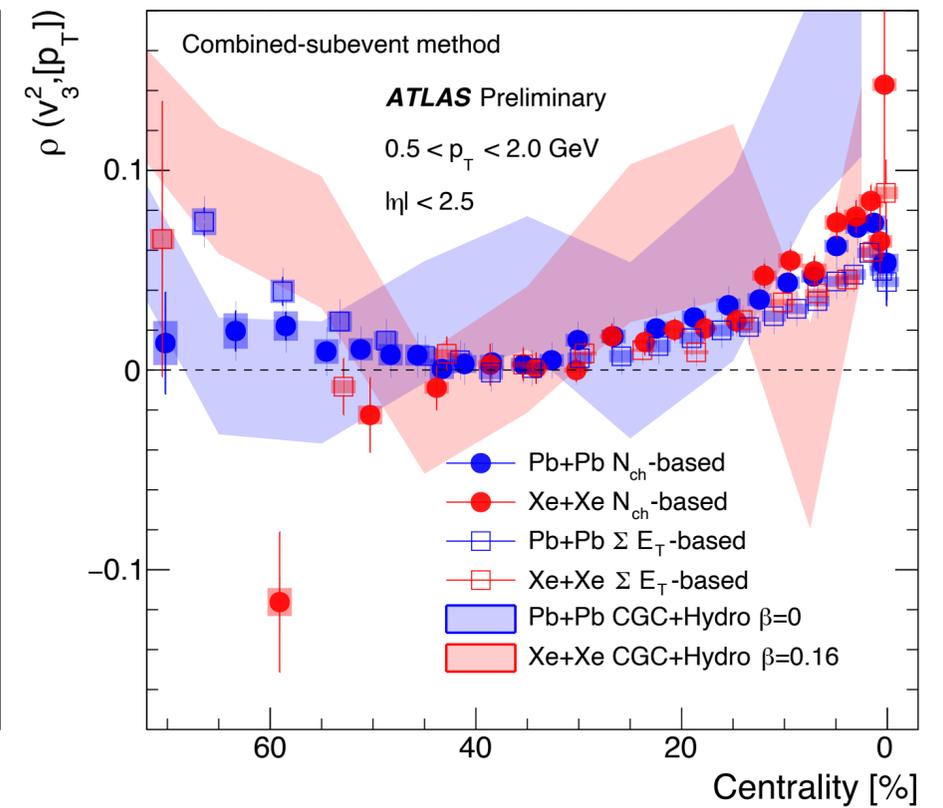
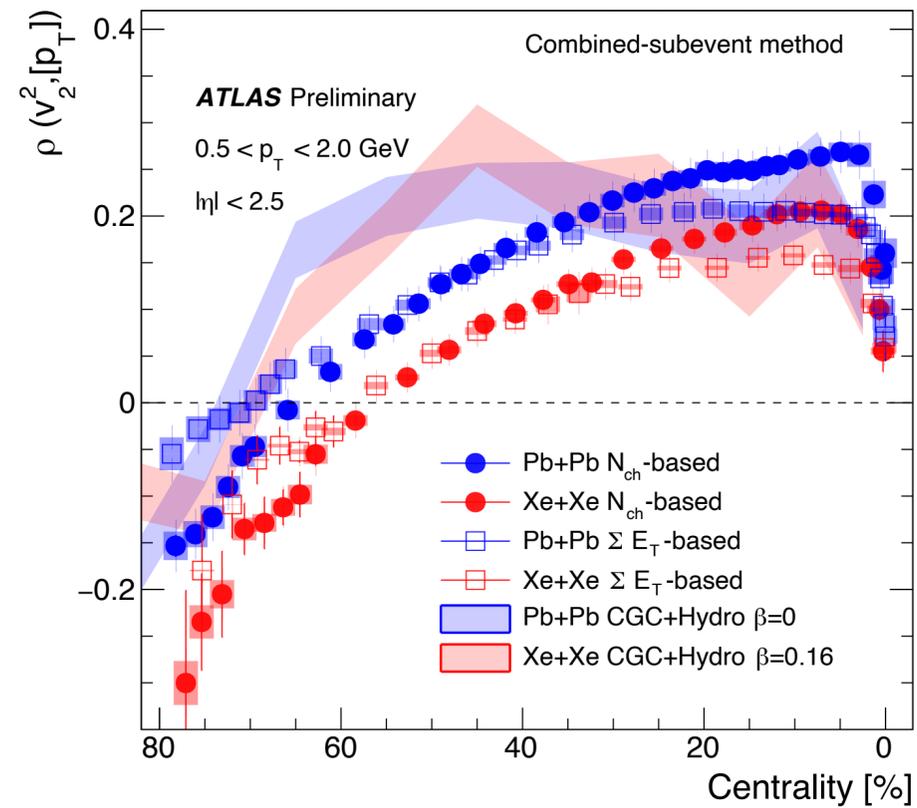
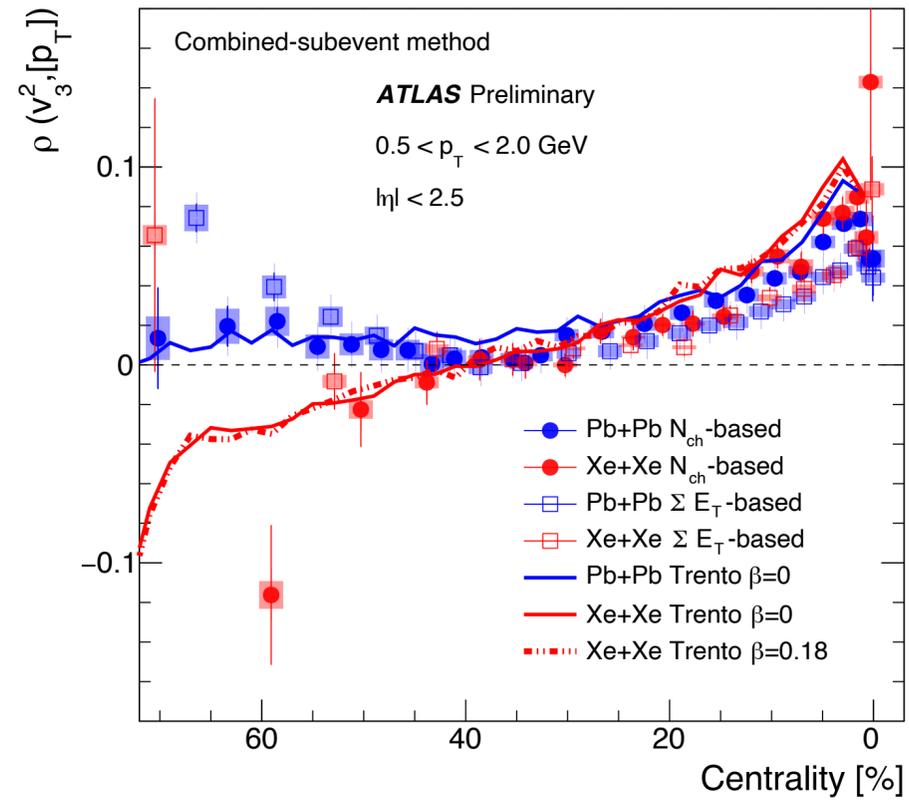
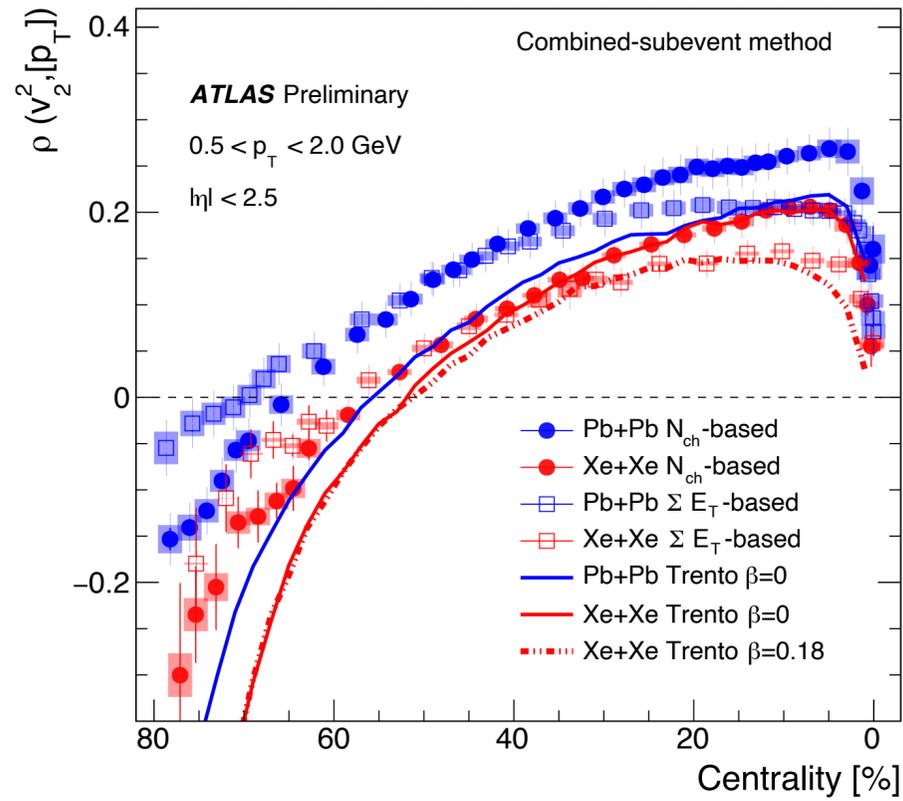


- $E_T$  and  $N_{ch}$  are mapped to centrality (based on  $E_T$  cuts)
- Large influences of centrality fluctuations for all harmonics
- Trends similar in Pb+Pb and Xe+Xe

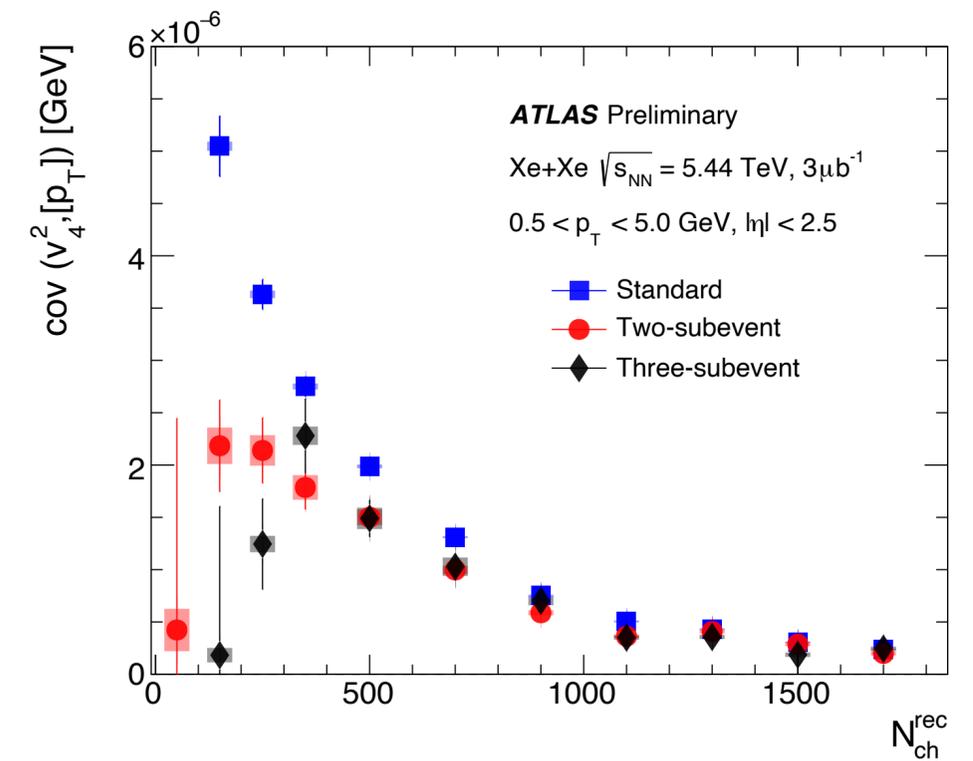
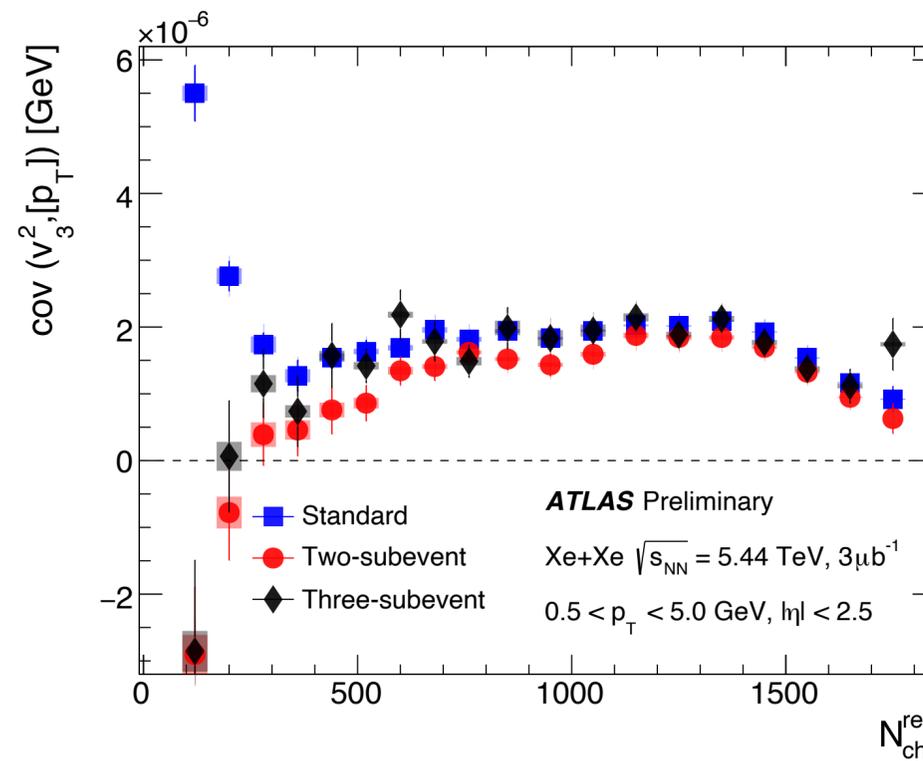
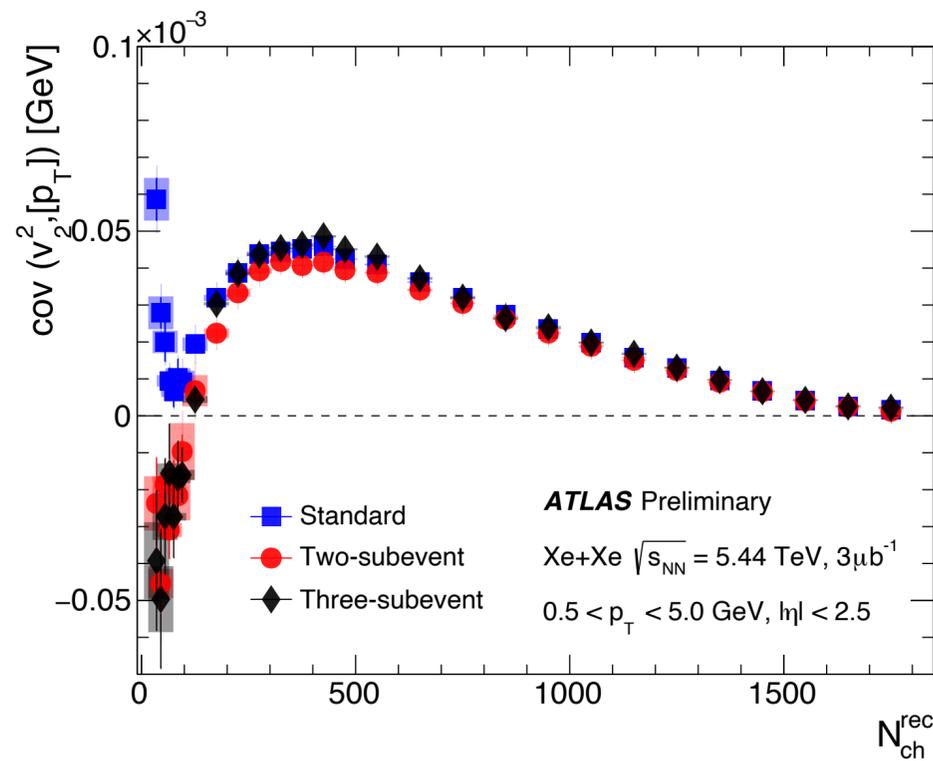
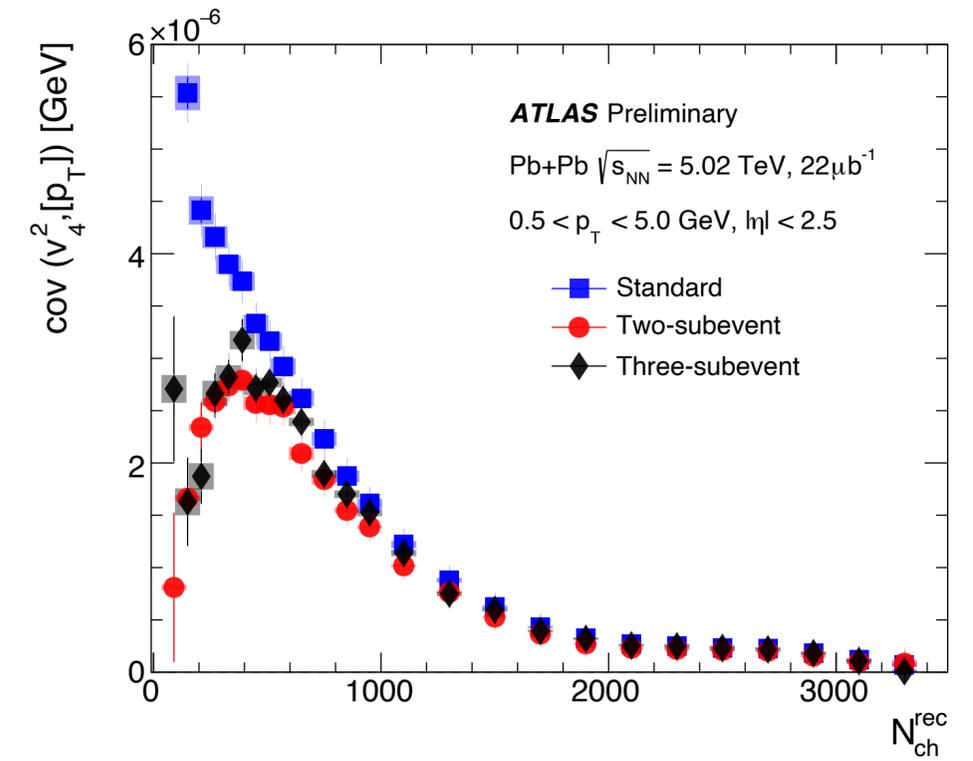
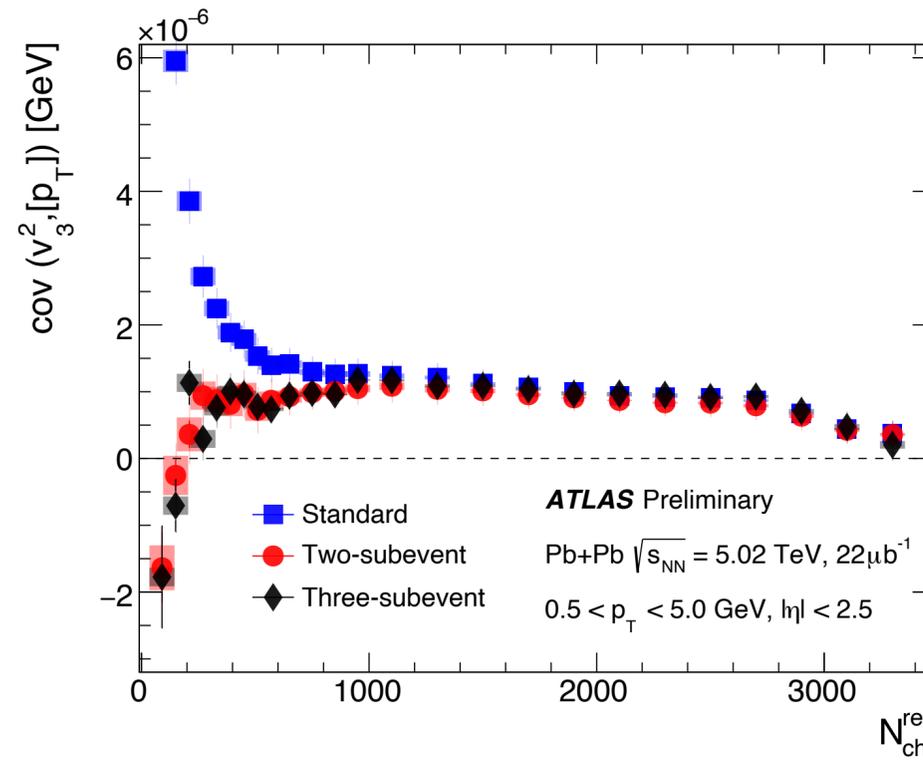
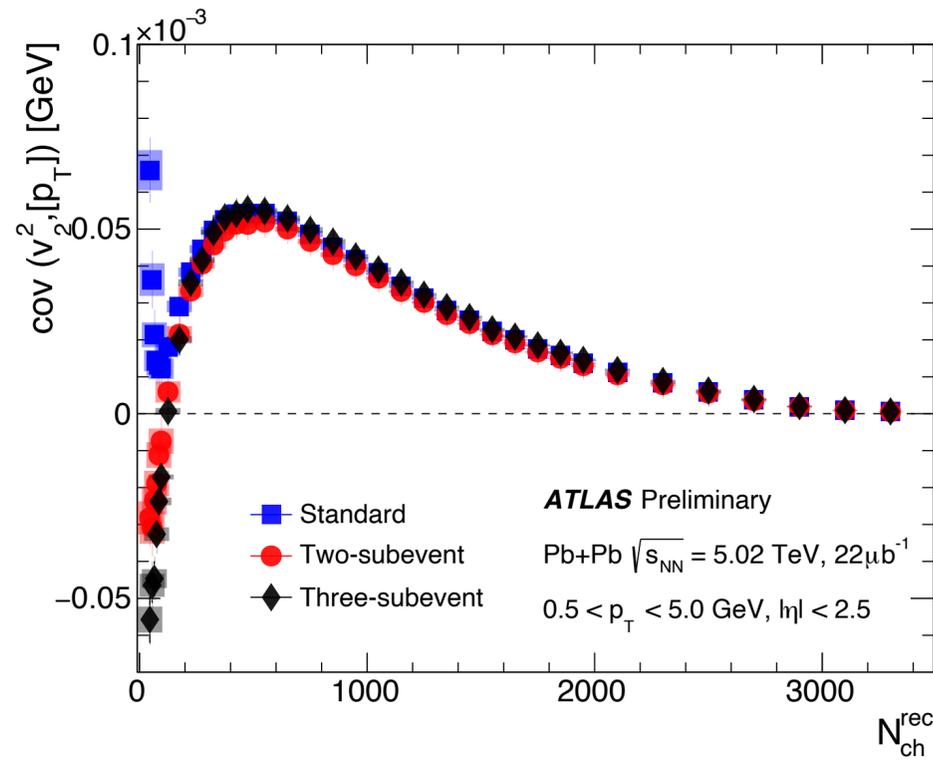
# Comparison with Theory



# Comparison with Theory



# Comparison of $\text{cov}(v_n^2, [p_T])$ - subevents methods



# Comparison of $\rho(v_n^2, [p_T])$ - subevents methods

