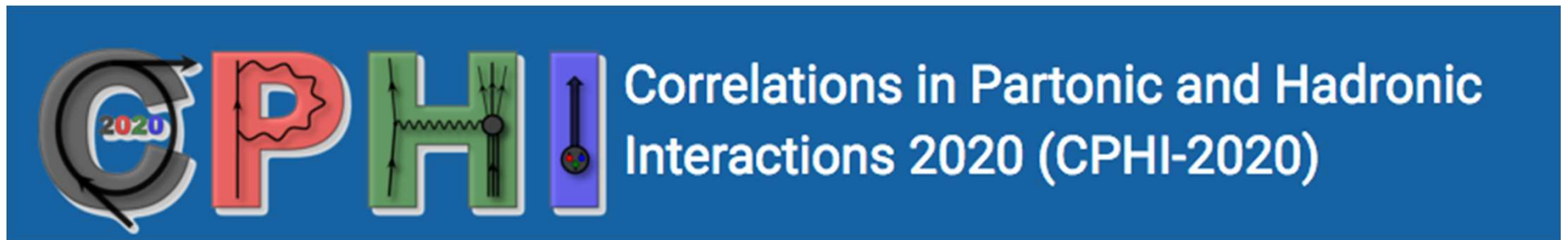


Studies of Spin-Orbit Correlations

H. Avakian (JLab)



- **Understanding azimuthal distributions of hadrons**
- **Introducing studies of SSA**
- **Kotzinian-Mulders Asymmetries**
- **Target fragmentation and Fracture Functions**
- **Correlations of target and current fragmentation**
- **Summary**



ELSEVIER

Nuclear Physics B 441 (1995) 234–256

NUCLEAR
PHYSICS B



New quark distributions and semi-inclusive electroproduction on polarized nucleons

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SIDIS described in the LGHF

laboratory gamma-lepton frame (later known as Trento convention)

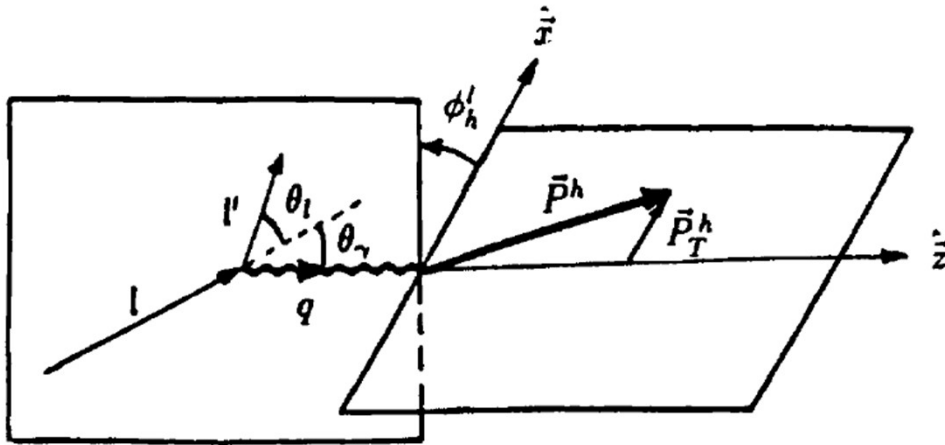


Fig. 2. Lepton and produced hadron momenta in the LGHF.

$$C_{h_{1L}^\perp}^{(S)} = -2(1-y) \sin 2\phi_l^h \frac{P_T^{h2}}{m_D m_F} \sum_q e_q^2 \alpha_{h_{1L}^\perp}^{(S)} (1 - \alpha_{h_{1L}^\perp}^{(S)}) A_{h_{1L}^\perp}^{(S)}. \quad (54)$$

As is clear from (54), one can separate the contributions of $C_{g_{1L}}^{(0)}$ and $C_{h_{1L}^\perp}^{(S)}$ by measuring the target longitudinal-spin asymmetry for different values of ϕ_l^h , P_T^h and y . If the experiment shows that $C_{h_{1L}^\perp}^{(S)} \neq 0$, then one can conclude that both the twist-two DF, h_{1L}^\perp , and FF, $F^{(S)}$, are nonzero. Thus, in principle, it is possible to investigate the Collins effect (a spin dependent FF) with a longitudinally polarized beam and target by analyzing existing SMC semi-inclusive data in different bins of ϕ_l^h , as was done without



Single-Spin Asymmetries in electroproduction

HERMES note 96.059

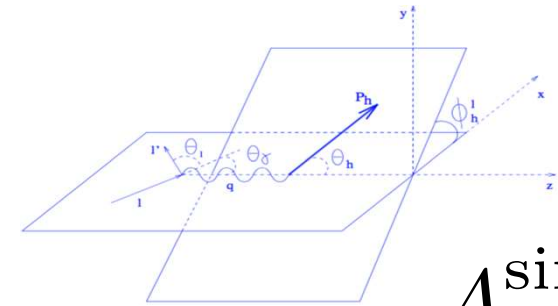
π^0 Electro-production in Deep Inelastic Scattering

H.R.Avakian, P.Di Nezza, V.Gyurjyan, K.Oganessyan

INFN - Laboratori Nazionali di Frascati

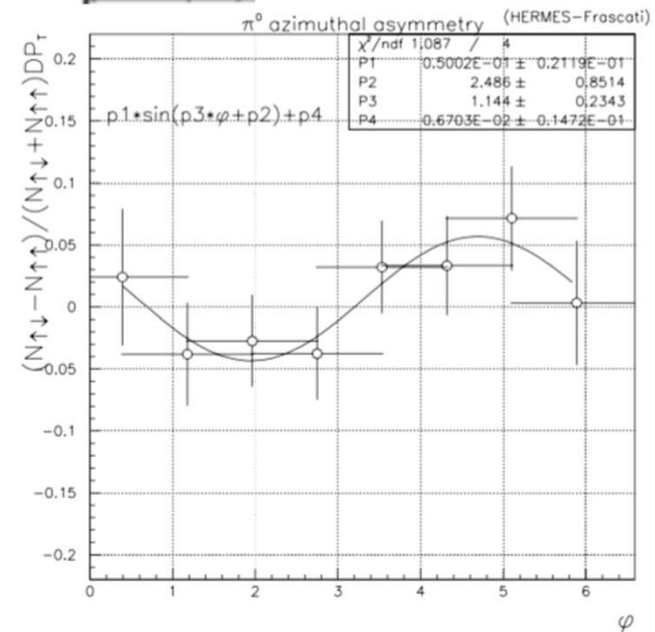
Frascati I-00044, Italy

Dec 1996



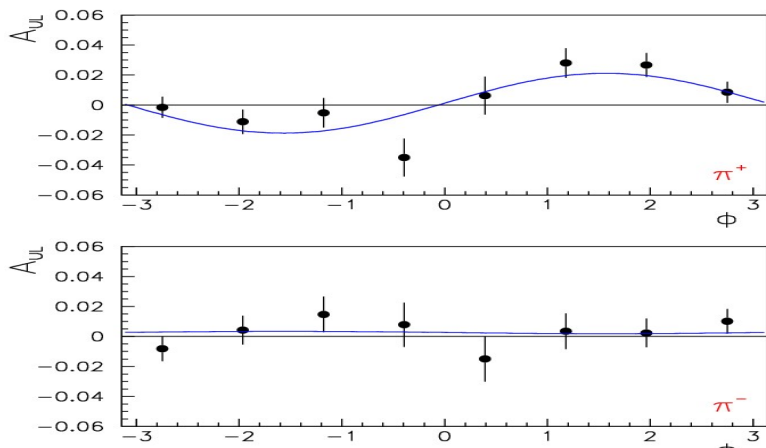
$$A_{UL}^{\sin \phi}$$

$(^3\text{He}-95)$





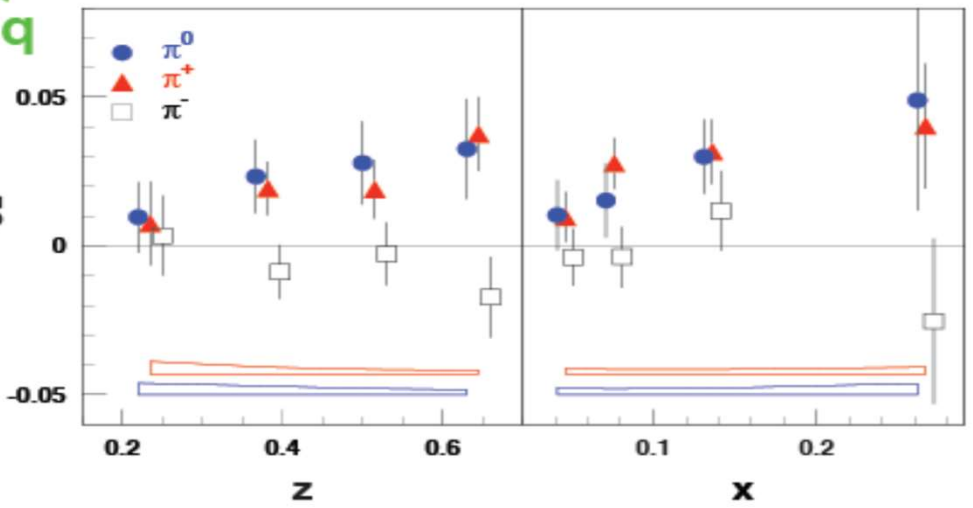
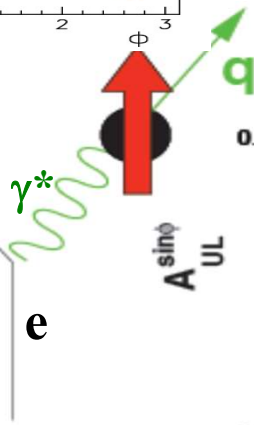
HERMES effect



Transverse with respect to γ^*

Collins
 $A_{UT} \sim (1-y) \mathbf{h}_1 H_1^\perp$

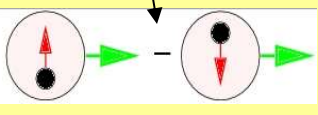
$$\sin \theta_\gamma = \sqrt{\frac{4M^2x^2}{Q^2 + 4M^2x^2} \left(1 - y - \frac{M^2x^2y^2}{Q^2}\right)}$$



First measurement of significant SSA in electroproduction



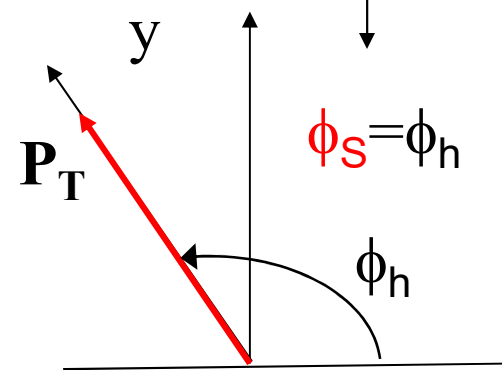
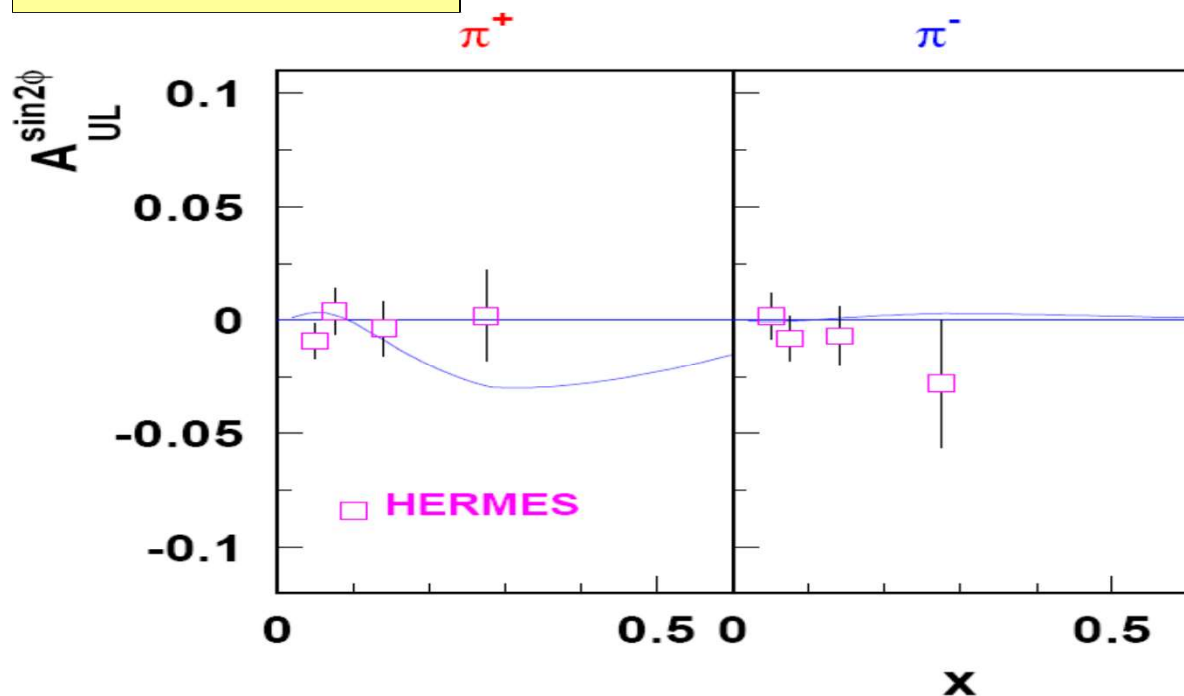
Z^q	U	L	T
U	f_1		h_1^\perp
L		g_1	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

$h_{1L}^\perp =$ 

Kotzinian-Mulders Asymmetry (1996)

$$A_{UL}^{\sin 2\phi} \sim h_{1L}^\perp H_1^\perp \sin 2\phi$$

$$(\mathbf{s}_T \mathbf{k}_T)(\mathbf{p} \mathbf{S}_L) \leftrightarrow h_{1L}^\perp$$



$$\sin(\phi_h + \phi_s) = \sin(2\phi_h)$$

curves, χ QSM
from Efremov et al

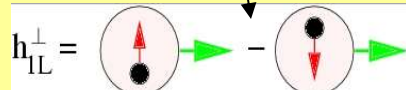
- Study transversely polarized quarks in the longitudinally polarized proton
- Provides independent information on the Collins function.

Collins fragmentation: Longitudinally polarized target

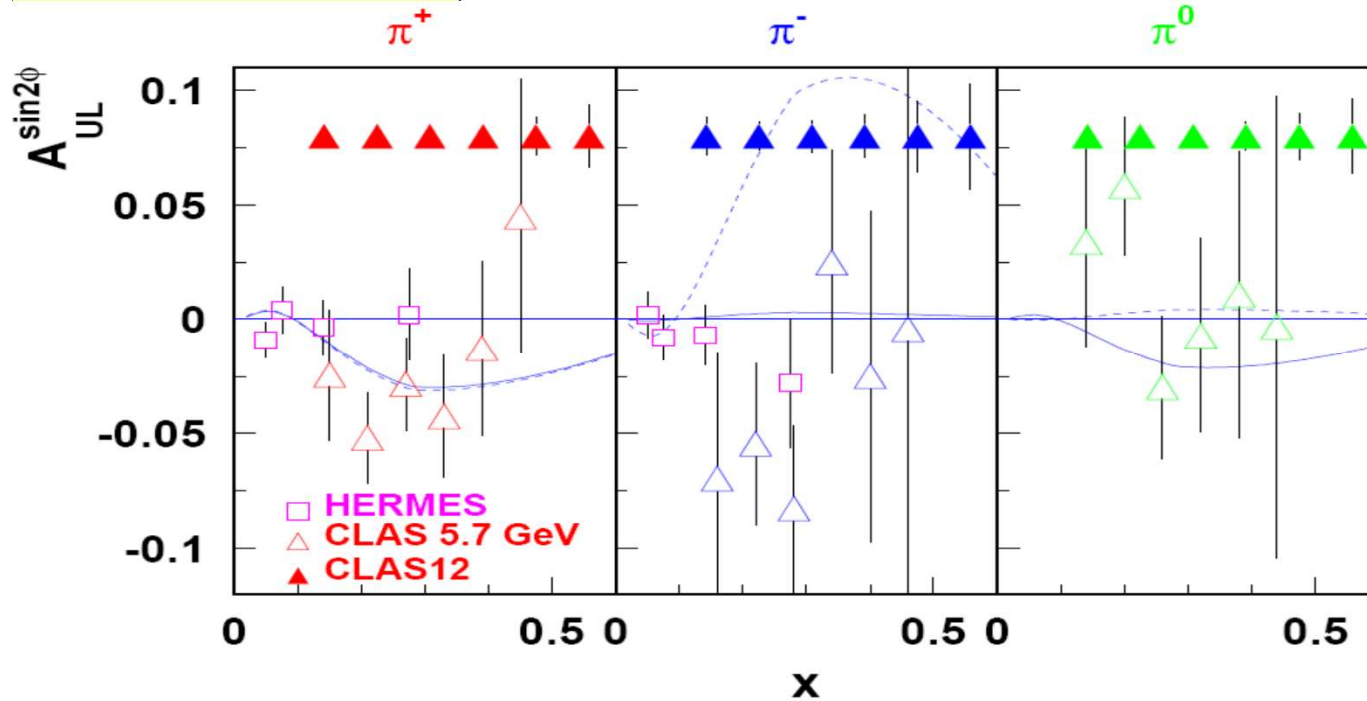
Z/a	U	L	T
U	f_1		h_{1L}^\perp
L		g_1	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	$h_{1L}^\perp, h_{1T}^\perp$

Kotzinian-Mulders Asymmetry

Transversely polarized quarks in the long. polarized nucleon



$$\sigma_{UL}^{KM} \sim h_{1L}^\perp H_1^\perp \sin 2\phi$$




curves, χ QSM from Efremov et al


$$H_1^\perp u \rightarrow \pi^+ \approx -H_1^\perp u \rightarrow \pi^-$$

- KM $\sin 2\phi$ moment, sensitive to spin-orbit correlations: the only leading twist azimuthal moment for longitudinally polarized target
- More info will be available from SIDIS (COMPASS, EIC) and DY (RHIC, GSI)

Quark distributions at large k_T : models

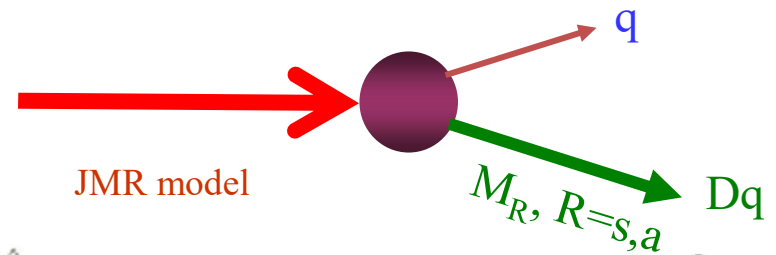



$$u^+(x, k_T) = f_1^u(x, k_T^2) + g_1^u(x, k_T^2)$$




$$u^-(x, k_T) = f_1^u(x, k_T^2) - g_1^u(x, k_T^2)$$

Effect of the orbital motion on the q^- may be most significant

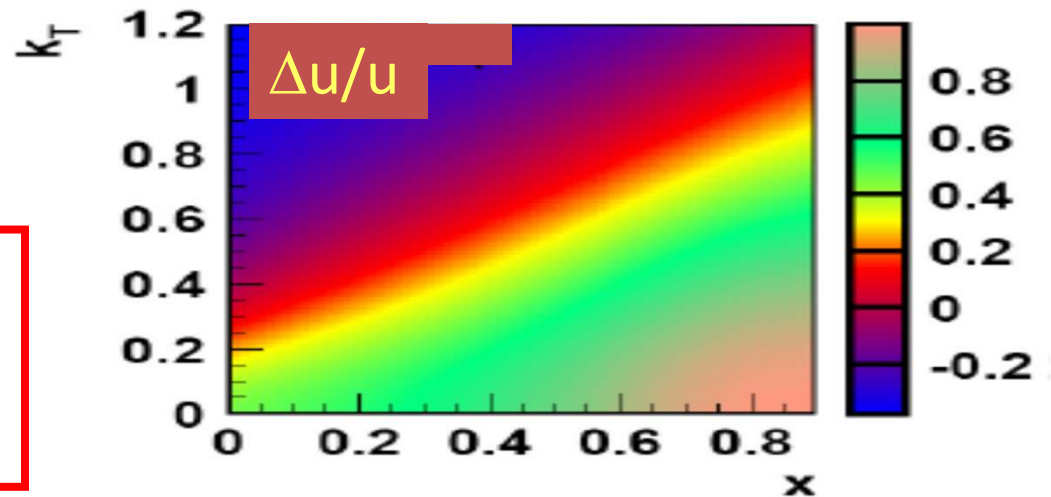




$$u^+(x, \mathbf{k}_T^2) \propto \frac{(xM + m)^2}{(\mathbf{k}_T^2 + \lambda_R^2)^{2\alpha}}$$


$$u^-(x, \mathbf{k}_T^2) \propto \frac{\mathbf{k}_T^2}{(\mathbf{k}_T^2 + \lambda_R^2)^{2\alpha}}$$

Higher probability to find a quark anti-aligned with proton spin at large k_T

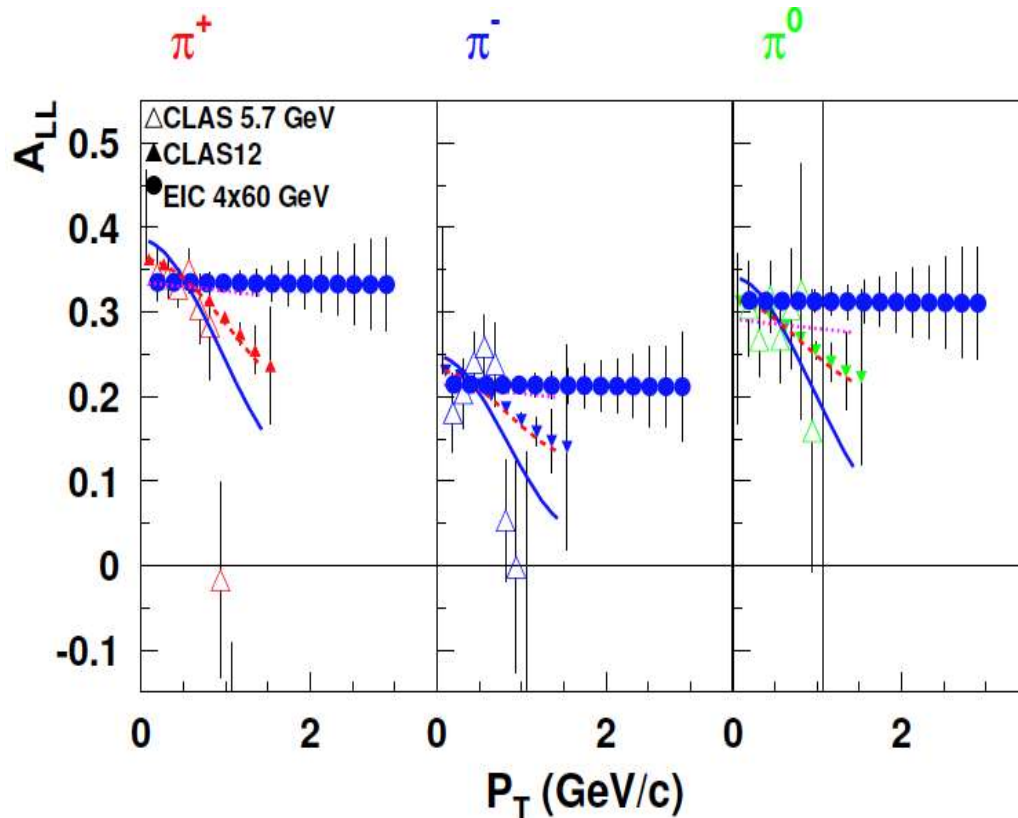


(dipole formfactor), J.Ellis, D-S.Hwang, A.Kotzinian

A_1 P_T -dependence in SIDIS

$$A_1(\pi) \propto \frac{\sum_q e_q^2 g_1^q(x) D_1^{q \rightarrow \pi}(z)}{\sum_q e_q^2 f_1^q(x) D_1^{q \rightarrow \pi}(z)} e^{-z^2 P_T^2 \frac{(\mu_0^2 - \mu_2^2)}{(\mu_D^2 + z^2 \mu_0^2)(\mu_D^2 + z^2 \mu_2^2)}}$$

M. Anselmino et al
hep-ph/0608048



$$f_1^q(x, k_T) = f_1(x) \frac{1}{\pi \mu_0^2} \exp\left(-\frac{k_T^2}{\mu_0^2}\right)$$

$$g_1^q(x, k_T) = g_1(x) \frac{1}{\pi \mu_2^2} \exp\left(-\frac{k_T^2}{\mu_2^2}\right)$$

$$D_1^q(z, p_T) = D_1(z) \frac{1}{\pi \mu_D^2} \exp\left(-\frac{p_T^2}{\mu_D^2}\right)$$

$$\mu_0^2 = 0.25 \text{ GeV}^2$$

$$\mu_D^2 = 0.2 \text{ GeV}^2$$

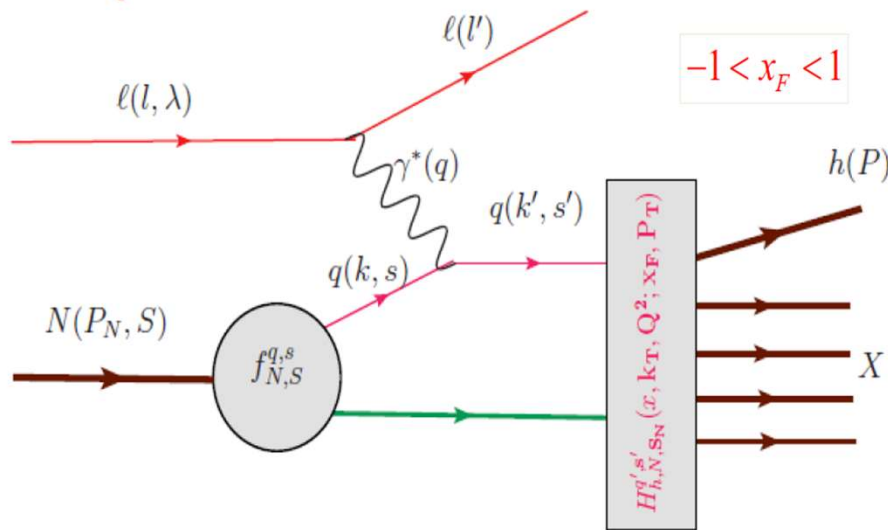
π^+ A_{LL} can be explained in terms of broader k_T distributions for f_1 compared to g_1
 π^- A_{LL} may require non-Gaussian P_T -dependence for different helicities and flavors

Hadronization and factorization

$$F_{XY}^h(x, z, P_T, Q^2) \propto \sum H^q \times f^q(x, k_T, \dots) \otimes D^{q \rightarrow h}(z, p_T, \dots) + Y(Q^2, P_T) + \mathcal{O}(M/Q)$$

$$\int d^2 \vec{k}_T d^2 \vec{p}_T \delta^{(2)}(z \vec{k}_T + \vec{p}_T - \vec{P}_T)$$

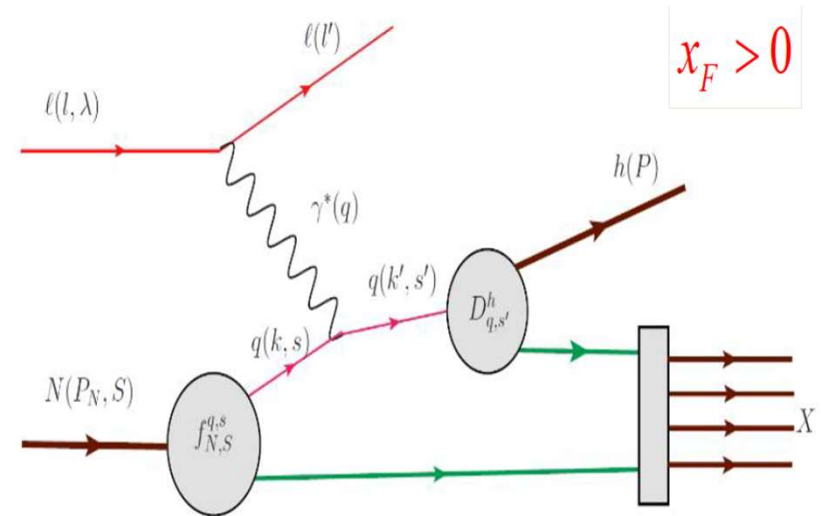
$$Q^2 \gg M_p^2$$



Hadronization Function

→ conditional probability to produce hadron h

$$H_{h/N}^{q'}(x, \mathbf{k}_T, Q^2; x_F, \mathbf{P}_T^h; \mathbf{s}'_q, \mathbf{S}_N)$$

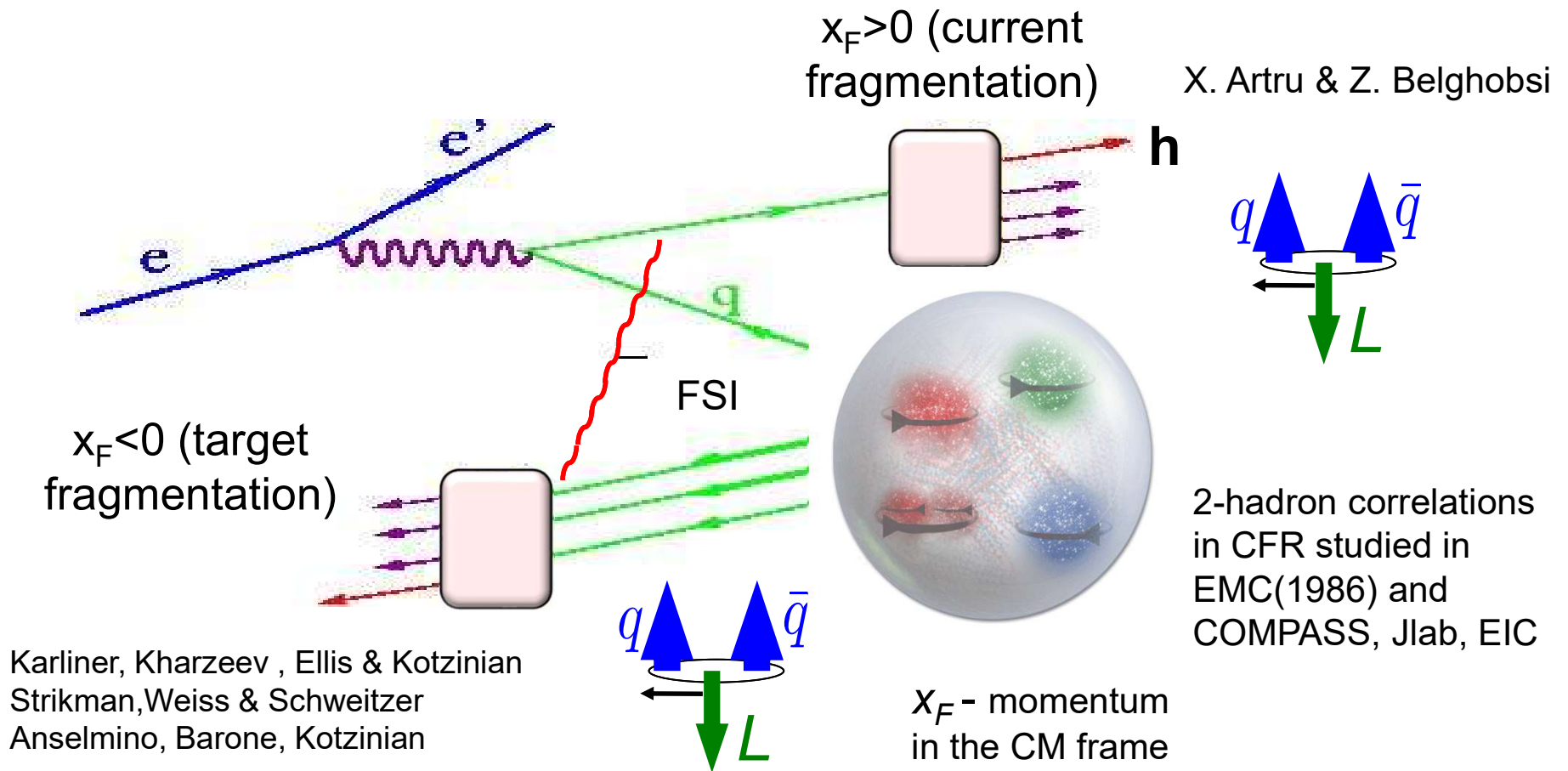


Quark Fragmentation Functions
(universal and independent)

$$D_{q,s'}^h(z, \mathbf{p}_T, Q^2)$$

← Where this works?

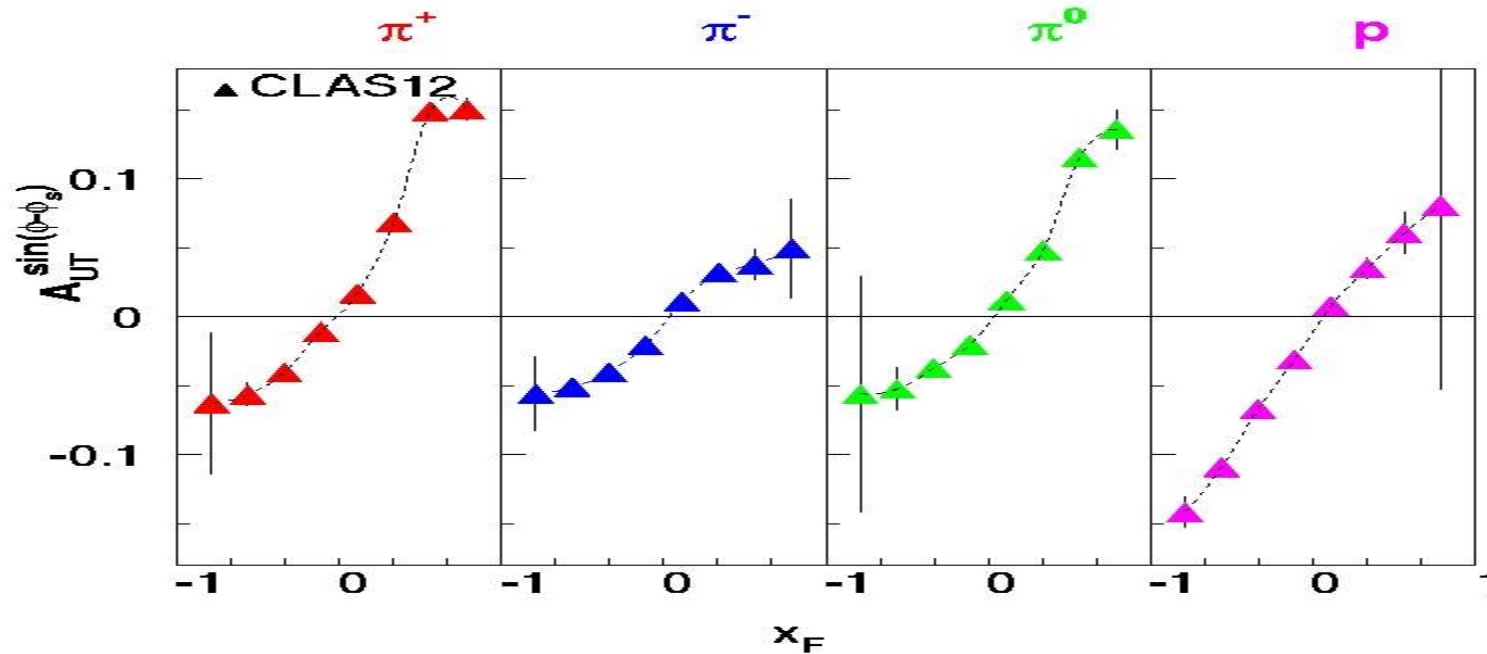
Hadron production in hard scattering



Correlations of the spin of the target or/and the momentum and the spin of quarks, combined with final state interactions define the azimuthal distributions of produced particles

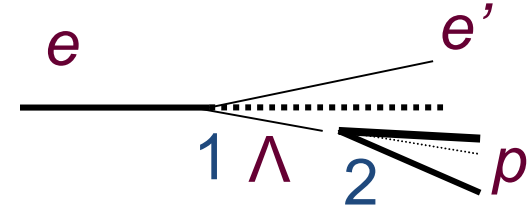
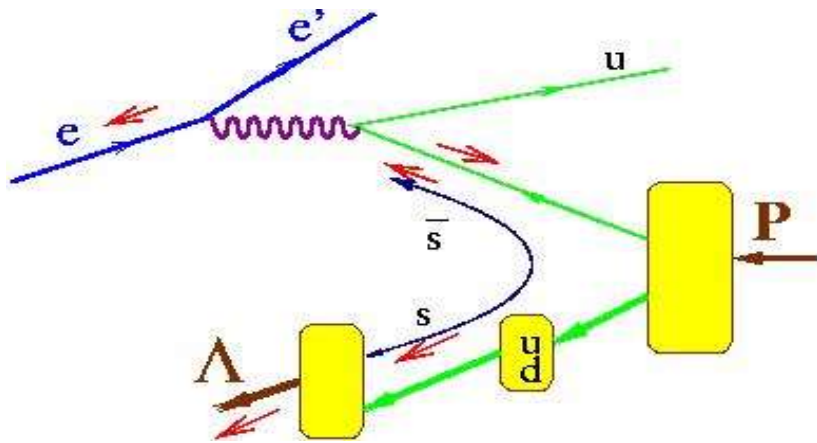
Sivers effect in the target fragmentation

A.Kotzinian

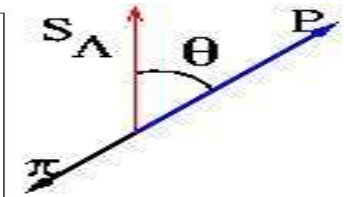
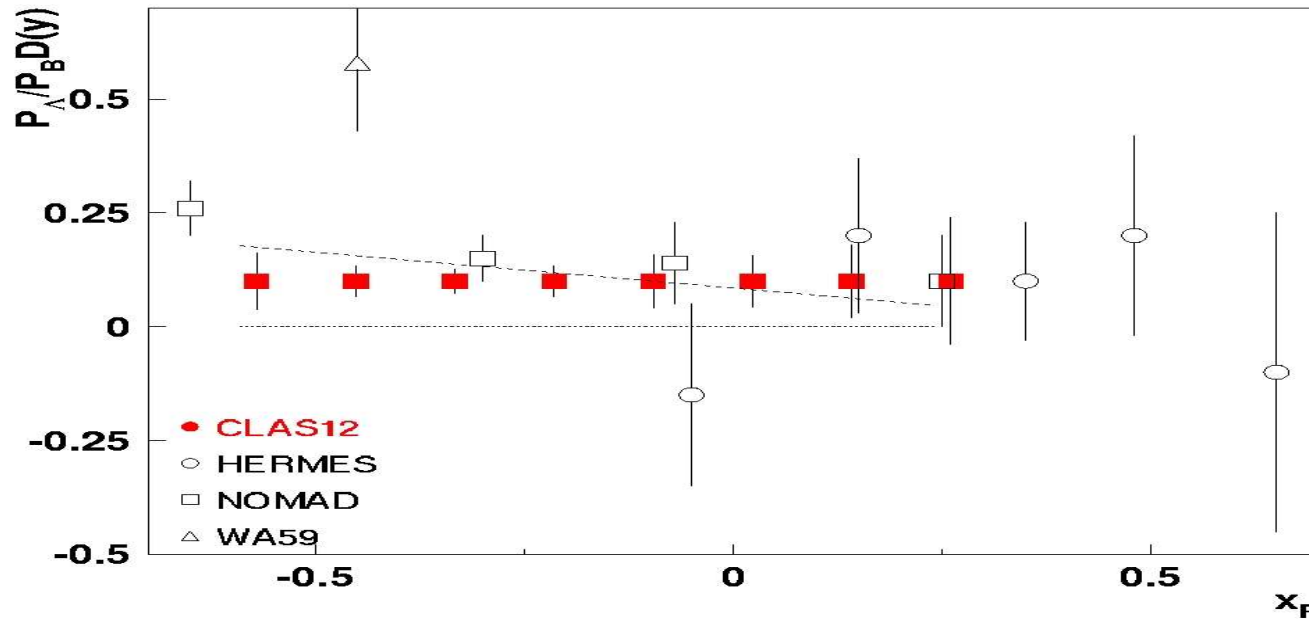


High statistics of **CLAS12** will allow studies of kinematic dependences of the Sivers effect in target fragmentation region

Λ polarization in the target fragmentation



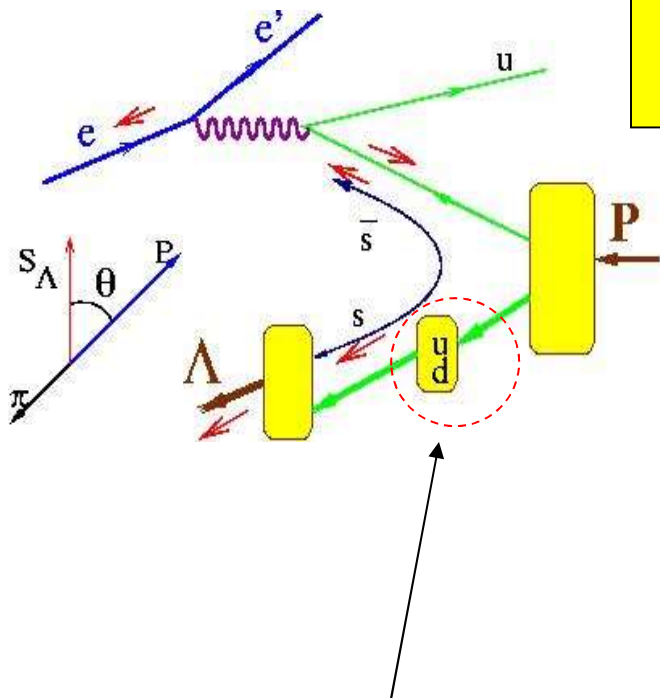
Λ – unique tool for polarization study due to self-analyzing parity violating decay



Wide kinematic coverage of CLAS12 allows studies of hadronization in the target fragmentation region

Λ production in the target fragmentation

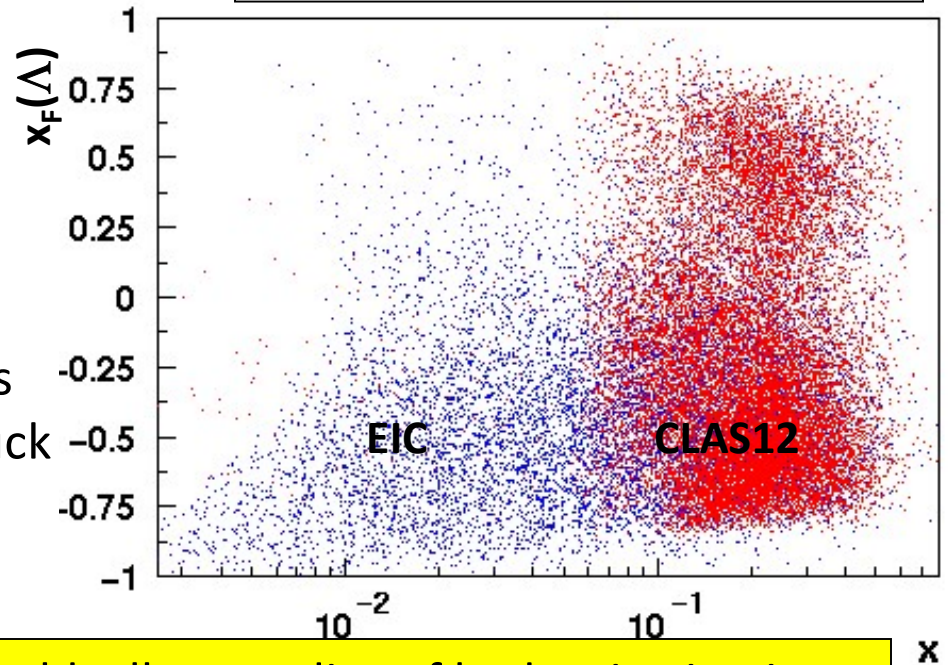
Λ polarization in TFR provides information on contribution of strange sea to proton spin



(ud)-diquark is a spin and isospin singlet s-quark carries whole spin of Λ

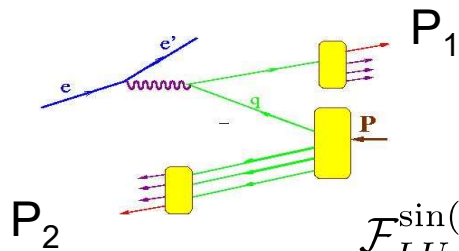
$$|\Lambda\rangle = |uds\rangle$$

Study polarized diquark fracture functions sensitive to the correlations between struck quark transverse momentum and the diquark spin.



Wide kinematical coverage of EIC would allow studies of hadronization in the target fragmentation region (fracture functions)

Target fragmentation in SIDIS

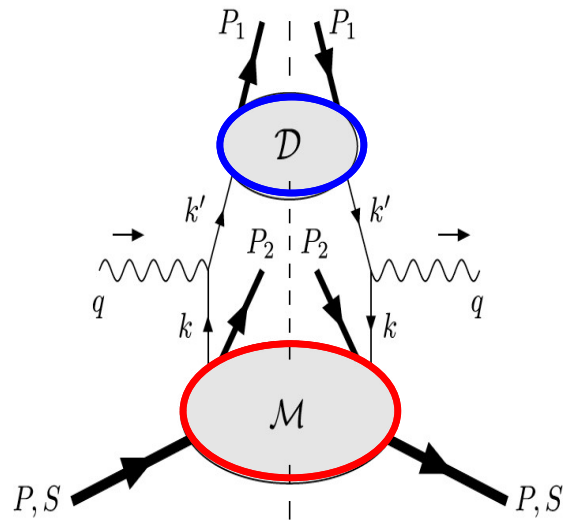


M. Anselmino, V. Barone and A. Kotzinian,
Physics Letters B 713 (2012)

$$\mathcal{F}_{LU}^{\sin(\phi_1 - \phi_2)} = \frac{|\vec{P}_{1\perp} \vec{P}_{2\perp}|}{m_N m_2} C[w_5 M_L^{\perp,h} D_1]$$

Leading Twist

	U	L	T
U	M	$M_L^{\perp,h}$	M_T^h, M_T^{\perp}
L	$\Delta M^{\perp,h}$	ΔM_L	$\Delta M_T^h, \Delta M_T^{\perp}$
T	$\Delta_T M_T^h, \Delta_T M_T^{\perp}$	$\Delta_T M_L^h, \Delta_T M_L^{\perp}$	$\Delta_T M_T, \Delta_T M_T^{hh}, \Delta_T M_T^{\perp\perp}, \Delta_T M_T^{\perp h}$



The beam–spin asymmetry appears, at leading twist and low transverse momenta, in the deep inelastic inclusive lepto-production of two hadrons, one in the target fragmentation region and one in the current fragmentation region.

$$\mathcal{A}_{LU} = -\frac{y(1 - \frac{y}{2})}{(1 - y + \frac{y^2}{2})} \frac{\mathcal{F}_{LU}^{\sin \Delta\phi}}{\mathcal{F}_{UU}} \sin \Delta\phi$$

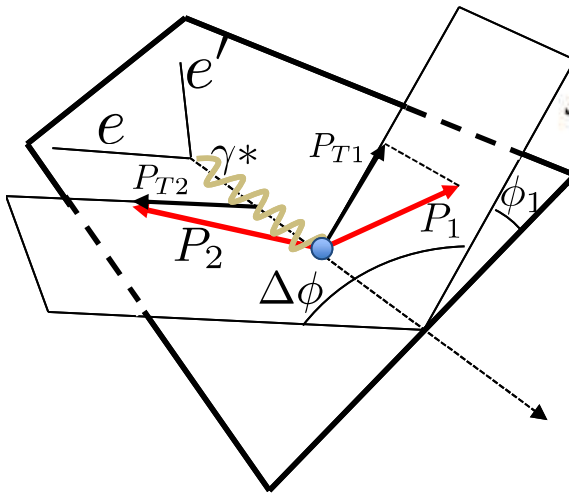
Understanding of Target Fragmentation Region (TFR) is important for interpretation of the Current FR

- Need a consistent theoretical description for TFR
- Measure/model fracture functions

B2B hadron production in SIDIS: First measurements

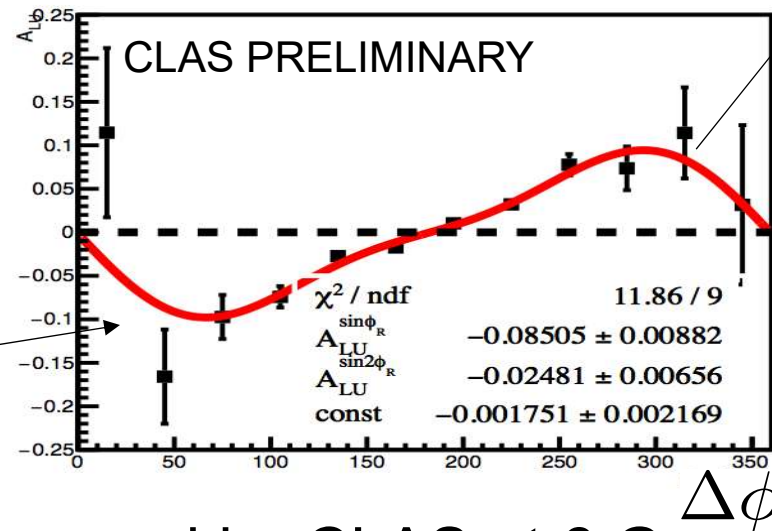
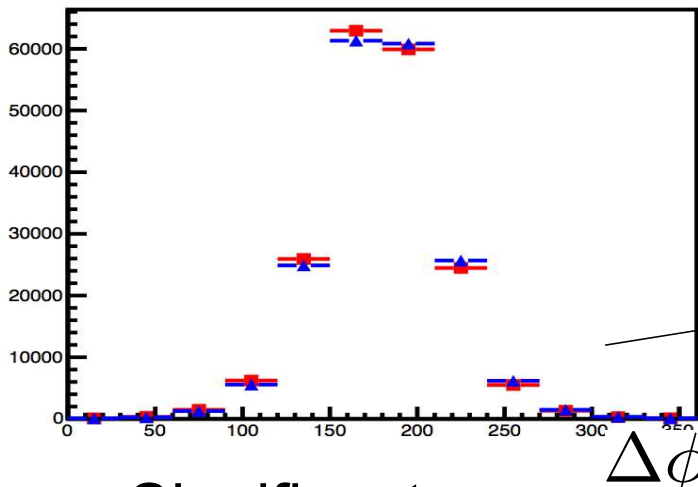
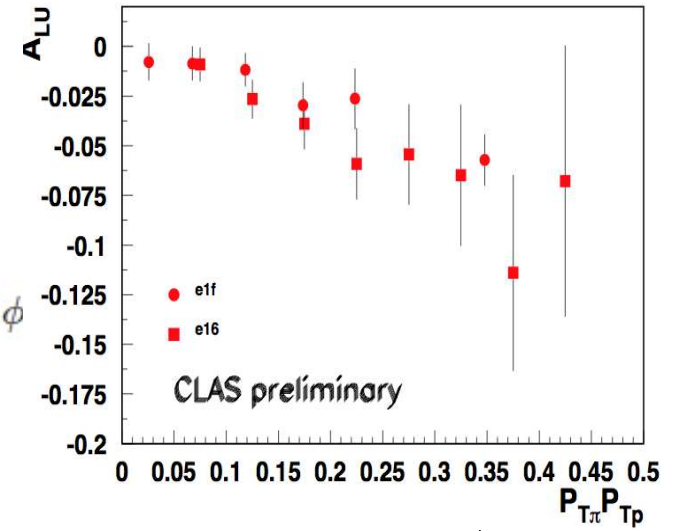
M. Anselmino, V. Barone and A. Kotzinian,
Physics Letters B 713 (2012)

$$ep \rightarrow e' p \pi^+ X$$



$$A_{LU} = -\frac{y(1-\frac{y}{2})}{(1-y+\frac{y^2}{2})} \frac{\mathcal{F}_{LU}^{\sin \Delta \phi}}{\mathcal{F}_{UU}} \sin \Delta \phi$$

$$= -\frac{|P_{1\perp}||P_{2\perp}|}{m_N m_2} \frac{y(1-\frac{y}{2})}{(1-y+\frac{y^2}{2})} \frac{C[w_5 M_L^{\perp, h} D_1^1]}{C[MD_1]} \sin \Delta \phi$$



Significant asymmetries observed by CLAS at 6 GeV

SUMMARY

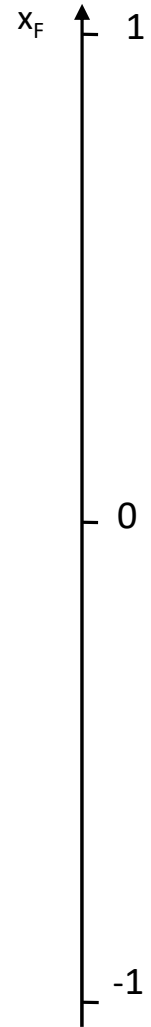
Correlations play a crucial role in non perturbative dynamics

Close communication of theorists and experimentalists was critical in extraction and interpretation of all kind of spin-azimuthal asymmetries

Target fragmentation can be an important (so far undervalued) domain for understanding of the partonic interactions and correlations

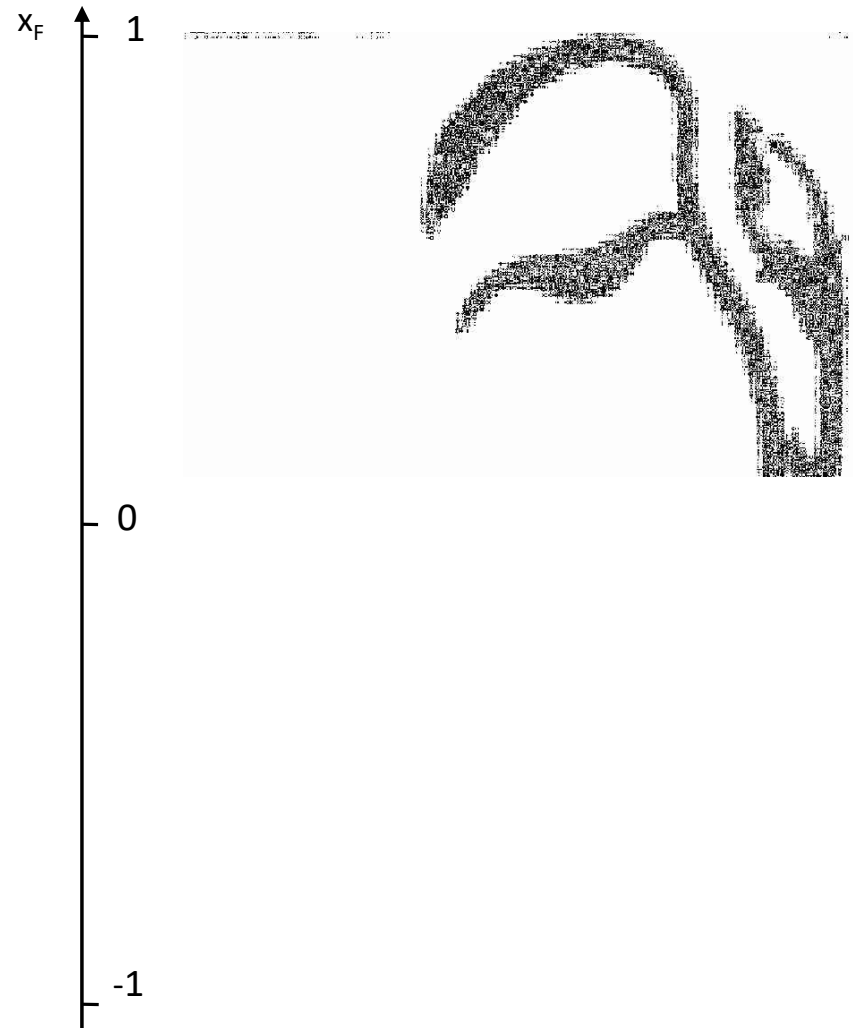
A proper visualization of the nucleon structure will require understanding of target fragmentation

CFR



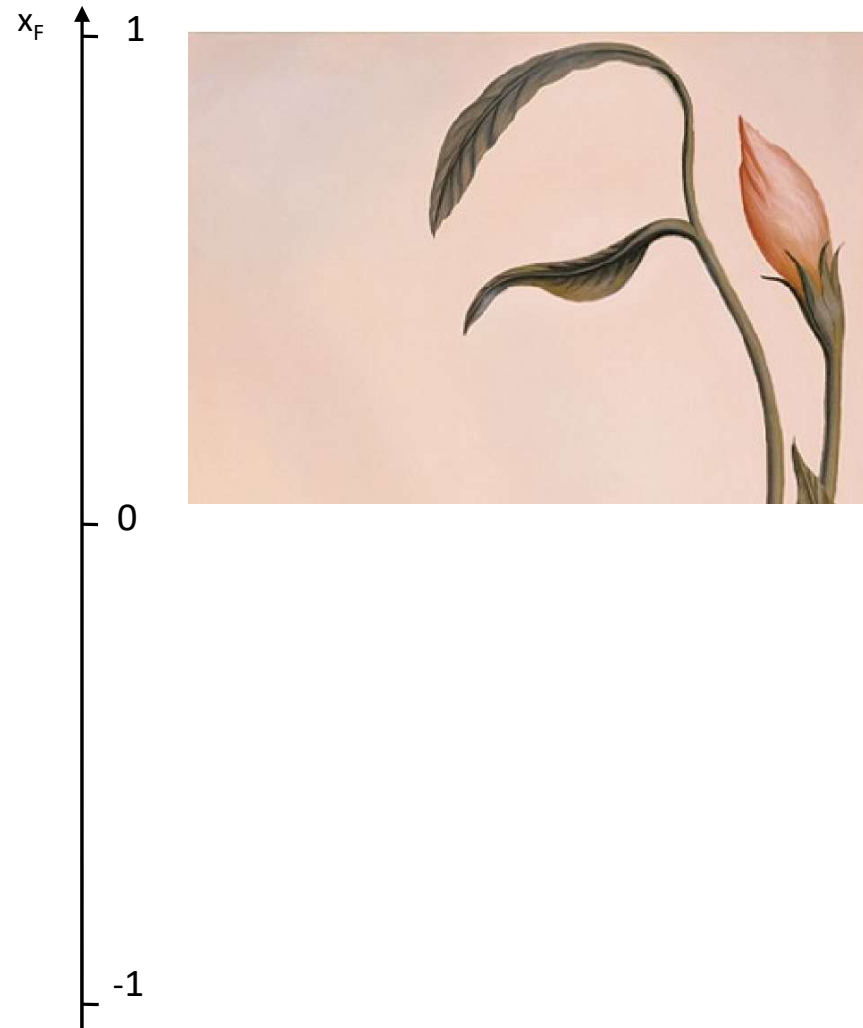
Saclay, 18-Nov-16

Larger phase space
higher W, z, x
different asymmetries

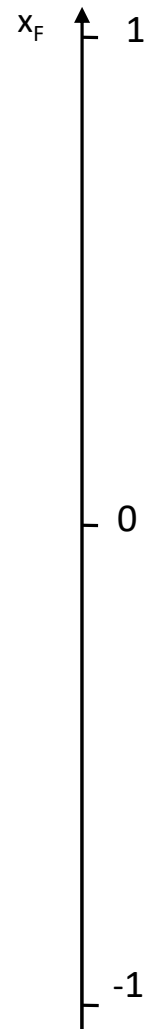


Saclay, 18-Nov-16

Better resolution,
higher statistics



Saclay, 18-Nov-16

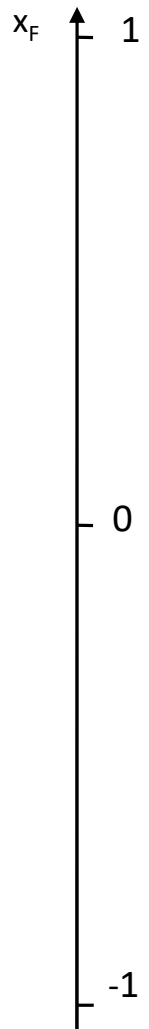


TFR with good resolution etc



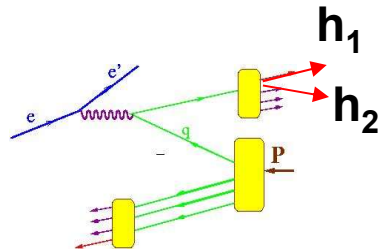
Saclay, 18-Nov-16

Full picture can be surprising and beautiful



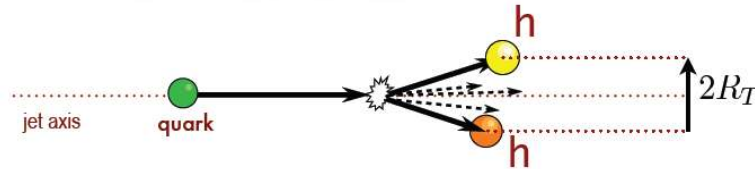
Support slides

Hadronization in current and target regions



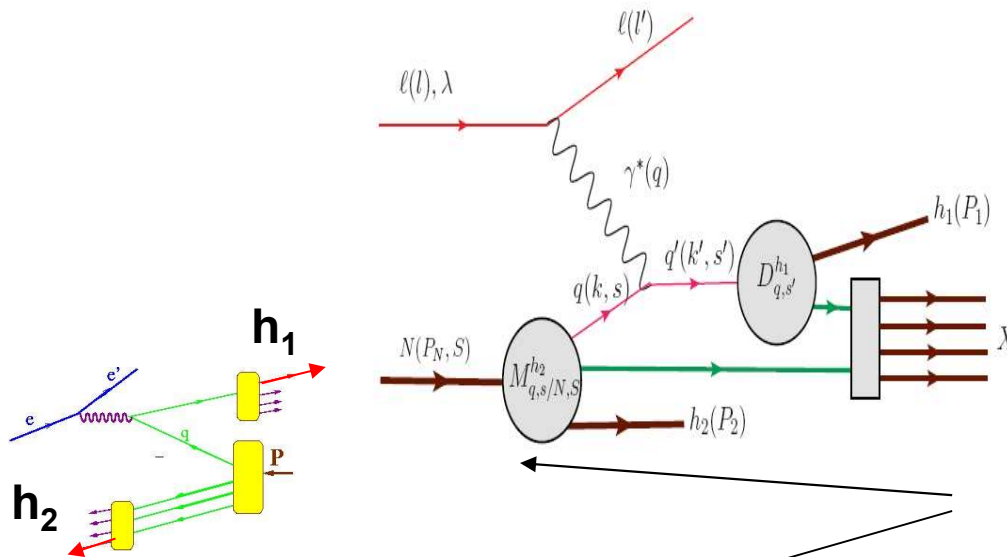
◆ DIFF

$$D_1^{q \rightarrow h_1 h_2}(z_1, z_2, R_T^2)$$



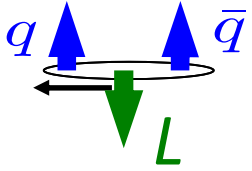
Collinear factorization

Anselmino/Barone/Kotzinian
arXiv:1107.2292 (2011)

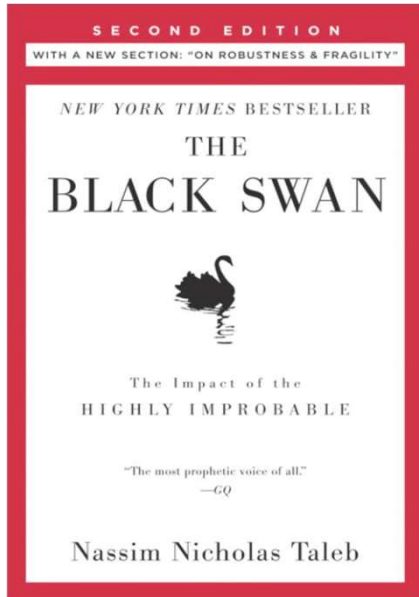


Fracture Function:
conditional probabilities to find a quark with certain polarization and longitudinal momentum fraction x_B and transverse momentum k_T inside a nucleon fragmenting into a hadron carrying a fraction z of the nucleon longitudinal momentum and a transverse momentum P_T

$$\sigma_{LU} = -\frac{P_{T1} P_{T2}}{m_2 m_N} F_{k1}^{\Delta \hat{g}_1^{\perp h} \cdot D_1} \sin(\phi_1 - \phi_2).$$



SSAs: Black Swans of Nucleon Structure



1. **rarity**: it is an outlier, as it lies outside the realm of regular expectations, because *nothing in the past can convincingly point to its possibility*.
2. **it carries an extreme impact**.
3. **retrospective** (not prospective)
predictability: in spite of its outlier status, human nature makes us concoct explanations for its occurrence *after the fact, making it explainable and predictable*.



One single observation can invalidate a general statement derived from millennia of confirmatory sightings of millions of white swans. All you need is one single (ugly) black bird.



Three stages for new phenomena

Any unexplained phenomenon passes through three stages before the reality of it is accepted.

- During the first stage it is considered **laughable**.
- During the second stage, it is **adamantly opposed**.
- Finally, during the third stage, it is accepted as **self-evident**.

Arthur Schopenhauer