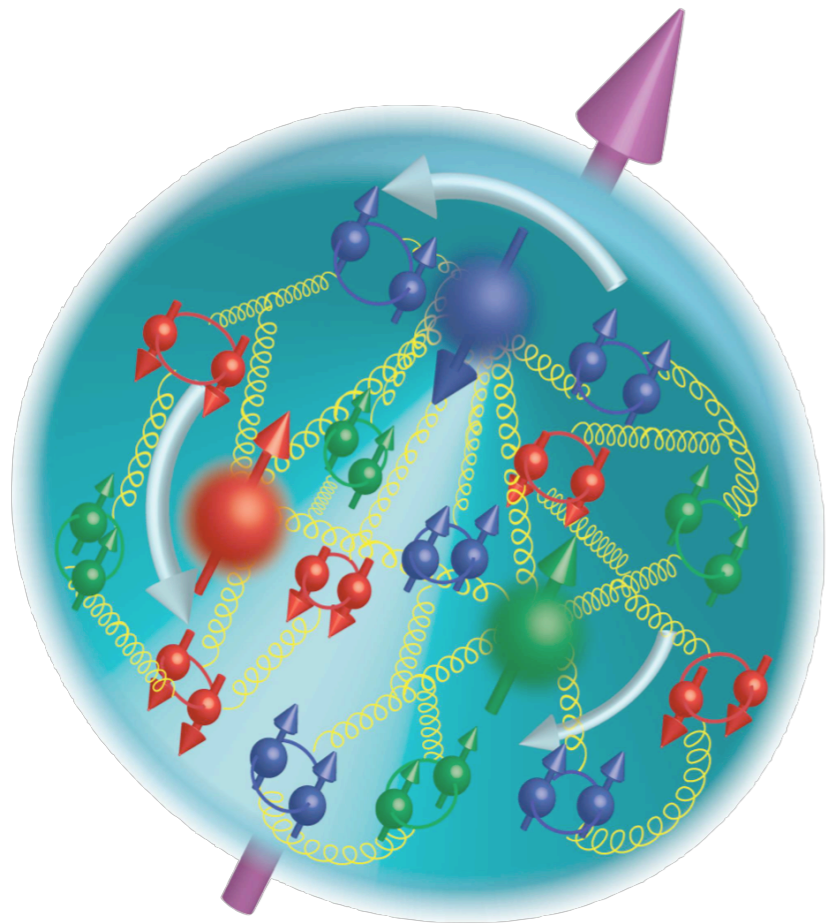


# THE ORIGIN OF SPIN ASYMMETRIES

Alexei Prokudin



## The origin of single transverse-spin asymmetries in high-energy collisions

Justin Cammarota,<sup>1,2,\*</sup> Leonard Gamberg,<sup>3,†</sup> Zhong-Bo Kang,<sup>4,5,6,‡</sup> Joshua A. Miller,<sup>2,§</sup>  
Daniel Pitonyak,<sup>2,¶</sup> Alexei Prokudin,<sup>3,8,\*\*</sup> Ted C. Rogers,<sup>7,8</sup> and Nobuo Sato<sup>8,††</sup>

<sup>1</sup>*Physics Department, William & Mary, Williamsburg, Virginia 23187, USA*

<sup>2</sup>*Department of Physics, Lebanon Valley College, Annville, Pennsylvania 17003, USA*

<sup>3</sup>*Division of Science, Penn State University Berks, Reading, Pennsylvania 19610, USA*

<sup>4</sup>*Department of Physics and Astronomy, University of California, Los Angeles, California 90095, USA*

<sup>5</sup>*Mani L. Bhaumik Institute for Theoretical Physics, University of California, Los Angeles, California 90095, USA*

<sup>6</sup>*Center for Frontiers in Nuclear Science, Stony Brook University, Stony Brook, New York 11794, USA*

<sup>7</sup>*Department of Physics, Old Dominion University, Norfolk, Virginia 23529, USA*

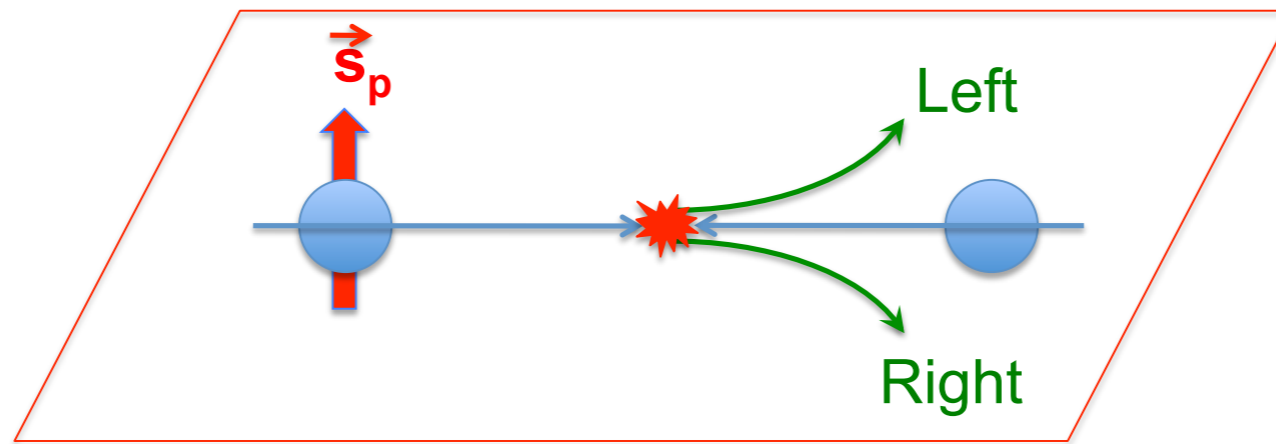
<sup>8</sup>*Thomas Jefferson National Accelerator Facility, Newport News, VA 23606, USA*

**Jefferson Lab Angular Momentum (JAM) Collaboration**

# SINGLE SPIN ASYMMETRIES

---

Consider polarized hadron - hadron collisions



Count pions going to the right or to the left with respect to the spin direction

$$A_N \equiv \frac{\sigma(\vec{s}_P) - \sigma(-\vec{s}_P)}{\sigma(\vec{s}_P) + \sigma(-\vec{s}_P)}$$

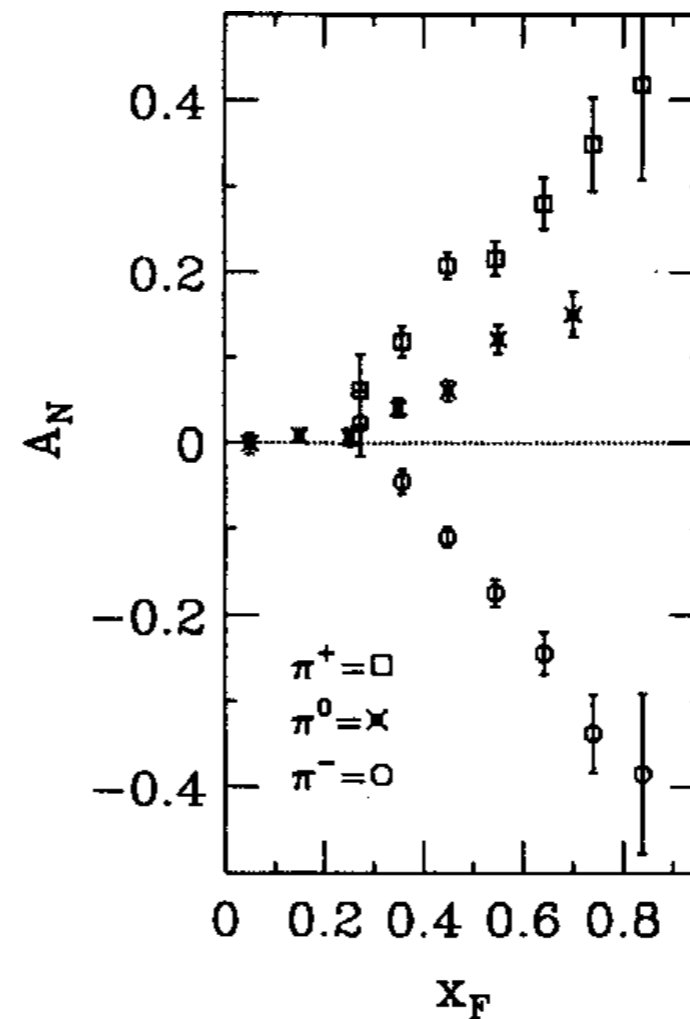
# CHALLENGE OF QCD: UNDERSTANDING SPIN ASYMMETRIES

Experiment proved this prediction wrong

QCD had a very simple prediction

$$A_N \propto \alpha_s \frac{m_q}{P_T} \rightarrow 0$$

Kane, Pumplin, Repko (1978)



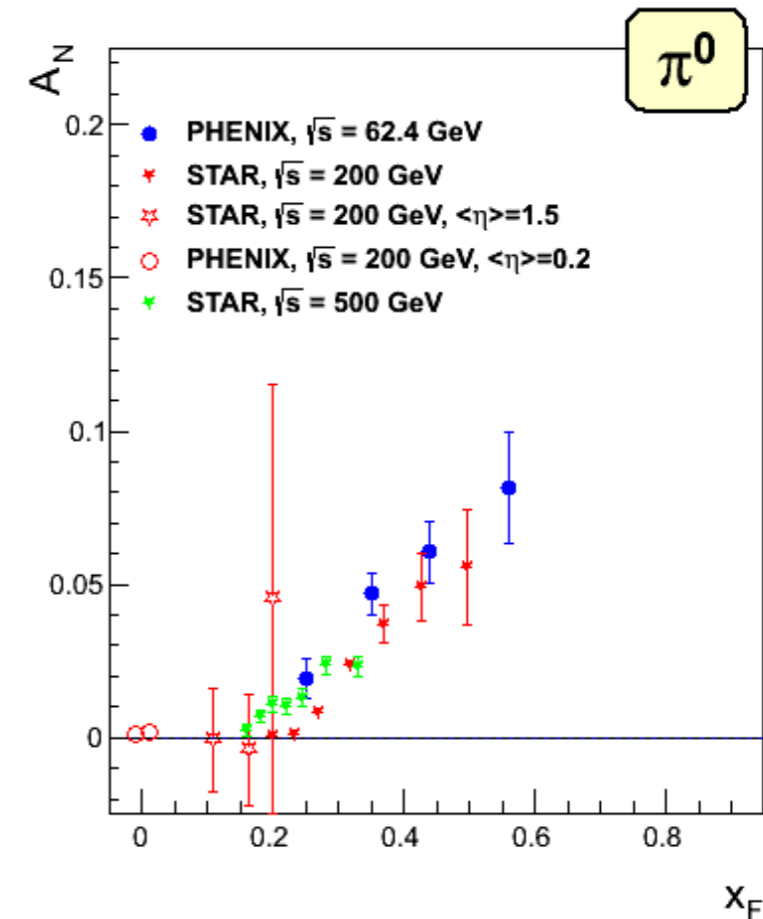
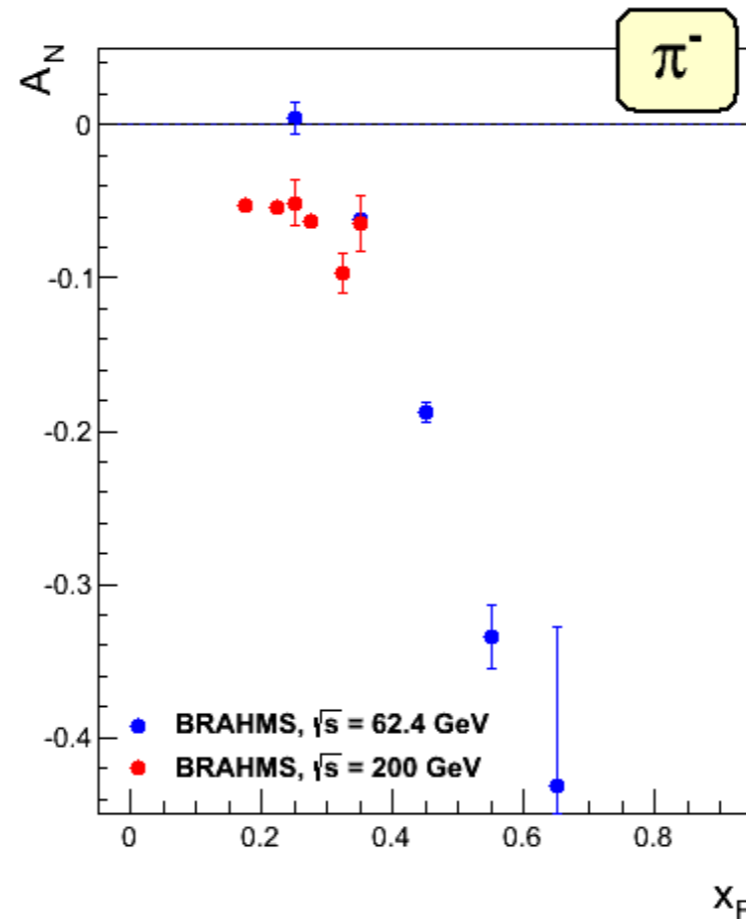
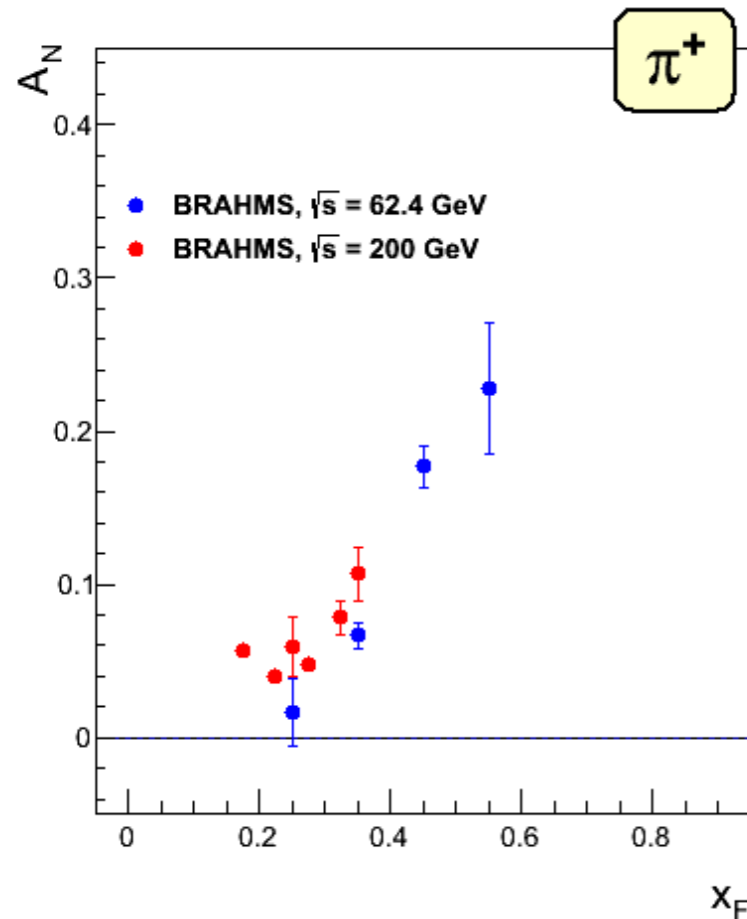
$$A_N \simeq 40\%$$

Fermilab experiment E704 (1991)  
 $\sqrt{s} \simeq 19$  (GeV)

# CHALLENGE OF QCD: UNDERSTANDING SPIN ASYMMETRIES

Asymmetry survives with growing collision energy

RHIC: STAR, BRAHMS, PHENIX



“The RHIC SPIN Program: Achievements and Future Opportunities”, Aschenauer et al (15)



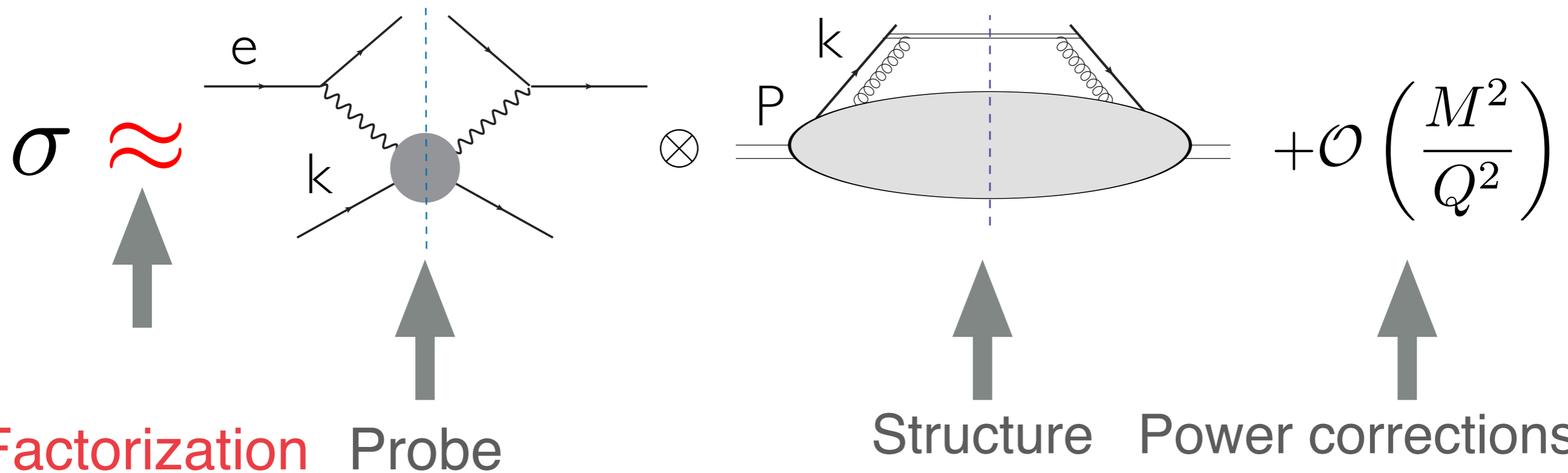
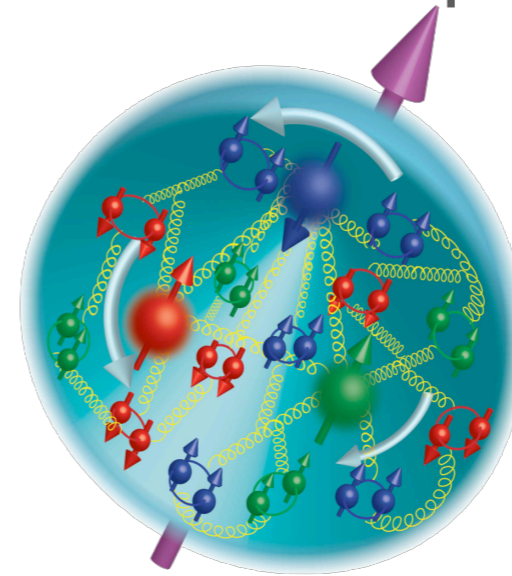
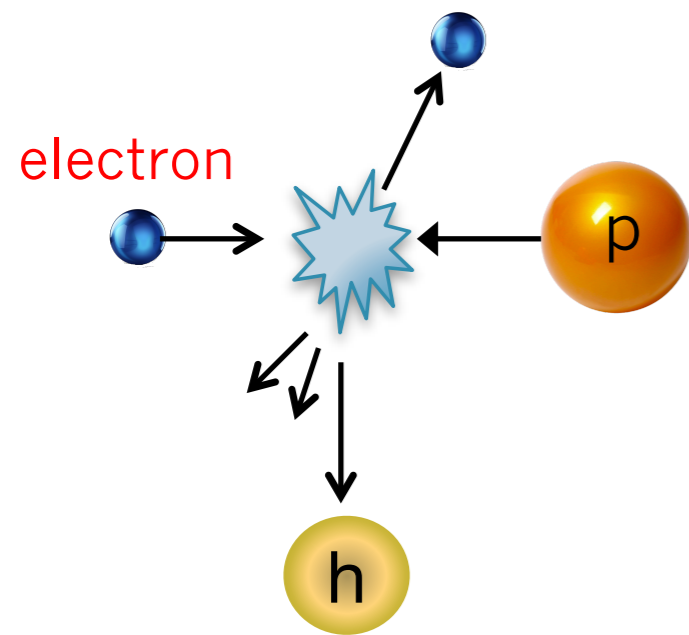
**FAILURE  
OF QCD?**



**BETTER  
UNDERSTANDING OF QCD!**

# QCD FACTORIZATION IS THE KEY!

We need a probe to “see” quarks and gluons



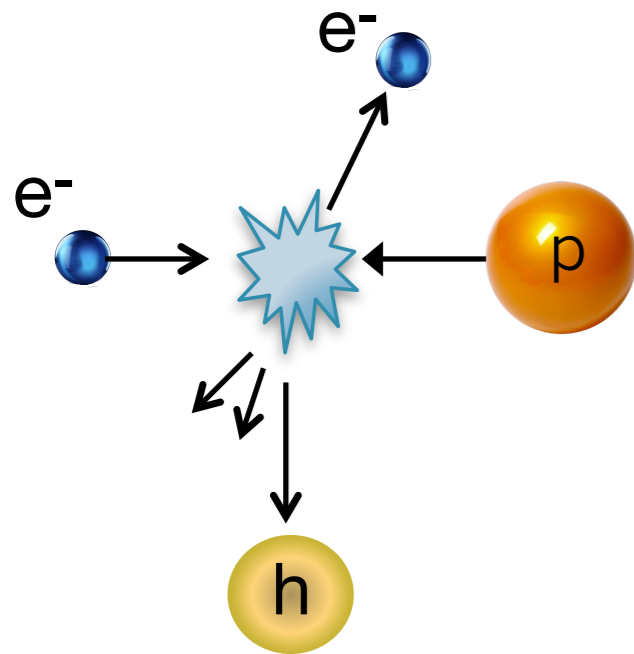


# TRANSVERSE MOMENTUM DEPENDENT FACTORIZATION

The confined motion ( $k_T$  dependence) is encoded in TMDs

## Semi-Inclusive DIS

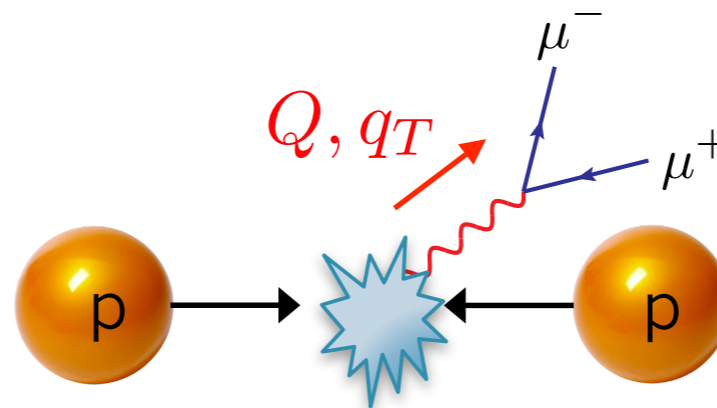
$$\sigma \sim f_{q/P}(x, k_T) D_{h/q}(x, k_T)$$



Meng, Olness, Soper (1992)  
 Ji, Ma, Yuan (2005)  
 Idilbi, Ji, Ma, Yuan (2004)  
 Collins (2011)

## Drell-Yan

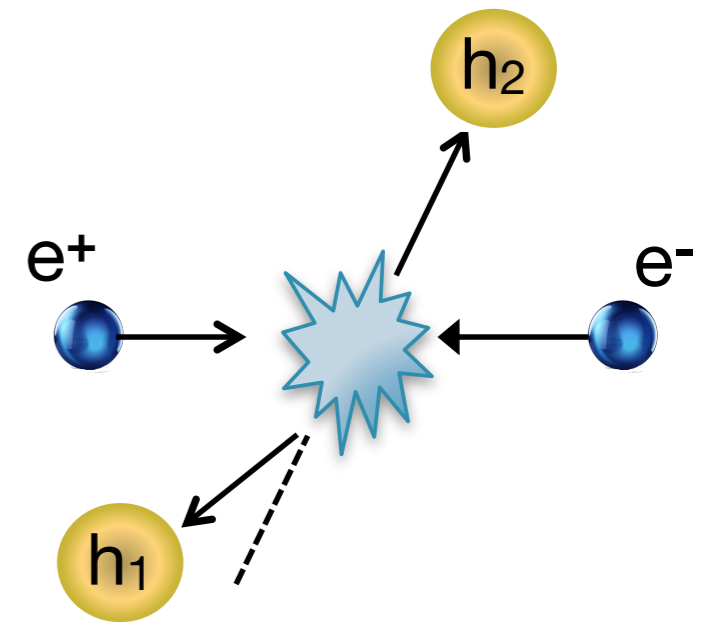
$$\sigma \sim f_{q/P}(x, k_T) f_{q/P}(x, k_T)$$



Collins, Soper, Sterman (1985)  
 Ji, Ma, Yuan (2004)  
 Collins (2011)

## Dihadron in $e^+e^-$

$$\sigma \sim D_{h_1/q}(x, k_T) D_{h_2/q}(x, k_T)$$



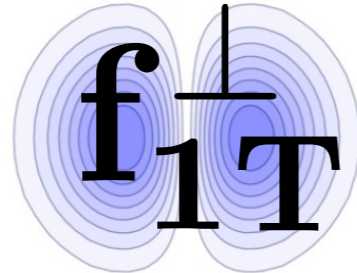
Collins, Soper (1983)  
 Collins (2011)

Small scale  $\longrightarrow q_T \ll Q \longleftarrow$  Large scale

# SIVERS AND COLLINS EFFECTS

---

## Sivers function



Sivers 1989

- Describes unpolarized quarks inside of transversely polarized nucleon
- Generates asymmetries in SIDIS and DY



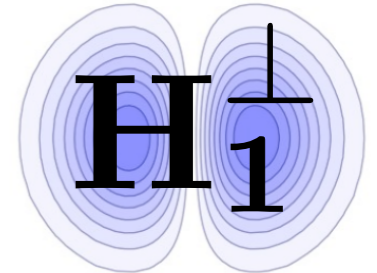
Kotzinian (1995)  
Mulders, Tangerman (1995)  
Boer, Mulders (1998)

- Changes sign in DY w.r.t. SIDIS



Brodsky, Hwang, Schmidt (2002)  
Collins (2002)

## Collins function



Collins 1992

- Describes fragmentation of transversely polarized quark into an unpolarized nucleon
- Generates asymmetries in SIDIS and  $e^+e^-$

Kotzinian (1995)  
Mulders, Tangerman (1995)  
Boer, Jakob, Mulders (1997)

- Universal in SIDIS,  $e^+e^-$ , and PP

Metz, Collins (2004)  
Yuan (2008)

# TWIST-3 FACTORIZATION

$$\sigma(Q, \vec{s}) \propto \left| \begin{array}{c} \text{Diagram 1} + \text{Diagram 2} + \text{Diagram 3} + \dots \end{array} \right|^2$$

*Qiu, Sterman (1991)*

Large scale  $\longrightarrow$   $q_T \simeq Q$   $\longleftarrow$  Large scale

Multi-parton correlations (twist-3 functions) contribute to the cross section and are dominant for asymmetries in PP scattering

# TMD AND COLLINEAR FACTORIZATIONS ARE RELATED

---

TMDs and collinear PDFs and FFs are related via Operator Product Expansion in CSS formalism

*Collins, Soper, Sterman (1985)*

TMD and collinear twist-3 (CT3) formalisms are “unified” in intermediate region of  $q_T$

*Ji, Qiu, Vogelsang, Yuan (2006)*

TMD and twist-3 (CT3) functions are related by integral relations

*Boer, Mulders, Pijlman (2003)*

$$\pi F_{FT}(x, x) = f_{1T}^{\perp(1)}(x)$$



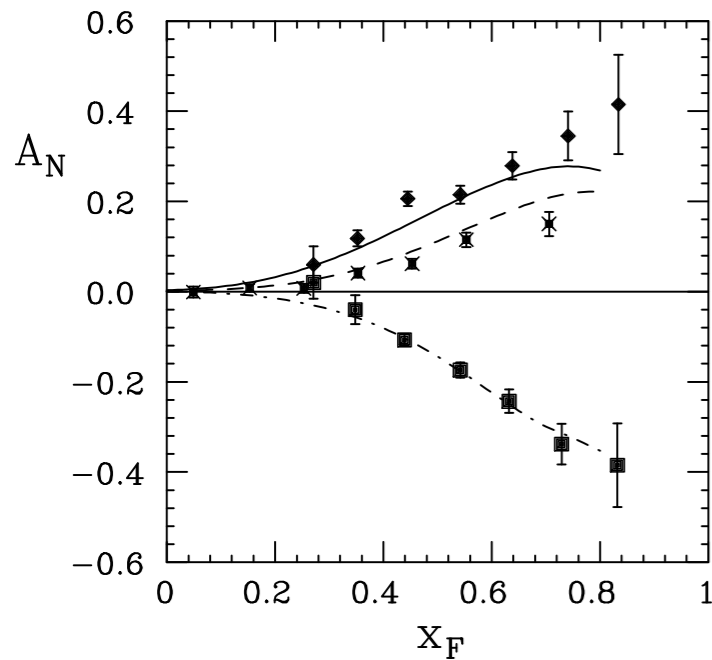
*Qiu-Sterman matrix element*



*The first  $k_T$  moment of Sivers function*

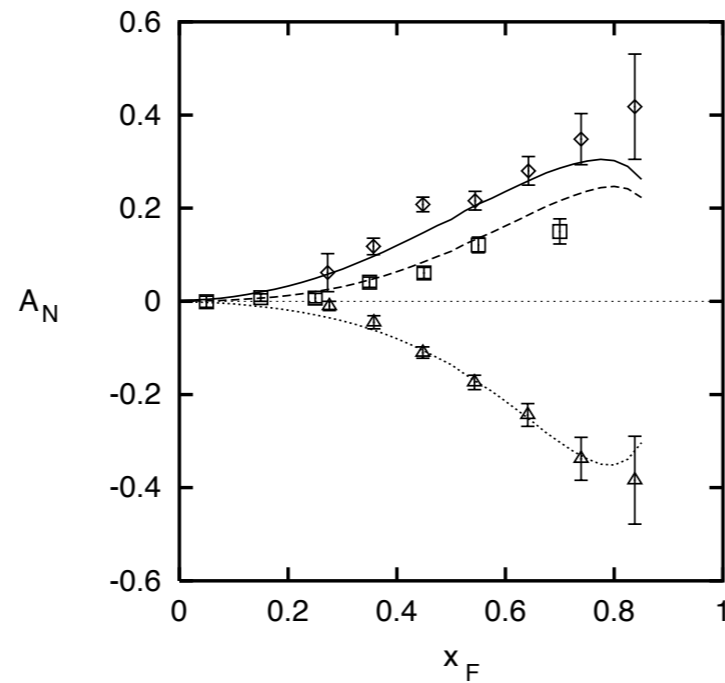
# TOWARDS THE SOLUTION OF 40 YEAR OLD PUZZLE

Anselmino, Murgia (1998)



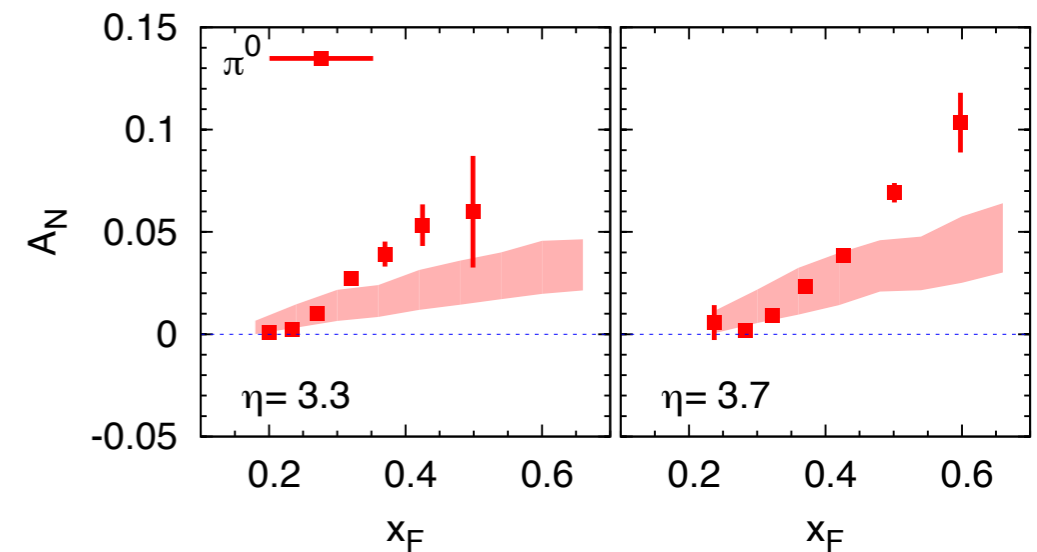
Sivers effect TMD fit

Anselmino, Boglione, Murgia (1999)



Collins effect TMD fit

Anselmino, Boglione, D'Alesio, Leader, Melis, Murgia, Prokudin (2013)

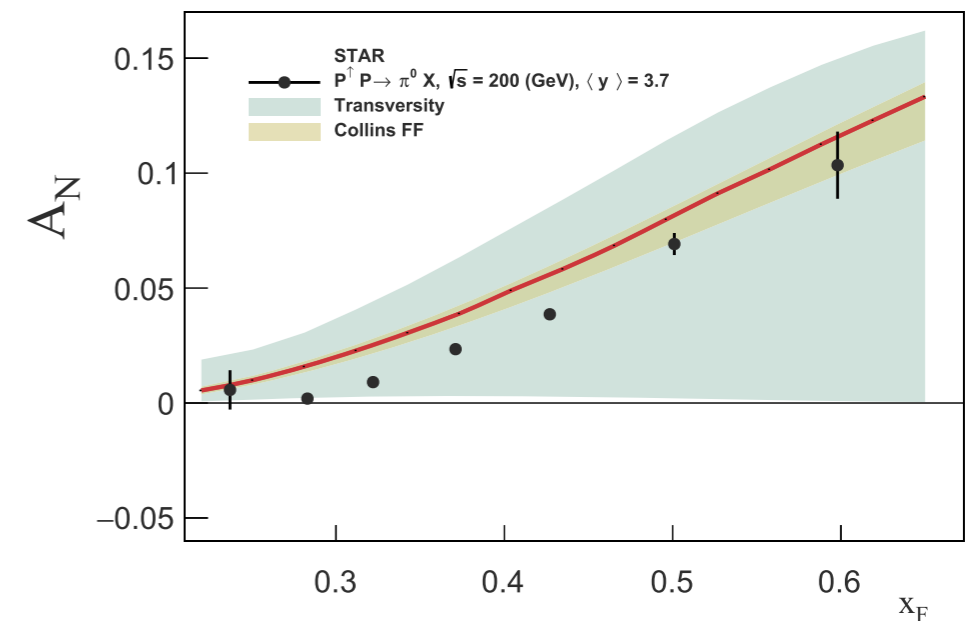
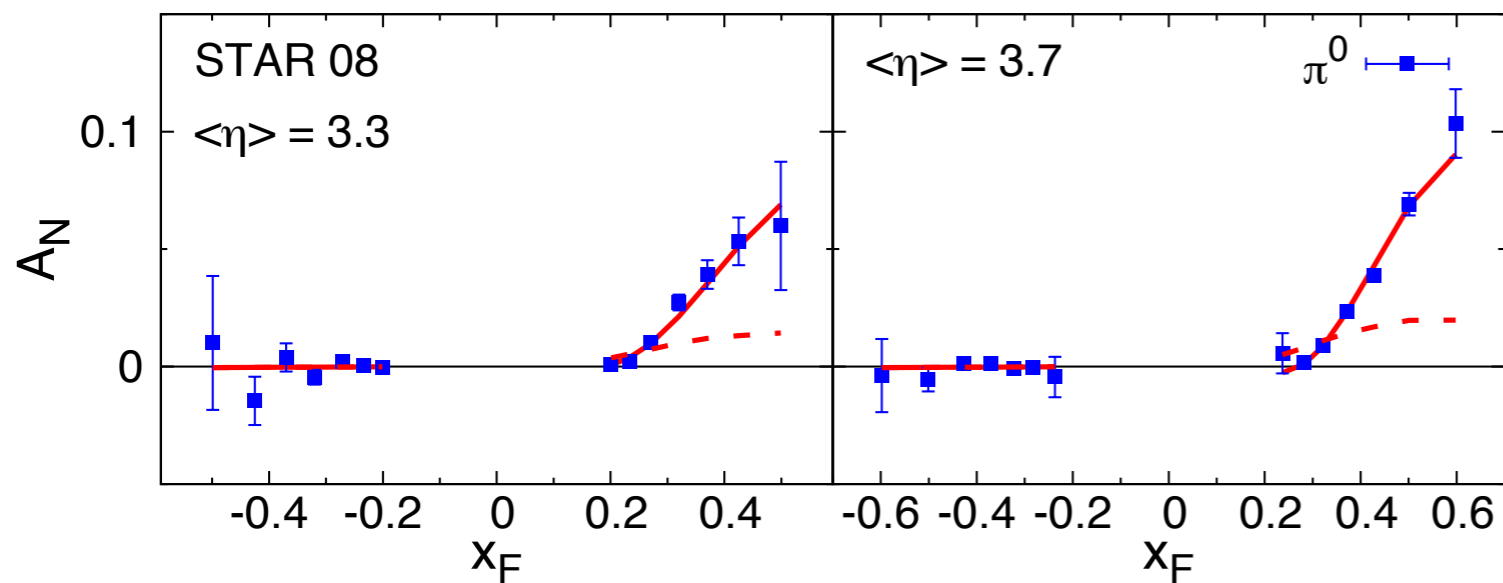


TMD Collins effect only from SIDIS

# TOWARDS THE SOLUTION OF 40 YEAR OLD PUZZLE

Kanazawa, Koike, Metz, Pitonyak PRD 89 (2014)

Gamberg, Kang, Pitonyak, Prokudin PLB 770 (2017)

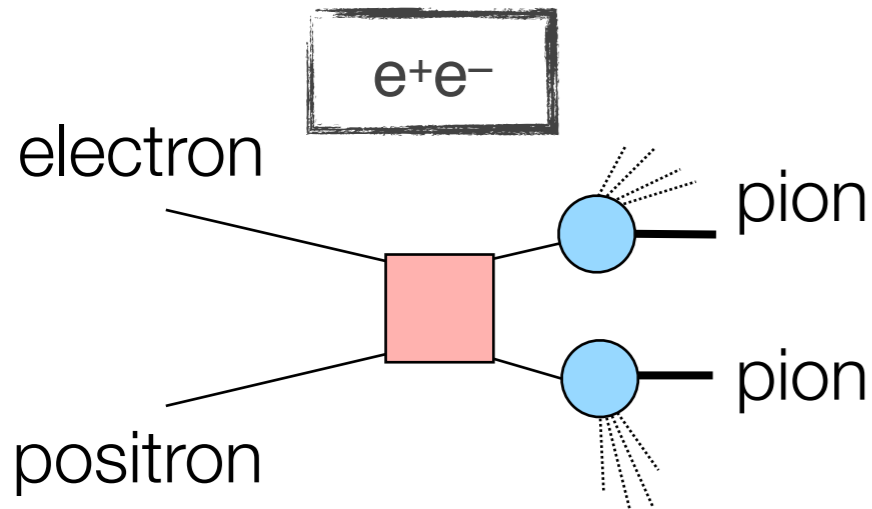


Explanation using fit of twist-3 fragmentation functions

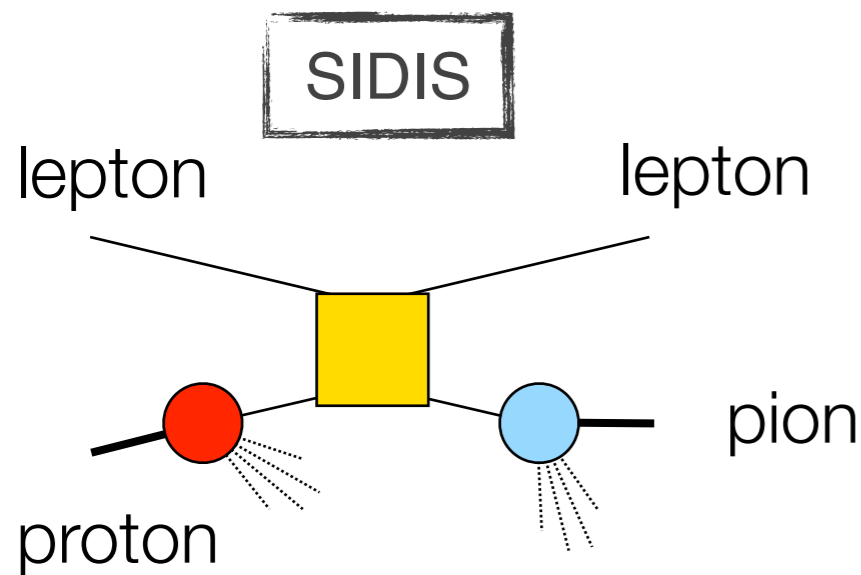
Prediction of  $A_N$  at STAR using only SIDIS and  $e^+e^-$  data information only

# UNIVERSAL GLOBAL FIT 2020

Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)

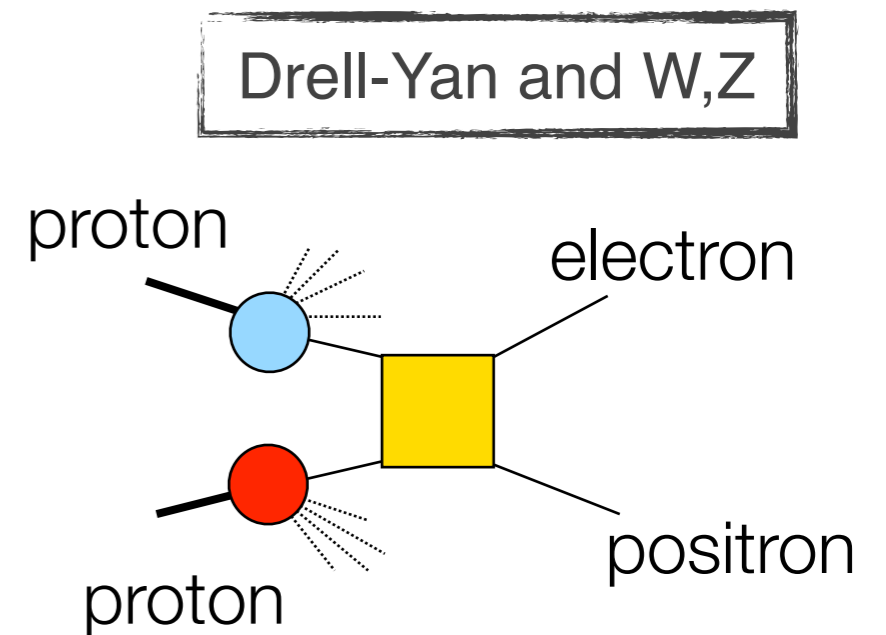


*Collins asymmetries  
BELLE, BaBar, BESIII data*

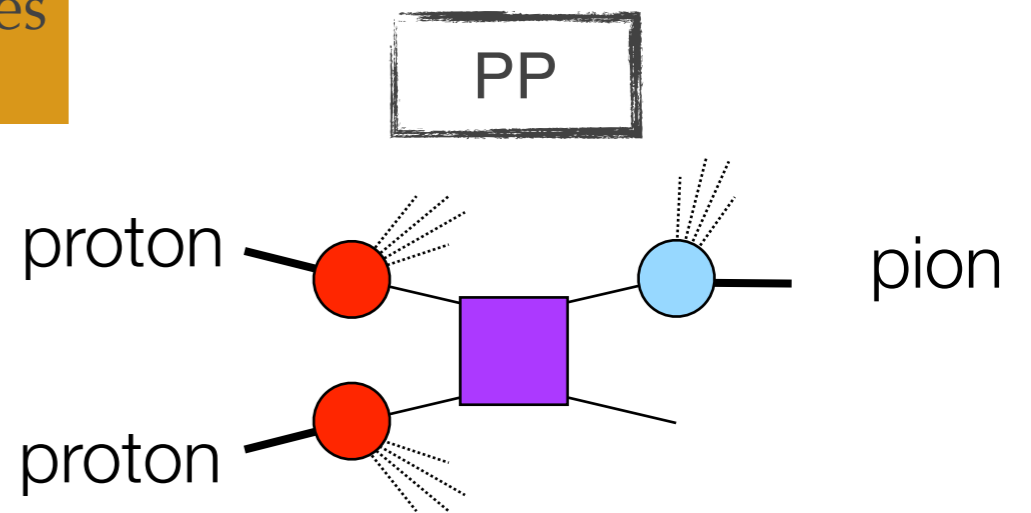


*Sivers, Collins asymmetries  
COMPASS, HERMES, JLab data*

To demonstrate the common origin of SSAs in various processes, we will combine all available data and extract a universal set of non perturbative functions that describes all of them



*Sivers asymmetries  
COMPASS, STAR data*



*$A_N$  asymmetry  
STAR, PHENIX, BRAHMS data*

# UNIVERSAL GLOBAL FIT 2020

.....  
Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)

The relevant set of collinear functions to extract

$h_1(x)$	transversity
$F_{FT}(x, x)$	Qiu-Sterman function
$H_1^{\perp(1)}(z)$	the first moment of Collins FF
$\tilde{H}(z)$	fragmentation twist-3 function

Flexible parametrization

$$F^q(x) = \frac{N_q x^{a_q} (1-x)^{b_q} (1 + \gamma_q x^{\alpha_q} (1-x)^{\beta_q})}{\text{B}[a_q + 2, b_q + 1] + \gamma_q \text{B}[a_q + \alpha_q + 2, b_q + \beta_q + 1]}$$



# UNIVERSAL GLOBAL FIT 2020

.....  
Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)

$\tilde{H}(z)$  fragmentation twist-3 function

Plays role in  $A_N$  in PP, generates asymmetry in SIDIS

$$A_{UT}^{\sin\phi_S}(x, z) \sim h_1(x)\tilde{H}(z)$$

This function is totally unconstrained in the current fit as data from COMPASS and HERMES are unavailable at the moment

We set it to zero in our analysis making it consistent with small asymmetry observed by COMPASS and HERMES

# UNIVERSAL GLOBAL FIT 2020

.....  
Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)

The relevant set of TMD functions to extract

$$\mathcal{G}_f(k_T^2) = \frac{1}{\pi \langle k_T^2 \rangle_f} e^{-\frac{k_T^2}{\langle k_T^2 \rangle_f}}$$

$$h_1(x, k_T) = h_1(x) \mathcal{G}_h(k_T^2) \quad \text{transversity}$$

$$f_{1T}^\perp(x, k_T) = \frac{2M^2}{\langle k_T^2 \rangle_{f_{1T}^\perp}} \pi F_{FT}(x, x) \mathcal{G}_{f_{1T}^\perp}(k_T^2)$$

Sivers function

$$H_1^\perp(z, zp_T) = \frac{2z^2 M^2}{\langle p_T^2 \rangle_{H_1^\perp}} H_1^{\perp(1)}(z) \mathcal{G}_{H_1^\perp}(z^2 p_T^2)$$

Collins function

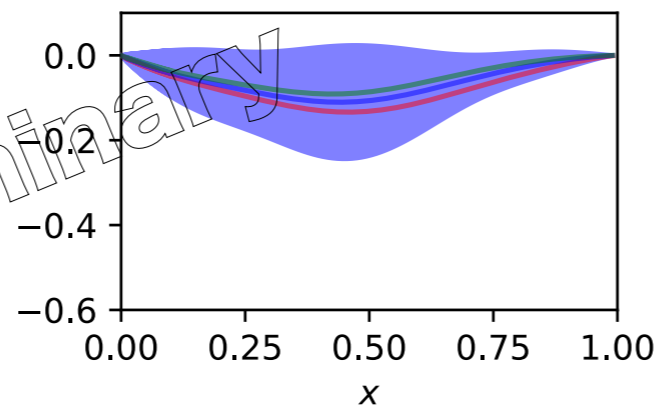
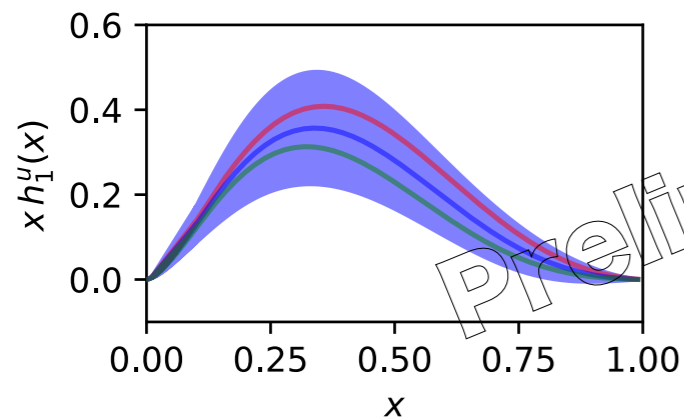
# UNIVERSAL GLOBAL FIT 2020

.....  
 Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)

Observable	Reactions	NP Function(s)
$A_{\text{SIDIS}}^{\text{Siv}}$	$e + (p, d)^{\uparrow} \rightarrow (\pi^+, \pi^-) + X$	$f_{1T}^{\perp}$
$A_{\text{SIDIS}}^{\text{Col}}$	$e + (p, d)^{\uparrow} \rightarrow (\pi^+, \pi^-, \pi^0) + X$	$h_1, H_1^{\perp}$
$A_{\text{SIA}}^{\text{Col}}$	$e^+ + e^- \rightarrow \pi^+ \pi^- (UC, UL) + X$	$H_1^{\perp}$
$A_{\text{DY}}^{\text{Siv}}$	$\pi^- + p^{\uparrow} \rightarrow \mu^+ \mu^- + X$	$f_{1T}^{\perp}$
$A_{\text{DY}}^{\text{Siv}}$	$p^{\uparrow} + p \rightarrow (W^+, W^-, Z) + X$	$f_{1T}^{\perp}$
$A_N$	$p^{\uparrow} + p \rightarrow (\pi^+, \pi^-, \pi^0) + X$	$h_1, F_{FT} (= \frac{1}{\pi} f_{1T}^{\perp(1)}), H_1^{\perp(1)}, \tilde{H}$

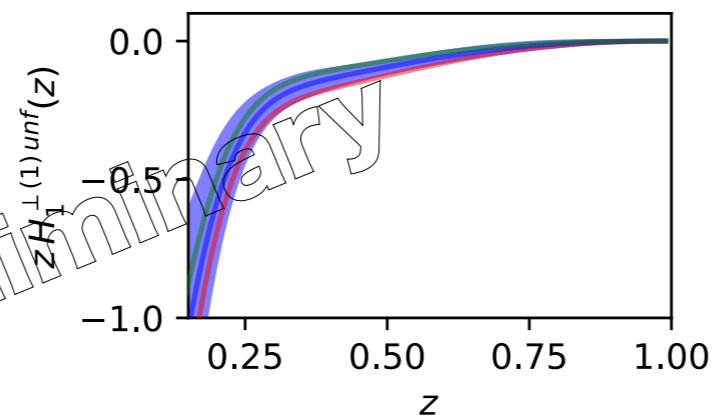
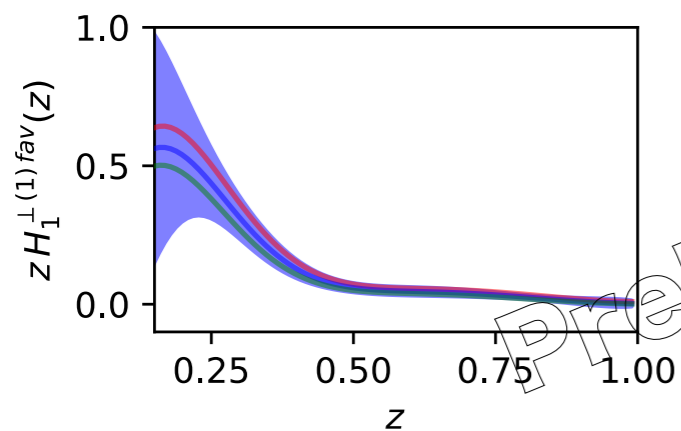
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Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)



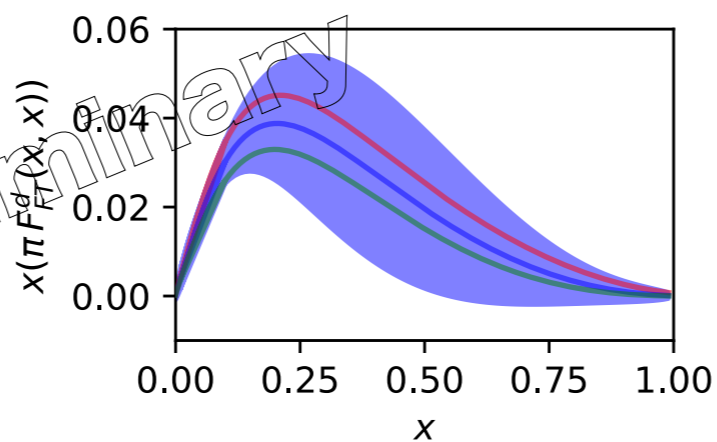
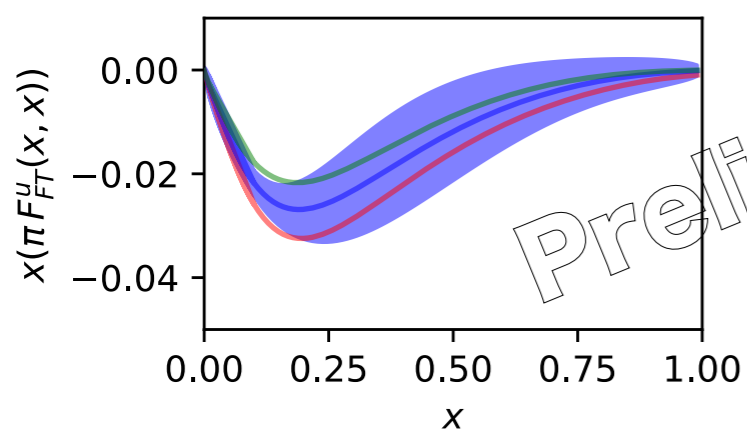
Transversity

$$h_1(x)$$



Collins FF

$$H_1^{\perp(1)}(z)$$



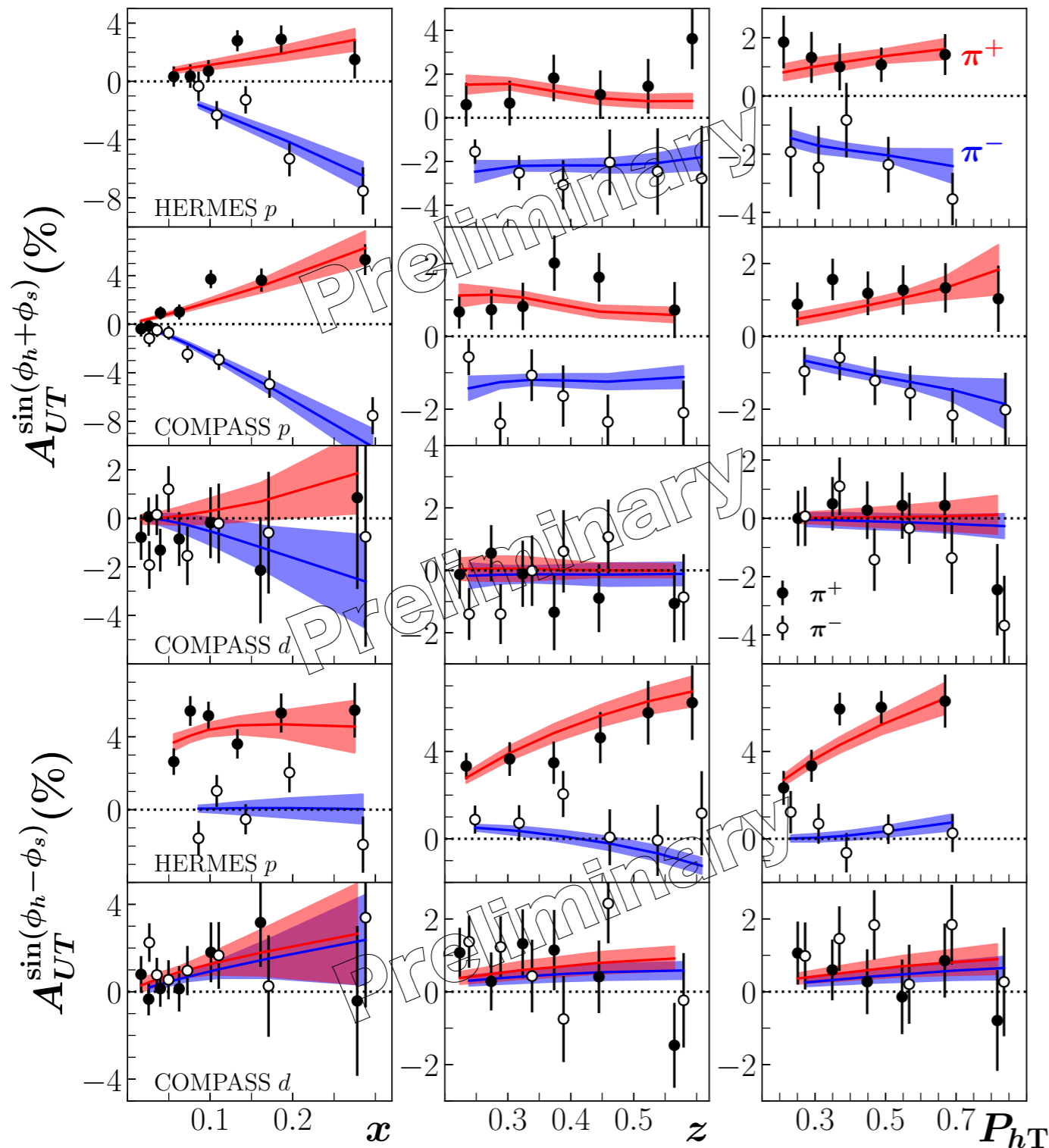
Sivers

$$f_{1T}^{\perp(1)}(x)$$

# UNIVERSAL GLOBAL FIT 2020

Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)

## SIDIS



## Collins asymmetry

$$\frac{\chi^2}{npoints} = \frac{107.1}{126} = 0.85$$

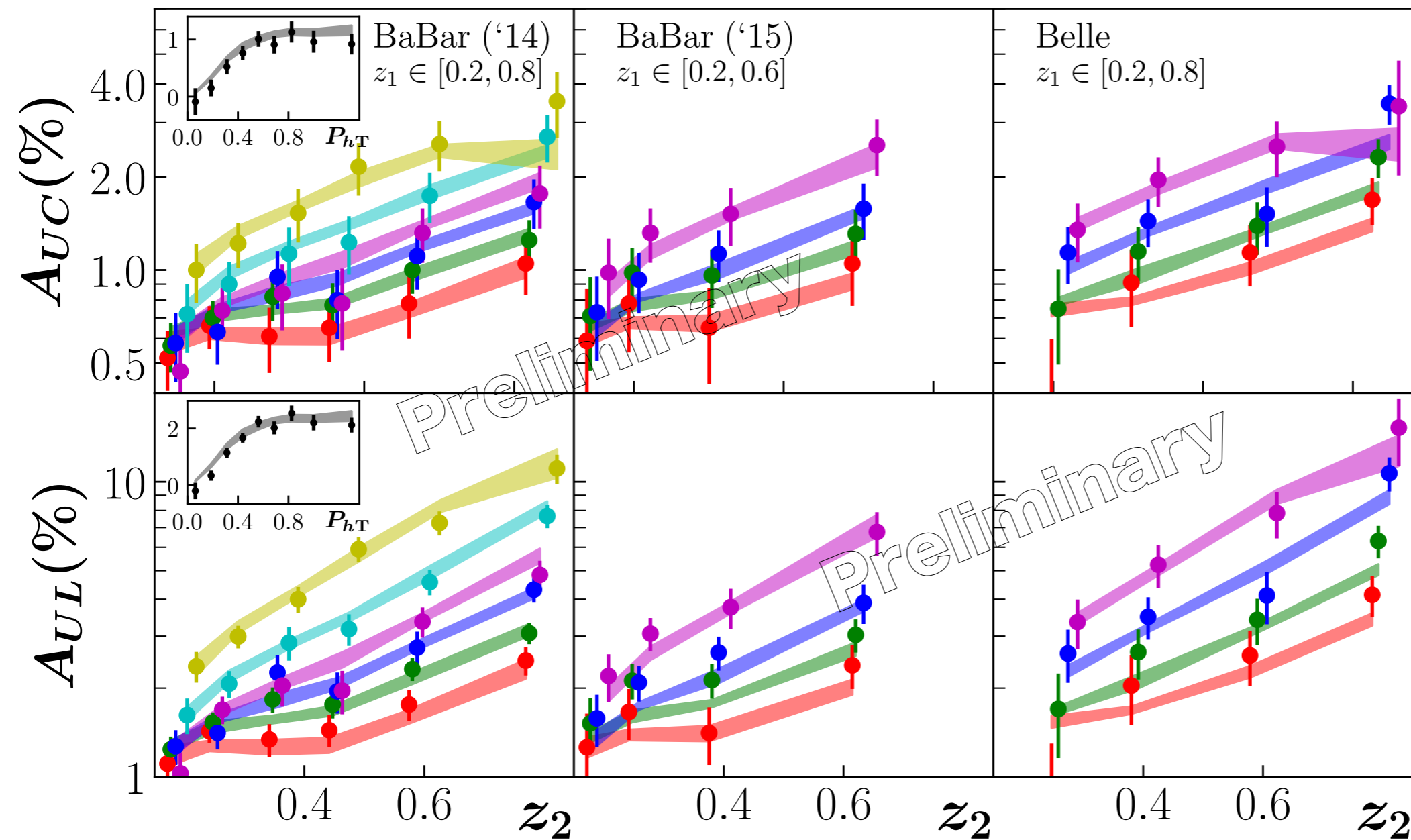
## Sivers asymmetry

$$\frac{\chi^2}{npoints} = \frac{85.4}{88} = 0.97$$

# UNIVERSAL GLOBAL FIT 2020

Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)

$e^+e^-$

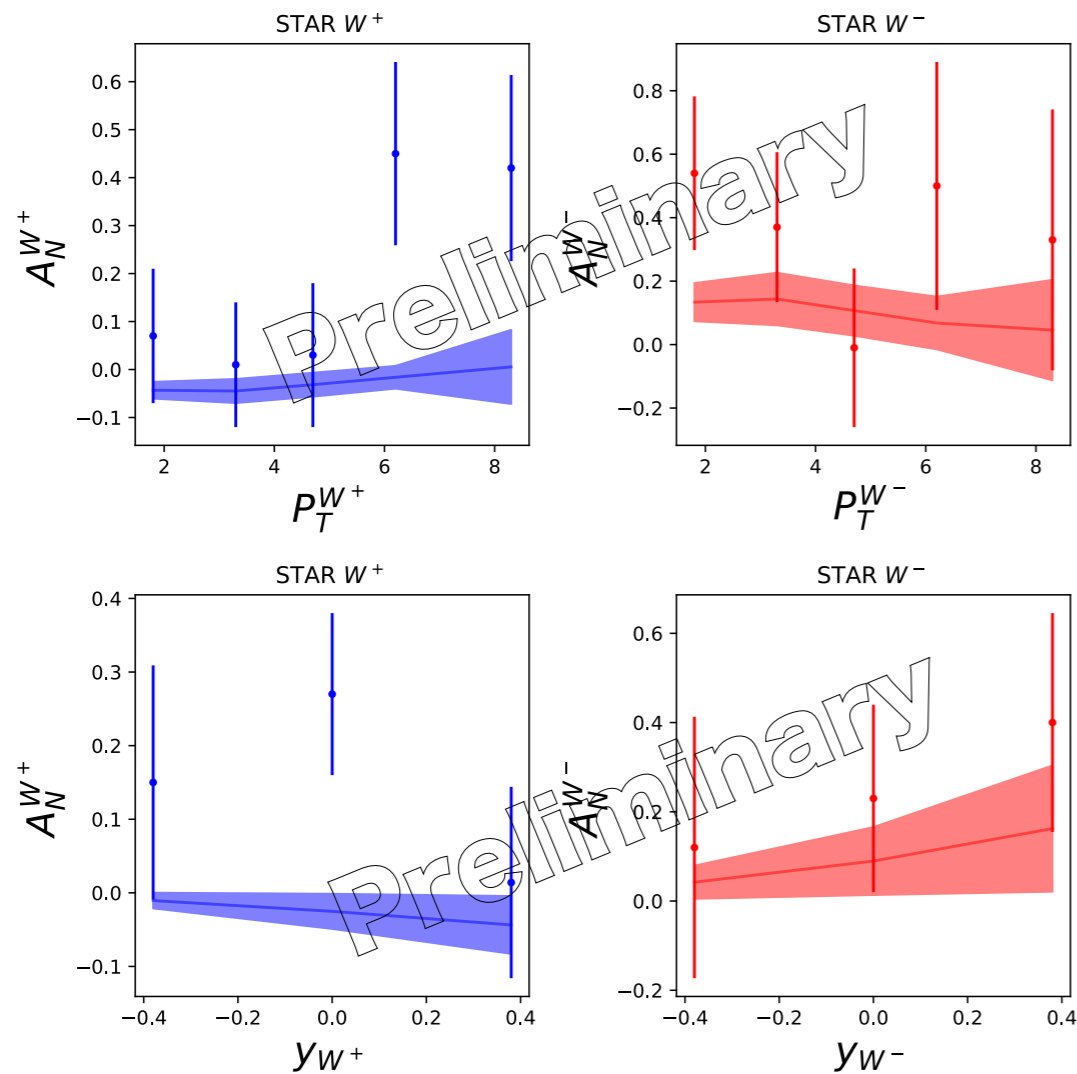


$$\frac{\chi^2}{npoints} = \frac{149.6}{176} = 0.85$$

# UNIVERSAL GLOBAL FIT 2020

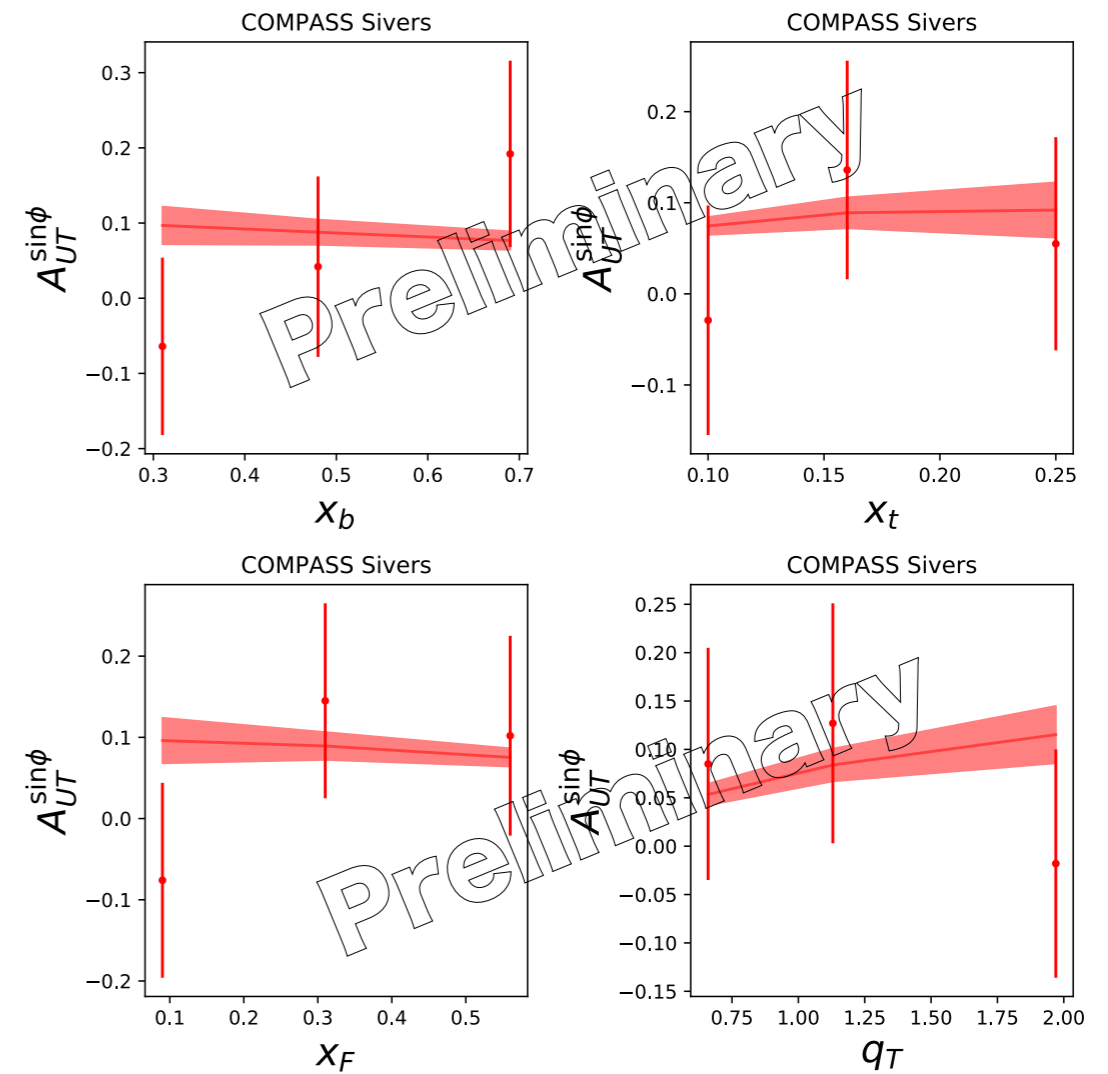
Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)

## Drell-Yan



$$\frac{\chi^2}{npoints} = \frac{29.8}{17} = 1.75$$

STAR



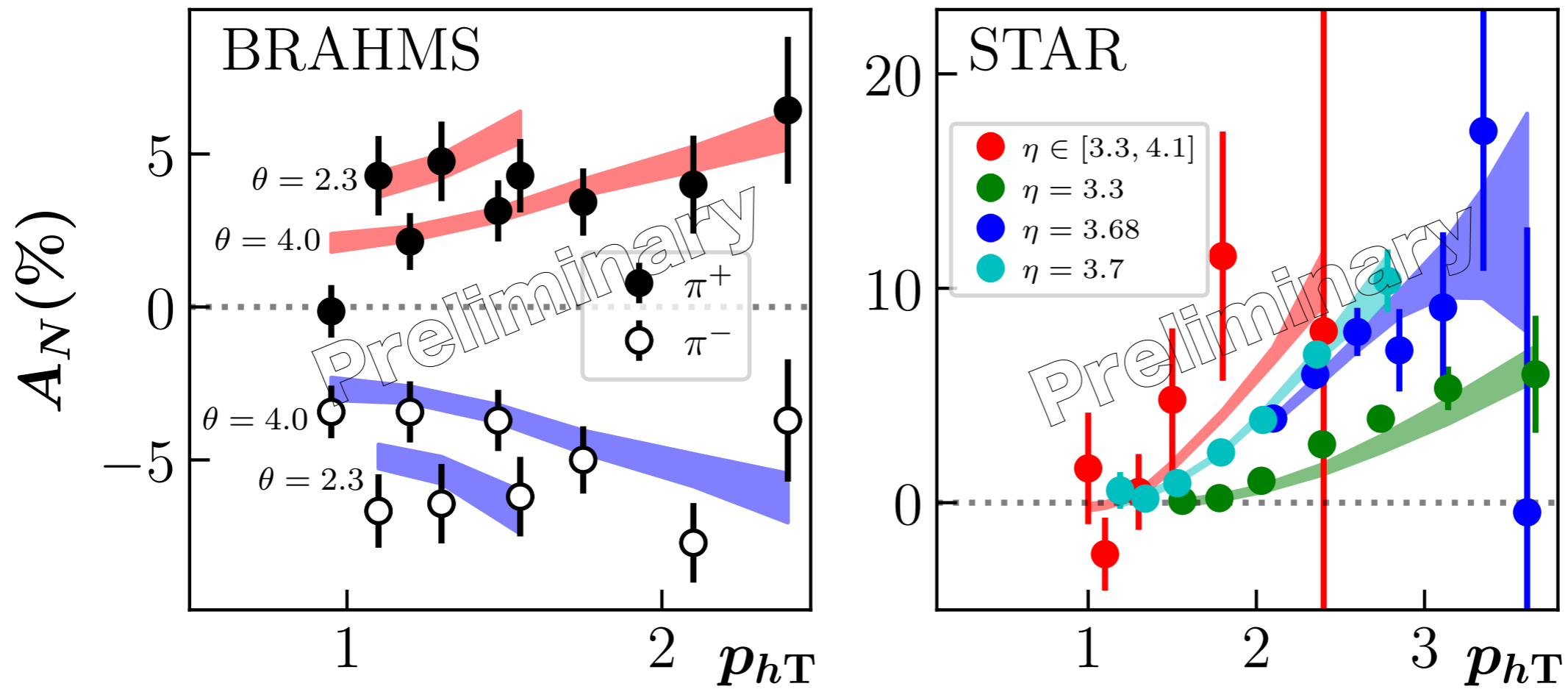
$$\frac{\chi^2}{npoints} = \frac{7.6}{12} = 0.63$$

COMPASS DY

# UNIVERSAL GLOBAL FIT 2020

Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)

proton-proton  $A_N$

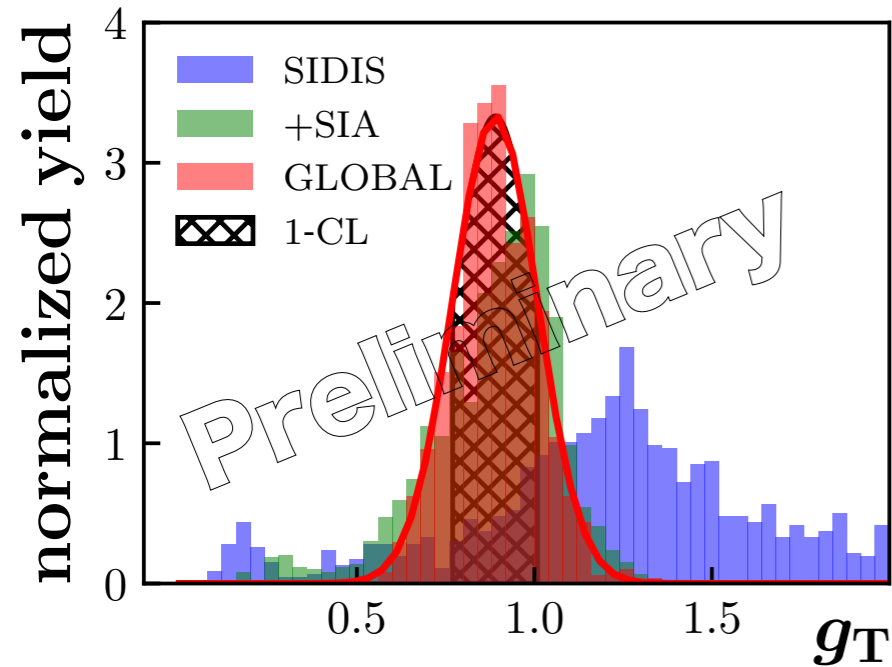


$$\frac{\chi^2}{npoints} = \frac{72.0}{60} = 1.2$$

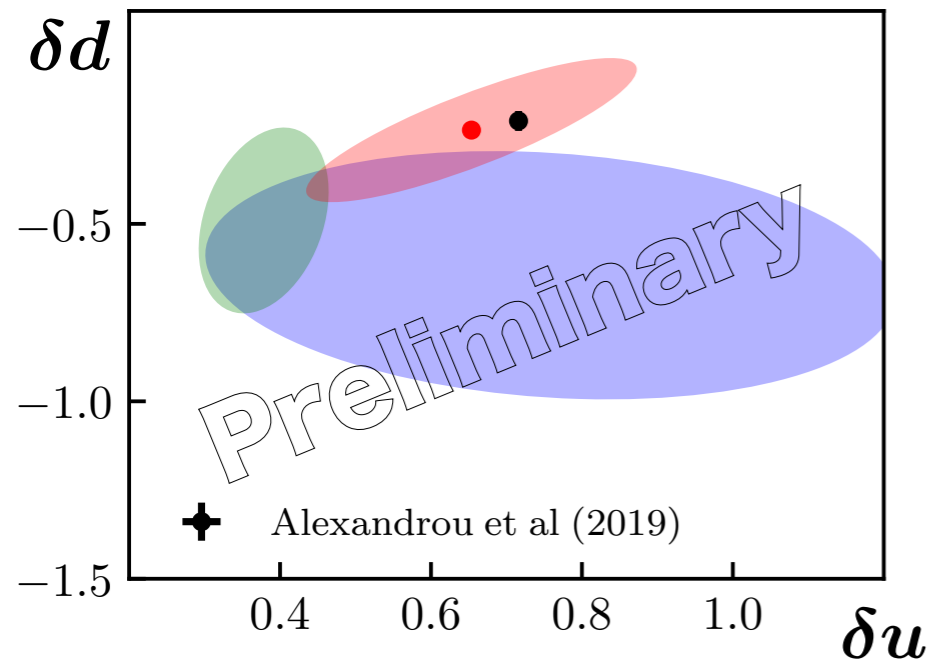


# UNIVERSAL GLOBAL FIT 2020

Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)



- Isovector tensor charge  $g_T = \delta u - \delta d$   
 $g_T = 0.89 \pm 0.12$  compatible with lattice results



- **Tensor charge** from up and down quarks is constrained and compatible with lattice results

$\delta u$  and  $\delta d$   $Q^2=4$   $\text{GeV}^2$

$$\delta u = 0.65 \pm 0.22$$

$$\delta d = -0.24 \pm 0.2$$

# THEORETICAL AND PHENOMENOLOGICAL DEVELOPMENT

---

- Shown for the first time that transverse spin asymmetries in a variety of processes SIDIS, Drell-Yan,  $e^+e^-$ , and proton proton scattering have the same origin
- Extracted a universal set of non perturbative functions responsible for spin asymmetries
- Shown consistency of phenomenological results with lattice QCD in extraction of isovector tensor charge and individual contributions from up and down quark

# BACKUP SLIDES

---

# TREATMENT OF EVOLUTION

---

TMDs are parametrized with gaussian  $k_T$  dependence (no widening with  $Q^2$ ) and x-,z- dependent collinear functions evolved in  $Q^2$

Evolution in collinear functions are done by  $Q^2$  parametrization using Duke, Owens method Phys. Rev. D 30, 49 (1984)

$$N_0 + N_1 \log \left( \frac{\log(Q^2/\Lambda^2)}{\log(Q_0^2/\Lambda^2)} \right)$$

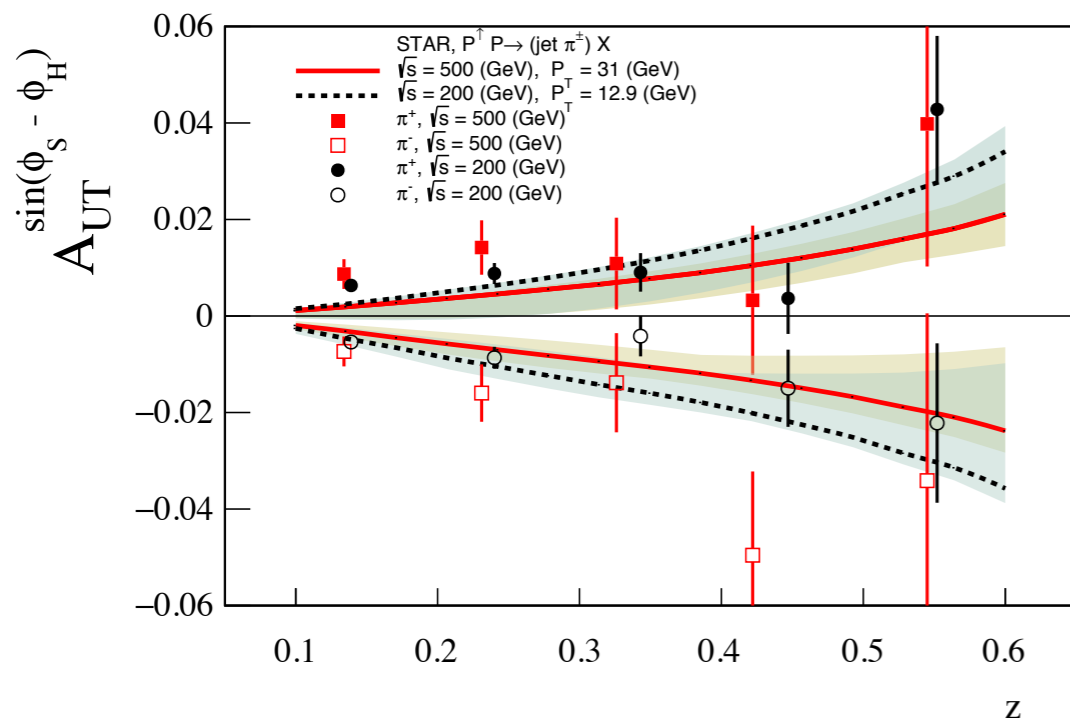
Success is achieved with Gaussian shapes for the transverse momentum dependence further implies that the effects are dominantly non-perturbative and intrinsic to the hadron wavefunctions.

# TREATMENT OF EVOLUTION

Results of this approach are consistent with resummation for asymmetries

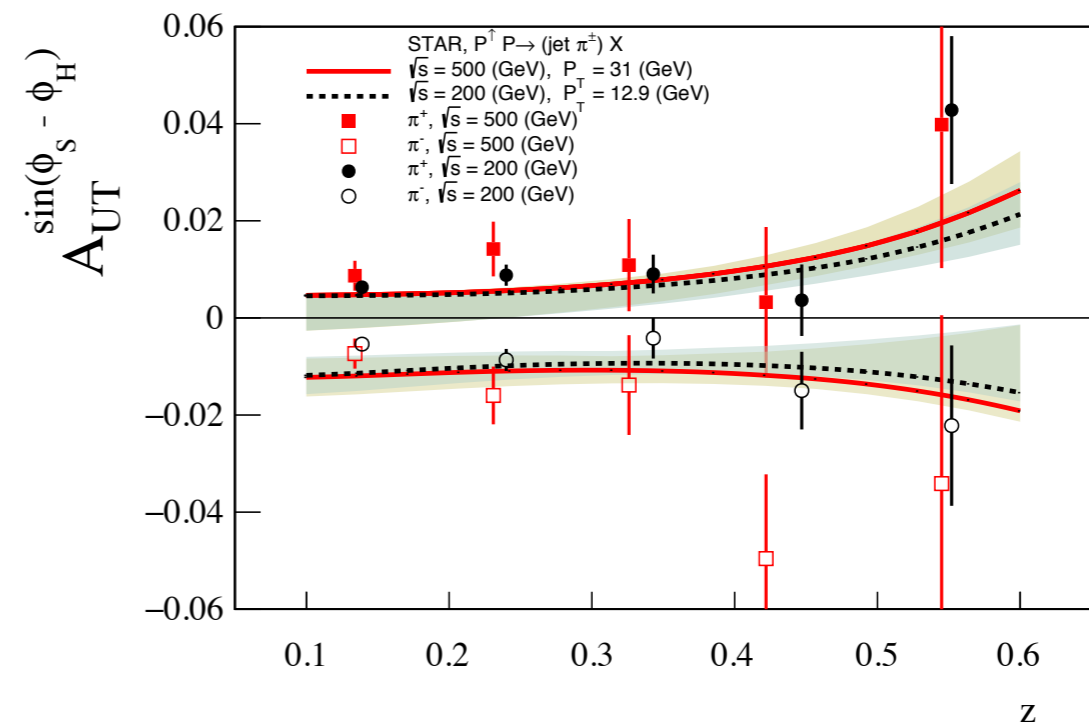
*Kang, Prokudin, Ringer, Yuan (2017)*

## NLL TMD evolution



*functions: Kang, Prokudin, Sun, Yuan (2015)*

## Gaussian Torino model



*functions: Anselmino et al (2015)*

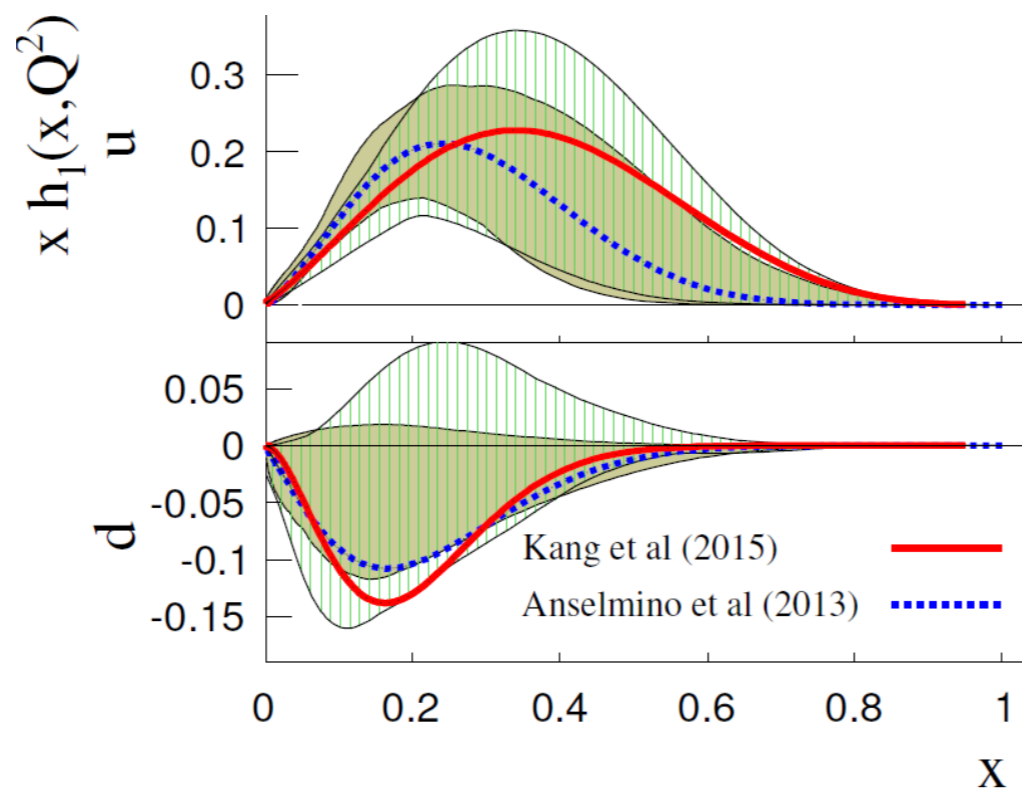
# TREATMENT OF EVOLUTION

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*Kang, Prokudin, Ringer, Yuan (2017)*

NLL TMD evolution

Gaussian Torino model



*functions: Kang, Prokudin, Sun, Yuan (2015)*

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