Baryon-to-meson Transition Distribution Amplitudes: basic properties, physical interpretation and experimental perspectives

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# Outline

- Introduction: Forward and backward kinematical regimes, DAs, GPDs, TDAs;
- Baryon-to-meson TDAs: definition and properties;
- O Physical contents of baryon-to-meson TDAs;
- Current status of experimental analysis at JLab;
- **5** Summary and Outlook.

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In collaboration with:
B. Pire, L. Szymanowski,
and
K. Park, W. Li, G. Huber, S. Diehl, M. Zambrana, B. Ramstein, E. Atomssa.
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#### Factorization regimes for hard meson production I

J. Collins, L. Frankfurt and M. Strikman'97: the collinear factorization theorem for

$$\gamma^*(q) + N(p) \rightarrow N(p') + M(p_M)$$

in the generalized Bjorken limit

$$-q^2 = Q^2, W^2 - \text{large}; x_B = \frac{Q^2}{2p \cdot q} - \text{fixed}; -t = -(p'-p)^2 - \text{small}.$$

- Description in terms of nucleon GPDs and meson DAs.
- A complementary factorization regime:

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Hard exclusive pseudoscalar meson electroproduction and spin structure of the nucleon

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### Factorization regimes for hard meson production II

#### Two complementary regimes in generalized Bjorken limit :

- $t \sim 0$  (near-forward kinematics): GPDs and meson DAs;
- $u \sim 0$  (near-backward kinematics): baryon-to-meson TDAs and nucleon DAs B. Pire, L. Szymanowski'05;



# GPDs, DAs and TDAs

• Quark-antiquark bilinear light-cone  $(z^2 = 0)$  operator:

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\langle A|\bar{\Psi}(0)[0;z]\Psi(z)|B\rangle
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 $\Rightarrow$  PDFs, meson DAs, GPDs, transition GPDs, etc.

• Three-quark trilinear light-cone  $(z_i^2 = 0)$  operator:

 $\langle A|\Psi(z_1)[z_1;z_2]\Psi(z_2)[z_2;z_3]\Psi(z_3)[z_3;z_1]|B\rangle$ 

- $\langle A| = \langle 0|; |B\rangle$  baryon;  $\Rightarrow$  baryon DAs.
- Let  $\langle A |$  be a meson state  $(\pi, \eta, \rho, \omega, ...) | B \rangle$  baryon  $\Rightarrow$  baryon-to-meson TDAs.

TDAs have common features with:

- baryon DAs: same operator;
- GPDs:  $\langle B |$  and  $|A \rangle$  are not of the same momenta  $\Rightarrow$  skewness

$$\xi = -\frac{(p_A - p_B) \cdot n}{(p_A + p_B) \cdot n}.$$

TDAs are universal non-perturbative objects with known evolution properties.

# Nucleon e.m. FF: a well known examples

#### A word of caution:



# Nucleon e.m. FF in pQCD at leading order

- S. Brodsky & P. Lepage'81 A. Efremov &
- A. Radyushkin'80



# A list of questions:

- What are the properties and physical contents of baryon-to-meson TDAs?
- Can we build models for baryon-to-meson TDAs?
- Can we access backward reactions experimentally?
- What are the marking signs for the onset of the collinear factorization regime?
- What new information can we get about hadrons?

# Leading twist proton-to- $\pi^0$ TDAs

J.P.Lansberg, B.Pire, L.Szymanowski and K.S.'11  $(n^2 = p^2 = 0; 2p \cdot n = 1; \text{LC gauge } A \cdot n = 0)$ .

- 8 TDAs:  $H^{\pi N}(x_1, x_2, x_3, \xi, \Delta^2, \mu^2) \equiv \{V_i^{\pi N}, A_i^{\pi N}, T_i^{\pi N}\}(x_1, x_2, x_3, \xi, \Delta^2, \mu^2)$ • *C.f.* 3 leading twist nucleon DAs:  $\{V^p, A^p, T^p\}(y_1, y_2, y_3)$ 
  - $$\begin{split} 4(P \cdot n)^{3} &\int \left[\prod_{k=1}^{3} \frac{dz_{k}}{2\pi} e^{i x_{k} z_{k}(P \cdot n)}\right] \langle \pi^{0}(p_{\pi})| \varepsilon_{c_{1}c_{2}c_{3}} u_{\rho}^{c_{1}}(z_{1}n) u_{\tau}^{c_{2}}(z_{2}n) d_{\chi}^{c_{3}}(z_{3}n) | N^{p}(p_{1},s_{1}) \rangle \\ &= \delta(2\xi x_{1} x_{2} x_{3}) i \frac{f_{N}}{f_{\pi}M} \\ &\times \left[V_{1}^{\pi N}(\hat{P}C)_{\rho \tau}(\hat{P}U)_{\chi} + A_{1}^{\pi N}(\hat{P}\gamma^{5}C)_{\rho \tau}(\gamma^{5}\hat{P}U)_{\chi} + T_{1}^{\pi N}(\sigma_{P\mu}C)_{\rho \tau}(\gamma^{\mu}\hat{P}U)_{\chi} \\ &+ V_{2}^{\pi N}(\hat{P}C)_{\rho \tau}(\hat{\Delta}U)_{\chi} + A_{2}^{\pi N}(\hat{P}\gamma^{5}C)_{\rho \tau}(\gamma^{5}\hat{\Delta}U)_{\chi} + T_{2}^{\pi N}(\sigma_{P\mu}C)_{\rho \tau}(\gamma^{\mu}\hat{\Delta}U)_{\chi} \\ &+ \frac{1}{M}T_{3}^{\pi N}(\sigma_{P\Delta}C)_{\rho \tau}(\hat{P}U)_{\chi} + \frac{1}{M}T_{4}^{\pi N}(\sigma_{P\Delta}C)_{\rho \tau}(\hat{\Delta}U)_{\chi} \Big] \end{split}$$

• 
$$P = \frac{p_1 + p_\pi}{2}; \Delta = (p_\pi - p_1); \sigma_{P\mu} \equiv P^{\nu} \sigma_{\nu\mu};$$
  
 $\xi = -\frac{\Delta \cdot n}{2P \cdot n}$ 

- C: charge conjugation matrix;
- $f_N = 5.2 \cdot 10^{-3} \text{ GeV}^2$  (V. Chernyak and A. Zhitnitsky'84);



# A list of fundamental properties I:

B. Pire, L.Szymanowski, KS'10,11:

• Restricted support in  $x_1$ ,  $x_2$ ,  $x_3$ : intersection of three stripes  $-1 + \xi \le x_k \le 1 + \xi$ ( $\sum_k x_k = 2\xi$ ); ERBL-like and DGLAP-like I, II domains.



• Mellin moments in  $x_k \Rightarrow \pi N$  matrix elements of local 3-quark operators

$$\left[i\vec{D}^{\mu_1}\dots i\vec{D}^{\mu_{n_1}}\Psi_{\rho}(0)\right]\left[i\vec{D}^{\nu_1}\dots i\vec{D}^{\nu_{n_2}}\Psi_{\tau}(0)\right]\left[i\vec{D}^{\lambda_1}\dots i\vec{D}^{\lambda_{n_3}}\Psi_{\chi}(0)\right].$$

Need to be studied on the lattice!

• Polynomiality in  $\xi$  of the Mellin moments in  $x_k$ :

$$\int_{-1+\xi}^{1+\xi} dx_1 dx_2 dx_3 \delta(\sum_k x_k - 2\xi) x_1^{n_1} x_2^{n_2} x_3^{n_3} H^{\pi N}(x_1, x_2, x_3, \xi, \Delta^2)$$

= [Polynomial of order  $n_1 + n_2 + n_3\{+1\}](\xi)$ .

## A list of fundamental properties II:

• Spectral representation A. Radyushkin'97 generalized for  $\pi N$  TDAs ensures polynomiality and support:

$$\begin{split} & \mathcal{H}(x_{1}, x_{2}, x_{3} = 2\xi - x_{1} - x_{2}, \xi) \\ &= \left[\prod_{i=1}^{3} \int_{\Omega_{i}} d\beta_{i} d\alpha_{i}\right] \delta(x_{1} - \xi - \beta_{1} - \alpha_{1}\xi) \,\delta(x_{2} - \xi - \beta_{2} - \alpha_{2}\xi) \\ &\times \delta(\beta_{1} + \beta_{2} + \beta_{3}) \delta(\alpha_{1} + \alpha_{2} + \alpha_{3} + 1) F(\beta_{1}, \beta_{2}, \beta_{3}, \alpha_{1}, \alpha_{2}, \alpha_{3}); \end{split}$$

- Ω<sub>i</sub>: {|β<sub>i</sub>| ≤ 1, |α<sub>i</sub>| ≤ 1 − |β<sub>i</sub>|} are copies of the usual DD square support;
  F(...): six variables that are subject to two constraints ⇒ quadruple distributions;
- Can be supplemented with a D-term-like contribution (with pure ERBL-like support):

$$\frac{1}{(2\xi)^2} \delta(x_1 + x_2 + x_3 - 2\xi) \left[ \prod_{k=1}^3 \theta(0 \le x_k \le 2\xi) \right] D\left( \frac{x_1}{2\xi}, \frac{x_2}{2\xi}, \frac{x_3}{2\xi} \right).$$

# **TDAs and light-cone wave functions**

• Light-front quantization approach:  $\pi N$  TDAs provide information on next-to-minimal Fock components of light-cone wave functions of hadrons B. Pasquini et al. 2009:



# A connection to the quark-diquark picture I



- $\varphi_{\rm as}(x) = 120x_1x_2x_3$ .
- V. Chernyak, Zhitnitsky'84:

$$\varphi_{\rm CZ}(x) = \varphi_{\rm as}(x) \sum_i c_i A_i(x).$$

• Large asymmetry between quarks in nucleon:

$$\varphi^{(1,0,0)} \simeq 0.6; \ \varphi^{(0,1,0)} \simeq \varphi^{(0,0,1)} \simeq 0.2.$$

• Z. Dziembowski, J. Franklin'90: diquark-like clustering

$$p:\uparrow\downarrow\uparrow$$
  $\underbrace{ud\uparrow\downarrow}$   $u\uparrow$ .

• No confirmation of asymmetric behavior: e.g. V. Braun, A. Lenz, M. Wittmann'06 .

# A connection to the quark-diquark picture II

• Quark-diquark coordinates (one of 3 possible sets):

$$v_3 = rac{x_1 - x_2}{2}; \ w_3 = x_3 - \xi; \ x_1 + x_2 = 2\xi_3'; \ \left(\xi_3' \equiv rac{\xi - w_3}{2}\right).$$

• The TDA support in quark-diquark coordinates:

$$-1 \le w_3 \le 1; \quad -1 + \left| \xi - \xi_3' 
ight| \le v_3 \le 1 - \left| \xi - \xi_3' 
ight|$$

•  $v_3$ -Mellin moment of  $\pi N$  TDAs:

$$\int_{-1+|\xi-\xi'_{3}|}^{1-|\xi-\xi'_{3}|} dv_{3}H^{\pi N}(w_{3}, v_{3}, \xi, \Delta^{2})$$

$$\sim h_{\rho\tau\chi}^{-1} \int \frac{d\lambda}{4\pi} e^{i(w_{3}\lambda)(P\cdot n)} \langle \pi^{0}(p_{\pi})| \underbrace{u_{\rho}(-\frac{\lambda}{2}n)u_{\tau}(-\frac{\lambda}{2}n)d_{\chi}(\frac{\lambda}{2}n)}_{\hat{\mathcal{O}}_{\rho\tau\chi}^{\{uu\}d}(-\frac{\lambda}{2}n, \frac{\lambda}{2}n)} |N^{\rho}(p_{1})\rangle$$

#### An interpretation in the impact parameter space I

- A generalization of M. Burkardt'00,02; M. Diehl'02 for v<sub>3</sub>-integrated TDAs.
- Fourier transform with respect to

$$\mathbf{D} = rac{\mathbf{p}_{\pi}}{1-\xi} - rac{\mathbf{p}_{N}}{1+\xi}; \quad \Delta^{2} = -2\xi \left(rac{m_{\pi}^{2}}{1-\xi} - rac{M_{N}^{2}}{1+\xi}
ight) - (1-\xi^{2})\mathbf{D}^{2}.$$

• A representation in the DGLAP-like I domain:



# An interpretation in the impact parameter space II



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# Building up a consistent model for $\pi N$ TDAs

Key requirements:

- support properties in x<sub>k</sub> and polynomialty;
- isospin + permutation symmetry;
- **3** crossing  $\pi N$  TDA  $\leftrightarrow \pi N$  GDA;
- Soft pion theorem P. Pobylitsa, M. Polyakov and M. Strikman'01; V. Braun, D. Ivanov, A. Lenz, A. Peters'08:  $\pi N$  GDA at the threshold  $\xi = 1$ ,  $\Delta^2 = M^2$  in terms of nucleon DAs.

#### How to model quadruple distributions?

- No enlightening  $\xi = 0$  limit as for GPDs ( *cf.* RDDA A. Radyushkin'97
- Instead,  $\xi \rightarrow 1$  fixed from the soft pion theorem;
- A factorized Ansatz with input at  $\xi = 1$  designed in J.P. Lansberg, B. Pire, K.S., L. Szymanowski'12
- Cross-channel exchange as a source of the *D*-term-like contribution:  $\tilde{E}$  GPD v.s. TDA



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#### Calculation of the amplitude

• LO amplitude for  $\gamma^* + N^p \rightarrow \pi^0 + N^p$ computed as in J.P. Lansberg, B. Pire and L. Szymanowski'07;



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• 21 diagrams contribute;

$$\mathcal{I} \sim \int_{-1+\xi}^{1+\xi} d^3x \delta(x_1 + x_2 + x_3 - 2\xi) \, \int_0^1 d^3y \delta(1 - y_1 - y_2 - y_3) \left(\sum_{lpha=1}^{21} R_lpha
ight)$$

Each  $R_{\alpha}$ , has the structure:

 $R_{\alpha} \sim K_{\alpha}(x_1, x_2, x_3) \times Q_{\alpha}(y_1, y_2, y_3) \times$ [combination of  $\pi N$  TDAs] × [combination of nucleon DAs]

$$R_{1} = \frac{q^{u}(2\xi)^{2}[(V_{1}^{\rho\pi^{0}} - A_{1}^{\rho\pi^{0}})(V^{\rho} - A^{\rho}) + 4T_{1}^{\rho\pi^{0}}T^{\rho} + 2\frac{\Delta_{T}^{2}}{M^{2}}T_{4}^{\rho\pi^{0}}T^{\rho}]}{(2\xi - x_{1} + i\epsilon)^{2}(x_{3} + i\epsilon)(1 - y_{1})^{2}y_{3}}$$

c.f. 
$$\int_{-1}^{1} dx \frac{H(x,\xi)}{x \pm \xi \mp i\epsilon} \int_{0}^{1} dy \frac{\phi_{M}(y)}{y} \text{ for HMP}$$

# $N\gamma^* ightarrow \pi N$ amplitude and the cross section

•  $N\gamma^* \rightarrow \pi N$  helicity amplitudes:

$$\mathcal{M}_{s_1s_2}^{\lambda} = -i \frac{(4\pi\alpha_s)^2 \sqrt{4\pi\alpha_{em}} f_N^2}{54f_{\pi}} \frac{1}{Q^4} \Big[ \mathcal{S}_{s_1s_2}^{\lambda} \mathcal{I}(\xi, \Delta^2) - \mathcal{S'}_{s_1s_2}^{\lambda} \mathcal{I'}(\xi, \Delta^2) \Big],$$

where  $S_{s_1s_2}^{\lambda} \equiv \bar{U}(p_2, s_2)\hat{\epsilon}^*(\lambda)\gamma_5 U(p_1, s_1); \quad S_{s_1s_2}' \equiv \frac{1}{M}\bar{U}(p_2, s_2)\hat{\epsilon}^*(\lambda)\hat{\Delta}_T \gamma_5 U(p_1, s_1),$ • Unpolarized cross section for hard leptoproduction of a pion off nucleon:

$$\frac{d^{5}\sigma}{dE'd\Omega_{e'}d\Omega_{\pi}} = \Gamma \times \frac{\Lambda\left(s, m^{2}, M^{2}\right)}{128\pi^{2}s\left(s - M^{2}\right)} \times \sum_{s_{1}, s_{2}} \left\{ \frac{1}{2} \left( \left| \mathcal{M}_{s_{1}s_{2}}^{1} \right|^{2} + \left| \mathcal{M}_{s_{1}s_{2}}^{-1} \right|^{2} \right) + \ldots \right\} = \Gamma \times \left( \frac{d^{2}\sigma_{T}}{d\Omega_{\pi}} + \ldots \right).$$

#### Distinguishing features of the TDA-based mechanism

- Dominance of the transverse cross section  $\frac{d^2 \sigma_T}{d\Omega_{\pi}}$ .
- $1/Q^8$  scaling behavior of the cross section.
- $\bullet\,$  Non-zero imaginary part of the amplitude. Transverse Target Single Spin Asymmetry  $\sim\,$  Im part of the amplitude

# Backward pion electroproduction @ CLAS I



• Analysis of JLab @ 6 GeV data (Oct.2001-Jan.2002 run) for the backward  $\gamma^* p \rightarrow \pi^+ n$ K. Park et al. (CLAS Collaboration) and B. Pire and K.S., PLB 780 (2018)



# Backward pion electroproduction @ CLAS II



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# Backward pion electroproduction @ CLAS III

S. Diehl et al. (CLAS collaboration), analysis approved by the collaboration.

The cross section can be expressed as

$$\frac{d^{4}\sigma}{dQ^{2}dx_{B}d\varphi dt} = -\sigma_{0} \cdot \left(1 + A_{UU}^{\cos(2\varphi)} \cdot \cos(2\varphi) + A_{UU}^{\cos(\varphi)} \cdot \cos(\varphi) + A_{LU}^{\sin(\varphi)} \cdot \sin(\varphi)\right).$$

Beam Spin Asymmetry

$$BSA(Q^2, x_B, -t, \varphi) = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} = \frac{A_{LU}^{\sin(\varphi)} \cdot \sin(\varphi)}{1 + A_{UU}^{\cos(\varphi)} \cdot \cos(\varphi) + A_{UU}^{\cos(2\varphi)} \cdot \cos(2\varphi)};$$

•  $\sigma^{\pm}$  is the cross-section with the beam helicity states (±).



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# Backward pion electroproduction @ CLAS IV

 Beam Spin Asymmetry is a subleading twist effect both in the forward and backward regimes.



# Backward $\omega$ -production at JLab Hall C I

- A generalization of the TDA formalism for the case of light vector mesons ( $\rho$ ,  $\omega$ ,  $\phi$ ) B. Pire, L. Szymanowski and K.S'15.
- The analysis W. Li, G. Huber et al. (The JLab F<sub>π</sub> Collaboration) and B. Pire, L. Szymanowski, J.-M. Laget and K.S., PRL 123 (2019).
- Clear signal from backward regime of  $ep \rightarrow e' p\omega$ .



• Full Rosenbluth separation:  $\sigma_{\rm T}$  and  $\sigma_{\rm L}$  extracted.

$$2\pi \frac{d^2\sigma}{dtd\phi} = \frac{d\sigma_{\rm T}}{dt} + \epsilon \frac{d\sigma_{\rm L}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \frac{d\sigma_{\rm LT}}{dt} \cos\phi + \epsilon \frac{d\sigma_{\rm TT}}{dt} \cos 2\phi$$

# Backward $\omega$ -production at JLab Hall C II

• For  $Q^2=2.45~{
m GeV^2}$ :  $\sigma_{
m L}/\sigma_{
m T}<\mu^2/Q^2$  and  $\sigma_{
m T}\gg\sigma_{
m L}$ ;



- Experiment v.s. the predictions of the cross-channel nucleon exchange model for  $p \rightarrow \omega$  TDAs.
- Combined (CLAS and  $F_{\pi}$ -2 data for  $\gamma^* p \rightarrow \omega p$ ).
- TDA-based predictions v.s. the Regge-based J.M. Laget's JML'18 model.

# Baryon to meson TDAs at PANDA





• J.P. Lansberg et al.'12; B. Pire, L. Szymanowski, KS,'13:  $\pi N$  TDAs occur in factorized description of

$$ar{N} + N 
ightarrow \gamma^*(q) + \pi 
ightarrow \ell^+ + \ell^- + \pi;$$
  
 $ar{N} + N 
ightarrow J/\psi + \pi 
ightarrow \ell^+ + \ell^- + \pi;$ 

- Two regimes (forward and backward). C invariance ⇒ perfect symmetry;
- Test of universality of TDAs;

•  $(1 + \cos^2 \theta_{\ell})$  distribution marks the reaction mechanism: transverse polarization dominance (leading twist accuracy).



• M. C. Mora Espi, M. Zambrana, F. Maas, K.S.'15: feasibility of  $\bar{p}p \rightarrow e^+e^-\pi^0$ .

• B. Ramstein, E. Atomssa and PANDA collaboration and K.S., PRD 95'17 feasibility of  $\bar{p}p \rightarrow J/\psi \pi^0$ .

# Deep deuteron electrodissociation with a B = 1 exchange in the cross

# channel

- More use for 3q light-cone operator: TDAs for  $B \rightarrow B 1$  baryons as a tool for nuclear physics.
- Deep deuteron electrodissociation with a baryon number exchange in the cross channel:

$$\gamma^*(q) + d(p_d) \to p(p_p) + n(p_n); \quad |u| = |(p_d - p_n)^2| \ll Q^2, \ W^2 = (q + p_d)^2.$$



- BAND coverage in  $\theta$ : 155 176°.
- Can CLAS measure this reaction?

## Backward DVCS and nucleon-to-photon TDAs

• Nucleon-to-photon TDAs J.P. Lansberg, B. Pire, and L. Szymanowski'07 : 16  $N \rightarrow \gamma$  TDAs at the leading twist-3 .



- Cross channel processes  $N\bar{N} \rightarrow \gamma^* \gamma$  can be studied with  $\bar{P}ANDA$ .
- New information on the subtraction constant in the dispersion relation for the DVCS amplitude (*D*-term FF).
- May be important in connection with the J = 0 fixed pole universality conjecture S. Brodsky,
   F. Llanes-Estrada, and A. Szczepaniak'09, D. Müller and K.S.'15.

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# **Conclusions & Outlook**

- In Nucleon-to-meson TDAs provide new information about correlation of partons inside hadrons. A consistent picture for integrated TDAs emerges in the impact parameter representation.
- We strongly encourage to try to detect near forward and backward signals for various mesons (π, η, ω, ρ) and photons: there is an interesting physics around!
- **3** The experimental success achieved for backward  $\gamma^* N \to N' \pi$  and  $\gamma^* N \to N' \omega$  already with the old 6 GeV data set (more is expected at 12 GeV).
- First evidences for the onset of the factorization regime in backward  $\gamma^* N \rightarrow N' \omega$  from JLab Hall C analysis.
- **5**  $\bar{p}N \to \pi \ell^+ \ell^-$  ( $q^2$  timelike) and  $\bar{p}N \to \pi J/\psi$  at PANDA would allow to check universality of TDAs.
- **1** TDAs as a tool for nuclear physics: deuteron-to-nucleon TDAs.