

One fluid may not rule them all

- Collectivity in Pb-Pb, p-Pb and p-p collisions

Huichao Song

宋慧超

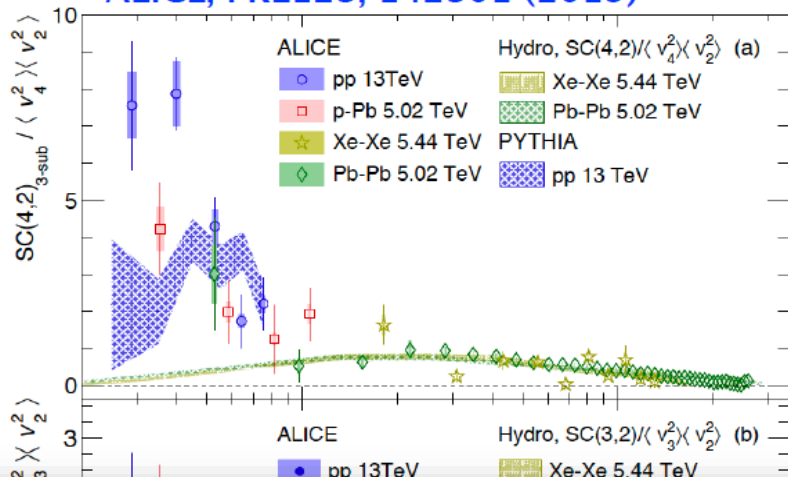
Peking University

Initial Stages2021, Jan. 10-16, 2021

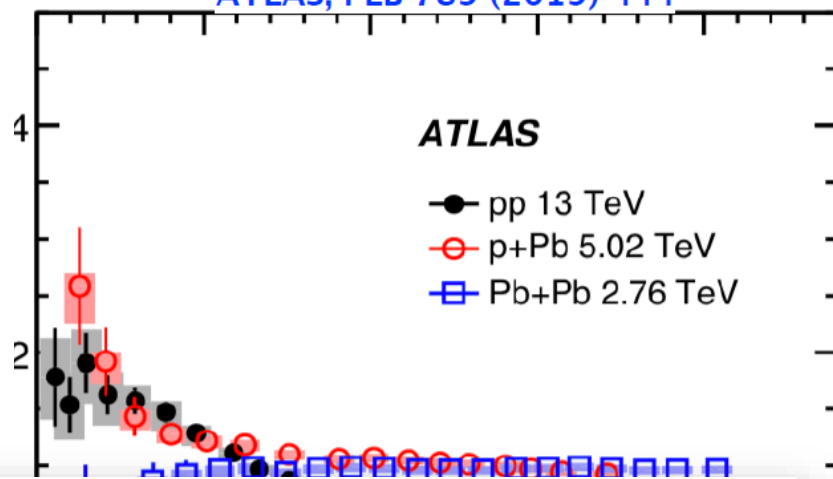
Jan 12, 2021

Various flow observables in large and small systems

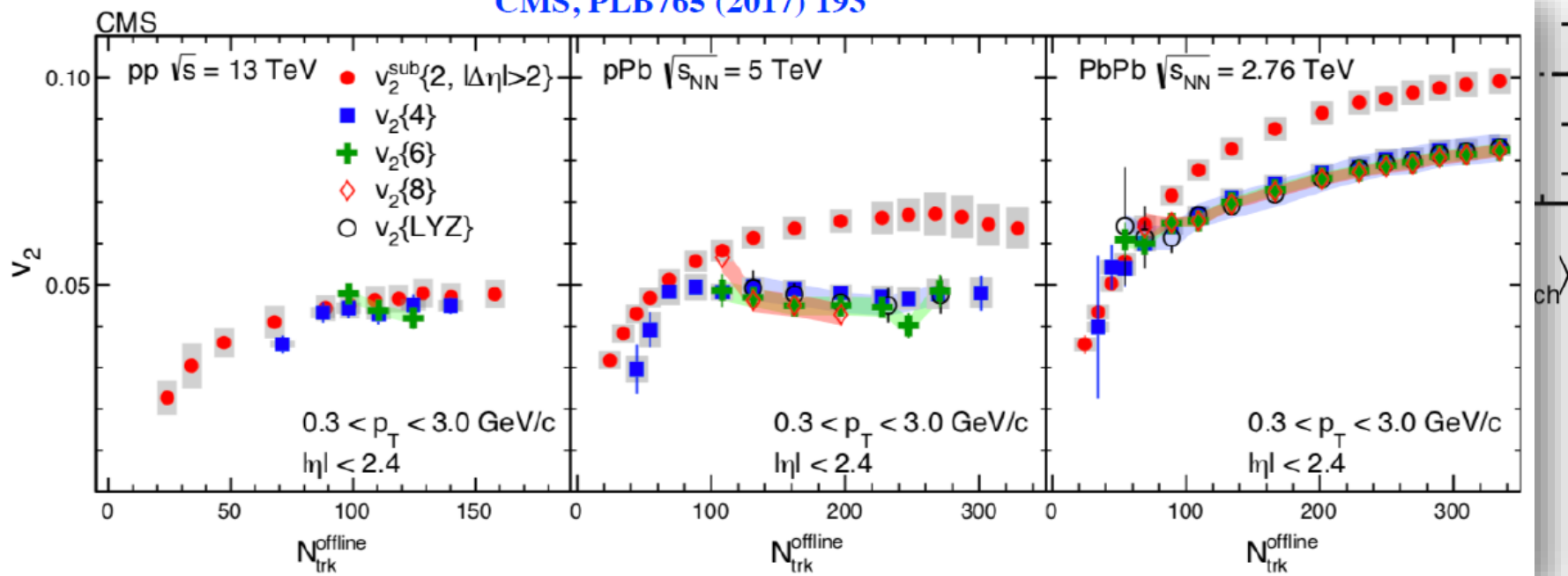
ALICE, PRL123, 142301 (2019)



ATLAS, PLB 789 (2019) 444



CMS, PLB765 (2017) 193



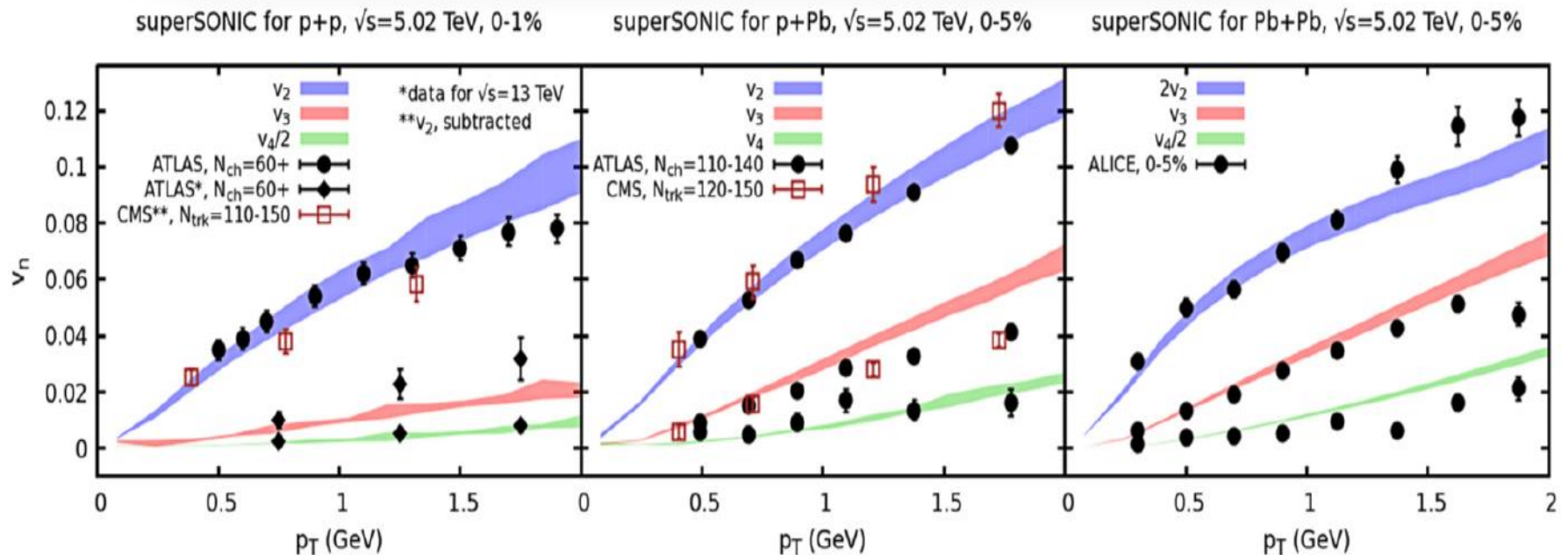
Observable or effect	Pb–Pb	p–Pb (high mult.)	pp (high mult.)
Low p_T spectra (“radial flow”)	yes	yes	yes
Intermediate p_T (“recombination”)	yes	yes	yes
Particle ratios	GC level	GC level except Ω	GC level except Ω
Statistical model	$\gamma_s^{\text{GC}} = 1, 10\text{--}30\%$	$\gamma_s^{\text{GC}} \approx 1, 20\text{--}40\%$	MB: $\gamma_s^{\text{C}} < 1, 20\text{--}40\%$
HBT radii ($R(k_T), R(\sqrt[3]{N_{\text{ch}}})$)	$R_{\text{out}}/R_{\text{side}} \approx 1$	$R_{\text{out}}/R_{\text{side}} \lesssim 1$	$R_{\text{out}}/R_{\text{side}} \lesssim 1$
Azimuthal anisotropy (v_n) (from two particle correlations)	$v_1\text{--}v_7$	$v_1\text{--}v_5$	$v_2\text{--}v_4$
Characteristic mass dependence	$v_2\text{--}v_5$	v_2, v_3	v_2
Directed flow (from spectators)	yes	no	no
Charge-dependent correlations	yes	yes	yes
Higher-order cumulants (mainly $v_2\{n\}, n \geq 4$)	“4 \approx 6 \approx 8 \approx LYZ” +higher harmonics	“4 \approx 6 \approx 8 \approx LYZ” +higher harmonics	“4 \approx 6”
Symmetric cumulants	up to SC(5, 3)	only SC(4, 2), SC(3, 2)	only SC(4, 2), SC(3, 2)
Non-linear flow modes	up to v_6	not measured	not measured
Weak η dependence	yes	yes	not measured
Factorization breaking	yes ($n = 2, 3$)	yes ($n = 2, 3$)	not measured
Event-by-event v_n distributions	$n = 2\text{--}4$	not measured	not measured
Direct photons at low p_T	yes	not measured	not observed
Jet quenching through dijet asymmetry	yes	not observed	not observed
Jet quenching through R_{AA}	yes	not observed	not observed
Jet quenching through correlations	yes (Z–jet, γ –jet, h–jet)	not observed (h–jet)	not measured
Heavy flavor anisotropy	yes	yes	not measured
Quarkonia production	suppressed [†]	suppressed	not measured

One fluid rules all – early work

One fluid to rule them all: Viscous hydrodynamic description of event-by-event central p+p, p+Pb and Pb+Pb collisions at $\sqrt{s} = 5.02$ TeV

Ryan D. Weller^a, Paul Romatschke^{a,b,*}

[Physics Letters B 774 \(2017\) 351–356](#)



- superSONIC describes v_2 and v_3 data in pp, p-Pb and Pb-Pb using a single choice for the fluid parameter
- Suggests **common hydrodynamic origin** including pp collisions

Can one fluid rules them all ?

-a detailed evaluations from hydrodynamics

Brief review for Pb-Pb, p-Pb collisions

-Success of hydrodynamics (Pb-Pb)

-hydro descriptions; initial /final state effects (p-Pb)

Pb+Pb, p-Pb, p-p collisions

-can one hydrodynamics (with the same parameters) rules them all ?

p-p collisions

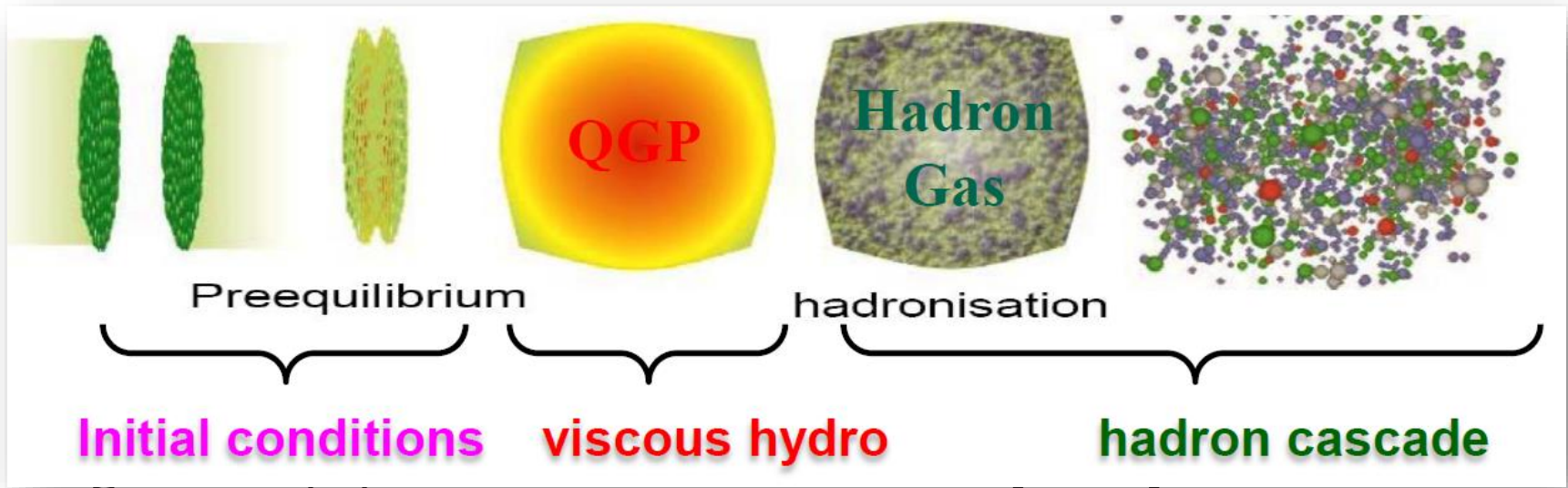
-sign of $C_2\{4\}$ & non-linear effect from hydrodynamics

Can one fluid rules them all ?

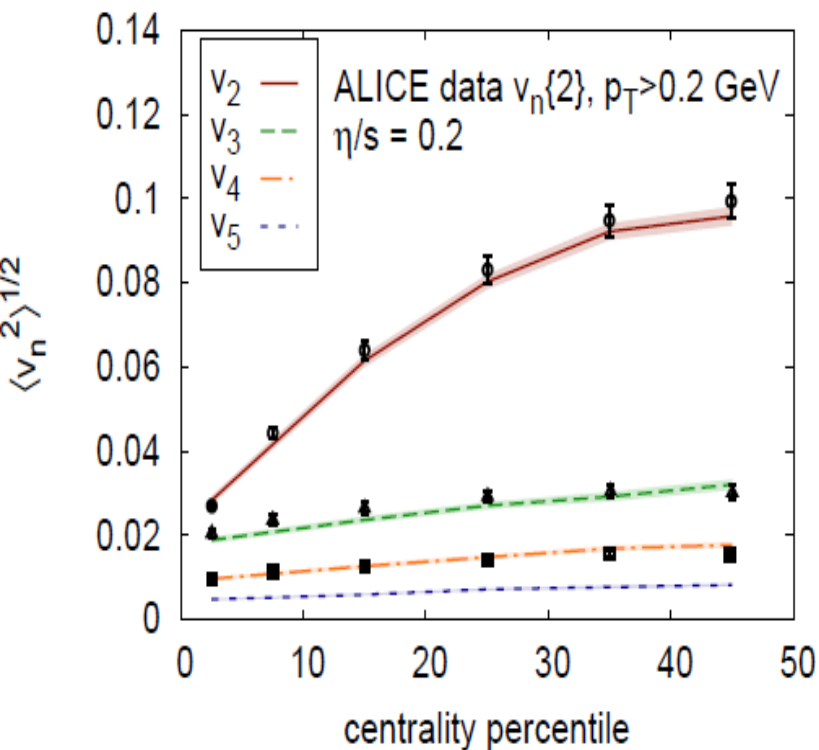
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Brief review for Pb-Pb, p-Pb collisions

-Success of hydrodynamics (Pb-Pb)



The Success of Hydrodynamics in Pb+Pb collisions



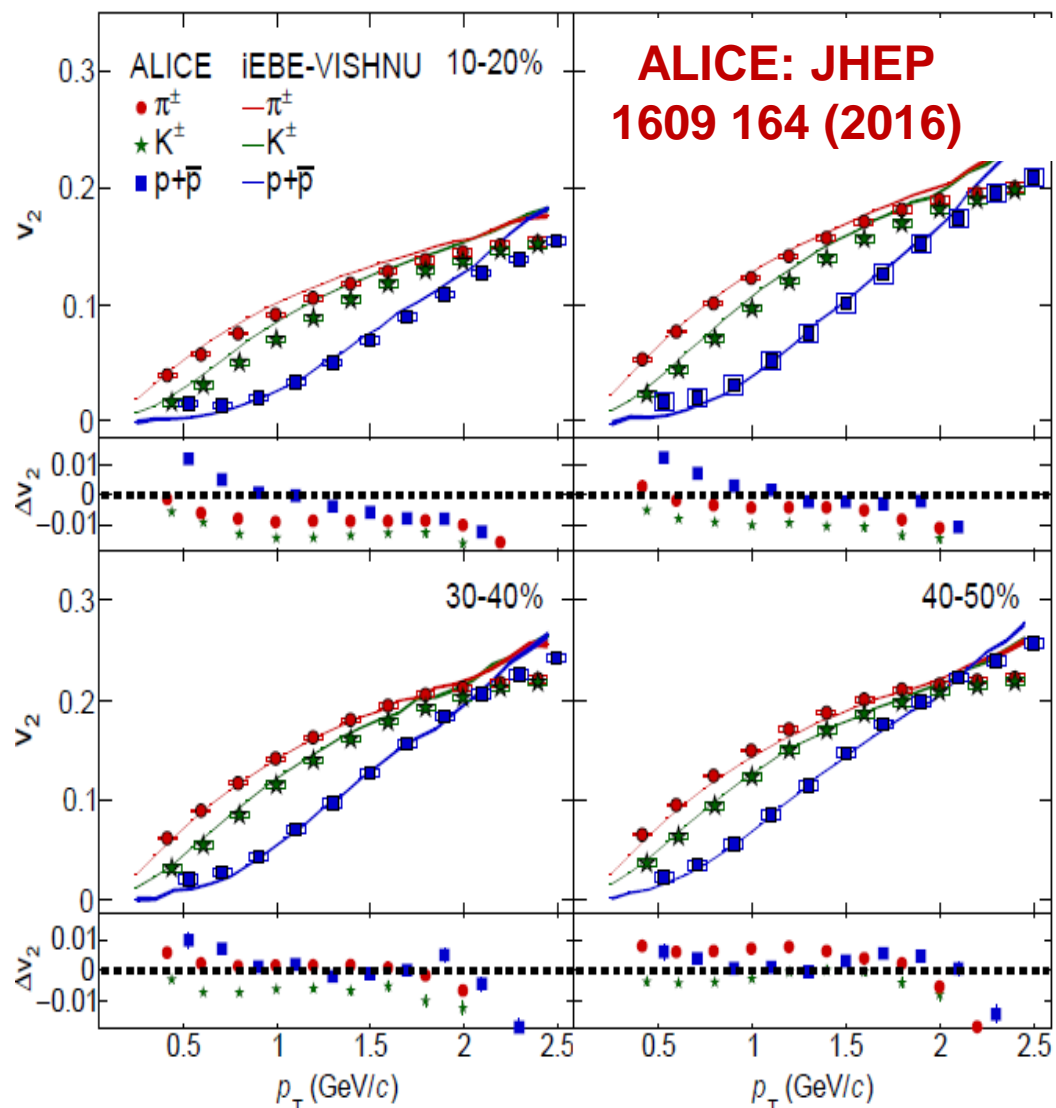
-Hydro + IP-Glasma

Gale, et. Al, PRL2013

-iEBE-VISHNU + AMPT

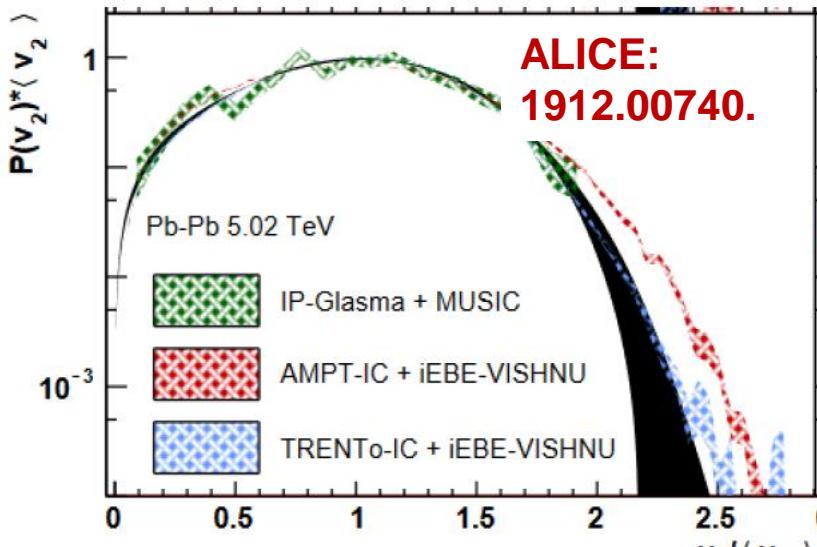
Xu, Li, Song, PRC 2016

-hydrodynamics nice describe of integrated and differential V_n of all charged and identified hadrons

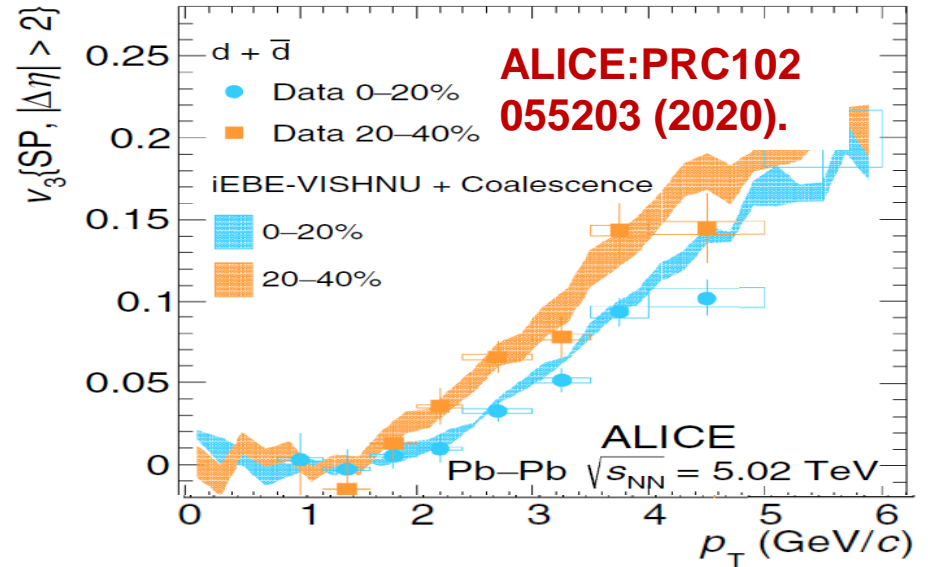


The Success of Hydrodynamics in Pb+Pb collisions (II)

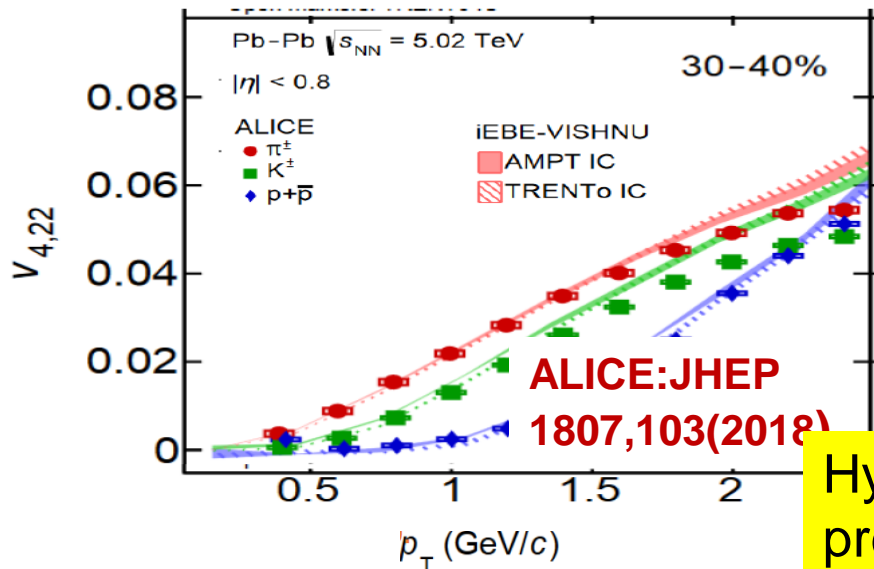
Flow distributions



V2, V3 for deuterons



Non-Linear flow modes



Hydro calculations / predictions:

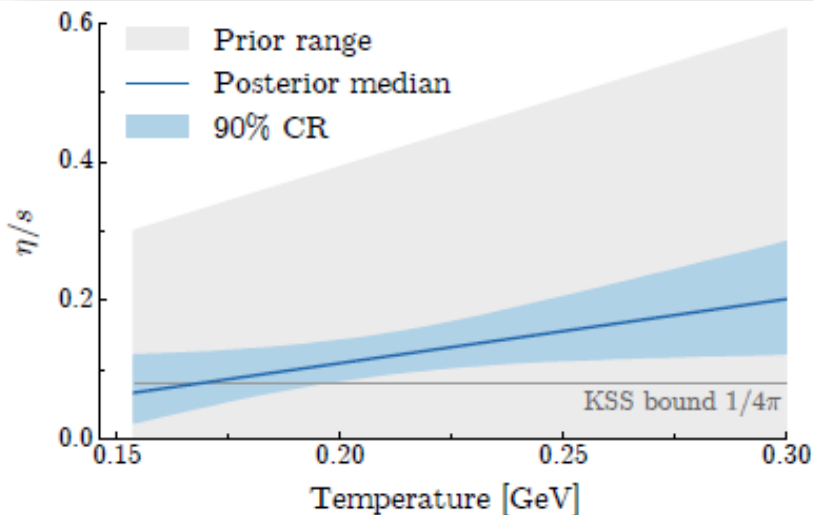
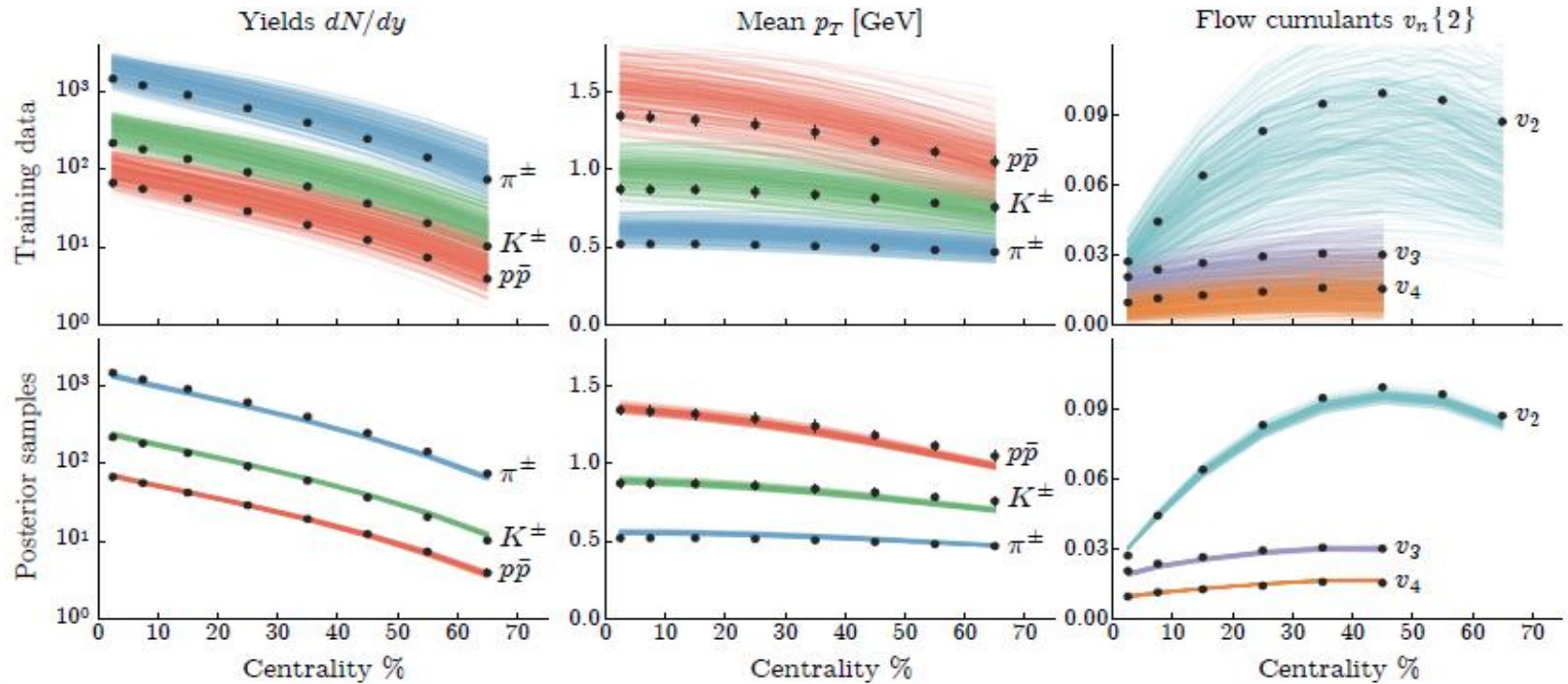
iEBE-VISHNU: Zhao, Xu & Song, Eur. Phys. J. C 77, no. 9, 645 (2017).

Hydro output + coalescence model predictions:

iEBE-VISHNU+coalescence: Zhao, Zhu, Zheng, Ko, Song, Phys. Rev. C 98 5, 054905 (2018)

Hydro quantitatively / qualitatively describe / predict various flow data for Pb+Pb collisions

An quantitatively extract the QGP viscosity



-An quantitatively extraction of the QGP viscosity with iEBE-VISHNU and the massive data evaluation

- $\eta/s(T)$ is very close to the KSS bound of $1/4\pi$

J. Bernhard, etc.al.PRC94,024907 (2016).
Nature Phys.15 (2019) 11, 1113.

Can one fluid rules them all ?

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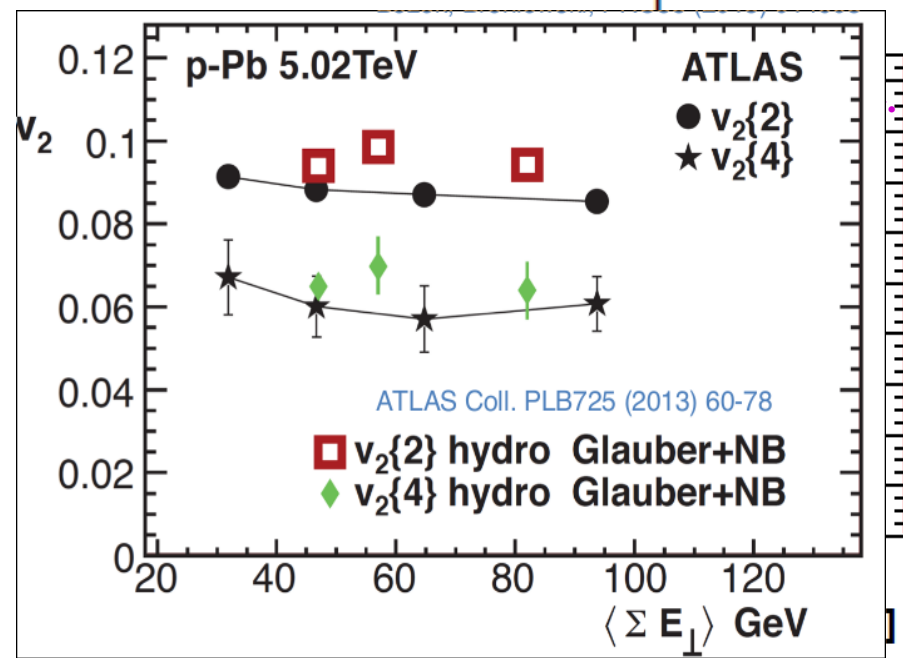
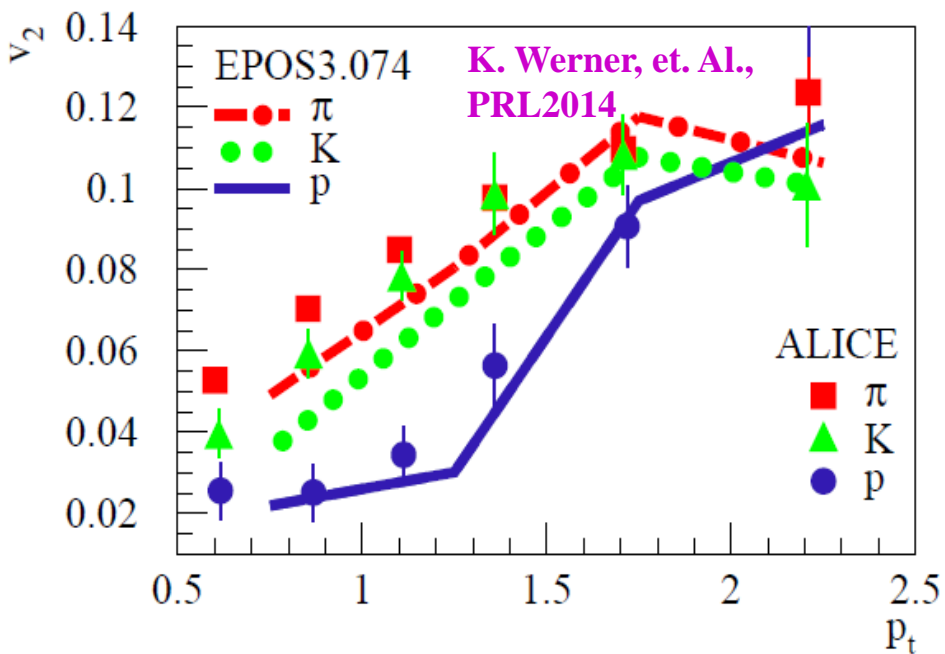
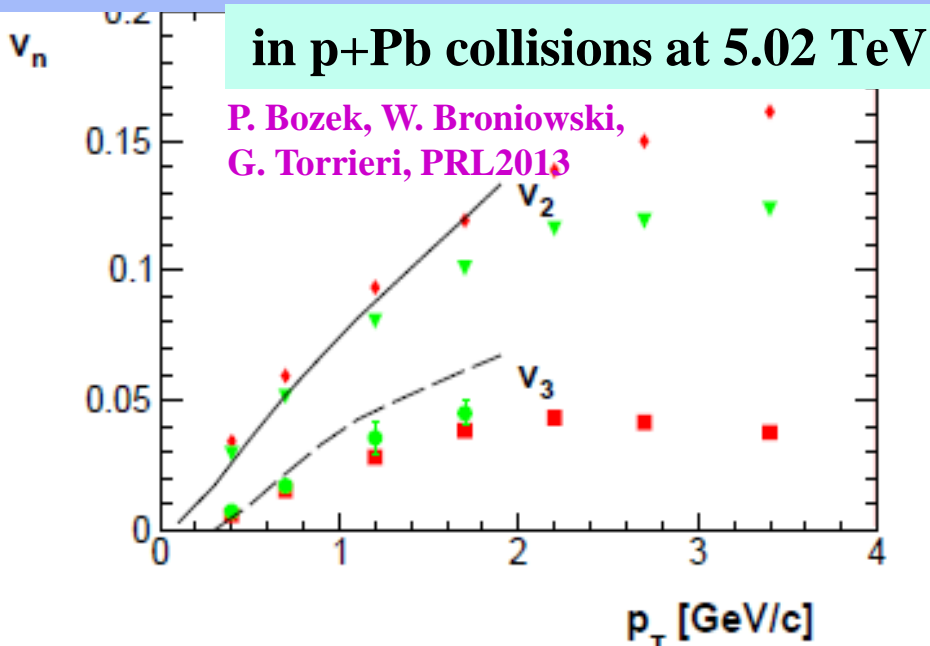
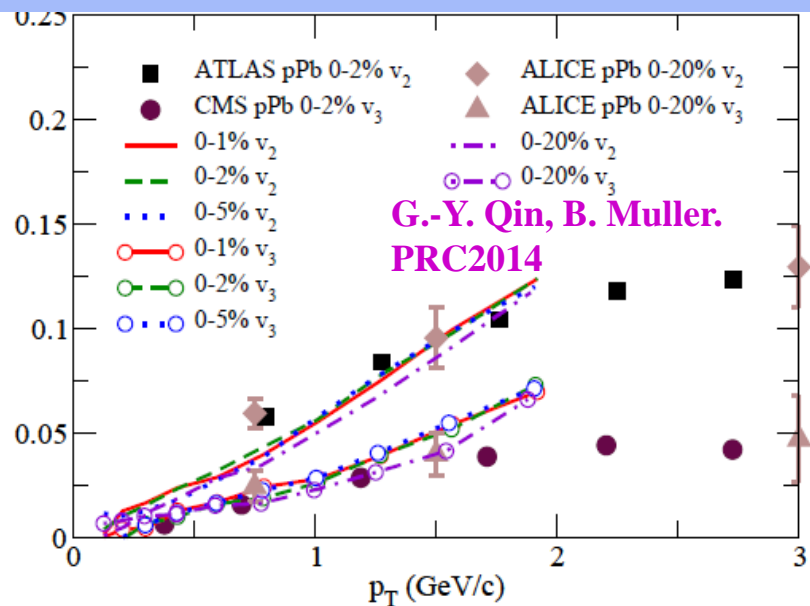
Pb+Pb, p-Pb, p-p collisions

-can one hydrodynamics (fluid) rules them all ?

p-p collisions

-sign of $C_2\{4\}$ & non-linear effect from hydrodynamics

Flow in p-Pb -- Hydrodynamics Simulations



Initial state or Final state effects?

Initial state effects:

– Various Models interpolations

- K. Dusling and R. Venugopalan, PRL 2012, PRD2013, NPA 2014
- A. Dumitru and A. V. Giannini, NPA 2015, A. Dumitru and V. Skokov PRD2015
- B. Schenke, S. Schlichting, P. Tribedy, and R. Venugopalan, PRL2016
- K. Dusling et al, Phys. Rev. Lett 120 042002 (2018)
- C. Zhang, et al Phys. Rev. Lett. 122, no. 17, 172302 (2019).

... ..

Final state interactions:

- P. Bozek, W. Broniowski, G. Torrieri, PRL2013
- K. Werner, et. Al., PRL2014
- G.-Y. Qin, B. Muller. PRC2014
- Y. Zhou, X. Zhu, P. Li, and H. Song, PRC2015
- P. Bozek, A. Bzdak, and G.-L. Ma, PLB2015
- P. Romatschke, Eur.Phys.J. C77 21(2017)
- W. Zhao, Y. Zhou, H. Xu, W. Deng and H. Song, Phys. Lett. B 780, 495 (2018)

... ..



Can one fluid rule them all ?

-a detailed evaluations from hydrodynamics

Brief review for Pb-Pb, p-Pb collisions

-Success of hydrodynamics (Pb-Pb)

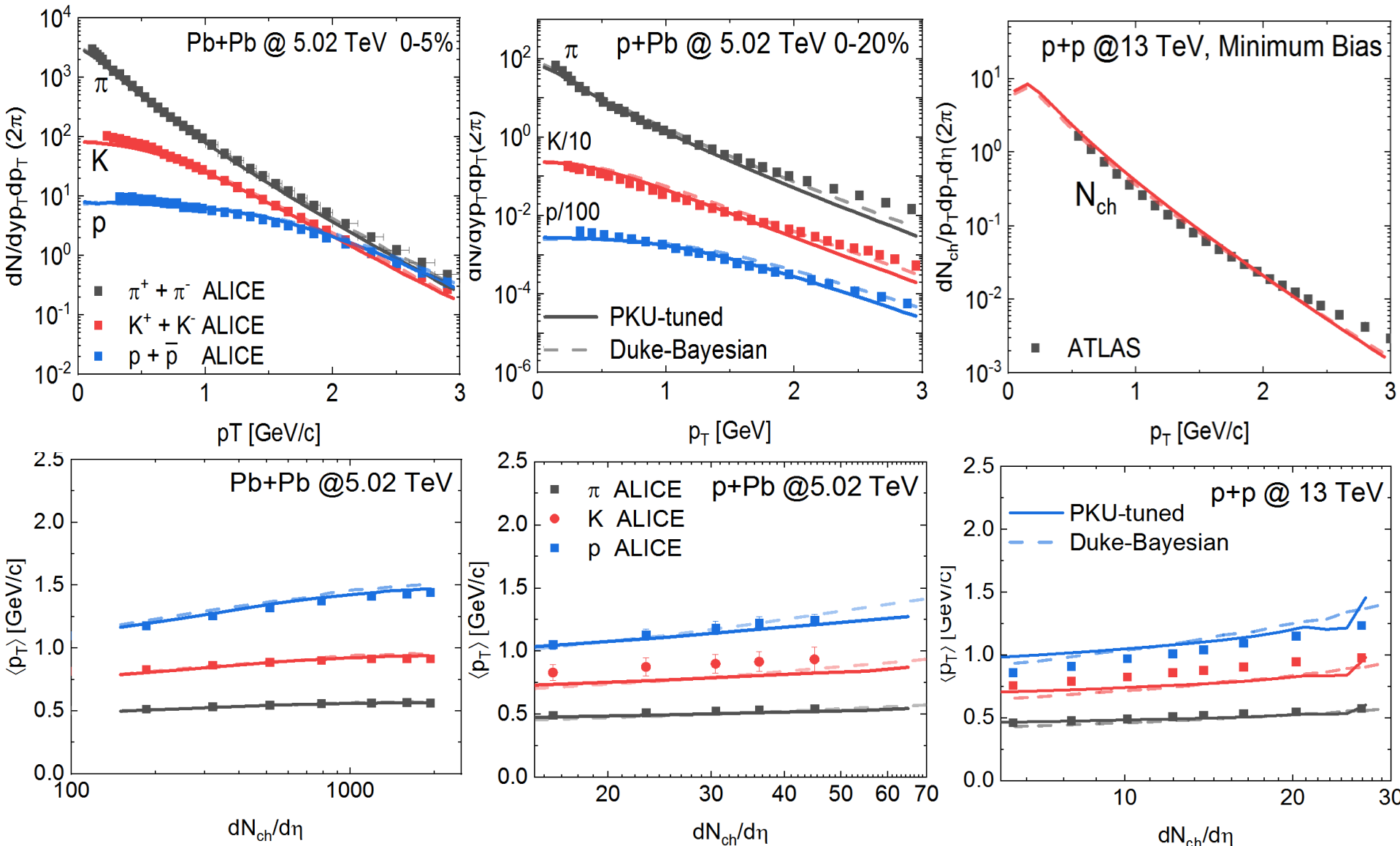
-hydro descriptions; initial /final state effects (p-Pb)

Pb+Pb, p-Pb, p-p collisions

-can one hydrodynamics with the same parameters rule them all ?

p-p collisions

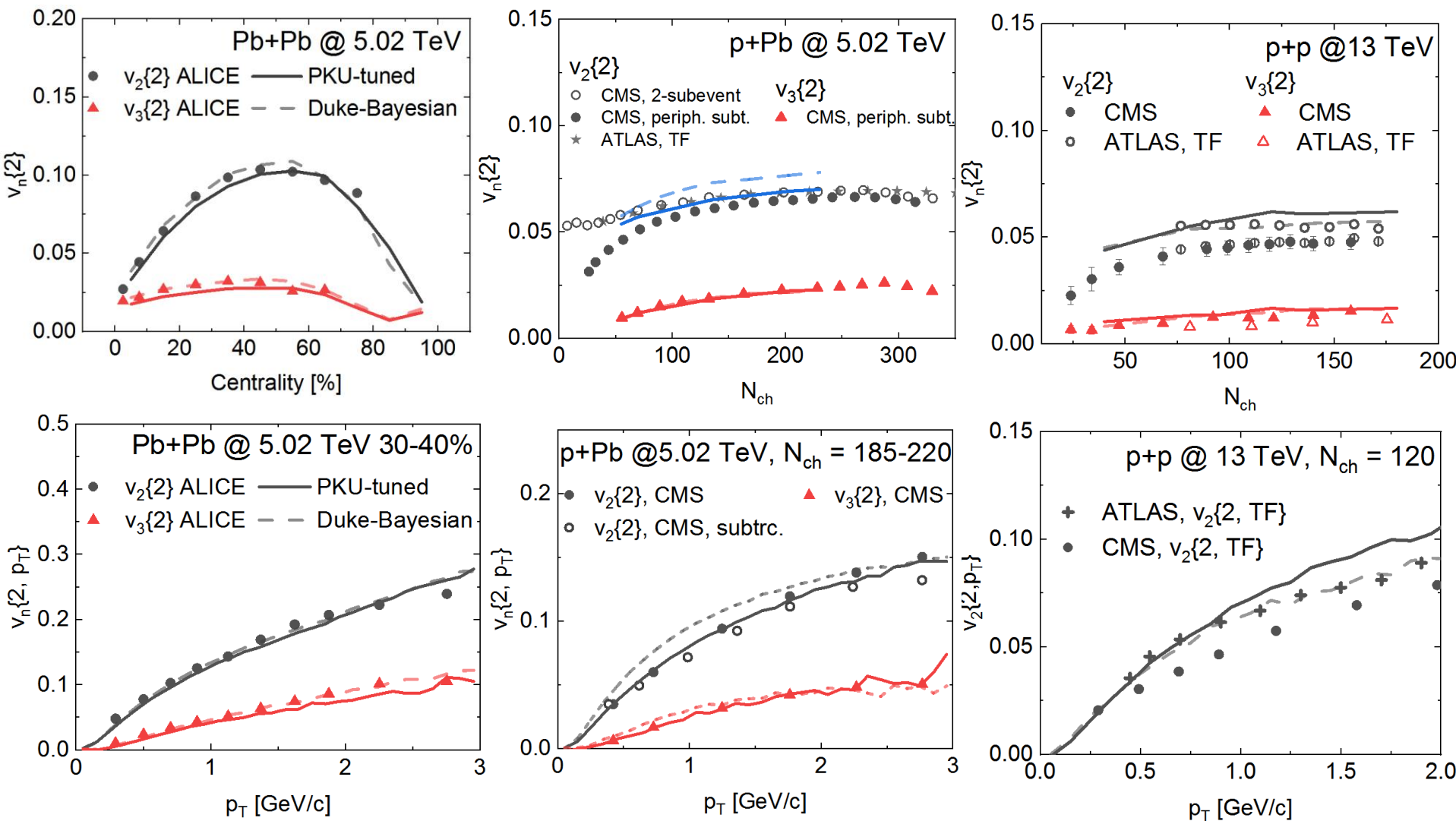
-sign of $C_2\{4\}$ & non-linear effect from hydrodynamics



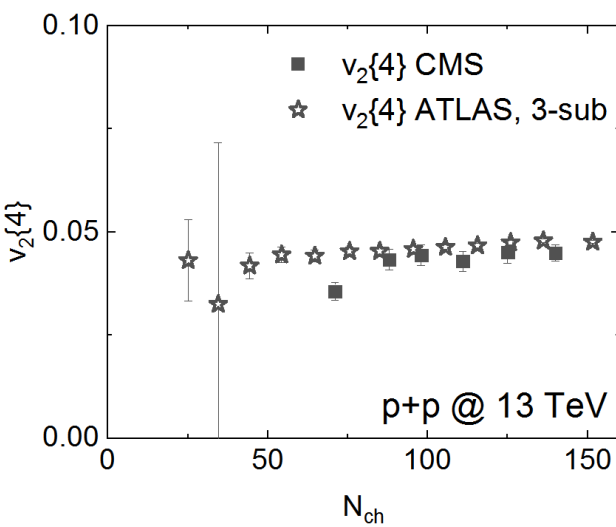
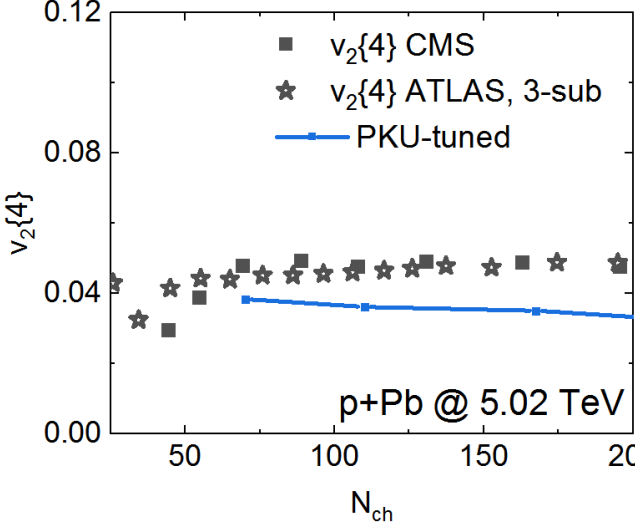
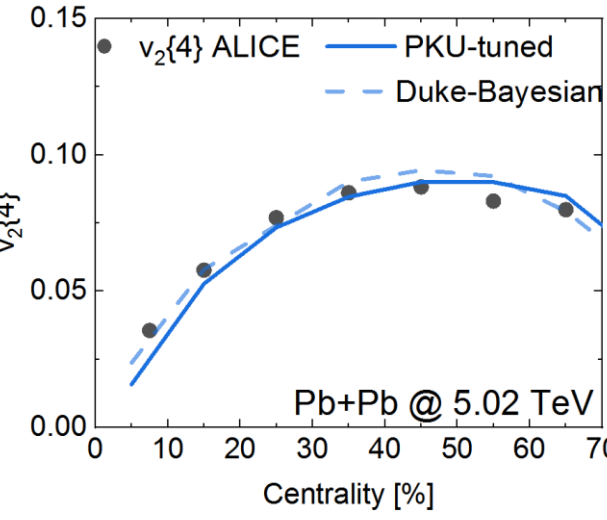
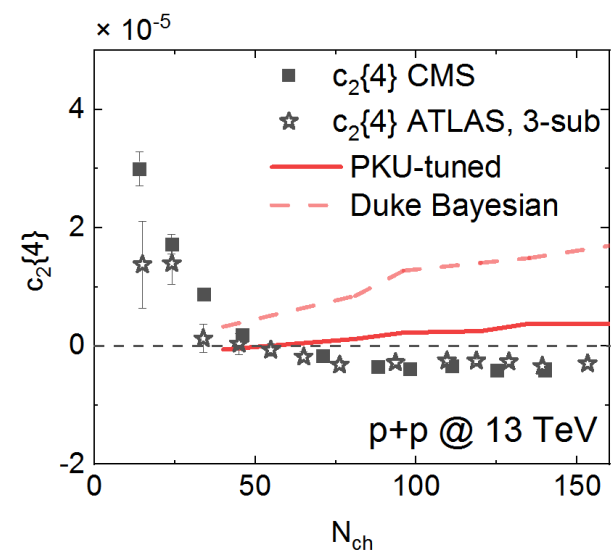
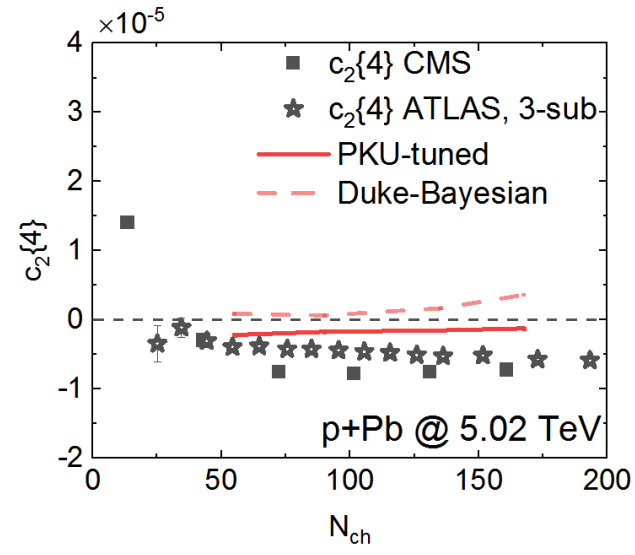
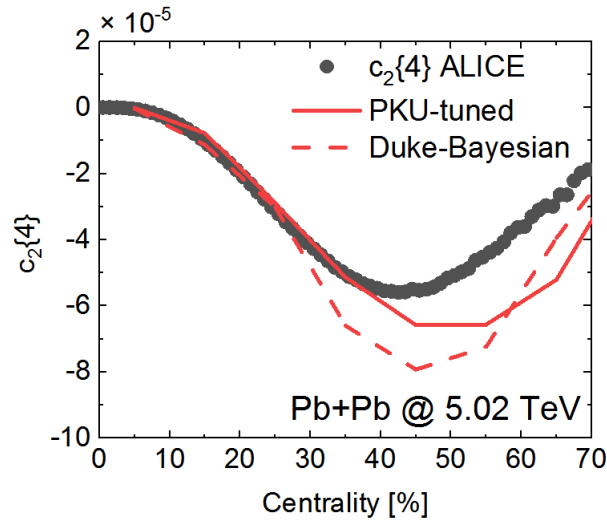
Hydrodynamic simulations (iEBE-VISHNU +TRENTo) nicely fit the P_T spectra and $\langle P_T \rangle$ for Pb-Pb, p-Pb and p-p collisions with the same parameter set

-Duke parameter: Phys.Rev.C 101 (2020) 2, 024911

-PKU parameter: (smaller fluctuations) Fu, Zhao & Song, in preparation



Hydrodynamic simulations (iEBE-VISHNU +TRENTo) with both Duke Bayesian parameter / PKU tuned parameter roughly fit v_2 v_3 measured from 2 particle correlations.



Hydrodynamic simulations (iEBE-VISHNU +TRENTo) with both Duke / PKU parameters fails to reproduce negative $c_2\{4\}$

One fluid rule can not them (Pb-Pb,p-Pb, p-p) all

Sign problem of $c_2\{4\}$ in p-p collisions

Fu, Zhao & Song, in preparation

Can one fluid rules them all ?

-a detailed evaluations from hydrodynamics

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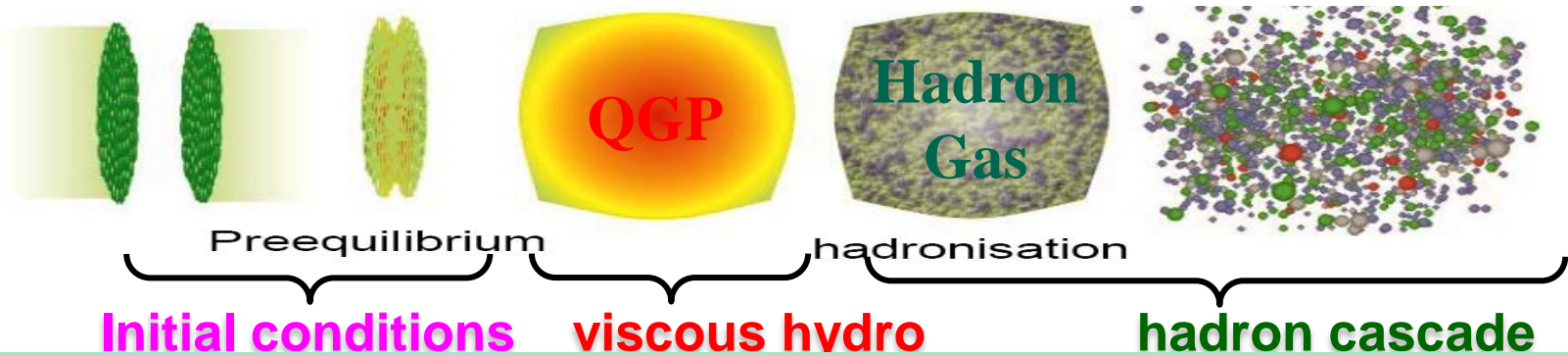
Pb+Pb, p-Pb, p-p collisions

-can one hydrodynamics (fluid) rules them all ?

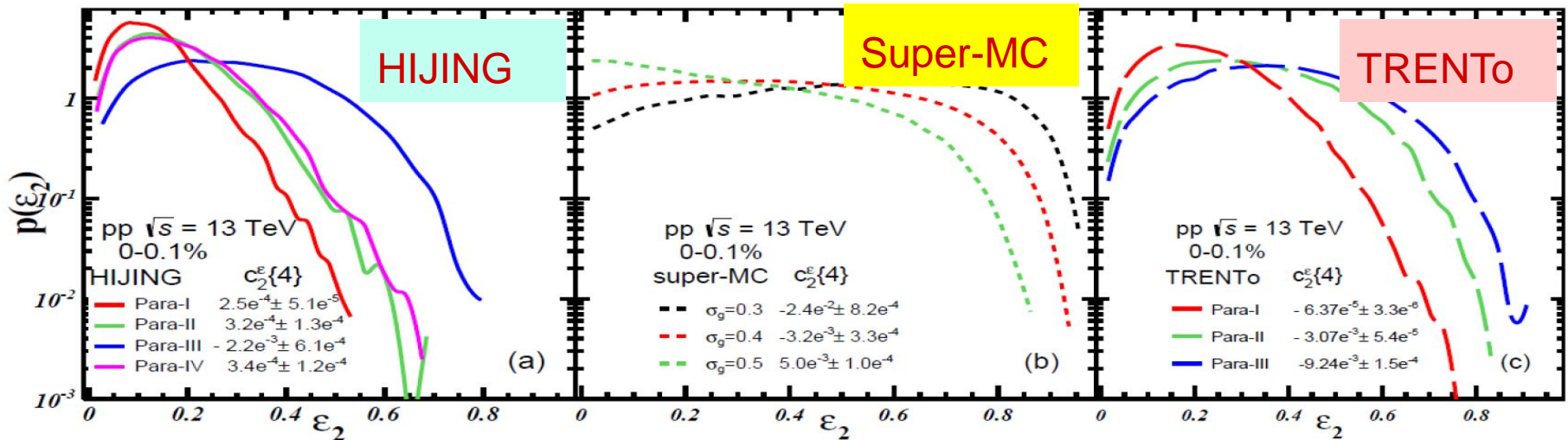
p-p collisions

-sign problem of $C_2\{4\}$ & non-linear effect from hydrodynamics

iEBE-VISHNU hybrid model

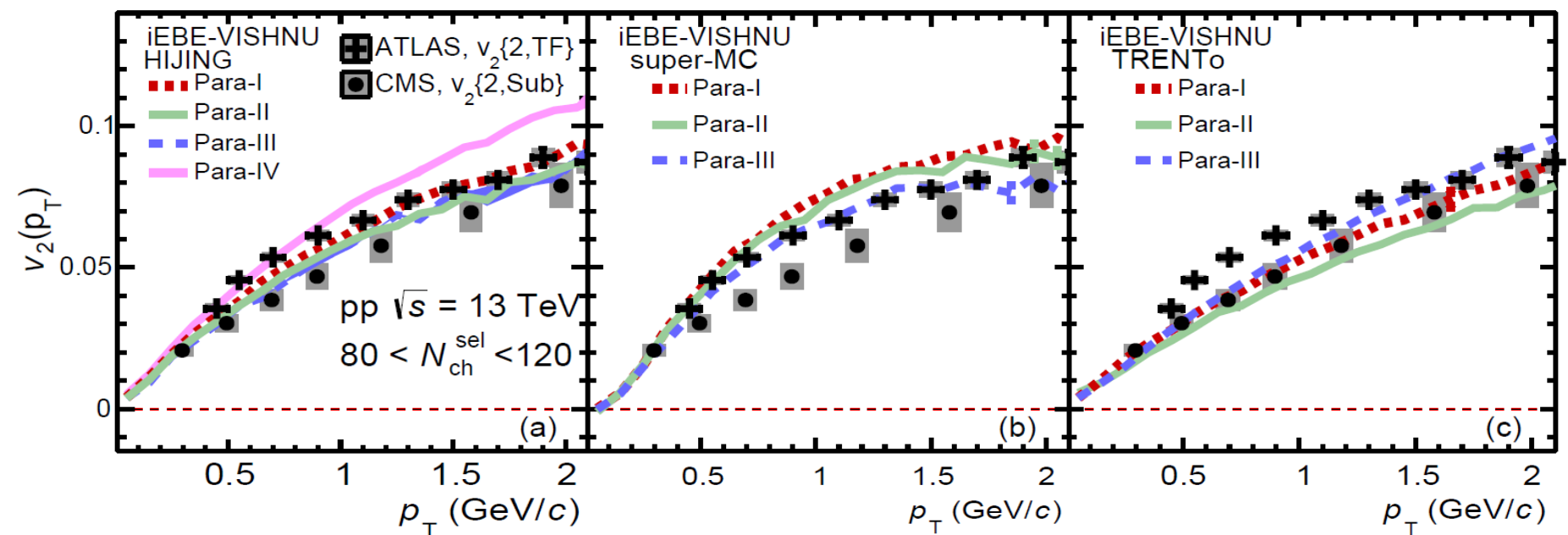
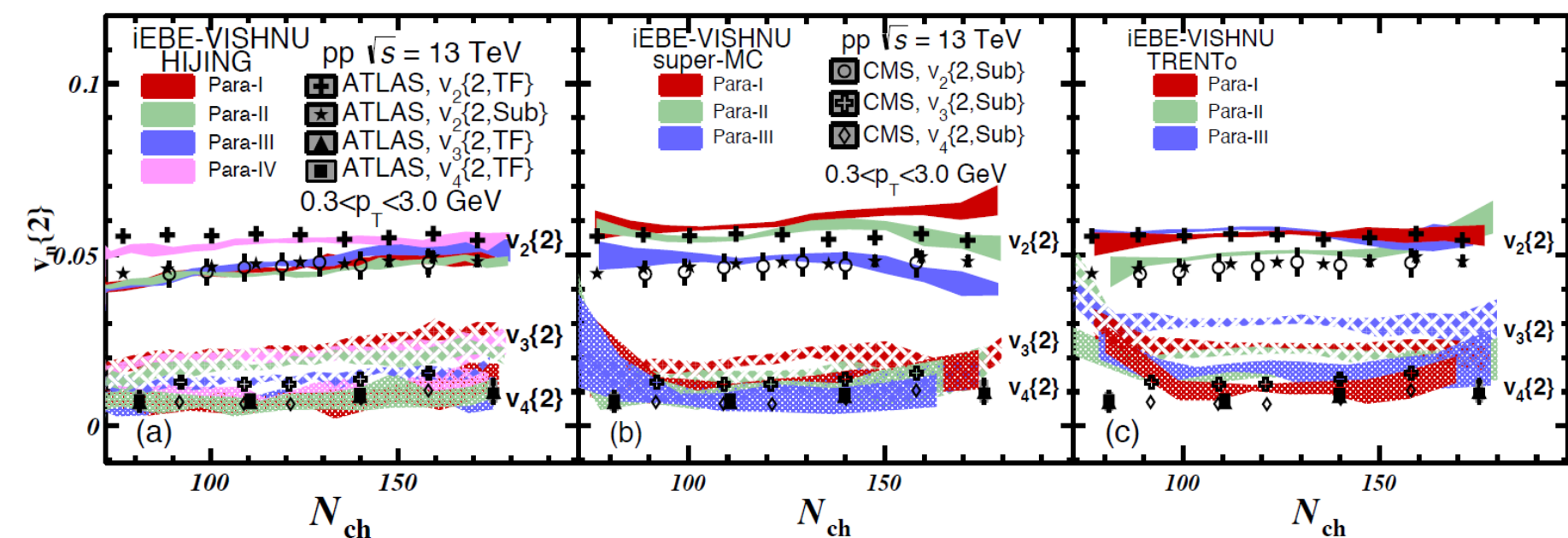


Different initial conditions

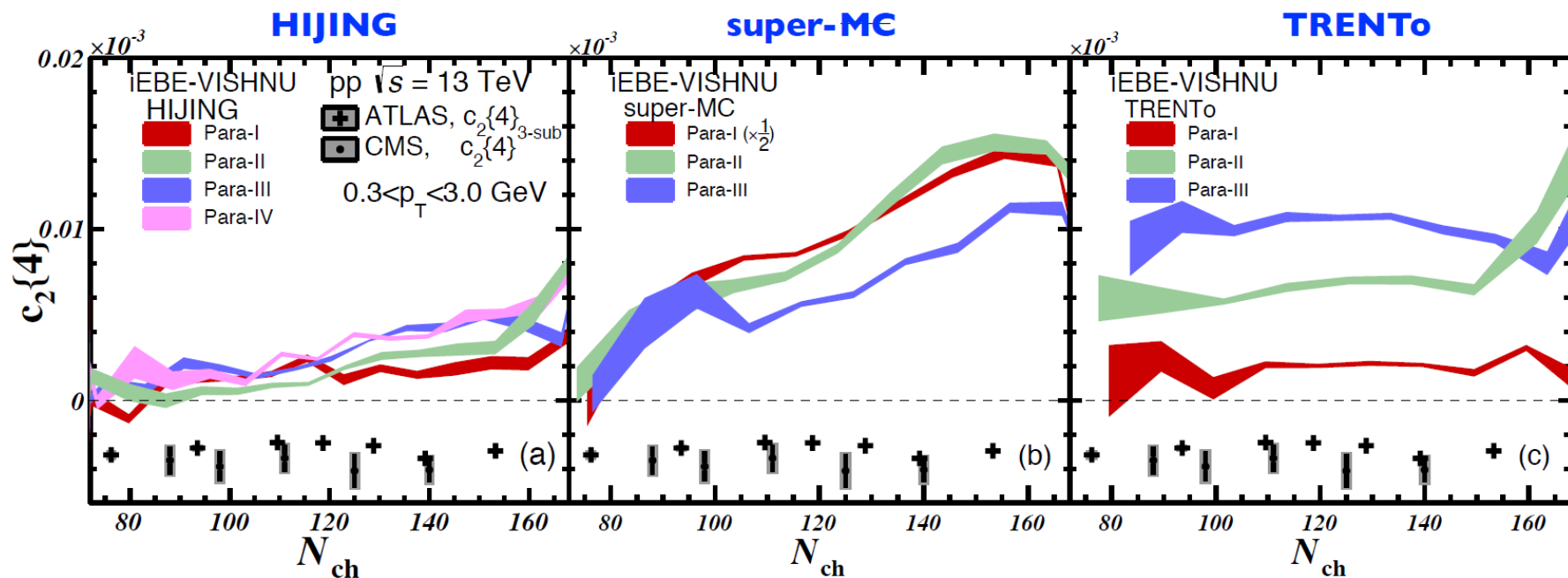
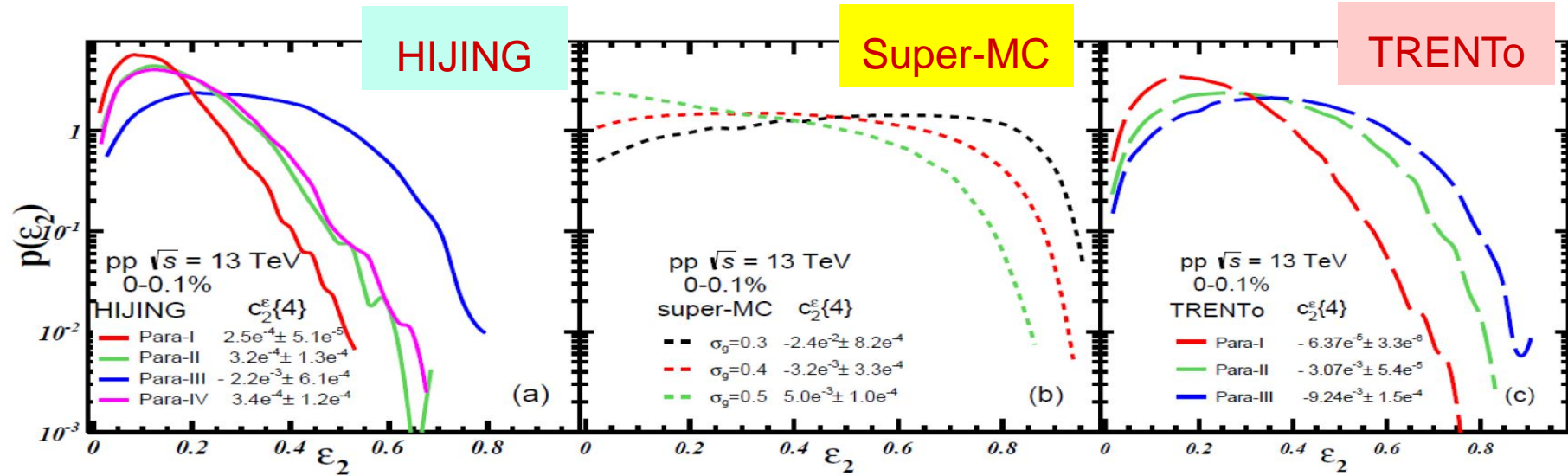


-Different $p(\epsilon_2)$ distributions with positive and negative $C_2\{4\}$

HIJING Zhao Zhou, Xu, Deng & Song, Phys. Lett. B 780, 495 (2018); Super-MC Welsh, Singer & Heinz, PRC 94,024919 (2016). TRENTo: Moreland, Bernhard and Bass, PRC 101, 024911 (2020).

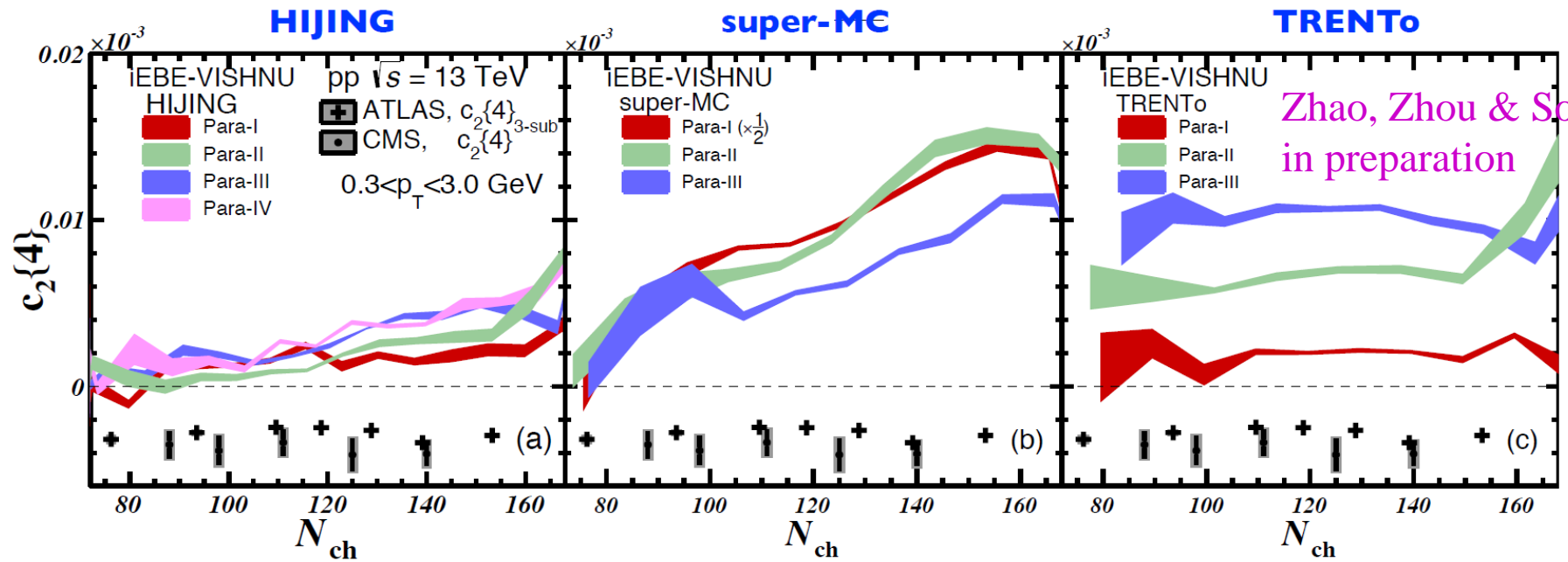


-Hydrodynamics with different initial conditions could roughly describe v_2 & v_3

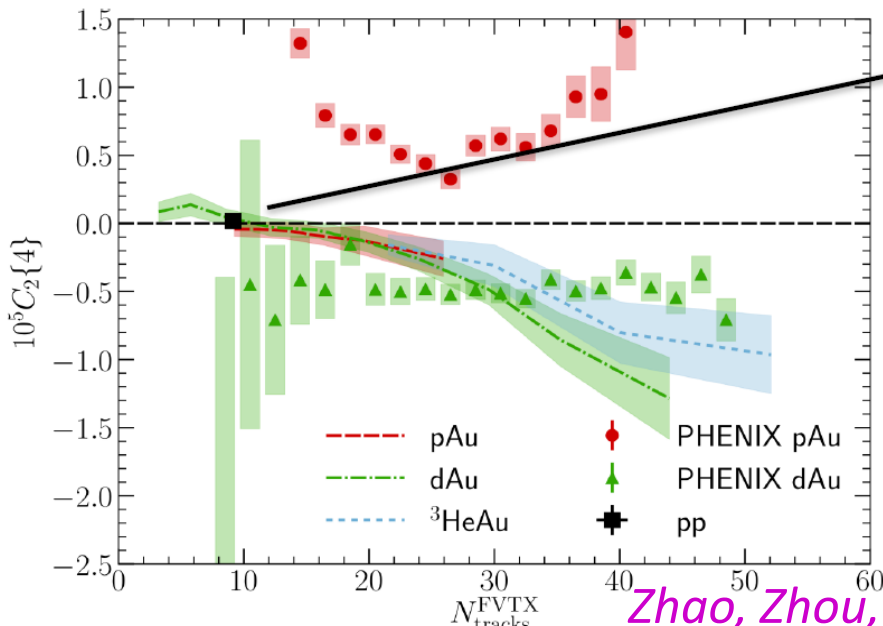


Hydro simulations with various initial conditions fails to reproduce negative $C_2\{4\}$

$C_2\{4\}$ from hydro with various initial conditions



Zhao, Zhou & Song, in preparation

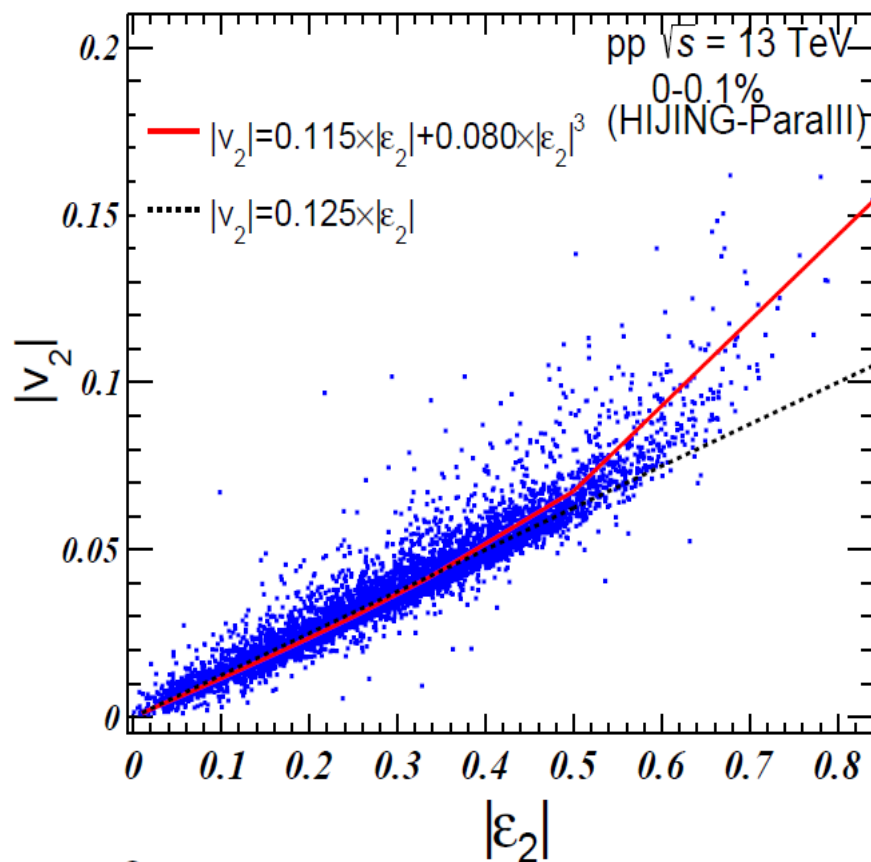
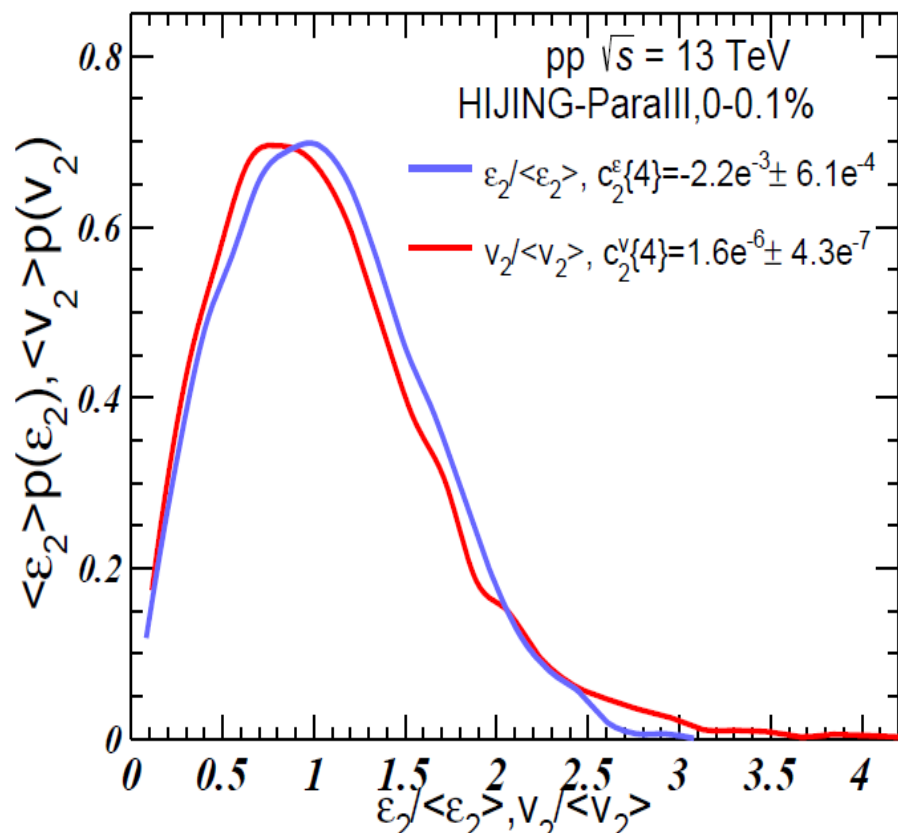


The sign problem of $C_2\{4\}$

-IEBE-VISHNU with various initial conditions can not describe negative $c_2\{4\}$.

-MUSIC with IP-glasma also give positive $c_2\{4\}$ in pp collisions

$P(v_2)$ and $P(\varepsilon_2)$ distributions: from $C_2^\varepsilon\{4\}$ to $C_2^v\{4\}$



-Cubic response: $|v_2| = 0.115|\varepsilon_2| + 0.080|\varepsilon_2|^3$

-Certain deviations between $P(v_2/\langle v_2\rangle)$ and $P(\varepsilon_2/\langle\varepsilon_2\rangle)$

Leading small negative $C_2^\varepsilon\{4\}$ change to small positive $C_2^v\{4\}$

Such sign problem of $c_2\{4\}$ in p-p collisions is natural for hydro simulations

Can one fluid rules them all ?

-a detailed evaluations from hydrodynamics

Pb+Pb, p-Pb, p-p collisions

-can one hydrodynamics (fluid) rules them all ?

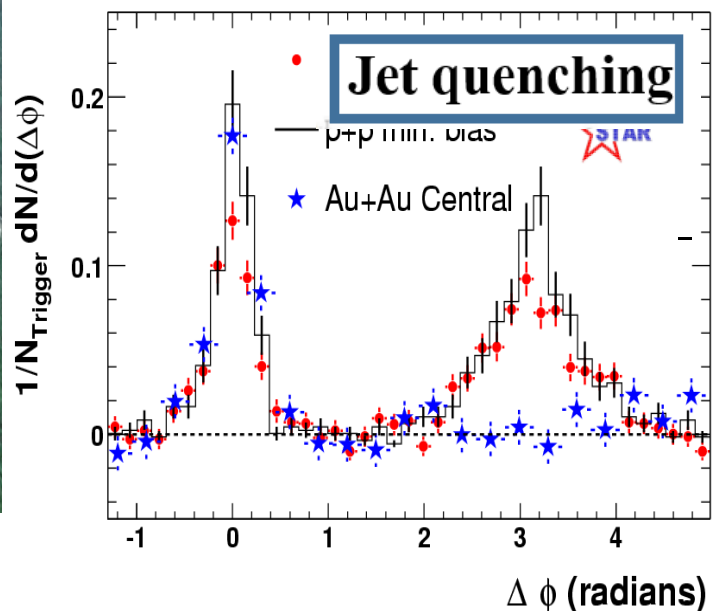
p-p collisions

-sign problem of $C_2\{4\}$ & non-linear effect from hydrodynamics

Is QGP formed in the small systems?

(p-Pb collisions)

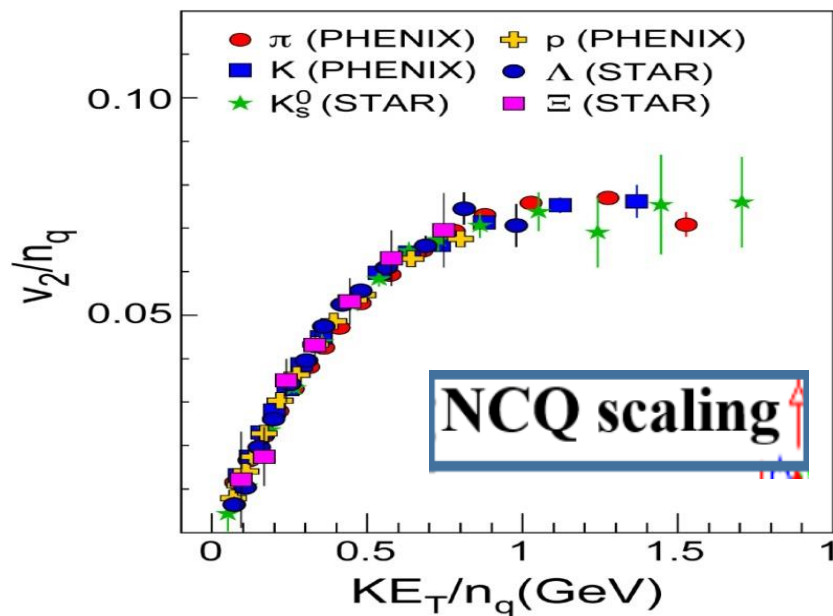
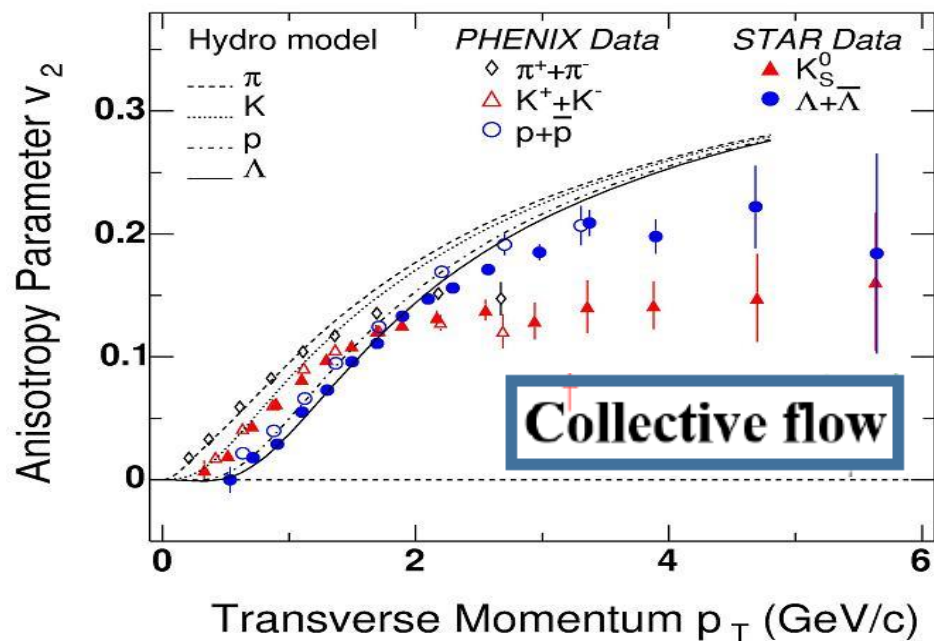
Reminder: QGP signals in large systems



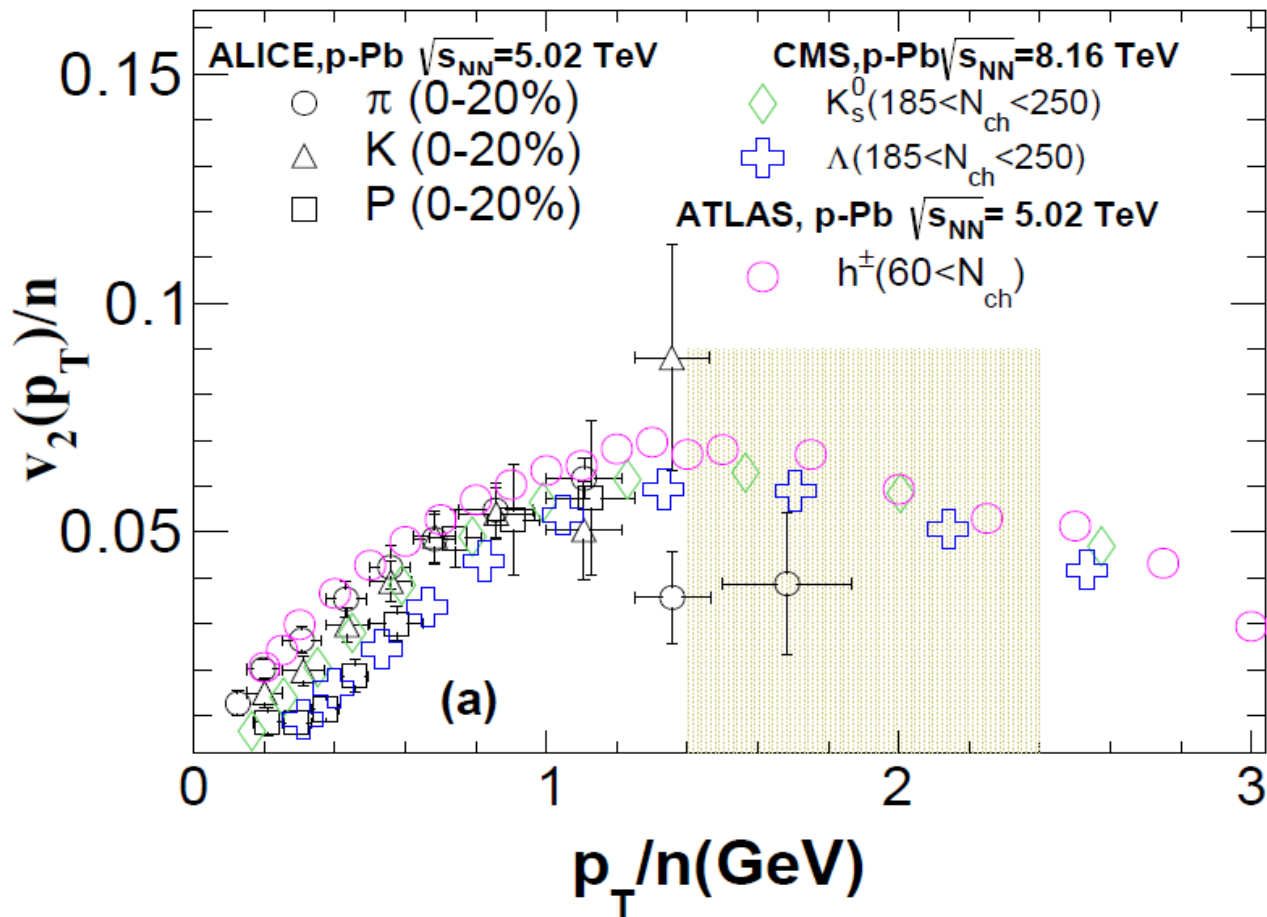
Au+Au / Pb+Pb

QGP was discovered
@RHIC & LHC

- strong elliptic flow
- jet quenching
- NCQ scaling of elliptic flow



NCQ scaling of v_2 in p-Pb collisions (EXP)



ALICE data: PLB, 726, 164 (2013).
CMS data: PRL, 121, 082301 (2018).
ATLAS data: PRC, 96, 024908 (2017).

- An observation of the approximately NCQ scaling at intermediate p_T in high multiplicity events of p-Pb collision in data.
- Is it an indication of the partonic degree of freedom?

Hydro-Coal-Frag Hybrid Model

Thermal hadrons (VISH2+1):

- generated by hydro.

with Cooper-Frye.

Meson: $P_T < 2P_1$; baryon: $P_T < 3P_1$.

Coalescence hadrons (Coal Model):

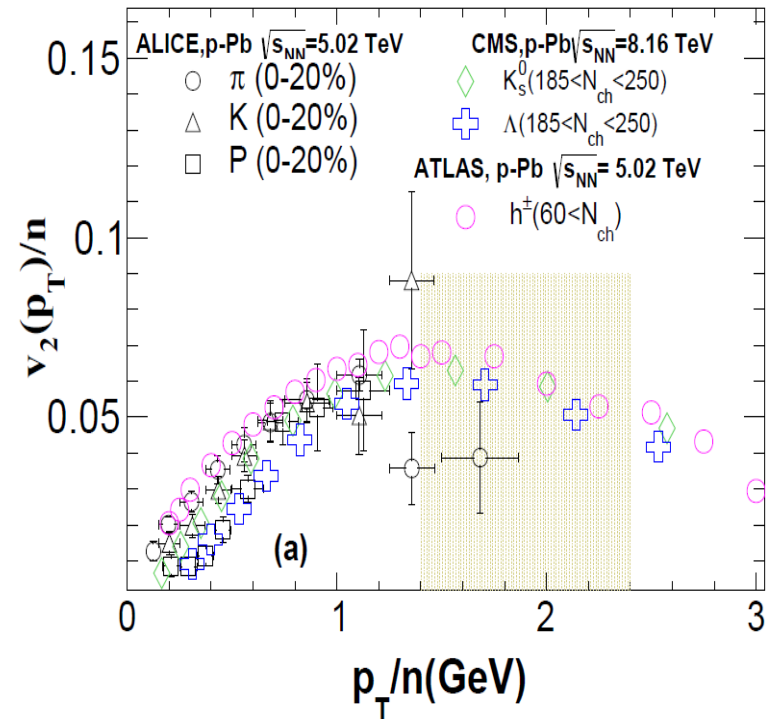
-generated by coalescences model including thermal-thermal, thermal-hard & hard-hard parton coalescence.

Fragmentation hadrons (LBT):

-the remnant hard quarks feed to fragmentation .

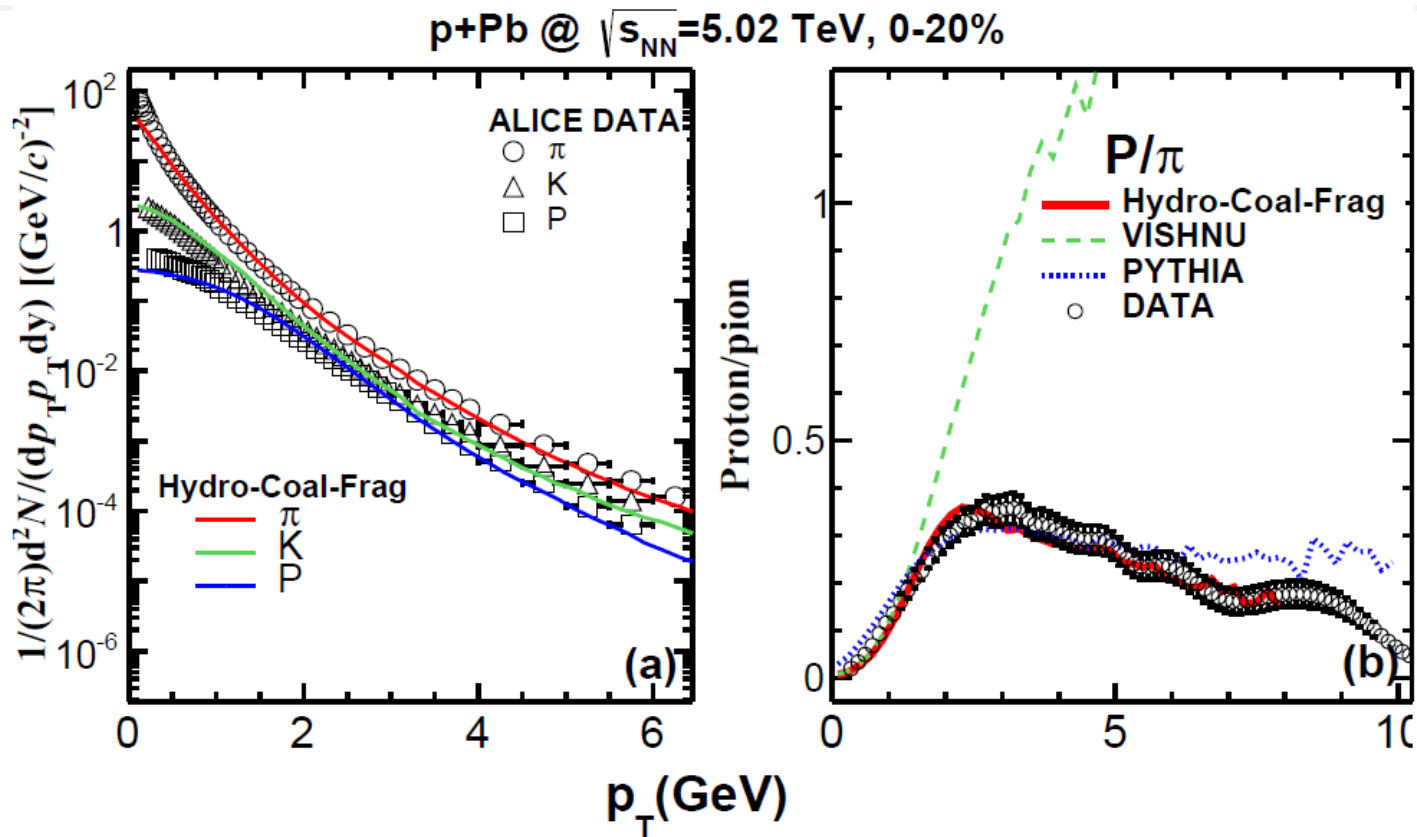
UrQMD afterburner:

-All hadrons are feed into UrQMD for hadronic evolution, scatterings and decays



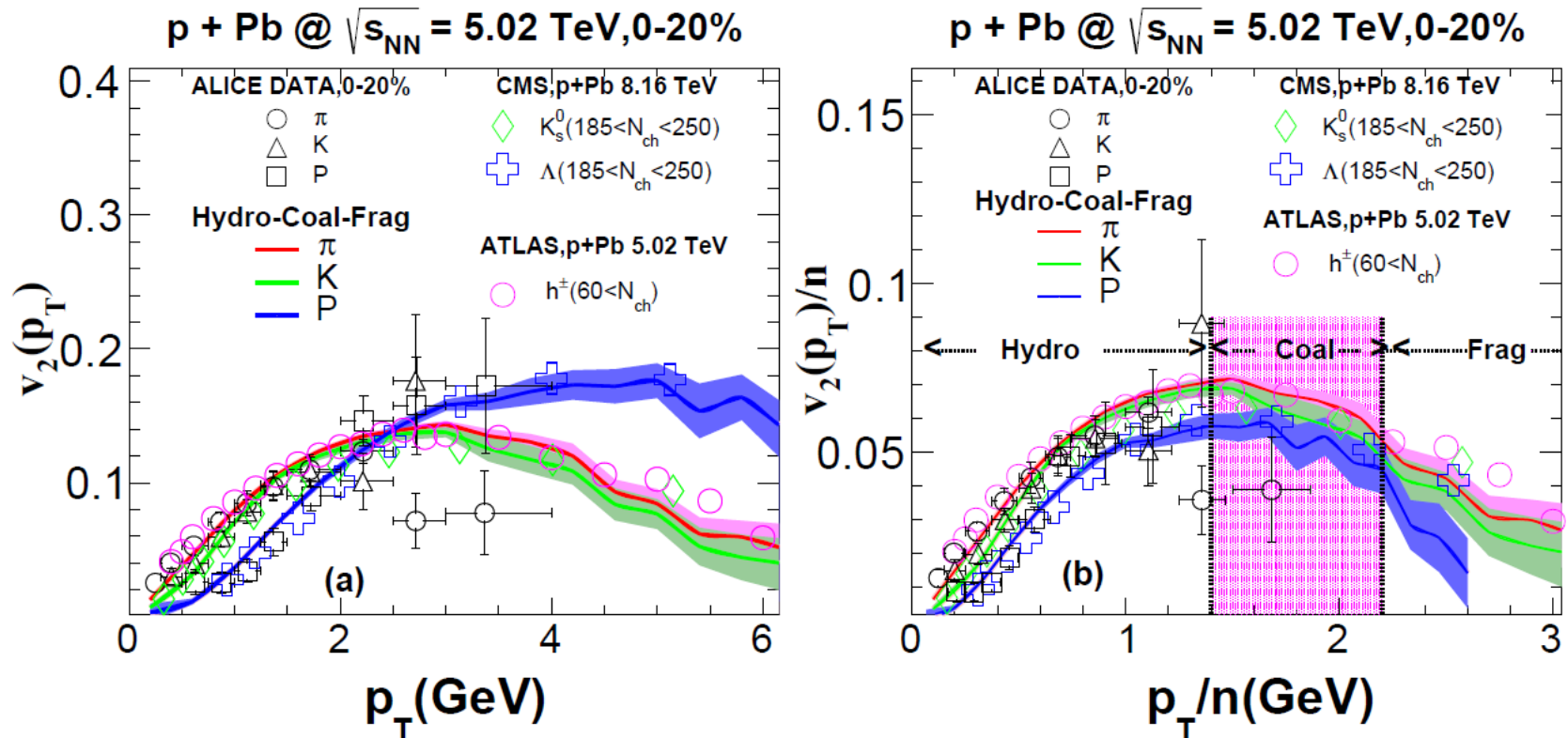
Zhao, Ko, Liu, Qin & Song,
Phys. Rev. Lett. 125 7 072301
(2020)

Spectra of pions, kaons and protons



Our combined model, Hydro-Coal-Frag, gives a nice description of spectra of pion, kaon and proton as well as the P/π over p_T from 0 to 6 GeV.

$v_2(p_T)$ and NCQ scaling



-Hydro-Coal-Frag model gives a nice description of $v_2(p_T)$ of pion, kaon and proton over p_T from 0 to 6 GeV.

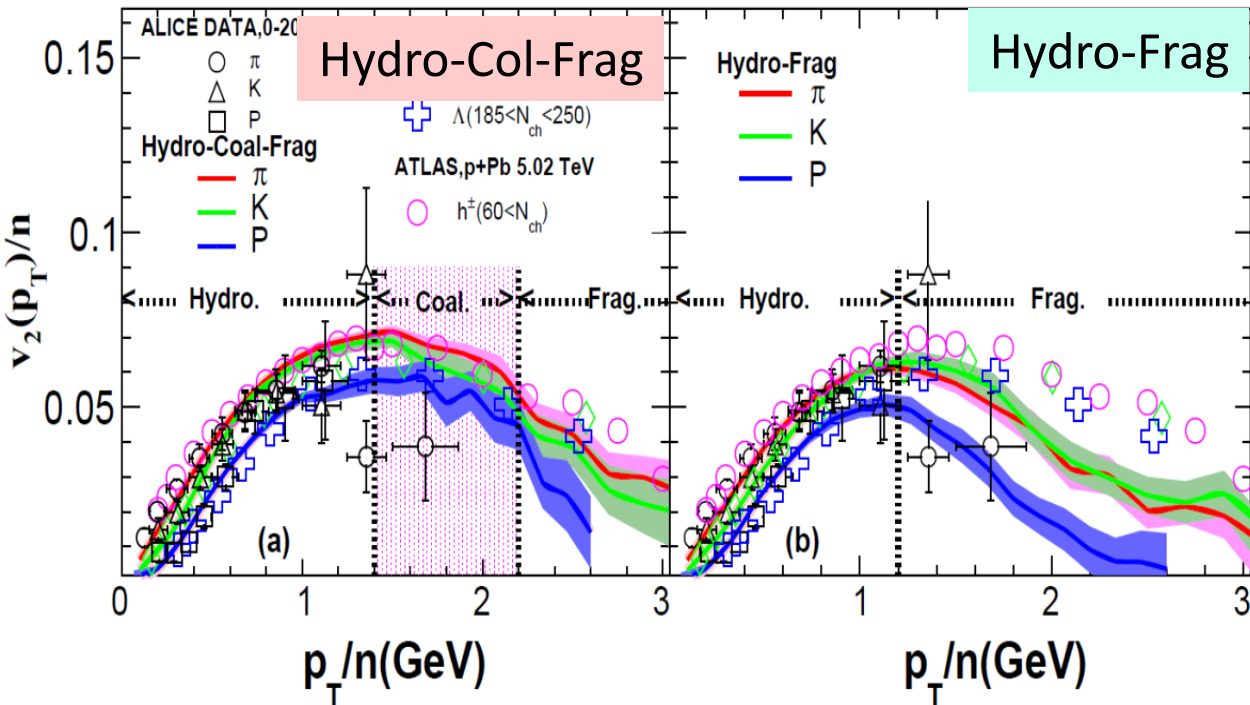
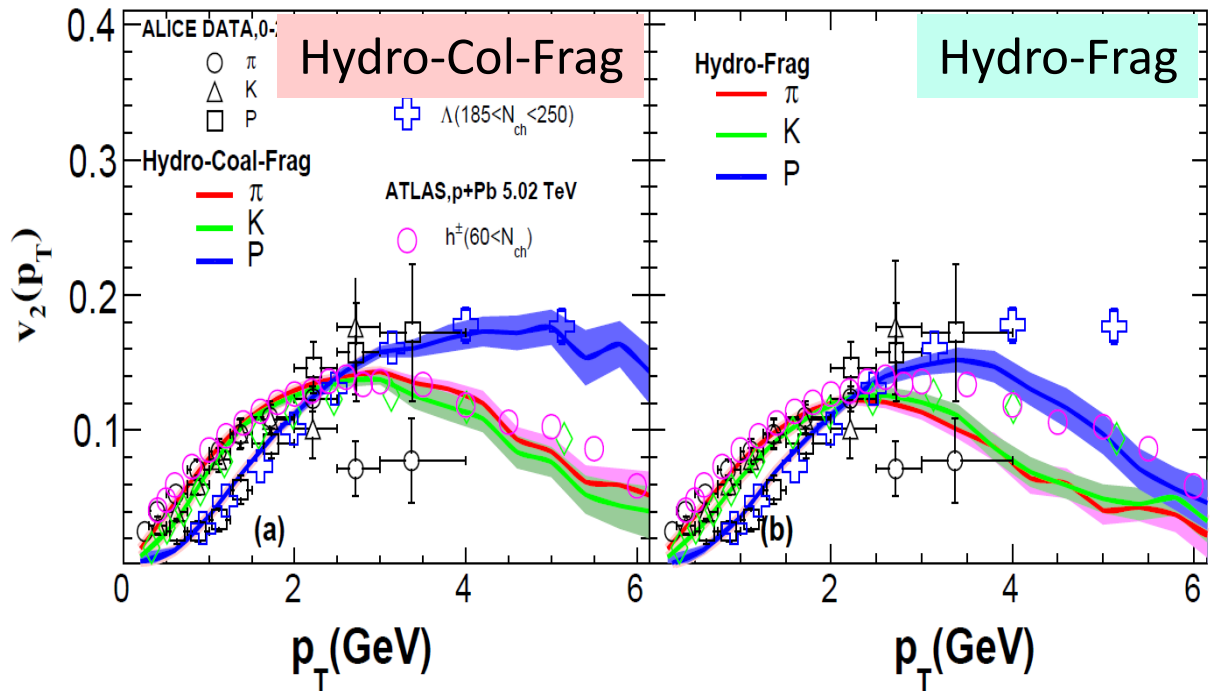
-At intermediate p_T , Hydro-Coal-Frag model can obtain an approximate NCQ scaling as shown by the data.

Strongly indication of partonic degree of freedom in small system.

The importance of quark coalescence in p-Pb collisions

Without coalescence, Hydro-Frag largely underestimates the $v_2(p_T)$ at intermediate p_T , violating the NCQ Scaling of v_2

Strongly indication of partonic degree of freedom in small system !



Zhao, Ko, Liu, Qin & Song, Phys. Rev. Lett. 125 7 072301 (2020)

Summary

-Can one fluid rule them all (Pb-Pb, p-Pb, p-p collisions) ?

NO !

Hydro simulations with various initial conditions **fails to reproduce negative $C_2\{4\}$ in p-p collisions**, due to non-linear response.

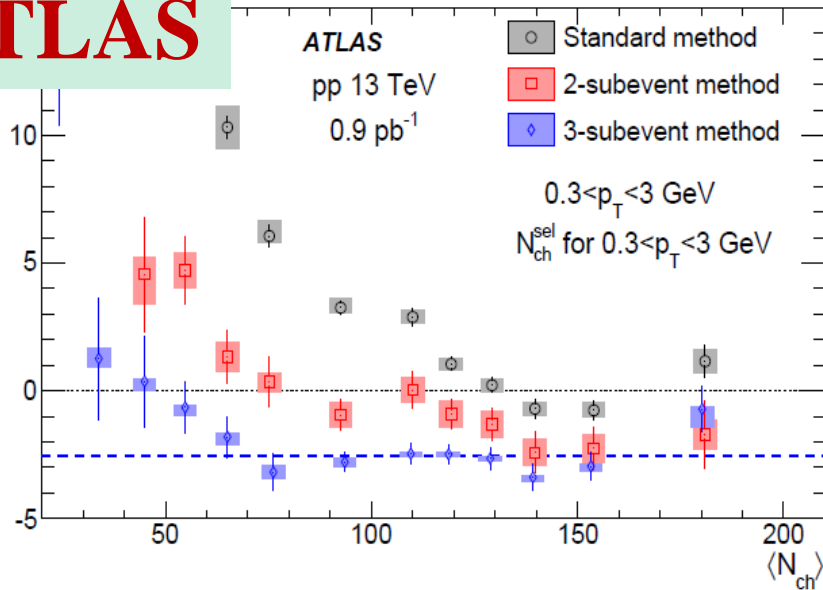
-Is QGP formed in the small systems (p-Pb collisions)?

Hydro-Coal-Frag calculations (Coalescence mechanism) nicely described NCQ scaling of v_2 at mediate p_T ,

strongly hint partonic degrees of freedom in high multiplicity p-Pb collisions

C2{4} - Experimental measurements

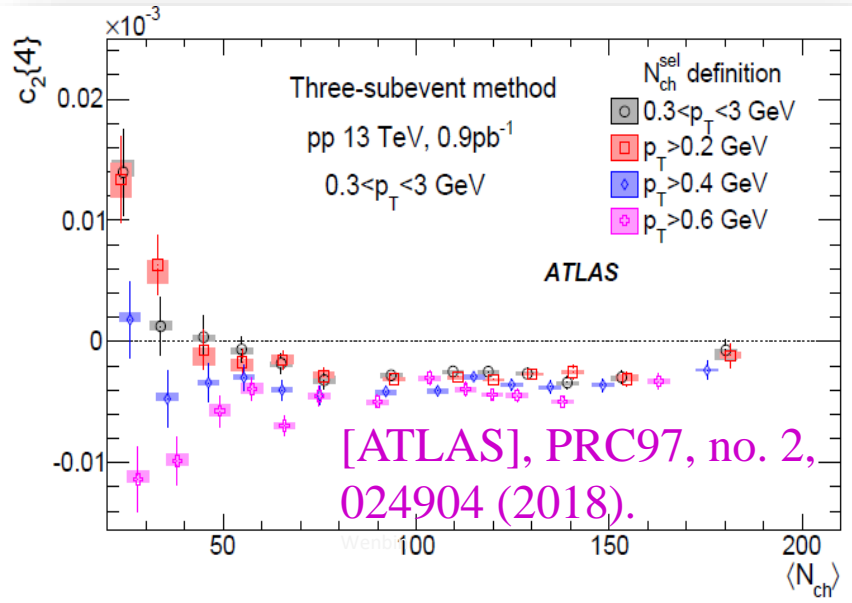
ATLAS



Due to non flow effects, $c_2\{4\}$ obtained by standard method strongly depend on N_{ch}^{sel} , even reversing the sign.

3 subevent cumulant can largely suppress the non-flow effects.

$C_2\{4\}$ obtained by 3-subevent weakly depend on N_{ch}^{sel} at larger $\langle N_{ch} \rangle$.

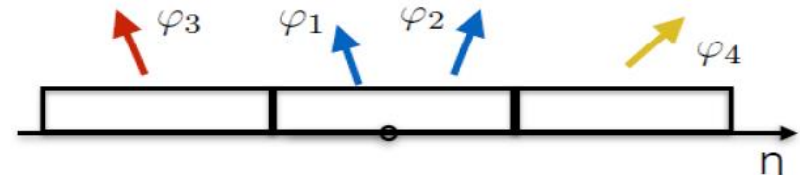


$$\langle\langle 4 \rangle\rangle_{3\text{sub}} = \langle\langle \cos n(\varphi_1 + \varphi_2 - \varphi_3 - \varphi_4) \rangle\rangle$$

$$\langle\langle 2 \rangle\rangle_{3\text{sub}}^2 = \langle\langle \cos n(\varphi_1 - \varphi_3) \rangle\rangle \langle\langle \cos n(\varphi_2 - \varphi_4) \rangle\rangle$$

$$\langle\langle 2 \rangle\rangle_{3\text{sub}}^2 = \langle\langle \cos n(\varphi_1 - \varphi_4) \rangle\rangle \langle\langle \cos n(\varphi_2 - \varphi_3) \rangle\rangle$$

$$c_n\{4\}_{3\text{sub}} = \langle\langle 4 \rangle\rangle_{3\text{sub}} - 2 \cdot \langle\langle 2 \rangle\rangle_{3\text{sub}}^2$$



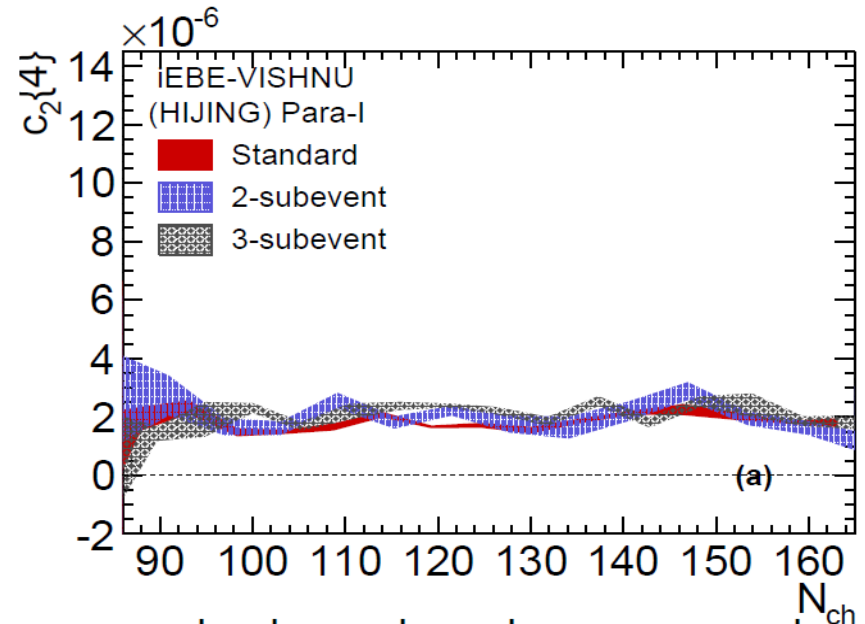
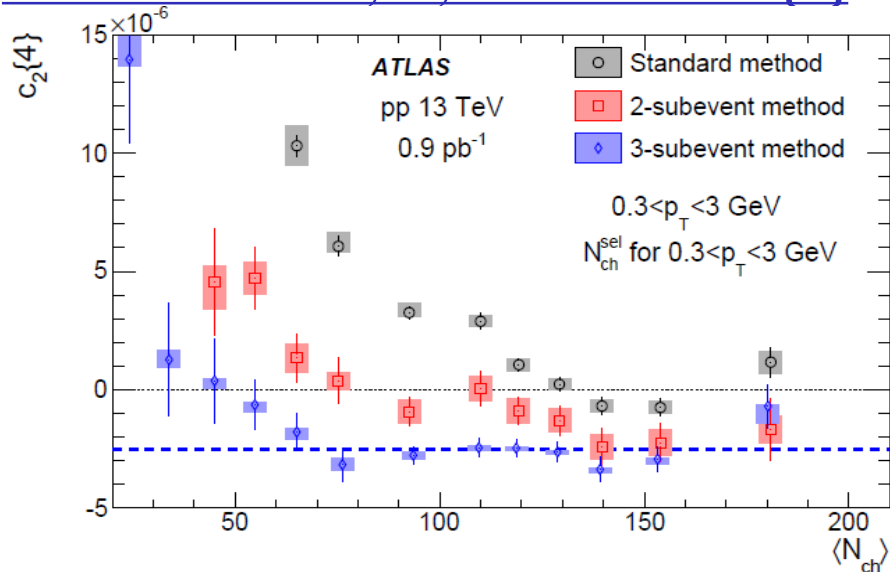
More details on $C_2\{4\}$ calculations

Minimize multiplicity fluctuations: (same method as used by ATLAS)

ATLAS-CONF-2017-002

- 1) Cut the multiplicity class with N_{ch}^{sel} within $0.3 < p_T < 3.0$ GeV, $|\eta| < 2.4$, calculate $c_2\{2\}$ & $c_2\{4\}$ for events with the same N_{ch}^{sel} to minimize multiplicity fluctuation.
- 2) Combined $c_2\{2\}$ & $c_2\{4\}$ of several N_{ch}^{sel} for the event ensemble.
- 3) Map the N_{ch}^{sel} to the common event activity measure N_{ch} with $p_T > 0.4$ GeV, $|\eta| < 2.4$ to compare with experiment data

Check standard, 2-, 3-subevent $C_2\{4\}$



In iEBE-VISHNU, no jets, non-flow mainly from resonance decays, standard method gives same results as 2- and 3- subevent methods.

coalescence model & NCQ scaling of v2

Coalescence model

$$\frac{dN_M}{d^3\mathbf{P}_M} = g_M \int d^3\mathbf{x}_1 d^3\mathbf{p}_1 d^3\mathbf{x}_2 d^3\mathbf{p}_2 f_q(\mathbf{x}_1, \mathbf{p}_1) f_{\bar{q}}(\mathbf{x}_2, \mathbf{p}_2) \times W_M(\mathbf{y}, \mathbf{k}) \delta^{(3)}(\mathbf{P}_M - \mathbf{p}_1 - \mathbf{p}_2)$$

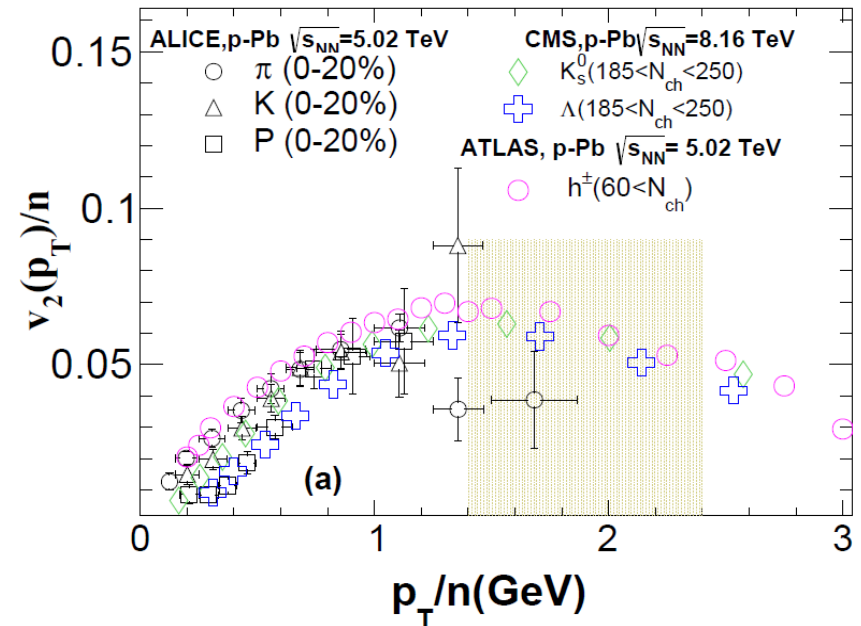
$$\begin{aligned} \frac{dN_B}{d^3\mathbf{P}_B} &= g_B \int d^3\mathbf{x}_1 d^3\mathbf{p}_1 d^3\mathbf{x}_2 d^3\mathbf{p}_2 d^3\mathbf{x}_3 d^3\mathbf{p}_3 f_{q_1}(\mathbf{x}_1, \mathbf{p}_1) \\ &\times f_{q_2}(\mathbf{x}_2, \mathbf{p}_2) f_{q_3}(\mathbf{x}_3, \mathbf{p}_3) W_B(\mathbf{y}_1, \mathbf{k}_1; \mathbf{y}_2, \mathbf{k}_2) \times \delta^{(3)}(\mathbf{P}_B - \mathbf{p}_1 - \mathbf{p}_2 - \mathbf{p}_3) \end{aligned}$$

Thermal & hard Partons:

- **Thermal partons** generated by hydro
- **Hard partons** generated by PYTHIA8, then suffered with energy loss by LBT

Coalescence processes:

- thermal - thermal parton coalescence
- thermal - hard parton coalescence
- hard - hard parton coalescence



Hydro-Coal-Frag Hybrid Model

Thermal hadrons (VISH2+1):

- generated by hydro.

with Cooper-Frye.

Meson: $P_T < 2P_1$; baryon: $P_T < 3P_1$.

Coalescence hadrons (Coal Model):

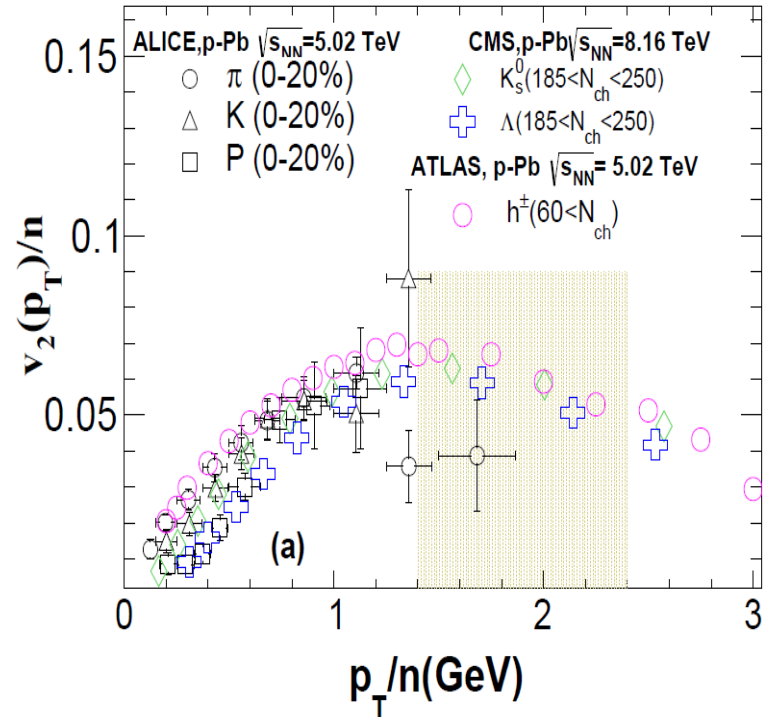
-generated by coalescences model including thermal-thermal, thermal-hard & hard-hard parton coalescence.

Fragmentation hadrons (LBT):

-the remnant hard quarks feed to fragmentation .

UrQMD afterburner:

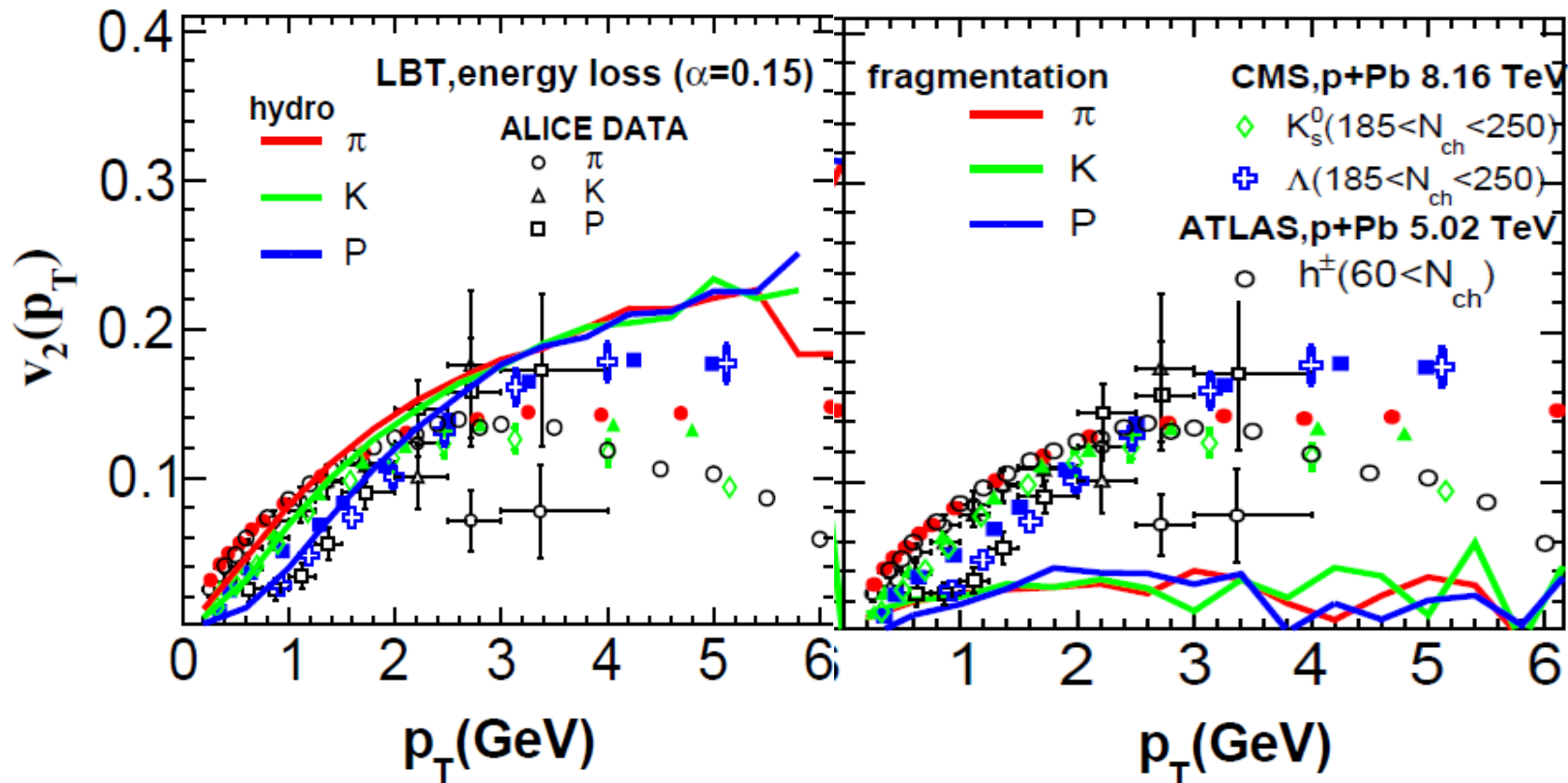
-All hadrons are feed into UrQMD for hadronic evolution, scatterings and decays



Zhao, Ko, Liu, Qin & Song,
Phys. Rev. Lett. 125 7 072301
(2020)

$v_2(p_T)$ from hydro or fragmentation alone

$p + \text{Pb} @ \sqrt{s_{NN}} = 5.02 \text{ TeV}, 0\text{-}20\%$



Hydro or Fragmentation alone can not describe $v_2(p_T)$ in high multiplicity p-Pb collisions