

# Non-equilibrium Attractors of QCD Kinetic Theory at Zero and Finite Density

**Xiaojian Du | Bielefeld University**

**Based on X. D, S. Schlichting**

**arXiv: 2012.09068 (attractor, phenomenology)**

**arXiv: 2012.09079 (QCD kinetic theory)**

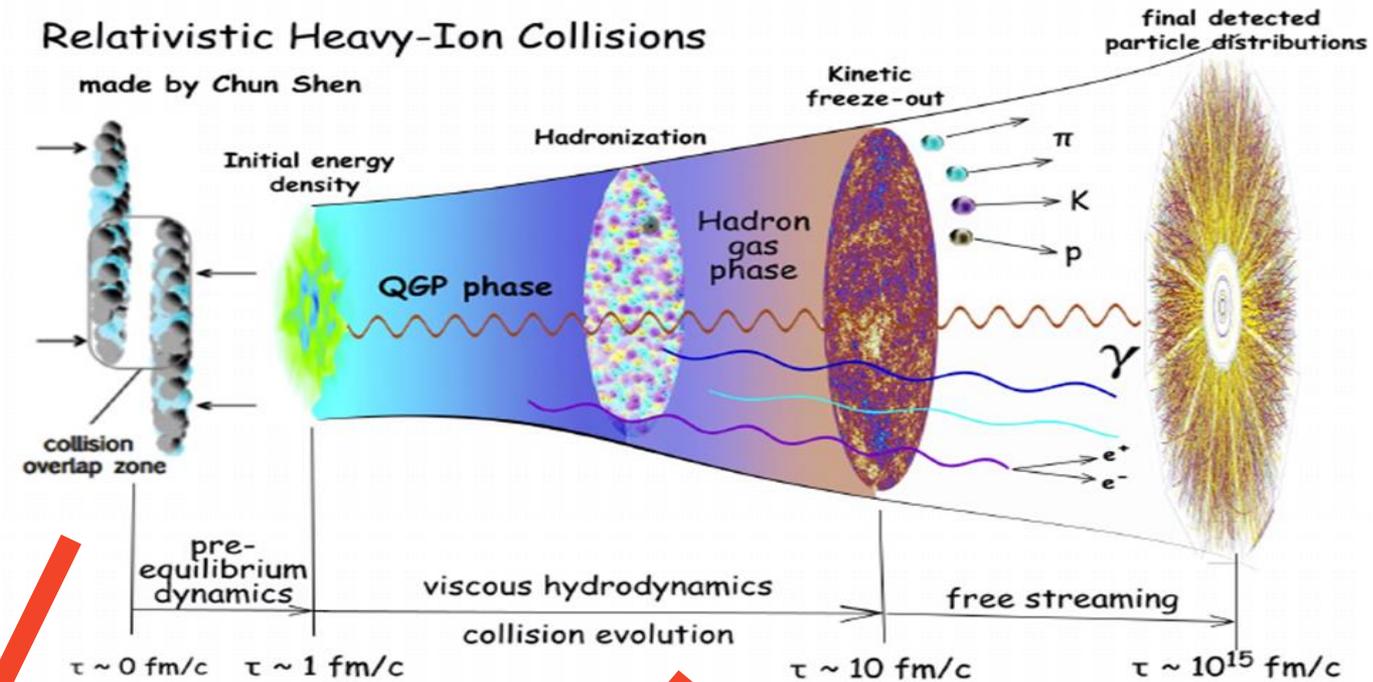
**Initial Stages 2021**

**Jan. 13, 2021**

**Weizmann Institute of Science, Israel [Online]**



# Pre-Equilibration Quark-Gluon Plasma



- Initial Collision
  - Off-Thermal
  - Gluon Saturation
- 
- Pre-Equilibrium QGP
  - Thermalization
  - Chemical Equilibration
- 
- Hydrodynamic
  - Thermal
  - Gluon/Quarks

# QCD Effective Kinetic Theory

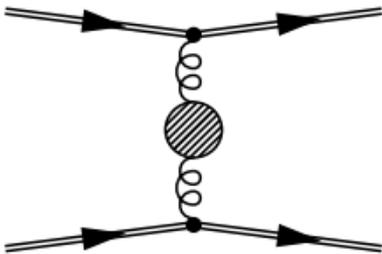
Effective Kinetic Theory (Arnold, Moore, Yaffe) at LO

AMY, JHEP01 (2003) 030  
 AMY, JHEP0206(2002)030  
 Kurkela, Mazeliauskas, PRD99 (2019) 054018

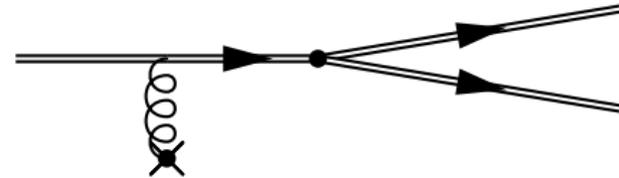
$$\left[ \frac{\partial}{\partial \tau} - \frac{p_{\parallel}}{\tau} \frac{\partial}{\partial p_{\parallel}} \right] f_a(\tau, p_T, p_{\parallel}) = -C_a^{2 \leftrightarrow 2}[f](\tau, p_T, p_{\parallel}) - C_a^{1 \leftrightarrow 2}[f](\tau, p_T, p_{\parallel})$$

Boltzmann equation for massless gluon and 3 light quarks/anti-quarks  $a = g, u, \bar{u}, d, \bar{d}, s, \bar{s}$

Including  $2 \leftrightarrow 2$  elastic processes and  $1 \leftrightarrow 2$  inelastic processes



$2 \leftrightarrow 2$ : Color screening by Debye mass fit to HTL calculation



$1 \leftrightarrow 2$ : Collinear radiation including LPM effect via effective vertex resummation

# Non-equilibrium evolution

System initially highly anisotropic with CGC inspired gluon dist. & finite baryon/charge density

Universal scaling variable: 1<sup>st</sup>-order hydrodynamics near equilibrium

$$\tilde{\omega} = \frac{(e+p)\tau}{4\pi\eta} \quad \frac{p_L}{e} = \frac{1}{3} - \frac{4}{9\pi} \underbrace{\left( \frac{\eta T_{\text{eff}}}{e+p} \right)}_{\text{const.}} \frac{4\pi}{\tau T_{\text{eff}}} \quad \longrightarrow \quad \frac{p_L}{e} = \frac{1}{3} - \frac{4}{9\pi\tilde{\omega}}$$

Larger  $\mu_B$ : slower isotropization:

Ineffectiveness of quark interaction

Spin degeneracy

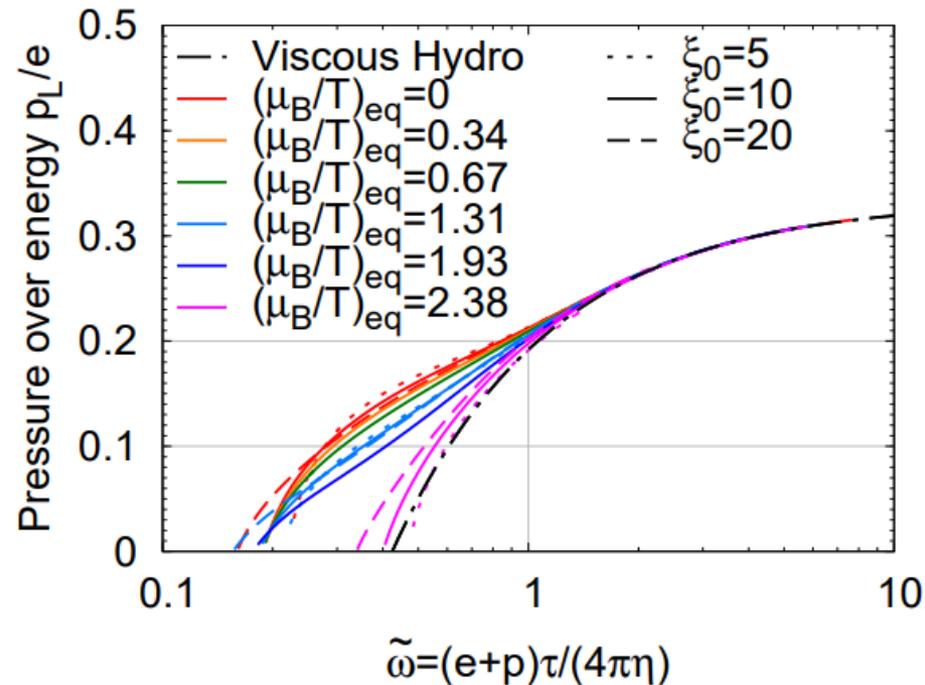
Quantum statistics

Non-equilibrium attractors from kinetic theory:

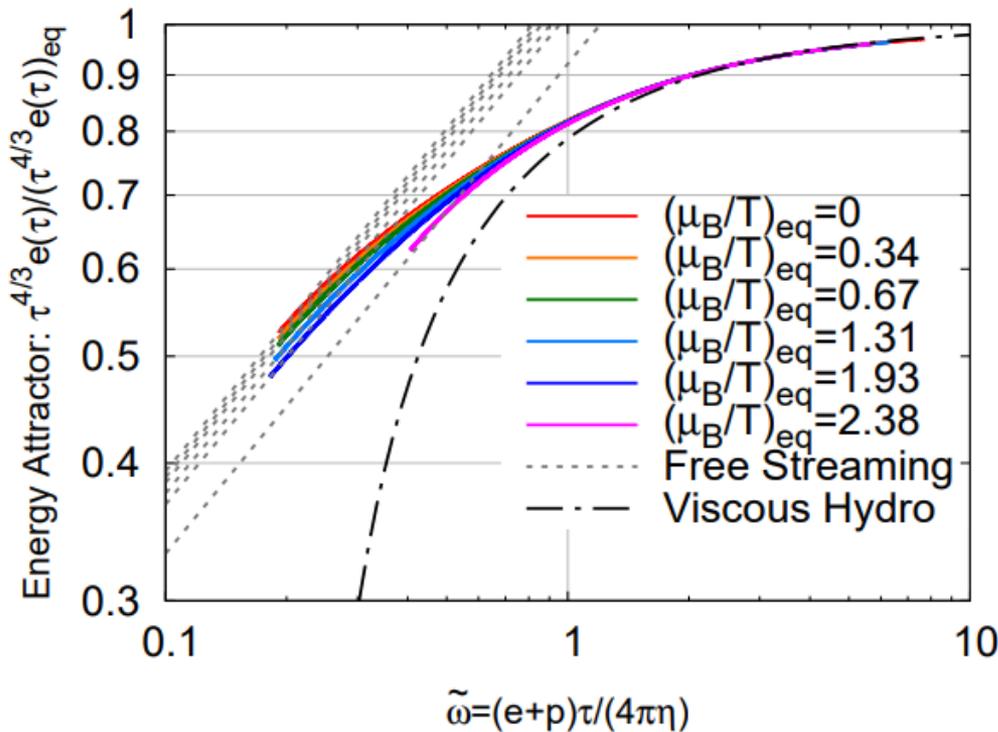
Effective constitutive relations (far-from equilibrium)

$$\frac{p_L}{e} = f(\tilde{\omega})$$

Isotropization later than hydrodynamization



# Connection to Hydrodynamics



Non-equilibrium attractor

$$\mathcal{E}\left(\tilde{\omega} = \left(\frac{e+p}{\eta T_{\text{eff}}}\right) \frac{\tau T_{\text{eff}}}{4\pi}\right) = \frac{\tau^{\frac{4}{3}} e}{\left(\tau^{\frac{4}{3}} e\right)_{\text{eq}}}$$

Asymptotes:

$$\mathcal{E}(\tilde{\omega} \gg 1) \simeq 1 - \frac{2}{3\pi\tilde{\omega}} \quad \text{Hydrodynamics}$$

$$\mathcal{E}(\tilde{\omega} \ll 1) \simeq C_{\infty}^{-1} \tilde{\omega}^{\frac{4}{9}} \quad \text{Free streaming}$$

Pre-equilibrium description connects initial state to hydrodynamics

$$\left(\tau^{\frac{4}{3}} e\right)_{\tilde{\omega}} = \left(4\pi \frac{\eta T_{\text{eff}}}{e+p}\right)^{\frac{4}{9}} \left(\frac{\pi^2 \nu_{\text{eff}}}{30}\right)^{\frac{1}{9}} \boxed{(e\tau)_0^{\frac{8}{9}}} C_{\infty} \mathcal{E}(\tilde{\omega})$$

$$(\tau \Delta n_f)_{\tilde{\omega}} = \boxed{(\tau \Delta n_f)_0}$$

Input to hydrodynamics through pre-equilibrium evolution

Giacalone, Mazeliauskas, Schlichting PRL 123(2019)26

# Phenomenological Consequence

In equilibrium:

Entropy:  $(s\tau)_{\text{eq}} = \frac{(e + p - \sum_f \mu_f \Delta n_f) \tau}{T}$  ←

Net Baryon Number:

$\Delta n_B = \frac{1}{3} \Delta n_u + \frac{1}{3} \Delta n_d$  ←

Fixed from experimental/lattice data

Charged particle multiplicity:

$\frac{dN_{ch}}{d\eta} \simeq \frac{N_{ch}}{JS} (\tau s)_{\text{eq}} S_T \simeq 0.12 (\tau s)_{\text{eq}} S_T$

Entropy per baryon:

$\frac{S}{N_B} = \left( \frac{\tau s}{\tau \Delta n_B} \right)_{\text{eq}}$



From non-equilibrium attractor:

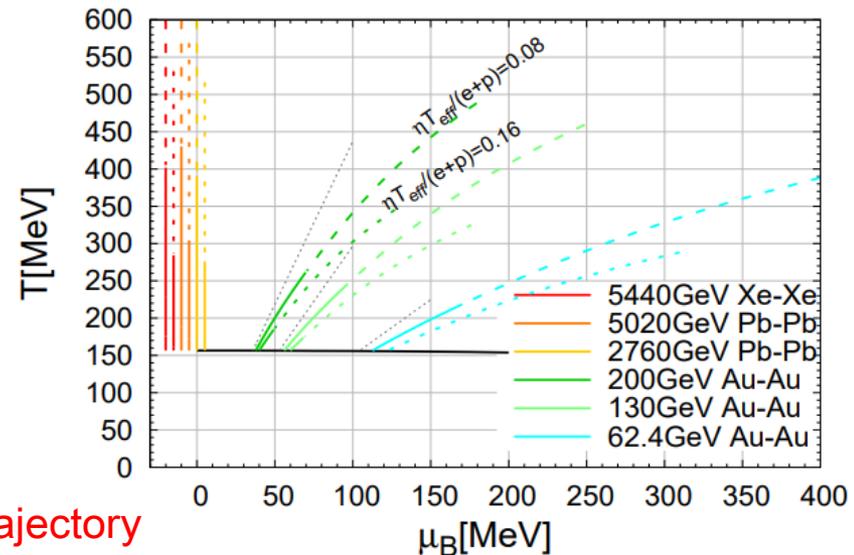
$(\tau^{\frac{4}{3}} e)_{\tilde{\omega}} = (4\pi \frac{\eta T_{\text{eff}}}{e+p})^{\frac{4}{9}} \left( \frac{\pi^2 \nu_{\text{eff}}}{30} \right)^{\frac{1}{9}} (e\tau)_0^{\text{c/nc}} C_{\infty} \mathcal{E}(\tilde{\omega})$   
 $(\tau \Delta n_f)_{\tilde{\omega}} = (\tau \Delta n_f)_0$



From Landau matching:  
Time-dependent  $T$  and  $\mu$



Non-equilibrium trajectory  
to higher baryon density



# Conclusion and Outlook

⇒ Theoretical and phenomenological consequence:

- Non-equilibrium **effective constitutive relation** from QCD kinetic theory
  - Before hydrodynamic regime
- **Trajectory of pre-equilibrium QGP** in T-μ diagram
  - Before hydrodynamic regime
- **Applicable time and temperature** for hydrodynamics
  - By fixing scales from experiments/IQCD

$$\tau \simeq 1.3 \text{ fm}/c \left( \frac{4\pi\eta/s}{2} \right)^{\frac{3}{2}} \left( \frac{dN_{ch}/d\eta}{1942} \right)^{-\frac{1}{2}} \left( \frac{S_{\perp}}{138\text{fm}^2} \right)^{\frac{1}{2}}$$

$$T \simeq 300\text{MeV} \left( \frac{4\pi\eta/s}{2} \right)^{-\frac{1}{2}} \left( \frac{dN_{ch}/d\eta}{1942} \right)^{\frac{1}{2}} \left( \frac{S_{\perp}}{138\text{fm}^2} \right)^{-\frac{1}{2}}$$

⇒ Application:

- pre-equilibrium di-lepton production
  - See talks by Maurice Coquet on Tuesday

