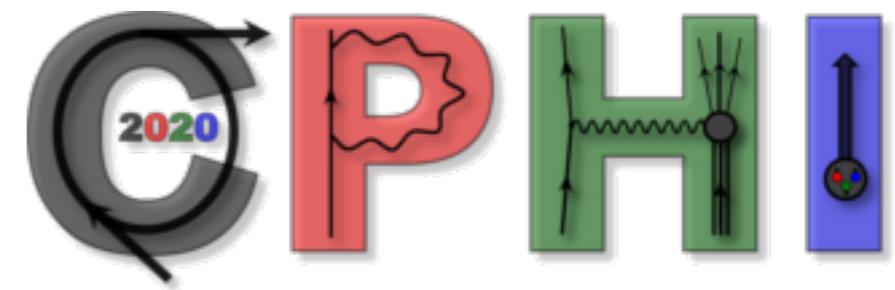
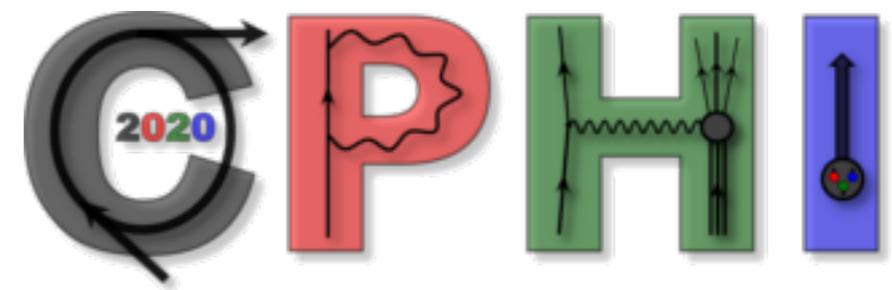


Correlations in Partonic and Hadronic  
Interactions (CPHI-2020)  
CERN, February 3-7, 2020



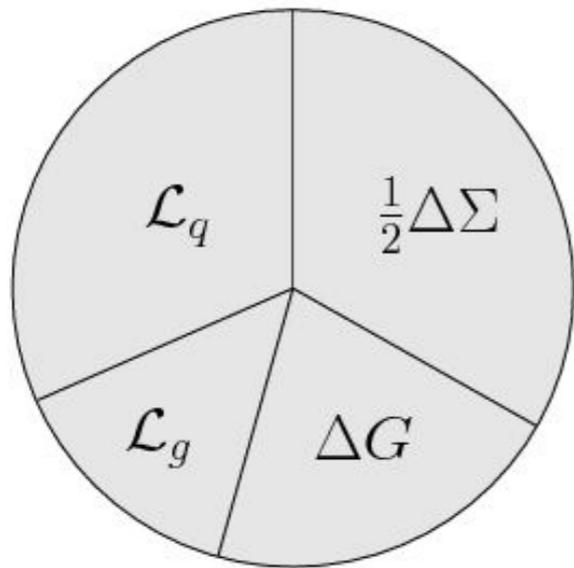
Recent HERMES results on polarized semi-  
inclusive deep-inelastic scattering

Correlations in Partonic and Hadronic  
Interactions (CPHI-2020)  
CERN, February 3-7, 2020



Longitudinal double-spin asymmetries in  
semi-inclusive DIS of electrons and  
positrons by protons and deuterons  
[PRD 99 (2019) 112001]

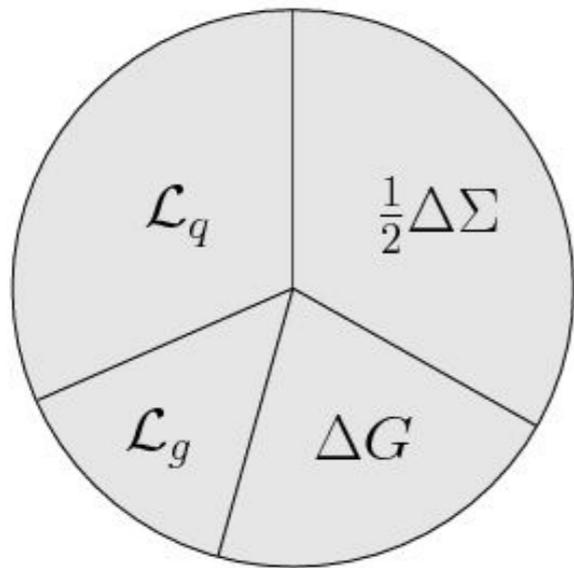
# Access to angular momentum in (SI)DIS



‘pizza quattro stagioni’

[M. Burkardt]

# Access to angular momentum in (SI)DIS

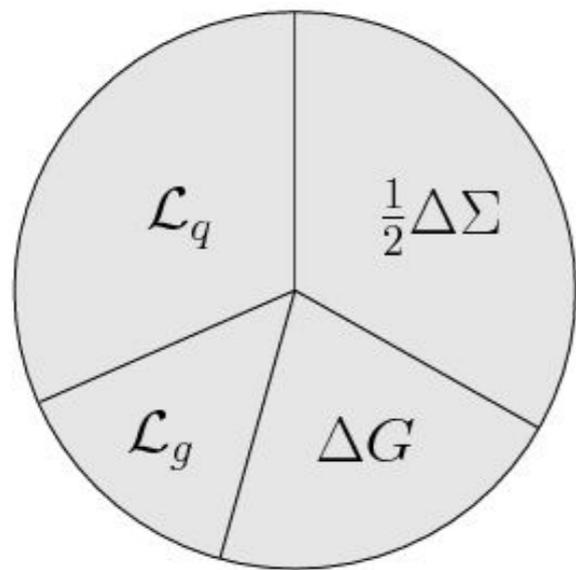


'pizza quattro stagioni'

[M. Burkardt]

← evolution, high- $p_T$  hadrons  
[better: polarized pp]

# Access to angular momentum in (S)DIS



'pizza quattro stagioni'

[M. Burkardt]

(semi-)inclusive  
longitudinal double-spin  
asymmetries

evolution, high- $p_T$  hadrons  
[better: polarized pp]

# ... other paths to the proton structure

Z. Phys. C 69, 467–474 (1996)

**ZEITSCHRIFT  
FÜR PHYSIK C**  
© Springer-Verlag 1996

## The proton spin puzzle and $\Lambda$ polarization in deep-inelastic scattering

John Ellis<sup>1,★</sup>, Dmitri Kharzeev<sup>1,2,★★</sup>, Aram Kotzinian<sup>3,4,★★★</sup>

PHYSICAL REVIEW D

VOLUME 54, NUMBER 1

1 JULY 1996

## Longitudinal quark polarization in transversely polarized nucleons

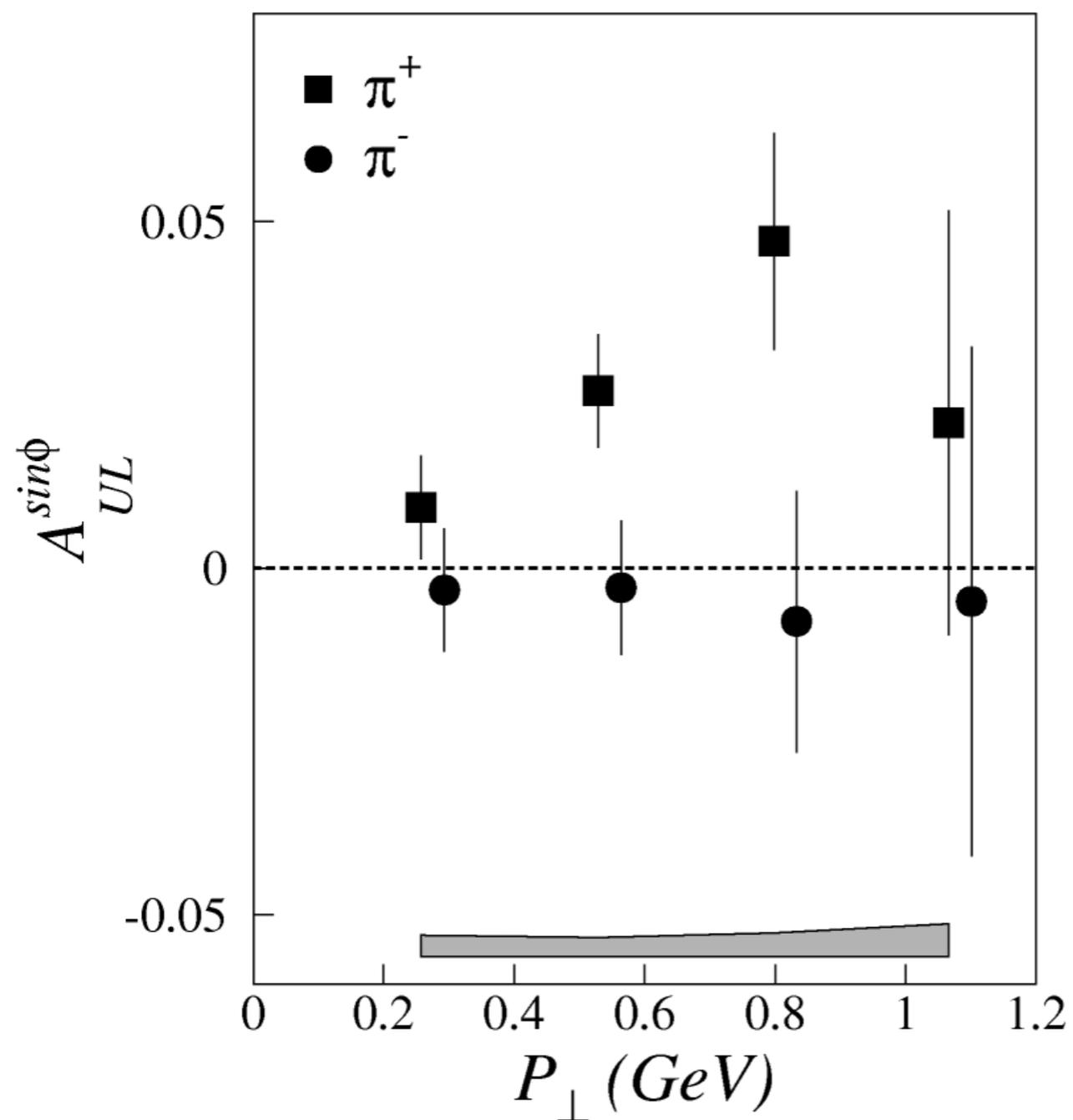
A. M. Kotzinian<sup>\*</sup>

*Yerevan Physics Institute, Alikhanian Brothers St. 2, AM-375036, Yerevan, Armenia*

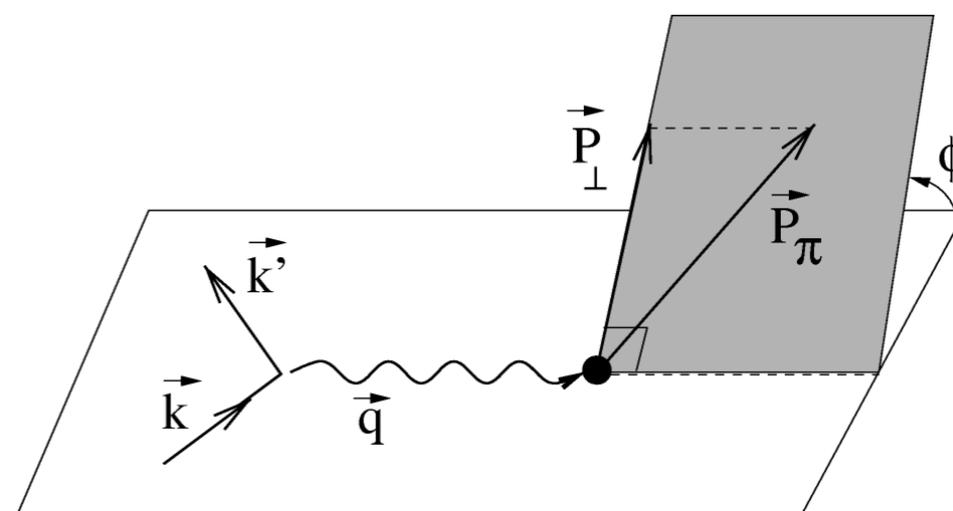
P. J. Mulders<sup>†</sup>

*Department of Physics and Astronomy, Free University of Amsterdam and National Institute for Nuclear Physics and High-Energy Physics, P.O. Box 41882, NL-1009 DB Amsterdam, The Netherlands*

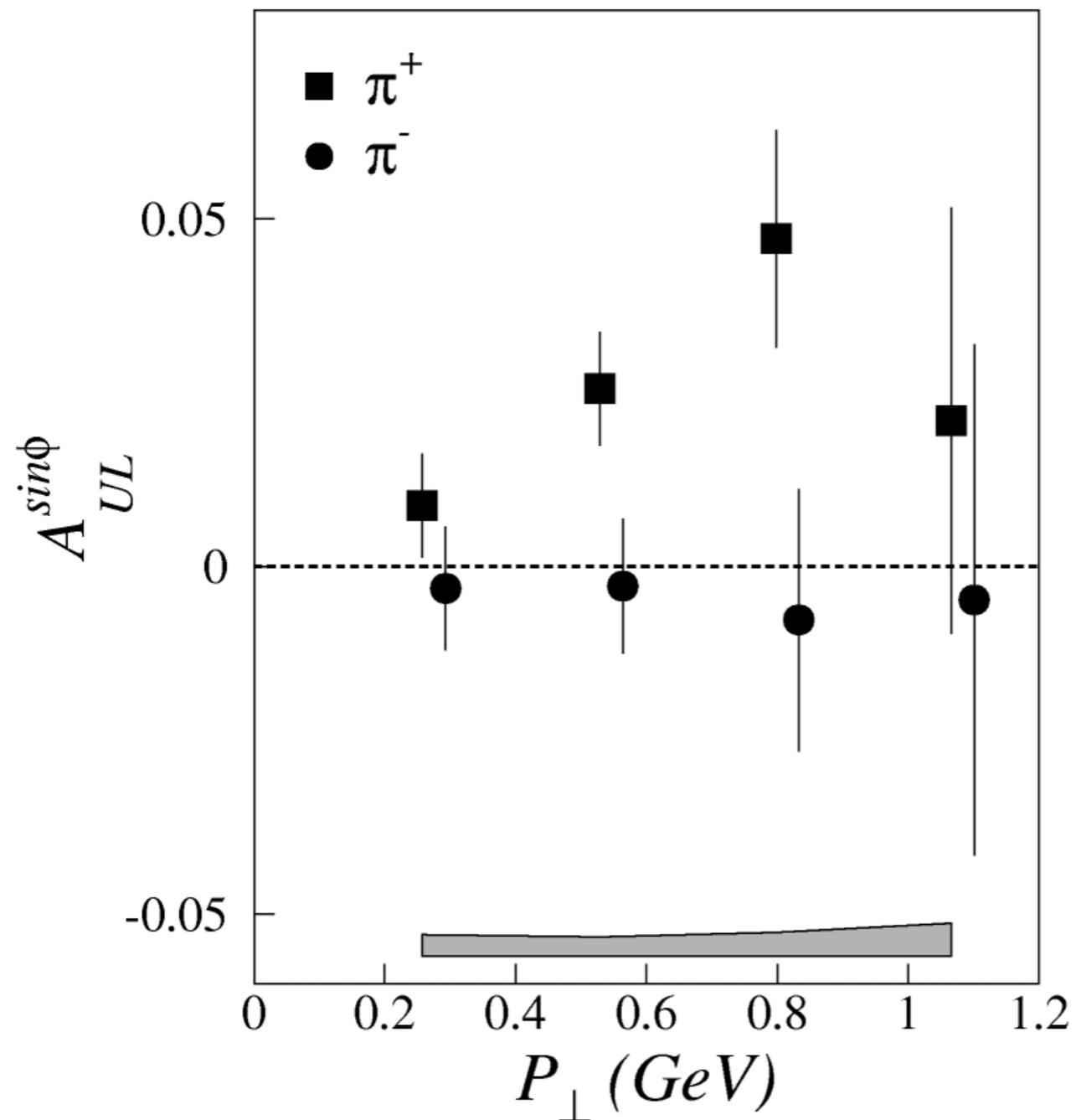
# Evidence for a Single-Spin Azimuthal Asymmetry in Semi-inclusive Pion Electroproduction



$$A_{UL} = \frac{1}{|P_B|} \frac{N^{\rightarrow}(\phi) - N^{\leftarrow}(\phi)}{N^{\rightarrow}(\phi) + N^{\leftarrow}(\phi)}$$

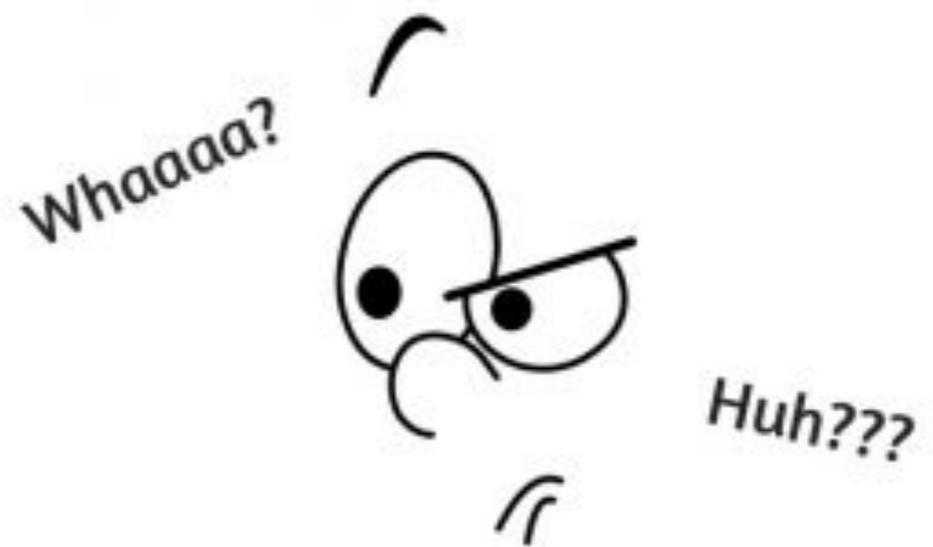


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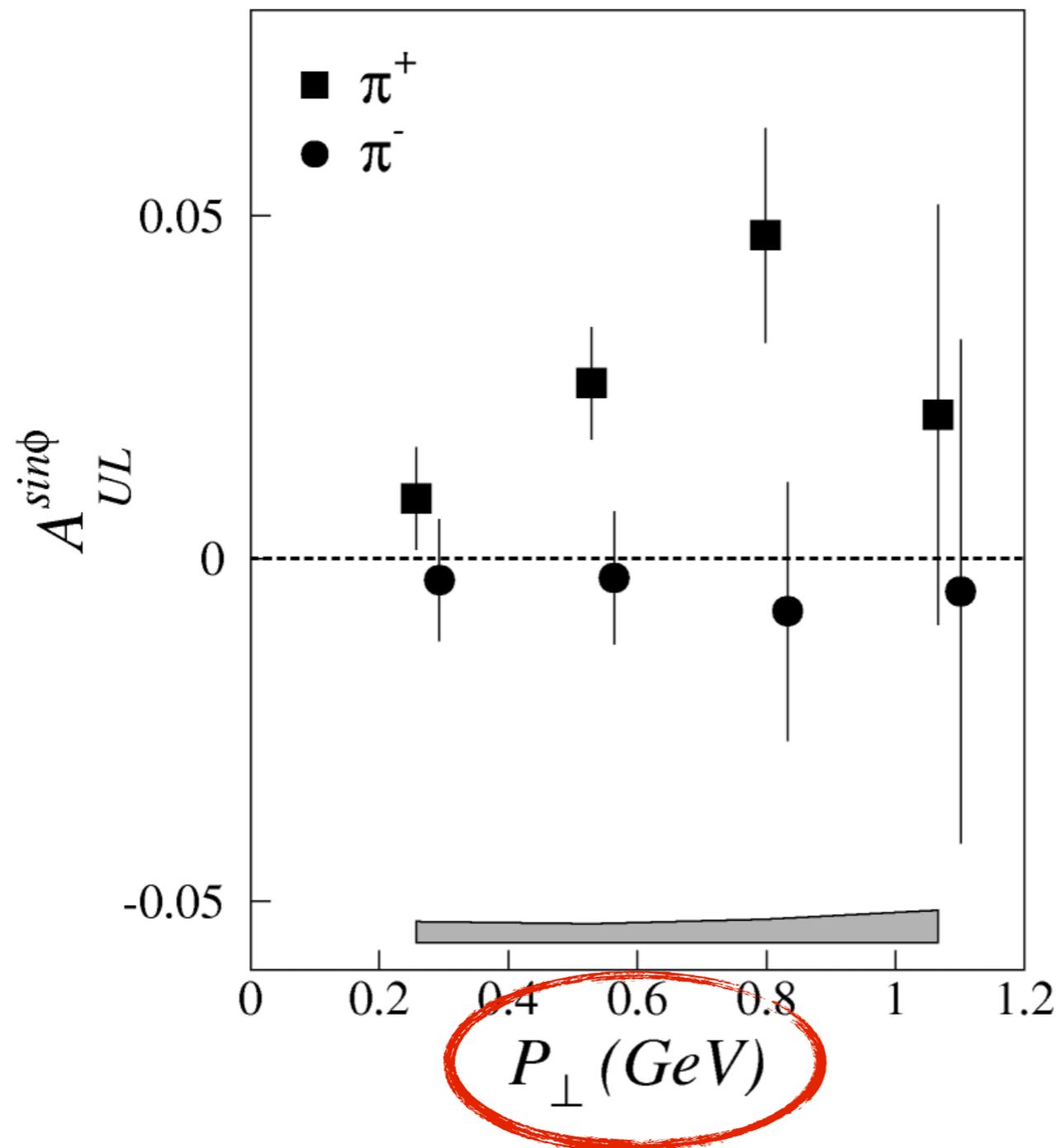


$$A_{UL} = \frac{1}{|P_B|} \frac{N^{\rightarrow}(\phi) - N^{\leftarrow}(\phi)}{N^{\rightarrow}(\phi) + N^{\leftarrow}(\phi)}$$

$$\sim \sin \phi ?$$

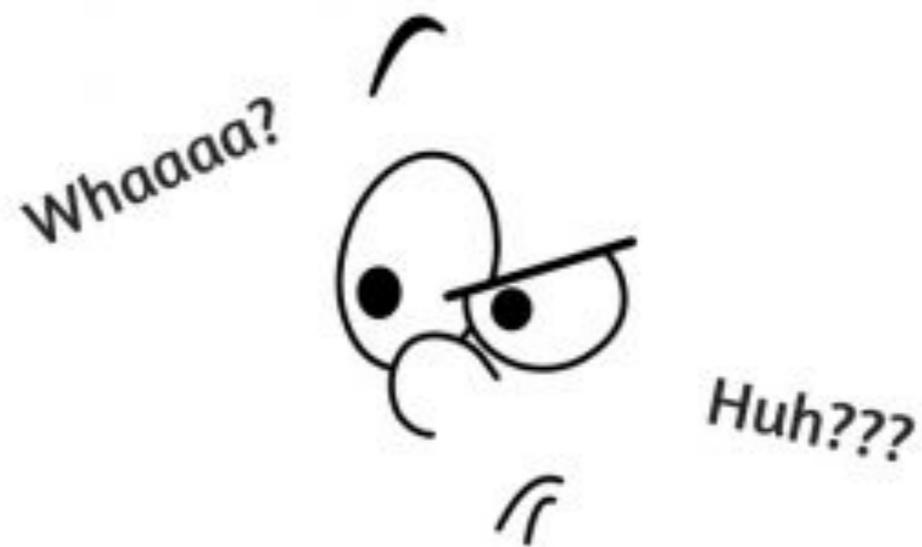


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Physics Letters B 530 (2002) 99–107

PHYSICS LETTERS B

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# Final-state interactions and single-spin asymmetries in semi-inclusive deep inelastic scattering <sup>☆</sup>

Stanley J. Brodsky <sup>a</sup>, Dae Sung Hwang <sup>a,b</sup>, Ivan Schmidt <sup>c</sup>

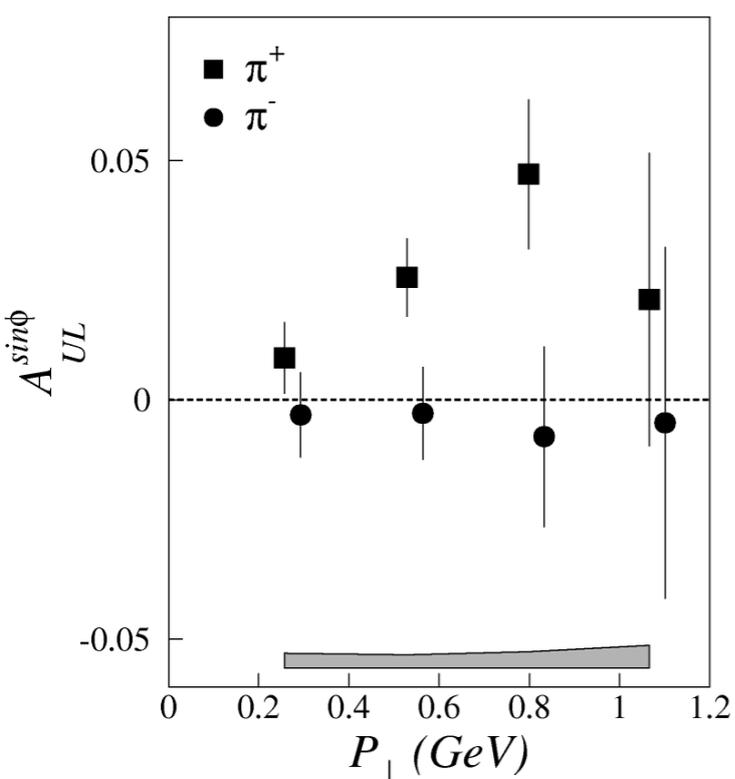
<sup>a</sup> *Stanford Linear Accelerator Center, Stanford University, Stanford, CA 94309, USA*

<sup>b</sup> *Department of Physics, Sejong University, Seoul 143-747, South Korea*

<sup>c</sup> *Departamento de Física, Universidad Técnica Federico Santa María, Casilla 110-V, Valparaíso, Chile*

Received 2 February 2002; accepted 2 February 2002

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PHYSICS LETTERS B

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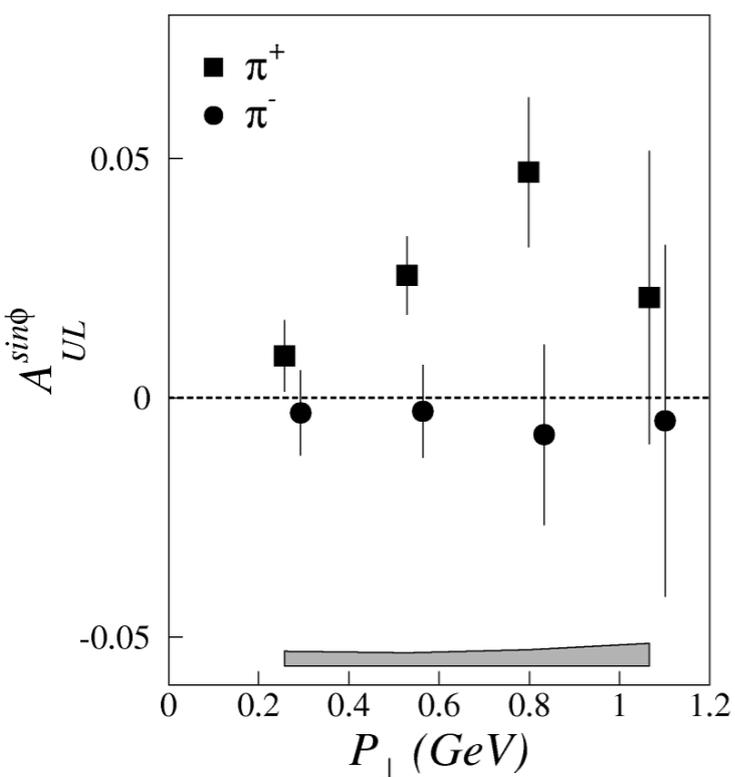
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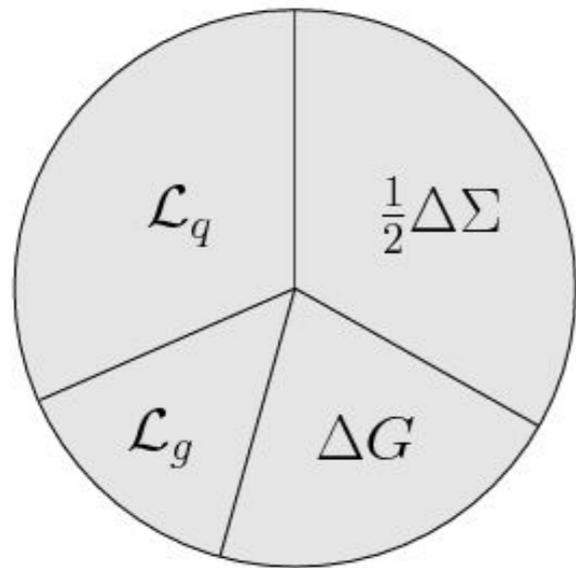
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# Access to angular momentum in (SI)DIS



'pizza quattro stagioni'

[M. Burkardt]

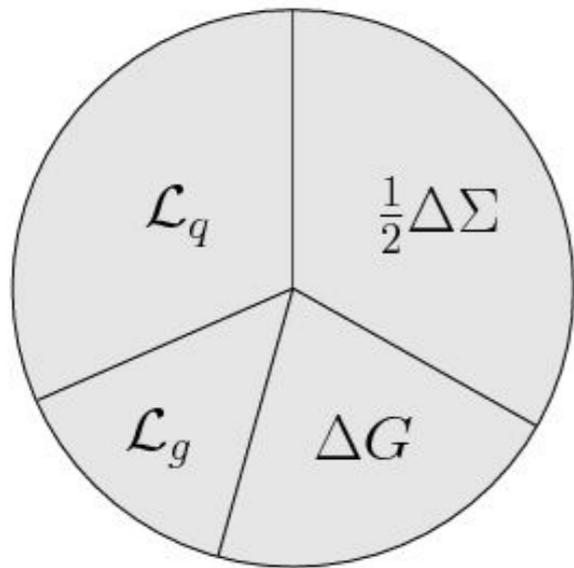
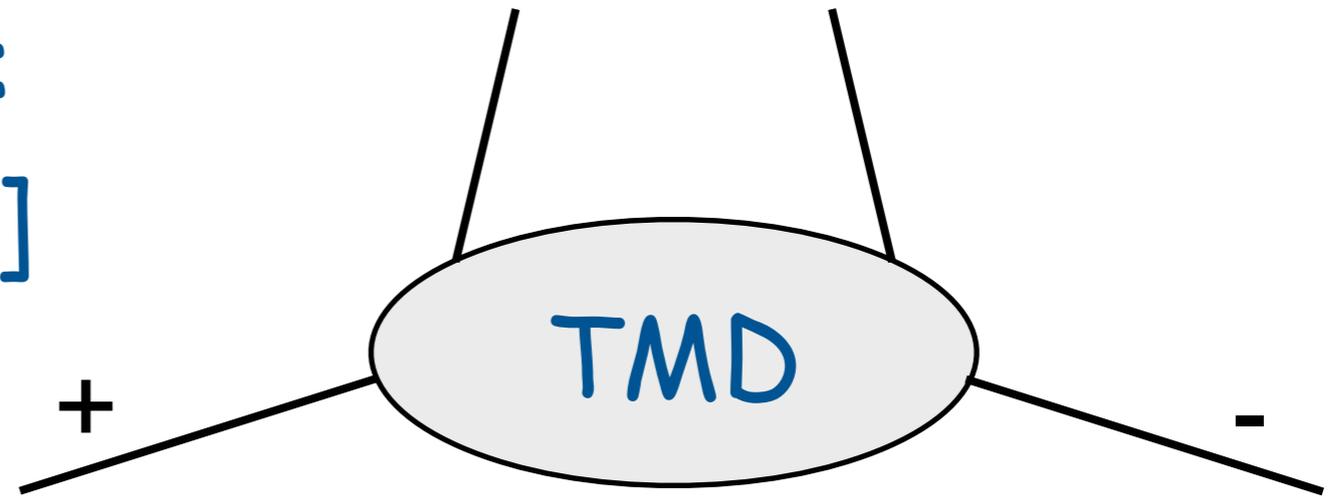
(semi-)inclusive  
longitudinal double-spin  
asymmetries

evolution, high- $p_T$  hadrons  
[better: polarized pp]

# Access to angular momentum in (SI)DIS

TMDs? (SIDIS):  
[better(?): GPDs]

$$\Delta\mathcal{L}_q = \pm 1 (\text{or } 2)$$



(semi-)inclusive  
longitudinal double-spin  
asymmetries

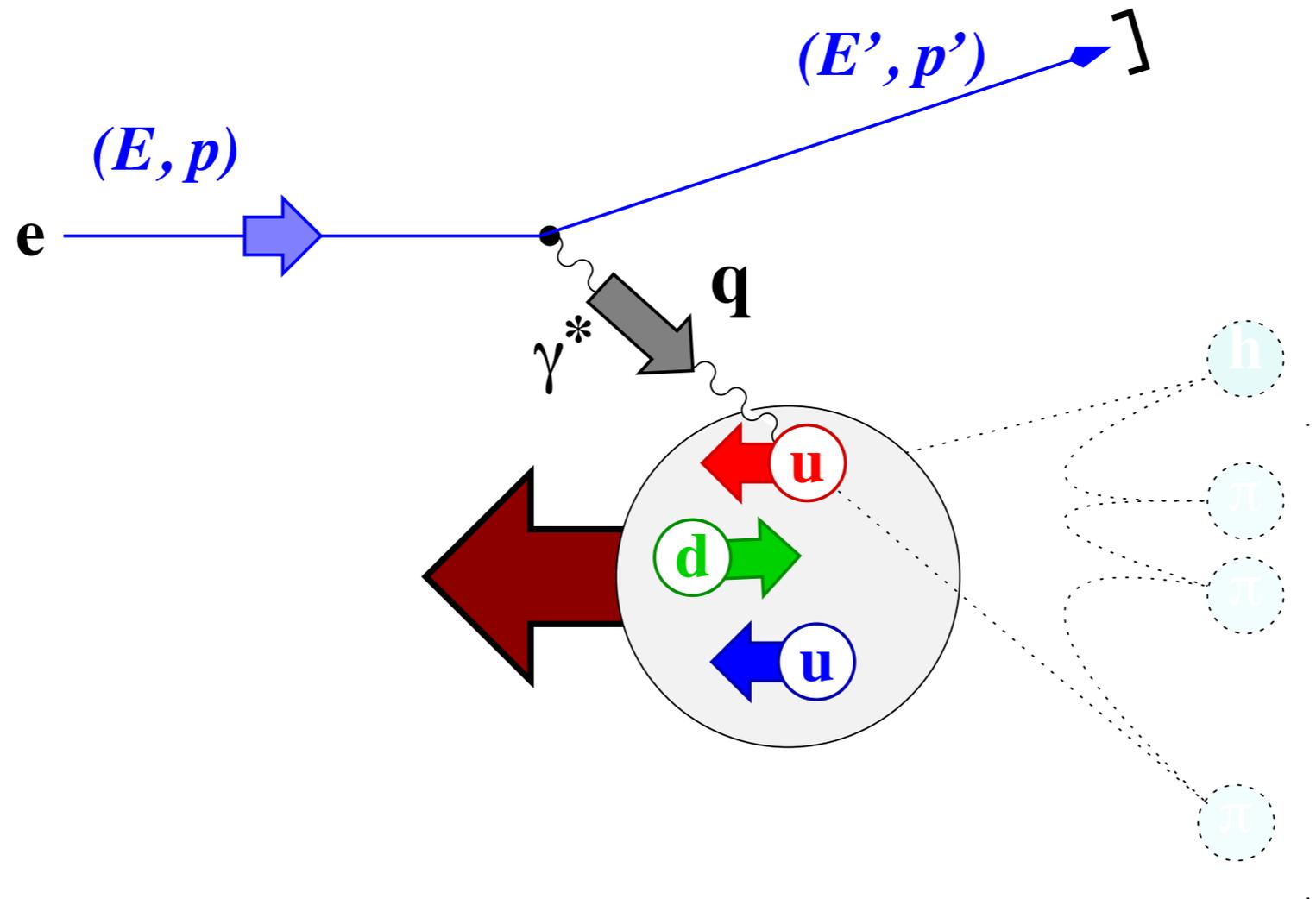
'pizza quattro stagioni'

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# deep-inelastic scattering

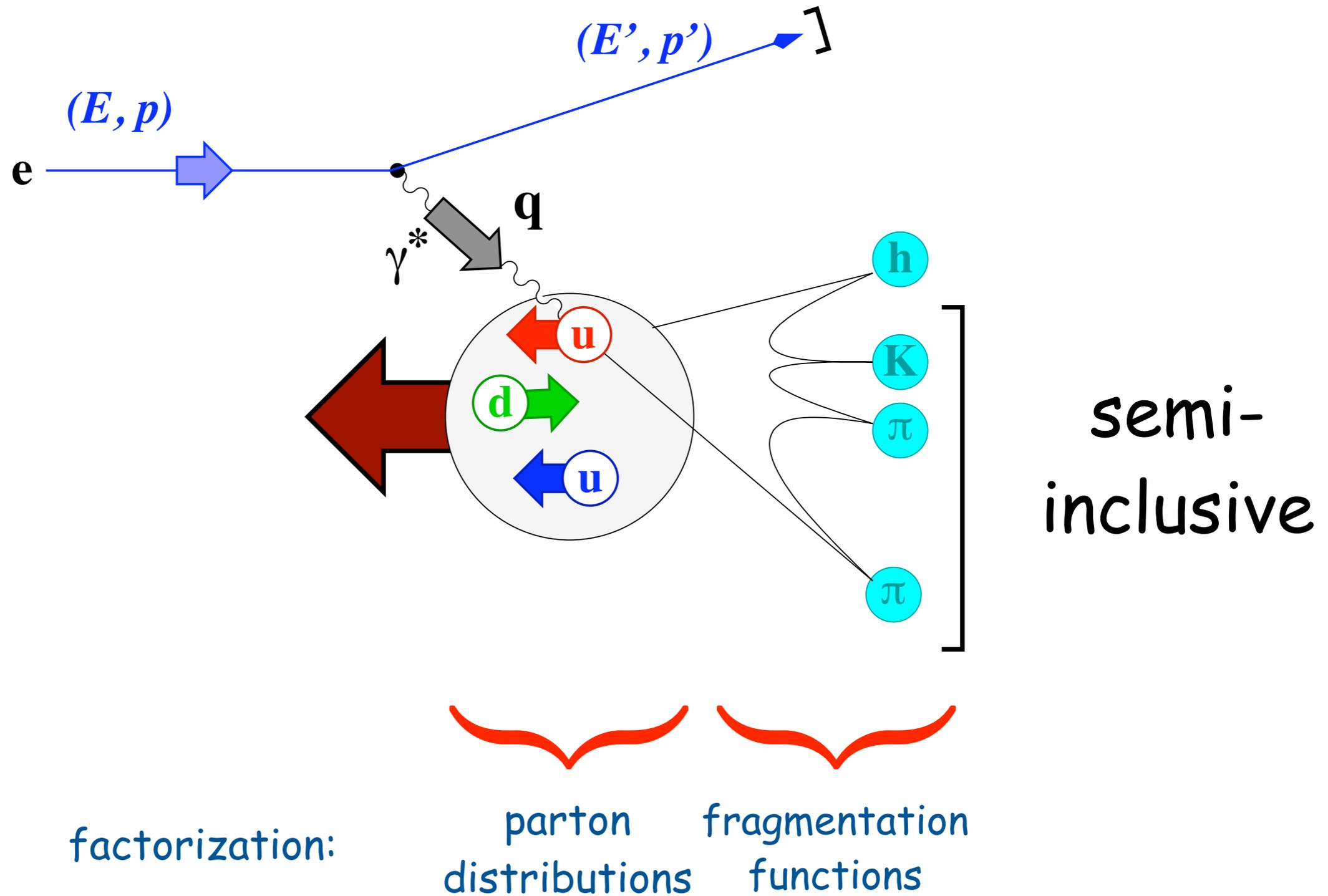
inclusive



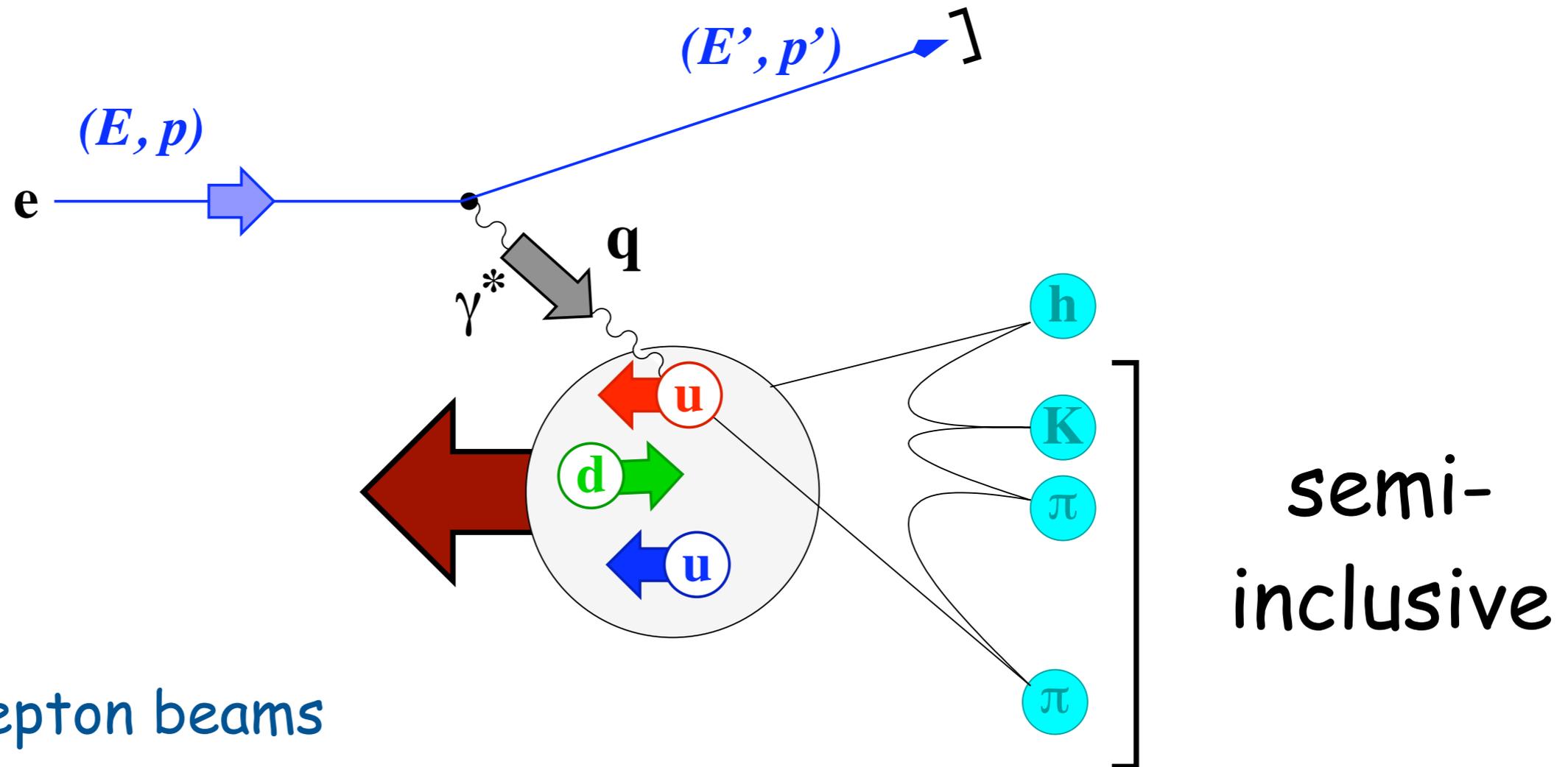
factorization:

parton  
distributions

# deep-inelastic scattering



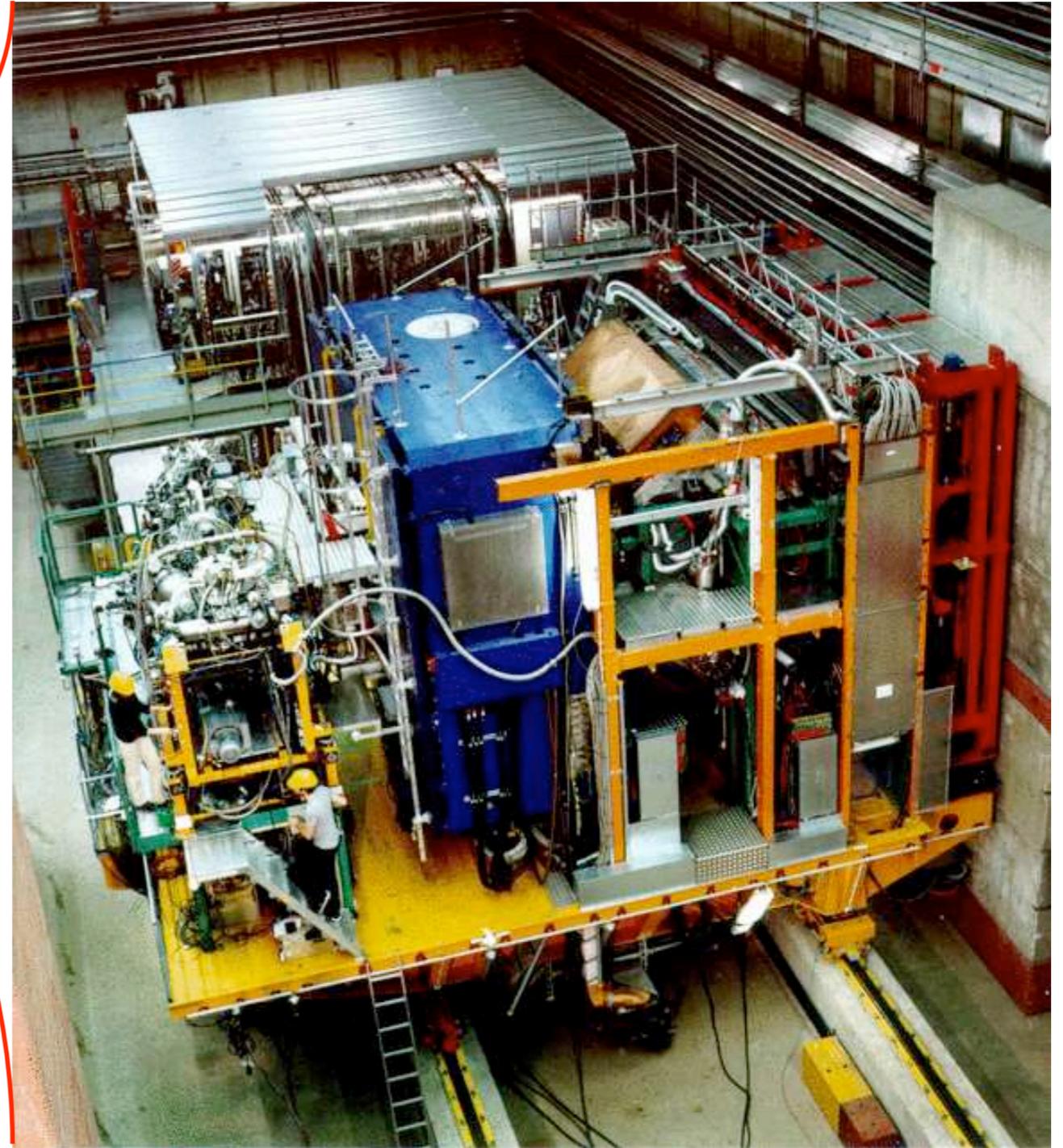
# deep-inelastic scattering



- polarized lepton beams
- polarized targets
- large-acceptance spectrometer
- good particle identification (PID)

# HERMES (†2007) @ DESY

27.6 GeV polarized  $e^+/e^-$  beam  
scattered off ...

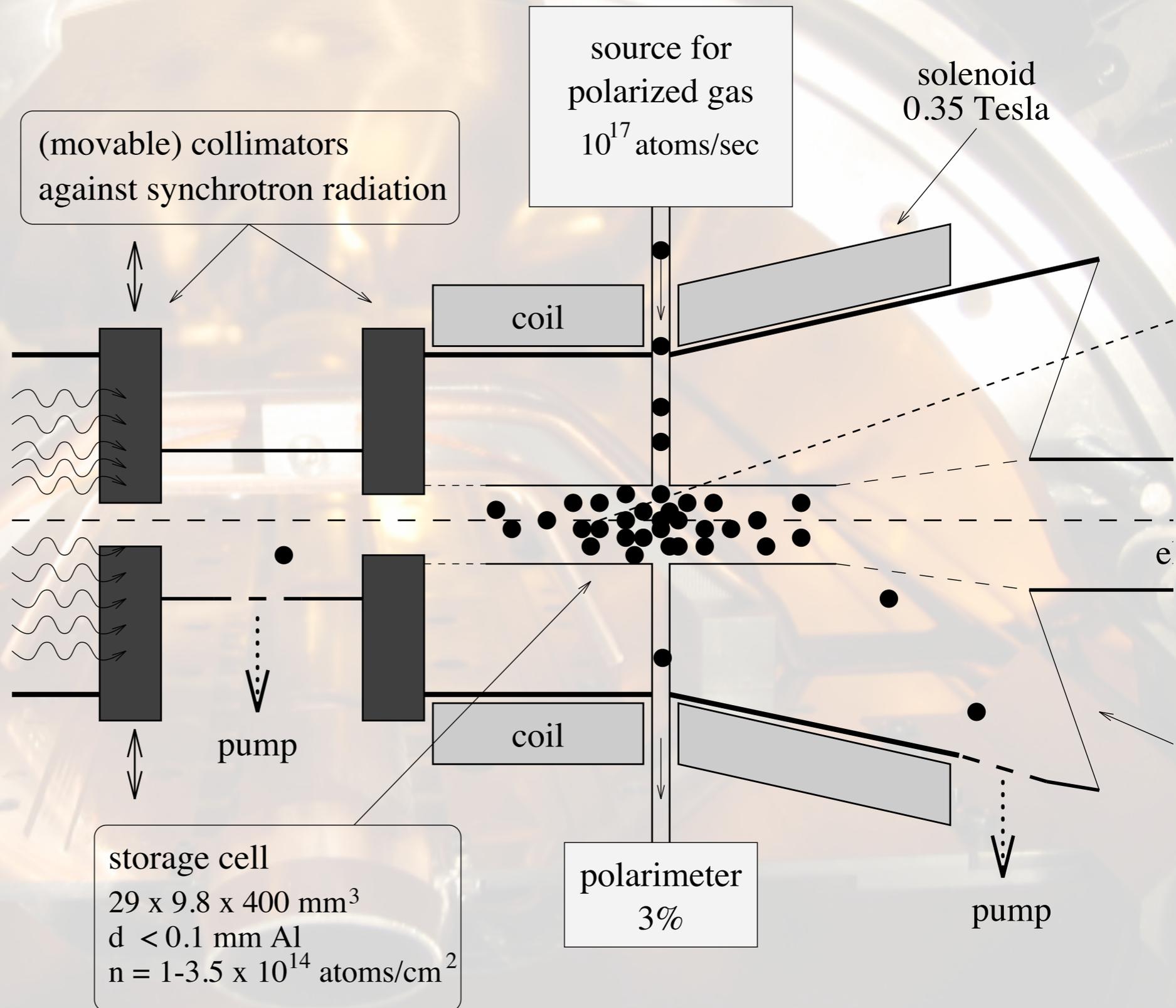


- unpolarized (H, D, He, ..., Xe)
- as well as transversely (H) and longitudinally polarized (pure) H, D &  $^3\text{He}$  gas targets

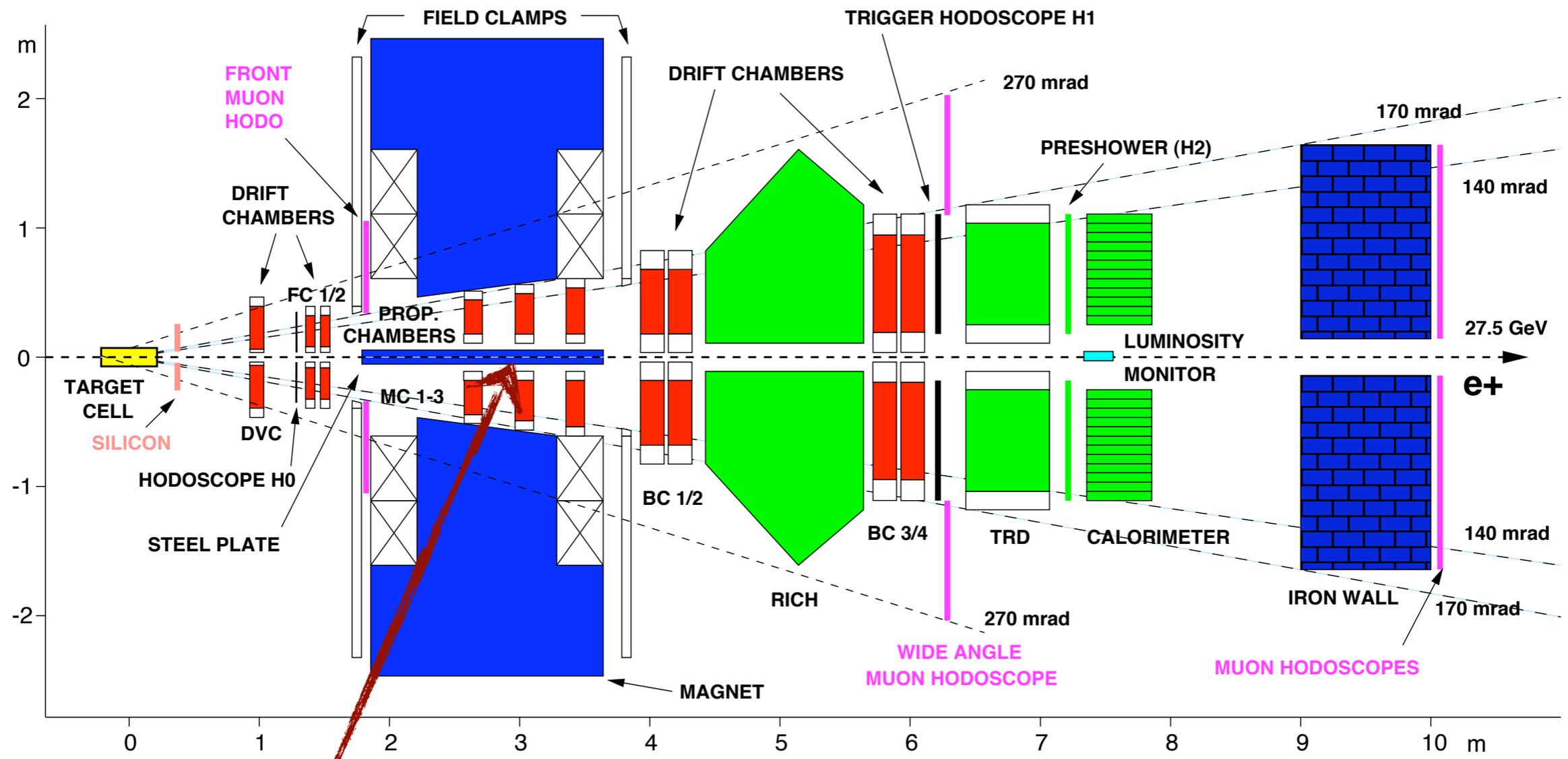
# HERMES polarized target

**Polarization:**  
longitudinal: ~85%  
transversal: ~75%

**fast/frequent spin reversal**

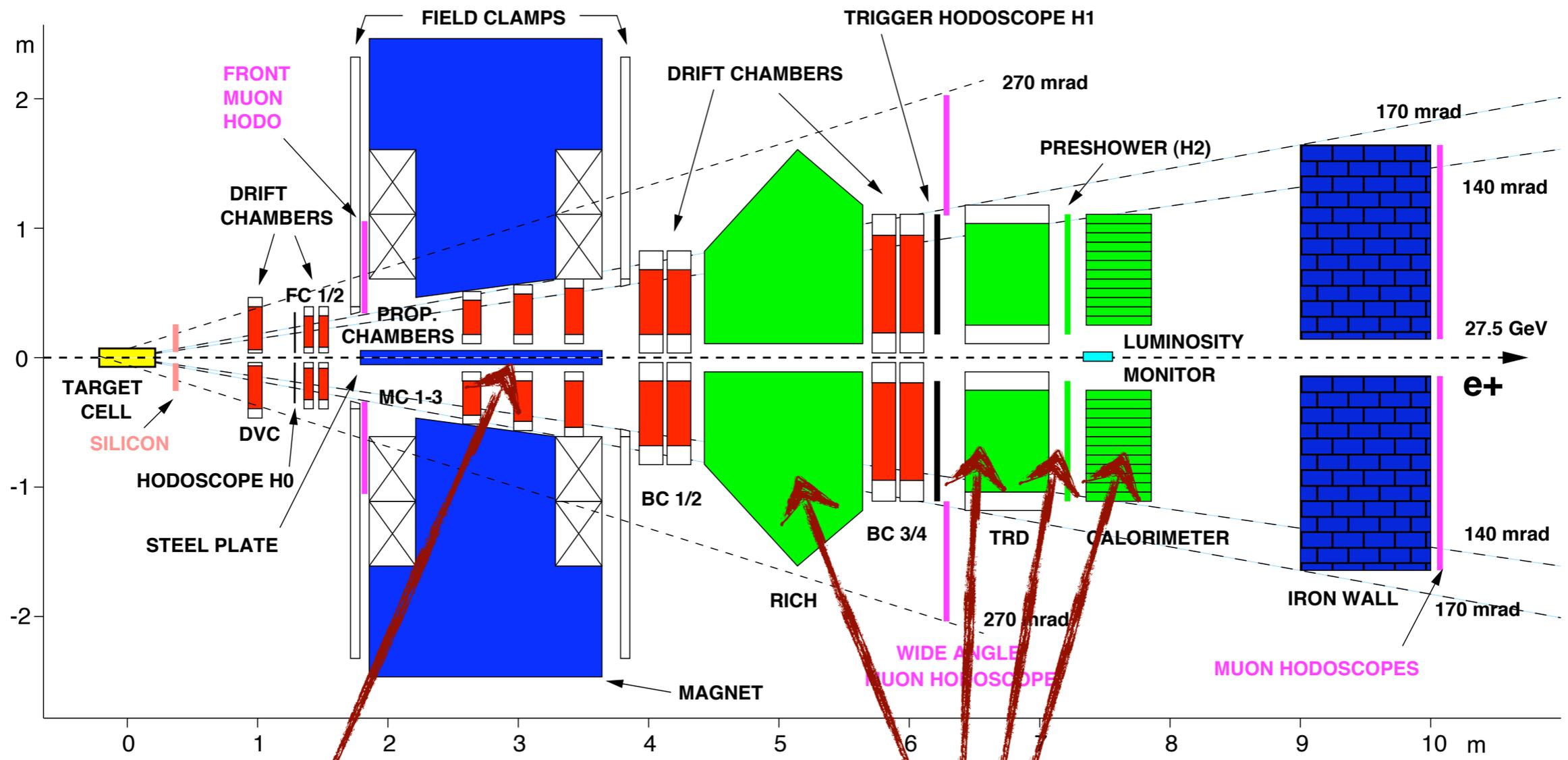


# HERMES (1998-2005) schematically



two (mirror-symmetric) halves

# HERMES (1998-2005) schematically



two (mirror-symmetric) halves

Particle ID detectors allow for

- lepton/hadron separation
- dual-radiator RICH: pion/kaon/proton discrimination  $2 \text{ GeV} < p < 15 \text{ GeV}$



# semi-inclusive DIS

- excluding transverse polarization:

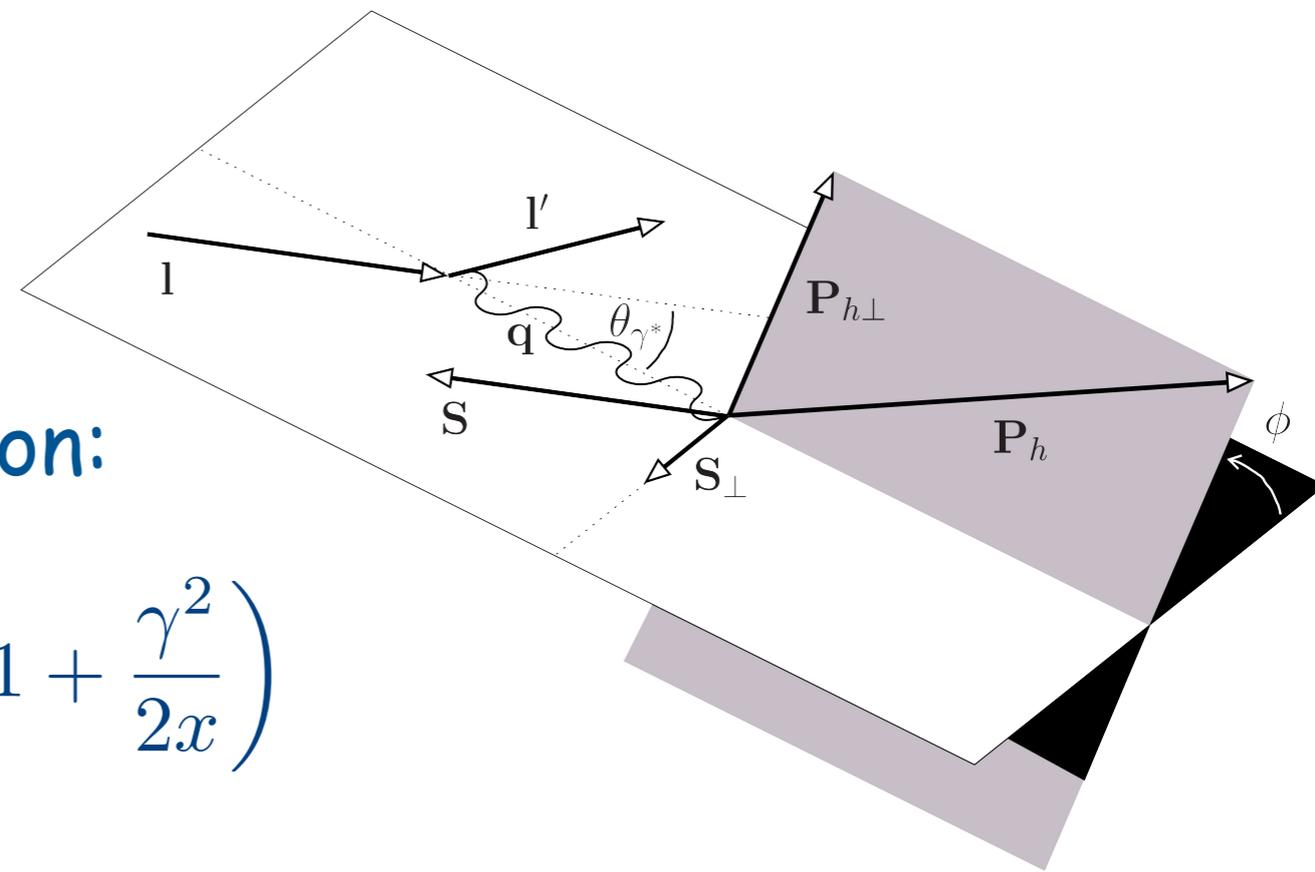
$$\frac{d\sigma^h}{dx dy dz dP_{h\perp}^2 d\phi} = \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left( 1 + \frac{\gamma^2}{2x} \right)$$

$$\left\{ F_{UU,T}^h + \epsilon F_{UU,L}^h + \lambda\Lambda\sqrt{1-\epsilon^2} F_{LL}^h \right.$$

$$+ \sqrt{2\epsilon} \left[ \lambda\sqrt{1-\epsilon} F_{LU}^{h,\sin\phi} + \Lambda\sqrt{1+\epsilon} F_{UL}^{h,\sin\phi} \right] \sin\phi$$

$$+ \sqrt{2\epsilon} \left[ \lambda\Lambda\sqrt{1-\epsilon} F_{LL}^{h,\cos\phi} + \sqrt{1+\epsilon} F_{UU}^{h,\cos\phi} \right] \cos\phi$$

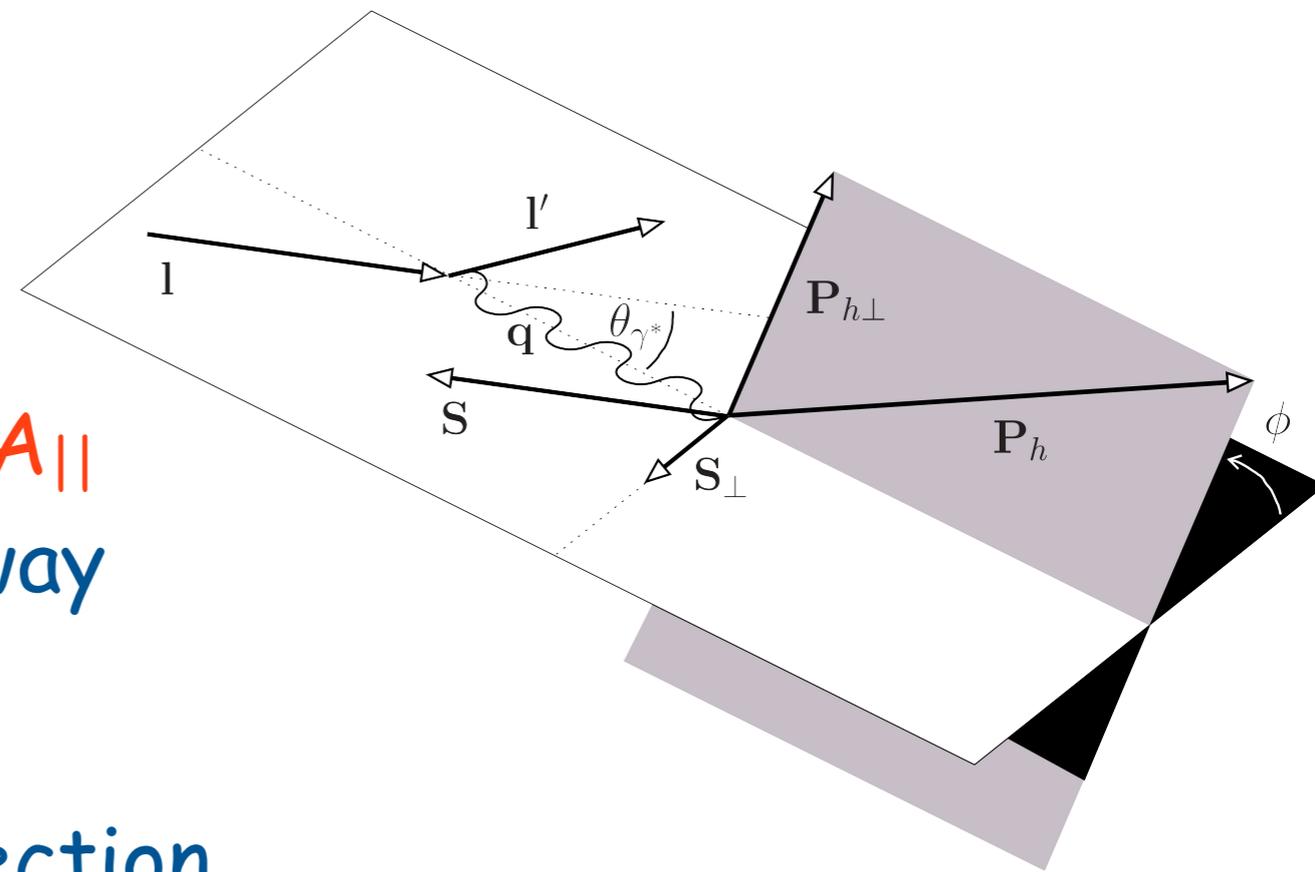
$$\left. + \Lambda\epsilon F_{UL}^{h,\sin 2\phi} \sin 2\phi + \epsilon F_{UU}^{h,\cos 2\phi} \cos 2\phi \right\}$$



- double-spin asymmetry

$$A_{LL}^h \equiv \frac{\sigma_{++}^h - \sigma_{+-}^h + \sigma_{--}^h - \sigma_{-+}^h}{\sigma_{++}^h + \sigma_{+-}^h + \sigma_{--}^h + \sigma_{-+}^h}$$

# semi-inclusive DIS



- in experiment extract instead  $A_{||}$  which differs from  $A_{LL}$  in the way the polarization is measured:
- $A_{LL}$ : along virtual-photon direction
- $A_{||}$ : along beam direction (results in small admixture of transverse target polarization and thus contributions from  $A_{LT}$ )
- $A_{||}$  related to virtual-photon-nucleon asymmetry  $A_1$

$$A_1^h = \frac{1}{D(1 + \eta\gamma)} A_{||}^h$$

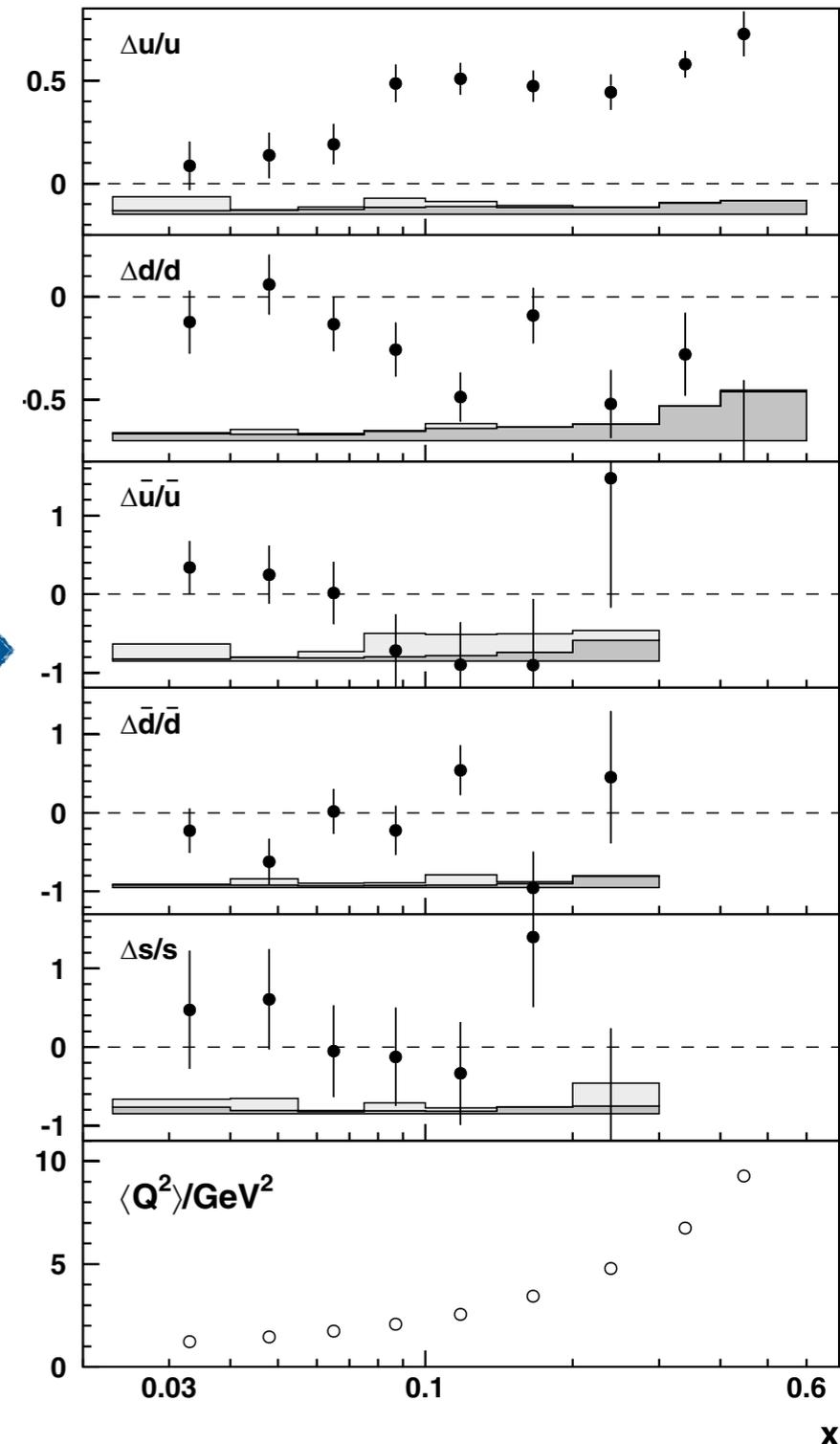
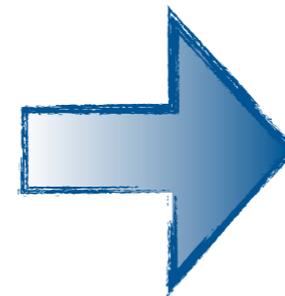
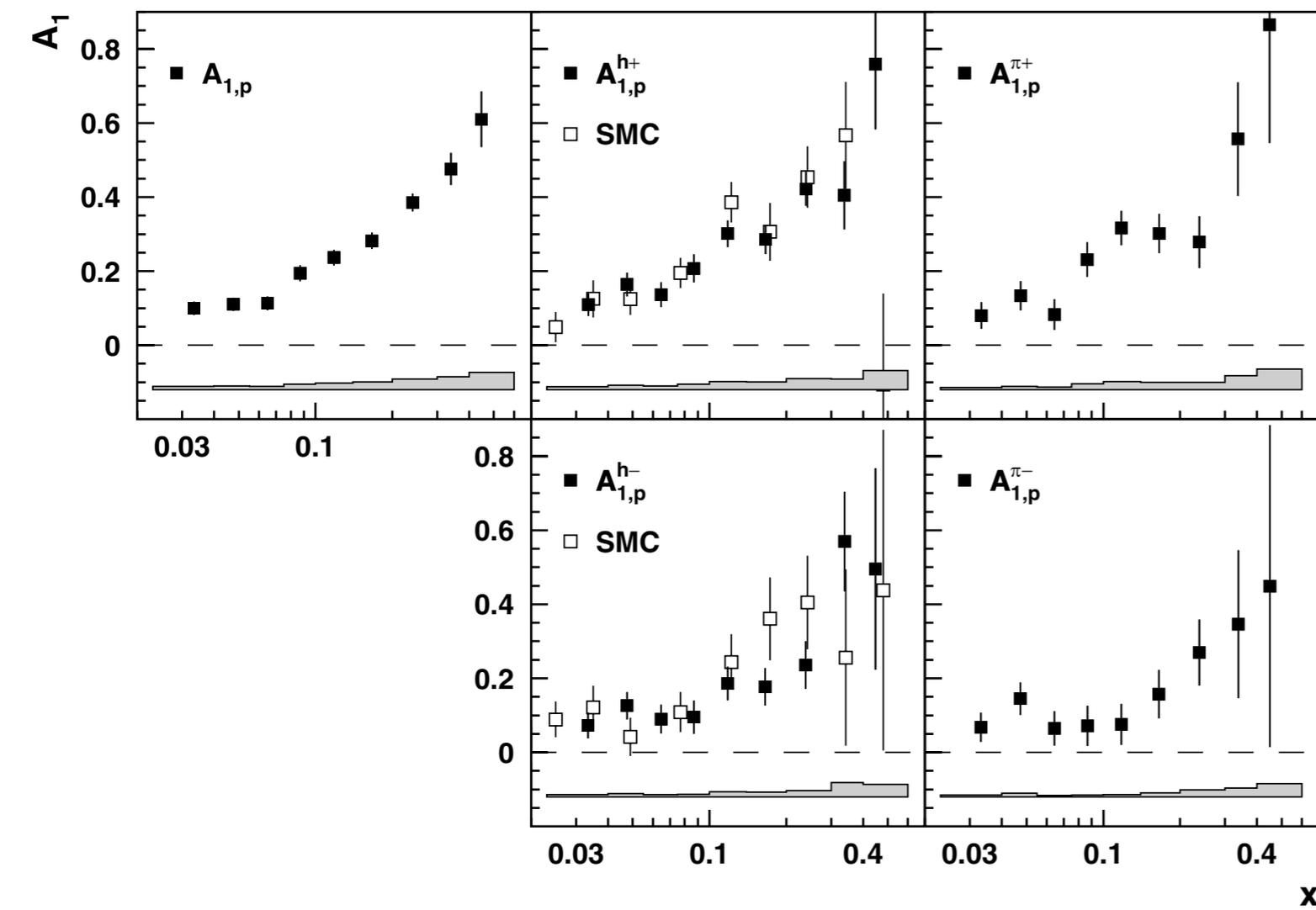
$$D = \frac{1 - (1 - y)\epsilon}{1 + \epsilon R}$$

$$\eta = \frac{\epsilon\gamma y}{1 - (1 - y)\epsilon}$$

# previous HERMES analysis

- (semi-) inclusive asymmetries used for LO extraction of helicity PDFs

PHYSICAL REVIEW D 71, 012003 (2005)



x

# re-analysis of double-spin asymmetries

- revisited [PRD 71 (2005) 012003]  $A_1$  analysis at HERMES in order to
  - exploit slightly larger data set (less restrictive momentum range)
  - provide  $A_{\parallel}$  in addition to  $A_1$

$$A_1^h = \frac{1}{D(1 + \eta\gamma)} A_{\parallel}^h \quad D = \frac{1 - (1 - y)\epsilon}{1 + \epsilon R}$$

R (ratio of longitudinal-to-transverse cross-sec'n) still to be measured!  
[only available for inclusive DIS data, e.g., used in  $g_1$  SF measurements]

- correct for D-state admixture (deuteron case) on asymmetry level
- correct better for azimuthal asymmetries coupling to acceptance
- look at multi-dimensional ( $x, z, P_{h\perp}$ ) dependences
- extract twist-3 cosine modulations

# azimuthal-asymmetry corrections

measured

"polarized Cahn" effect etc.

$$\tilde{A}_{\parallel}^h(x, Q^2, z, P_{h\perp}) = \frac{\int d\phi \sigma_{\parallel}^h(x, Q^2, z, P_{h\perp}, \phi) \xi(\phi)}{\int d\phi \sigma_{UU}^h(x, Q^2, z, P_{h\perp}, \phi) \xi(\phi)}$$

Boer-Mulders and Cahn effects etc.

azimuthal acceptance

- both numerator and in particular denominator  $\phi$  dependent
- in theory integrated out
- in praxis, detector acceptance also  $\phi$  dependent
- convolution of physics & acceptance leads to bias in normalization of asymmetries

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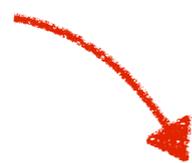
- both numerator and in particular denominator  $\phi$  dependent
  - in theory integrated out
  - in praxis, detector acceptance also  $\phi$  dependent
  - convolution of physics & acceptance leads to bias in normalization of asymmetries
- implement data-driven model for azimuthal modulations [PRD 87 (2013) 012010] into MC → extract correction factor & apply to data

# double-spin asymmetry $A_{||}$

$$A_{||}^h \equiv \frac{C_{\phi}^h}{f_D} \left[ \frac{L_{\Rightarrow} N_{\Leftarrow}^h - L_{\Leftarrow} N_{\Rightarrow}^h}{L_{P,\Rightarrow} N_{\Leftarrow}^h + L_{P,\Leftarrow} N_{\Rightarrow}^h} \right]_B$$

# double-spin asymmetry $A_{||}$

azimuthal  
correction


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nucleon-in-nucleus  
depolarization factor  
(0.926 for deuteron due  
to D-state admixture)

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luminosities

$$\left[ \frac{L_{\Rightarrow} N_{\Leftarrow}^h - L_{\Leftarrow} N_{\Rightarrow}^h}{L_{P,\Rightarrow} N_{\Leftarrow}^h + L_{P,\Leftarrow} N_{\Rightarrow}^h} \right]_B$$

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polarization-weighted  
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nucleon-in-nucleus  
depolarization factor  
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polarization-weighted  
luminosities

unfolded for  
QED radiation  
to Born level

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- dominated by statistical uncertainties

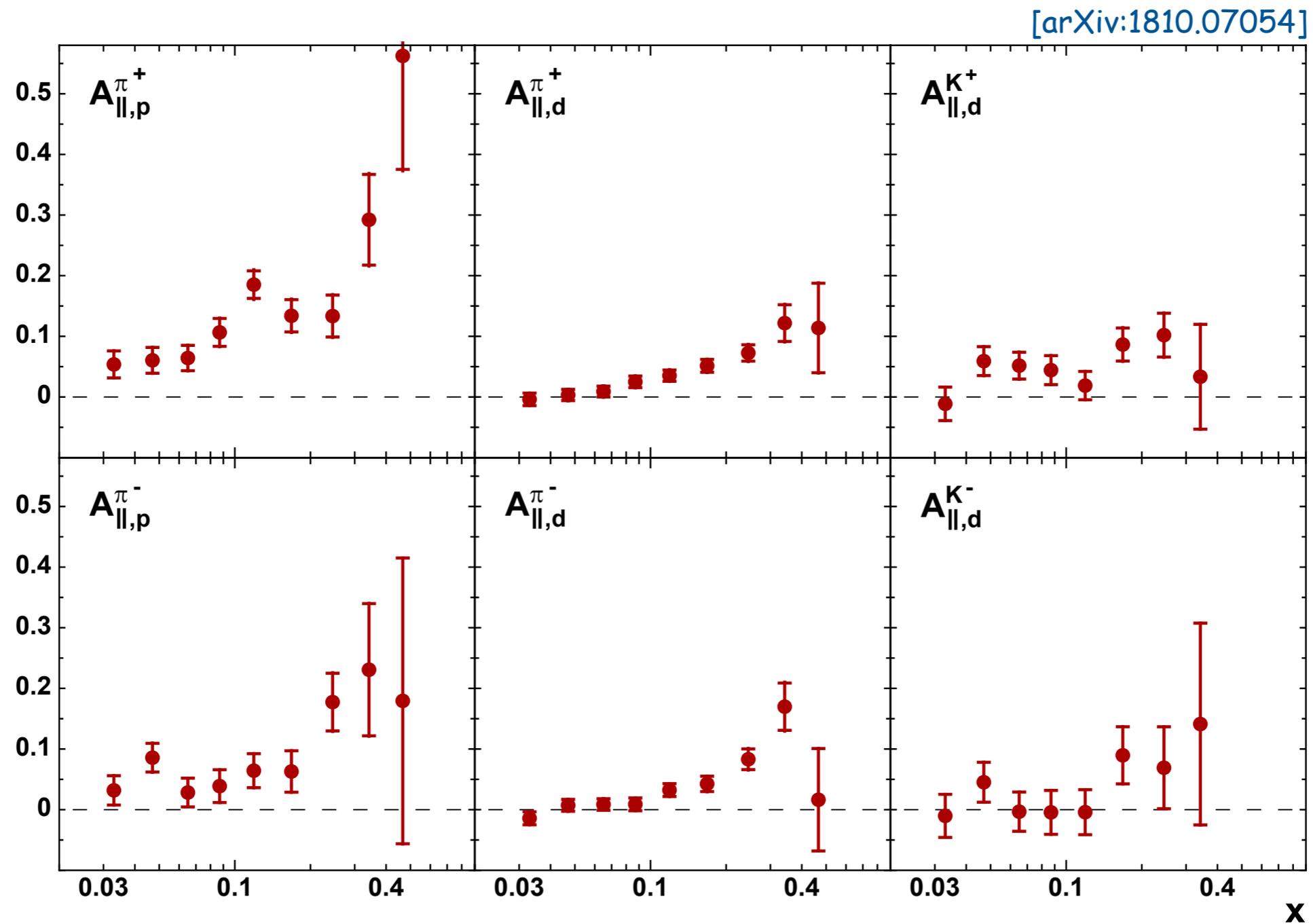
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- dominated by statistical uncertainties
- main systematics arise from
  - polarization measurements [6.6% for hydrogen, 5.7% for deuterium]
  - azimuthal correction [O(few %)]

# x dependence of $A_{||}$

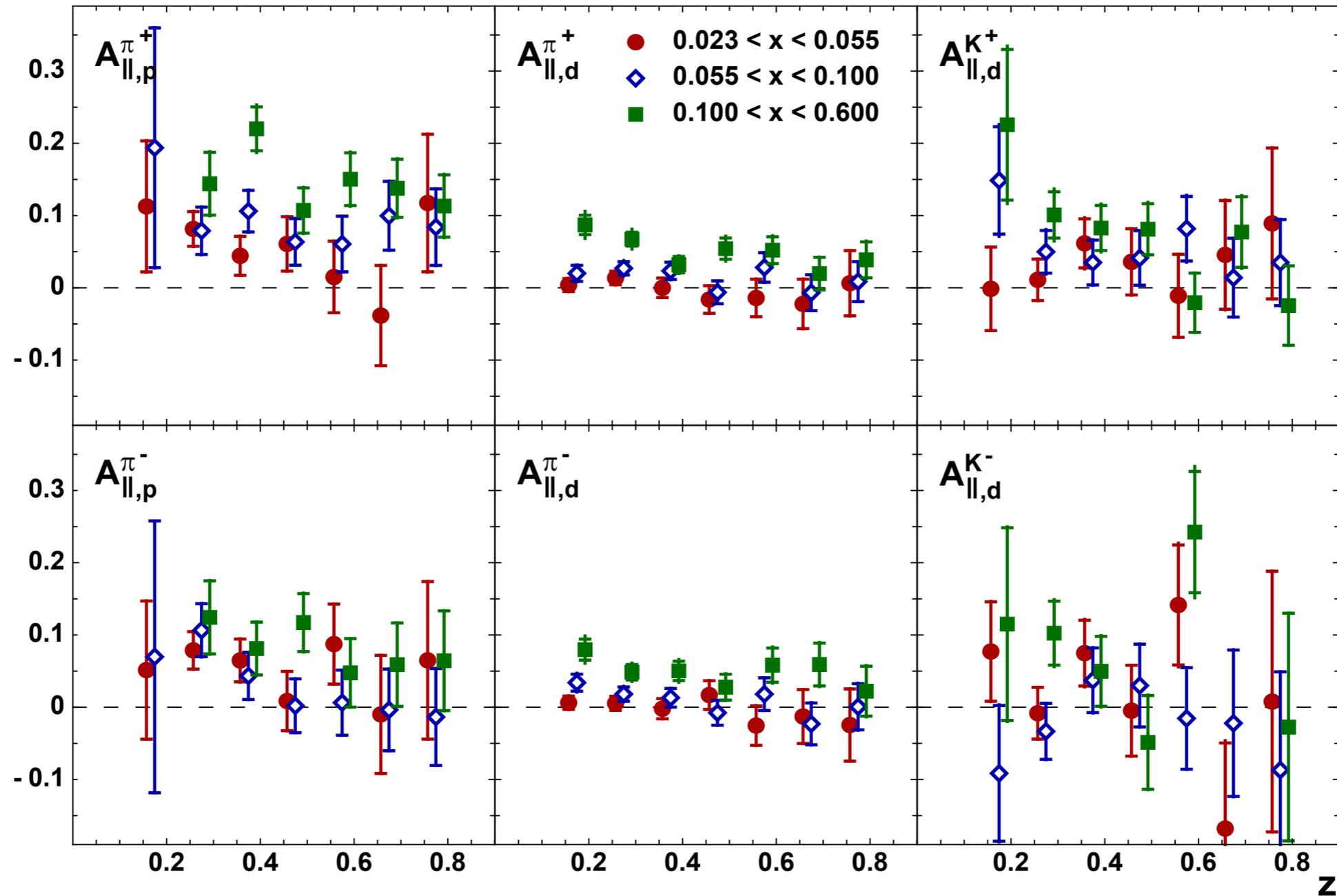
- consistent with previous HERMES publication [PRD 71 (2005) 012003]



# z dependence of $A_{||}$ (three x ranges)

- in general, no strong z-dependence visible

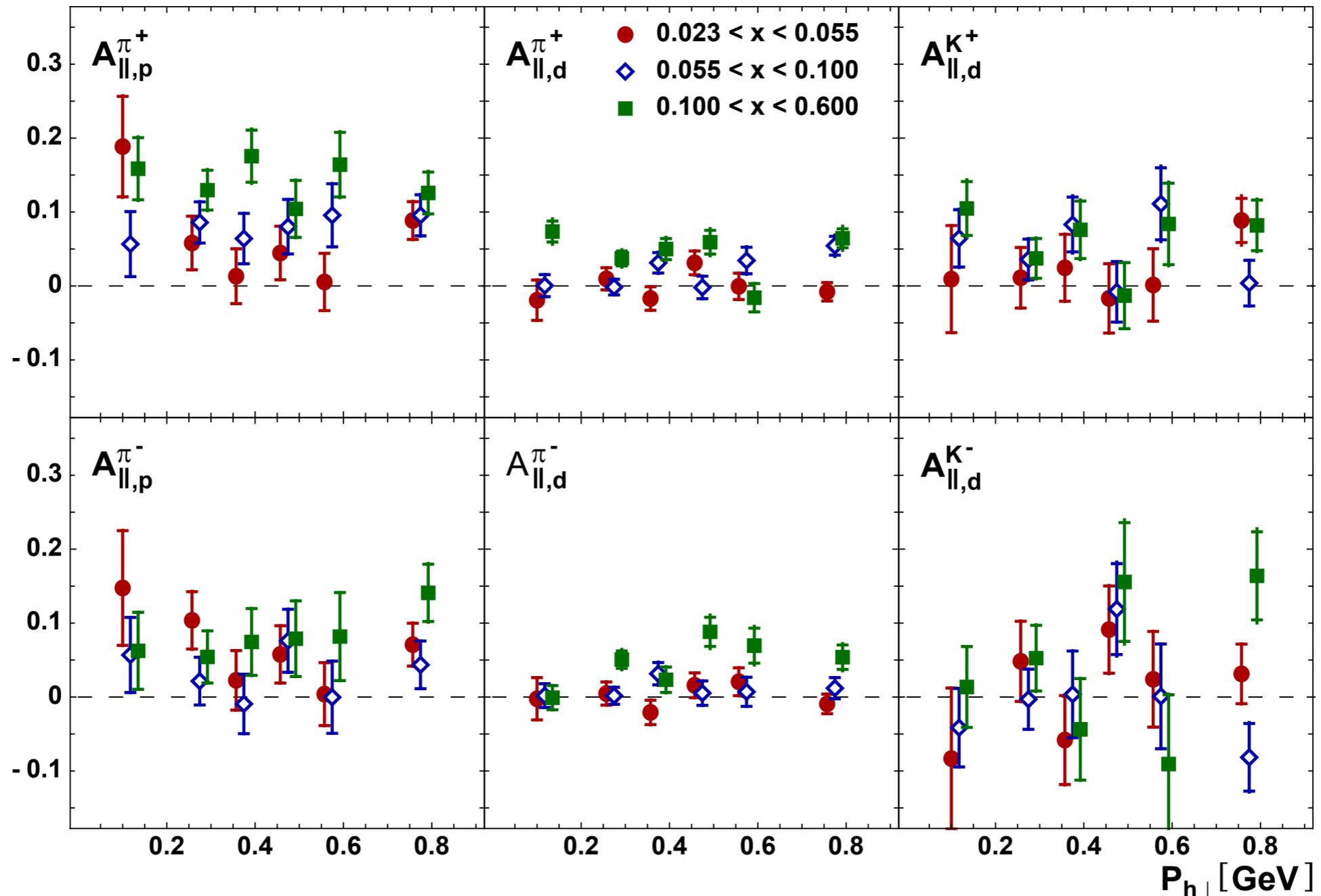
[arXiv:1810.07054]



# $P_{h\perp}$ dependence of $A_{||}$ (three x ranges)

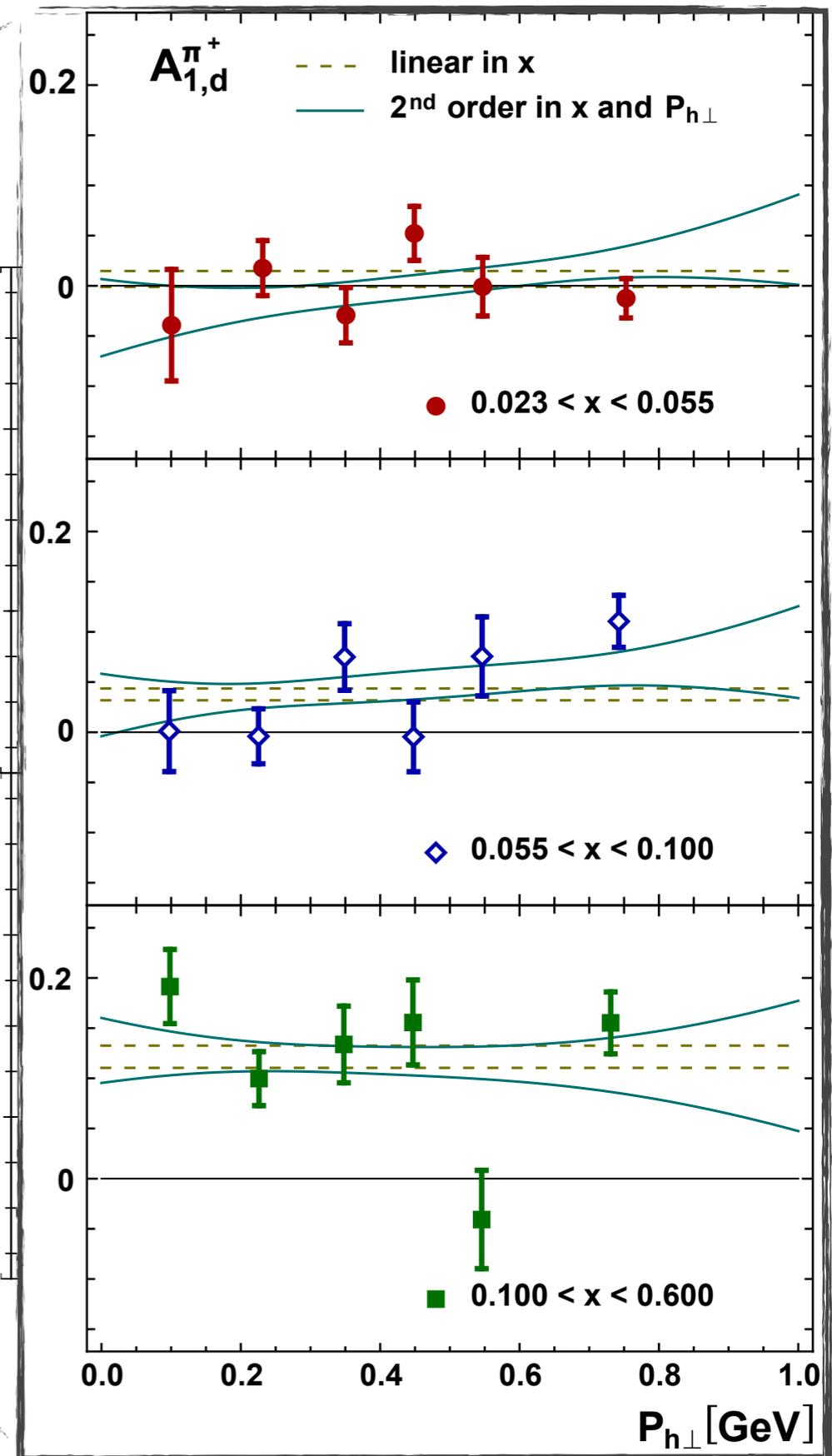
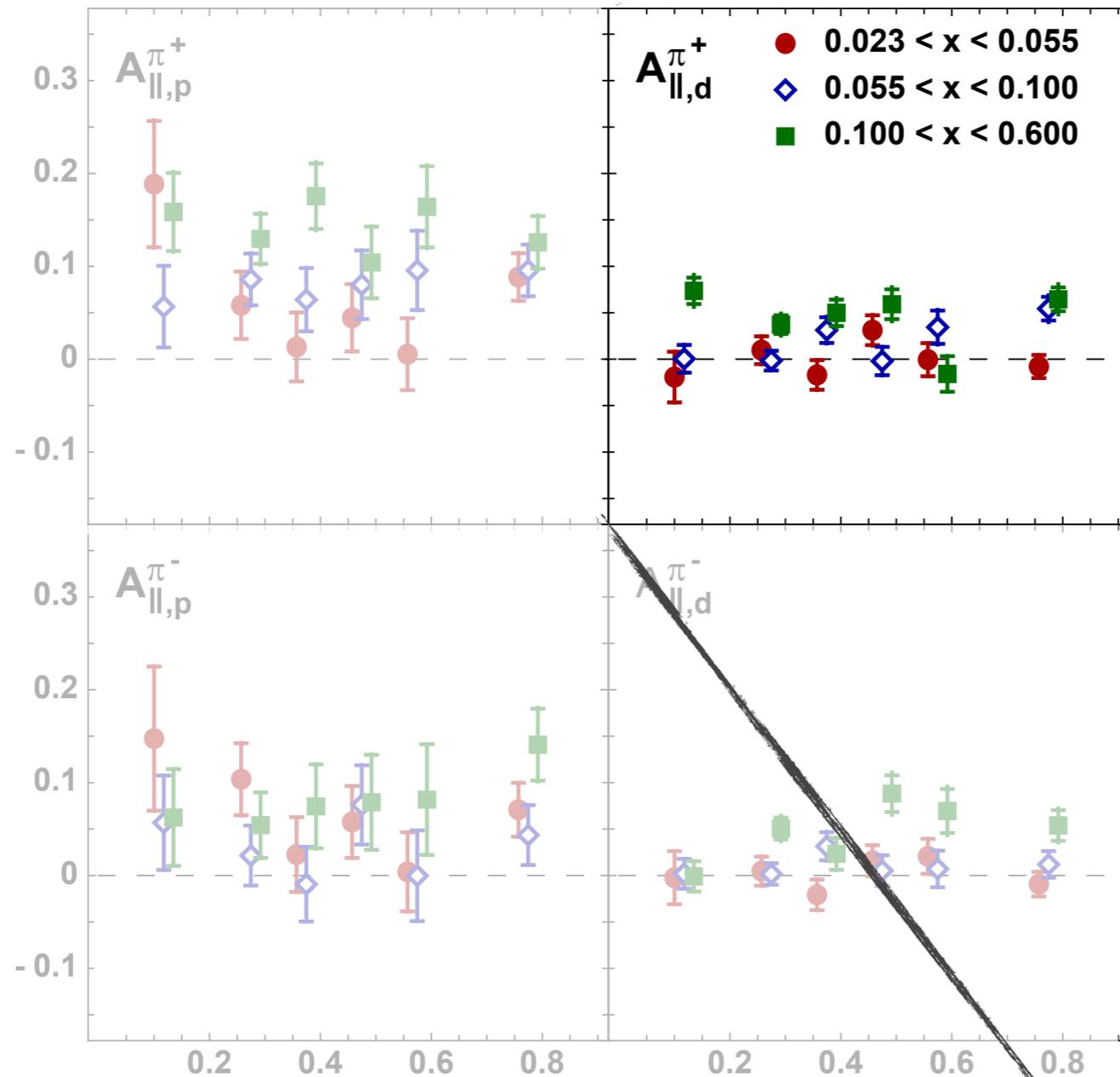
- again, no strong dependence (beyond on x)

[arXiv:1810.07054]



# $P_{h\perp}$ dependence of $A_{||}$ (three $x$ ranges)

- again, no strong dependence (beyond on  $x$ )



- also fit to  $A_1$  fit does not favor an additional dependence on  $P_{h\perp}$

interlude: dealing with  
multi-d dependences

# multi-d dependences

- TMD cross sections differential in at least 5 variables
  - some easily parametrized (e.g., azimuthal dependences)
  - others mostly unknown

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  - e.g., binning in  $x$  involves [incomplete] integration(s) over  $P_{h\perp}$

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  - e.g., binning in  $x$  involves [incomplete] integration(s) over  $P_{h\perp}$
- further complication: physics (cross sections) folded with acceptance
  - NO experiment has flat acceptance in full multi-d kinematic space

# multi-d dependences

$$\frac{N^+(x) - N^-(x)}{N^+(x) + N^-(x)} = \frac{\int d\omega \epsilon(x, \omega) \Delta\sigma(x, \omega)}{\int d\omega \epsilon(x, \omega) \sigma(x, \omega)}$$

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- measured cross sections / asymmetries often contain "remnants" of experimental acceptance  $\epsilon$

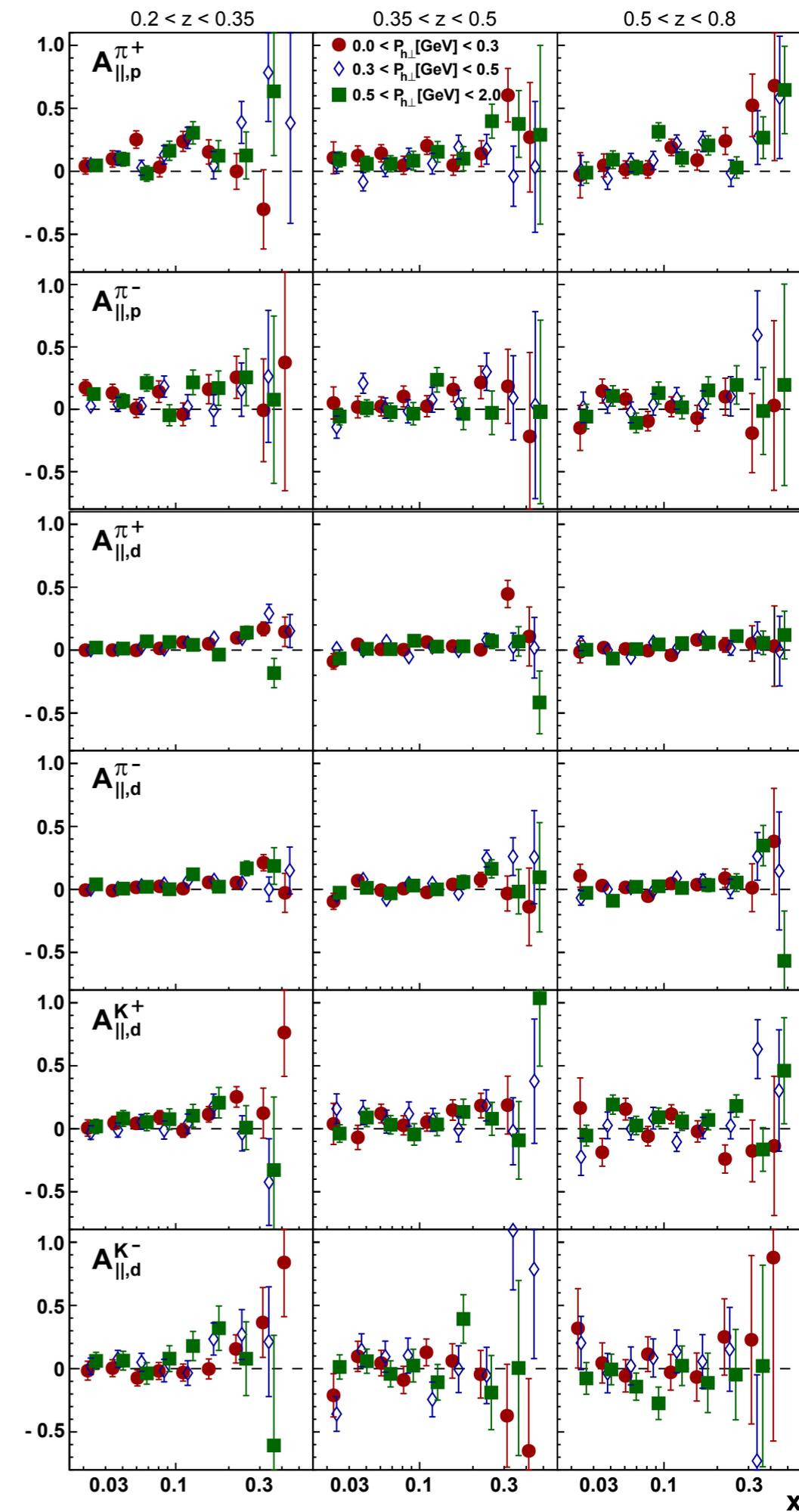
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- measured cross sections / asymmetries often contain "remnants" of experimental acceptance  $\epsilon$
- difficult to evaluate precisely in absence of good physics model
  - general challenge to statistically precise data sets
  - avoid 1d binning/presentation of data
  - theorist: watch out for precise definition (if given!) of experimental results reported ... and try not to treat data points of different projections as independent

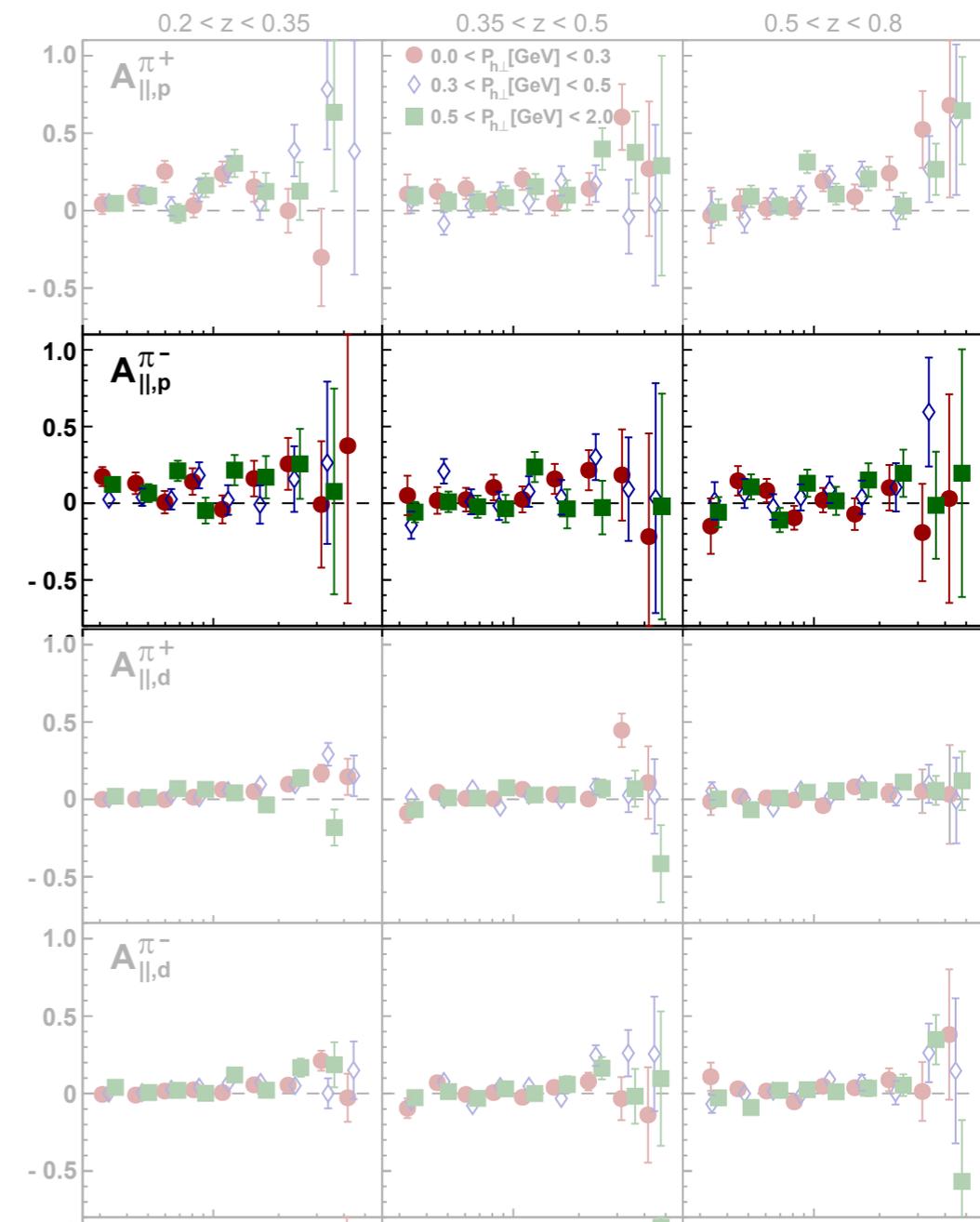
# 3-dimensional binning

- 3d dependences provides transverse-momentum dependence

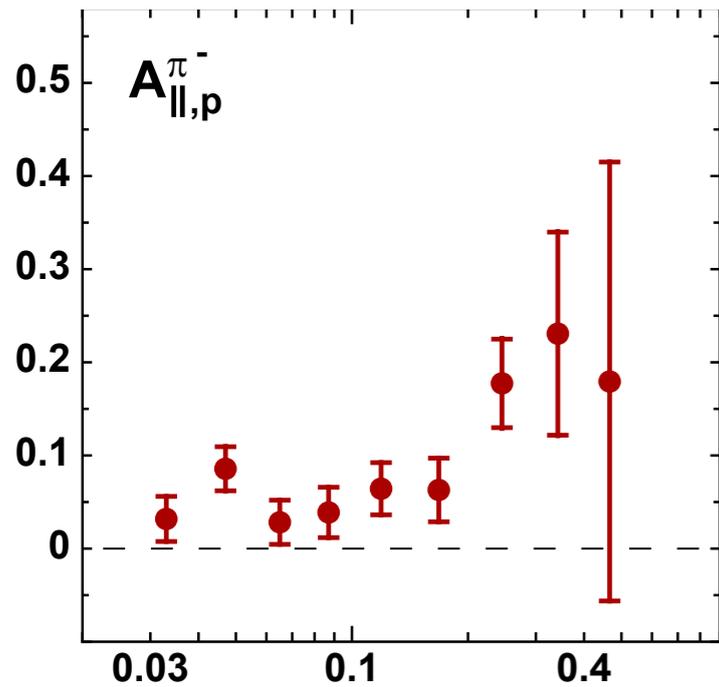


# 3-dimensional binning

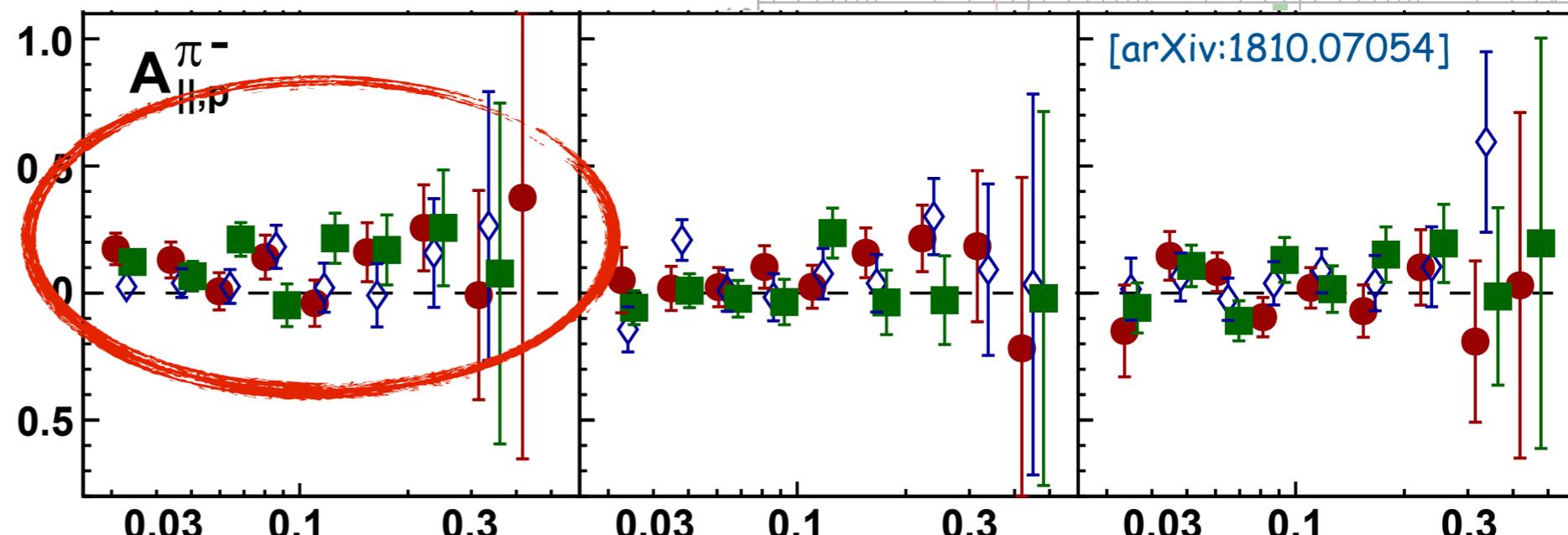
- 3d dependences provides transverse-momentum dependence
- but also extra flavor sensitivity, e.g.,
  - $\pi^-$  asymmetries mainly coming from **low- $z$**  region where **disfavored fragmentation** large and thus **sensitivity to the large positive up-quark polarization**



1d



3d



# charge-difference asymmetries

$$A_1^{h^+ - h^-}(x) \equiv \frac{\left(\sigma_{1/2}^{h^+} - \sigma_{1/2}^{h^-}\right) - \left(\sigma_{3/2}^{h^+} - \sigma_{3/2}^{h^-}\right)}{\left(\sigma_{1/2}^{h^+} - \sigma_{1/2}^{h^-}\right) + \left(\sigma_{3/2}^{h^+} - \sigma_{3/2}^{h^-}\right)}$$

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- at leading-order and leading-twist, assuming charge conjugation symmetry for fragmentation functions:

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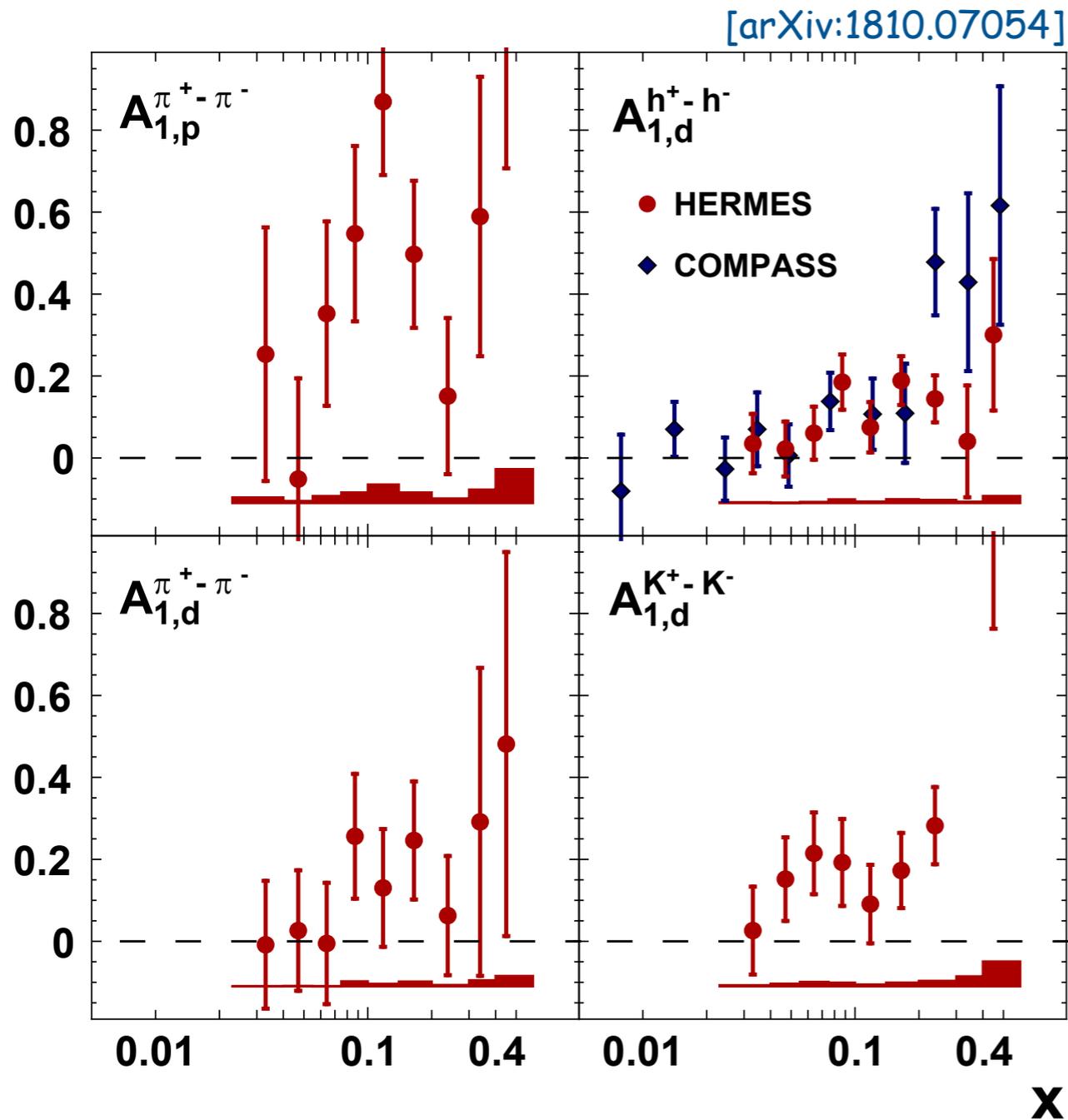
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- can be used to extract valence helicity distributions

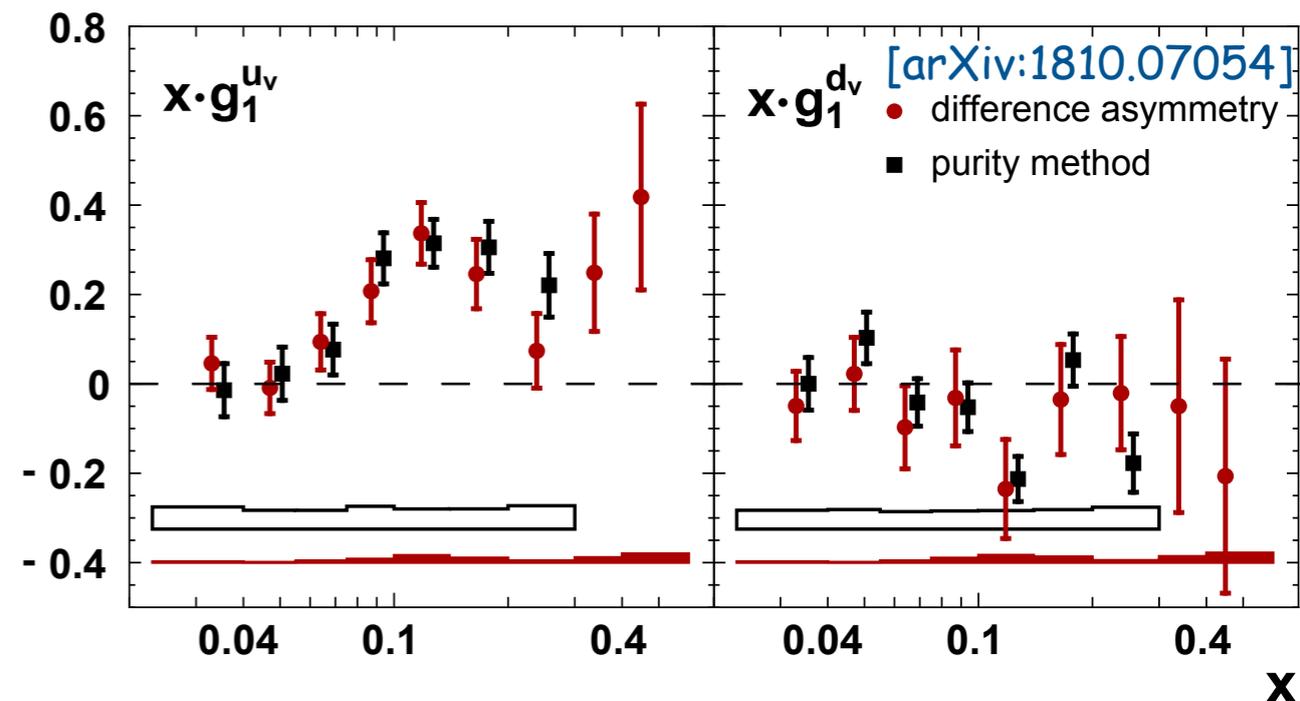
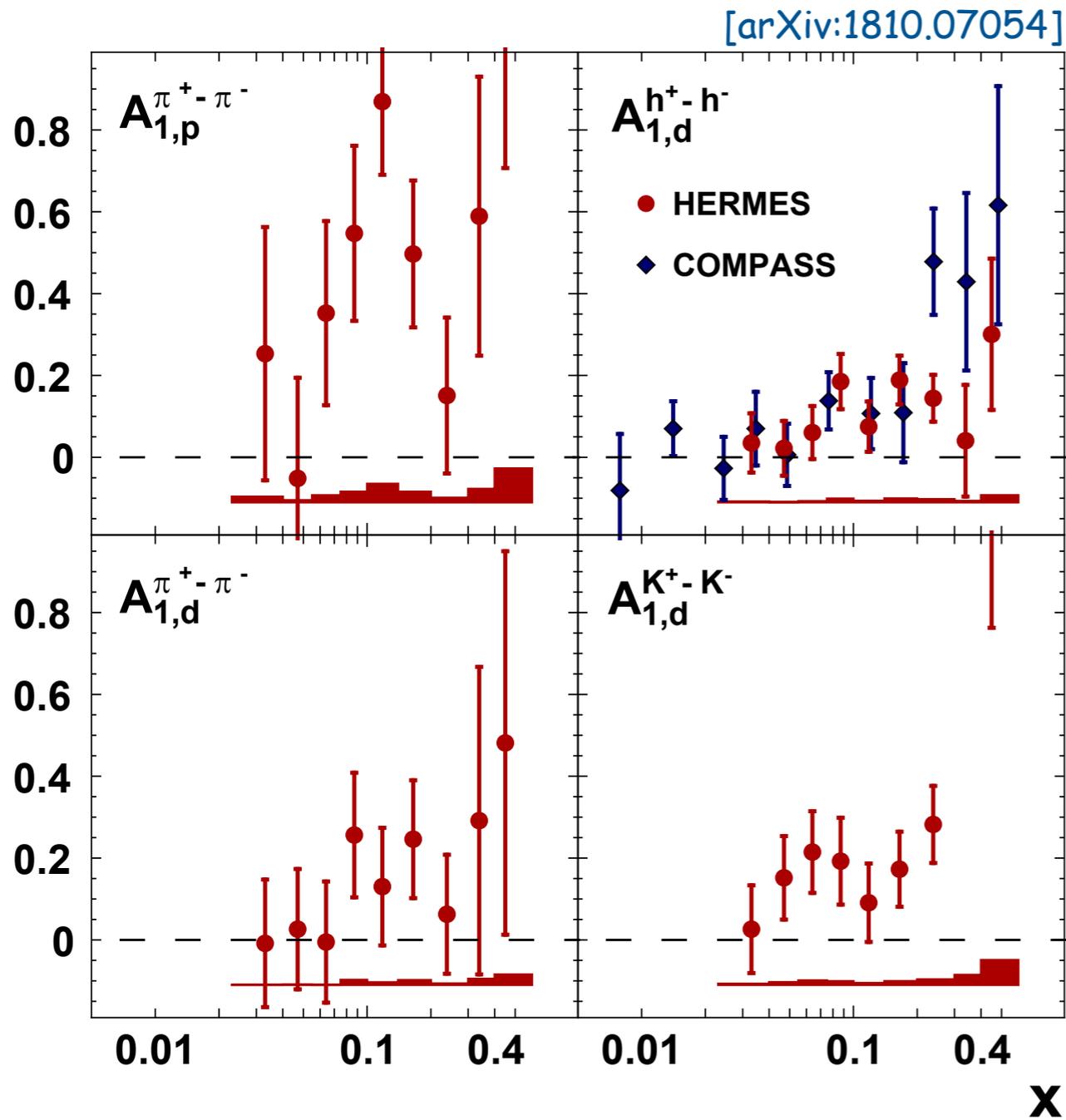
# charge-difference asymmetries

- no significant hadron-type dependence for deuterons
- deuteron results (unidentified hadrons) consistent with *COMPASS*



# charge-difference asymmetries

- no significant hadron-type dependence for deuterons
- deuteron results (unidentified hadrons) consistent with *COMPASS*
- valence distributions consistent with *JETSET*-based extraction:

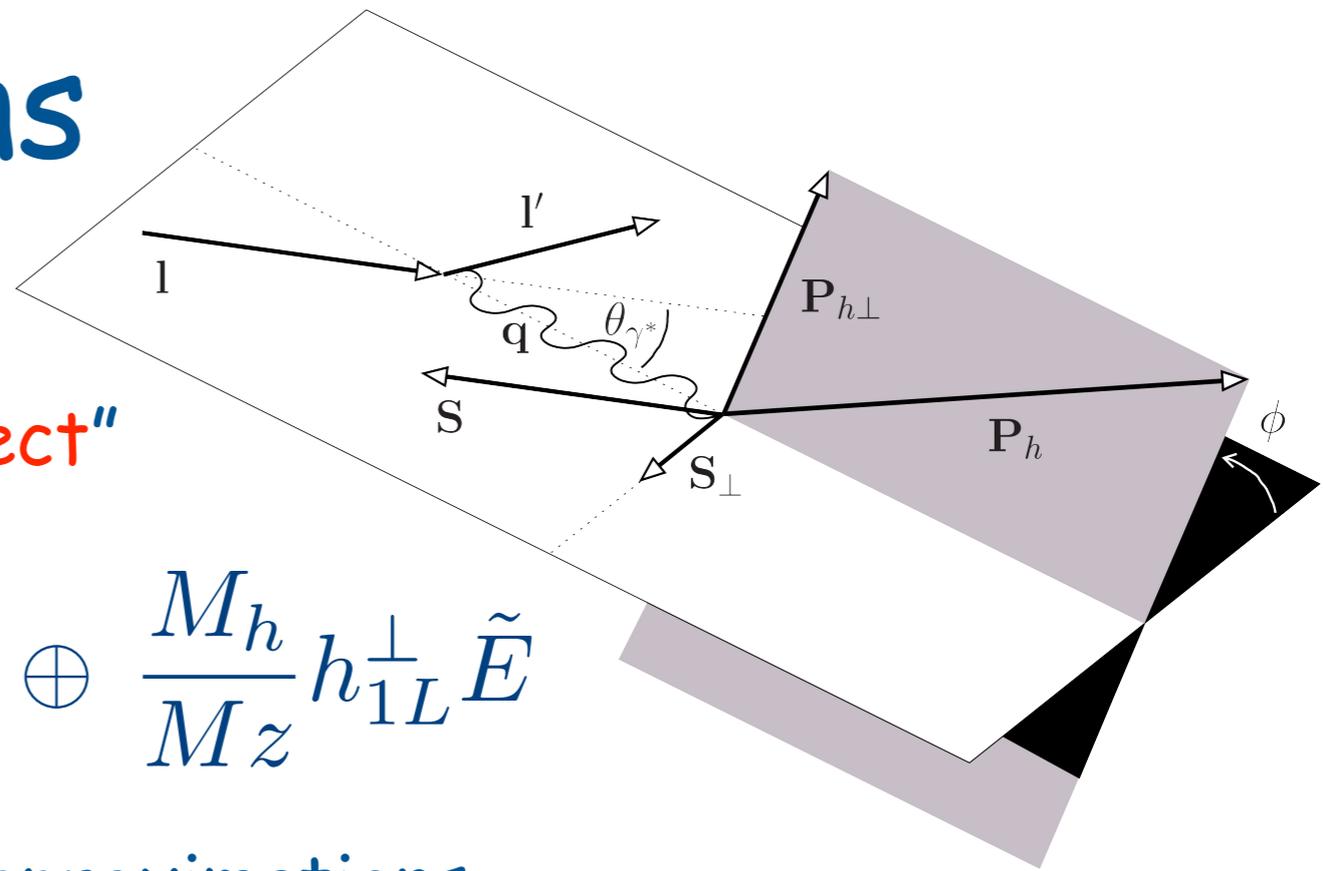


# azimuthal modulations

- twist-3 → various contributions
- most prominent: "polarized Cahn effect"

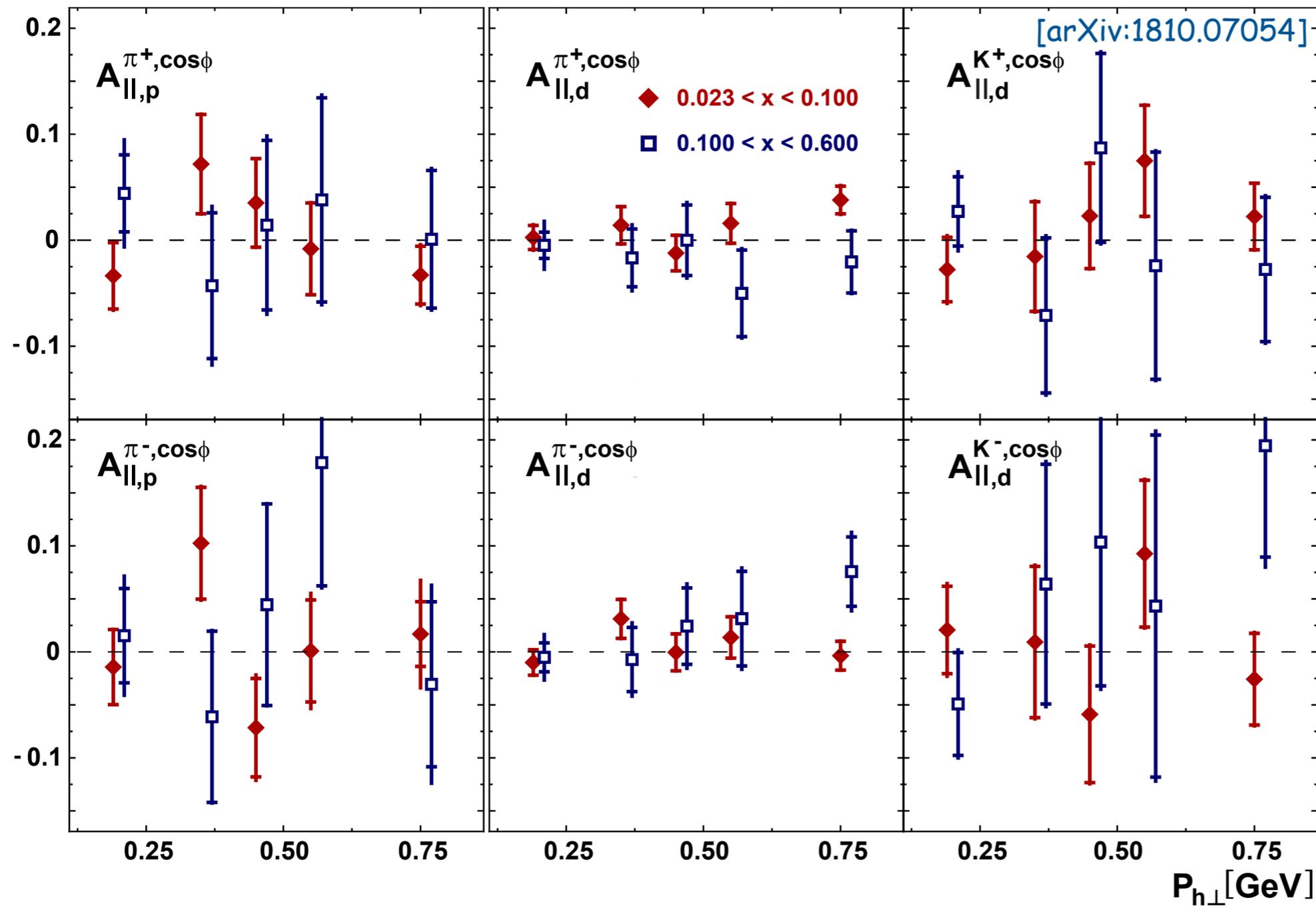
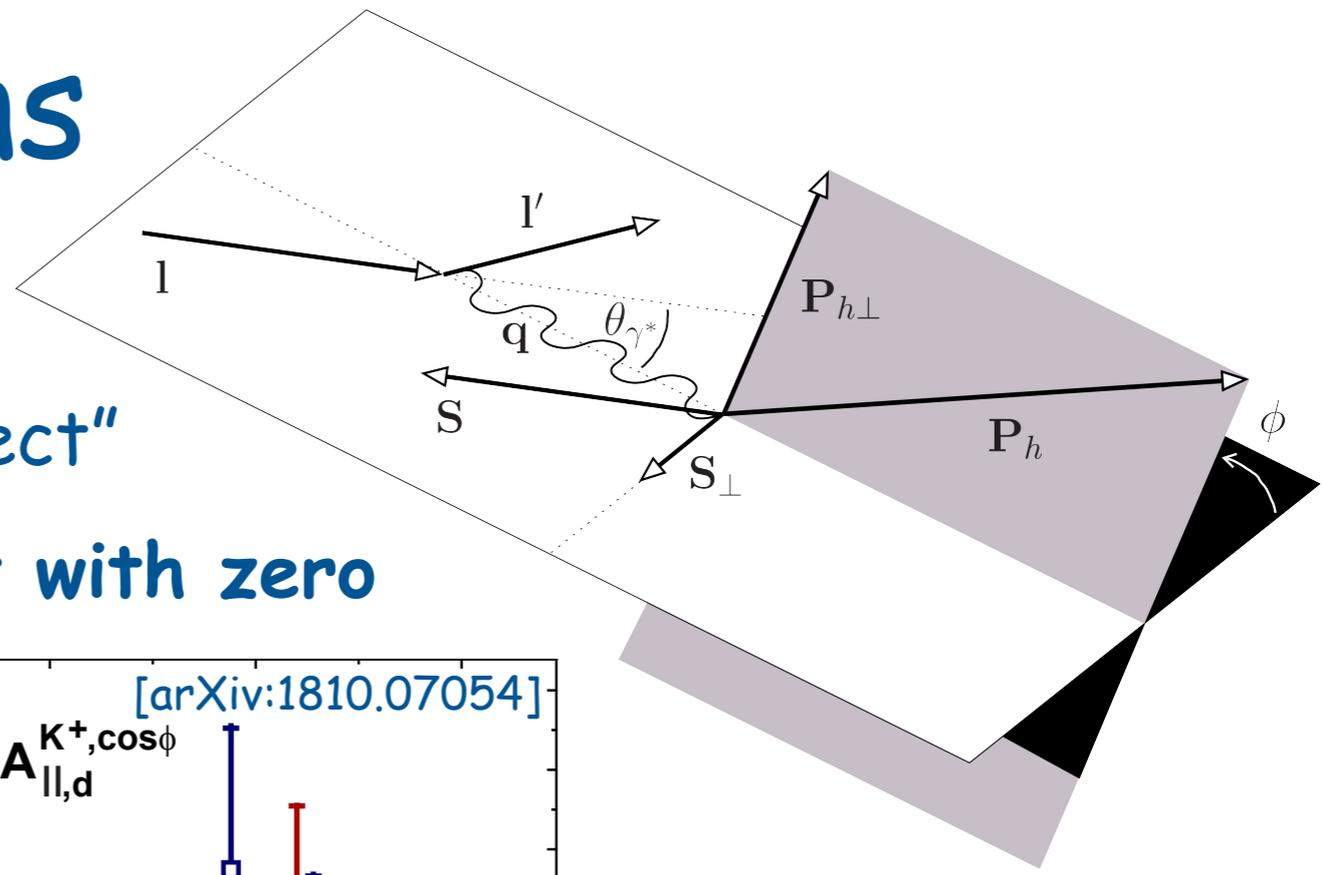
$$xg_L^\perp D_1 \oplus \frac{M_h}{M_z} g_1 \tilde{D}^\perp \oplus xe_L H_1^\perp \oplus \frac{M_h}{M_z} h_{1L}^\perp \tilde{E}$$

- the only one surviving WW-type approximations



# azimuthal modulations

- twist-3  $\rightarrow$  various contributions
- most prominent: "polarized Cahn effect"
- cosine modulations largely consistent with zero



# summary

- several longitudinal double-spin asymmetries in SIDIS have been presented that
  - extend the analysis of previous HERMES publications to include also transverse-momentum dependence and for the first time also a 3d binning
  - provide  $A_{||}$  in addition to  $A_1$
- within precision of the measurements, the virtual-photon-nucleon asymmetries display no significant dependence on  $z$  and  $P_{h\perp}$
- hadron-charge difference asymmetries in agreement with COMPASS
  - used for LO, leading-twist extraction of valence helicity PDFs
- $\cos \phi$  moments of semi-inclusive double-spin asymmetry compatible with zero

backup

Year	Beam Type	Target Gas	Hadron Type	Hadron Momentum $P_h$
1996	$e^+$	H	$\pi^\pm$	4–13.8 GeV
1997	$e^+$	H	$\pi^\pm$	4–13.8 GeV
1998	$e^-$	D	$\pi^\pm, K^\pm$	2–15 GeV
1999	$e^+$	D	$\pi^\pm, K^\pm$	2–15 GeV
2000	$e^+$	D	$\pi^\pm, K^\pm$	2–15 GeV