



# Attributions of fluctuations in azimuthal anisotropies

by

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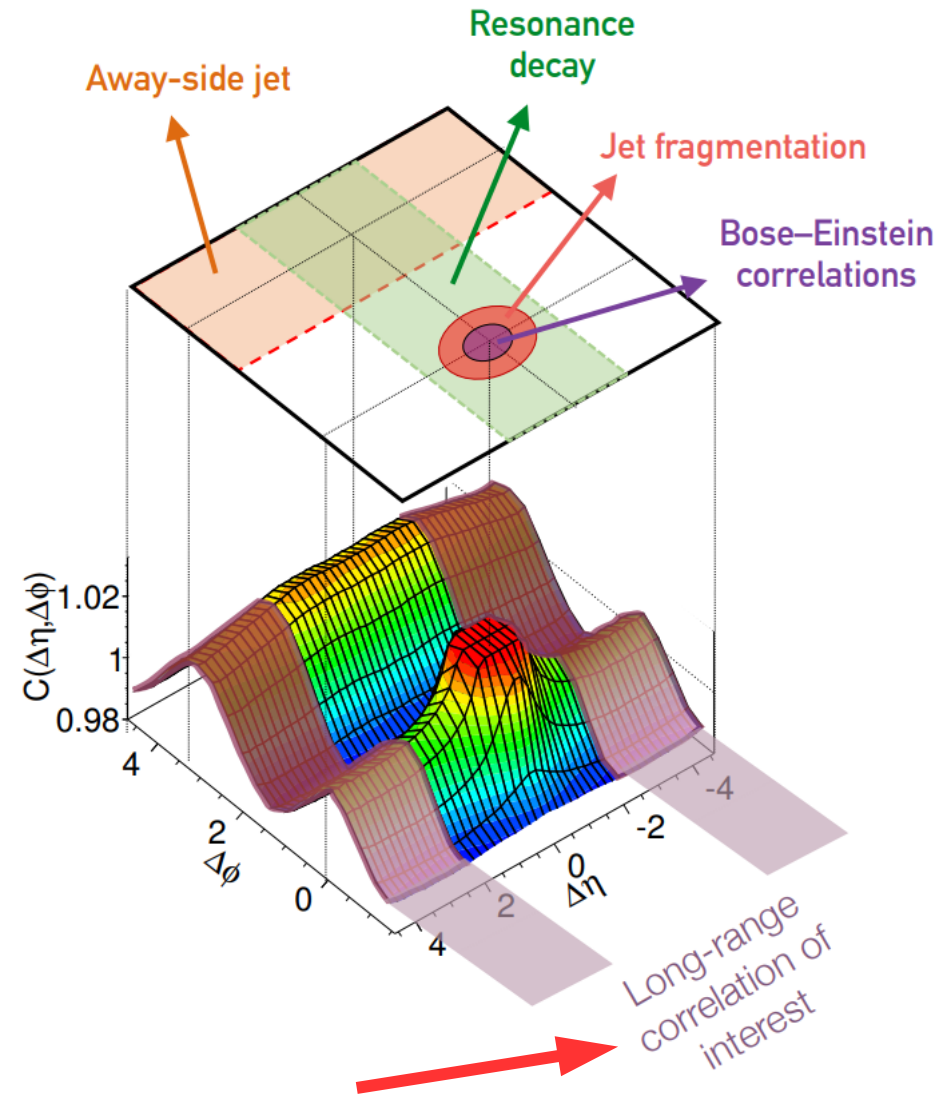
ANISOTROPY IN LARGE AND SMALL SYSTEMS



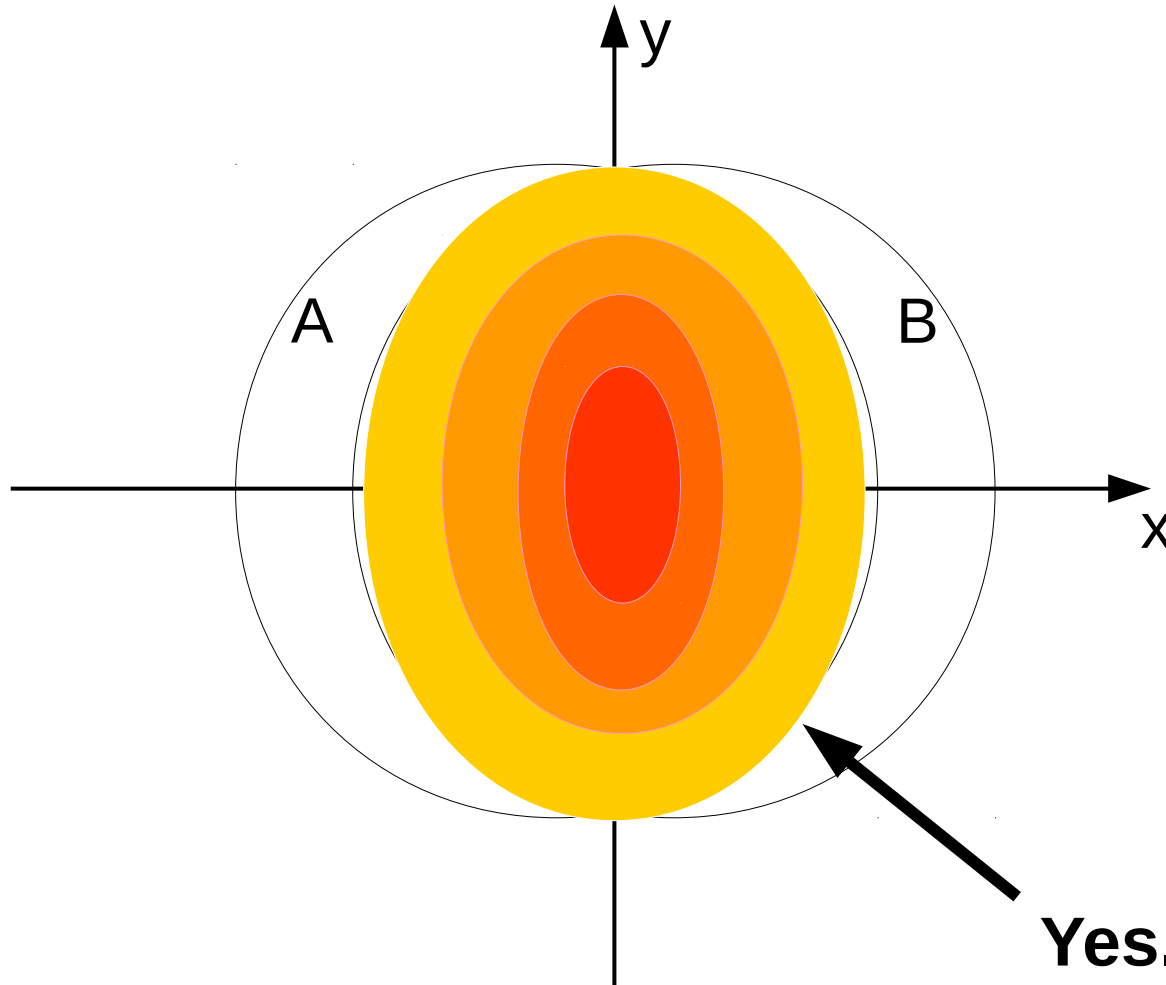
FLUCTUATIONS ON DIFFERENT SCALES

IN THIS TALK:

- Anisotropy is a collective long-range phenomenon.
- Fluctuations are dynamical (driven by initial-state physics).
- **Focus on questions driven by new data/developments.**



# THE EXOTIC QUESTION is there anisotropy without fluctuations?



[Ollitrault, 1992]

Eccentricity of the average energy density,  $\langle T^{00} \rangle$ .

$$\rightarrow \varepsilon = \frac{\int dx dy (x^2 - y^2) \langle T^{00}(x, y) \rangle}{\int dx dy (x^2 + y^2) \langle T^{00}(x, y) \rangle}$$

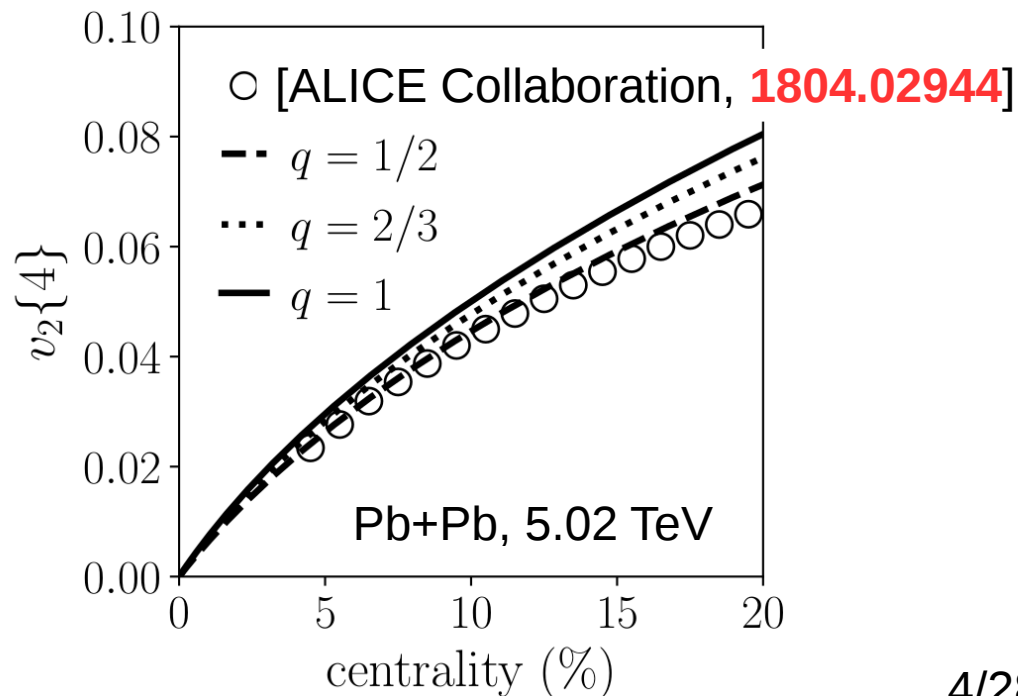
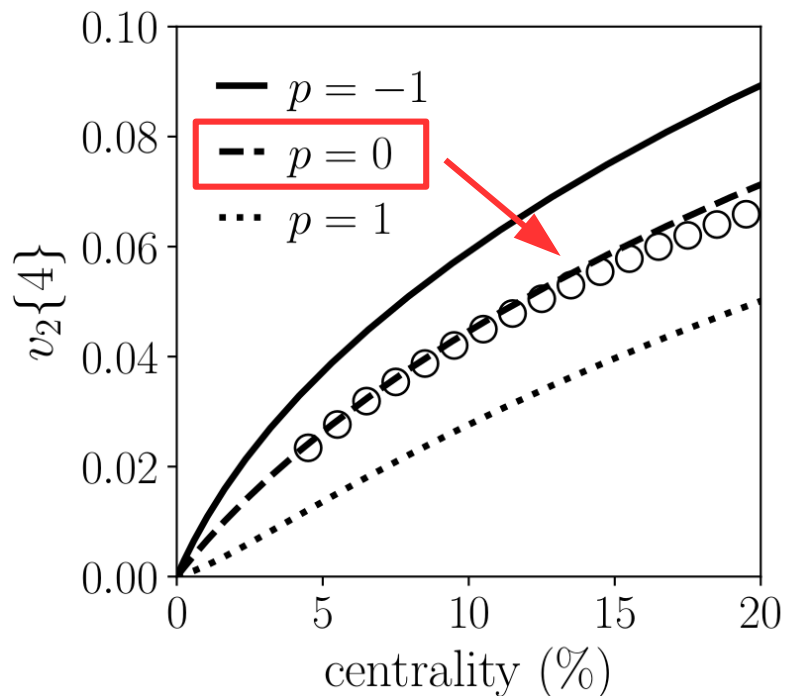
Central to mid-central collisions, one has:

$$v_2\{4\} \approx \kappa \varepsilon \rightarrow \boxed{\kappa \sim 0.25 \text{ with ALICE cuts}}$$

I dub  $T_A$  and  $T_B$  the optical participant densities.

$$\langle T^{00}(\mathbf{x}) \rangle \propto \left( \frac{T_A^p(\mathbf{x}) + T_B^p(\mathbf{x})}{2} \right)^{1/p}$$

$$\langle T^{00}(\mathbf{x}) \rangle \propto \left( T_A(\mathbf{x}) T_B(\mathbf{x}) \right)^q$$



Experimental data suggests:

$$\left\langle T^{00}(\mathbf{x}, \tau = 0^+) \right\rangle \propto \left( T_A(\mathbf{x}) T_B(\mathbf{x}) \right)^q$$

**q=1** → prediction of the color glass condensate (CGC).  
[Lappi [hep-ph/0606207](#)]

**q=1/2** → Only TRENTo parametrization of the form  $T_A^* T_B$ .  
Strongly favored by Bayesian analyses.  
[Bass, Bernhard, Moreland [1412.4708](#), [1605.03954](#),  
[Nature Phys. 15 \(2019\)](#) ]

Time evolution of **q** is known fairly well.

[Lappi, Venugopalan [nucl-th/0609021](#)]

[Giacalone, Mazeliauskas, Schlichting, [1908.02866](#)]

**Average anisotropy in data is consistent with a CGC-like model.**

## 2005: Breakthrough discovery by the PHOBOS collaboration.

nucl-ex/0610037

At a given impact parameter:

$$\langle T^{00}(\mathbf{x})T^{00}(\mathbf{y}) \rangle - \langle T^{00}(\mathbf{x}) \rangle \langle T^{00}(\mathbf{y}) \rangle \neq 0$$

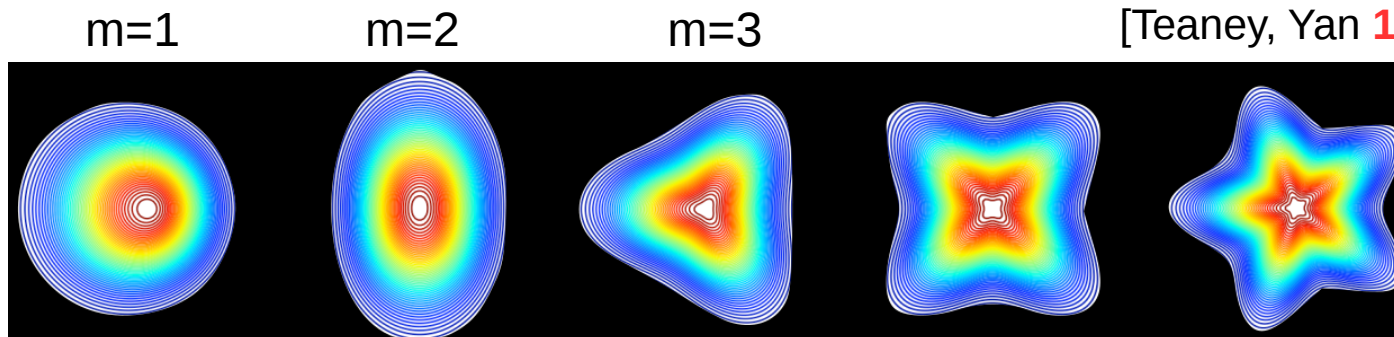
**The initial condition fluctuates event-by-event!**

Anisotropy is broken to all orders in the interaction region.  
The energy density has **non-vanishing multipole moments**.

$$\mathcal{E} \propto \int r dr d\phi r^m e^{im\phi} T^{00}(r, \phi) \neq 0$$

[Alver, Roland [1003.0194](#)]

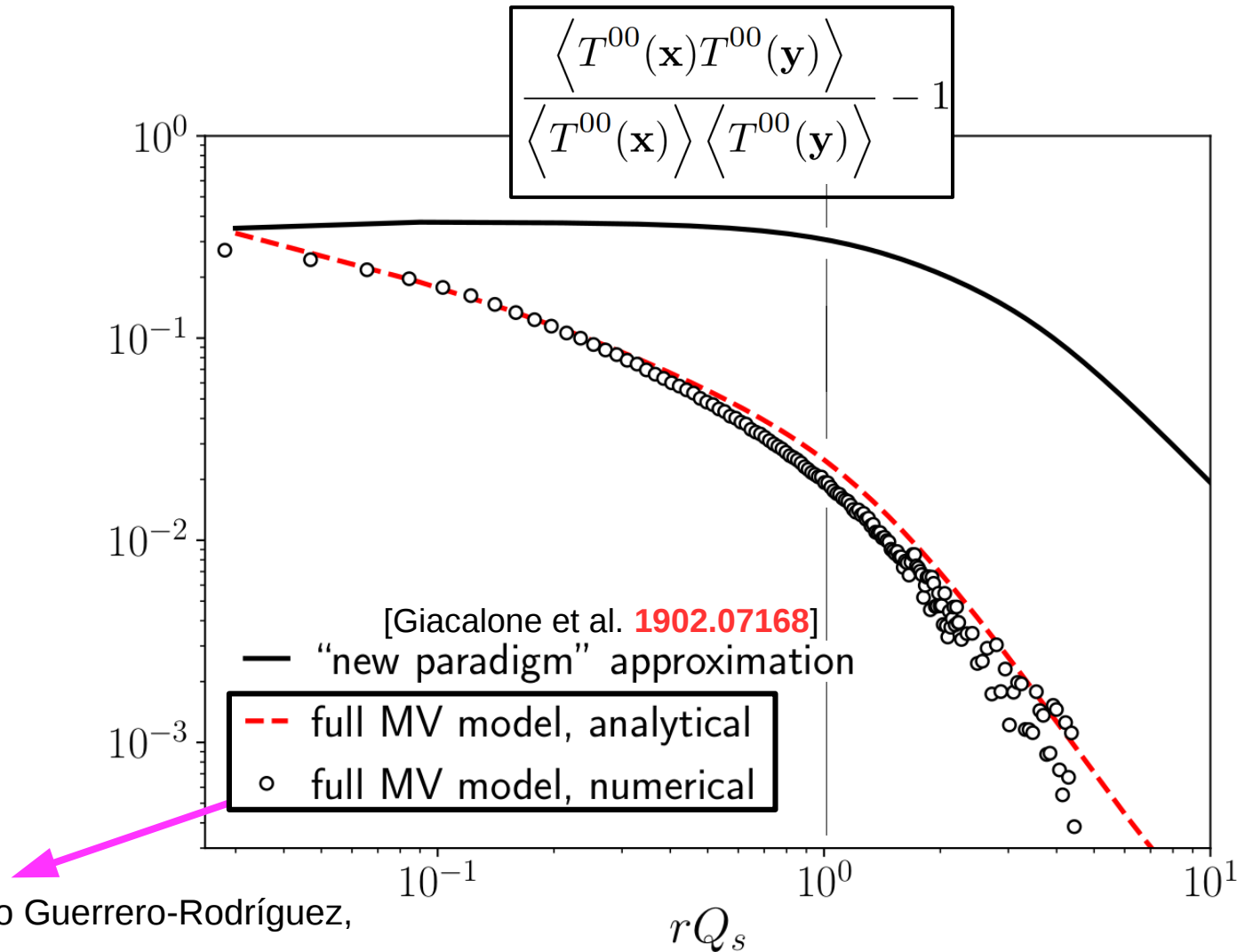
[Teaney, Yan [1010.1876](#)]



# Does the CGC give us also the fluctuations?

Connected 2-point function in the CGC derived in:

[Albacete, Guerrero-Rodriguez, Marquet [1808.00795](#)]



[courtesy: Pablo Guerrero-Rodríguez, Sanghoon Lim, Jamie Nagle]

**Color-charge fluctuations are small, scale is  $\sim 1/Q_s$ .**

**We need additional fluctuations on nuclear/hadronic scales.**

# ANISOTROPY #1 – nuclear structure: collective phenomena

Deformation: emergent property of nuclei.

Collective ‘organization’ of nucleons.

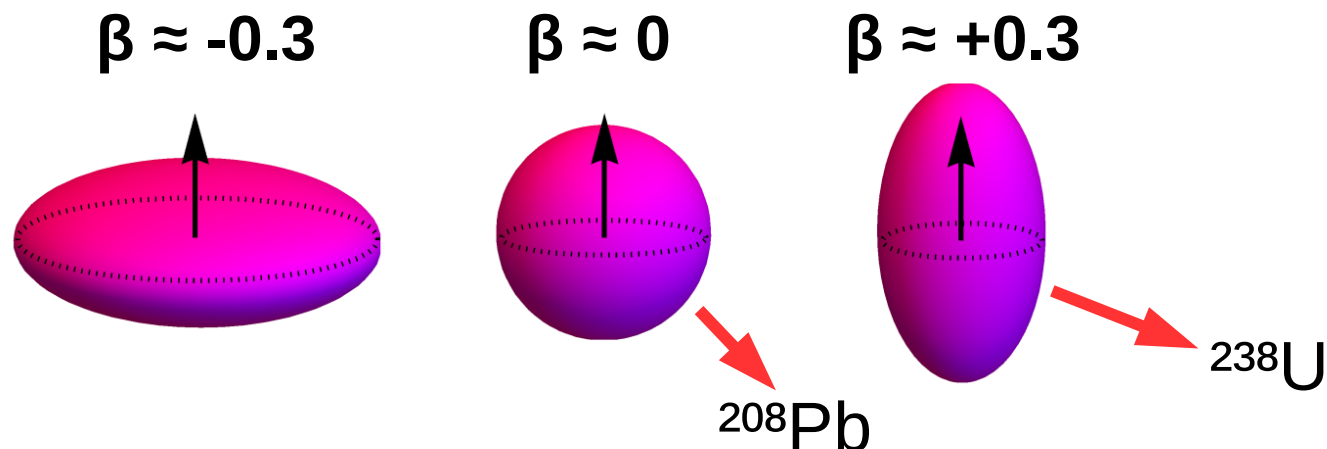
[Bohr, Mottelson 1957]

Rotational model: nuclei as ellipsoids with a random orientation.

$$Q_2 \propto \langle Y_2^0(\Theta, \Phi)r^2 \rangle \neq 0$$

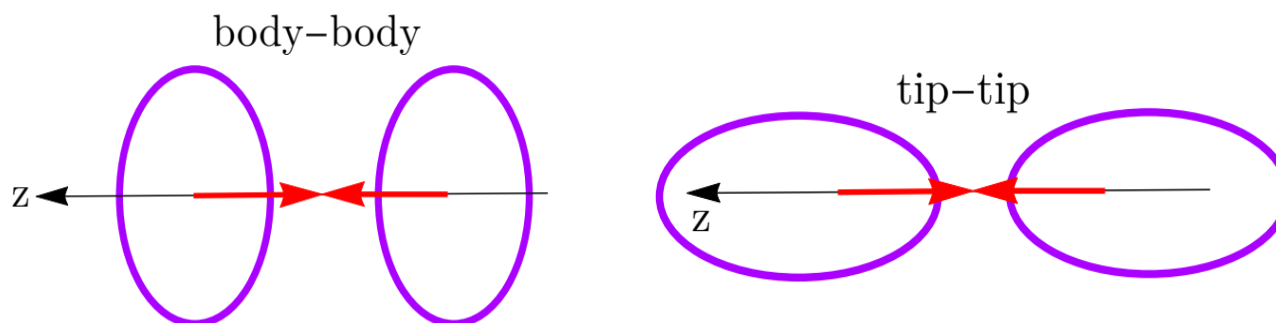
Dimensionless deformation parameter:

$$\beta \propto \frac{Q_2}{\langle r^2 \rangle}$$



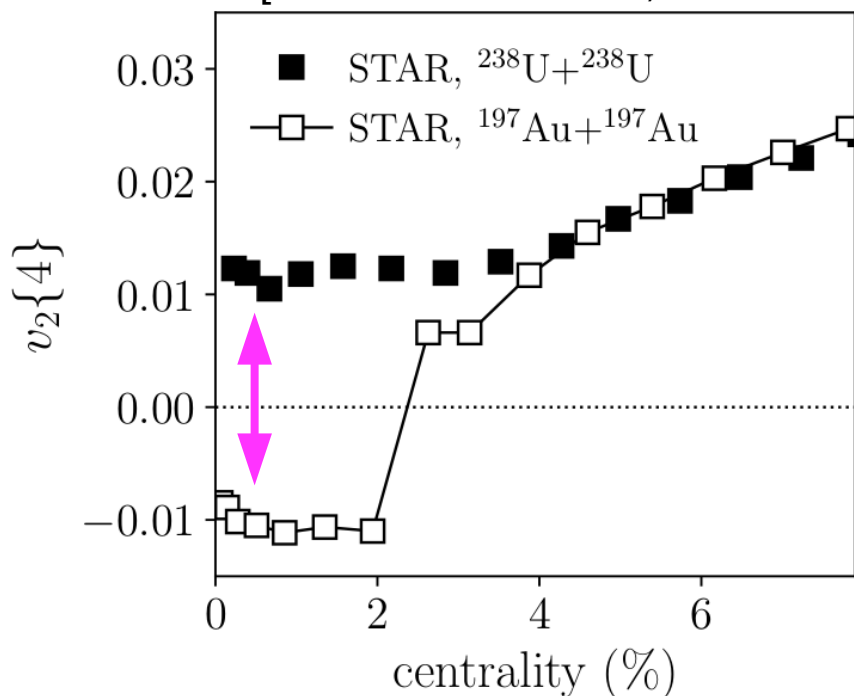


New source of fluctuations: the shape of the overlap area.

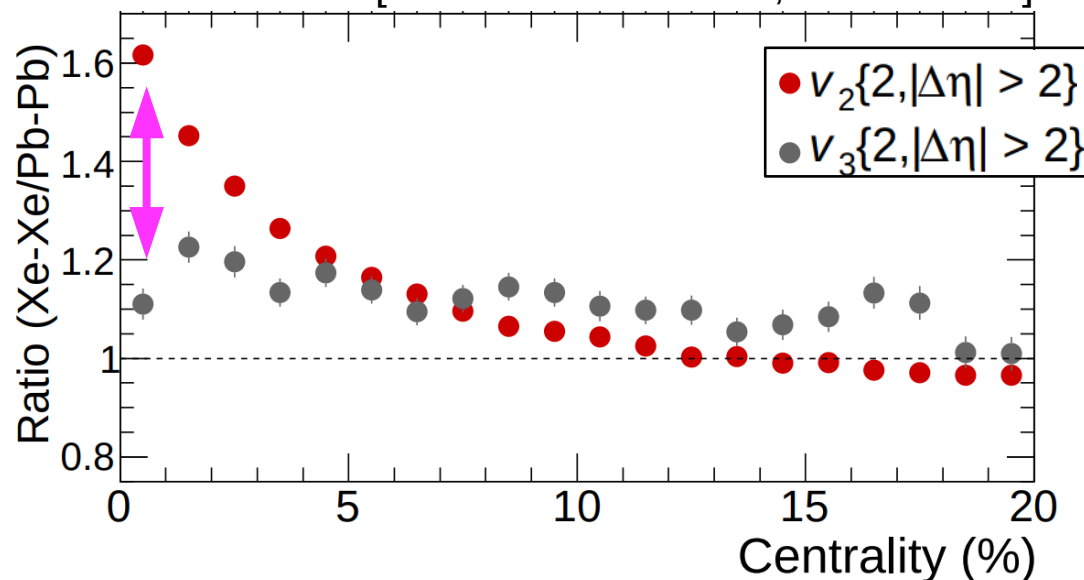


Manifestations observed in elliptic flow data.

[STAR Collaboration, 1505.07812]



[ALICE Collaboration, 1805.01832]



New spectacular signatures discovered at STAR this year.

[ Talk by J. Jia, Thursday Jan 14<sup>th</sup>, contribution #55 ]

# “Can Xe-Xe @ LHC have the same impact as Cu-Cu @ RHIC?”

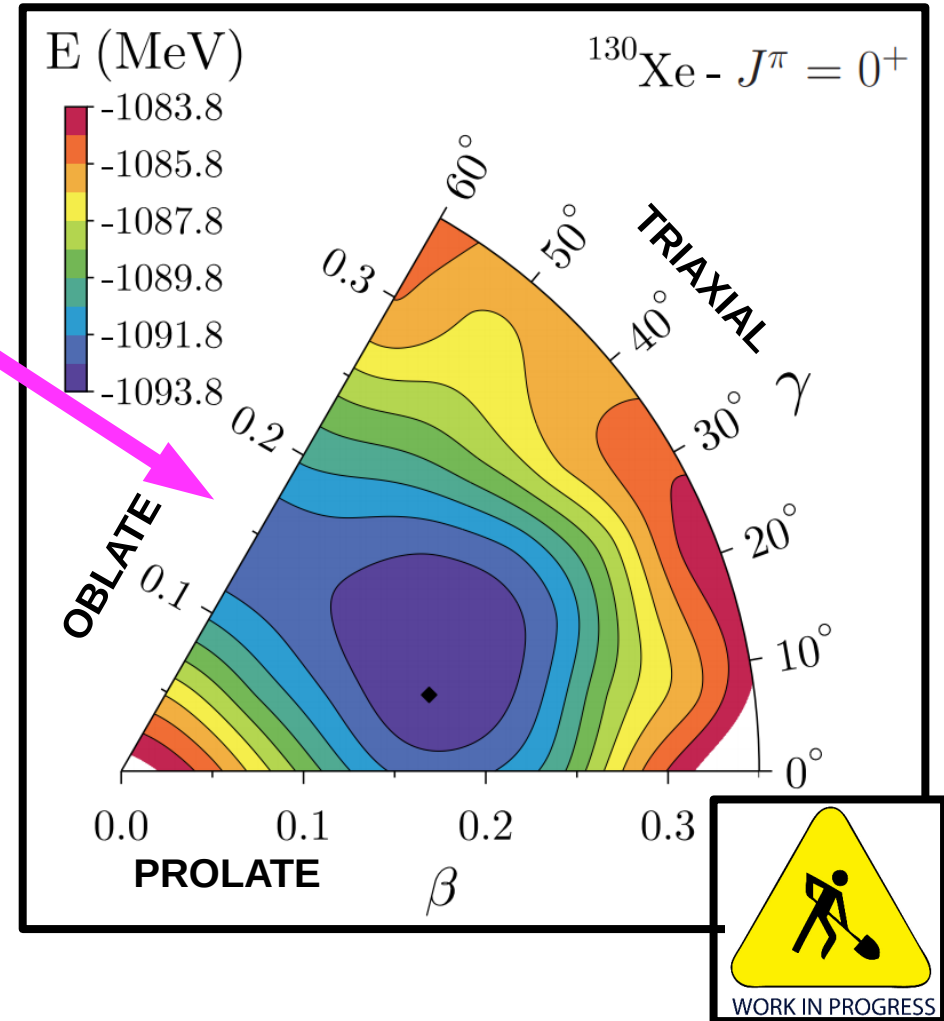
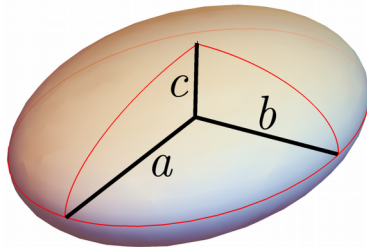
[potential energy for  $^{130}\text{Xe}$ ,  
courtesy Benjamin Bally]

**129Xe is not 238U.**

Shape is not sharply defined.

**Co-existence of prolate and oblate configurations.**

Average geometry is triaxial.



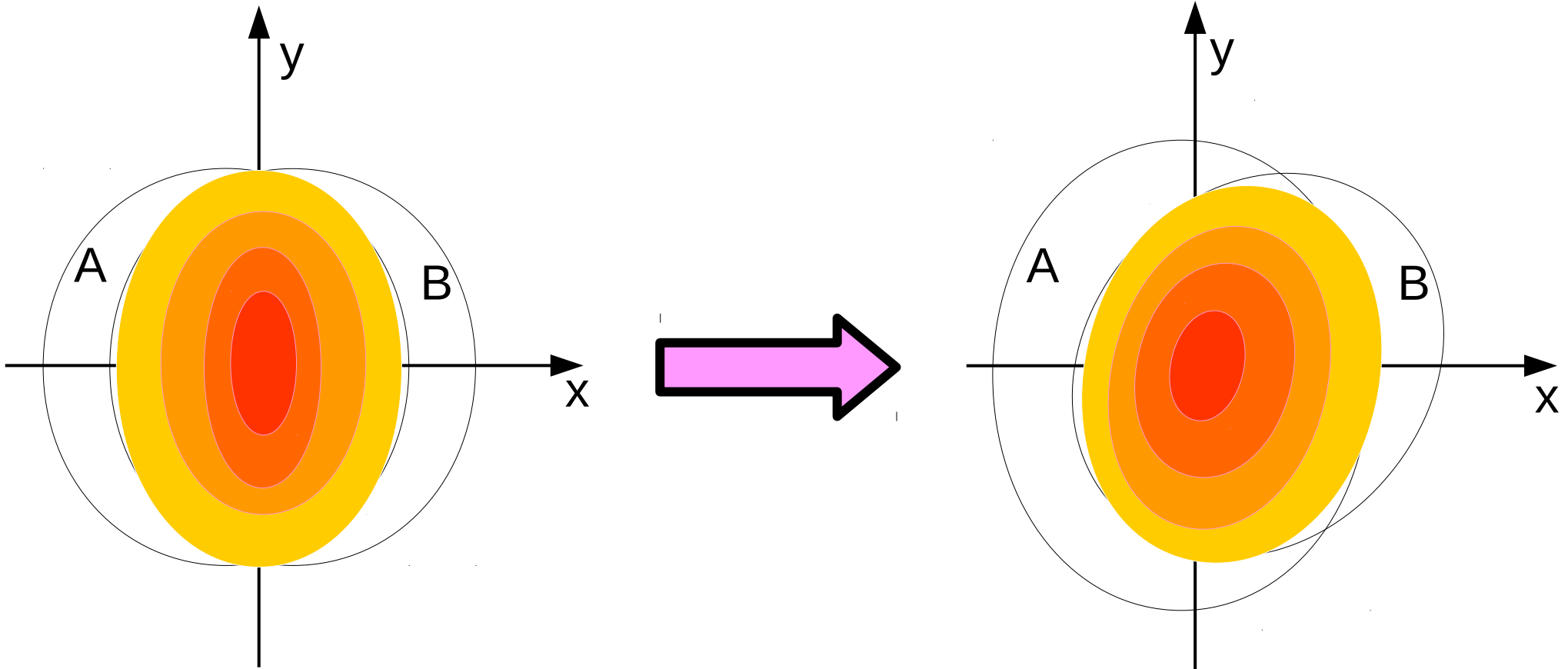
[Giacalone, [2101.00168](#)]

**Precision data on elliptic flow requires state-of-the-art nuclear theory.**



# NUCLEAR DEFORMATION

length scale  $\sim R_A$

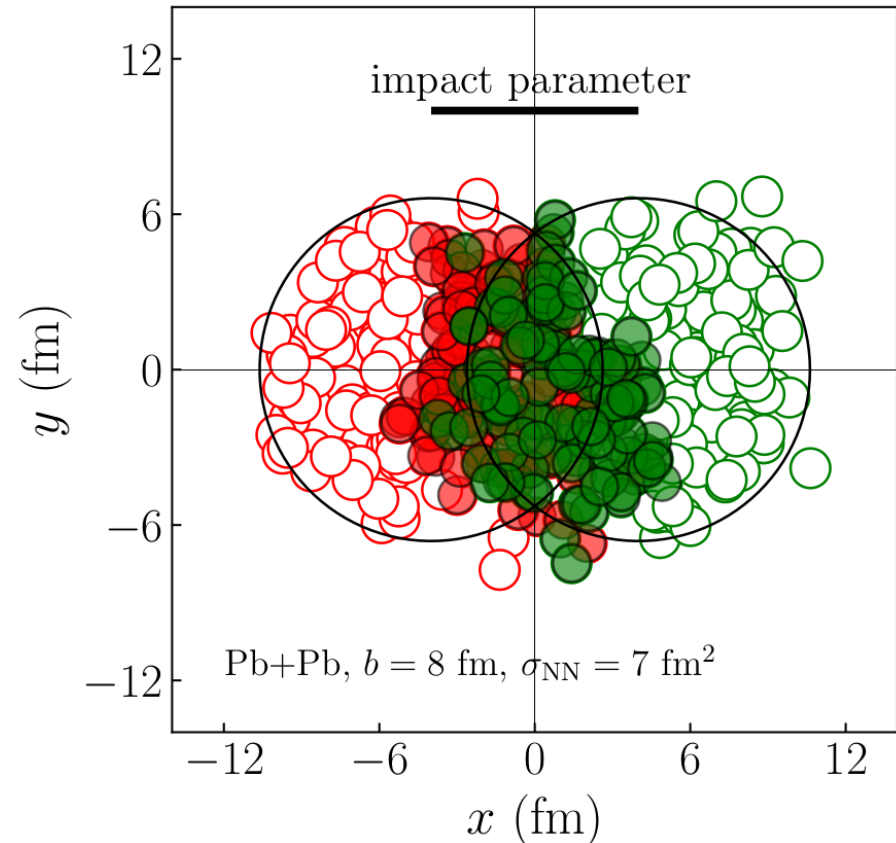


# ANISOTROPY #2 – nuclear structure: individual nucleons

Nuclear structure on shorter scales: Quantum noise due to nucleons.  
A mean-field approach: **Glauber Monte Carlo**.

[Miller, Reygers, Sanders, Steinberg  
[nucl-ex/0701025](#)]

$$\rho(r) = \frac{\rho_0}{1 + \exp\left(\frac{r-R}{a}\right)}$$

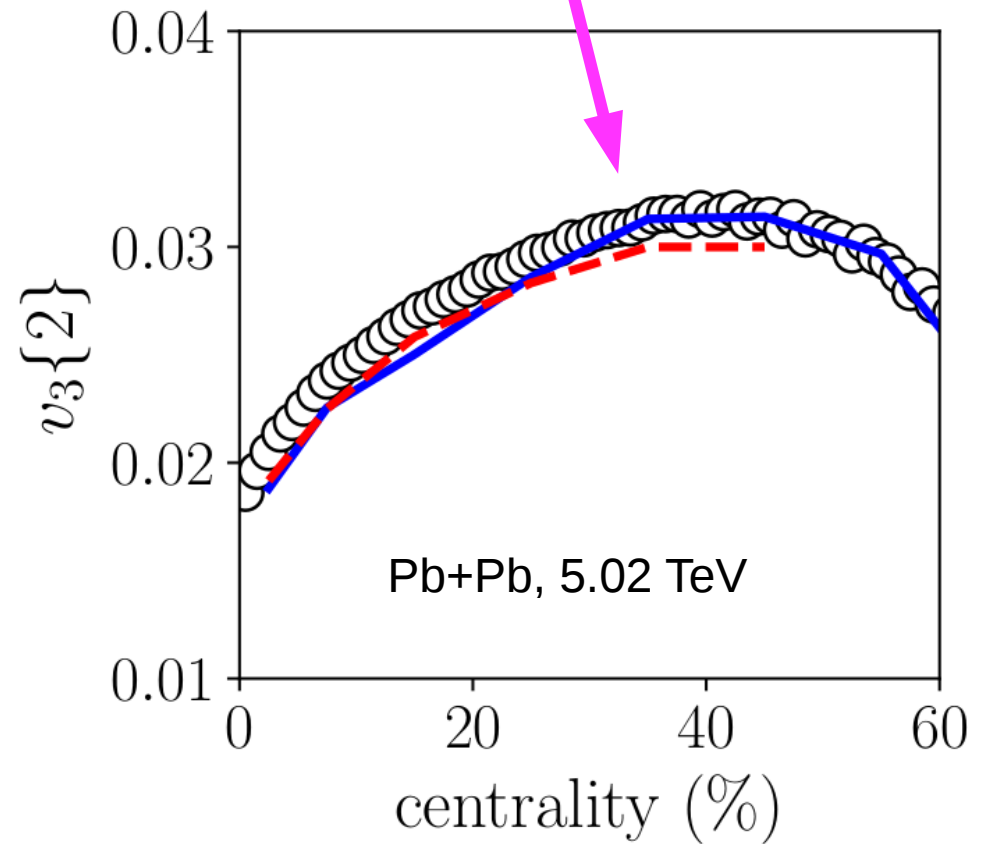
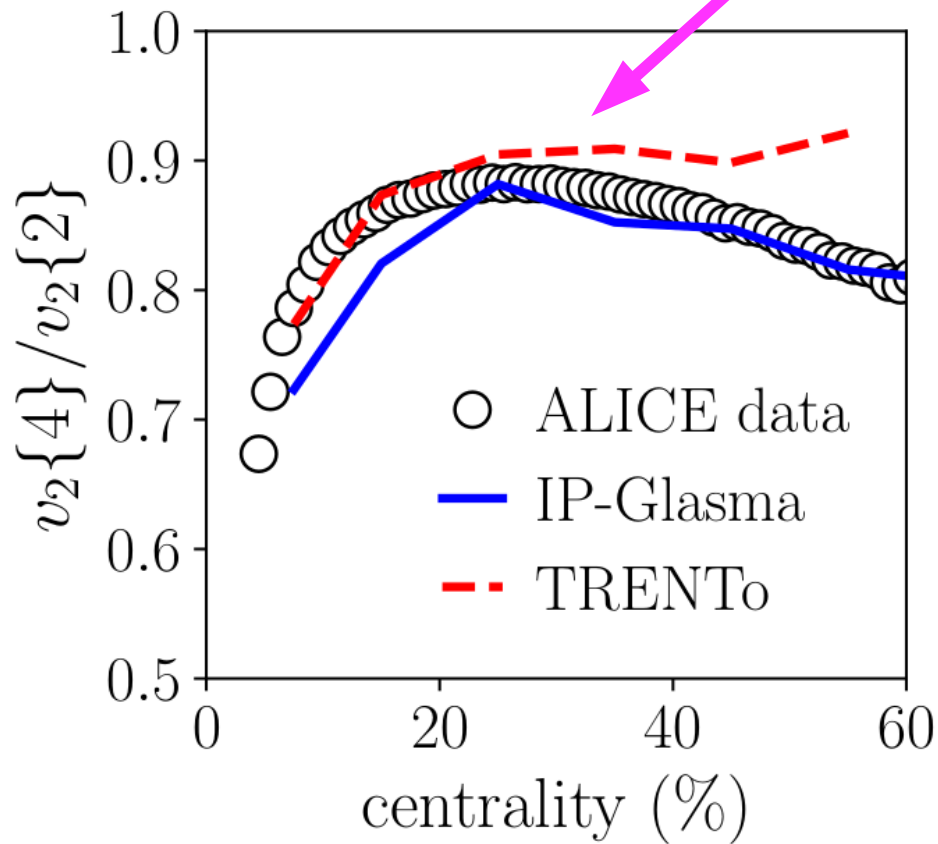


**Energy density obtained from nucleon-nucleon interactions.**

$$T_A(\mathbf{x})T_B(\mathbf{x}) \longrightarrow \sum_{i,j} T_{A,i}(\mathbf{x})T_{B,j}(\mathbf{x})$$

single nucleon

# Explains elliptic flow fluctuations and triangular flow.



- [ALICE Collaboration, [1804.02944](#)]
- IP-Glasma+MUSIC+urQMD [Schenke, Shen, Tribedy [2005.14682](#)]
- TRENTo+hydro [Bass, Bernhard, Moreland [Nature Phys. 15 \(2019\)](#)]

**But wait a minute...**

... those models “look” fairly different.

Picture of the QGP over the years. (b=0, initial energy density)

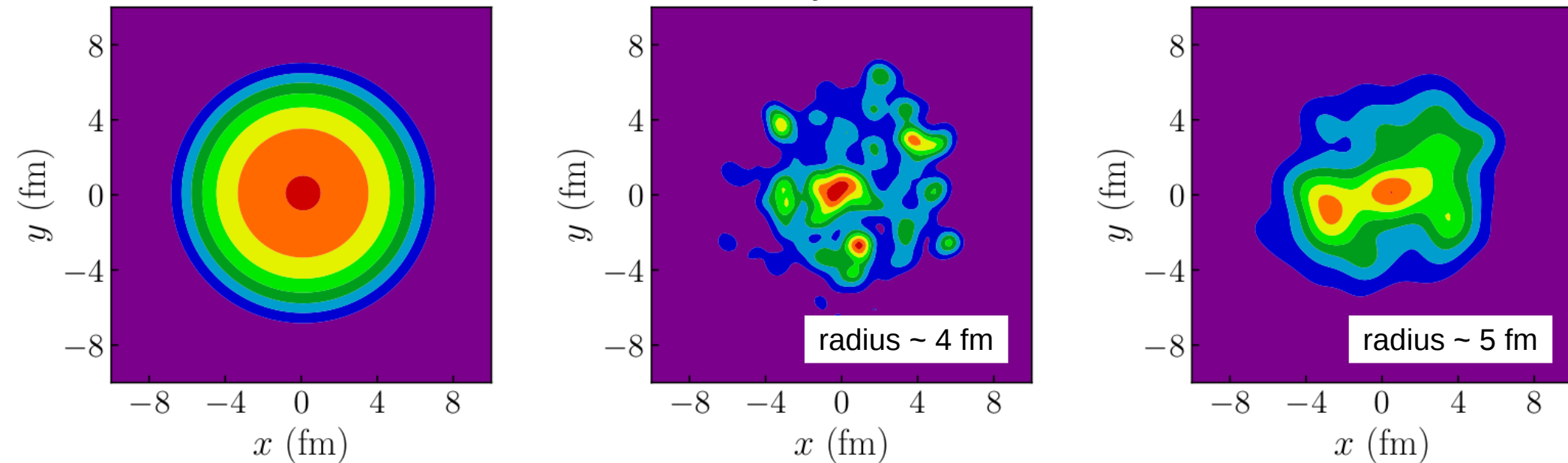
IP-Glasma-like, first TRENTo

latest TRENTo's

before 2005

2005 < year < 2019

after 2019



- QGP has been rather spiky until 2019-2020.

- Latest Bayesian analyses return smoother medium.

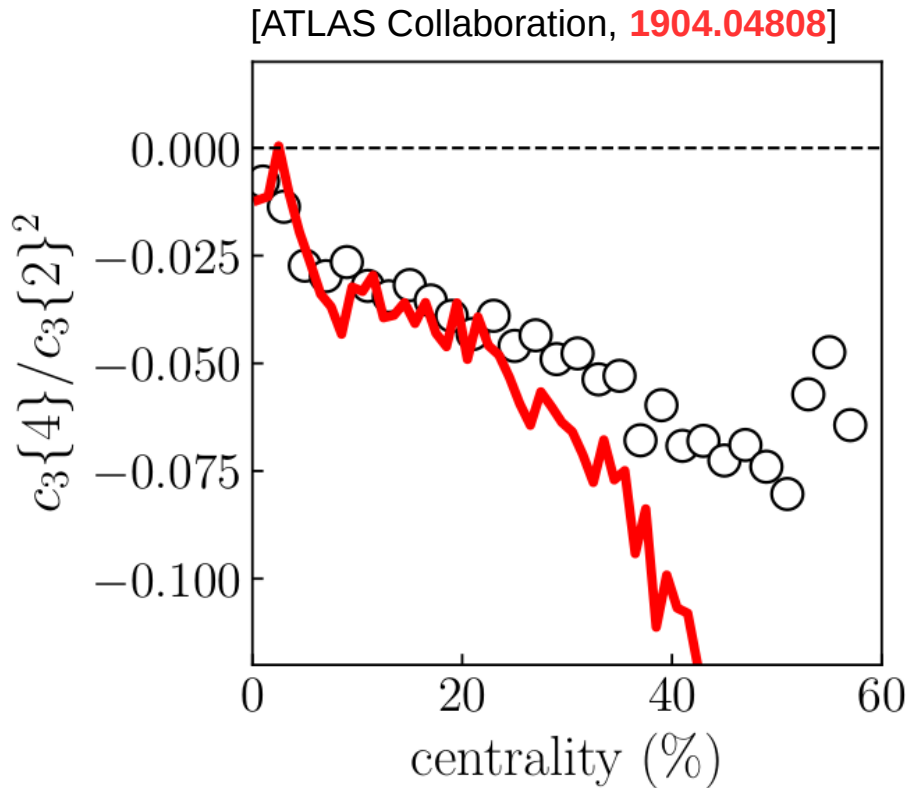
[Bass, Bernhard, Moreland [1808.02106](#), *Nature Phys.* **15** (2019)]

[JETSCAPE Collaboration [2011.01430](#), [2010.03928](#)] [Nijs, van der Schee, Gürsoy, Snellings [2010.15130](#), [2010.15134](#)]

- Anisotropies  $v_n\{2\}$  are roughly the same.

# Can anisotropy discern spiky and smooth profiles?

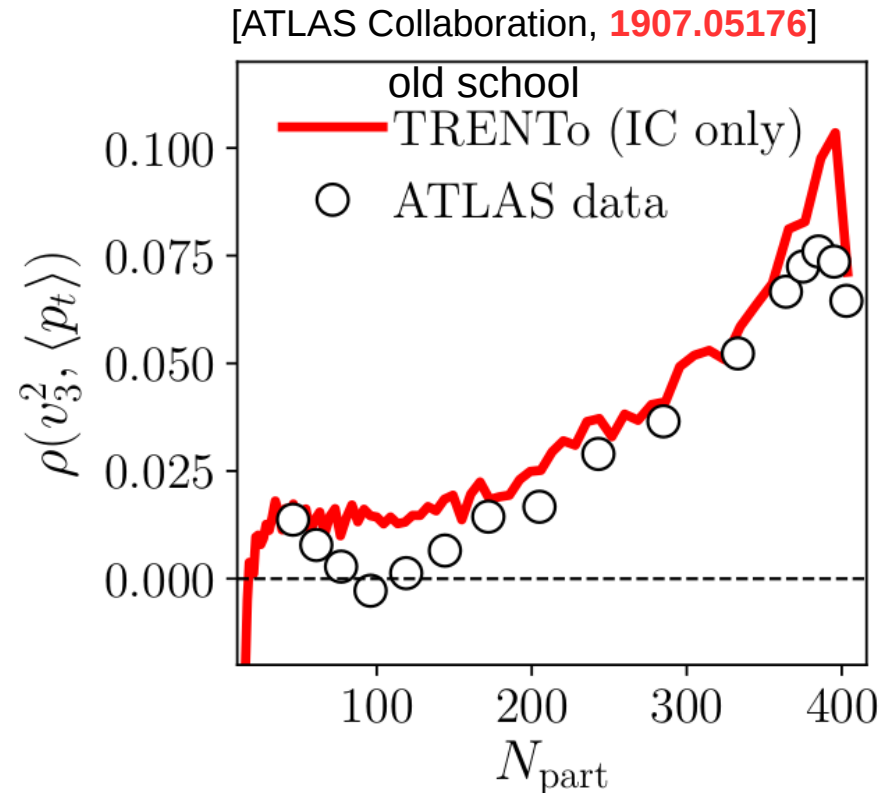
## Golden probes: do not involve the 1-point function! (i.e. v2)



**Primordial non-Gaussianity  
(is negative!)**

[Abbasi, Allahbakhshi,  
Davody, Taghavi 1704.06295]

[Bhalerao, Giacalone,  
Ollitrault, 1904.10350]



**Ultra-sensitive to fluctuations**

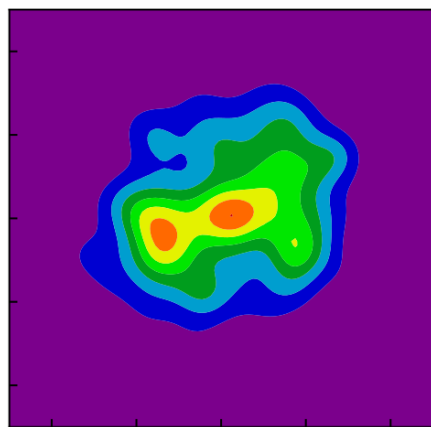
[Giacalone, Gardim,  
Noronha-Hostler, Ollitrault, 2004.01765]

[Giacalone, 2004.14463]

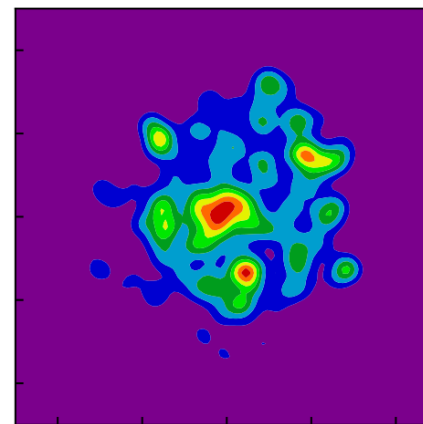
**Simple IP-Glasma-like TRENTo calculation captures the data.**

# QUESTION ADDRESSED BY THESE COMPARISONS:

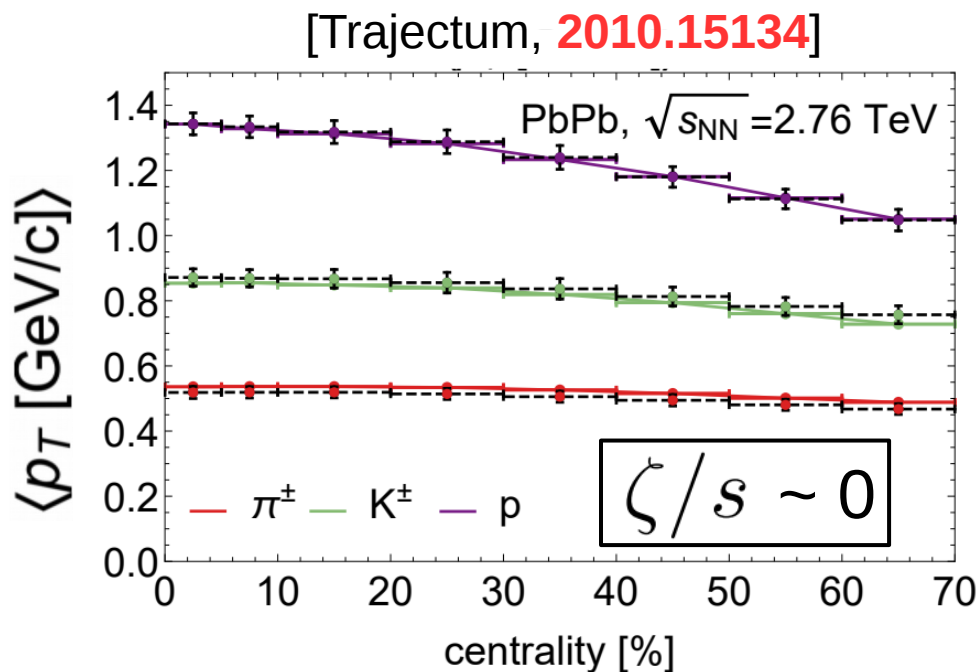
## 1 – Role of short-scale structures.



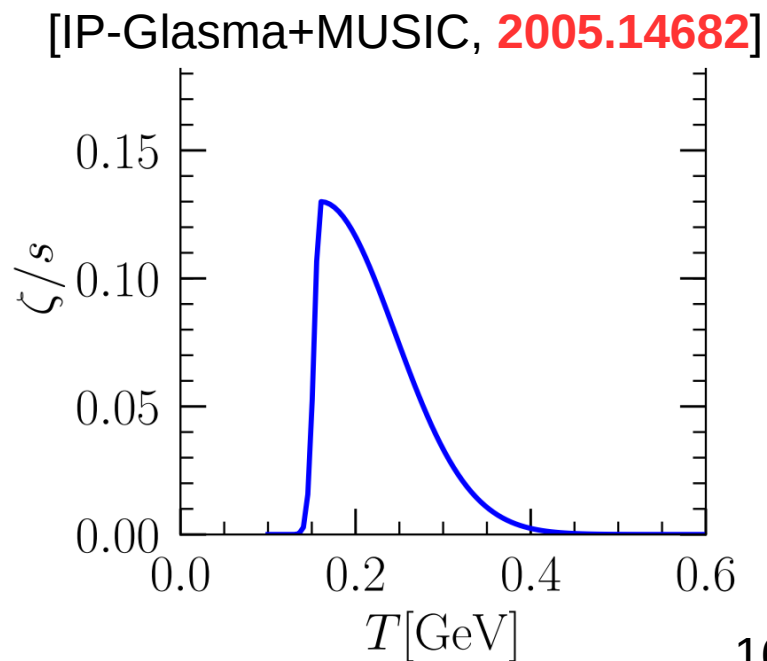
VS



## 2 – The fate of the bulk viscosity. Tension in the literature?



VS







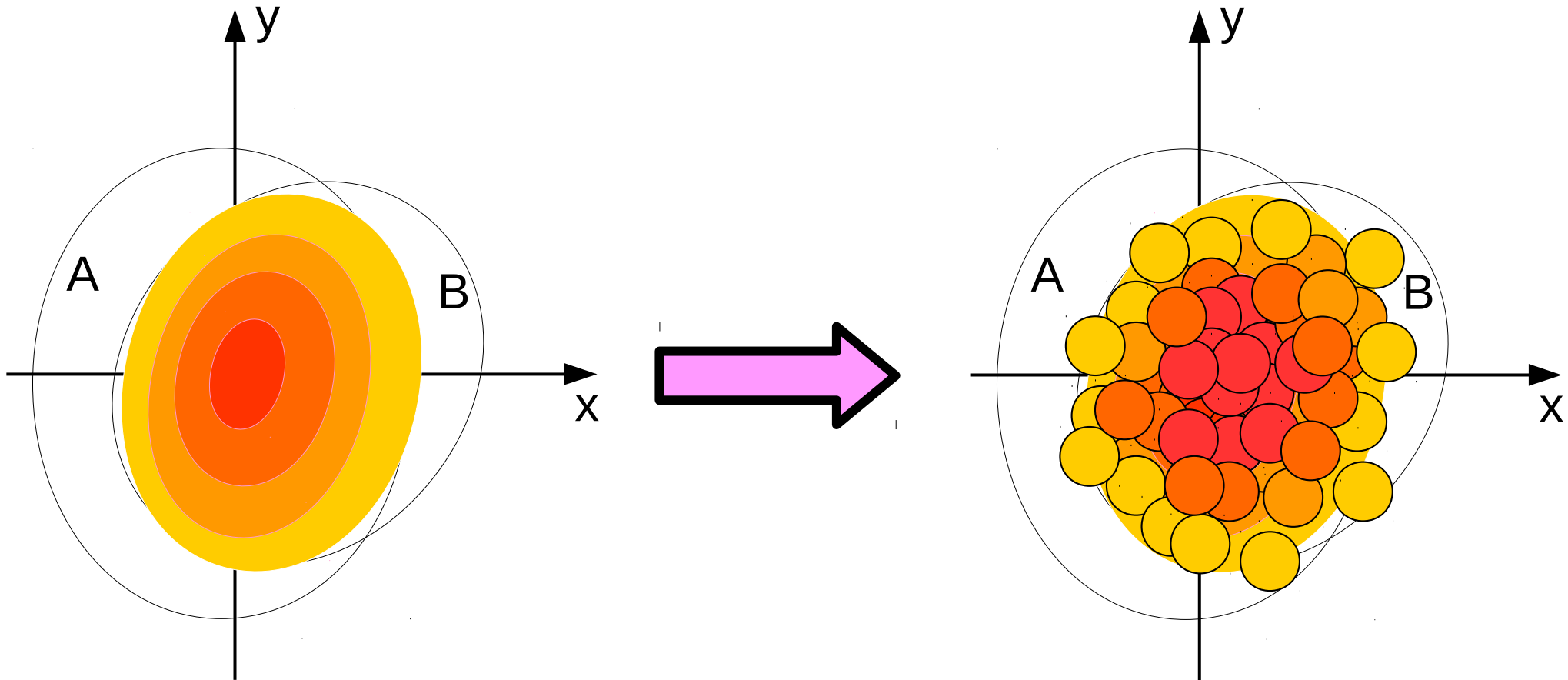
**NUCLEAR DEFORMATION**

length scale  $\sim R_A$



**INDIVIDUAL NUCLEONS**

length scale  $\sim [1 \text{ fm} , R_A ]$



# ANISOTROPY #3 – nucleon structure

[ talk by A. Soto-Ontoso,  
Friday Jan 15<sup>th</sup>, #233]

**Anisotropy observed in pA (and pp).**

The crucial question: **can we use the same 1-point function?**

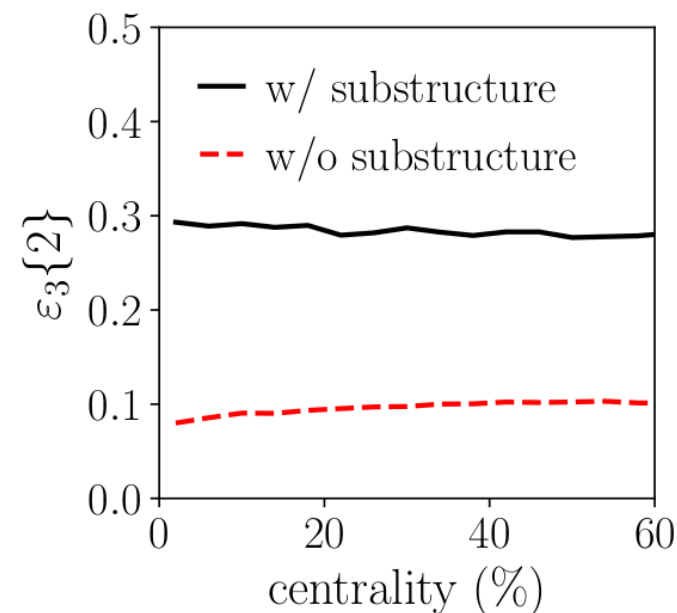
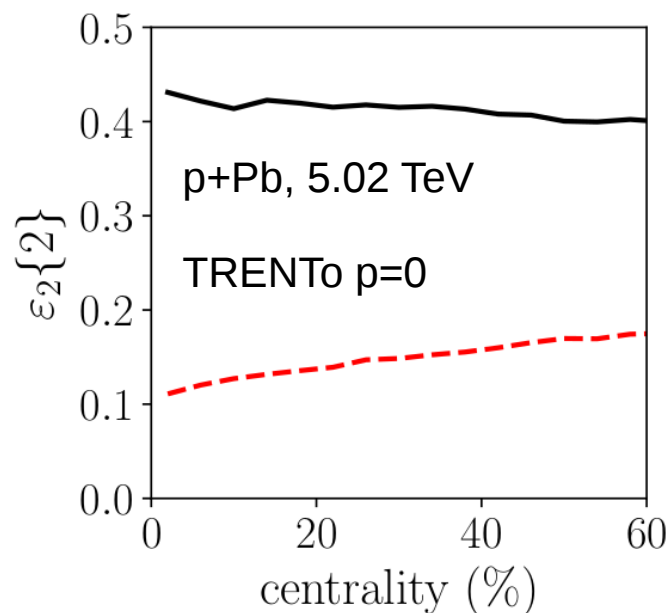
$$\langle T^{00}(\mathbf{x}, \tau = 0^+) \rangle \propto \left( T_A(\mathbf{x}) T_B(\mathbf{x}) \right)^q$$

Yes, but you'll need more structures. [Schenke, Venugopalan [1405.3605](#)]

**IP-Glasma:** Shape fluctuations in protons. [Mäntysaari, Schenke [1603.04349](#), [1607.01711](#)]  
[Mäntysaari, Schenke, Shen, Tribedy [1705.03177](#)]

**TRENTo:** Combined analysis of p-Pb and Pb-Pb collisions

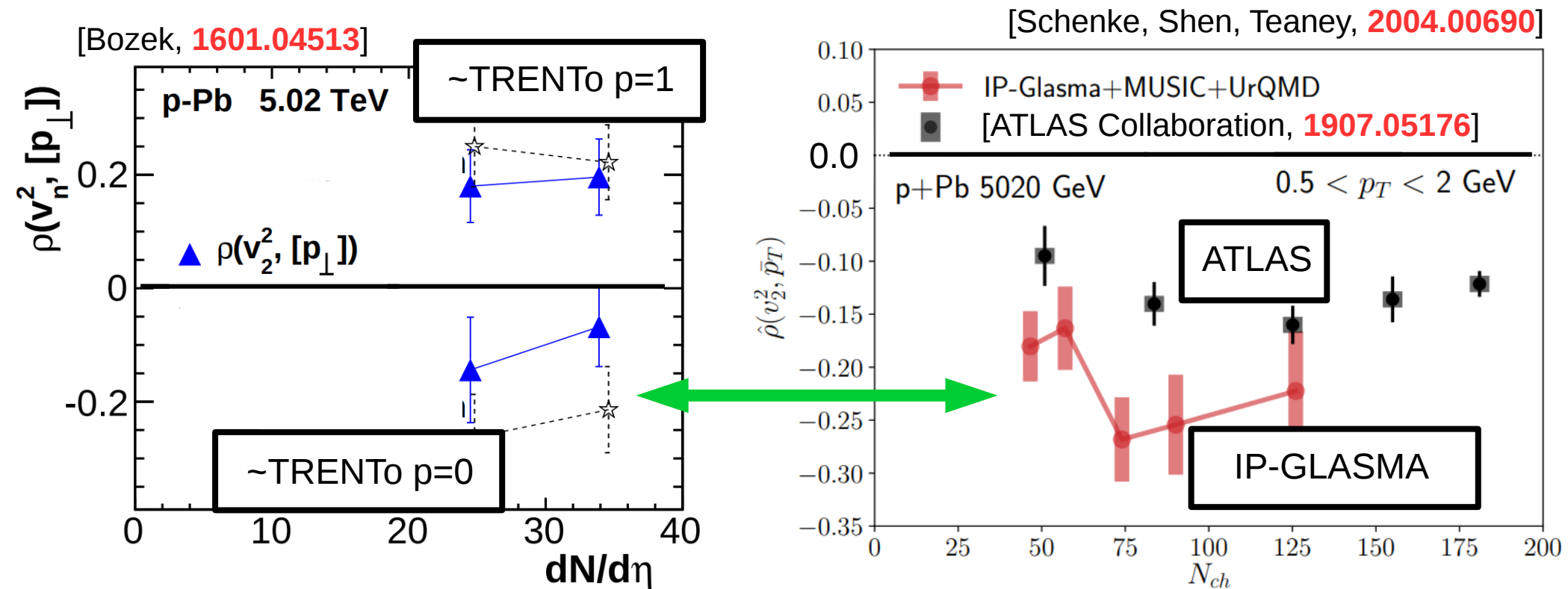
[Bass, Bernhard, Moreland [1808.02106](#)]  
[Nijs, van der Schee, Gürsoy, Snellings [2010.15130](#), [2010.15134](#)]



Is there experimental evidence of this behavior in small systems?

$$\langle T^{00}(\mathbf{x}, \tau = 0^+) \rangle \propto \left( T_A(\mathbf{x}) T_B(\mathbf{x}) \right)^q$$

**Nontrivial information from  $v_n$ - $\langle p_T \rangle$  correlation.**

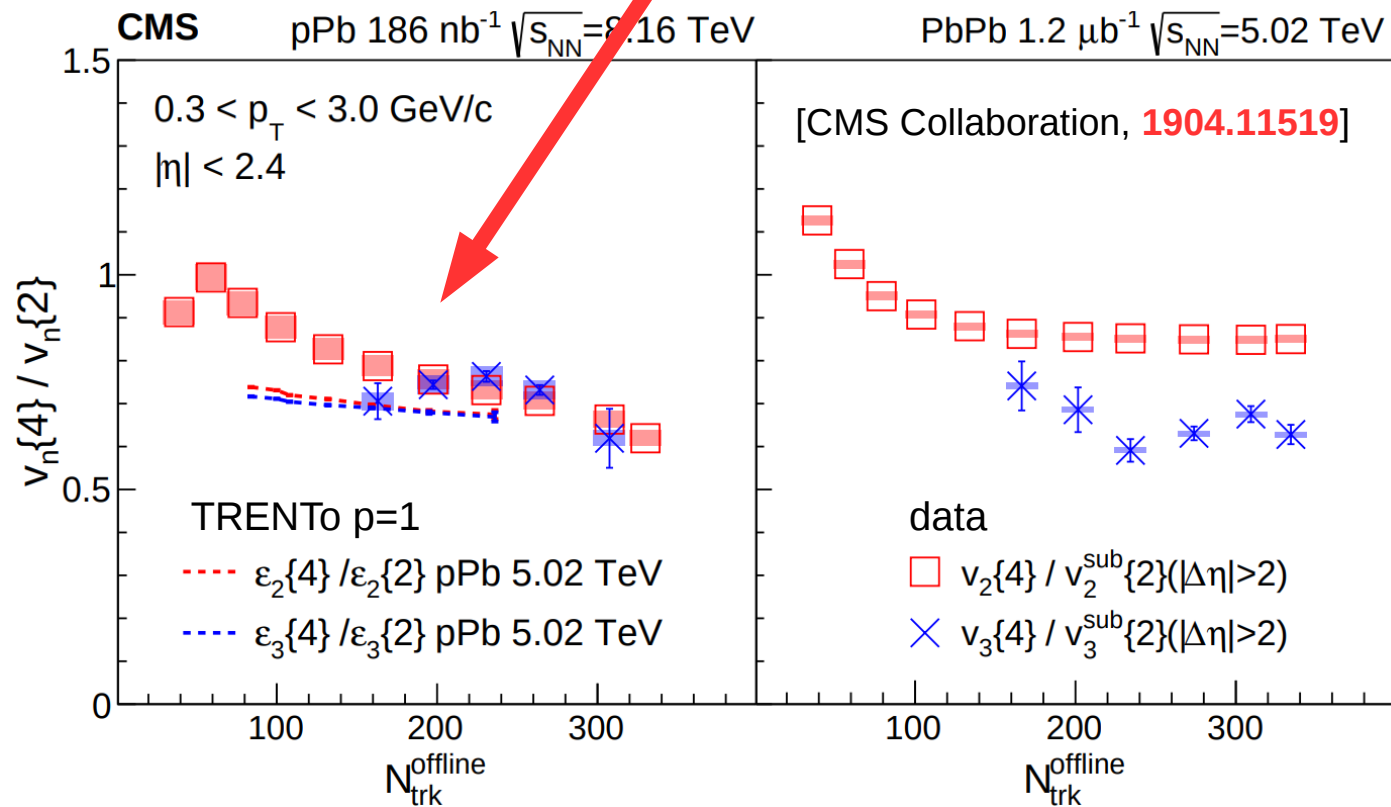


- Experimental ATLAS data is **negative** in high-multiplicity pA.
- Supports IP-Glasma or TRENTo p=0-like scaling.

# DO WE HAVE THE RIGHT MODEL: OPEN QUESTIONS #1

Beautiful observation by CMS in p-Pb collisions:

$$v_2\{4\}/v_2\{2\} = v_3\{4\}/v_3\{2\}$$

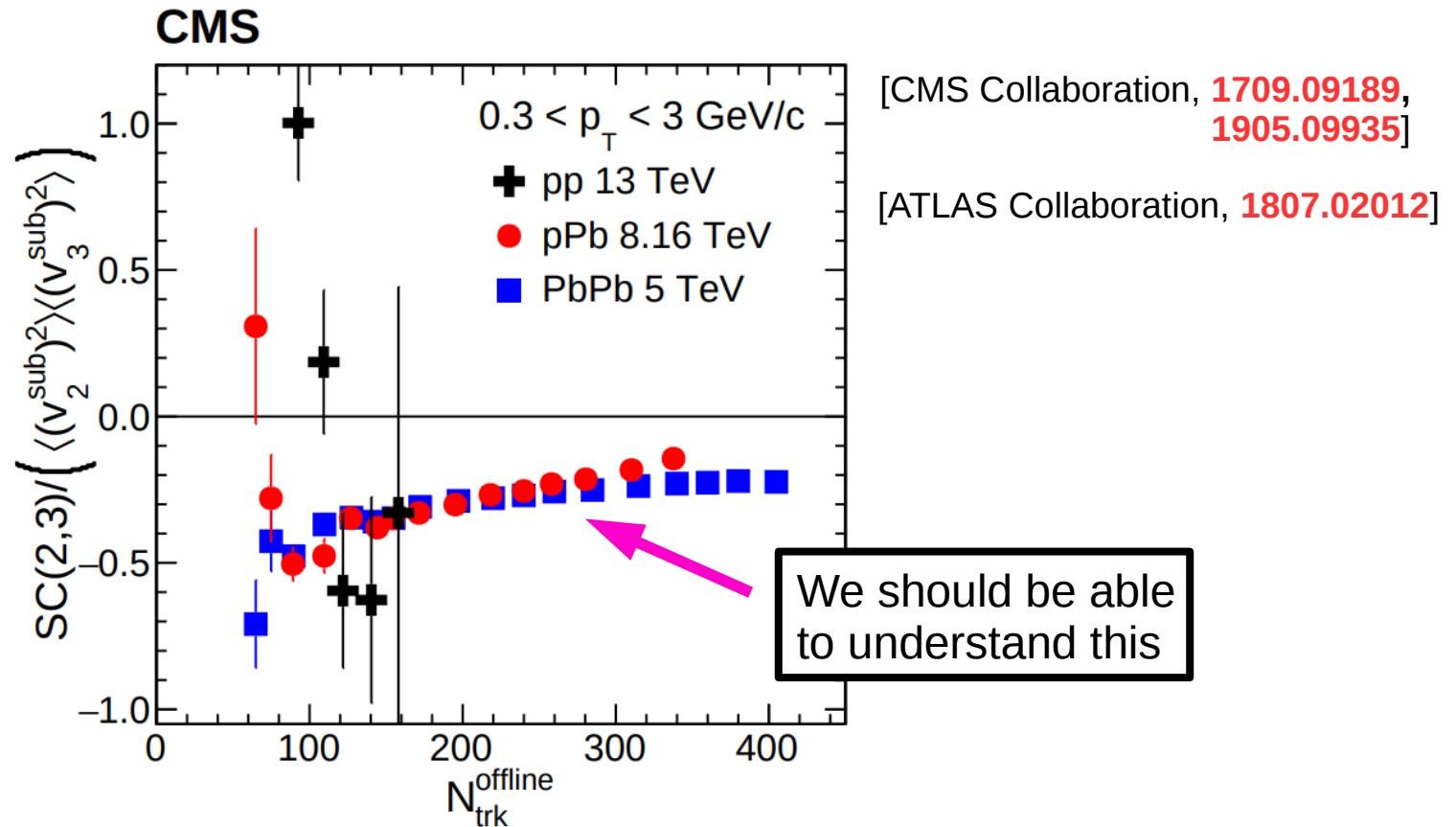


– Calculation with TRENTo p=1 (wounded nucleons) points to geometric origin of observables. [Giacalone, Noronha-Hostler, Ollitrault, [1702.01730](#)]

– **TRENTo p=1 is ruled out... results from sub-structure models?**

# DO WE HAVE THE RIGHT MODEL: OPEN QUESTIONS #2

Mixed correlations measured with great accuracy.



There are no results from recent sub-structure models.

**I tried with the eccentricities and get the wrong sign. [NSC(3,2)>0]**

[also observed in p-p: Zhao, Zhou, Murase, Song 2001.06742]

Results for p-p (or  $N_{\text{trk}} \sim 100$ ) sensitive to details of hot-spot deposition.

[Albacete, Elfner, Soto-Ontoso 1707.05592]



**NUCLEAR DEFORMATION**

length scale  $\sim R_A$



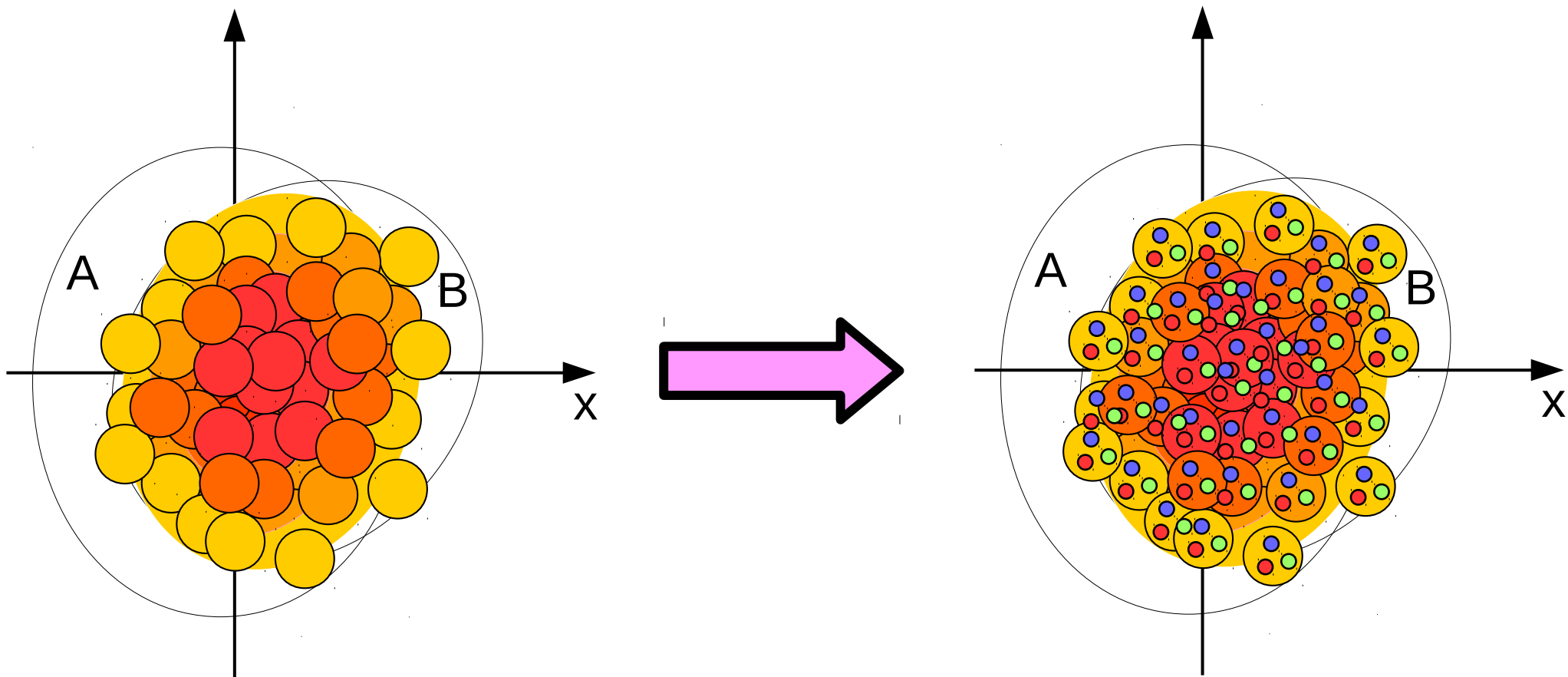
**INDIVIDUAL NUCLEONS**

length scale  $\sim [1 \text{ fm} , R_A ]$



**SUB-NUCLEONIC STRUCTURES**

length scale  $\sim [1/Q_s , 1 \text{ fm} ]$

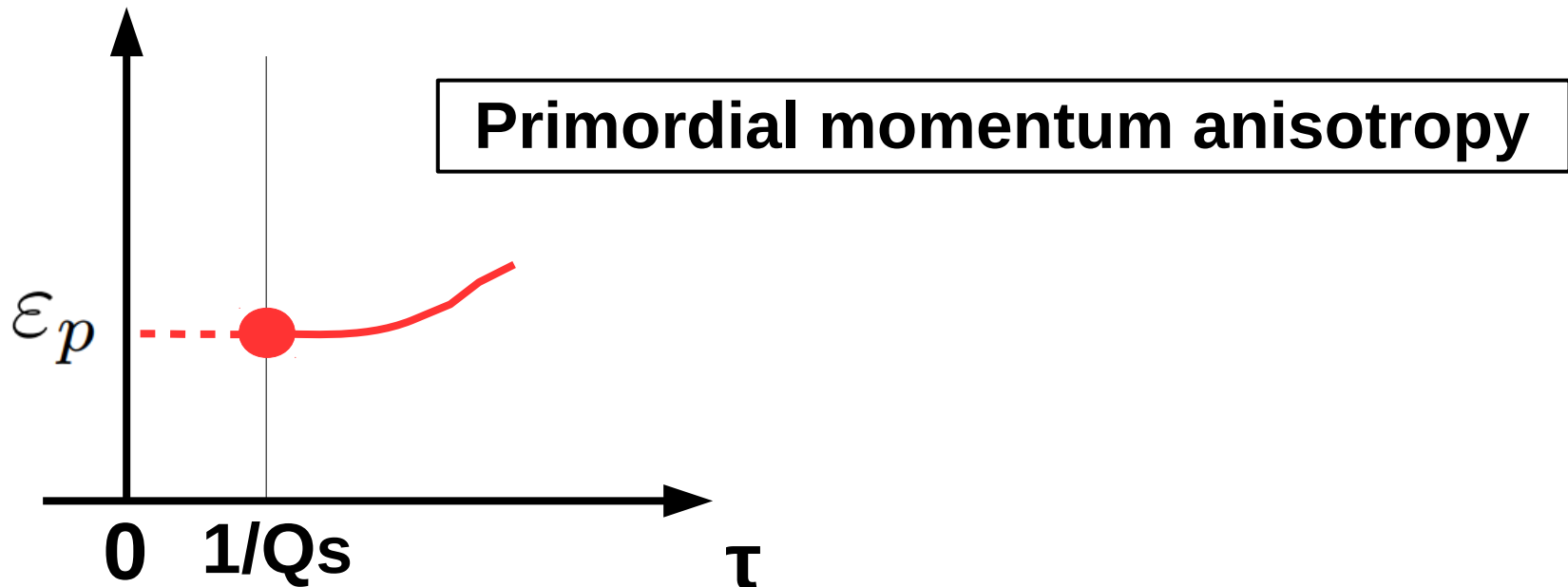


# ANISOTROPY #4 – momentum space deformation

Vast literature describing long-range anisotropy in pp, pA collisions from initial-state effects in the CGC. [Altinoluk, Armesto 2004.08185]

Address the question with IP-Glasma initial conditions.  
**Ellipticity of the tensor modes:**

$$\boxed{\mathcal{E}_p} \equiv \varepsilon_p e^{i2\Psi_2^p} \equiv \frac{\langle T^{xx} - T^{yy} \rangle + i\langle 2T^{xy} \rangle}{\langle T^{xx} + T^{yy} \rangle}$$

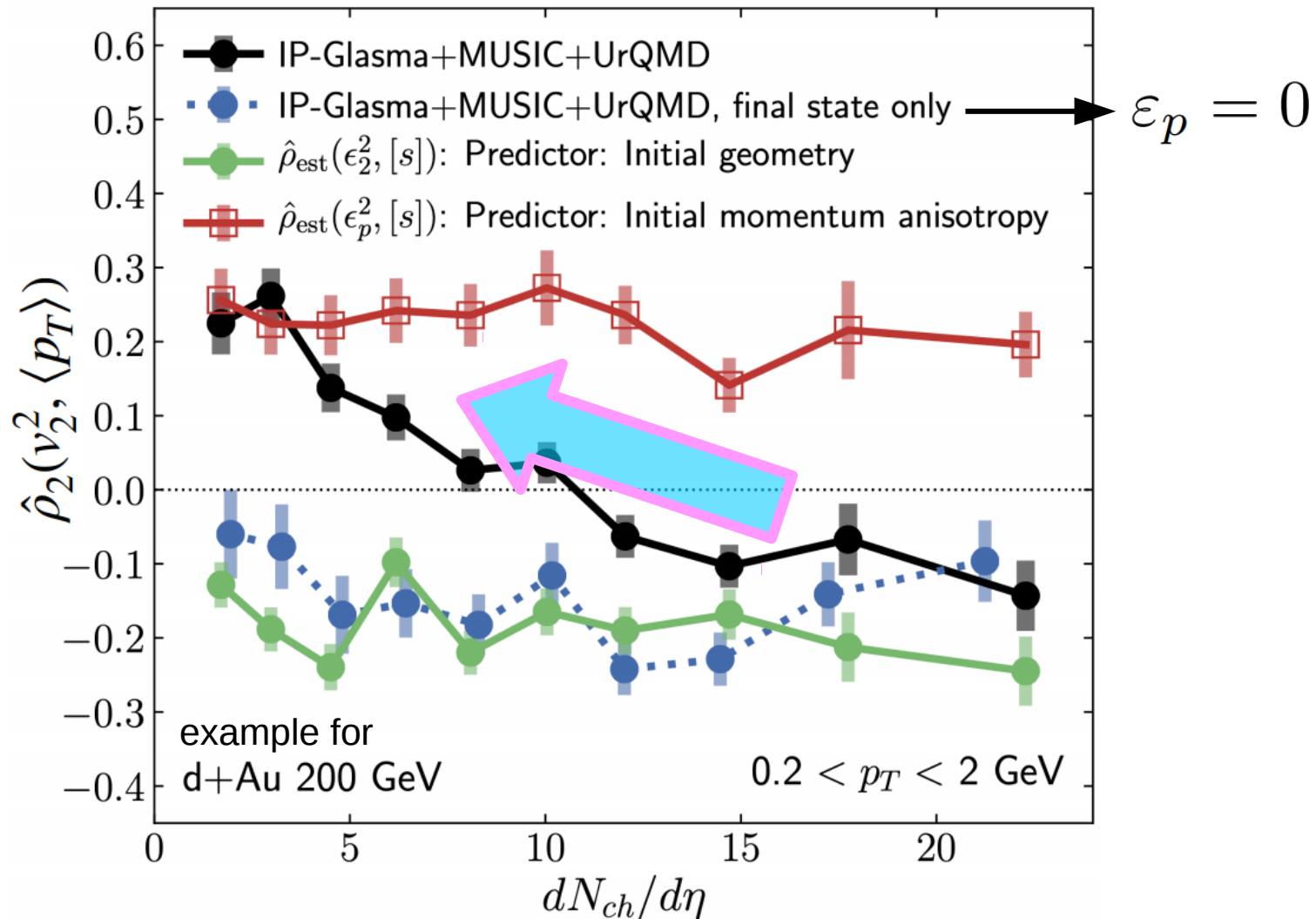


For small multiplicities,  $\epsilon_p$  is the dominant source of elliptic flow.

[Schenke, Shen, Tribedy, 1908.06212]

## OUR FINDING: QUALITATIVE SIGNATURES IN SMALL SYSTEMS

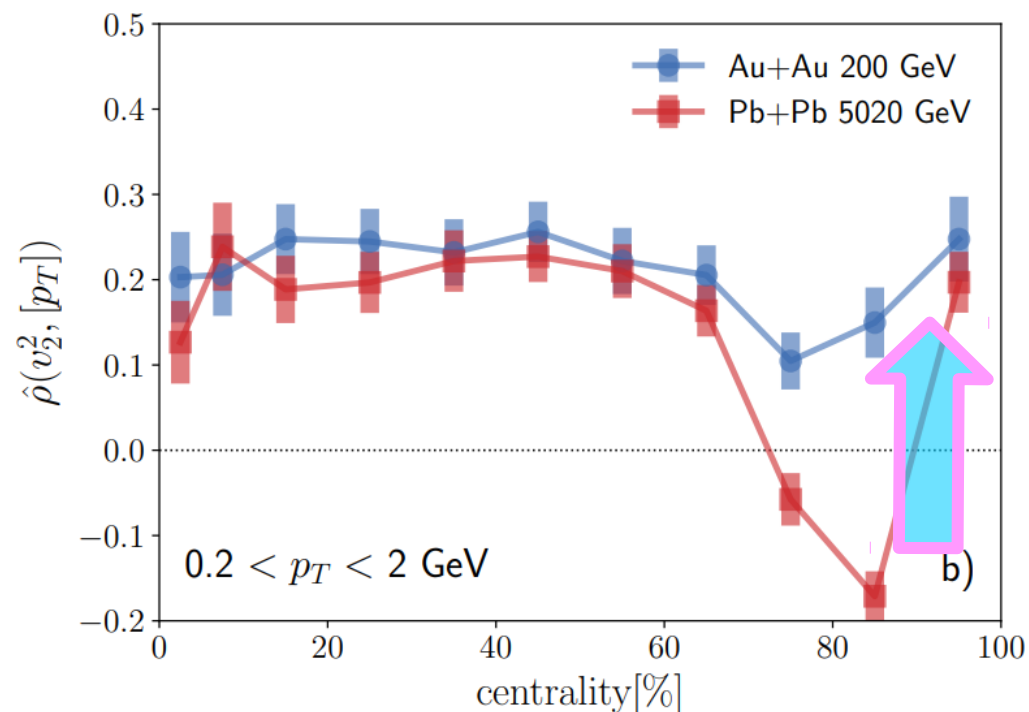
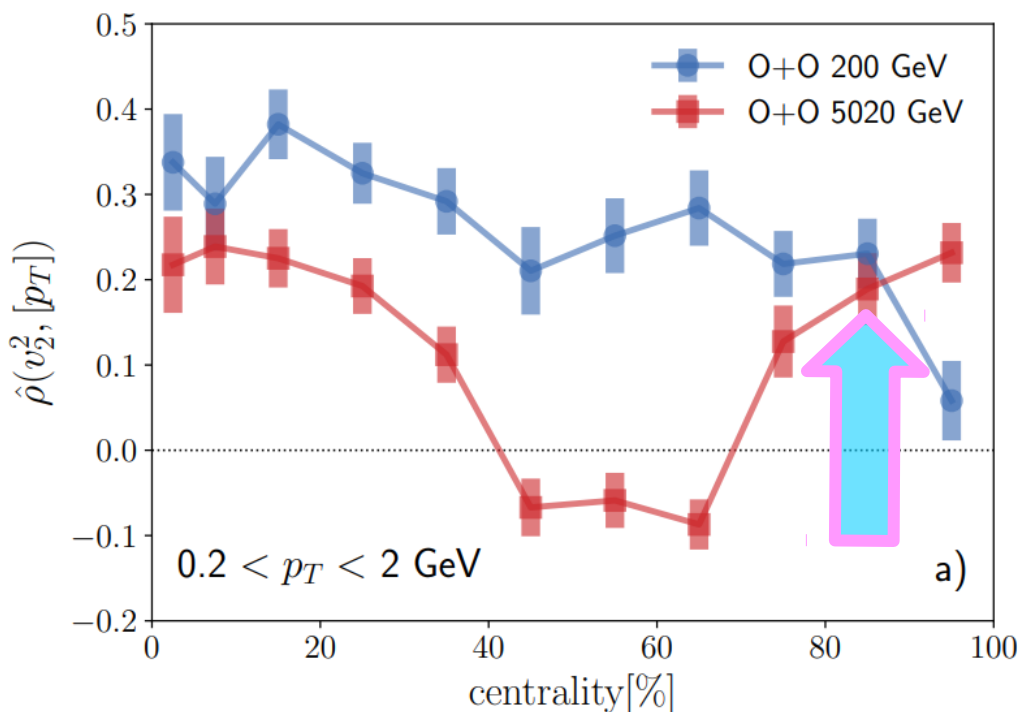
[Giacalone, Schenke, Shen, 2006.15721]



Correlator goes from negative to positive as we decrease  $dN/d\eta$ .



# QUALITATIVE SIGNATURES IN PERIPHERAL A-A

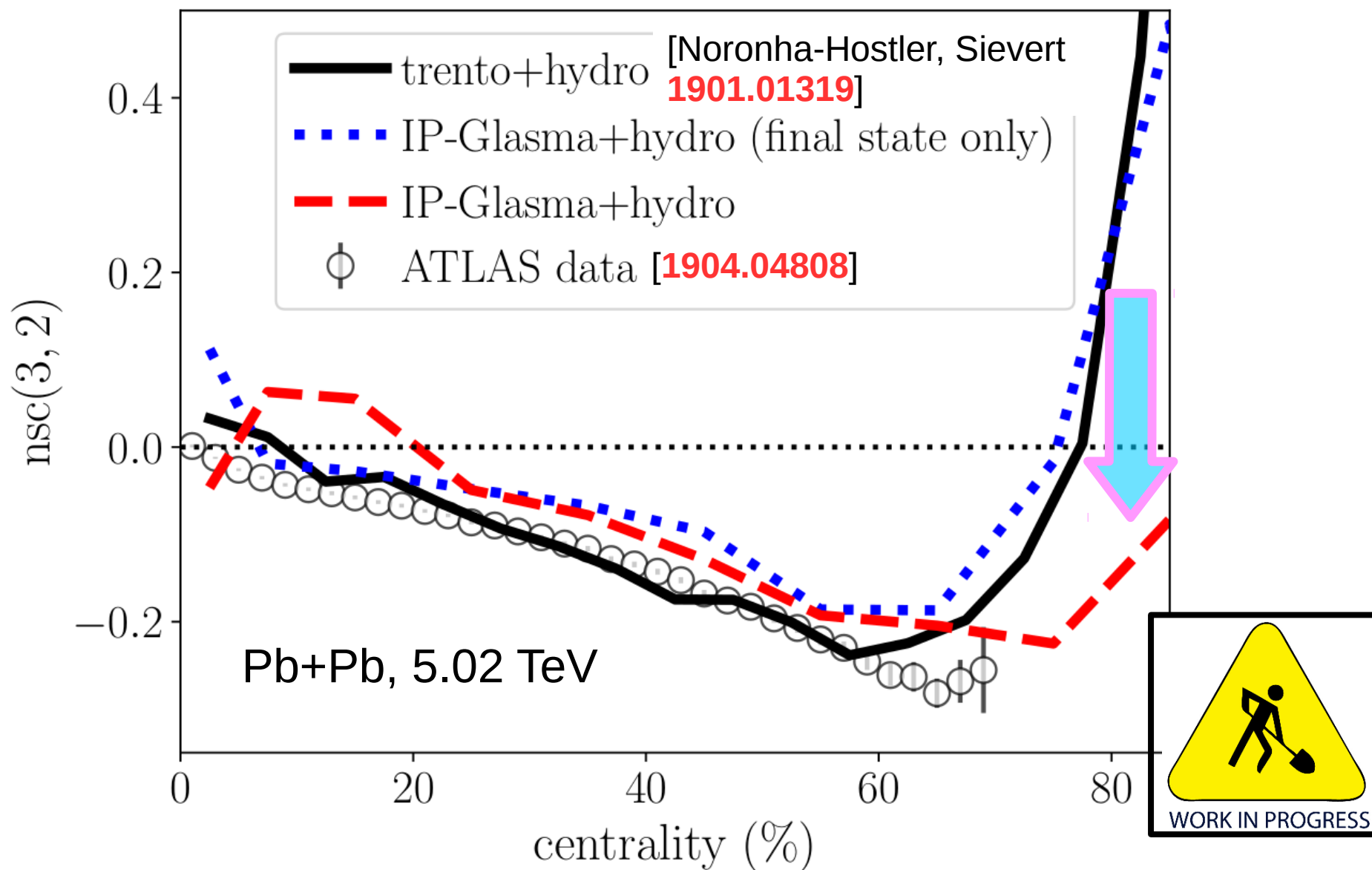


- Double sign change @ LHC

- No sign change @ RHIC

[consistent with preliminary STAR data]

Normalized symmetric cumulant shows similar signatures.



With initial momentum anisotropy the cumulant stays negative!



**NUCLEAR DEFORMATION**

length scale  $\sim R_A$



**INDIVIDUAL NUCLEONS**

length scale  $\sim [1 \text{ fm} , R_A]$

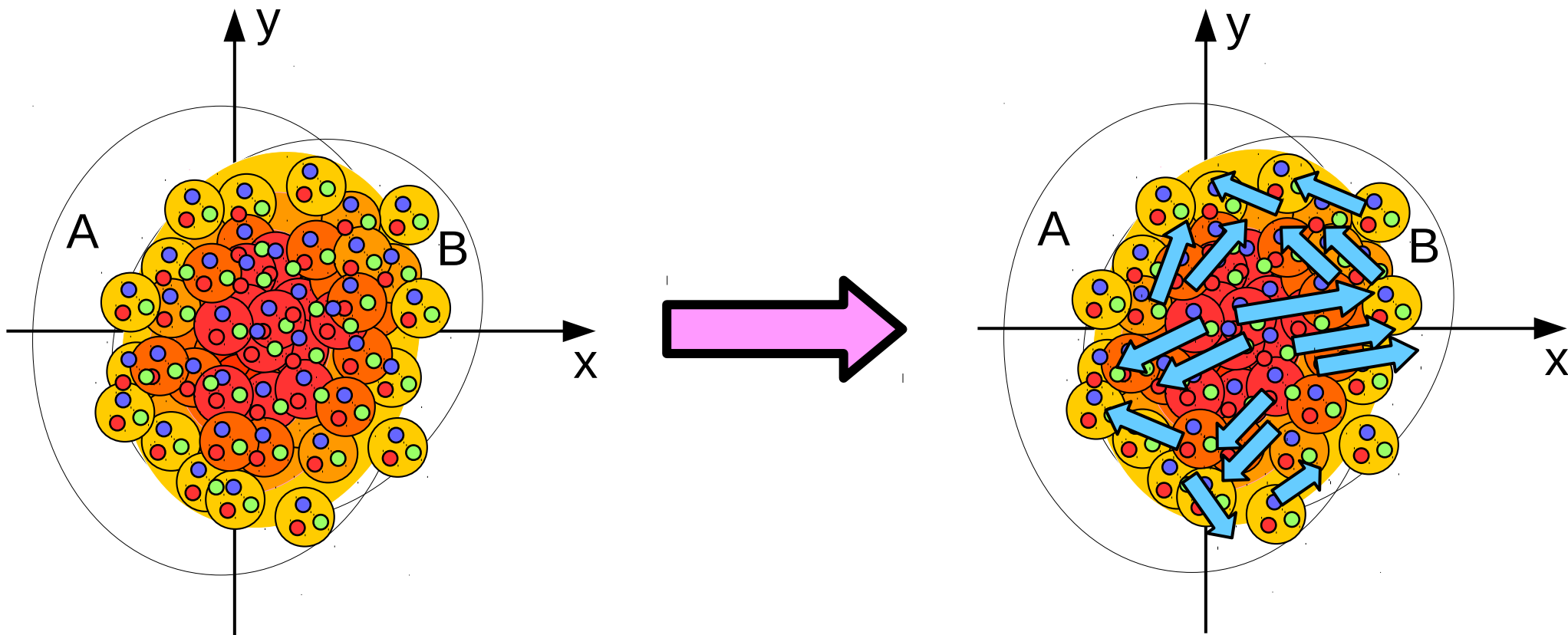


**SUB-NUCLEONIC STRUCTURES**

length scale  $\sim [1/Q_s , 1 \text{ fm}]$



**MOMENTUM SPACE ANISOTROPY**



# ALL TOGETHER: "HEAVY-ION COLLISIONS 2.0"

