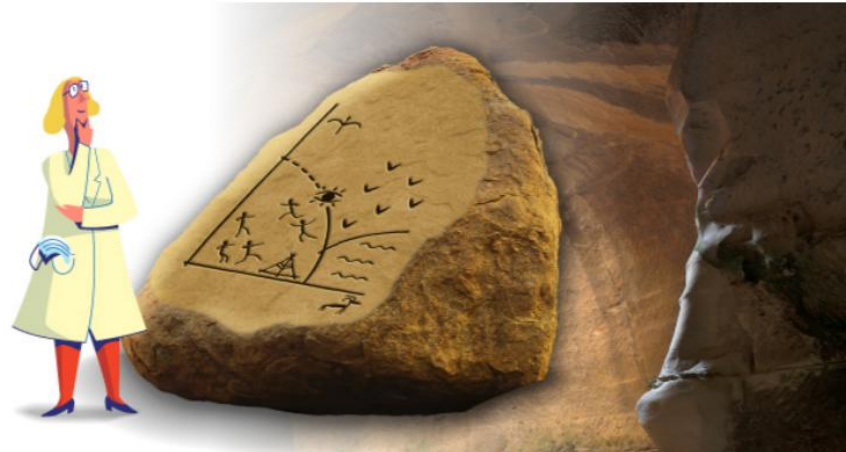


IS2021

The VIth International Conference on the
INITIAL STAGES
OF HIGH-ENERGY NUCLEAR
COLLISIONS



Probing quantum entanglement and collectivity effects in ep collisions at HERA

Chuan Sun(孙川) for H1 Collaboration
Shandong University(山东大学)



H1 at HERA

HERA Collider

Operated from 1992 to 2007

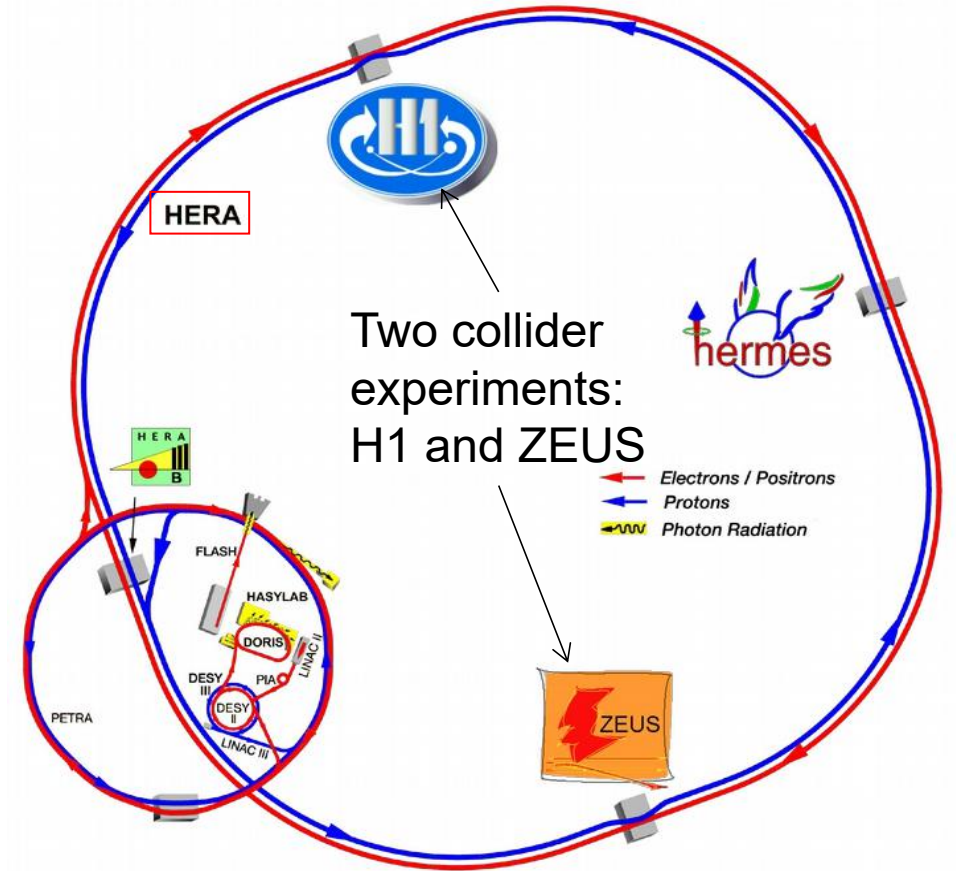
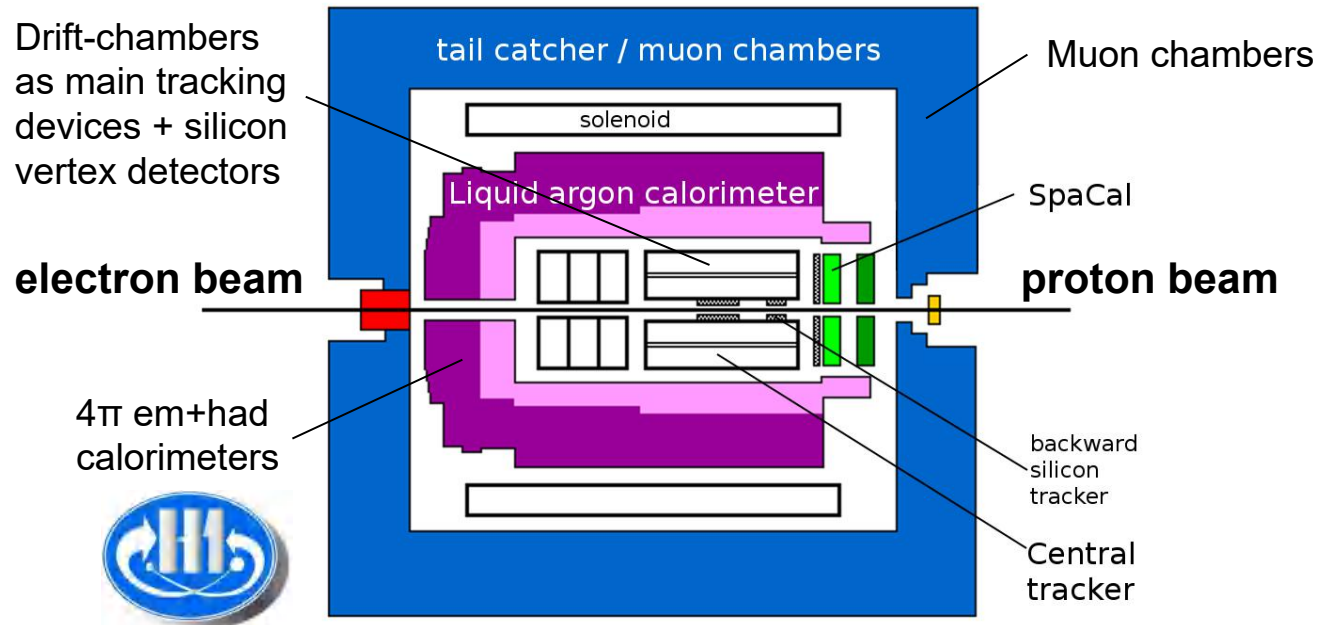
Circumference 6.3 km

Asymmetric detectors

Electrons or positrons colliding with protons

$E_e=27.6$ GeV, $E_p=460 - 920$ GeV

Centre-of-mass system is boosted to proton-direction



H1 Detector

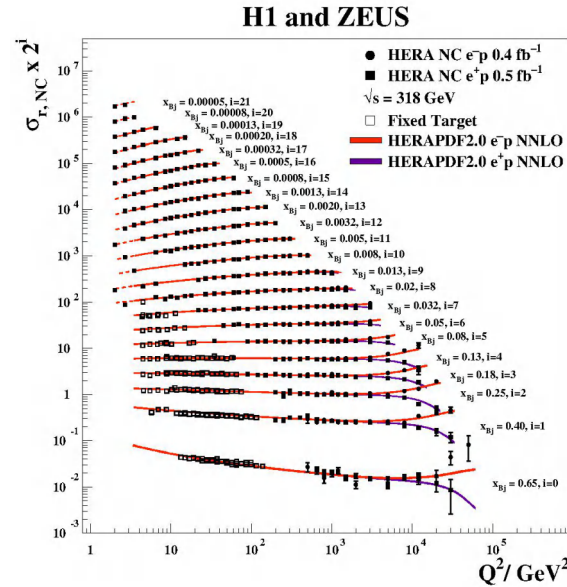
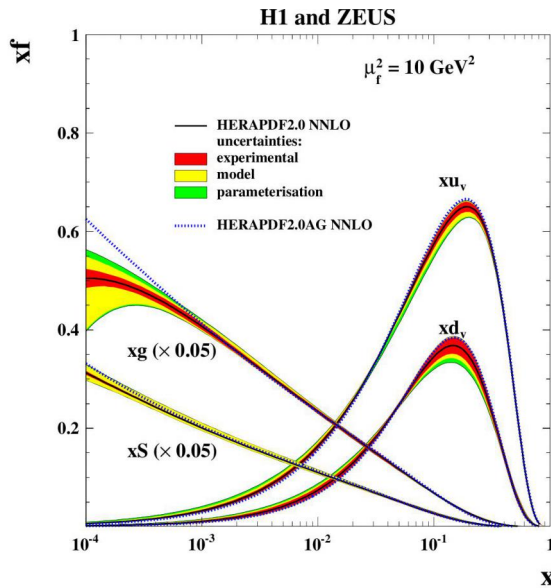
Central tracker acceptance $|\eta| < 1.6$

LAr calorimeter for hadronic final state

SpaCal calorimeter for detecting electrons

with $5 < Q^2 < 100$ GeV²

Nucleon Structure



Eur. Phys. J. C (2015)75:580

Our understanding is mostly based on 1D nucleon structure function, Parton Distribution Functions(PDFs)... Parton correlation, as well as dynamical picture of partons inside nucleon are not well-understood

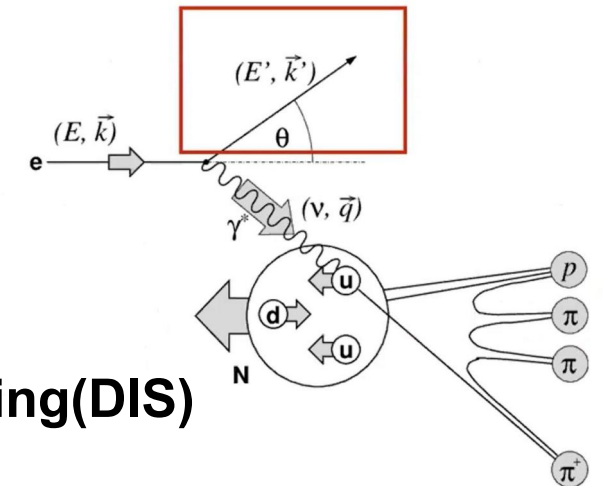
In order to explore parton correlation, two approaches used:
Predictions from quantum entanglement; Collectivity

Dataset

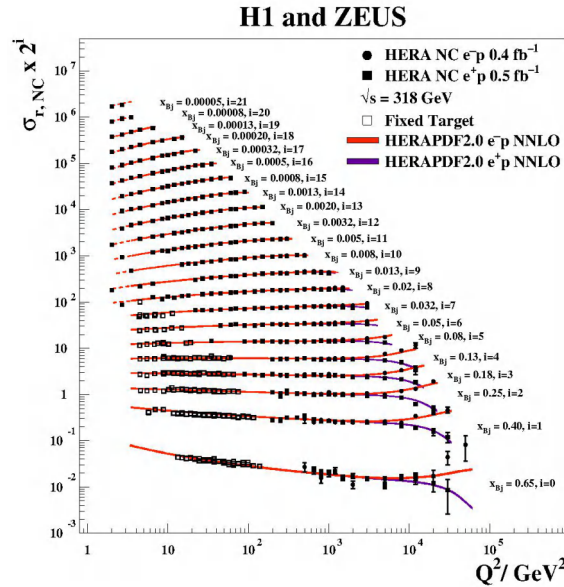
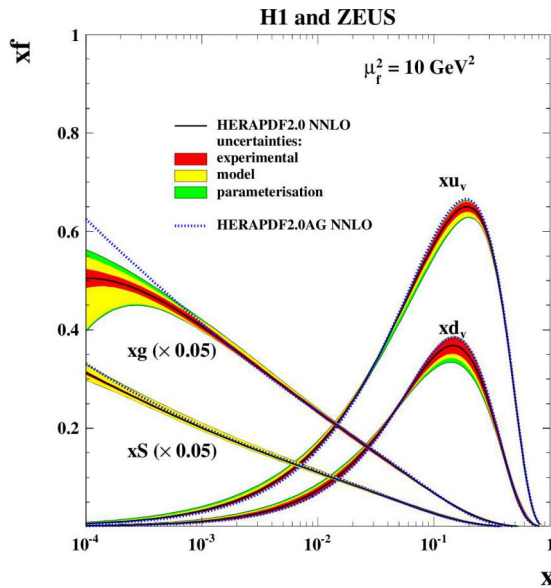
Operated from 2006 - 2007
 Beam energy: $E_e=27.6$ GeV, $E_p=920$ GeV
 Integrated luminosity: 136 pb^{-1}

Deep Inelastic Scattering(DIS)

kinematics:
 momentum transfer squared: $Q^2=(k-k')^2$
 momentum fraction of struck quark: x



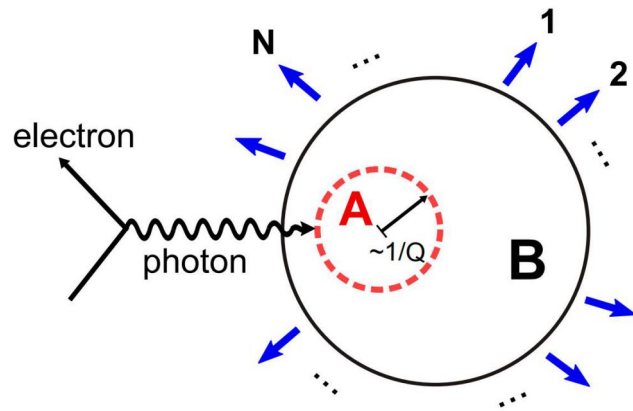
Nucleon Structure



Eur. Phys. J. C (2015)75:580

Our understanding is mostly based on 1D nucleon structure function, Parton Distribution Functions(PDFs)... Parton correlation, as well as dynamical picture of partons inside nucleon are not well-understood

In DIS, **Quantum entanglement** as a probe of parton correlation:



Regions A and B are entangled
-> entropy

Compare $S_{\text{gluon}} = \ln[xG]$

PRD 95, 114008 (2017)

gluon density from PDFs

with $S_{\text{hadron}} = -\sum P(N) \ln[P(N)]$

hadron multiplicity distribution $P(N)$

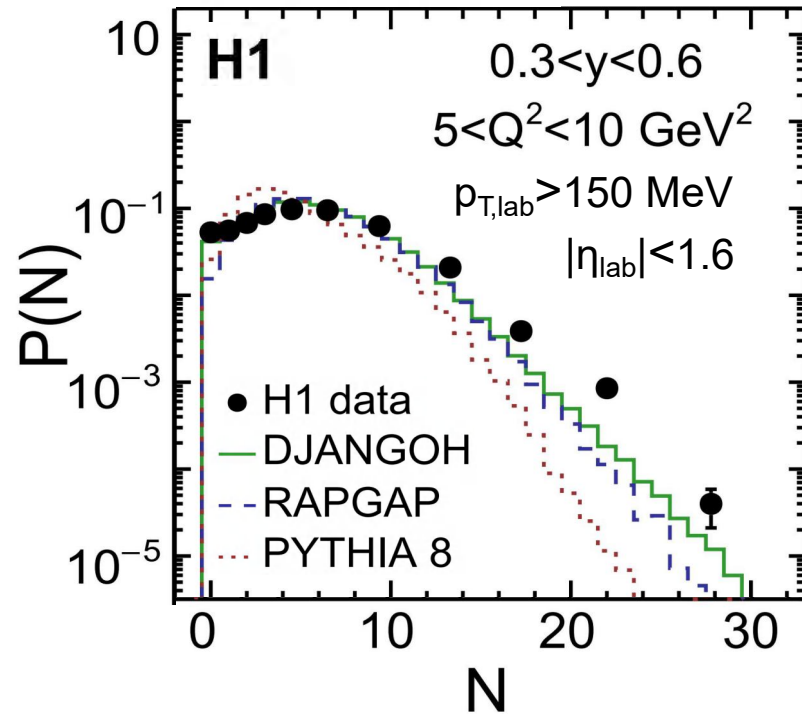
Theory prediction $S_{\text{gluon}} = S_{\text{hadron}}$

Quantum entanglement in ep DIS

Charged particle multiplicity distribution $P(N)$

arXiv:2011.01812 [hep-ex]

ep $\sqrt{s} = 319$ GeV

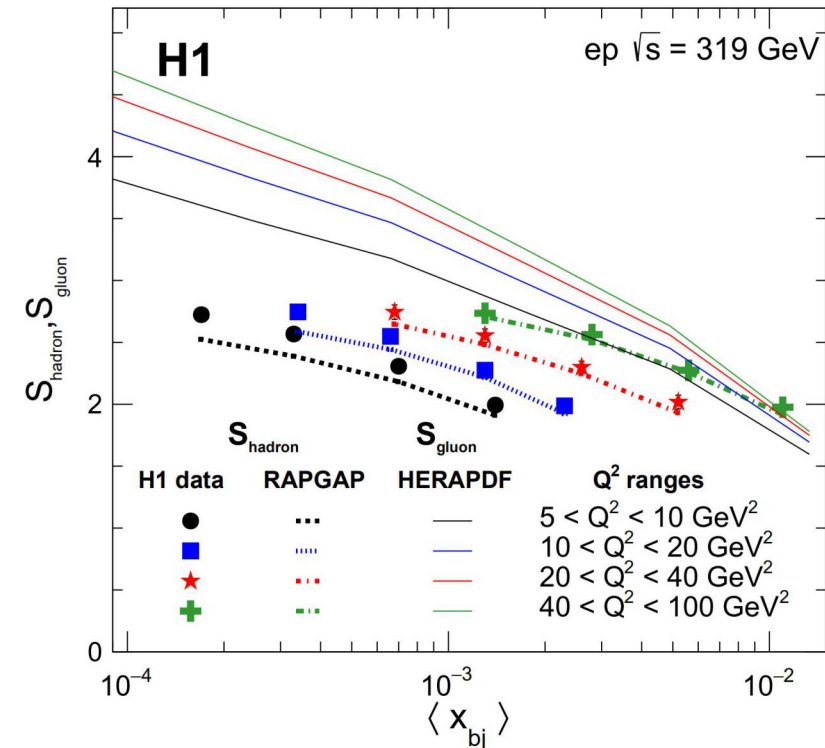


The charged particle multiplicity distributions are measured for particles on a 4×4 grid in x and Q^2
High multiplicity: MC cannot fully explain data

Predictions based on quantum entanglement

$$S_{\text{hadron}} \equiv - \sum P(N) \ln P(N) = \ln [xG(x, Q^2)] \equiv S_{\text{gluon}}$$

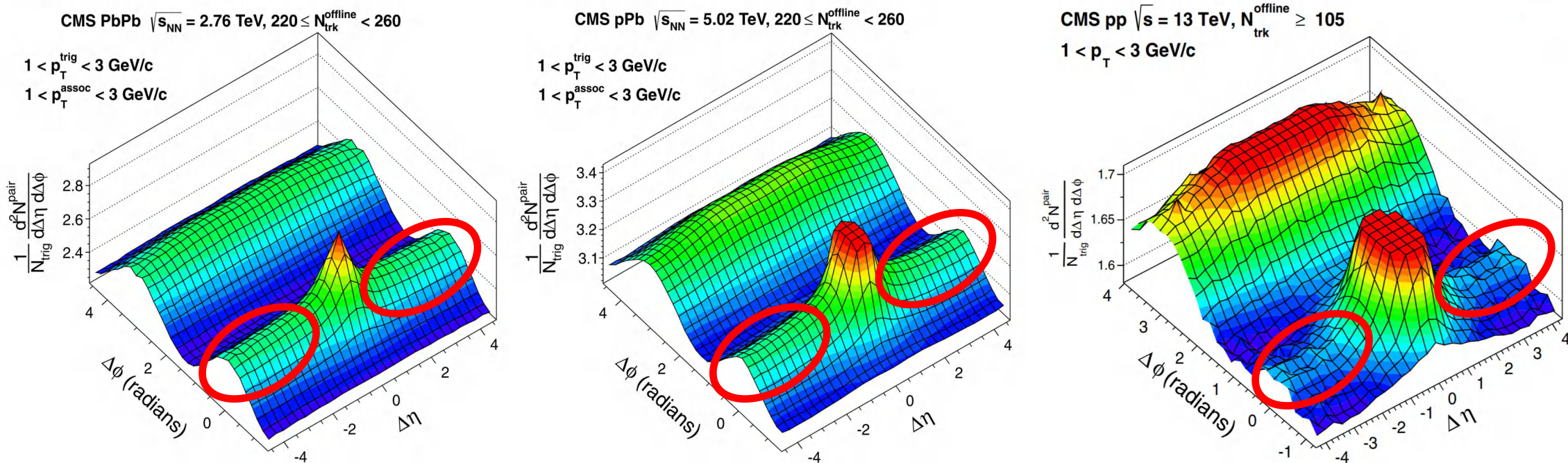
$0 < \eta^* < 4.0$ **HCM frame**



Entropy of gluons disagree with the hadron entropy
 Data does not support the prediction

Collectivity in small system

PLB 724 (2013) 213–240; PRL 116, 172302 (2016)



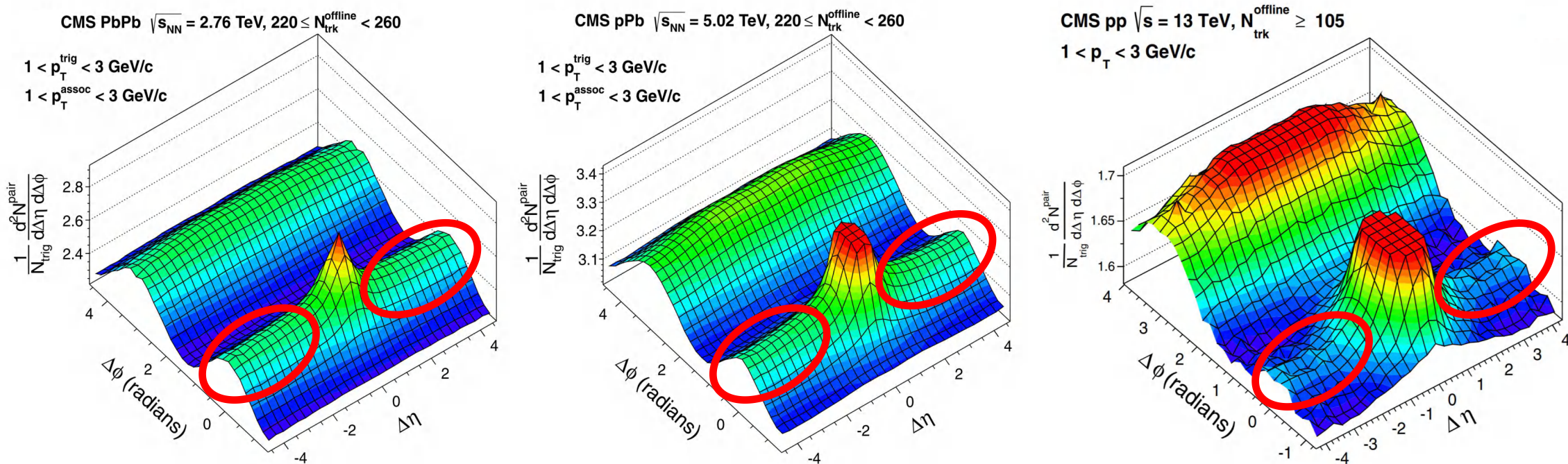
Collectivity as a probe of parton correlation:

Lots of evidence of collectivity in high multiplicity pp and pPb collisions, similar to heavy-ion collisions attributed to the perfect liquid nature of QGP

What about even smaller system?

Collectivity in small system

PLB 724 (2013) 213–240; PRL 116, 172302 (2016)



Collectivity as a probe of parton correlation:

Lots of evidence of collectivity in high multiplicity pp and pPb collisions, similar to heavy-ion collisions attributed to the perfect liquid nature of QGP

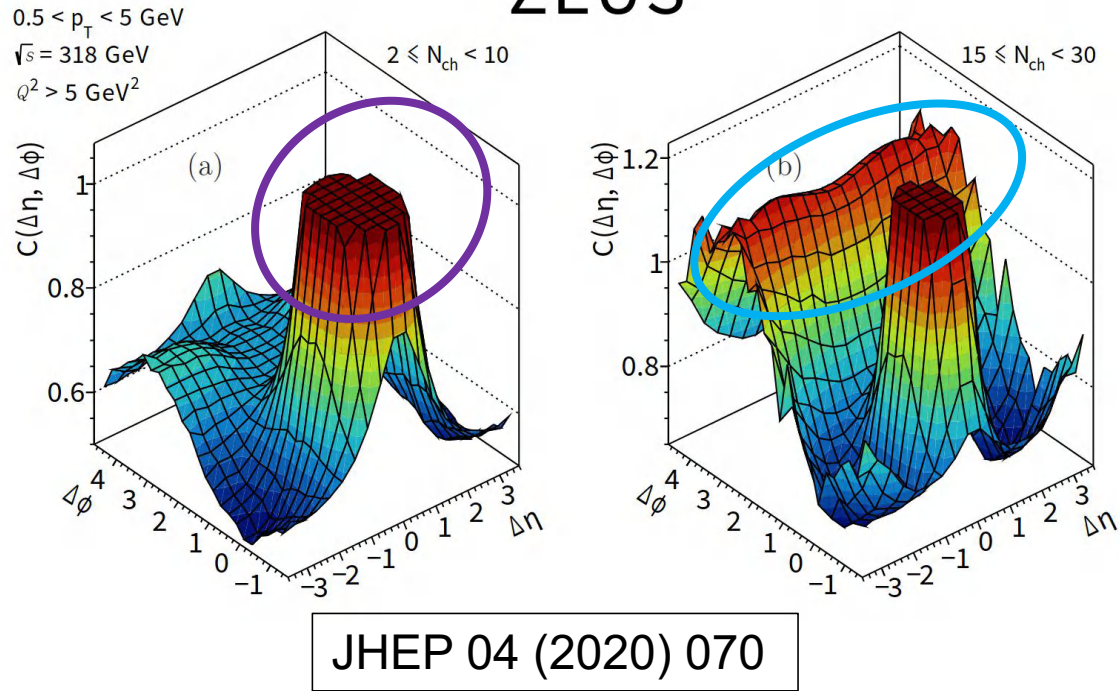
What about even smaller system?

In DIS and photoproduction events:

Two-particle correlation (Ridge, $V_{n\Delta}$), Four-particle correlation ($C_2\{4\}$)

Search for collectivity in ep DIS

ZEUS



Clear peak

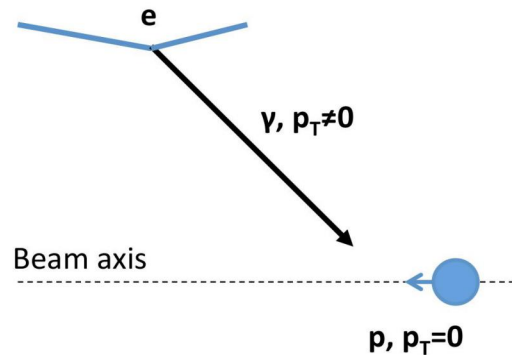
short-range effects (Jets, boosted decays...)

Back-to-back

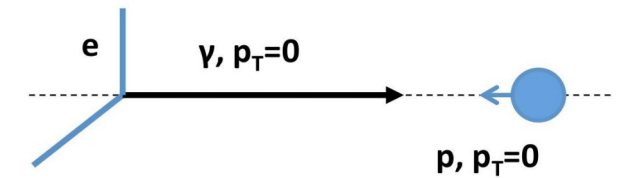
dijets...

No near-side ridge observed in lab frame

Lab Frame



Hadronic CMS frame



lab frame: inhomogeneous p_T space

HCM frame: homogeneous p_T space

Search for collectivity with H1 data in HCM frame

Two-particle correlation functions in ep DIS

H1prelim-20-033: https://www-h1.desy.de/publications/H1preliminary.short_list.html

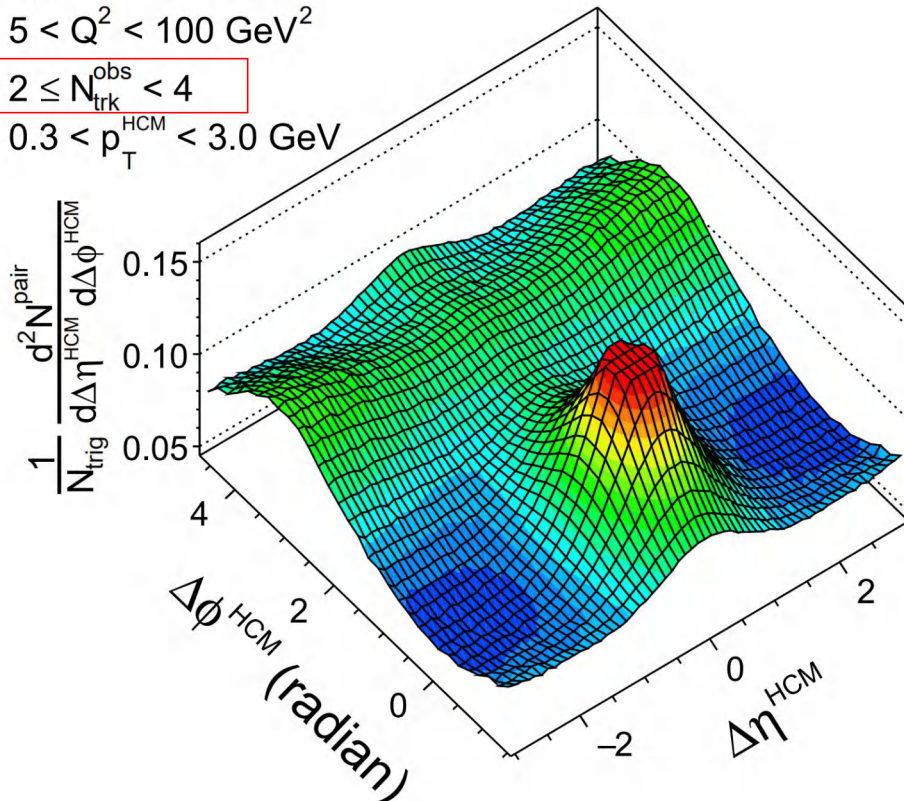
H1 Preliminary

ep $\sqrt{s} = 319$ GeV

$5 < Q^2 < 100$ GeV²

$2 \leq N_{\text{trk}}^{\text{obs}} < 4$

$0.3 < p_{\text{T}}^{\text{HCM}} < 3.0$ GeV



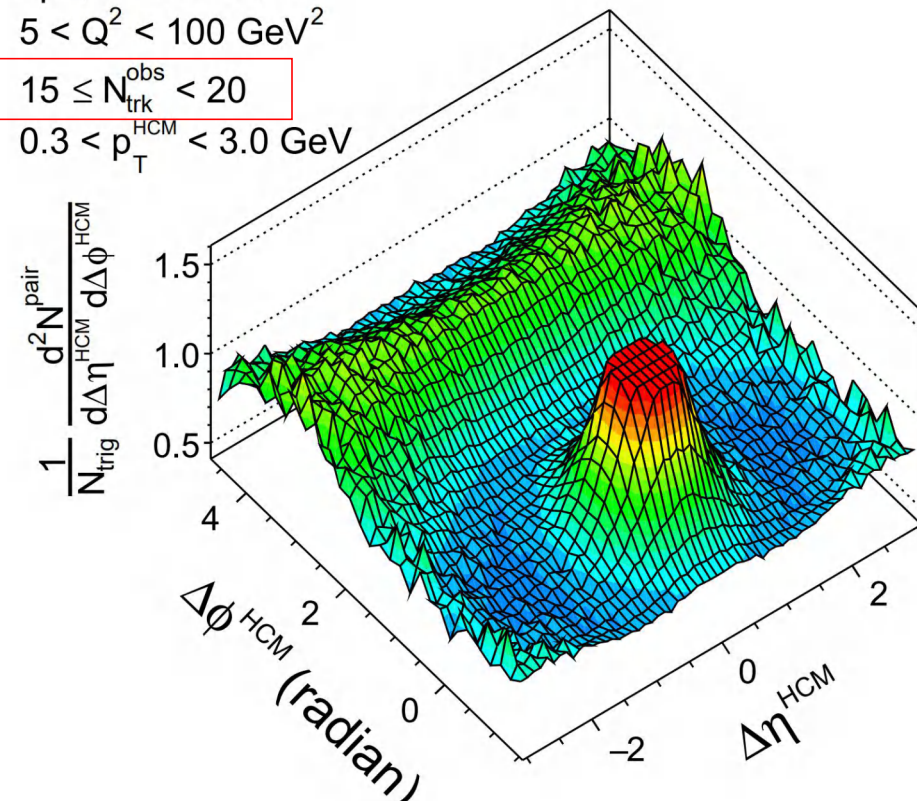
H1 Preliminary

ep $\sqrt{s} = 319$ GeV

$5 < Q^2 < 100$ GeV²

$15 \leq N_{\text{trk}}^{\text{obs}} < 20$

$0.3 < p_{\text{T}}^{\text{HCM}} < 3.0$ GeV

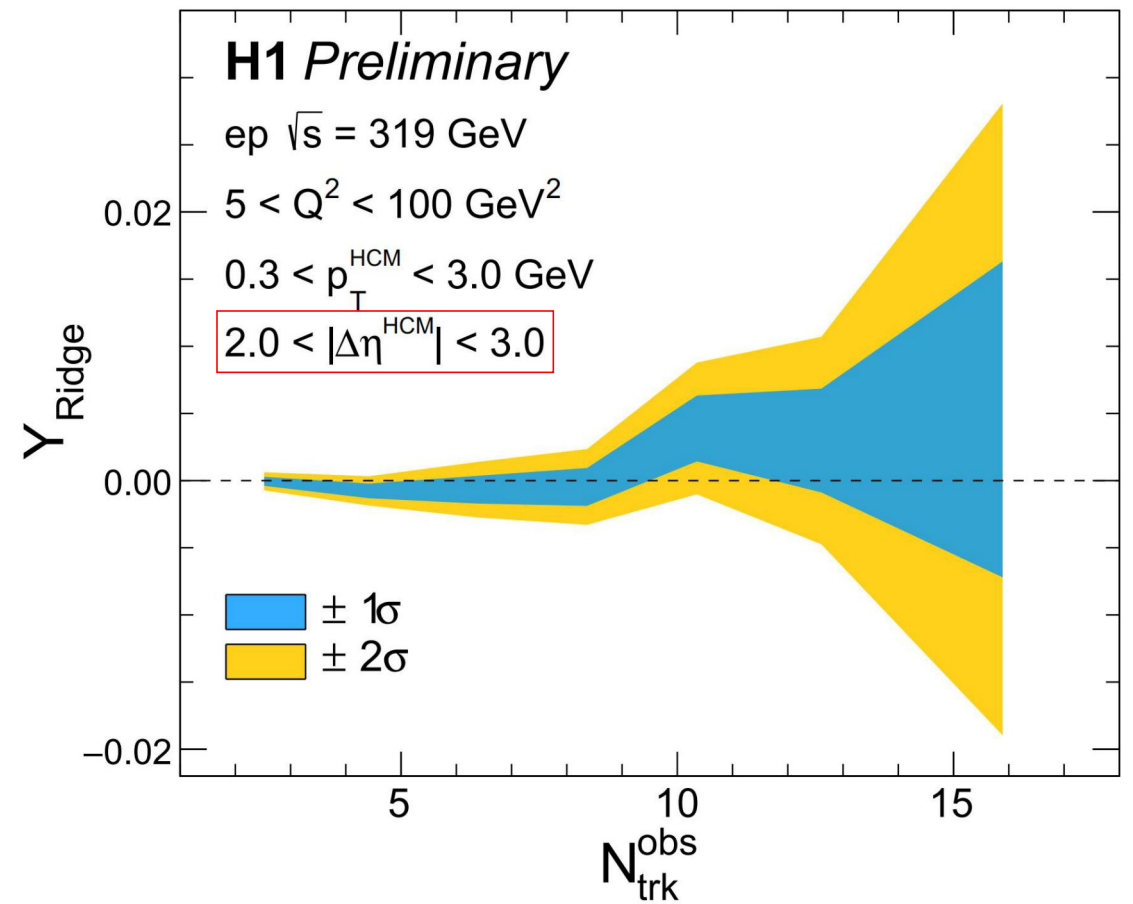
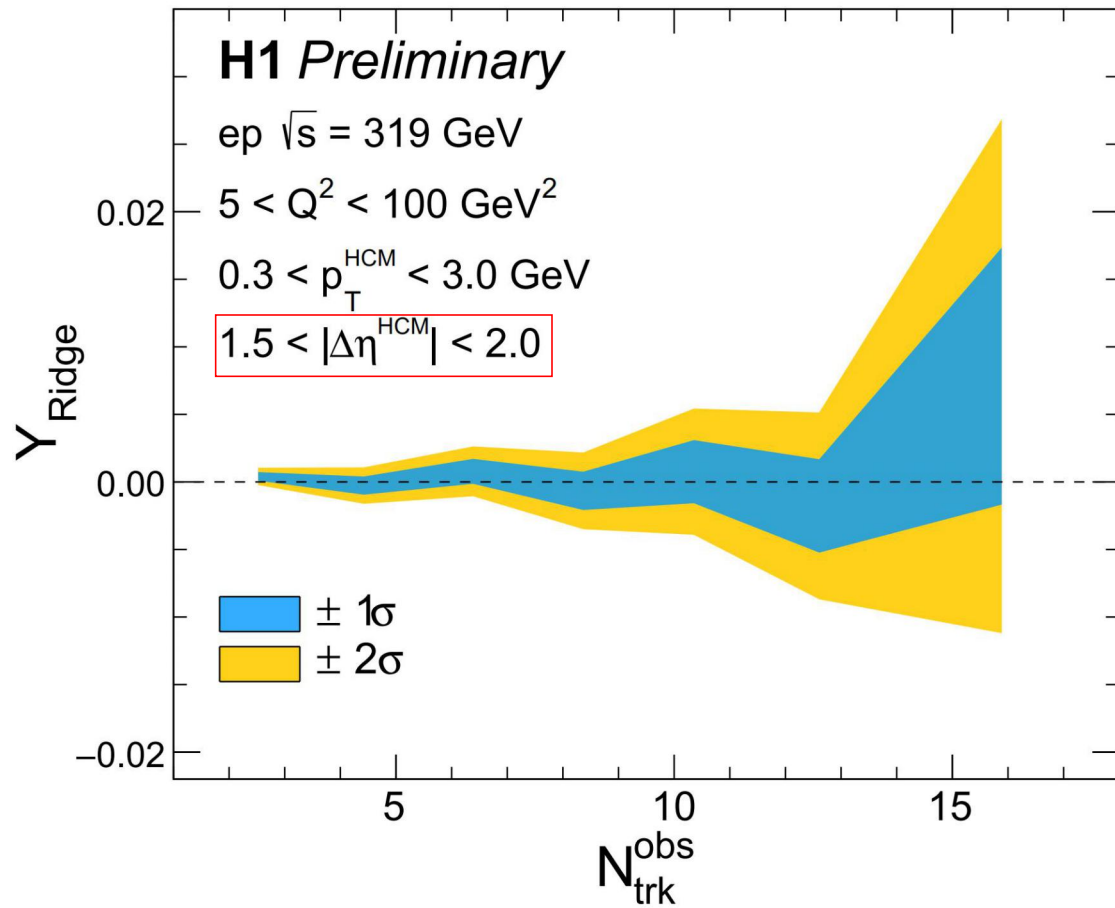


No near-side long-range ridge with H1 DIS data

Extract ridge yield limits through ZYAM and booststrap procedure

DIS HCM

Ridge yield limits in ep DIS



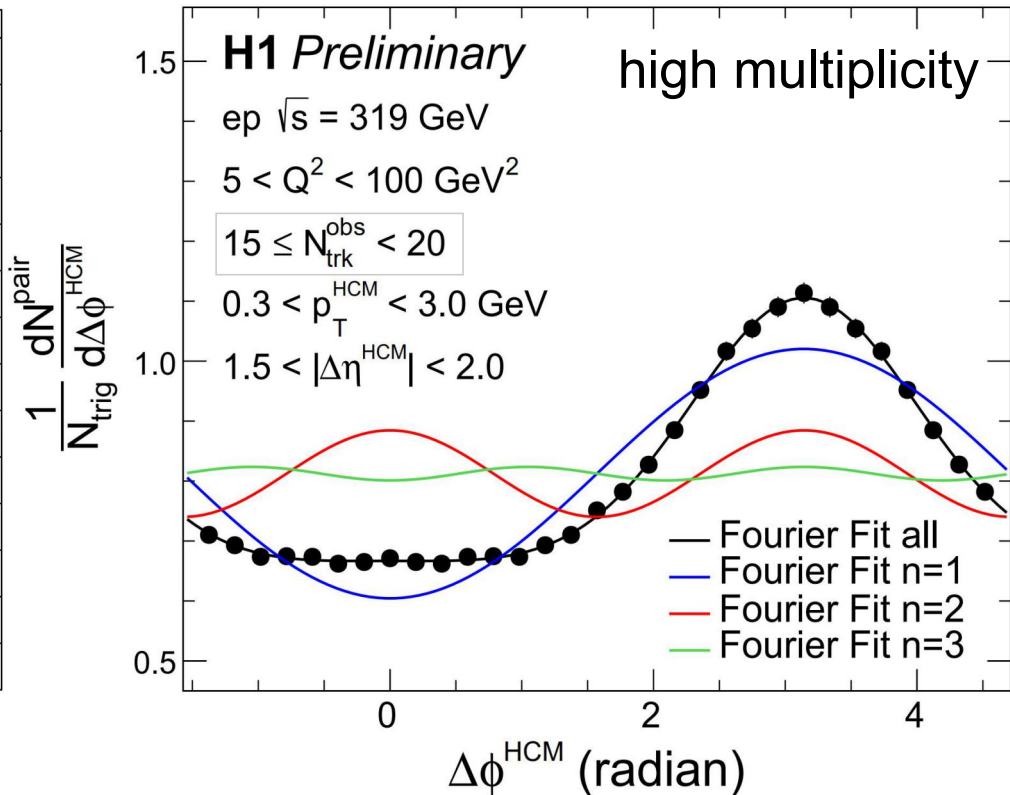
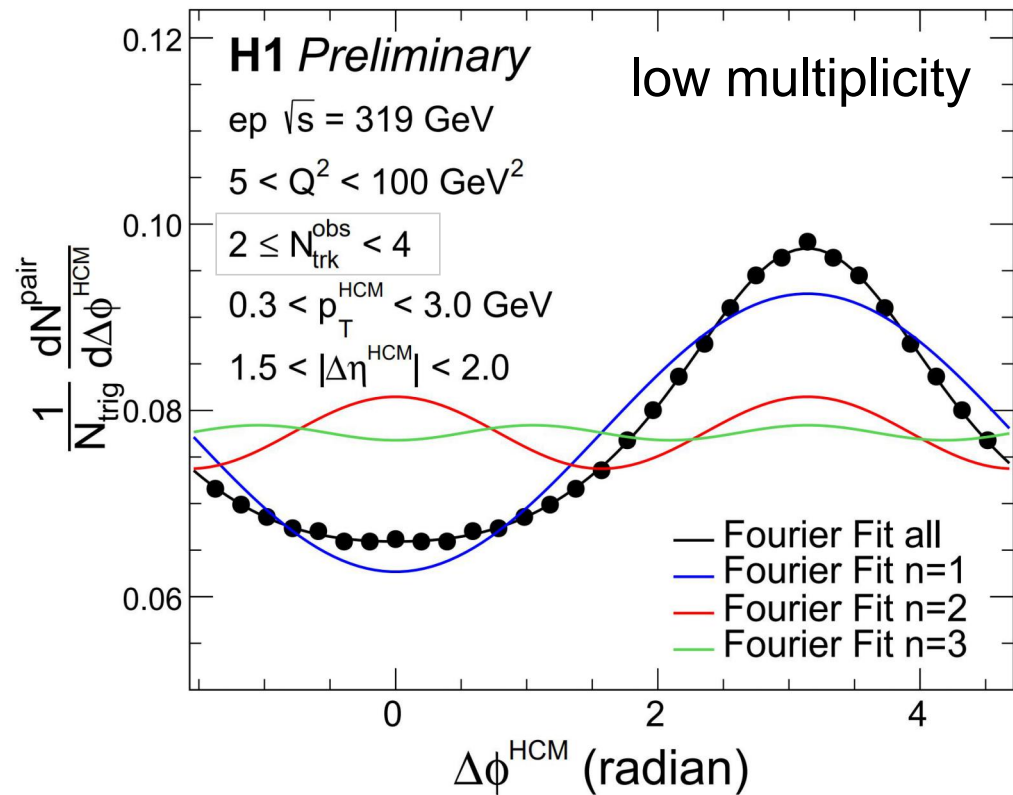
Limits set for ridge yield
Small room for existence of ridge

DIS HCM

Fourier coefficient $V_{n\Delta}$ extraction procedure

Long-range 1-D projections of 2PC functions on $\Delta\phi$ direction

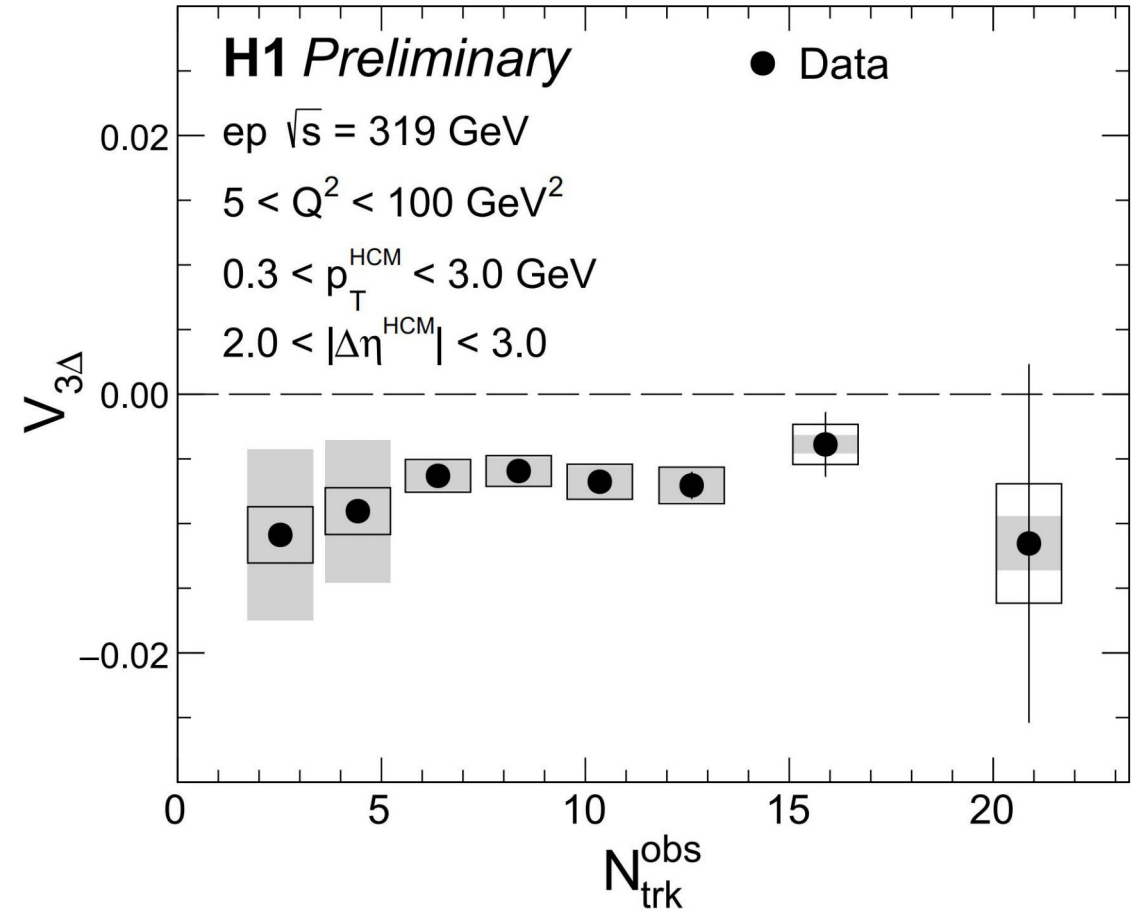
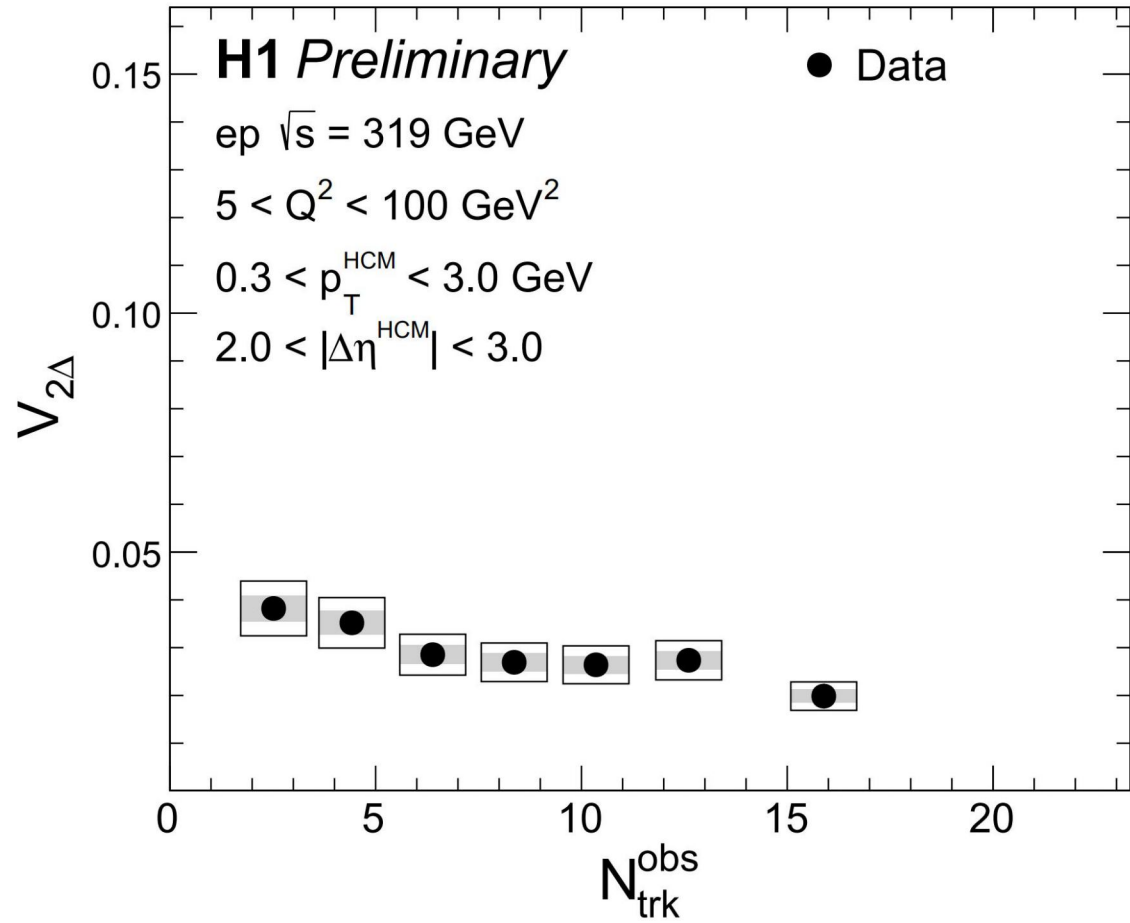
$$\frac{1}{N_{trig}} \frac{dN^{pair}}{d\Delta\phi} = \frac{N_{assoc}}{2\pi} \left(1 + \sum_n 2V_{n\Delta} \cos(n\Delta\phi) \right)$$



Similar shapes in low and high multiplicity

DIS HCM

Fourier coefficient $V_{n\Delta}$ in ep DIS

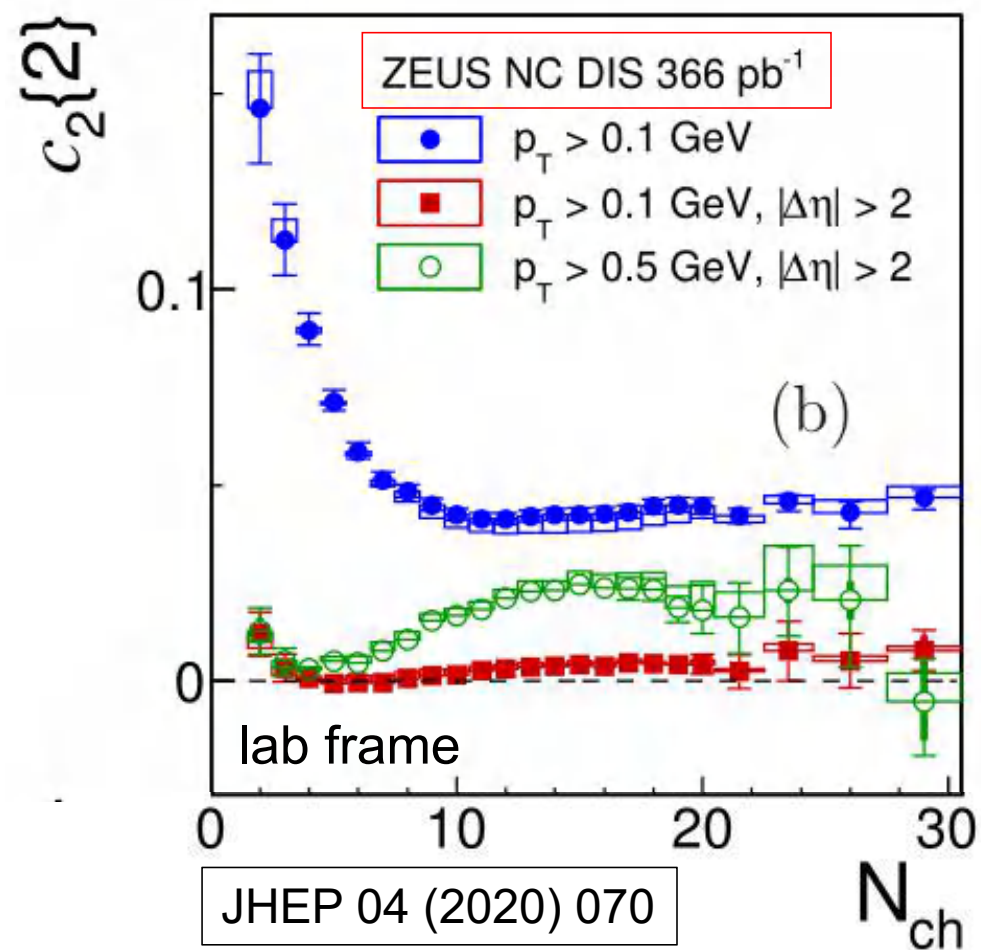
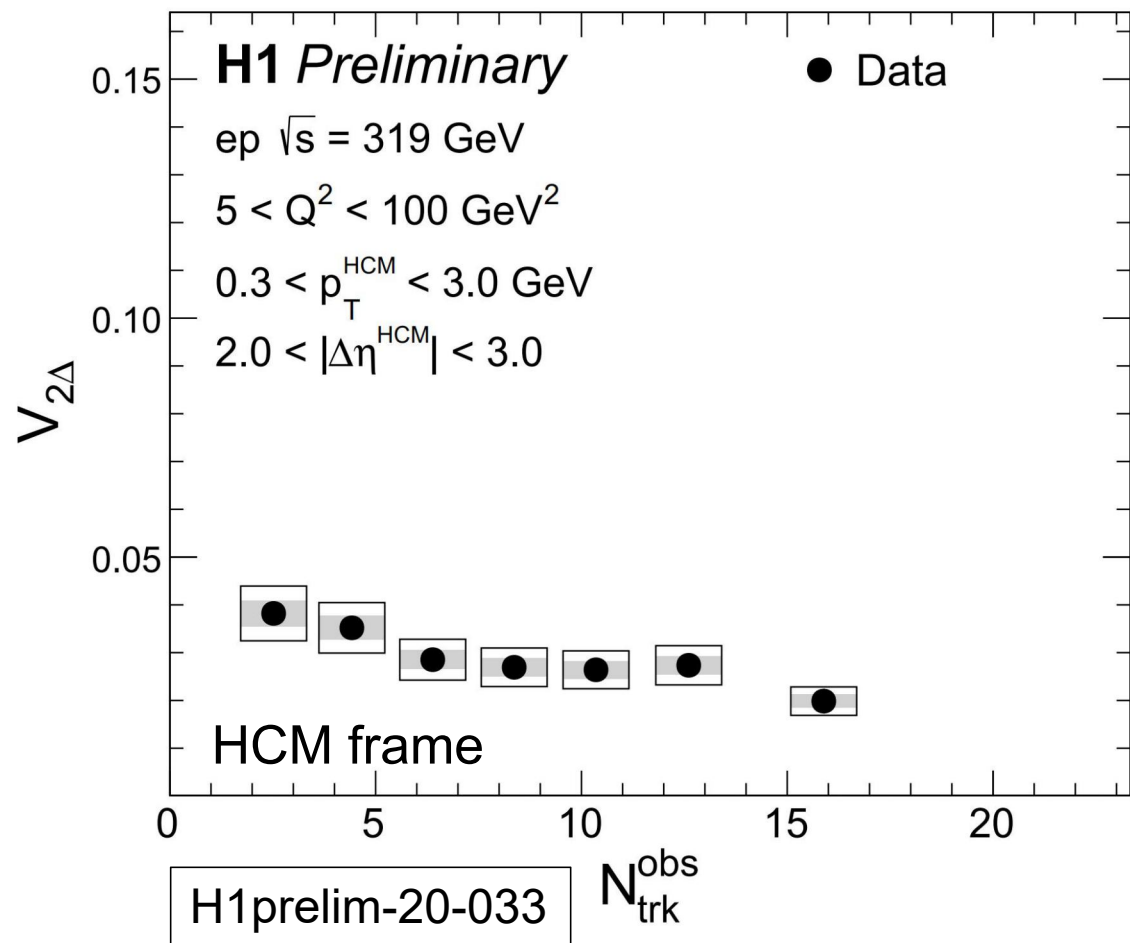


$V_{2\Delta}$ value drops in high multiplicity

$V_{3\Delta}$ remains negative, indicating no collectivity

DIS HCM

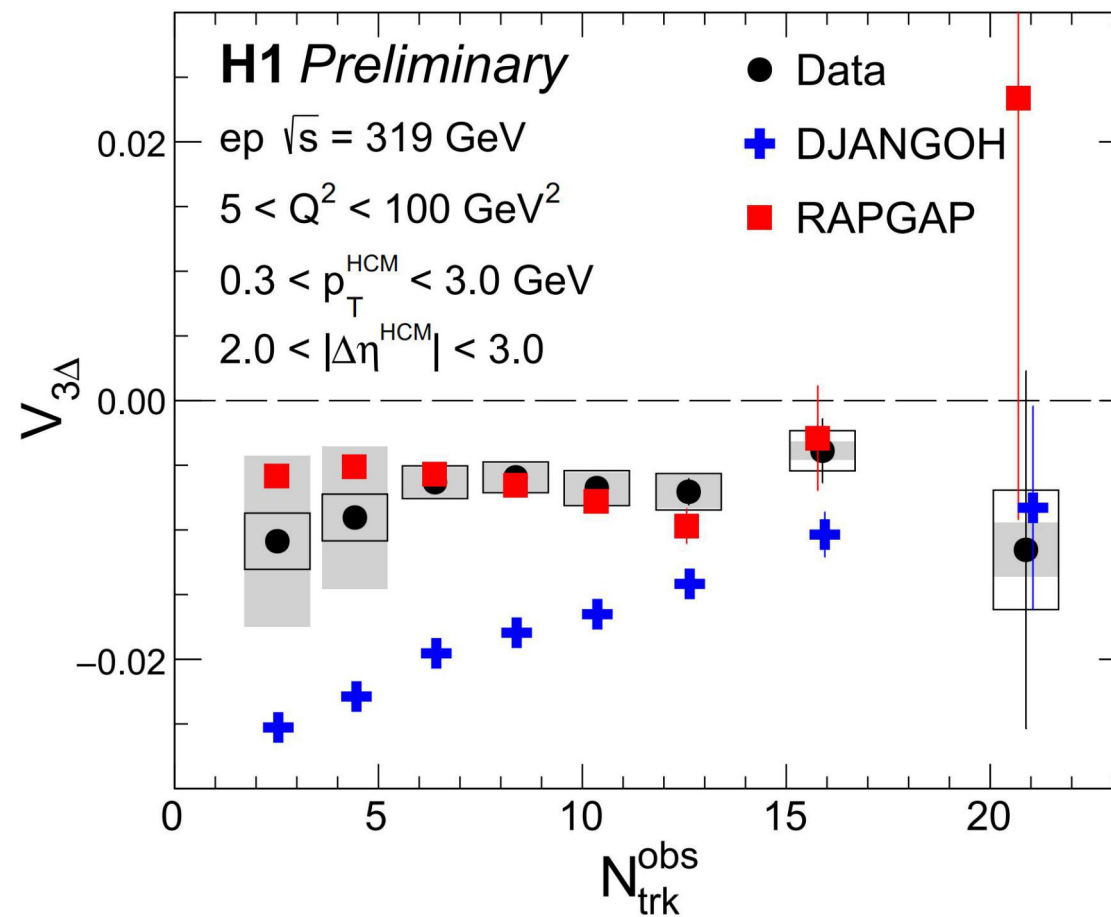
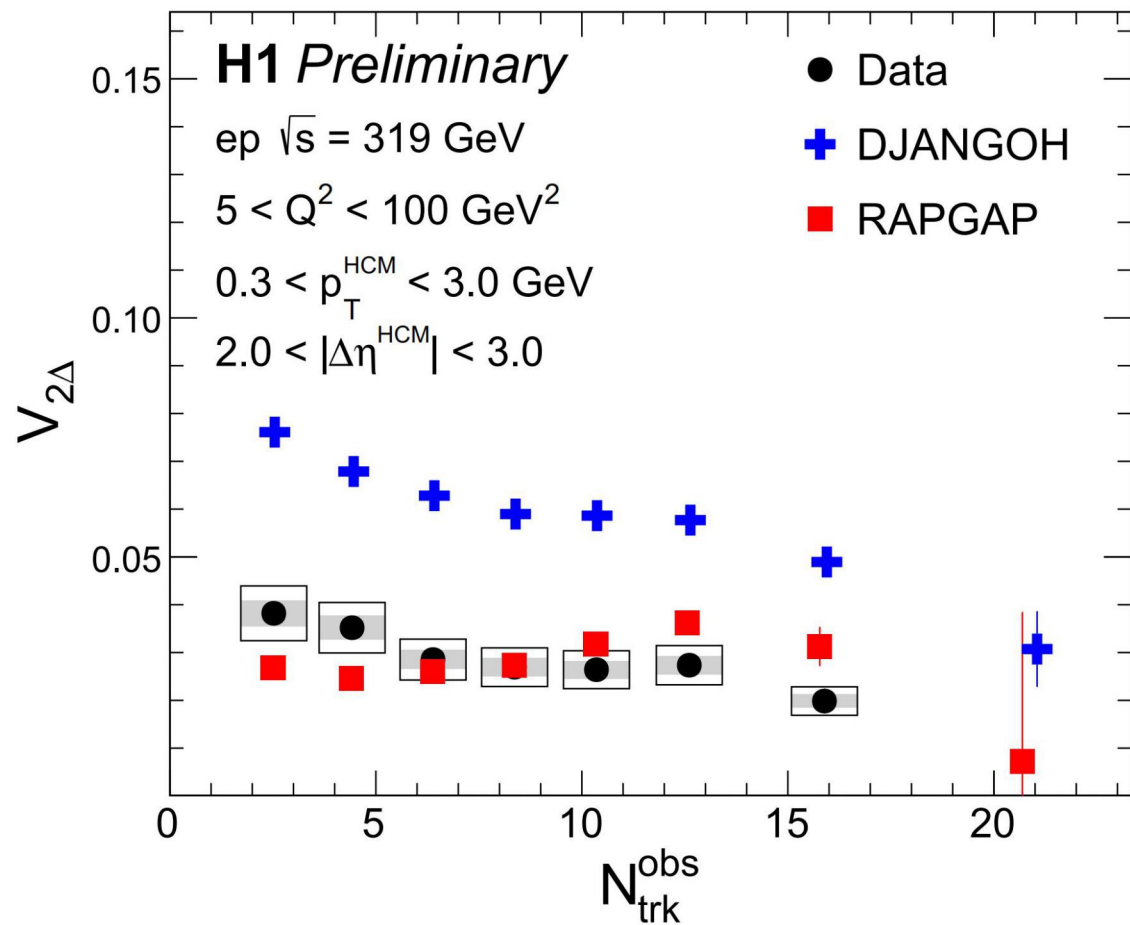
Fourier coefficient $V_{n\Delta}$ in ep DIS



Similar trend as ZEUS result

DIS HCM

Fourier coefficient $V_{n\Delta}$ in ep DIS



RAPGAP has better description on DIS data than DJANGO

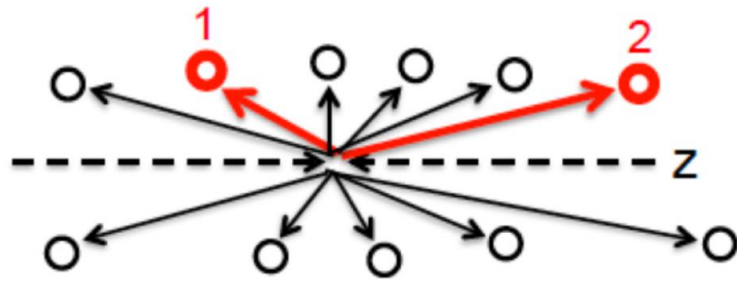
The difference between RAPGAP and DJANGO is still under investigation

Data can be described by MC(RAPGAP) w/o collectivity

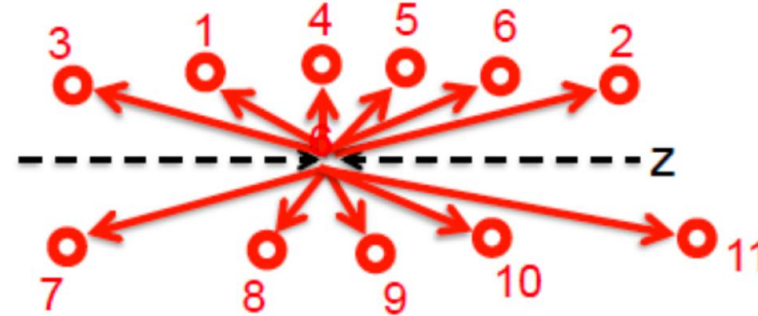
DIS HCM

Multi-particle correlation

Two-particle correlation



Multi-particle correlation



$$\langle 2 \rangle = \langle e^{in(\phi_1 - \phi_2)} \rangle = \frac{Q_n^2 - M}{M(M-1)}$$

$$Q_n \equiv \sum_{i=1}^M e^{in\phi_i}$$

$$\langle 4 \rangle = \langle e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)} \rangle = \frac{Q_n^4 - 2\text{Re}[Q_{2n} Q_n^{*2}] - 4(M-2)Q_n^2 + 2M(M-3) + Q_{2n}^2}{M(M-1)(M-2)(M-3)}$$

$$c_n\{4\} = \langle\langle 4 \rangle\rangle - 2\langle\langle 2 \rangle\rangle^2$$

$$v_n\{4\} = \sqrt[4]{-c_n\{4\}}$$

Phys. Rev. C 83, 044913

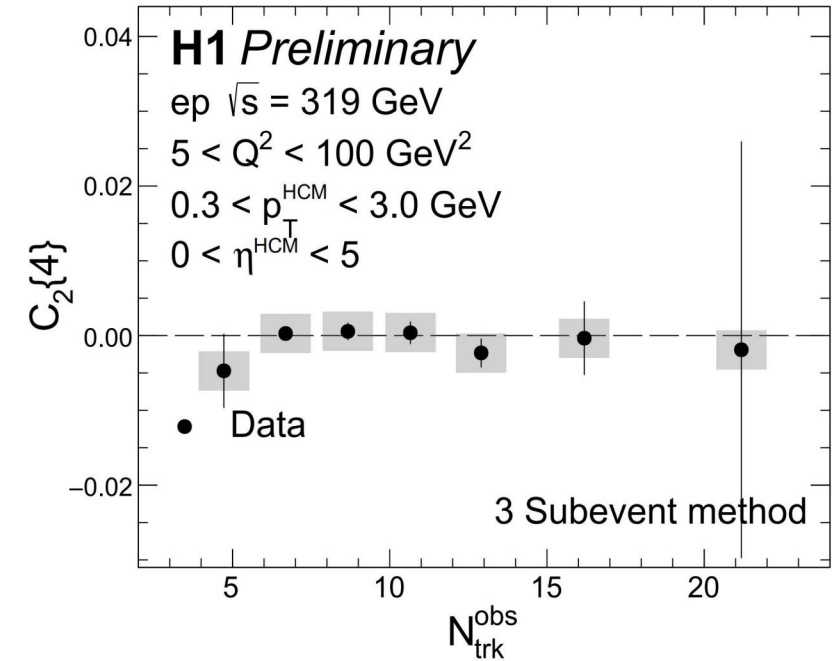
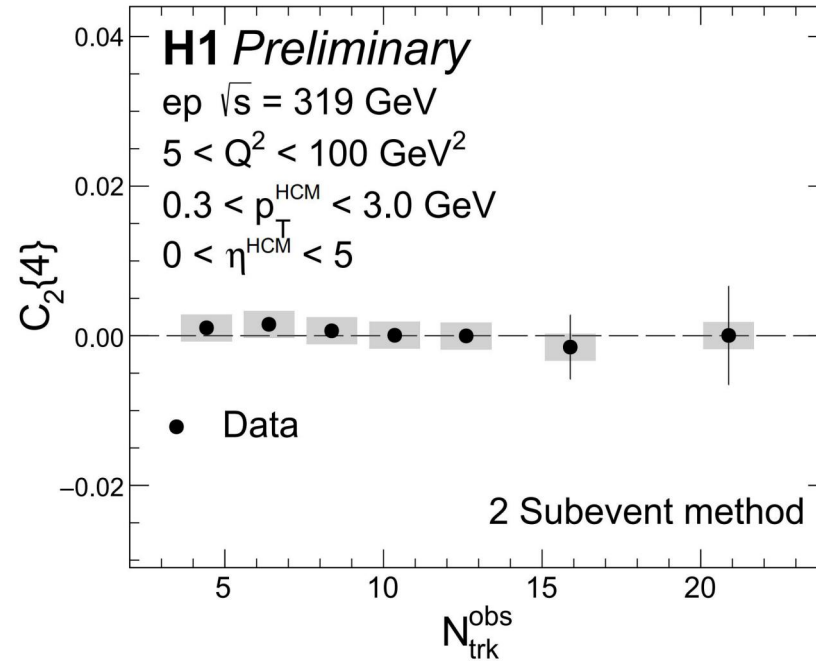
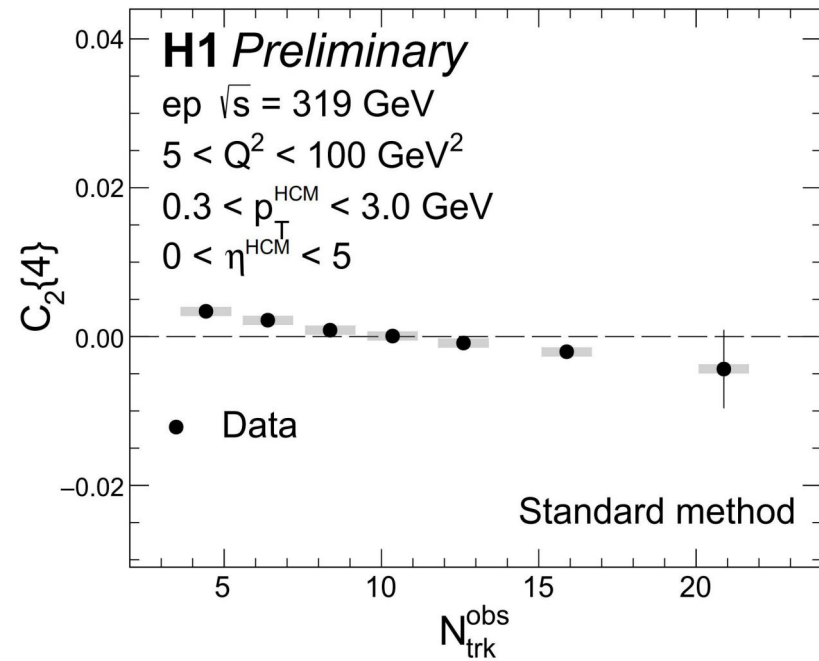
Phys. Rev. C 96, 034906

Few particle correlation suppressed

Collective behavior leads to negative $C_n\{4\}$

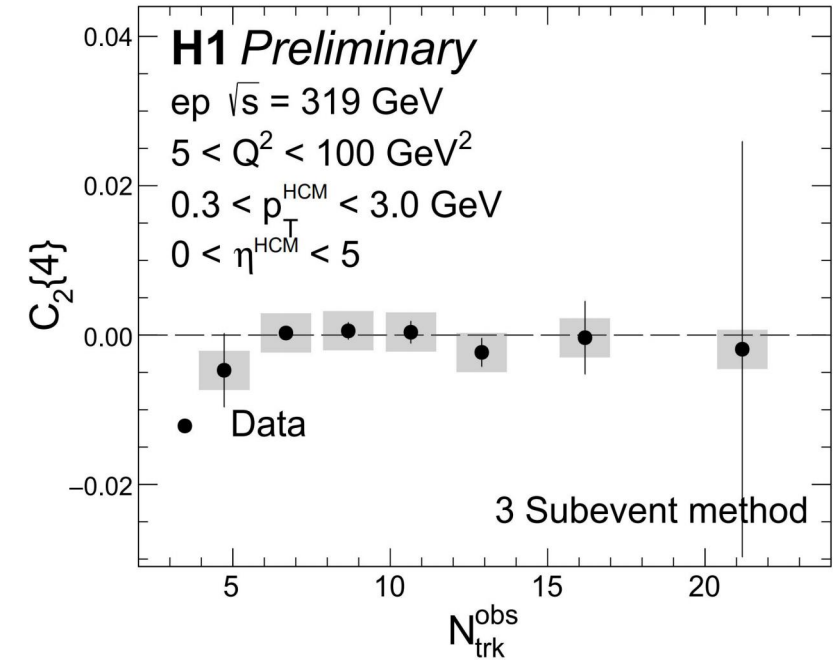
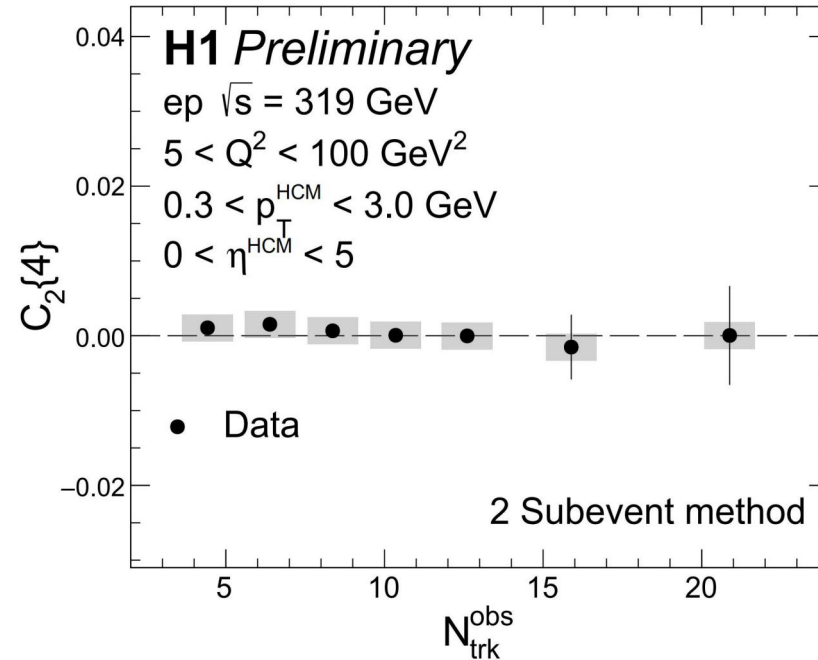
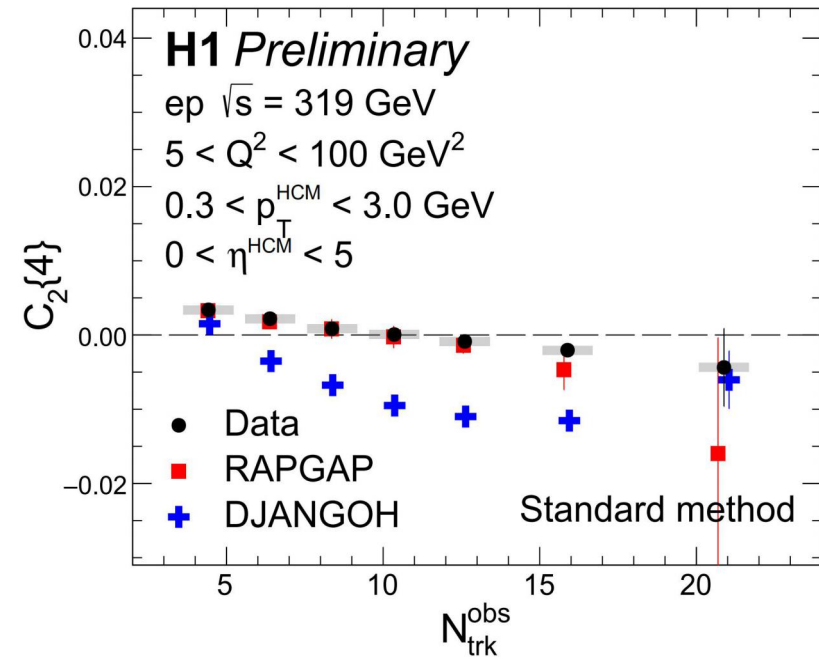
Subevent cumulants also investigated, providing more reliable results on collectivity

Multi-particle correlation in ep DIS



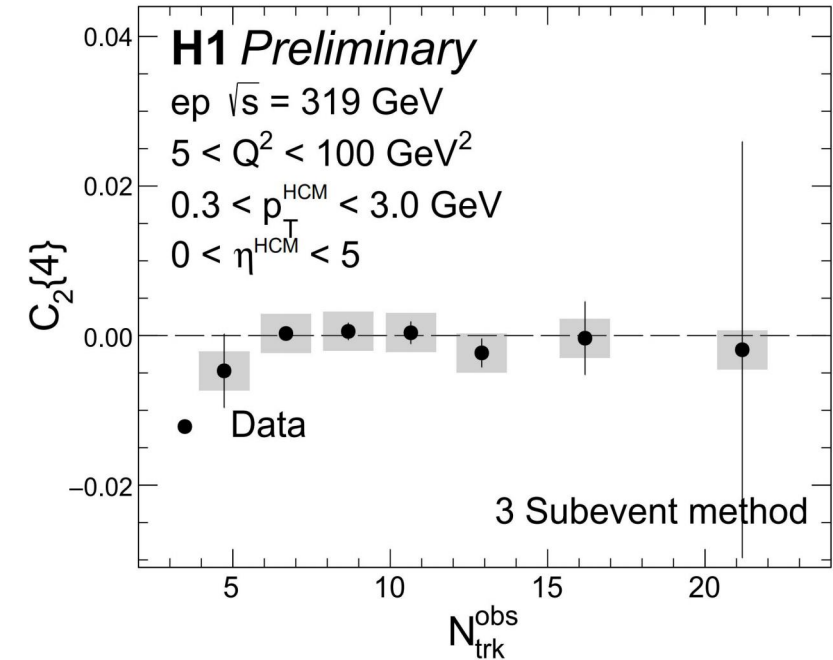
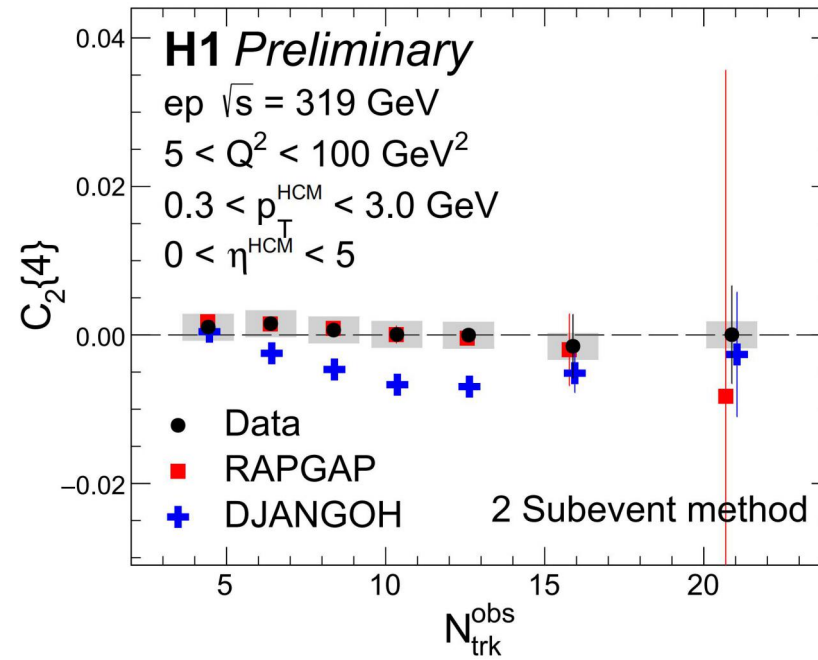
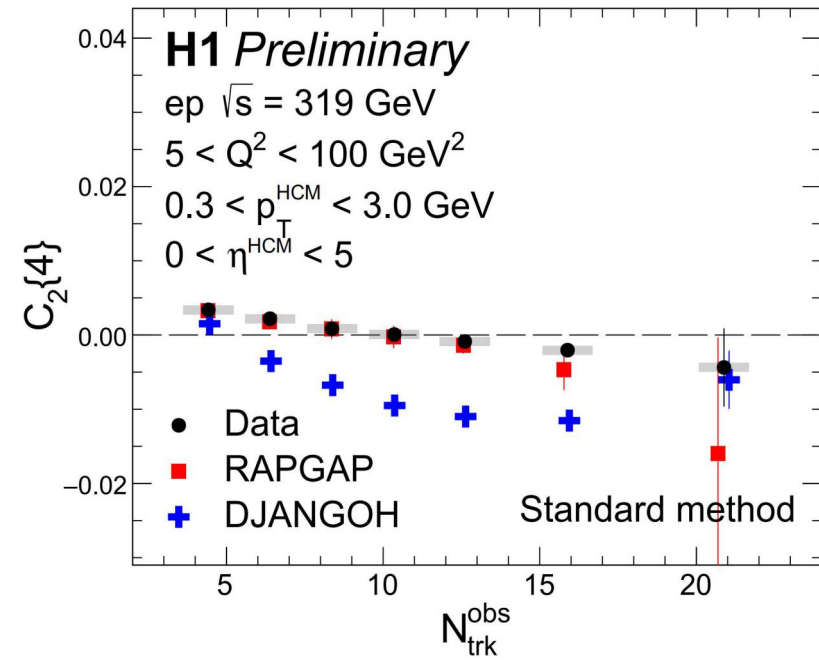
No obvious negative $C_2\{4\}$ in DIS

Multi-particle correlation in ep DIS



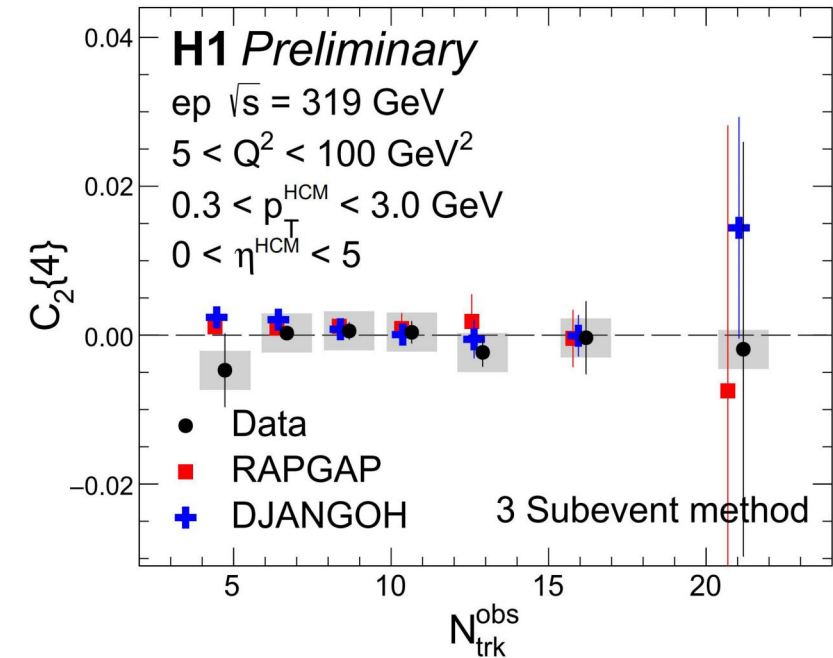
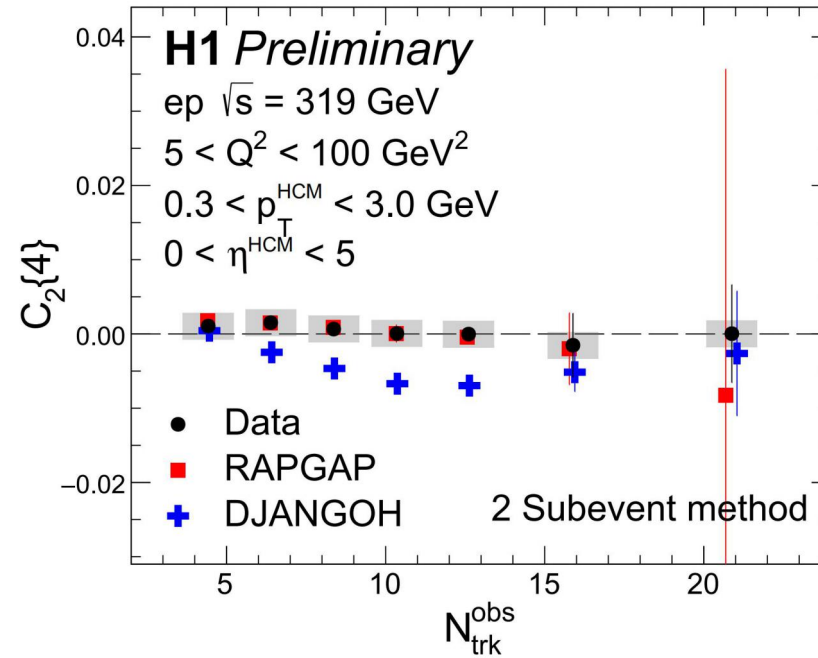
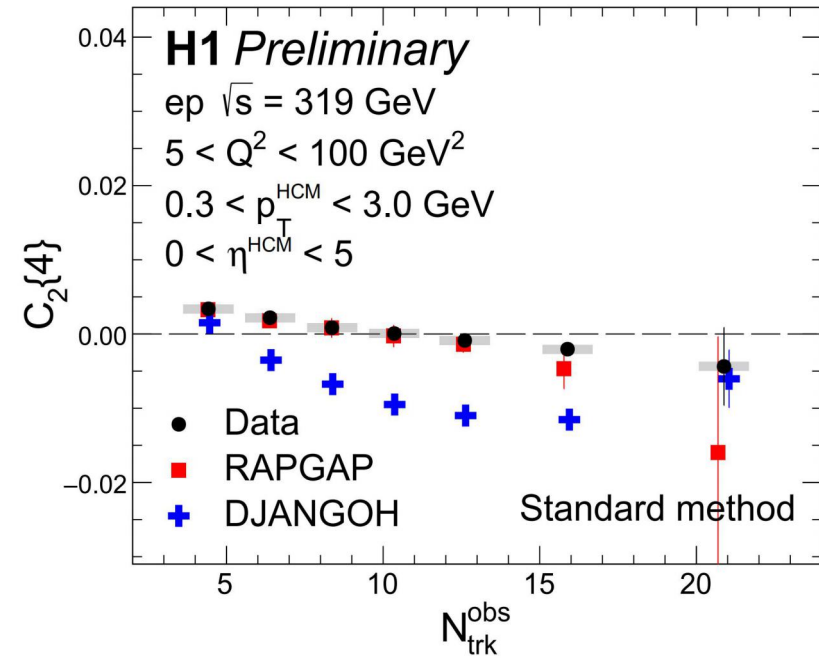
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Multi-particle correlation in ep DIS



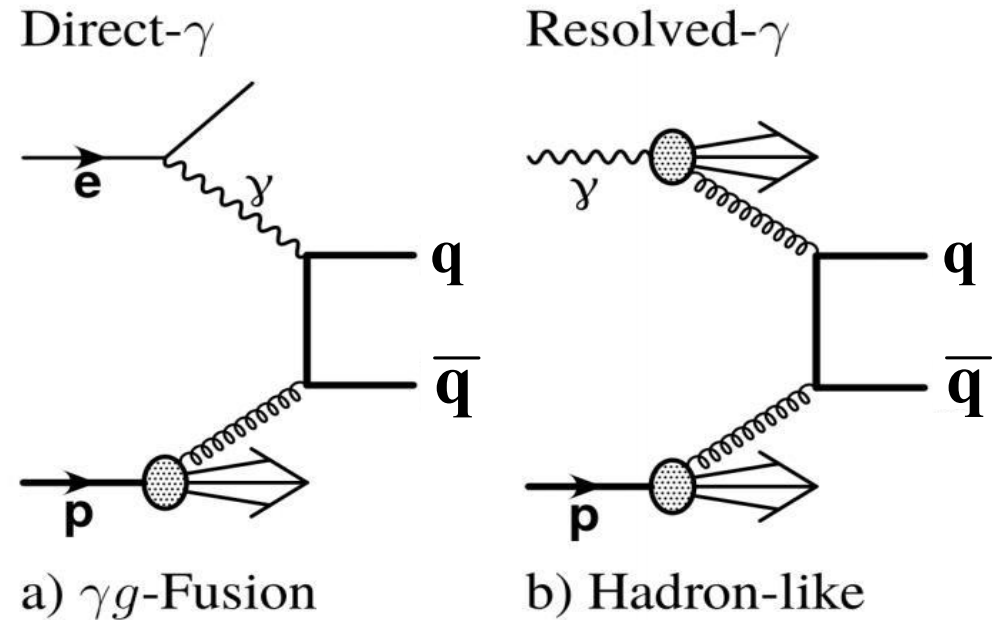
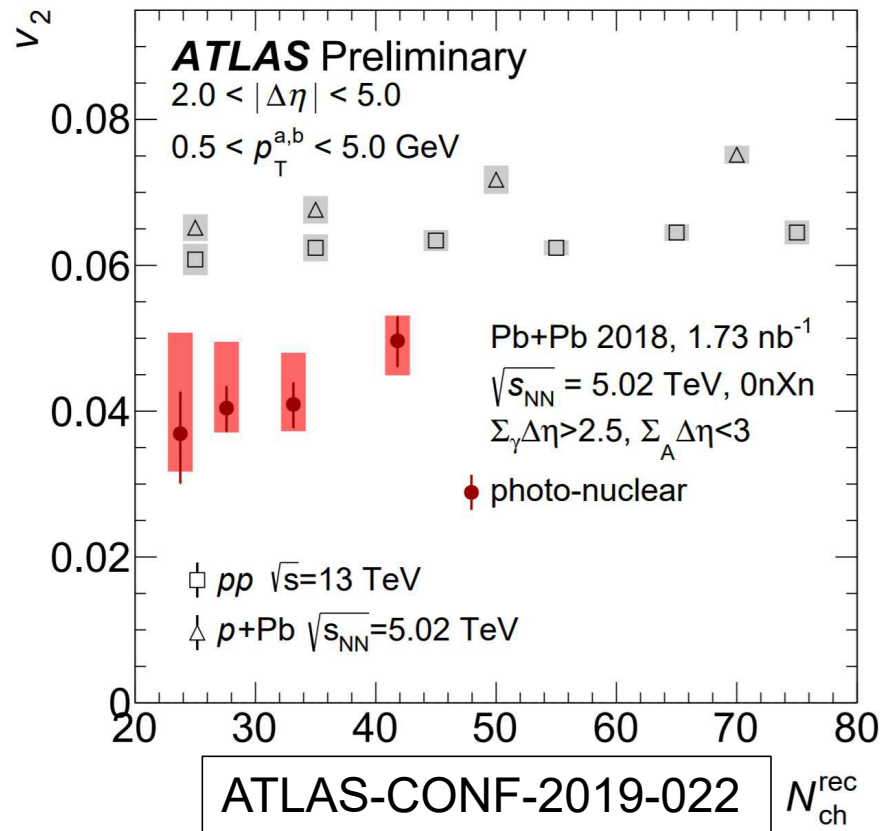
No obvious negative $C_2\{4\}$ in DIS

Multi-particle correlation in ep DIS



No obvious negative $C_2\{4\}$ in DIS
RAPGAP has better agreement with data

Search for collectivity in ep photoproduction



Non-zero v_2 values observed in PbPb ultra-peripheral collisions(photo-nuclear collisions)
Evidence of collectivity in hadron-like collisions

The resolved photoproduction process in ep collisions can be regarded as hadronic collisions
Collectivity in ep photoproduction?

Ridge yield limit in ep photoproduction

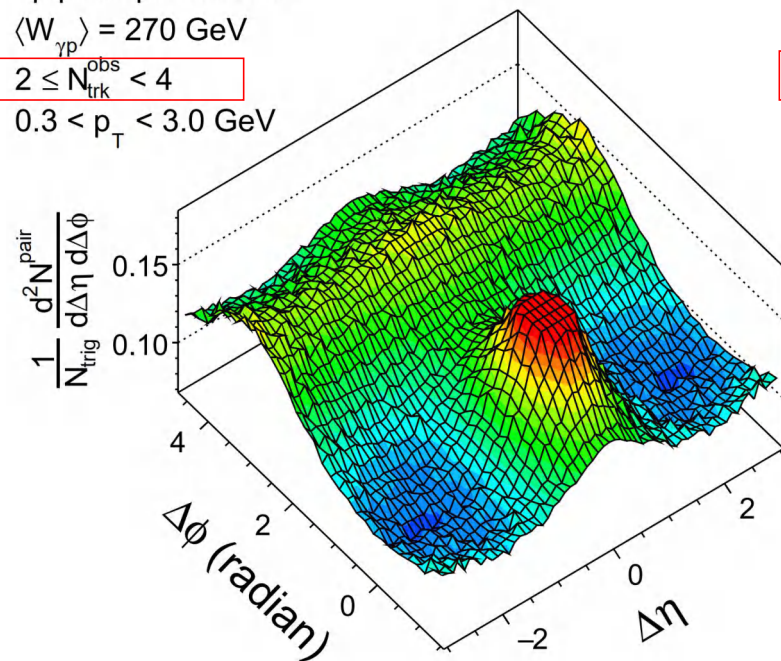
H1 Preliminary

ep photoproduction

$\langle W_{\gamma p} \rangle = 270$ GeV

$2 \leq N_{\text{trk}}^{\text{obs}} < 4$

$0.3 < p_{\text{T}} < 3.0$ GeV



low multiplicity

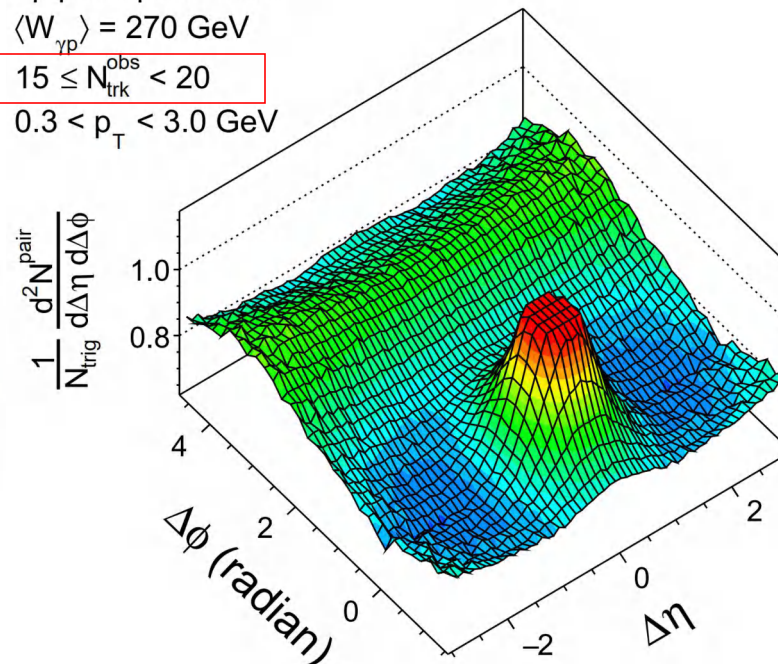
H1 Preliminary

ep photoproduction

$\langle W_{\gamma p} \rangle = 270$ GeV

$15 \leq N_{\text{trk}}^{\text{obs}} < 20$

$0.3 < p_{\text{T}} < 3.0$ GeV



high multiplicity

No near-side long-range ridge with H1
photoproduction data

photoproduction

Ridge yield limit in ep photoproduction

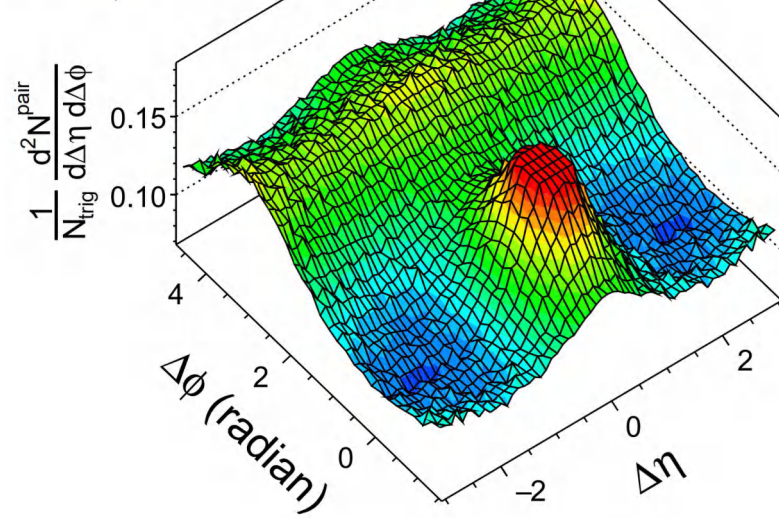
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low multiplicity

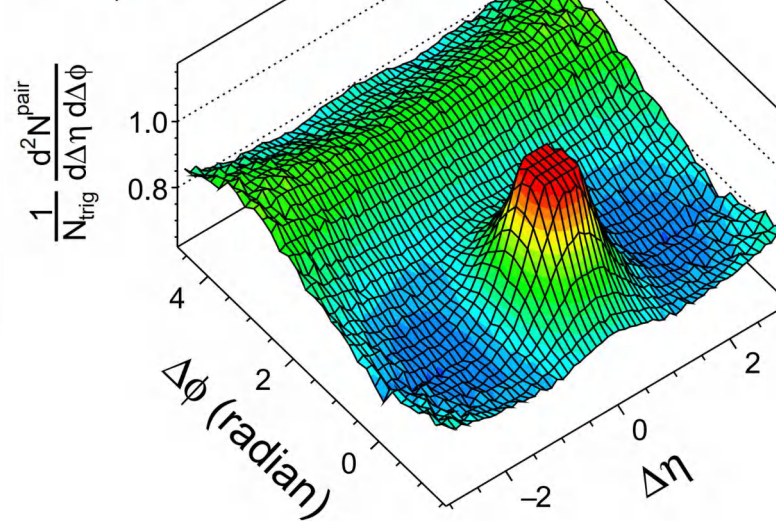
H1 Preliminary

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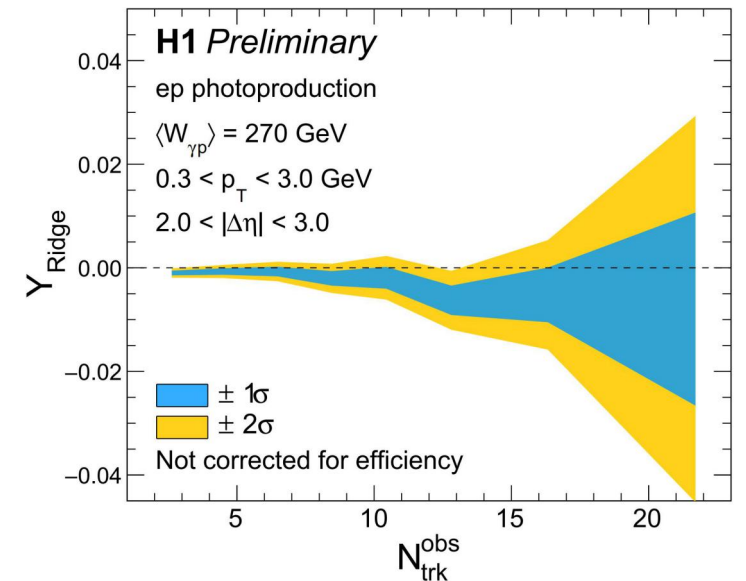
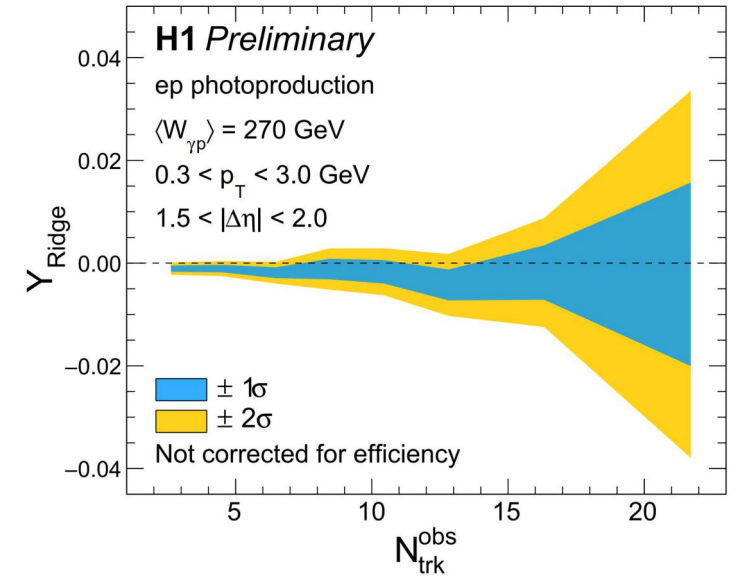


high multiplicity

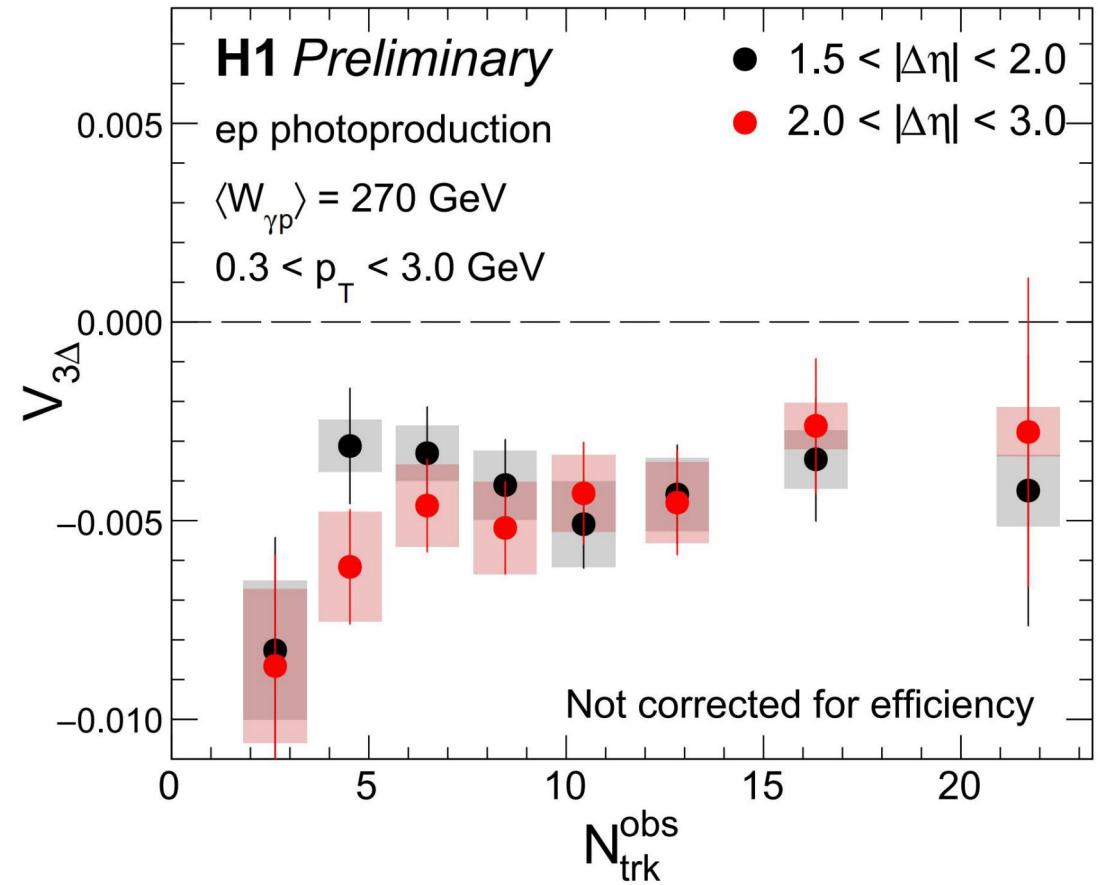
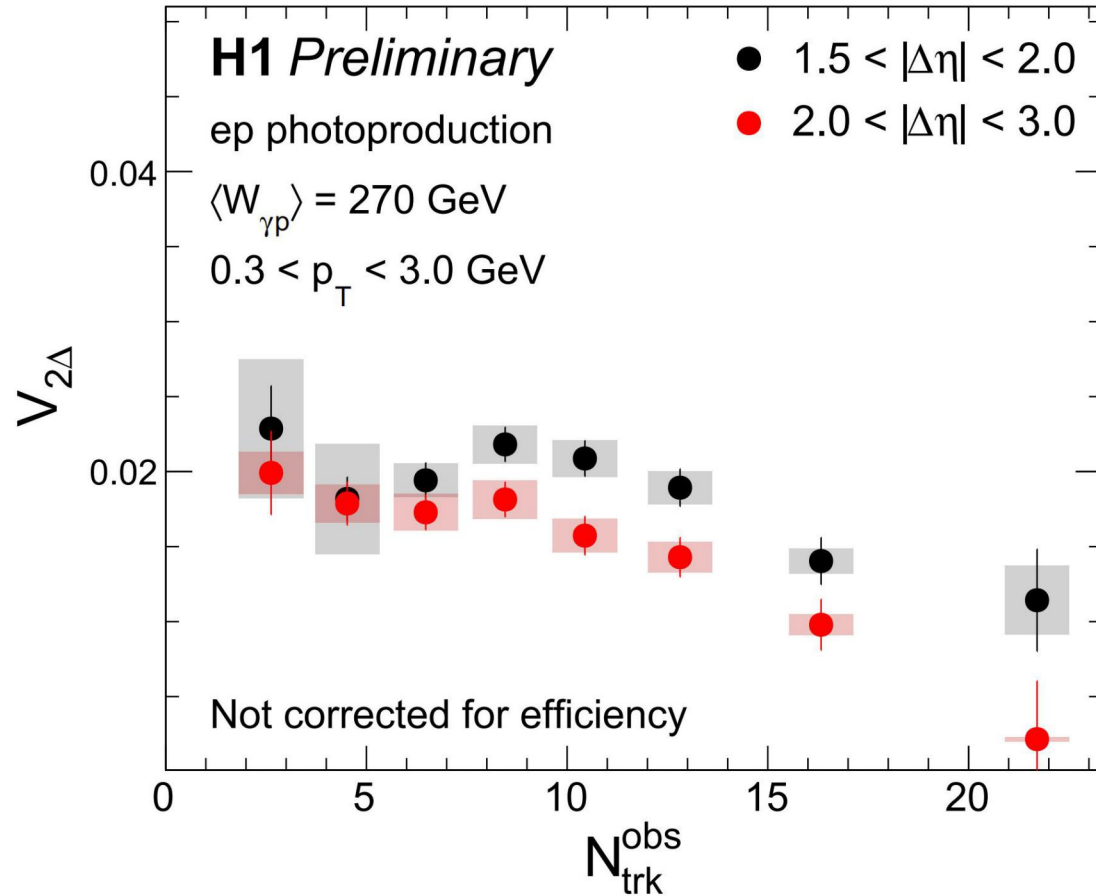
No near-side long-range ridge with H1
photoproduction data

Limits indicate small room for existence of ridge

photoproduction



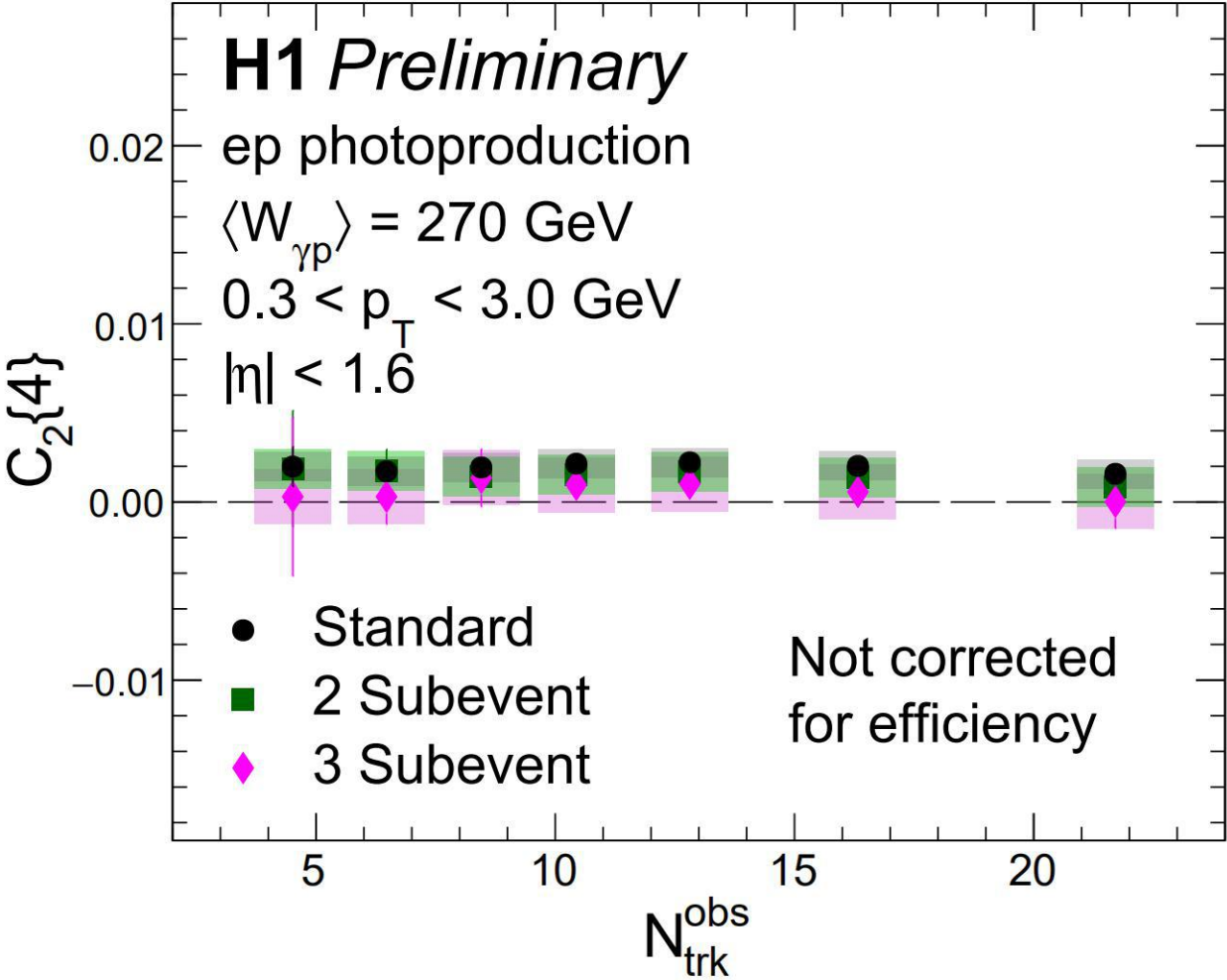
Fourier coefficient $V_{n\Delta}$ in ep photoproduction



Similar behavior in photoproduction data as in DIS

photoproduction

Multi-particle correlation in ep photoproduction



No evidence of negative $C_2\{4\}$, no sign of collectivity

photoproduction

Summary

Test of the predictions based on quantum entanglement in DIS H1 ep collisions

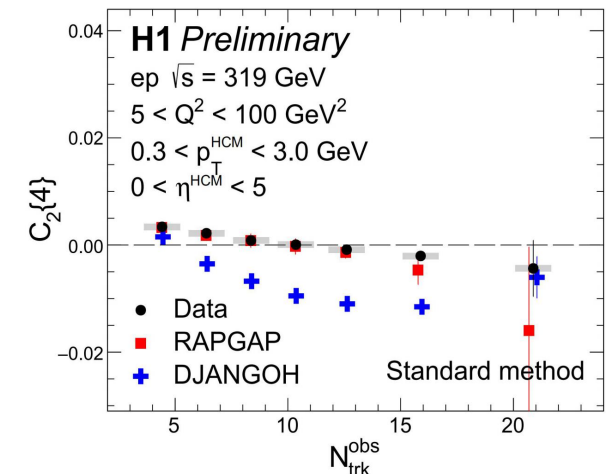
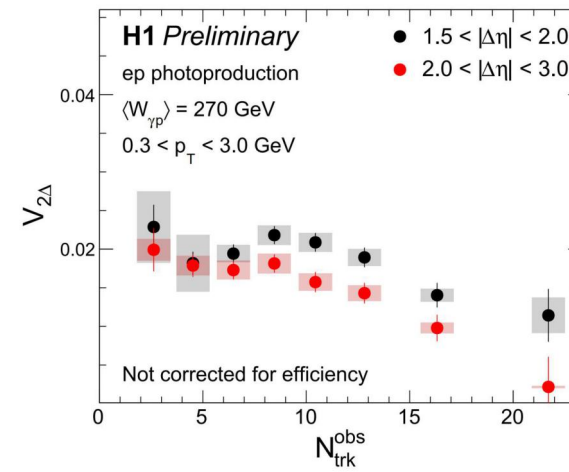
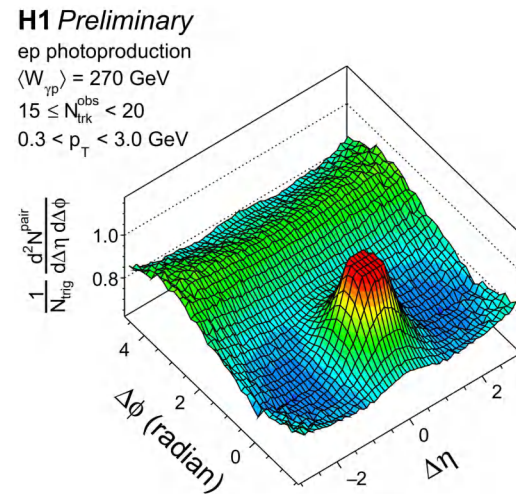
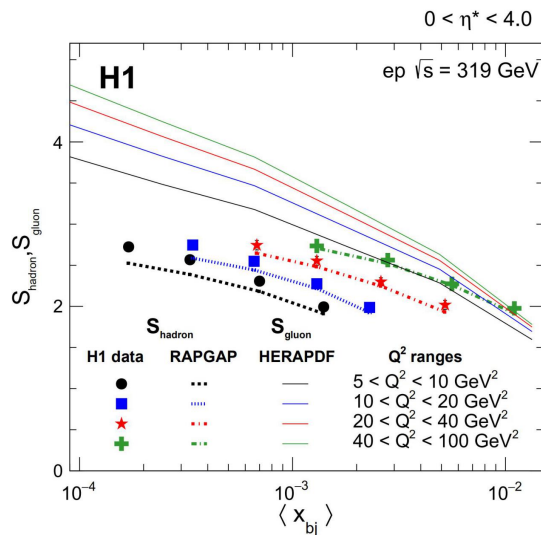
The predictions from the entropy of gluons disagree with the hadron entropy obtained from the multiplicity measurements

No collectivity observed in either DIS or photoproduction in H1 ep collisions

No long-range near-side ridge

$V_{2\Delta}, V_{3\Delta}$ in DIS can be described by RAPGAP w/o collectivity

No negative $C_2\{4\}$



Summary

Test of the predictions based on quantum entanglement in DIS H1 ep collisions

The predictions from the entropy of gluons disagree with the hadron entropy obtained from the multiplicity measurements

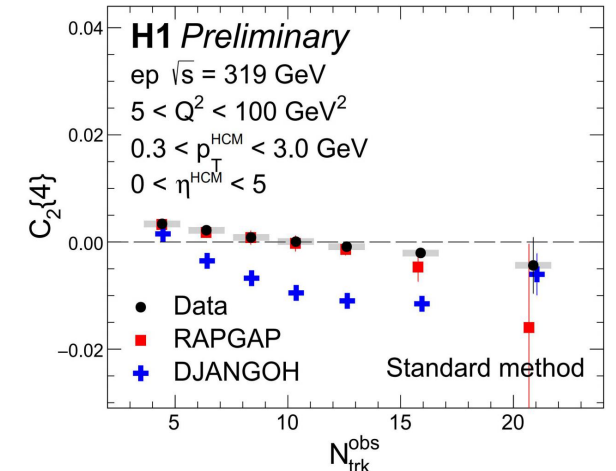
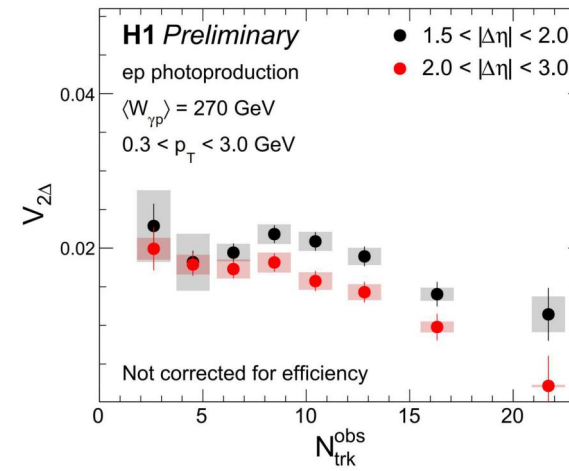
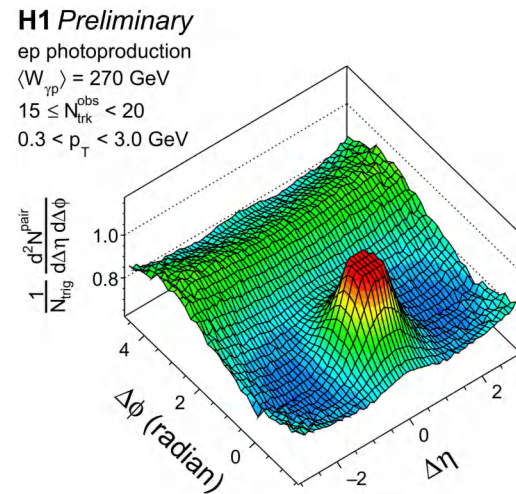
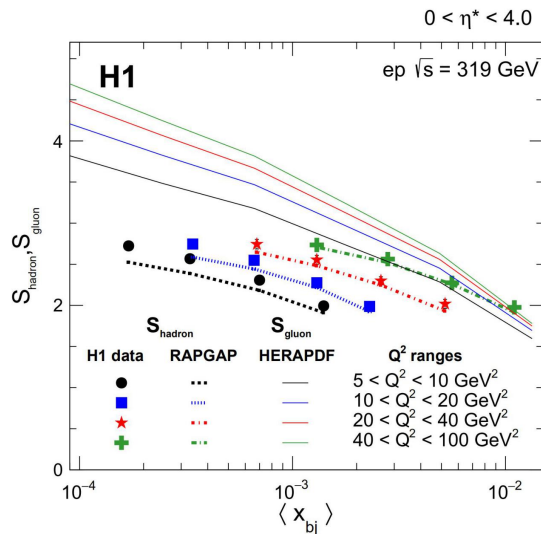
No collectivity observed in either DIS or photoproduction in H1 ep collisions

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$V_{2\Delta}, V_{3\Delta}$ in DIS can be described by RAPGAP w/o collectivity

No negative $C_2\{4\}$

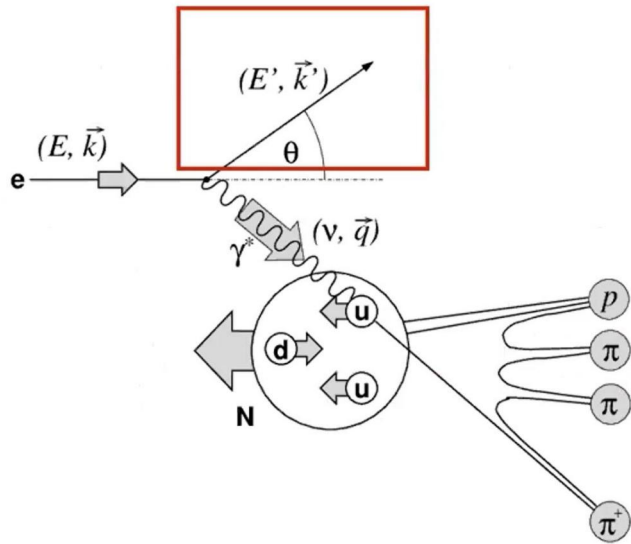
Are there any ridge structure in high multiplicity eA collisions? Stay tuned for EIC



Thanks for attention!

Back up

Kinematics in DIS

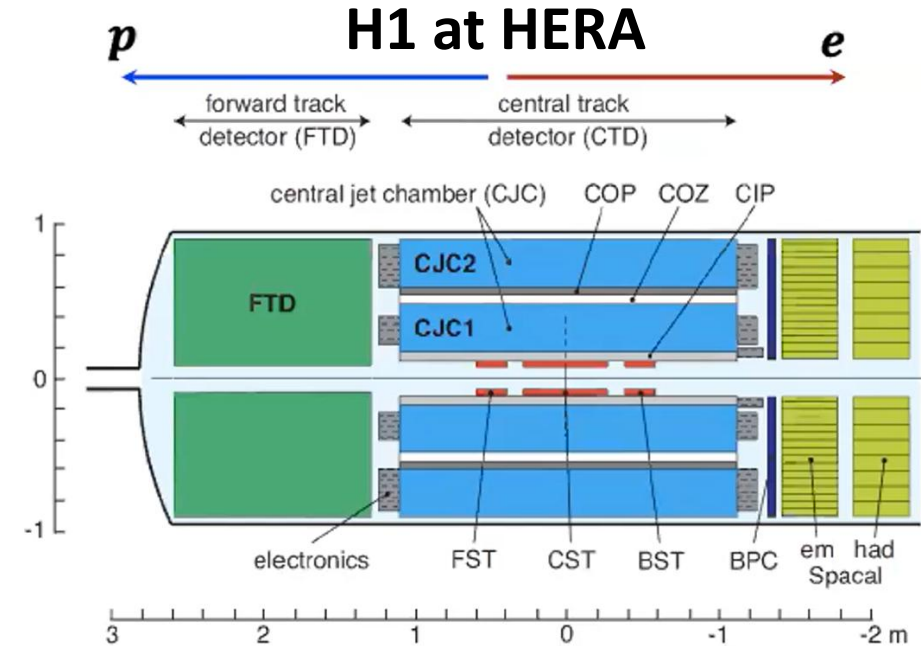


$$Q^2 = -q^2$$

$$y = \frac{\nu}{E_e} = \frac{E_e - E_{e'}}{E_e}$$

$$s = (k + P)^2$$

$$x = \frac{Q^2}{sy}$$



Textbook: we only need to measure scattered electron for kinematics. However, at HERA, there are as least 4-6 different methods to construct kinematics, and each method has its pros and cons. Not only electron is used.

SpalCal, EM Calorimeter to detect scattered electrons in degrees.
 CTD covers from 25-155 degrees. (backward~-1.5unit)
 FTD+FST covers 5-25 degrees.(forward~3unit)

Two-particle correlation method

In our analysis, the 2PC functions are filled with the difference $\Delta\eta$, $\Delta\Phi$ of particle pairs. The trigger particle is the charged particles in an event passing track selections. So in the same event, the signal distribution is per-trigger-particle yield of correlated pairs, including detector acceptance effects:

$$S(\Delta\eta, \Delta\phi) = \frac{1}{N_{trig}} \frac{d^2 N^{same}}{d\Delta\eta d\Delta\phi}$$

The mix-event background distributions is constructed with trigger particles from one event are correlating with all of the associated particles from different events within $|Z_{VTX}| < 2\text{cm}$. In this analysis, each event is paired with 5 randomly chosen events. The result is given by

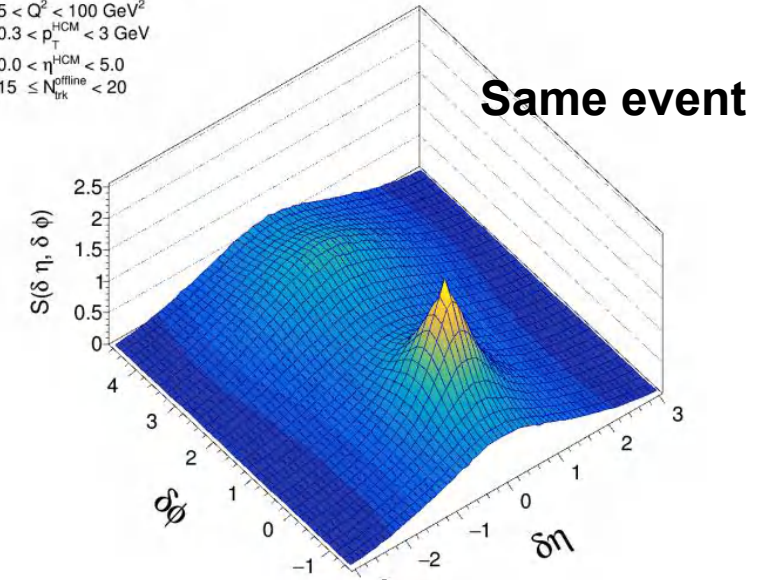
$$B(\Delta\eta, \Delta\phi) = \frac{1}{N_{trig}} \frac{d^2 N^{mix}}{d\Delta\eta d\Delta\phi}$$

The signal distribution, divided by the background distribution, is the final 2PC function. The pair acceptance of the detector can be corrected.

$$\frac{1}{N_{trig}} \frac{d^2 N^{pair}}{d\Delta\eta d\Delta\phi} = B(0, 0) \times \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)}$$

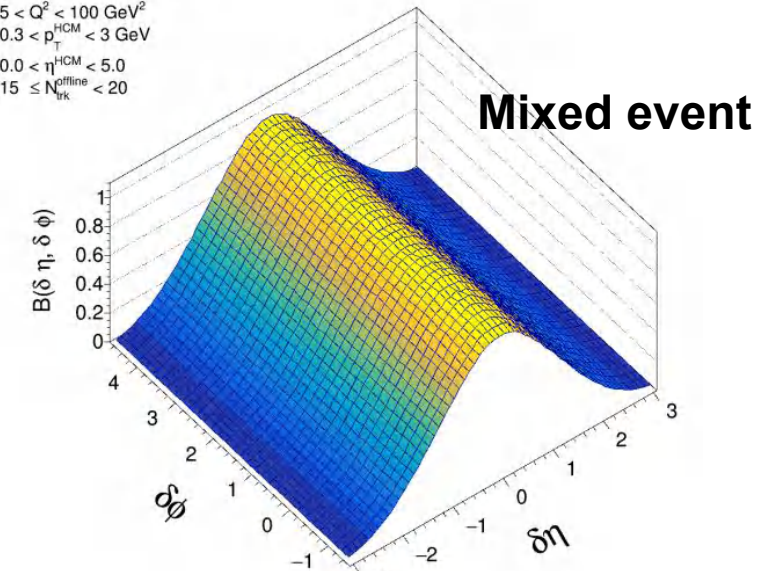
H1 DIS Data (HCM frame)

$5 < Q^2 < 100 \text{ GeV}^2$
 $0.3 < p_T^{HCM} < 3 \text{ GeV}$
 $0.0 < \eta^{HCM} < 5.0$
 $15 \leq N_{trk}^{offline} < 20$



H1 DIS Data (HCM frame)

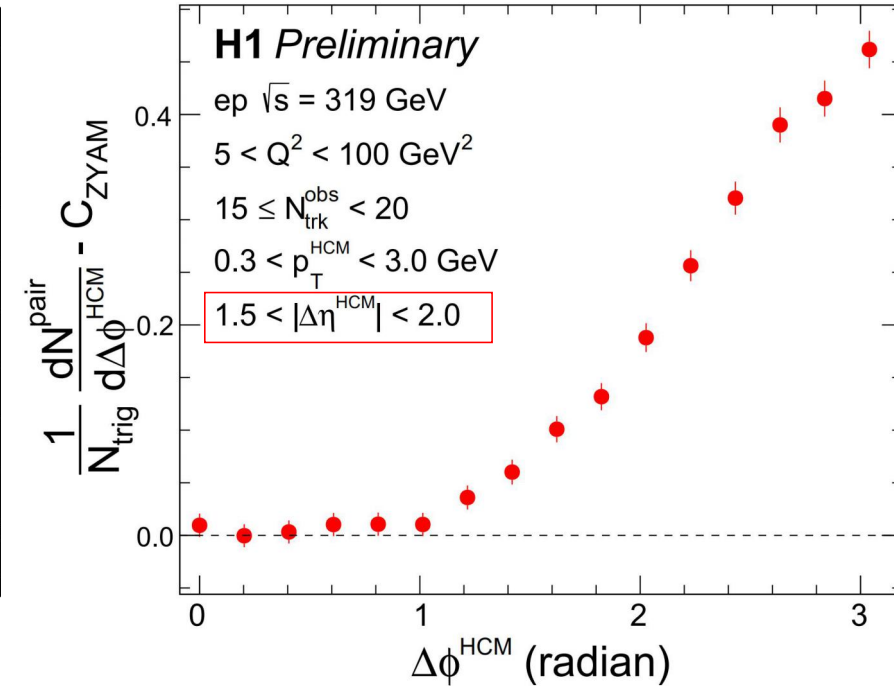
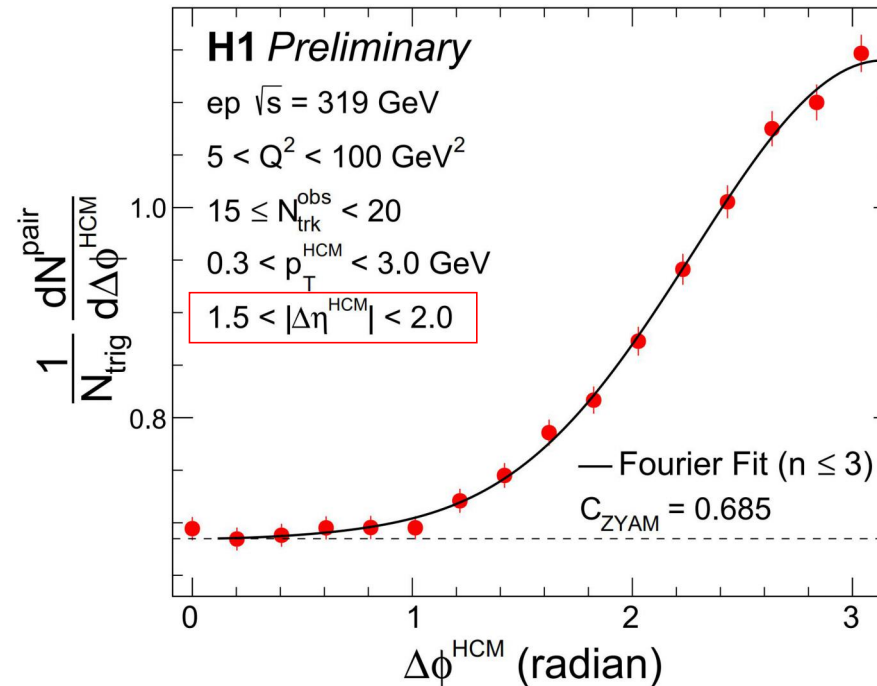
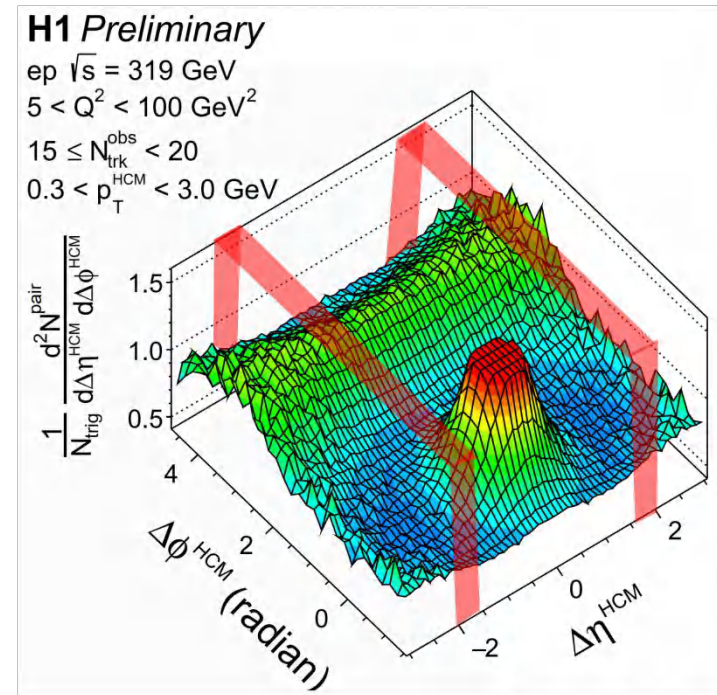
$5 < Q^2 < 100 \text{ GeV}^2$
 $0.3 < p_T^{HCM} < 3 \text{ GeV}$
 $0.0 < \eta^{HCM} < 5.0$
 $15 \leq N_{trk}^{offline} < 20$



Ridge yield extraction procedure

Zero-yield-at-minimum(ZYAM)

Phys.Rev.C 81 (2010) 014905



Step1: long-range 1D projection

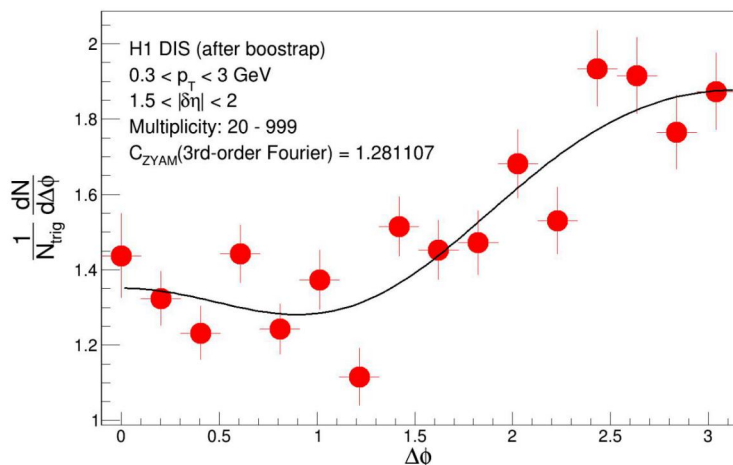
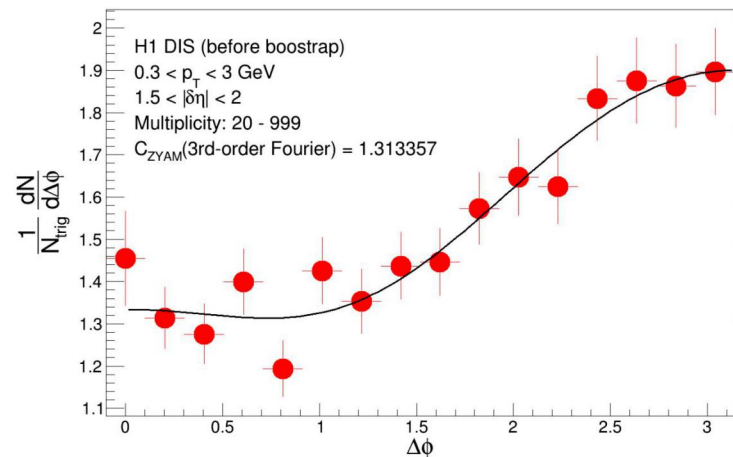
Step2: third-order Fourier fit

Step3: subtraction

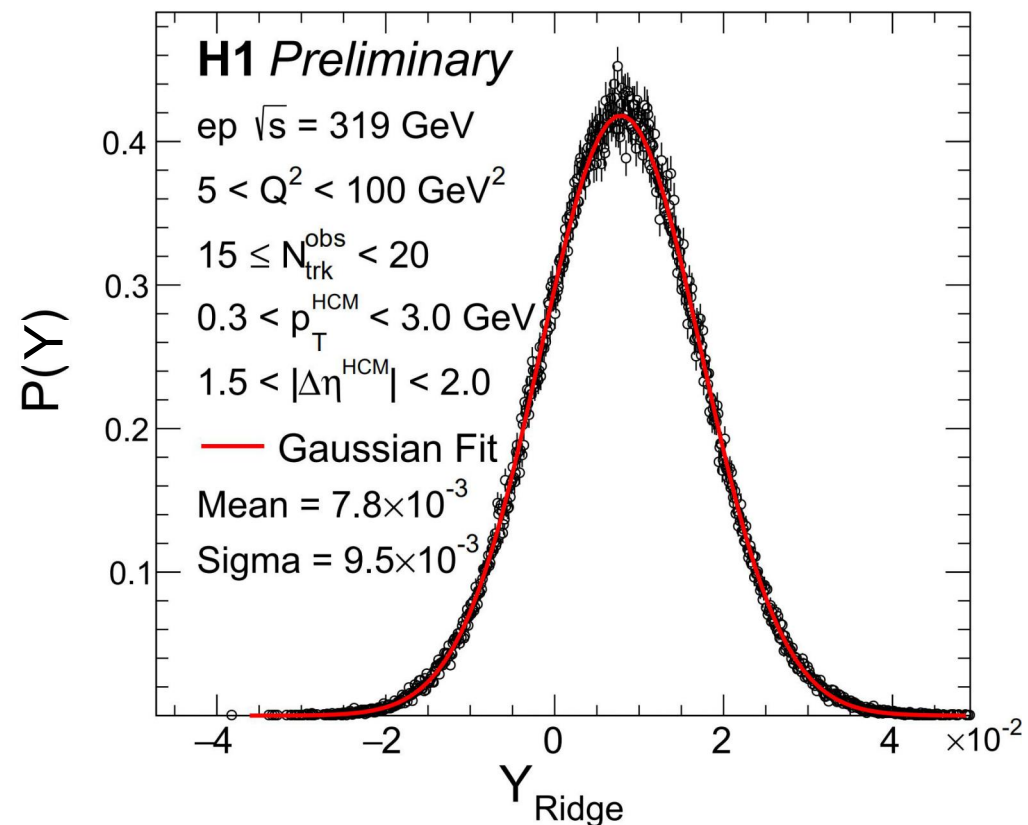
Then integrate from $\Delta\Phi=0$ to where the minimum value of ZYAM occurs as the ridge yield value

Bootstrap procedure

Each azimuthal differential yield distribution is varied according to their statistical and systematic uncertainties
One time bootstrap, one new ridge yield value



Each yield distribution is sampled 2.5×10^5 times

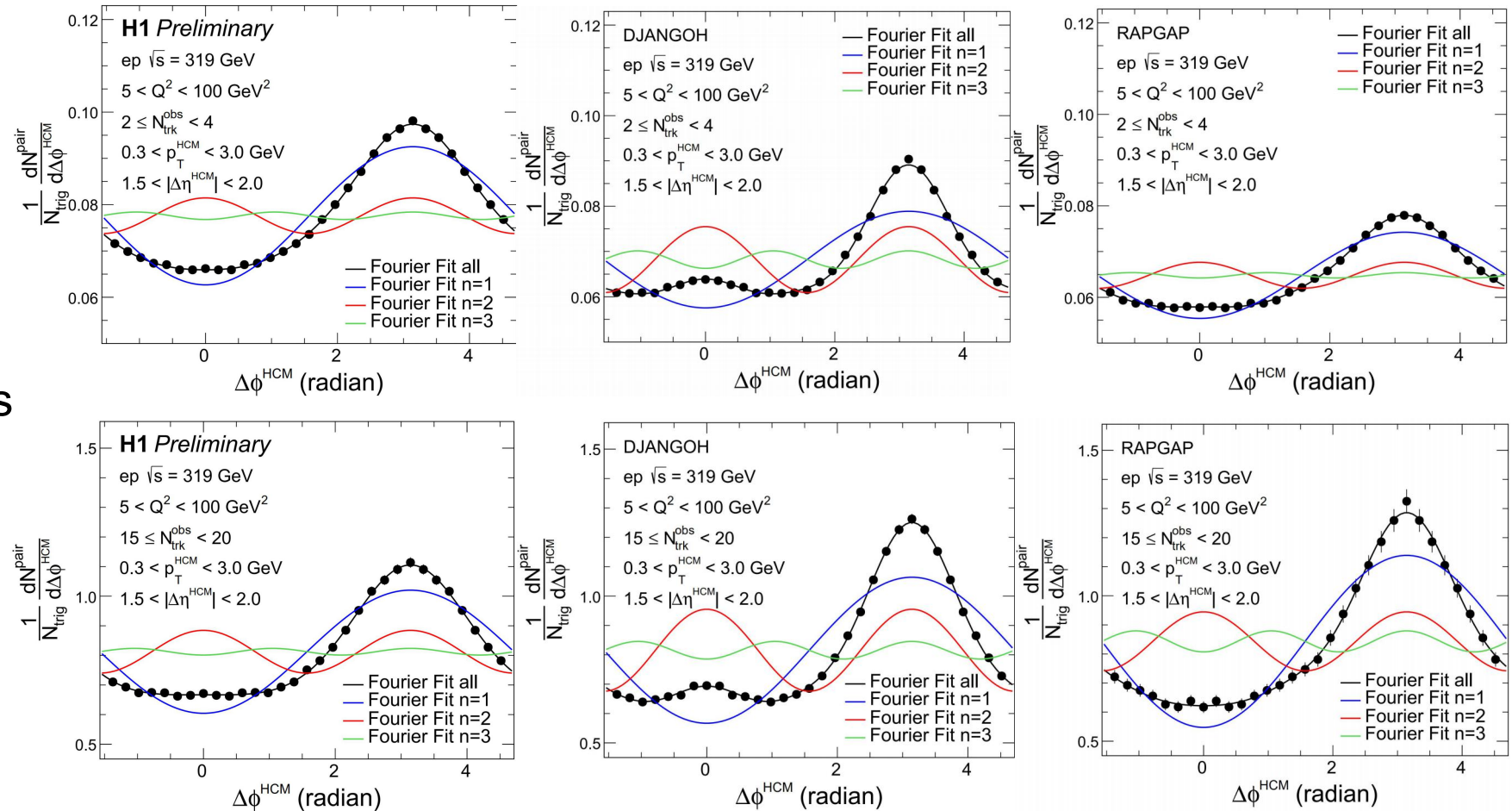


Ridge yield limit extracted from the mean and sigma value of the Gaussian function

Fourier coefficient $V_{n\Delta}$ extraction procedure

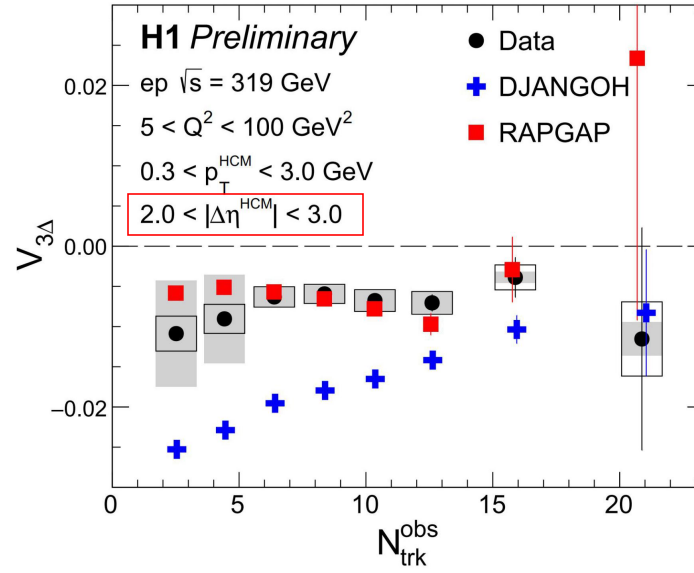
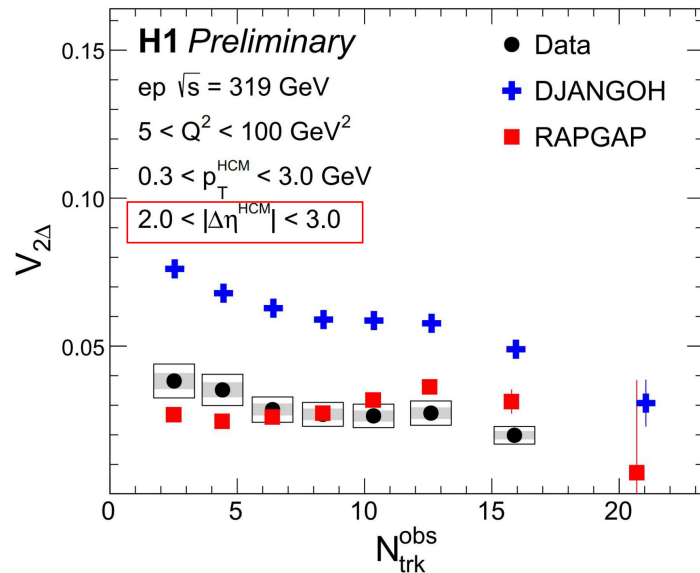
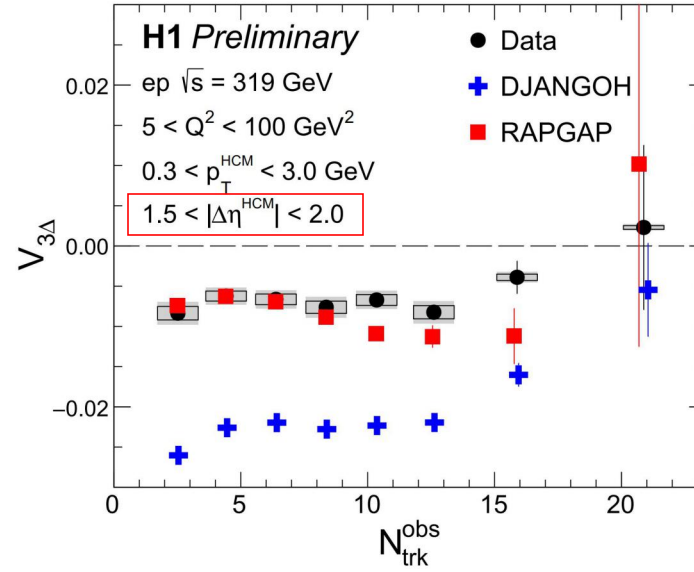
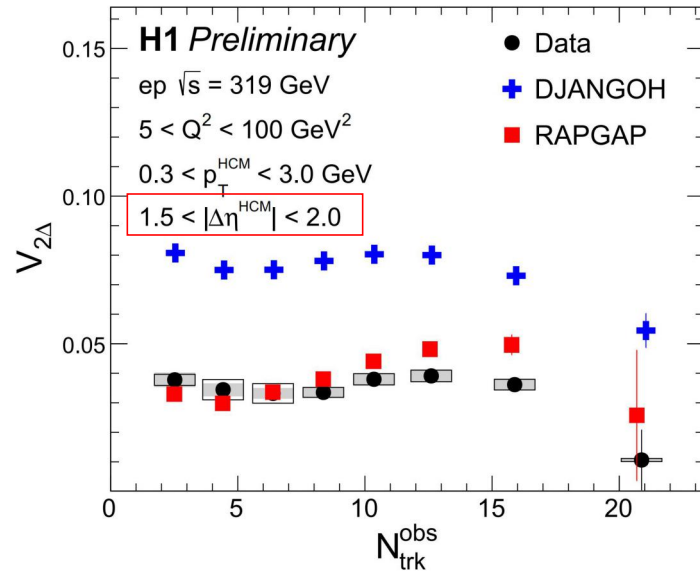
The azimuthal anisotropy harmonics are determined from a Fourier decomposition of long-range two-particle correlation functions on $\Delta\phi$ direction.

1-D comparisons



The comparison between data and MCs. Similar shapes in high and low multiplicity.

Fourier coefficient $V_{n\Delta}$



MC RAPGAP has better description on DIS data than MC DJANGO
Data can be described by MC w/o collectivity

Mechanism in RAPGAP and DJANGO

Comput.Phys.Commun. 86 (1995) 147-161

Sov.J.Nucl.Phys. 15 (1972) 438-450, Yad.Fiz. 15 (1972) 781-807

The RAPGAP 3.1

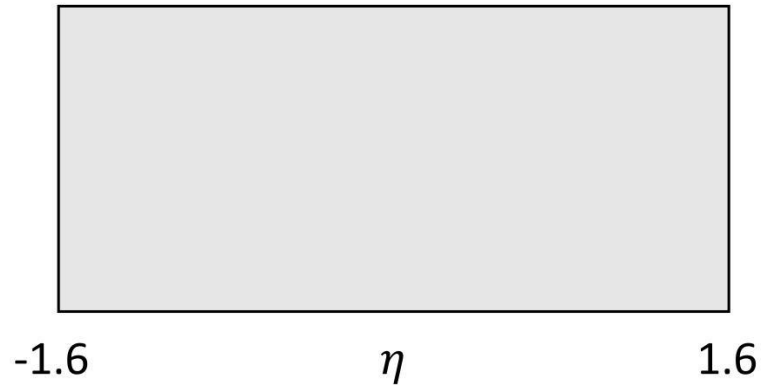
MC event generator matches **first order QCD matrix elements to the Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) parton showers** with strongly ordered transverse momenta of subsequently emitted partons. The factorisation and renormalisation scales are set to $u_f = u_r = \sqrt{Q^2 + \hat{p}_T^2}$, where \hat{p}_T is the transverse momentum of the outgoing hard parton from the matrix element in the center-of-mass frame of the hard subsystem. The CTEQ 6L leading order parametrisation of the parton density function (PDF) is used.

The DJANGO 1.4

MC event generator used the **Color Dipole Model (CDM) as implemented in ARIADNE, which models first order QCD processes and creates dipoles between colored partons**. Gluon emission is treated as radiation from these dipoles, and new dipoles are formed from the emitted gluons from which further radiation is possible. The radiation pattern of the dipoles includes interference effects, thus modelling gluon coherence. The transverse momenta of the emitted partons are not ordered in transverse momentum with respect to rapidity, producing a configuration **similar to the Balitsky-Fadin-Kuraev-Lipatov (BFKL) treatment of parton evolution**. The CTEQ 6L at leading order is used as the PDF.

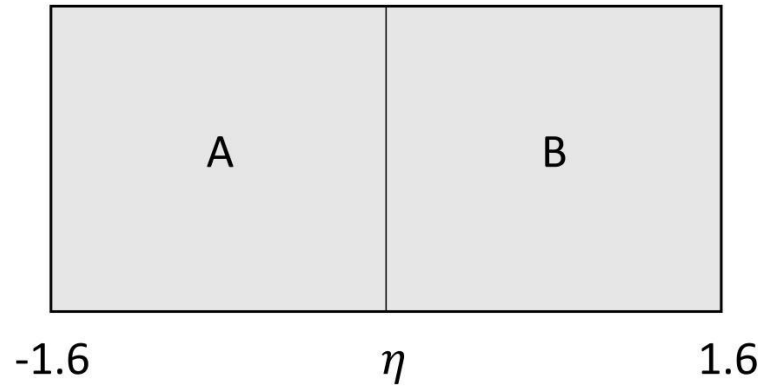
Multi-particle correlation

Standard method



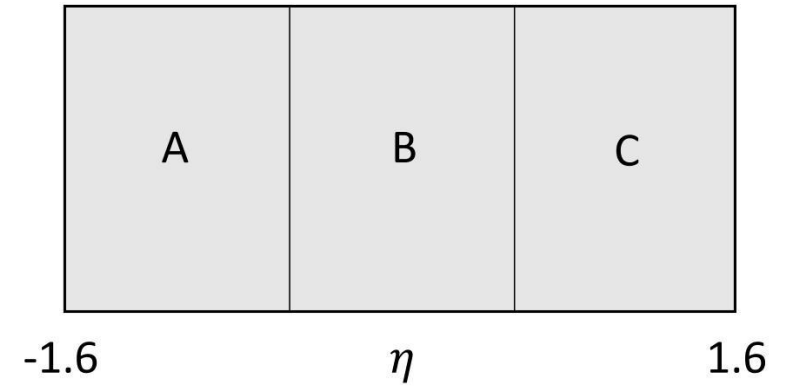
4 particles from the same range

2 sub-event method



2 particles from A
2 particles from B

3 sub-event method



1 particle from A
2 particles from B
1 particle from C

More advanced sub-event methods can further suppress few particle correlation

Method paper: Phys. Rev. C **96**, 034906, arXiv.1701.03830

2 and 3-subevent methods provide more reliable results on collectivity