

The effect of the equation of state on η/s of strongly interacting matter

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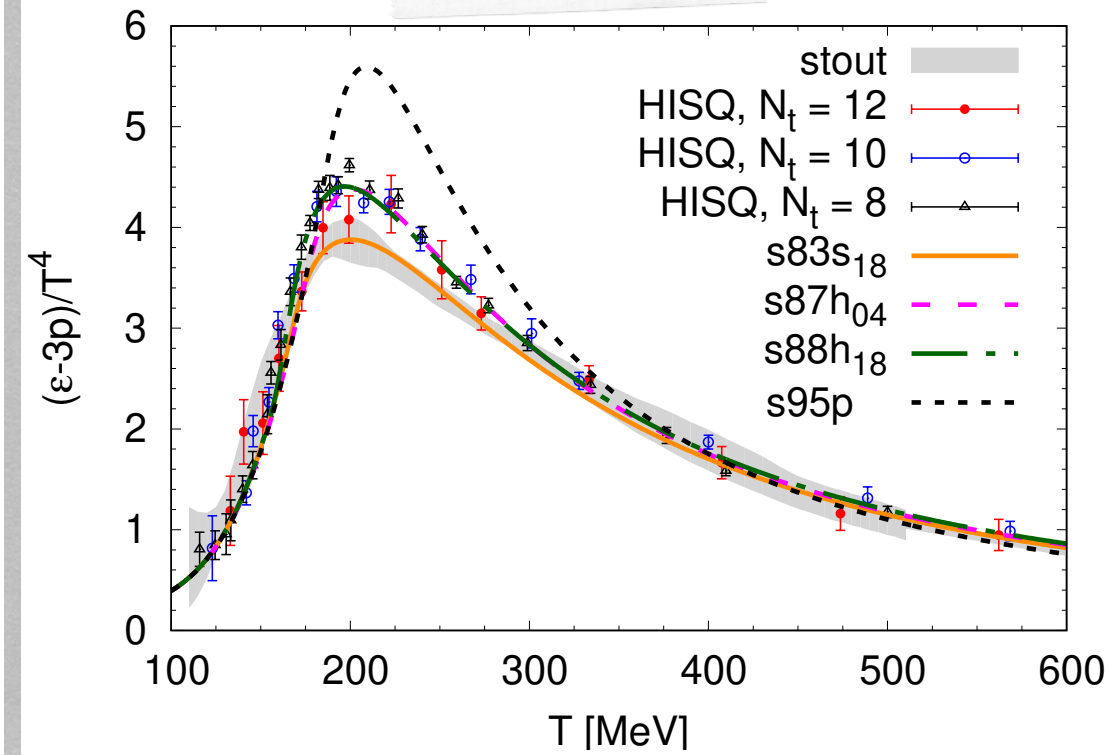
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1. Three new equations of state

- Serve as updates for the well-known **s95p** EoS [1]
- Match hadron resonance gas at low T , lattice data at high T
- Each parametrization uses different PDG summary tables for HRG and/or different lattice data, labeled as “stout” or “HISQ” based on the discretization scheme

Name	PDG	Lattice data
s83s18	2018	stout [2]
s87h04	2004	HISQ [3]
s88h18	2018	HISQ [3]



Trace anomaly comparison

3. Modeling the heavy ion collision

Initial energy density from the EKRT minijet saturation model [5]:

$$\epsilon(\vec{r}_T, \tau_s(\vec{r}_T)) = \frac{K_{\text{sat}}}{\pi} [p_{\text{sat}}(\vec{r}_T, K_{\text{sat}})]^4; \tau_s(\vec{r}_T) = 1/p_{\text{sat}}(\vec{r}_T, K_{\text{sat}})$$

For each centrality class, produce a number of energy density profiles, convert to entropy density via EoS, and average over events

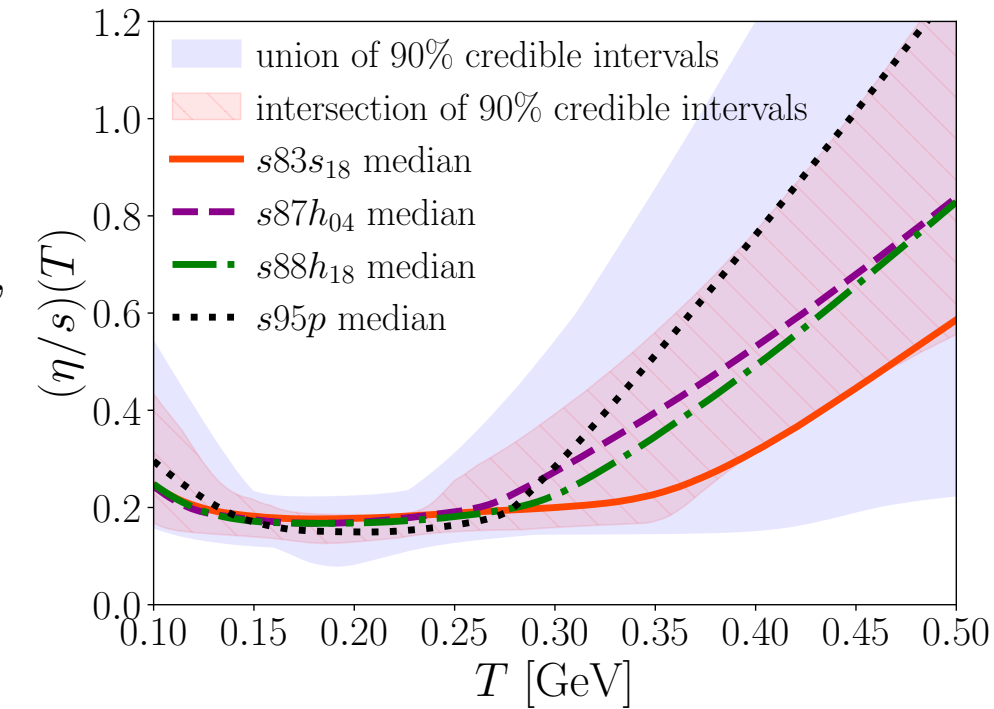
2+1D viscous hydrodynamics [6] with a temperature dependent shear viscosity coefficient η/s

$$(\eta/s)(T) = S_{\text{HG}}(T_{\text{H}} - T) + (\eta/s)_{\text{min}}, T < T_{\text{H}}$$

$$(\eta/s)(T) = (\eta/s)_{\text{min}}, T_{\text{H}} \leq T \leq T_{\text{H}} + W_{\text{min}}$$

$$(\eta/s)(T) = S_{\text{QGP}}(T - T_{\text{H}} - W_{\text{min}}) + (\eta/s)_{\text{min}}, T > T_{\text{H}} + W_{\text{min}}$$

Kinetic decoupling temperature T_{dec} and chemical freeze-out temperature T_{chem} are also adjustable parameters



Uncertainties of $(\eta/s)(T)$

2. Bayesian analysis with Gaussian process emulator

Model input (parameters): $\vec{x} = (x_1, \dots, x_n)$ [$K_{\text{sat}}, (\eta/s)_{\text{min}}, T_{\text{H}}, W_{\text{min}}, S_{\text{HG}}, S_{\text{QGP}}, T_{\text{dec}}, T_{\text{chem}}$]

Model output $\vec{y} = (y_1, \dots, y_m) \Leftrightarrow$ Experimental values \vec{y}^{exp} [$dN/dy, \langle p_T \rangle, v_2$]

Bayes' theorem: Posterior probability \propto Likelihood \cdot Prior knowledge

Prior knowledge: Range of input parameter values to investigate

Likelihood: $\mathcal{L}(\vec{x}) \propto \exp(-\frac{1}{2}(\vec{y}(\vec{x}) - \vec{y}^{\text{exp}})\Sigma^{-1}(\vec{y}(\vec{x}) - \vec{y}^{\text{exp}})^T)$

where Σ is the covariance matrix representing the uncertainties

Use Gaussian Process (GP) emulator to quickly estimate $\vec{y}(\vec{x})$:

We establish a GP covariance matrix $\mathcal{C}_{A,B} = \{c(\vec{a}, \vec{b})\}$, $\vec{a} \in A, \vec{b} \in B$,

by defining the covariance function

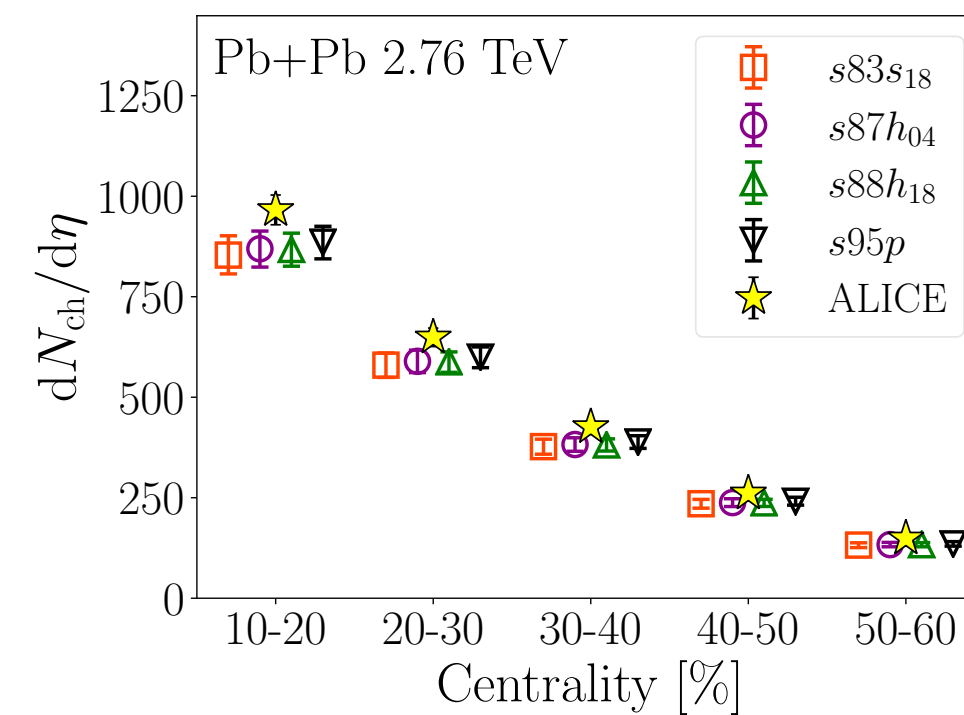
$$c(\vec{a}, \vec{b}) = \theta_0 \exp\left(-\sum_{i=1}^n \frac{(a_i - b_i)^2}{2\theta_i^2}\right) + \theta_{\text{noise}}\delta_{\vec{a}\vec{b}}.$$

Knowing a set of model outputs U for a set of parameter combinations T ,

we can derive the GP conditional predictive mean and the associated

covariance as $y^{\text{GP}}(\vec{x}_0) = \mathcal{C}_{0,T}\mathcal{C}_{T,T}^{-1}U$; $\sigma^{\text{GP}}(\vec{x}_0)^2 = \mathcal{C}_{0,0} - \mathcal{C}_{0,T}\mathcal{C}_{T,T}^{-1}\mathcal{C}_{T,0}$

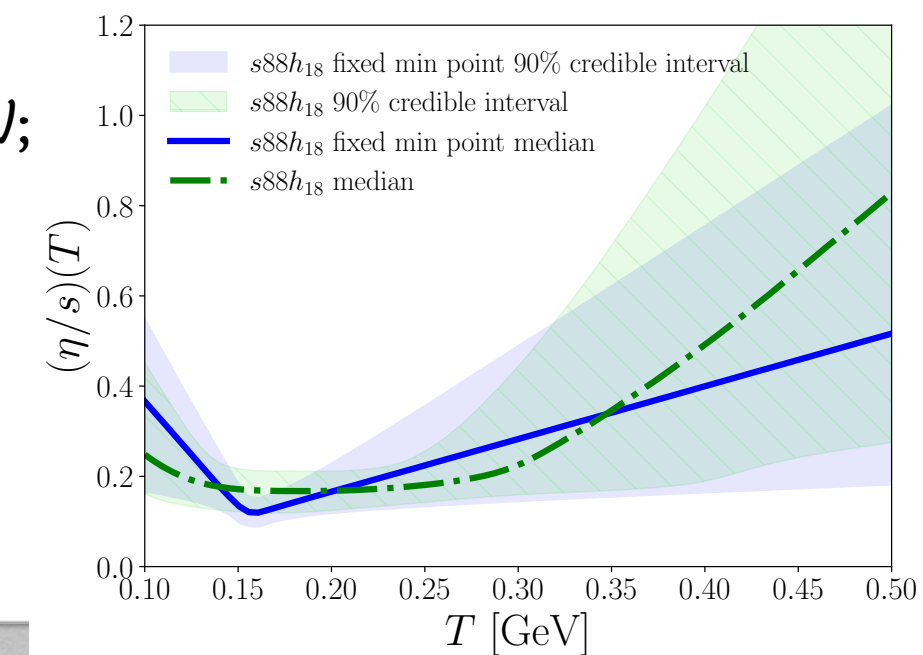
Similar to [4], we use Markov chain Monte Carlo to sample the posterior probability: Random walk in input parameter space, constrained by the prior



Emulator estimates for posterior samples

4. Summary of the results

- **Tightest constraints on η/s in the temperature range $T \approx 150$ -- 220 MeV; η/s approximately constant in this interval**
- **Accounting for all four EoSs: $0.08 < \eta/s < 0.23$**
- **Only s83s18 and s88h18: $0.12 < \eta/s < 0.23$**
- **Restricting the η/s minimum to a point leads to a smaller minimum value**
- **Differences due to equations of state within uncertainties**



Minimum point vs. plateau

References

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